

**A Precise Measurement of the Proton Elastic Form Factors  
for  $1.75 \leq Q^2 \leq 8.83 \text{ (GeV/c)}^2$**

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SLAC-Report-726

Prepared for the Department of Energy  
under contract number DE-AC03-76SF00515

Printed in the United States of America. Available from the National Technical Information Service, U.S. Department of Commerce, 5285 Port Royal Road, Springfield, VA 22161.

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\*Ph.D. thesis, The American University, Washington, DC 20016

**Order Number 9505489**

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**The American University, 1993**

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A PRECISE MEASUREMENT OF THE PROTON ELASTIC  
FORM FACTORS FOR  $1.75 \leq Q^2 \leq 8.83$  (GeV/c) $^2$

by

Lisa Clogher

submitted to the

Faculty of the College of Arts and Sciences

of The American University

in Partial Fulfillment of

the Requirements for the Degree

of

Doctor of Philosophy

in

Physics

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To my grandfather, Eaton James Clogher, who told me time and time again:  
"The important thing is to learn *how* to think, not *what* to think".

A PRECISE MEASUREMENT OF THE PROTON ELASTIC  
FORM FACTORS FOR  $1.75 \leq Q^2 \leq 8.83$  (GeV/c) $^2$ .

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ABSTRACT

The proton elastic electric and magnetic form factors,  $G_{Ep}(Q^2)$  and  $G_{Mp}(Q^2)$ , have been separated out to  $Q^2$  of 8.83 (GeV/c) $^2$ , more than doubling the  $Q^2$  range of previous data. The results for  $G_{Mp}(Q^2)/\mu_p G_D(Q^2)$  decrease smoothly from 1.05 to 0.92, while  $G_{Ep}(Q^2)/G_D(Q^2)$  is consistent with unity. Comparisons are made to QCD Sum Rule, diquark, constituent quark, and VMD models, none of which agree with all of the new data. The ratio  $Q^2 F_2/F_1$  approaches a constant value for  $Q^2 > 3$  (GeV/c) $^2$ .

## ACKNOWLEDGMENTS

Experiment NE11 was the collective effort of twenty-seven physicists from thirteen institutions. I wish to extend my appreciation for the hard work and commitment each member gave to the experiment, and for the spirit they brought with them to the group. Three members to whom particular thanks should be given for their untiring efforts and tremendous contributions during both the data-taking and analysis stages of the experiment are, Dr. Peter Bosted, spokesperson for the experiment, and then students, now doctors, Allison Lung and Linda Stuart.

In addition to the physicists, this experiment could not have gotten off the ground, much less been a success, without the skill and dedication of the many SLAC technicians and support staff. I would like to personally thank Gerry Davis, Bob Eisele, Carl Hudspeth, and Bill O'Hanlon for their efforts, and for the opportunity I had to work with them and dabble in the arts of their trades.

There are several people whose help and influence I have greatly benefitted from. To Ray Arnold, I owe a particular gratitude for first introducing me to the physics going on at SLAC, and then encouraging me to join the group and supporting me during my stay at SLAC. Frank Dietrich, with whom I can say it was a pleasure to work, deserves a standing ovation for his guidance and patience during the many, long months of the floating wire calibration and ensuing analysis. His tidbits of wisdom and his scientific dogma will remain with me for quite some time. Special thanks goes to Larry Whitlow who made my early years out at SLAC quite an

enlightening experience. I am grateful for his help and continual encouragement over the years. Lastly, I wish to thank Bruce Flanders for his help in the final stage of this thesis.

To those who traveled this path before me, and whose insightful conversations and friendship helped make my road less burdensome, I thank Marc Frodyma, Javier Gomez, Mina Katramatou and Makis Petratos. And yes, I do agree with Javier: A thesis is something one does only once.

And to those who have traveled this path with me, by virtue of their unfailing support, love and understanding, I thank Rosemari and Paul Clogher, my parents; Sue Williams and Paula Clogher, my sisters; Michael Clogher, my brother; and Dimitri Andivahis, my husband. In many respects this thesis is as much a product of their efforts as it is of mine.

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