On the Measurability of $\mathbf{B}^{0}_{s} \mathbf{B}$ -bar $^{0}_{s}$ Mixing

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ON THE MEASURABILITY OF $B^0_s \ \overline{B}^0_s$ MIXING

By

Terry W. Reeves

Dissertation

Submitted to the Faculty of the Graduate School of Vanderbilt University in partial fulfillment of the requirements for the degree of

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Millard Brewer Florine Brewer January 18, 1906 — August 24, 1983 March 7, 1907 — November 12, 1983

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