

## **Two Photon Exclusive Production of Charged Pion and Kaon Pairs<sup>\*</sup>**

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Two-Photon Exclusive Production of  
Charged Pion and Kaon Pairs

A dissertation submitted in partial satisfaction of the  
requirements for the degree Doctor of Philosophy  
in Physics

by

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1995

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# Curriculum Vita

## VITA

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## PUBLICATIONS

"Two-Photon Exclusive Production of  $\pi^+\pi^-$  and  $K^+K^-$ ," Gary S. Greenbaum, plenary talk on Exclusive  $\gamma\gamma$  Reactions, in *The Xth International Workshop on Photon-Photon Collisions*, Submitted for publication in Proceedings of the Workshop, Sheffield, UK, 1995.

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"Study of  $\chi_{c2}$  Production in Photon-Photon Collisions," D.A. Bauer, *et al.*, *Phys. Lett.* **B302**, 345 (1993).

## **ABSTRACT OF THE DISSERTATION**

**Two-Photon Exclusive Production of  
Charged Pion and Kaon Pairs**

by

**Gary S. Greenbaum**  
Doctor of Philosophy in Physics  
University of California, San Diego, 1995  
Professor Wayne Vernon, Chair

Two-photon exclusive hadron production at large momentum transfer probes the short distance physics of perturbative Quantum Chromodynamics and explores the long distance physics of bound-state quark dynamics. The differential cross section is measured for the exclusive reactions  $\gamma\gamma \rightarrow \pi^+\pi^-$  and  $\gamma\gamma \rightarrow K^+K^-$  in the two-photon invariant mass region  $1.4 \leq M_{\gamma\gamma} < 4.0$  GeV/c<sup>2</sup> and center-of-mass scattering angle  $|\cos \theta^*| < 0.8$ . The SU(3)-flavor symmetry breaking effects of the kaon wave function are examined. This analysis is performed using 139 pb<sup>-1</sup> of untagged data collected with the TPC/Two-Gamma detector.