RELATIVISTIC PARTICLE IDENTIFICATION BY dE/dx:

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THE FRUITS OF EXPERIENCE WITH ISIS

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Summary

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The experience of ten years of studying dE/dx is summarised. First, a helpful, if qualitative, picture of the electromagnetic field of a relativistic particle passing through a medium is discussed. Second, the salient steps in a rigorous calculation of dE/dx are outlined. Results of calculations for a variety of gases and configurations are given and the weakness of the calculation is pointed out. In the third section the practical experience gained from the ISIS project is discussed. The systematic effects that have been overcome are listed and the status and successes achieved with ISIS1 and ISIS2 to date are described.

A Qualitative Picture of the Field of a Particle in a Medium

A charged particle passing through a medium carries with it a pulse of electromagnetic field. To simplify the picture we may ignore the vector nature of the field and pretend that we are working in two dimensions only x in the direction of the particle velocity \underline{v} and y transverse. The pulse is made up of a full spectrum of frequency components. Let us consider the component of frequency ω and suppose that the phase velocity of e.m. waves of frequency ω in the dispersive medium is u (ω). This component will have a wave-vector <u>k</u> which must satisfy:

$$\frac{\omega}{|\underline{k}|} = u.$$

Furthermore, since the phase of the component is static as seen by an observer co-moving with the charged particle, the x-component of k must satisfy:

$$\frac{\omega}{k_x} = v. \qquad (or \ \omega = \underline{k}.\underline{v})$$

The transverse component of k is therefore given by

$$k_{y} = \frac{\omega}{v} \left(\frac{v^{2}}{u^{2}} - 1\right)^{\frac{1}{2}}$$

There are two cases of interest.

If v > u, k_y is real and the component of frequency ω represents a real travelling wave at an angle $\cos^{-1}(^u/v)$. This is the case of Cerenkov Radiation.

If v < u, k_y is purely imaginary and the component propagates as an evanescent wave in the transverse direction:

$$\exp i \frac{\omega}{v} (x - vt) \exp - \frac{y}{y_0}$$

where the range y_0 is given by

$$y_0 = \frac{v}{\omega \sqrt{1 - \frac{v^2}{u^2}}}$$

Re-expressed in terms of $\beta' = \frac{v}{u}$, $\gamma' = (1-\beta'^2)^{-\frac{1}{2}}$ and $\dot{\pi} = \frac{u}{\omega}$, the free wavelength over 2π , the range becomes

y_o = `β'γ'

The transverse range of the e.m. field expands with a factor $\beta'\gamma'$ as the Cerenkov threshold is approached. It is this expansion, normally referred to as the relativistic expansion but in reality only depending on the wave nature of the field, which is responsible for the 'relativistic rise' of the ionisation cross section for a particle moving in a medium.

Relativistic kinematics only enters through the limit v < c. There are then two cases of interest. First, below the principal absorption lines and in the optical region where the refractive index is greater than unity, u < c and the field expands as v is increased and the Cerenkov threshold may be reached. Second, in the u.v. and X-ray regions where the refractive index is less than unity, u > c and, although the field starts to expand as v is increased, the Cerenkov threshold is beyond the limit v = c. The expansion therefore saturates with a maximum range

$$y_0 = \frac{c}{u^2} (1 - \frac{c^2}{u^2})^{-\frac{1}{2}}$$

Expressed in terms of the refractive index $n = \frac{c}{u}$ and the familiar $\beta = \frac{v}{c}$ and $\gamma = (1 - \beta^2)^{-\frac{1}{2}}$

 $y_0 = \pi \beta [\frac{1}{\gamma^2} + (1-n^2)\beta^2]^{-\frac{1}{2}}$

which is effectively reached already when $\beta \simeq n$. This is the Fermi plateau region. The saturation is sometimes called the density effect because its onset depends on the density through n.

As an illustration, consider $\hbar\omega = 80 \text{ eV}$. At this u.v. energy, the refractive index of argon at normal pressure is about 0.99998 and the range of free photons is a few hundred microns. Fig. 1 shows the transverse range of the field as a function of the velocity of the charged particle. Fig. 2 shows the same on a vastly expanded non-linear velocity scale including the kinematic limit v = c.



Fig. 1 Transverse range of a field component as a function of velocity.

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Of course such a crude picture, though qualitatively correct, is no basis for calculation. For this we must turn to the Photo absorption Ionisation Model.¹

The Photoabsorption Ionisation Model for Calculation of dE/dx

This has been described in detail elsewhere.¹ Here we point out the five main steps involved.

Step 1

Step 1 is a student problem in Classical Electromagnetism. We solve Maxwell's Equations in a medium $(\underline{D} = \varepsilon \underline{E}, \mu = 1)$ due to a charge density $\rho = \varepsilon \delta^3 (\underline{r} - \underline{\beta} ct)$ and current density $\underline{j} = \underline{\beta} c\rho$, which together describe the charge moving with velocity $\underline{\beta} c$. In the Coulomb Gauge one obtains

$$\phi(\underline{k},\omega) = 2e \ \delta(\underline{\omega} - \underline{k},\underline{\beta}c)/k^2 \varepsilon$$

$$\underline{A}(\underline{k},\omega) = 2e \ \frac{(\underline{\omega}\underline{k}/k^2c - \underline{\beta})}{(-k^2 + \varepsilon\frac{\omega^2}{c-2})} \ \delta(\underline{\omega} - \underline{k},\underline{\beta}c)$$

and

$$E(\underline{\mathbf{r}},t) = \frac{1}{(2\pi)^2} \iint [i\frac{\omega}{c^{\mathbf{A}}}(\underline{\mathbf{k}},\omega) - i\underline{\mathbf{k}}\phi(\underline{\mathbf{k}},\omega)]$$

x exp $i(\underline{\mathbf{k}},\underline{\mathbf{r}}) - \omega t d^{3}kd\omega$

Step 2

The energy loss is due to this electric field doing work on the particle itself.

$$\langle \frac{dE}{dx} \rangle = \frac{eE(\beta ct, t).\beta}{\beta}$$

Step 3

Step 3 is to point out that this energy loss, which is expressed as an integral over Fourier components, is not a smooth rate of energy loss but needs to be reinterpreted, as in semiclassical radiation theory, as a probability of energy transfers $h\omega$. Thus

$$\frac{dE}{dx} = -\int_0^\infty \int_{\frac{\omega}{1+\omega}}^\infty NE \frac{d^2\sigma}{dEdp} \pi^2 d\omega dk$$

where N is the electron density, $E = \pi\omega$, $p = \pi k$ and $\frac{d^2\sigma}{dEdp}$ is the double differential cross section per electron. Doing the implied algebra we get

$$\frac{d^2\sigma}{dEdp} = \frac{2e^2}{N\beta^2\pi\hbar^2} \left[p\left(\beta^2 - \frac{E^2}{p^2c^2}\right) \mathscr{I}m\left(\frac{1}{\varepsilon E^2 - p^2c^2}\right) - \frac{1}{pc^2} \mathscr{I}m\left(\frac{1}{\varepsilon}\right) \right]$$

The only unknown in this expression is ε . All we need therefore is $\varepsilon(k,\omega)$, which is essentially the inelastic structure function of the medium. This involves a model¹ derived from:

- detailed photoabsorption spectra and their sum rules²
- Kramers Kronig relation for the real part of ε
- dipole approximation for the small k off-mass-shell region of $\boldsymbol{\varepsilon}$
- constituent (i.e. electron) scattering and sum rules for the large k off-mass-shell region of ε.

Step 5

Involves integrating the cross section over momentum transfer analytically and then folding the cross section numerically to derive the dE/dx spectrum in a finite thickness of gas.

A FORTRAN program is available to calculate spectra etc. for gas mixtures, pressures, sample thicknesses and velocities of interest.

Results of Calculations

We have calculated the 'relativistic' rise for a number of gases at atmospheric pressure together with the corresponding resolution. One must be specific about what is being calculated in considering these results. Table I shows data relevant to dE/dx spectra in 1.5 cm samples. Rises, defined as the ratio for electrons to protons at 4 GeV/c, are quoted for the peak, the half-height point on the low side and half-height point on the high side of the dE/dx spectrum. The resolution is the FWHM figure per $(metre)^{-\frac{1}{2}}$ derivable from a maximum likelihood fit (for protons at 4 GeV/c). The figures show that, whereas noble gases have the larger rises, they also have the poorer resolutions. In large measure these two effects offset one another. In the last six columns of Table I we show figures indicating the separation of masses divided by the FWHM resolution at 4 GeV/c and 20 GeV/c. The values are remarkably independent of the choice of gas. It is important to note however that for the noble gases with their larger rise and poorer resolution, systematic effects in practical devices will be less important than would be the case for molecular gases.

In Fig. 3 we show the effect of changing the density. The calculation is for pure argon. As the density increases, the rise decreases due to the 'density effect' but the resolution improves. However, the effective mass separation does not improve much beyond 2-3 bar. The choice of gas density depends to a certain extent on whether separation is required at higher momenta.

TABLE	T
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6	Deel	Rel.	Rise %	Resolution	Mass Separation (FWHM) units per metre ^{$\frac{1}{2}$})					
Gas	Peak	LO POINT	HI POINT	3 FWHM	At 4 GeV/C: e/m	π/Κ	K/ P	At 20 GeV/c: e/π	π/Κ	K/p
Не	58	86	45	15	1.5	.9	.3	.3	.9	.5
Ne	57	72	57	13	1.8	1.1	.4	.6	1.1	.6
Ar	57	66	49	12	1.6	1.1	.4	.6	.9	.6
Kr	63	65	61	11	2.2	1.3	.5	.9	1.1	.7
Xe	67	76	64	13	2.2	1.2	.4	1.0	1.0	.6
N ₂	56	59	48	11	1.8	1.3	.4	.7	1.0	.7
02	54	54	47	9	2.0	1.5	.5	.7	1.1	. 8
cō	55	56	48	11	2.0	1.3	.5	.7	1.1	.8
NO	54	56	47	10	2.0	1.5	.5	.7	1.1	.8
C02	48	52	41	8	2.0	1.6	.5	.6	1.1	.9
N20	48	52	41	8	2.0	1.6	.5	.7	1.1	.8
CH ₄	43	45	39	9	1.6	1.5	.5	.5	1.0	.8
C ₂ H ₄	42	46	38	8	1.7	1.5	.5	.6	1.0	.8
С2Н6	38	41	34	8	1.6	1.6	.5	-	-	-
C4H10	23	24	21	6	1.8	1.3	.3	.6	1.0	.8
Ar/20% CO ₂	55	62	48	12	1.9	1.2	.4	-	-	-









Fig. 4 shows the results of calculations on sample size. As the sample size is increased the relativistic rise decreases and the resolution per metre gets worse. Both effects tell us to sample as finely as possible. However, below 1 cm atm thickness in argon (or equivalent for other gases) the dE/dx distribution is no longer a smooth shape. It develops structures whose relative importance changes with velocity.³ Fitting these, to realise the ideal resolution may not be practicable. The effect of diffusion in generating cross talk between fine samples is equally important in limiting how finely one should measure dE/dx in practice.⁴ sity and the static dielectric constant (by adding

% Rise of peak

a)

Critical Discussion

There have been calculations of dE/dx before. All have been found wanting at some stage. The present PAI Model would appear to be at least as good as presently available data. Nevertheless we summarise here its weaker points.

First, the available photoabsorption speactra are not beyond criticism.² However, when they are massaged to satisfy the sum rules representing the electron den-



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oscillator strength near threshold) they cannot be too far wrong.

Second, the model for the $\varepsilon(k,\omega)$ is very crude. However, in very thin samples the important collisions are largely governed by the dipole approximation anyway. Results are therefore rather insensitive to the model.

Third, the assumed linear relation between energy deposited and number of ionisation electrons is physically implausible. The model assumes that the relation holds at least statistically with the same proportionality for every type of collision. Would the momentum of the secondary electron be a better guide to the probability of further ionisation? I believe that this weakness will give rise to discrepancies between theory and experiment sooner or later.

The Fruits of Experience with ISIS

The ISIS project for the Identification of Secondaries by Ionisation Sampling started ten years ago. Those most closely involved in it have been C.B. Brooks (project engineer), J.H. Cobb (pioneering graduate student) and P.D. Shield (electronics engineer). After the initial idea in April 1972^{5+6} we built a first lm drift prototype, ISISO. This was run in a test beam in November 1973 and showed clear evidence both for the space charge problem and the separation of pions and protons after an 85 cm drift.⁷ After further tests and proposals the 2m drift prototype, ISIS1, was constructed in 1978. Following successful operation in a test beam at NIMROD⁸ it was used in anger as part of the European Hybrid Spectrometer at CERN in 1980 for the NA16 small bubble chamber charm experiment.⁹ Since then it has been replaced by ISIS2 which ran in a preliminary experiment in July 1981 and is now running again in NA27, the second charm experiment (March 1982).

I will sketch the basic idea of ISIS first and then enumerate the principal problems, illustrating the points with data from our experience. Finally, I will show you where we have got to.



Fig. 5 Schematic diagram of ISIS.

The Idea

ISIS is a pictorial drift chamber similar to the more recent TPC but working at ambient pressure in a Cartesian geometry at a fixed target accelerator. Its prime role is particle identification; tracking is a free but impressive by-product. Fig. 5 shows a diagram of the chamber in the beam plane. Track signals are drifted to a single central wire plane perpendicular to the diagram. Multihit electronics can record between 30 and 50 hits per event on each wire. The electronics have been described elsewhere.¹⁰ They record the drift time and pulse height for each hit. The third coordinate is not measured and the up-down ambiguity is not resolved by the chamber alone. Table 2 gives the "vital" statistics of ISIS1 and ISIS2. The only important difference is the length, i.e. the number of samples per track.

	ISISI	ISIS2
Acceptance	$4 \times 2m^2$	$4 \times 2m^2$
Drift distance	2 x 2m	2 x 2m
Voltage (present≤120)	100-200KV	100-200KV
Samples	60-80	320
Volume	50m ³	120m ³
Ionisation resolution, FWHM	14%	7%

Table 2

Hazard 1 Base Line Restoration

Generally dE/dx pulse heights are measured from a.c. coupled signals. It follows that the mean signal is zero. In particular, if the signal occupancy is f% within one a.c. coupling time constant, the baseline will shift by f% of the pulse height. See Fig. 6. This is an unacceptably large effect in general. It cannot be computed from the amplitude of earlier pulses with good confidence in software because of the uncertainties surrounding the frequent saturating signals. The problem cannot be solved with linear filters. There are two solutions. Either you digitise the background level between pulses and correct in the software or you feedback the background signal level in the electronics itself. We have chosen the latter method.¹⁰ Once this problem is solved one can achieve excellent rejection of low frequency hum or at least its linear consequences.



Fig. 6 a.c. coupled signals

Hazard 2 Pulse Shape

The impulse response of the gas amplifier has a $1/t \ tail.^{11}$ Inverting this to provide optimal clipping without undershoot is a linear problem. In ISIS we do it with 3 passive filter time constants - 2 is probably enough.

Hazard 3 Shape-Independent Integration of Track Signals

Even after filtering, track signals are not sharp due to the combined effects of diffusion, track angle, drift path variation as well as the finite band-width of the electronics. Because these effects vary from track to track, to measure the signal charge it is necessary to do a proper gated integration. The track signal must be integrated from some time before the discriminator fired until 99% of the shaped pulse has arrived. This may be done in software if the whole signal has been digitised or in hardware with 'on' and 'off' thresholds. In ISIS we do the latter. The strict definition of complete integration (±1%) carries with it a conservative 2-track resolution. Fig. 7 shows the 2-track resolution in ISIS. The line superimposed on the histogram is the expectation of Poisson statistics. All track hits above 12 mms are resolved. The figures below each bin show the mean pulse height for the first and second hits of such pairs. We note that resolved hits above 12 mms are unaffected by the presence of the other at the level of 1-2%.

ISIS 1 1980



Fig. 7 Distribution showing loss of track hits at close separation.

Hazard 4 Bulk Space Charge

As a result of cosmics, background and earlier events the drift volume of a large device always contains positive ions released during the gas amplification process. It is usually possible to estimate roughly the space charge density knowing the gas amplification, the mean ionisation rate and the positive ion drift velocity (\lowleta cm/s/volt/cm). Bulk space charge will be a problem for both spatial and dE/dx distortion if

 $\frac{\int \rho(z) dz}{\int z} > f$

where the integral is the line integral of the space charge density through the drift volume and σ is the drift electrode charge density per unit area. f must be of order 10⁻³. We have seen spectacular effects from such space charge^{7,8}.

In ISIS we have cured it by gating the gas amplification off except during the bubble chamber sensitive time.⁸ We currently run in a beam of 3 x 10^4 s⁻¹, gas gain 10^4 , EHT 100 KV, 30 Hz x 2 ms sensitive time.



Fig. 8 Avalanche region for track at angle θ .

Hazard 5 Local Space Charge

Consider the track shown in Fig. 8 which crosses a number of anodes at an angle θ to the normal. The avalanche for this track (ignoring diffusion) takes place over a length of wire s θ . The size of the avalance is of order

G(gain) x P(bar) x 10(electrons/mm) x s(mm) x $1.6x10^{-19}$

giving a linear density

$$GP \theta^{-1} \times 1.6 \times 10^{-18}$$
 Coulombs/mm

If this charge density is significant compared with the charge density on the wire <u>causing</u> the avalanche, the gain will be non linear. The latter is typically 12 pC/mm for 25 μ m wire. To avoid this problem at the 1% level we need GP0⁻¹ < 2 x 10⁵. In ISIS we have GP = 10⁴ so that saturation effects should be confined to tracks at less than 50 mrad. This may be responsible for a 25% loss of measured pulse height in the beam region (θ =0) in ISIS1. Certainly this figure agrees within a factor 2 with the empirical bench test observations of local space charge by Frehse et al.¹² No such effect has been observed in ISIS2 where the chamber is rotated so that no track has an angle less than 50 mrad.

This problem is serious if GP must be kept high to get good charge division as in JADE and UA1. The problem in TPC should be no worse than in ISIS. In practice diffusion will help a bit. The problem may be compounded if the local rate is so high that a second track arrives before the positive ions from the earlier one have moved away.

Hazard 6 Calibration

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In every event in ISIS there is both an electronic track fed to all preamps and a false trigger track that samples 'zero pulse height' background. These are monitored carefully. All signals are corrected for gain and pedestal variations although the variation is now small enough that this is unnecessary.

Hazard 7 Cross Talk

Capacitative nearest neighbour cross talk is not serious, as shown by Monte Carlo simulation. Diffusion between neighbouring gas samples is potentially more serious. Because the dE/dx distribution is highly <u>skew</u>, cross talk can, not only change the shape of the spectrum but actually <u>shift</u> the peak. This has not been observed yet. It is a small effect.

Long range coupling between many channels whether capacitative in the chamber or a technical problem in the electronics can be disastrous for the resolution.¹³ Coherent pick up has the same effect.

Hazard 8 Gas Purity

For long drift paths and accurate pulse heights the gas must be pure. This requires leak tight systems, purification and instrumentation to measure the oxygen concentration. In our experience at purities of 1 part per million and less the latter causes the most trouble. In ISIS2 we are able to measure the attenuation directly by fitting the measured pulse heights on steep tracks. We assume that

$$\ln p_i = \ln \omega_i - \alpha t_i$$

where p_i is the measured signal, ω_i is a sample from a dE/dx distribution uncorrelated with t_i where t_i is the drift time. Moments accumulated for a track give a value of α . A thousand or so tracks give a distribution of attenuation factors α which enable the loss factor to be determined with an error of order 1%. Our best performance so far is about 14% loss on 2 metres. We expect a significant improvement on this soon.

Ionisation Fitting

As described elsewhere we employ a single parameter maximum likelihood fit.³ Fig. 9 shows how this works for a particular track. The histogram of pulse heights is fitted with a sliding scale parameter to a tabulated dE/dx function. In this case the track was known to be an electron from the spectrometer reconstruction where it associated with a γ conversion in the Bubble Chamber. Even with the modest statistics of ISISI the data clearly confirm the electron identification. Also shown in Fig. 9 are the data for an ISIS track which was associated to <u>two</u> tracks in the spectrometer. The likelihood fit correctly found the ISIS track to be 3 x minimum ionising although most of the pulse heights saturated the ADC. Such a case cannot be treated by a truncated mean method.

Fig. 10 shows new data from ISIS2 on the dE/dx distribution. The curve is the best calculation (without correction for cross talk) for the Argon/20% CO₂ mixture used. The data are actually fractionally sharper than the model. (The energy axis of the data has been scaled to give a best fit.)





Fig. 9 (a) Pulse height histrogram for a known electron with predictions for e, π, p.
(b) Histogram for a known double track with prediction.



Fig. 10 Experimental and theoretical dE/dx distributions.

Particle Identification with ISIS1 in the NA16 Experiment

Fig. 11 shows the layout of the European Hybrid Spectrometer at CERN with ISIS1 downstream of the LEBC bubble chamber as run in 1980.^{9,14} Fits of ISIS1 tracks to the spectrometer gave residuals of 4 mms and 5 mrad RMS. Samples of electrons from γ conversions in the bubble chamber and pions from K° decays in the bubble chamber were used to test the performance of ISIS. Fig. 12 shows the ratio of observed to expected ionisation for these tracks. The width of 18.6% FWHM is significantly worse than found previously⁸ and predicted (14%). The systematic discrepancy is due to various problems that have been cured in ISIS2 (see below). Nevertheless Fig. 13 shows clear separation of electrons and pions in the two cases.

Fig. 14 shows a real case of physics interest. The bubble chamber picture (reproduced here with some difficulty) contains a D°D° pair. The D° decays to $K^+\pi^+\pi^-\pi^-$.



Fig. 12 Resolution of ISIS1. Curve is 18.6% FWHM.



Fig. 14 A bubble chamber photograph from NA16 showing a D°D° event. The first decay is 4.2mm from the vertex.



Fig. 13 The chisquare for one degree of freedom for electron and pion mass assignments for tracks of known identity. The lines in the plots represent the two standard deviation limits.

The ionisation for the K⁺ track has a χ^2 of 10.1 (1d.f) when interpreted at π^+ . The proper time is 4.5×10^{-13} s. The D° decays as a 2 prong vee which does not point to production. The positive track has a momentum of 18 GeV/c and is associated with a shower of this energy in the EHS lead-glass γ -detector. For this track the ISIS ionisation χ^2 are 3.4 and 0.07 for the π^+ and e⁺ interpretation respectively. Although this analysis is preliminary, it is interesting as a first clear use of

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relativistic dE/dx for physics and as a clear case of the infrequent semileptonic decay of a $D^{\circ}.$

Particle Identification with ISIS2

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ISIS1 was built as a prototype. For full $e/\pi/K/p$ separation the extra resolution and better systematics of ISIS2 are needed. Fig. 15 shows views of the mammoth $100m^3$ device during construction. Fig. 16 shows the



Fig. 15a Construction of electronics in Oxford for ISIS2.



Fig. 15c Corner shield of ISIS2 to prevent breakdown

Fig. 15b View of ISIS2 during construction. The double wall of field-shaping tubes and the epoxy impregnated wooden frames can be seen.



Fig. 15d View of chamber complete except for the lower tubes. The wire plane at 2m is just above technician's head.

layout of EHS more or less in it s present form. In July 1981 a conventional diffraction experiment was run and ISIS2 used for the first time. Fig. 17 shows a fairly high multiplicity event in which many secondaries and decay products are seen passing through the chamber. The tracks have sagittae of 400 ± 1000 µm over their 5m length. Typically there are 250 good resolved spatial points per track with 230 good pulse heights. The pulse generator artificial track is seen at the top of the picture. Its mean pulse height has a variation 1.0% FWHM from event to event and a jitter after reconstruction of 1.2 mms and 0.2 mrad. It is reconstructed and





Fig. 18 The measured ionisation of beam tracks in ISIS2. The horizontal scale is chosen for convenience. The 'maverick' track is at 1.4. The 'overflow' is the only track not plotted.



Fig. 17 Spatial data for a single event in ISIS2. Each point is a track hit and is associated with a measured pulse height (not shown). The horizontal axis (512cm) is the wire number. The vertical axis (2x200cm) is the drift direction. Tracks, low energy electrons and noise hits may be seen. Track vectors reconstructed in ISIS space are superposed on the raw data.

recognised by the software in 99.85 (±15)% of events.

Fig. 18 shows the ionisation of out-of-time beam tracks found within these events. These show a resolution of 7.4% FWHM. There is no evidence of the significant gain variations found in the beam region in ISIS1. This is attributed to better control of space charge effects. We expect that this resolution will be confirmed for other tracks although this analysis is not yet complete.

Conclusion

In Fig. 19 we show contours of resolution as a function of device length and number of samples. The resolution values are theoretical and assume a full analysis by maximum likelihood ratio. These curves, which change a little with $\beta\gamma$, are in fair agreement with more empirical estimates for sample thickness greater than 1 cm atm. Below this the difference between the use of a truncated mean method and a likelihood ratio analysis is significant. For this reason other workers predict a worse resolution than shown here.¹⁵



Fig. 19 The ionisation resolution (%FWHM) of a multisampling detector filled with pure argon calculated with the PAI model for $\beta\gamma$ = 100. The dashed lines are loci of constant sample thickness.

The cross labelled 'ISIS2' shows the ideal resolution for a track with 320 points. With 230 points as realised in the analysis of ISIS2 data after excluding double track regions, bad channels and lost pulse heights, the theoretical resolution is 6.8%. (Walenta predicts 7% on 300 samples or 8% on 230).¹⁵ This is to be compared with our observed resolution of 7.4%.

We consider that these figures support the view that there is no real uncertainty about calculations of ionisation resolution or indeed the consequent mass resolution. The important questions concern systematics. In ISIS2 we believe we are close to realising the full potential of the dE/dx technique.

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