# COMPARISON OF CONDOR, FCI AND MAFIA CALCULATIONS FOR A 150MW S-BAND KLYSTRON WITH MEASUREMENTS

U.Becker, T.Weiland, TH-Darmstadt, Schlossgartenstr. 8, 64289 Darmstadt, Germany M.Dohlus, DESY, Notkestr. 85, 22603 Hamburg, Germany S.Lütgert, Philips, Stresemannallee 101, 22529 Hamburg, Germany

D.Sprehn, SLAC, Stanford, CA 94309, USA

### Abstract

To facilitate the design of high power klystrons an investigation into the reliability and accuracy of three modern particle-in-cell codes was performed. A 150MW S-band klystron for which measurements were available was used for this comparison. The field calculations of the particlein-cell codes are based on a finite difference time domain scheme, and use a port approximation to speed up the convergence to steady state. However they differ in many details (eg. calculation of  $\mathbf{E}$ ,  $\mathbf{B}$  or  $\mathbf{A}$ ,  $\phi$ ; space charge correction; 2D or 3D modelling of output cavity).

# I. INTRODUCTION

The developement of high power klystrons requires computer programs simulating the complex interaction of electrons with electromagnetic fields as realistic as possible. To analyse and verify the abilities of three modern codes (CONDOR, FCI and MAFIA) their calculations are compared with measurements at the 150-MW S-band klystron, which has been designed and built at SLAC [1] for the SBLC test facility at DESY. The design of the 7 cavity klystron is based on CONDOR calculations.

	design	operation
	values	values
Beam voltage	535 kV	527 kV
Beam current	700 A	680 A
RF Pulsewidth, rep rate	$3 \mu s, 60 Hz$	$3 \ \mu s, 60 \ Hz$
RF output power	150 MW	> 150 MW
Saturated gain	55 dB	54 dB
Efficiency	≥ 40 %	42 %
Center frequency	2998 MHz	3002 MHz
Solenoidal focusing field	0.21 T	0.18 T

# **II. COMPUTER CODES**

State of the art are two dimensional particle-in-cell (PIC) codes as CONDOR, FCI and MAFIA-TS2. These codes use the fact that with exception of input and output cavities most klystrons have a pure symmetry of revolution. In these codes the beam is simulated by macroscopic ring charges (macro particles) and their motion is integrated numerically (in 5D phase space). Therefore the electromagnetic fields or their potential representations are calculated in time-domain and take into account: electrostatic fields (eg. gun or dc beam), magnetostatic fields (eg. solenoid), resonant fields (cavities), transient processes and

self-consistent field particle interactions. Problems are: the long simulation time (many periods until steady state), the noise caused by macro particles (gain > 55 dB), unphysical properties of numerical field calculation and the space charge conservation. The first problem is solved by Yu's port approximation (PAp) [2]: only the beam pipe is simulated, the cavities are represented by their boundary fields, the fundamental mode of each cavity is simulated by an equivalent circuit while the higher modes are neglected. The amplitude of the circuit resonator is controled by a predictor corrector technique to reach steady state in few rf periods. The effect of noise rises with simulation time and is therefore reduced by the fast turning on process. A further reduction is obtained by spatial filtering of fields and current densities and a systematic (not randomized) particle injection. To fulfil the continuity either the mapping of the particle motions to grid currents and the filtering have to be charge conserving (FCI, MAFIA) or the space charge has to be corrected from time to time (CONDOR).

## A. CONDOR

The space charge correction in CONDOR is calculated as a correction potential. Poisson's equation for  $\operatorname{div} \vec{D} - \rho$ is solved and the correction is added every nth cycle where n is set by the user. In these calculations n was set between 1 and 3. The klystron is split into two segments (cavities 1 to 4 and 5,6,7). To transfer particles from one segment to the next, the particle data for the last rf periods are stored in a data dump and when the next segment is started the particles are reinjected periodically. To reduce the noise, the particle data were averaged over four periods. The fields are solved at the split-boundary using Neumann boundaries, no EM fields are dumped, and harmonics travelling in the drift tube are neglected. Therefore, it is best to devide the klystron at a point where the rf currents are relatively small. The output cavity is modelled directly in rz-coordinates (no PAp) whereby the dissipation of the output power is simulated by the  $r_{max}$ -boundary.

## B. FCI

For the calculation [3] of the time dependent EM-fields, the wave equation for the scalar and vector potentials  $\phi$ , **A** in the Lorentz gauge are employed rather than for fields **E**, **B**, because in the potential representation the Lorentz condition is consistent with the continuity equation for charge and current which is automatically satisfied in the simulation. The field distribution of the cavity modes in the drift tube is calculated by the FD method bu using a refined mesh in the cavity region of the drift tube. Particle noise is controlled by a sophisticated filtering algorithm as well as by introducing a small damping term into Maxwell's equations. PAp is used for all cavities. Because the output cavity is of a pill-box type, the field calculation for this cavity has a reduced accuracy.

### C. MAFIA

In the 2D simulations the steady state solution for all cavities is derived with the PAp. Therefore, for every dc voltage a special run is necessary to obtain the beamloading conductances of the cavity modes which are later needed to perform the iteration process of the PAp. Unsymmetric effects and the excitation of higher order modes in the output circuit due to the strong coupling to the external waveguides ( $Q_{ext} \approx 14$ ) are studied with a 3D PIC-simulation using MAFIA-TS3. The interface plane between the two and three dimensional simulation is located between cavity 6 and 7. There the periodic particle and electromagnetic field information is stored in the 2D run and reinitialized in the 3D run. The 3D simulation takes into account the cavity with all modes and the real broadband waveguides extracting the power. A detailed description of the interface and other characteristics of klystron simulation using MAFIA is given in [5].

# III. INPUT PARAMETERS OF KLYSTRON CALCULATIONS

To ensure that the klystron simulations are based on the same operating conditions and to avoid differences caused by pre-calc. the following parameters have been chosen:

a) Coil Settings: the solenoid field can be adjusted with four independent coils:

coil	current dens. A/inch <sup>2</sup>	z <sub>min</sub> ,z <sub>max</sub> inch	r <sub>min</sub> ,r <sub>max</sub> inch
bucking	-123.8	13.67, 17.00	7.97, 10.04
1	1656	21.0, 73.5	8.34, 9.34
2	1710	21.0, 73.5	9.84, 11.173
3	1224	59.55, 72.86	9.84, 11.173

In this z scale the cathod center is located at z=14.415 inch. (The field is plotted in [4] and [5].)

b) Beam Voltage and Current: the PIC-simulation starts right behind the gun region, where the DC-current is reinjected according to the particle properties calculated by the codes EGUN (for CONDOR and MAFIA) and Super-SAM (for FCI). The calculated perveances differ less than 2% from the measured values. For the simulations the current was scaled or extrapolated to the values printed in the  $P_{out}(P_{in})$ -diagrams.

c) Cold Cavity Parameters: the parameters for the input and output cavity are design values and have been measured. The parameters of the other cavities have been calculated in good agreement by SUPERFISH, SuperLANS and MAFIA-E. The PIC simulations are very sensitive to the cavity parameters especially of cavity 2 and 3. Therefore the PAp is applied with identical cold cavity parameters in all three PIC-codes. Only the output cavity is simulated directly by MAFIA3D and CONDOR. The frequency

and Q factor of the complete 3D discretization (including coupling slots and waveguides) have been verified in a separate 3D calculation.

cavity	frequency MHz	R/Q Ohm	Qı	Z <sub>center</sub> inch
1	3000	87	127	27.775
2	3009.3	89	8200	33.195
3	3029	91	8300	39.665
4	3176.8	107	8900	55.765
5	3447.8	98	8700	62.695
6	3384.8	127	9500	66.015
7	2998	117	14	70.015

d) Changes: due to a late change of the geometrical description, the FCI calculation are done for a slightly different setup. The geometry of the bucking coil is:  $z_{min}=13.3$  inch,  $z_{max}=16.63$  inch,  $r_{min}=7.9$  inch,  $r_{max}=9.975$  inch. The cathod center is located at 14 in, the center of the first cavity at 26 inch while the distance between all other cavities is unchanged.

# IV. MEASUREMENTS AND COMPARISON

# A. Measurements

Only external parameters like input-, reflected-, outputpower and the intercepted current could be measured directly. A parasitic oscillation ( $f \approx 8.5 \text{GHz}$ ) was observed [1] and could be avoided by adjusting the solenoid field (see values in coil settings table). This instability cannot be predicted or analysed by the monopole monomode PAp model.

#### B. Comparison

a) Reflected Input Power: essentially the input power is either transfered to the beam or reflected. Neglecting wall losses, one can relate the cavity 1 voltage to the input power, reflection and cold cavity parameters:

$$V_1^2/P_{in} = 2(1+r)^2 Q_1 R/Q$$
,

which can be solved for r and compared:

$I_b/A$	480	495	511	523	527
measur.		0.179	0.190	0.187	0.183
CONDOR	0.169	0.216	0.179		0.219
FCI	0.046	0.046	0.058		0.059
MAFIA	0.176	0.184	0.193		0.206

The small reflection of the FCI calculation indicates an inaccurate simulation of the input cavity. The effect of this error is a reduced cavity 1 voltage and therefore a reduced gain ( $\approx$  -1dB).

b) Linear Gain: the gains calculated by all programs are too high: CONDOR +7.6dB, FCI +4.8dB, MAFIA2D +2.1dB MAFIA3D +1.8dB at operation frequency. In the MAFIA calculation the maximum of the frequency response is shifted by at least 8MHz to the measurement.

c) Fourier Coefficients of Beam Current: for  $U_b=511kV$  and identical cavity 1 voltage (3kV) the fourier components of the beam current and the cavity voltages are documented. In the range of the first three cavities the amplification of

the cavity voltages and the 1st harmonic of the current are highest in CONDOR and lowest in MAFIA. The difference between CONDOR and FCI at the beginning is completly compensated to the end of the tube. The amplification along the last drift space is significantly higher in MAFIA so that the cavity 7 voltage is only 2.5% lower than by the other codes.

d) Output Cavity  $(U_b=511kV, U_1=3kV)$ : even with very similar bunching and cavity 7 voltage the output power of CONDOR (155.1MW) and FCI (166.1MW) show a big difference. For these parameters MAF1A2D is in excellent agreement with CONDOR and MAF1A3D is further 10MW lower. The CONDOR/FCI differences and the MAFIA3D/2D differences of 10MW can only be explained by errors of the PAp. CONDOR (without PAp) and MAF1A2D (with PAp) give similar results because the cav. 7 voltage differs.

e) Numerical Effort:

[	CONDOR	FCI	MAFIA	MAFIA
			2D	3D <sup>(1)</sup>
δr/mm	0.880.87	1	1.5	
$\delta x/mm$				1.62
$\delta y/mm$				1.62.5
$\delta z/mm$	0.880.91	$2.5^{(2)}$	1.5	1.62
δt/ps	1.85	1.6 4.8 <sup>(3)</sup>	1.57	1.57
rf-periods	60	45	42	15
particles/ rf-period	1240	556	1065	8520

<sup>(1)</sup> output cavity, <sup>(2)</sup> increased resolution in the cavity regions, <sup>(3)</sup> integration of motion

## V. SUMMARY

The measured input reflection coefficient indicates that the beam loading of the input cavity is not simulated precisely by FCI. All codes calculate overly high gains (especially CONDOR) and saturated output powers (especially FCI). The linear frequency characteristicas are shifted upwards (especially by MAFIA). The port approximation causes significant errors in the output cavity.

### References

- D. Sprehn, R.M. Phillips, G. Caryotakis: "The Design and Performance of 150-MW S-Band Klystrons", SLAC-PUB-6677, Stanford Linear Accelerator Center, September 1994.
- [2] Simon Yu: "Particle-In-Cell Simulation of High Power Klystrons", SLAC-AP-34, September 1984.
- [3] T. Shintake: "High Power Klystron Simulations using FCI-Field Charge Interaction Code" KEK 90-3 A/D, May 1990.
- [4] S. Lütgert: "FCI Parameter Study for the 150 MW DESY Klystron", SBLC meeting at DESY, Hamburg, February 1995.
- [5] U. Becker, M. Dohlus, T. Weiland: "Three Dimensional Klystron Simulation", to be published in Particle Accelerators.

