# BABAR explores CP violation 

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The most recent results obtained by the BABAR experiment at the PEP-II asymmetric-energy $B$ Factory at SLAC on CP-violating asymmetries and branching fractions for neutral and charged B decays are presented here. The analysis was performed on a data sample of $\sim 88$ million $\Upsilon(4 S) \rightarrow B \bar{B}$ decays collected between 1999 and 2002. Using $b \rightarrow c \bar{c} s$ decays, we measure $\sin 2 \beta=0.741 \pm 0.067$ (stat) $\pm 0.034$ (syst). We also present $\sin 2 \beta$ measurements from, $b \rightarrow s \bar{s} s$ and $b \rightarrow c \bar{c} d$ processes. From neutral $B$ meson decays to two-body final states of charged pions and kaons, we derive for the CP violating parameters, $S_{\pi \pi}=0.02 \pm 0.34 \pm 0.05[-0.54,+0.58]$ and $C_{\pi \pi}=-0.30 \pm 0.25 \pm 0.04[-0.72,+0.12]$. First results for $B \rightarrow \pi^{+} \pi^{-} \pi^{0}$ and $K^{ \pm} \pi^{\mp} \pi^{0}$ final states dominated by the $\rho^{ \pm}$resonance, are also presented.

## 1. Introduction

The Standard Model of electroweak interactions describes $C P$ violation in weak interactions as a consequence of a complex phase in the threegeneration Cabibbo-Kobayashi-Maskawa (CKM) quark-mixing matrix[1]. From the CKM unitarity we derive six relationships between its elements, $V_{i j}$, forming triangles in the complex plane. In this framework, measurements of $C P$ asymmetries in the proper-time distribution of neutral $B$ decays to $C P$ eigenstates, provide a direct measurement for the angles of the unitarity triangle, $V_{u d} V_{u b}^{*}+V_{c d} V_{c b}^{*}+V_{t d} V_{t b}^{*}=0$. In the most general case the decay rate asymmetry as a function of time, $A_{C P}(\Delta t)$ between a $B^{0}$ and a $\bar{B}^{0}$ can be written as a function of two coefficients $S_{f}$ and $C_{f}$, depending on the final state, f .
$A_{C P}(\Delta t)=S_{f} \sin \left(\Delta m_{d} \Delta t\right)-C_{f} \cos \left(\Delta m_{d} \Delta t\right)$,
where $\Delta t=t_{\mathrm{rec}}-t_{\mathrm{tag}}$ is the difference between the proper decay times of the reconstructed $B$ meson ( $B_{\text {rec }}$ ) and the tagging $B$ meson $\left(B_{\text {tag }}\right)$, $\Delta m_{d}$ is the mixing frequency due to the eigenstate mass difference and the parameters $S_{f}$ and $C_{f}$ are defined as

$$
\begin{equation*}
S_{f} \equiv \frac{2 \mathcal{I} m \lambda_{f}}{1+\left|\lambda_{f}\right|^{2}} \quad \text { and } \quad C_{f} \equiv \frac{1-\left|\lambda_{f}\right|^{2}}{1+\left|\lambda_{f}\right|^{2}} \tag{2}
\end{equation*}
$$

where $\lambda_{f}=\frac{q}{p} \frac{\bar{A}(f)}{A(f)}$, with $A(f)$ and $\bar{A}(f)$ being the decay amplitudes leading to the final state f .

The sine term in equation 1 is due to the interference between direct decay and decay after flavour change, and when only one amplitude is contributing to the final state, it measures the sine of one of the unitarity triangle angles, $\alpha, \beta$ or $\gamma$. The cosine term is due to the interference between two or more decay amplitudes, a tree and a penguin for example, with different weak and strong phases. In this case the angle involved in the sine term, is modified by a strong phase and doesn't measure directly, $\alpha, \beta$ or $\gamma$. Notice, a cosine term different from zero, is a proof of direct $C P$ violation.

New physics, for example a coupling between super-symmetric and Standard Model fields, introduces new phases which may reshape the unitarity triangle. It is therefore very important to check the triangle consistency as precisely as possible, measuring the sides and the angles.

Both BABAR [2] and Belle [3] collaborations have established $C P$ violation in neutral $B$ decays. These results are consistent with the Standard Model expectations based on measurements and theoretical estimates of the magnitudes of the elements of the Cabibbo-Kobayashi-Maskawa quark-mixing matrix.

## 2. The BABAR experiment

The $B A B A R$ detector is located at the unique interaction region IR6, of the PEP-II rings at SLAC, running at a center of mass energy almost equal to the $\Upsilon(4 S)$ mass. The best peak luminosity achieved by the accelerator is $4.6 \times 10^{33} \mathrm{~cm}^{-2} \mathrm{~s}^{-1}$ for a designed value of $3.0 \times$ $10^{33} \mathrm{~cm}^{-2} \mathrm{~s}^{-1}$. PEP-II has delivered since October 1999, $99 \mathrm{fb}^{-1}$. BABAR has accumulated $81.2 \mathrm{fb}^{-1}$ on the $\Upsilon(4 S)$ peak and $9.6 \mathrm{fb}^{-1} 40 \mathrm{MeV}$ below, for background subtraction. The overall experiment's efficiency is $\sim 96 \%$.

The $\Upsilon(4 S)$ resonance decays, with $50 \%$ branching fraction to a coherent pair of a $B^{0}$ and $\bar{B}^{0}$ oscillating with exactly the opposite flavor, until one of the B decays. A time dependent asymmetry measurement implies, to fully reconstruct the final state of one $\mathrm{B}\left(B_{\mathrm{rec}}\right)$, the flavor tagging of the remaining $B$ meson ( $B_{\mathrm{tag}}$ ), and the measurement of the time difference $\Delta t$ between the two Bs.

A detailed description of the BABAR detector is presented in Ref.[4]. Charged particle (track) momenta are measured in a tracking system consisting of a 5-layer double-sided silicon vertex tracker (SVT) and a 40-layer drift chamber (DCH) filled with a gas mixture of helium and isobutane. The SVT and DCH operate within a 1.5 T superconducting solenoidal magnet. The typical decay vertex resolution for reconstructed $B$ decays is approximately $65 \mu \mathrm{~m}$ along the center-of-mass (CM) boost direction. Photons are detected in an electromagnetic calorimeter (EMC) consisting of $6580 \mathrm{CsI}(\mathrm{Tl})$ crystals arranged in barrel and forward endcap subdetectors. The flux return for the solenoid is composed of multiple layers of iron and resistive plate chambers for the identification of muons and long-lived neutral hadrons.

Particle identification is the key issue for many important analysis, like $B^{0} \rightarrow$ $\pi^{+} \pi^{-}, K^{+} \pi^{-}, K^{+} K^{-}$decays. Tracks are identified as pions or kaons by the Cherenkov angle $\theta_{c}$ measured with a detector of internally reflected Cherenkov light (DIRC). The typical separation between pions and kaons varies from $8 \sigma$ at $2 \mathrm{GeV} / c$ to $2.5 \sigma$ at $4 \mathrm{GeV} / c$, where $\sigma$ is the average resolution on $\theta_{c}$. Lower momentum kaons used
in $B$ flavor tagging are identified with a selection algorithm that combines $\theta_{c}$ (for momenta down to $0.6 \mathrm{GeV} / c$ ) with measurements of ionization energy loss $d E / d x$ in the DCH and SVT. The selection efficiency is approximately $85 \%$ for a pion misidentification probability of $2.5 \%$.

We use a multivariate technique [2] to determine the flavor of the $B_{\text {tag }}$ meson. Separate neural networks are trained to identify primary leptons, kaons, soft pions from $D^{*}$ decays, and high-momentum charged particles from $B$ decays. Events are assigned to one of five mutually exclusive tagging categories based on the estimated mistag probability and the source of the tagging information. The quality of tagging is expressed in terms of the effective efficiency $Q=\sum_{k} \epsilon_{k}\left(1-2 w_{k}\right)^{2}$, where $\epsilon_{k}$ and $w_{k}$ are the efficiencies and mistag probabilities, respectively, for events tagged in category $k$. The overall tagging efficiency measured in a data sample $B_{\text {flav }}$ of fully reconstructed neutral $B$ decays to $D^{(*)-}\left(\pi^{+}, \rho^{+}, a_{1}^{+}\right)$, is $(28.4 \pm 0.7) \%$.

The time interval $\Delta t$ between the two $B$ decays is calculated from the measured separation $\Delta z$ between the decay vertices of $B_{\text {rec }}$ and $B_{\text {tag }}$ along the collision $(z)$ axis [5]. The r.m.s. $\Delta t$ resolution is 1.1 ps .

## 3. $\sin 2 \beta$ measurement

A precise measurement of $\sin 2 \beta$ can be obtained using the golden decays, $b \rightarrow c \bar{c} s$, containing a charmonium meson in the final state. In addition other decays, $b \rightarrow d \bar{d} s$ or $b \rightarrow s \bar{s} s$, under some conditions also measure $\sin 2 \beta$. Looking for differences between all the measured values, may lead to new physics.

## 3.1. $b \rightarrow c \bar{c} s$

This mode is the cleanest, both from the theoretical and experimental point of view. Penguin contributions are suppressed by $\lambda_{\text {Cabibbo }}^{2}$, or have the same weak phase. No direct $C P$ violation is expected in the Standard Model, and the asymmetry can be simply written as:
$A_{C P}(\Delta t) \equiv-\eta_{f} \sin 2 \beta \sin \left(\Delta m_{d} \Delta t\right)$
with $\eta_{f}=-1$ for $J / \psi K_{S}^{0}, \psi(2 S) K_{S}^{0}, \chi_{c 1} K_{S}^{0}$, and $\eta_{c} K_{S}^{0}$, and +1 for $J / \psi K_{L}^{0}$. Due to the presence
of even $(L=0,2)$ and odd $(L=1)$ orbital angular momenta in the $B \rightarrow J / \psi K^{* 0}$ final state, there can be $C P$-even and $C P$-odd contributions to the decay rate. When the angular information in the decay is ignored, the measured $C P$ asymmetry in $J / \psi K^{* 0}$ is reduced by a factor $1-2 R_{\perp}$, where $R_{\perp}$ is the fraction of the $L=1$ component. We have measured $R_{\perp}=(16.0 \pm 3.5) \%$ [7], which gives $\eta_{f}=0.65 \pm 0.07$ after acceptance corrections in the $J / \psi K^{* 0}$ mode.

Experimentally the involved branching fractions are rather high, and the final state reconstruction, with a $K_{S}^{0}$ benefits from little background, as shown in figure 1.


Figure 1. Distributions for $B_{C P}$ candidates satisfying the tagging and vertexing requirements: a) $m_{\mathrm{ES}}$ for the final states $J / \psi K_{S}^{0}, \psi(2 S) K_{S}^{0}, \chi_{c 1} K_{S}^{0}$, $\eta_{c} K_{S}^{0}$, and $J / \psi K^{* 0}\left(K^{* 0} \rightarrow K_{S}^{0} \pi^{0}\right)$, b) $\Delta E$ for the final state $J / \psi K_{L}^{0}$.

We observe 2641 events after tagging and vertexing. Table 1 summarizes the number of events per channel, the signal purity, and the fitted $\sin 2 \beta$ value. Figure 2 shows the $\Delta t$ distributions and asymmetries in yields between $B^{0}$ tags and $\bar{B}^{0}$
tags for the $\eta_{f}=-1$ sample as a function of $\Delta t$, overlaid with the projection of the likelihood fit result.


Figure 2. Top) Number of $\eta_{f}=-1$ candidates $\left(J / \psi K_{S}^{0}, \psi(2 S) K_{S}^{0}, \chi_{c 1} K_{S}^{0}\right.$, and $\left.\eta_{c} K_{S}^{0}\right)$ in the signal region with a $B^{0}$ tag and with a $\bar{B}^{0}$ tag and bottom) the raw asymmetry $\left(N_{B^{0}}-N_{\bar{B}^{0}}\right) /\left(N_{B^{0}}+\right.$ $N_{\bar{B}^{0}}$ ) as functions of $\Delta t$. The red (blue) curves represent the fit projection in $\Delta t$ for $B^{0}\left(\bar{B}^{0}\right)$ tags. The shaded regions represent the background contributions.

From a simultaneous unbinned maximum likelihood fit to the $\Delta t$ distributions of the tagged $B_{C P}$ and $B_{\text {flav }}$ samples, taking into account the $\Delta t$ resolution, the tagging efficiency and the mistag rate, we measure [6] :
$\sin 2 \beta=0.741 \pm 0.067$ (stat) $\pm 0.034$ (syst)

This new value, improves both the statistical and systematic error, and it is consistent with our previous published results [2]. It is also consistent with the range implied by indirect measurements and theoretical estimates, as shown in figure 3.

From a fit only to the $\eta_{f}=-1$ sample, allowing for a non zero coefficient $C_{f}$ of equation 1, we measure $\left|\lambda_{c \bar{c} s}\right|=0.948 \pm 0.051$ (stat) $\pm$ 0.030 (syst), consistent with one, as expected from the Standard Model. In this case the coefficient of the $\sin \left(\Delta m_{d} \Delta t\right)$ term in Eq. 1 is measured to be $0.759 \pm 0.074$ (stat).


Figure 3. The red contour shows the allowed region for the unitarity triangle apex, as obtained from indirect measurements and theoretical calculations. In blue, the one and two sigma contours from the $\sin 2 \beta$ measurement [8].
3.2. CP asymmetries in the decay $B^{0} \rightarrow$ $D^{*+} D^{*-}$
The $B^{0} \rightarrow D^{*+} D^{*-}$ decay is a Cabibbo suppressed transition, $b \rightarrow c \bar{c} d$, dominated by the tree diagram. The CP asymmetry measures $\sin 2 \beta$
$\left(\beta \equiv \arg \left[-V_{\mathrm{cd}} V_{\mathrm{cb}}^{*} / V_{\mathrm{td}} V_{\mathrm{tb}}^{*}\right]\right)$ to be compared with $-\sin 2 \beta$ from $b \rightarrow c \bar{c} s$. However a small penguin contribution is also expected [9]. In addition $B^{0} \rightarrow D^{*+} D^{*-}$ is a pseudoscalar decay to a vector-vector final state, which requires the measurement of the $C P$-odd fraction, $R_{\perp}$.

$$
\begin{equation*}
R_{\perp}=\frac{M_{\perp}^{2}}{M_{0}^{2}+M_{\|}^{2}+M_{\perp}^{2}} \tag{4}
\end{equation*}
$$

where $M_{i}$ are the decay amplitudes for the three partial waves, $\mathrm{L}=0,1,2$. The angular distribution of the decay products expressed as a function of the transversity angle $\theta_{t r}$, is given by:
$\frac{1}{\Gamma} \frac{\mathrm{~d} \Gamma}{\mathrm{~d} \cos \theta_{\mathrm{tr}}}=\frac{3}{4}\left(1-R_{\perp}\right) \sin ^{2} \theta_{\mathrm{tr}}+\frac{3}{2} R_{\perp} \cos ^{2} \theta_{\mathrm{tr}}$
From un unbinned maximum likelihood fit of $\cos \theta_{\text {tr }}$ to our data, we measure [10] :
$R_{\perp}=0.07 \pm 0.06($ stat $) \pm 0.03($ syst $)$.
A priori sizeable penguin contribution can not be excluded, and therefore the weak phase difference $\operatorname{Im}\left(\lambda_{D^{*+} D^{*-}}\right)=-\sin 2 \beta$ can be affected. The value of $\lambda^{\cdot} D^{*+} D^{*-}$ can be different for the three transversity amplitudes because of possible different penguin-to-tree ratios. We include all these contributions in the parametrization of the decay rates which are now given by:

$$
\begin{align*}
& f_{ \pm}(\Delta t)=\frac{\mathrm{e}^{-|\Delta t| / \tau_{B^{0}}}}{4 \tau_{B^{0}}}\left\{O\left(1-\frac{1}{2} \Delta \mathcal{D}\right) \mp\right. \\
& \left.\mathcal{D}\left[S \sin \left(\Delta m_{d} \Delta t\right)+C \cos \left(\Delta m_{d} \Delta t\right)\right]\right\} \tag{6}
\end{align*}
$$

where $\mathcal{D}$, is the dilution factor due to the mistags and the coefficients $\mathrm{O}, \mathrm{C}$ and S depend on $\lambda_{+}$ and $\lambda_{\perp}$ parameters related to the $C P$-odd and $C P$-even states.
This analysis benefits from our high efficiency on low momentum track reconstruction. From $126 \pm 13 D^{*+} D^{*-}$ that we observe, we fit $\left|\lambda_{+}\right|$ and $\operatorname{Im}\left(\lambda_{+}\right)$. As the $C P$-odd fraction is small we fix $\left|\lambda_{\perp}\right|=1$ and $\operatorname{Im}\left(\lambda_{\perp}\right)=-0.741$. The results [10] obtained from the fit (Fig. 4) are as follows:

$$
\begin{aligned}
\operatorname{Im}\left(\lambda_{+}\right) & =0.31 \pm 0.43(\text { stat }) \pm 0.13(\text { syst }) \\
\left|\lambda_{+}\right| & =0.98 \pm 0.25(\text { stat }) \pm 0.09(\text { syst })
\end{aligned}
$$

| Sample | $N_{\text {tag }}$ | $P(\%)$ | $\sin 2 \beta$ |
| :--- | :---: | :---: | :---: |
| $J / \psi K_{S}^{0}, \psi(2 S) K_{S}^{0}, \chi_{c 1} K_{S}^{0}, \eta_{c} K_{S}^{0}$ | 1506 | 94 | $0.76 \pm 0.07$ |
| $J / \psi K_{L}^{0}\left(\eta_{f}=+1\right)$ | 988 | 55 | $0.72 \pm 0.16$ |
| $J / \psi K^{* 0}\left(K^{* 0} \rightarrow K_{S}^{0} \pi^{0}\right)$ | 147 | 81 | $0.22 \pm 0.52$ |
| Full $C P$ sample | 2641 | 78 | $0.74 \pm 0.07$ |
| $J / \psi K_{S}^{0}, \psi(2 S) K_{S}^{0}, \chi_{c 1} K_{S}^{0}, \eta_{c} K_{S}^{0}$ only $\left(\eta_{f}=-1\right)$ |  |  |  |
| $J / \psi K_{S}^{0}\left(K_{S}^{0} \rightarrow \pi^{+} \pi^{-}\right)$ | 974 | 97 | $0.82 \pm 0.08$ |
| $J / \psi K_{S}^{0}\left(K_{S}^{0} \rightarrow \pi^{0} \pi^{0}\right)$ | 170 | 89 | $0.39 \pm 0.24$ |
| $\psi(2 S) K_{S}^{0}\left(K_{S}^{0} \rightarrow \pi^{+} \pi^{-}\right)$ | 150 | 97 | $0.69 \pm 0.24$ |
| $\chi_{c 1} K_{S}^{0}$ | 80 | 95 | $1.01 \pm 0.40$ |
| $\eta_{c} K_{S}^{0}$ | 132 | 73 | $0.59 \pm 0.32$ |
| $B^{0}$ tags | 740 | 94 | $0.76 \pm 0.10$ |
| $\bar{B}^{0}$ tags | 766 | 93 | $0.75 \pm 0.10$ |
| $B_{\text {flav }}$ sample | 25375 | 85 | $0.02 \pm 0.02$ |
| $B^{+}$sample | 22160 | 89 | $0.02 \pm 0.02$ |

Table 1
Number of events $N_{\text {tag }}$ in the signal region after tagging and vertexing requirements, signal purity $P$, and results of fitting for $C P$ asymmetries in the $B_{C P}$ sample and in various subsamples, as well as in the $B_{\text {flav }}$ and charged $B$ control samples. Errors are statistical only.
$\operatorname{Im}\left(\lambda_{+}\right)$has to be compared with $-\sin 2 \beta=$ $-0.741 \pm 0.067$ from the golden modes. More data are needed to establish contributions from penguin diagrams or a difference with the $b \rightarrow c \bar{c} s$ process.

### 3.3. CP asymmetries in the decay $B^{0} \rightarrow$

 $J / \psi \pi^{0}$$B^{0} \rightarrow J / \psi \pi^{0}$ is an other Cabibbo suppressed, $b \rightarrow c \bar{c} d$ decay. The tree contribution has the same weak phase as the $b \rightarrow c \bar{c} s$ and measures $-\sin 2 \beta$. However in this case large penguin contributions are expected. Both tree and penguin diagrams contribute proportional to $\lambda_{\text {Cabibbo }}^{3}$. The weak phase of a portion of the penguin is different from the tree and both $S_{J / \psi \pi^{0}}$ and $C_{J / \psi \pi^{0}}$ should be non zero.

We measure [11] $S_{J / \psi \pi^{0}}$ and $C_{J / \psi \pi^{0}}$ by an unbinned maximum likelihood fit to 438 events consisting of signal events, $B^{0} \rightarrow J / \psi K_{S}^{0}\left(\pi^{0} \pi^{0}\right)$, inclusive $J / \psi, B \bar{B}$, and continuum background. Figure 5 shows the beam constrained mass, $m_{\mathrm{ES}}$, distribution for the signal and all four backgrounds. $40 \pm 7$ signal events are observed. The coefficients of the sinus and cosinus terms of the
time dependent asymmetry in equation 1, are then measured as:
$S_{J / \psi \pi^{0}}=0.05 \pm 0.49($ stat $) \pm 0.16$ (syst)
$C_{J / \psi \pi^{0}}=0.38 \pm 0.41($ stat $) \pm 0.09$ (syst)
Given the large statistical errors, there is no evidence for direct $C P$ violation, and the comparison of $S_{J / \psi \pi^{0}}$ with the golden channels doesn't bring new information. With increasing statistics in the future this channel will become quiet interesting as it also probes penguin contributions usually neglected in the golden modes.
3.4. $\sin 2 \beta$ from $B^{0} \rightarrow \phi K_{S}^{0}$

The charmless hadronic decay, $B^{0} \rightarrow \phi K_{S}^{0}$, is dominated by the $b \rightarrow s \bar{s} s$ gluonic penguins, figure 6. All other Standard model contributions are highly suppressed. The $C P$ asymmetry measures $\sin 2 \beta$, and only a $4 \%$ deviation is expected from the golden modes. The presence of the penguin loops, and the possibility to reveal new physics, make this channel very interesting. BABAR has measured with $45 \mathrm{M} B \bar{B}$ pairs a branching ratio of $B F\left(B^{0} \rightarrow \phi K^{0}\right)=\left(8.1_{-2.5}^{+3.1} \pm 0.8\right) \times 10^{-6}[12]$.


Figure 4. From top to bottom: number $N_{B^{0}}$ of candidate events in the signal region $\left(B^{0} \rightarrow\right.$ $D^{*+} D^{*-}$ ) with a $B^{0}$ tag, number $N_{\bar{B}^{0}}$ of candidates with a $\bar{B}^{0}$ tag, and the raw asymmetry $\left(N_{B^{0}}-N_{\bar{B}^{0}}\right) /\left(N_{B^{0}}+N_{\bar{B}^{0}}\right)$, as functions of $\Delta t$. The solid curves represent the result of the combined fit to the full sample. The shaded regions represent the background contributions.
$B$ mesons candidates are reconstructed in the decay mode $B^{0} \rightarrow \phi K_{S}^{0}$ with $K_{S}^{0} \rightarrow \pi^{+} \pi^{-}$and $\phi \rightarrow K^{+} K^{-}$. Figure 7 shows the $m_{\mathrm{ES}}$ distribution after tight cuts to reject a large background fraction. From a simultaneous unbinned maxi-


Figure 5. $m_{\mathrm{ES}}$, distribution for the signal $B^{0} \rightarrow$ $J / \psi \pi^{0}$ and all backgrounds
mum likelihood fit we find 51 signal, and 1301 background events. From the $\Delta t$ distribution for $B^{0}$ and $\bar{B}^{0}$ events, fixing $\left|\lambda_{\phi K_{S}^{0}}\right|=1$, we extract $\sin 2 \beta$ [13]:

$$
\sin 2 \beta=-0.19_{-0.50}^{+0.52}(\text { stat }) \pm 0.09(\text { syst })
$$

This result, dominated by the statistical error, differs of about two standard deviations from $\sin 2 \beta$ from the golden modes. However also in this case much more luminosity is needed before draw any conclusions.

## 4. $\sin 2 \alpha$ measurement

Measuring $\sin 2 \alpha$ is considerably more difficult than $\sin 2 \beta$ from the golden modes. There is no a single decay channel where only a tree diagramme contributes. On the contrary, in all the cases, important penguin contributions, pollute the weak phase difference $2 \alpha$ by an extra contribution, $\kappa$. Experimentalists do not measure $\alpha$ but $\alpha$ effective, $\alpha_{e f f}$, with $2 \alpha_{e f f}=2 \alpha+\kappa$. Depending on the decay channel and using other measurements or theoretical predictions, one could in principle,


Figure 6. Quark-level diagrams describing the decays $B \rightarrow \phi K$ : (a) internal penguin, (b) flavorsinglet penguin.


Figure 7. $m_{\mathrm{ES}}$ distribution for $B^{0} \rightarrow \phi K_{S}^{0}$ after tight signal selection criteria.
extract $\alpha$. On the experimental side, the situation is also difficult. The involved branching ratios are small, $\sim 10^{-6}$, and the background quite high. Measuring even $\alpha_{e f f}$ is quite challenging.

## 4.1. $C P$ asymmetries in the decay $B^{0} \rightarrow$ $\pi^{+} \pi^{-}$

For this decay mode the tree's diagramme weak phase is $\beta+\gamma$, while the penguin diagramme contributes with both a weak phase $-\beta$ and a strong phase $\delta$. In this case $S_{\pi \pi}=\sqrt{1-C_{\pi \pi}} \sin \alpha_{e f f}$ with $C_{\pi \pi} \sim \sin (\delta)$. Therefore $C_{\pi \pi}$ is expected to be different from zero, and direct $C P$ violation should show up.

The key issue for this analysis is particle identification at high momentum. Using the DIRC and $\mathrm{dE} / \mathrm{dx}$ information, from a control sample of $D^{*+} \rightarrow D^{0} \pi^{+}, D^{0} \rightarrow K^{-} \pi^{+}$decays, reconstructed from our data, we measure a typical separation between pions and kaons variyng from $8 \sigma_{\theta_{c}}$ at $2 \mathrm{GeV} / c$ to $2.5 \sigma_{\theta_{c}}$ at $4 \mathrm{GeV} / c$, where $\theta_{c}$ is the Cherenkov angle. For an efficiency of $85 \%$ the probability of a kaon to be identified as a pion is $1.7 \%$ while the probability for a pion to be identified as a kaon is $2.7 \%$.

Background events from the continuum $e^{+} e^{-} \rightarrow q \bar{q}(q=u, d, s, c)$ are rejected using a number of topological variables [14].

We build probability density functions (PDF) for signal and background relevant variables and we perform an unbinned maximum likelihood fit, ignoring tagging and $\Delta t$ information, to extract the branching fractions and the direct $C P$ asymmetry, $A_{K \pi}=\frac{B^{0} \rightarrow K^{+} \pi^{-}-B^{0} \rightarrow K^{-} \pi^{+}}{B^{0} \rightarrow K^{+} \pi^{-}+B^{0} \rightarrow K^{-} \pi^{+}}$. Table 2 summarizes the signal efficiencies, the branching ratios and the direct $C P$ asymmetry (only $B^{0} \rightarrow K^{+} \pi^{-}$) measurements for $B^{0} \rightarrow$ $\pi^{+} \pi^{-}, K^{+} \pi^{-}, K^{+} K^{-}$.

To validate our fit procedure and the data quality we measure $\Delta m_{d}$ and the $B^{0}$ life time $\tau$ using the sample $B^{0} \rightarrow K \pi$. We find $\Delta m_{d}=$ $(0.52 \pm 0.05) \mathrm{ps}^{-1}$ and $\tau=(1.56 \pm 0.07) \mathrm{ps}$, in very good agreement with the world averages.

To determine $S_{\pi \pi}$ and $C_{\pi \pi}$ we include tagging and $\Delta t$ information in the unbinned maximum likelihood. The $\Delta t \mathrm{PDF}$ for signal $K^{+} \pi^{-}$events takes into account $B^{0}-\bar{B}^{0}$ mixing based on the charge of the kaon and the flavor of $B_{\mathrm{tag}}$. From

Table 2
Summary of results for total detection efficiencies, fitted signal yields $N_{S}$, charge-averaged branching fractions $\mathcal{B}$, and $\mathcal{A}_{K \pi}$. Branching fractions are calculated assuming equal rates for $\Upsilon(4 S) \rightarrow B^{0} \bar{B}^{0}$ and $B^{+} B^{-}$. The upper limits for $N_{K^{+} K^{-}}$and $\mathcal{B}\left(B^{0} \rightarrow K^{+} K^{-}\right)$correspond to the $90 \%$ C.L.

| Mode | Efficiency (\%) | $N_{S}$ | $\mathcal{B}\left(10^{-6}\right)$ | $\mathcal{A}_{K \pi}$ | $\mathcal{A}_{K \pi} 90 \%$ C.L. |
| :--- | :---: | :---: | :---: | :---: | :---: |
| $\pi^{+} \pi^{-}$ | $38.0 \pm 0.8$ | $157 \pm 19 \pm 7$ | $4.6 \pm 0.6 \pm 0.2$ |  |  |
| $K^{+} \pi^{-}$ | $37.5 \pm 0.8$ | $589 \pm 30 \pm 17$ | $17.9 \pm 0.9 \pm 0.7$ | $-0.102 \pm 0.050 \pm 0.016$ | $[-0.188,-0.016]$ |
| $K^{+} K^{-}$ | $36.2 \pm 0.8$ | $1 \pm 8(<16)$ | $<0.6$ |  |  |

this fit we find :

$$
\begin{gathered}
S_{\pi \pi}=0.02 \pm 0.34(\text { stat }) \pm 0.05 \text { (syst) } \\
{[-0.54,+0.58]} \\
C_{\pi \pi}=-0.30 \pm 0.25(\text { stat }) \pm 0.04(\text { syst }) \\
{[-0.72,+0.12]}
\end{gathered}
$$

where the range in square brackets indicates the $90 \%$ C.L. interval taking into account the systematic errors. Figure 9 shows the $\Delta t$ distribution for $B^{0}$ and $\bar{B}^{0}$ events and the asymmetry, $A_{\pi \pi}(\Delta t)$. There is no evidence for direct $C P$ violation within the present errors.

## From $\alpha_{e f f}$ to $\alpha$

In order to extract $\alpha$ or the extra angle pollution $\kappa$, from $B^{0} \rightarrow \pi^{+} \pi^{-}$in the most general case a full isospin analysis is required [15]. One has to measure the branching fractions $\mathcal{B}\left(B^{ \pm} \rightarrow \pi^{ \pm} \pi^{0}\right)$, $\mathcal{B}\left(B^{0} \rightarrow \pi^{+} \pi^{-}\right)$, and $\mathcal{B}\left(B \rightarrow \pi^{0} \pi^{0}\right)$ for both $B^{0}$ and $\bar{B}^{0}$. If $\mathcal{B}\left(B \rightarrow \pi^{0} \pi^{0}\right)$ is small then using only an averaged measurement of $\mathcal{B}\left(B \rightarrow \pi^{0} \pi^{0}\right)=$ $\frac{1}{2}\left(\mathcal{B}\left(B^{0} \rightarrow \pi^{0} \pi^{0}\right)+\mathcal{B}\left(\bar{B}^{0} \rightarrow \pi^{0} \pi^{0}\right)\right)$, an upper bound [16] on $\kappa$ can be derived :

$$
\begin{align*}
\left|2 \alpha-2 \alpha_{e f f}\right| & \leq \arccos \frac{1}{\sqrt{1-C_{\pi \pi}^{2}}} \times \\
& \left(1-2 \frac{\mathcal{B}\left(B \rightarrow \pi^{0} \pi^{0}\right)}{\mathcal{B}^{ \pm} \rightarrow \pi^{ \pm} \pi^{0}}\right) \tag{7}
\end{align*}
$$

We have measured [17] the branching fractions for $B^{+} \rightarrow \pi^{+} \pi^{0}, B^{+} \rightarrow K^{+} \pi^{0}$ and $B^{0} \rightarrow K^{0} \pi^{0}$ decays as well as the direct $C P$ asymmetries integrated over the time. For the $K^{0} \pi^{0}$ mode we need to measure the flavor of the $B$ candidate in order to extract the $C P$ asymmetry.


Figure 8. Distributions of $m_{\mathrm{ES}}$ and $\Delta E$ for events enhanced in signal (a), (b) $\pi^{+} \pi^{-}$and (c), (d) $K^{\mp} \pi^{ \pm}$decays. Solid curves represent projections of the maximum likelihood fit, dashed curves represent $q \bar{q}$ and $\pi \pi \leftrightarrow K \pi$ cross-feed background.

Table 3
Summary of fitted signal yields, measured branching fraction $\mathcal{B}$ and $C P$ asymmetries $\mathcal{A}_{i}$. The first error is statistical and the second is systematic.

| Mode | Signal Yield | $\mathcal{B}\left(10^{-6}\right)$ | $\mathcal{A}_{i}$ | $\mathcal{A}_{i}(90 \% \mathrm{CL})$ |
| :---: | :---: | :---: | :---: | :---: |
| $\pi^{+} \pi^{0}$ | $125_{-21}^{+23} \pm 10$ | $5.5_{-0.9}^{+1.0} \pm 0.6$ | $-0.03_{-0.17}^{+0.18} \pm 0.02$ | $[-0.32,0.27]$ |
| $K^{+} \pi^{0}$ | $239_{-22}^{+21} \pm 6$ | $12.8_{-1.1}^{+1.2} \pm 1.0$ | $-0.09 \pm 0.09 \pm 0.01$ | $[-0.24,0.06]$ |
| $K^{0} \pi^{0}$ | $86 \pm 13 \pm 3$ | $10.4 \pm 1.5 \pm 0.8$ | $0.03 \pm 0.36 \pm 0.09$ | $[-0.58,0.64]$ |



Figure 9. Distributions of $\Delta t$ for events enhanced in signal $\pi \pi$ decays with $B_{\text {rec }}$ tagged as (a) $B^{0}$ or (b) $\bar{B}^{0}$, and (c) the asymmetry $\mathcal{A}_{\pi \pi}(\Delta t)$ as a function of $\Delta t$. Solid curves represent projections of the maximum likelihood fit, dashed curves represent the sum of $q \bar{q}$ and $K \pi$ background events.

Clear signals are observed for all three decay modes, and the direct $C P$ asymmetry is measured. All the results are summarized on Table 3 . No direct $C P$ violation is observed.

The analysis of $B \rightarrow \pi^{0} \pi^{0}$ is very challenging. The expected branching ratio is small, and we have to fight against an important background from $q \bar{q}$ events and $B^{ \pm} \rightarrow \rho^{ \pm} \pi^{0}$ decays. In addition to topological variables, we use the tagging information to further reduce the background. Our overall efficiency is $16.5 \%$. After un unbinned maximum likelihood fit, we observe $23_{-9}^{+10}$ events. We then extract an upper limit for the branching fraction of $B \rightarrow \pi^{0} \pi^{0}$ [18]:

$$
\begin{array}{r}
\mathcal{B}\left(B \rightarrow \pi^{0} \pi^{0}\right)<3.6 \times 10^{-6} \\
\quad \text { at } 90 \% \text { confidence level }
\end{array}
$$

The rather high value of this limit, gives a loose bound for $\left|2 \alpha-2 \alpha_{e f f}\right|<51^{\circ}$, Figure 10. If the branching ratio is higher than 1.5 or $2 \times 10^{-6}$, we will have to perform the complete isospin analysis, as the Grossman-Quin bound will not constrain $\alpha$ enough.
4.2. $C P$ asymmetries in the decays $B \rightarrow$ $\pi^{+} \pi^{-} \pi^{0}$ and $B \rightarrow K^{ \pm} \pi^{\mp} \pi^{0}$ final states
For these modes we restrict the analysis to the only final states dominated by the $\rho^{ \pm}$resonance. As in the case of $B \rightarrow \pi^{+} \pi^{-}$, the $\rho \pi$ mode also measures $\alpha$ as well as direct $C P$ violation. However it is not a $C P$ eigenstate and four amplitudes have to be considered, $\bar{B}^{0} \rightarrow \pi^{-} \rho^{+}, B^{0} \rightarrow \pi^{-} \rho^{+}$, $B^{0} \rightarrow \pi^{+} \rho^{-}$and $\bar{B}^{0} \rightarrow \pi^{+} \rho^{-}$. The decay rate distributions can be written as [19] :


Figure 10. $B \rightarrow \pi^{0} \pi^{0}$ branching fraction versus $2 \alpha-2 \alpha_{e f f}$

$$
\begin{align*}
& f_{B^{0} \mathrm{tag}}^{\rho^{ \pm} h^{\mp}}(\Delta t)=\left(1 \pm A_{C P}^{\rho h}\right) \frac{e^{-|\Delta t| / \tau}}{4 \tau} \times \\
& {\left[1+\left(\left(S_{\rho h} \pm \Delta S_{\rho h}\right) \sin \left(\Delta m_{d} \Delta t\right)\right.\right.} \\
&\left.\left.-\left(C_{\rho h} \pm \Delta C_{\rho h}\right) \cos \left(\Delta m_{d} \Delta t\right)\right)\right] \\
& f_{\bar{B}^{0} \mathrm{tag}}^{\rho^{ \pm} h^{\mp}}(\Delta t)=\left(1 \pm A_{C P}^{\rho h}\right) \frac{e^{-|\Delta t| / \tau}}{4 \tau} \times \\
& {\left[1-\left(\left(S_{\rho h} \pm \Delta S_{\rho h}\right) \sin \left(\Delta m_{d} \Delta t\right)\right.\right.} \\
&\left.\left.-\left(C_{\rho h} \pm \Delta C_{\rho h}\right) \cos \left(\Delta m_{d} \Delta t\right)\right)\right] \tag{8}
\end{align*}
$$

The time-integrated charge asymmetries $A_{C P}^{\rho \pi}$ and $A_{C P}^{\rho K}$ measure direct $C P$ violation. The time dependence is described by four parameters, $S_{\rho h}, C_{\rho h}, \Delta C_{\rho h}$ and $\Delta S_{\rho h}$. In the case of the self-tagging $\rho K$ mode, the values of these four parameters are known to be $C_{\rho K}=0, \Delta C_{\rho K}=-1$, $S_{\rho K}=0$, and $\Delta S_{\rho K}=0$. For the $\rho \pi$ mode, they allow us to probe $C P$ violation. Summing over the $\rho$ charge in Eq. 8, and neglecting the charge asymmetry $A_{C P}^{\rho \pi}$, one obtains the simplified $C P$ asymmetry between the number of $B^{0}$ and $\bar{B}^{0}$
tags, given by:

$$
A_{B^{0} / \bar{B}^{0}} \sim S_{\rho \pi} \sin \left(\Delta m_{d} \Delta t\right)-C_{\rho \pi} \cos \left(\Delta m_{d} \Delta t\right)
$$

The parameter $C_{\rho \pi}$ describes the time-dependent direct $C P$ violation and $S_{\rho \pi}$ measures $C P$ violation in the interference between mixing and decay related to the angle $\alpha$.

The parameters $\Delta C_{\rho \pi}$ and $\Delta S_{\rho \pi}$ are insensitive to $C P$ violation. The asymmetry between $N\left(B_{\rho \pi}^{0} \rightarrow \rho^{+} \pi^{-}\right)+N\left(\bar{B}_{\rho \pi}^{0} \rightarrow \rho^{-} \pi^{+}\right)$and $N\left(B_{\rho \pi}^{0} \rightarrow \rho^{-} \pi^{+}\right)+N\left(\bar{B}_{\rho \pi}^{0} \rightarrow \rho^{+} \pi^{-}\right)$is described by $\Delta C_{\rho \pi}$, while $\Delta S_{\rho \pi}$ is sensitive to the strong phase difference between the amplitudes contributing to $B^{0} \rightarrow \rho \pi$ decays. The naive factorization model [20] predicts $\Delta C_{\rho \pi} \sim 0.4$ while there is no prediction for $\Delta S_{\rho \pi}$.

To reduce the main background for these modes, coming from continuum $q \bar{q}$ (where $q=$ $u, d, s, c)$ events we use a neural network, combining two kinematic variables and two event shape variables. More than 80 charmless decay modes have been considered for potential cross-feed in the signal region. Fitting simultaneously the signal and background events we find $413_{-33}^{+34}$ (stat) $\rho \pi$ and $147_{-21}^{+22}$ (stat) $\rho K$ events in our data sample. Figure 11 shows the distributions of $m_{\mathrm{ES}}$ and $\Delta E$ for data samples that are enhanced in signal using cuts on the signal-to-continuum likelihood ratio of the other discriminating variables. For the $C P$ parameters we then measure [21]:

$$
\begin{gathered}
A_{C P}^{\rho K}=0.19 \pm 0.14 \text { (stat) } \pm 0.11 \text { (syst) } \\
A_{C P}^{\rho \pi}=-0.22 \pm 0.08 \text { (stat) } \pm 0.07 \text { (syst) } \\
C_{\rho \pi}=0.45_{-0.19}^{+0.18} \text { (stat) } \pm 0.09 \text { (syst) } \\
S_{\rho \pi}=0.16 \pm 0.25 \text { (stat) } \pm 0.07 \text { (syst) }
\end{gathered}
$$

The two other observables in the decay rates (Eq. 8) are measured to be

$$
\begin{aligned}
& \Delta C_{\rho \pi}=0.38_{-0.20}^{+0.19} \text { (stat) } \\
& \Delta S_{\rho \pi}=0.15 \pm 0.26 \text { (stat) }
\end{aligned}
$$

Alternatively, the results on direct $C P$ violation can be expressed using the asymmetries

$$
\begin{align*}
A_{+-} & =\frac{N\left(\bar{B}_{\rho \pi}^{0} \rightarrow \rho^{+} \pi^{-}\right)-N\left(B_{\rho \pi}^{0} \rightarrow \rho^{-} \pi^{+}\right)}{N\left(\bar{B}_{\rho \pi}^{0} \rightarrow \rho^{+} \pi^{-}\right)+N\left(B_{\rho \pi}^{0} \rightarrow \rho^{-} \pi^{+}\right)} \\
& =\frac{A_{C P}^{\rho \pi}-C_{\rho \pi}-A_{C P}^{\rho \pi} \cdot \Delta C_{\rho \pi}}{1-\Delta C_{\rho \pi}-A_{C P}^{\rho \pi} \cdot C_{\rho \pi}} \tag{10}
\end{align*}
$$



Figure 11. Distributions of $m_{\mathrm{ES}}$ and $\Delta E$ for samples enhanced in $\rho \pi$ signal using cuts on likelihood ratios. The solid curve represents a projection of the maximum likelihood fit result. The dashed curve represents the contribution from continuum events ( $\rho \pi$ and $\rho K$ candidates combined), and the dotted line indicates the combined contributions from continuum events and $B$-related backgrounds, including $\rho K$.

$$
\begin{align*}
A_{-+} & =\frac{N\left(\bar{B}_{\rho \pi}^{0} \rightarrow \rho^{-} \pi^{+}\right)-N\left(B_{\rho \pi}^{0} \rightarrow \rho^{+} \pi^{-}\right)}{N\left(\bar{B}_{\rho \pi}^{0} \rightarrow \rho^{-} \pi^{+}\right)+N\left(B_{\rho \pi}^{0} \rightarrow \rho^{+} \pi^{-}\right)} \\
& =-\frac{A_{C P}^{\rho \pi}+C_{\rho \pi}+A_{C P}^{\rho \pi} \cdot \Delta C_{\rho \pi}}{1+\Delta C_{\rho \pi}+A_{C P}^{\rho \pi} \cdot C_{\rho \pi}} \tag{11}
\end{align*}
$$

In the decays $\bar{B}_{\rho \pi}^{0} \rightarrow \rho^{+} \pi^{-}$and $B_{\rho \pi}^{0} \rightarrow \rho^{-} \pi^{+}$ the spectator quark is involved in the formation of the $\rho$ meson. These two decay modes are related to the direct $C P$ asymmetry $A_{+-}$according to Eq. 10. Similarly in Eq. 11, we probe direct $C P$ violation through the asymmetry $A_{-+}$using the decays $\bar{B}_{\rho \pi}^{0} \rightarrow \rho^{-} \pi^{+}$and $B_{\rho \pi}^{0} \rightarrow \rho^{+} \pi^{-}$. In this case the $\pi$ meson is formed from the spectator quark. From the above fitted values we obtain

$$
\begin{align*}
& A_{+-}=-0.82 \pm 0.31 \text { (stat) } \\
& A_{-+}=-0.11 \pm 0.16 \text { (stat) } \tag{12}
\end{align*}
$$

Extracting $\alpha$ from these measurements is not straight forward, and considerable theoretical input is needed.

## 5. The angle $\gamma$

The $B A B A R$ experiment takes data only on the $\Upsilon(4 S)$ resonance, below the $B_{s}$ threshold, whose decays can be used to measure the angle $\gamma$. However it has been proposed $[22,23]$ to use the branching ratios of the processes $B^{-} \rightarrow$ $D_{(C P)}^{0} K^{-}$and $B^{ \pm} \rightarrow D_{C P}^{0} K^{ \pm}$, where $D_{C P}^{0}$ indicates the $C P$-even or $C P$-odd states $\left(D^{0} \pm\right.$ $\left.\bar{D}^{0}\right) / \sqrt{2}$ and extract $2 \gamma$. As a first step for this analysis we have measured [24] the ratios,
$R \equiv \frac{\mathcal{B}\left(B^{-} \rightarrow D^{0} K^{-}\right)}{\mathcal{B}\left(B^{-} \rightarrow D^{0} \pi^{-}\right)}$
and

$$
R_{C P} \equiv \frac{\mathcal{B}\left(B^{-} \rightarrow D_{C P}^{0} K^{-}\right)+\mathcal{B}\left(B^{+} \rightarrow D_{C P}^{0} K^{+}\right)}{\mathcal{B}\left(B^{-} \rightarrow D_{C P}^{0} \pi^{-}\right)+\mathcal{B}\left(B^{+} \rightarrow D_{C P}^{0} \pi^{+}\right)}
$$

as well as the direct CP asymmetry

$$
A_{C P} \equiv \frac{\mathcal{B}\left(B^{-} \rightarrow D_{C P}^{0} K^{-}\right)-\mathcal{B}\left(B^{+} \rightarrow D_{C P}^{0} K^{+}\right)}{\mathcal{B}\left(B^{-} \rightarrow D_{C P}^{0} K^{-}\right)+\mathcal{B}\left(B^{+} \rightarrow D_{C P}^{0} K^{+}\right)}
$$

We reconstruct three $D^{0}$ decay modes, $D^{0} \rightarrow$ $K^{-} \pi^{+}, D^{0} \rightarrow K^{-} \pi^{+} \pi^{+} \pi^{-}, D^{0} \rightarrow K^{-} \pi^{+} \pi^{0}$ and
we combine them with a kaon or pion to reconstruct the decay $B^{-} \rightarrow D_{(C P)}^{0} K^{-}$. We then measure the ratio R for each $D^{0}$ mode, and the combined result is :
$R=(8.31 \pm 0.35 \pm 0.20) \%$
From the decay $D^{0} \rightarrow K^{-} K^{+}$combining with a charged kaon we compute
$R_{C P}=(7.4 \pm 1.7 \pm 0.6) \%$
Then the direct $C P$ asymmetry, integrated over time is measured to be :
$A_{C P}=0.17 \pm 0.23_{-0.07}^{+0.09}$

## 6. Summary

With more than $88 \mathrm{M} B \bar{B}$ pairs the BABAR experiment has measured a new value for $\sin 2 \beta=$ $0.741 \pm 0.067$ (stat) $\pm 0.034$ (syst) extracted from $b \rightarrow c \bar{c} s$ decays. Less precise measurements from other modes have also been performed and will allow in the future to probe for new physics effects. We have also measured $S_{\pi \pi}=0.02 \pm 0.34$ (stat) $\pm$ 0.05 (syst) and $C_{\pi \pi}=-0.30 \pm 0.25$ (stat) $\pm$ 0.04 (syst) and start building the full isospin analysis to extract $\alpha$. We have also studied for the first time the decay $B \rightarrow \pi^{+} \pi^{-} \pi^{0}$ dominated by the $\rho$ final states, and measure the $C P$ violating parameters. We do not have a strong evidence for direct $C P$ violation yet. We expect in the next years, as the integrated luminosity will increase significantly, to bring some answers to the whole picture of the $C P$ violation phenomenon.

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