# Search For the Decay $B \rightarrow D_{s 1}^{+}(2536) X$ 

CLEO Collaboration


#### Abstract

We have searched for the decay $B \rightarrow D_{s 1}^{+}(2536) X$ and measured an upper limit for the inclusive branching fraction of $\mathcal{B}\left(B \rightarrow D_{s 1}^{+} X\right)<0.95 \%$ at the $90 \%$ confidence level. This limit is small compared with the total expected $B \rightarrow \bar{D}^{(*)} D^{(*)} K X$ rate. Assuming factorization, the $D_{s 1}^{+}$decay constant is constrained to be $f_{D_{s 1}^{+}}<114 \mathrm{MeV}$ at the $90 \%$ confidence level, at least 2.5 times smaller than that of $D_{s}^{+}$.


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## I. INTRODUCTION

One of the outstanding issues in $B$ meson physics is the semileptonic branching fraction puzzle. Experimentally $\mathcal{B}(B \rightarrow X \ell \nu)$ is measured to be $(10.43 \pm 0.24) \%$ [1], whereas theoretical calculations have difficulties accommodating a branching fraction below $\sim 12.5 \%$ [2]. One way to reduce the theoretical expectations is through a two-fold enhancement in the assumed $\bar{b} \rightarrow \bar{c} c \bar{s}$ rate [3], which is estimated to be $\sim 15 \%$ from the measured inclusive rates for $B \rightarrow D_{s}^{+} X$ and $B \rightarrow \psi X$.

Recently, Buchalla et al. [4] and Blok et al. [5] have suggested that a significant fraction of the $\bar{b} \rightarrow \bar{c} c \bar{s}$ transition hadronizes into $B \rightarrow \bar{D} D K X$. This is supported by CLEO's [6] observation of "wrong-sign" $D$ mesons from $B$ decays, $\mathcal{B}(B \rightarrow D X)=(7.9 \pm 2.2) \%$, where the $D$ comes from the virtual $W^{+} \rightarrow c \bar{s}$. The ALEPH [7] and DELPHI [8] collaborations have also observed sizeable $B \rightarrow D^{(*)} \bar{D}^{(*)} X$ decay rates. Exclusive $B$ decays involving wrongsign $D$ mesons can result from (1) resonant $B \rightarrow \bar{D}^{(*)} D_{s}^{* *}$ decays, where the $W^{+} \rightarrow c \bar{s}$ hadronizes to an excited $D_{s}^{+}$meson that decays into $D K X$; and (2) non-resonant $B \rightarrow$ $\bar{D}^{(*)} D^{(*)} K$ decays. This paper explores one possibility in the first case, namely, the decays $B \rightarrow D_{s 1}^{+}(2536) X$ where $D_{s 1}^{+}$is the narrow P-wave $D_{s}^{+}$meson with $J^{P}=1^{+}$. The "uppervertex" production of $D_{s 1}^{+}$from $W^{+} \rightarrow c \bar{s}$ hadronization is shown in Figure [1(a). In addition, $D_{s 1}^{+}$mesons can be produced from "lower-vertex" decays $b \rightarrow c \bar{u} d$ with the creation of an $s \bar{s}$ quark pair, as shown in Figure 1 (b). This produces right-sign $D$ mesons; however, the decay rate is expected to be small. Throughout this paper charge conjugate states are implied.

Continuum $D_{s 1}^{+}$production has been thoroughly studied [1]. The $D_{s 1}^{+}$is just above the $D^{*} K$ mass threshold and decays dominantly into $D^{* 0} K^{+}$and $D^{*+} K^{0}$. Other possible decay channels are negligible: $D_{s}^{(*)+} \pi^{0}$ due to isospin conservation, $D_{s}^{(*)+}(n \pi)$ due to OZI suppression [9], $D K$ or $D_{s}^{+} \pi^{0}$ due to angular momentum and parity conservation, and $D_{s}^{(*)+} \gamma$ due to the small radiative decay rate.

## II. DATA SAMPLE AND EVENT SELECTION

The data used in this analysis were selected from hadronic events collected by the CLEO II detector at the Cornell Electron Storage Ring (CESR). The CLEO II detector [10] is a large solenoidal detector with 67 tracking layers and a CsI electromagnetic calorimeter that provides efficient $\pi^{0}$ reconstruction. The data consist of an integrated luminosity of 3.11 $\mathrm{fb}^{-1}$ at the $\Upsilon(4 S)$ resonance, corresponding to $3.3 \times 10^{6} B \bar{B}$ events. To evaluate non- $B \bar{B}$ backgrounds we also collected $1.61 \mathrm{fb}^{-1}$ of "continuum" data 60 MeV below the $\Upsilon(4 S)$ resonance.

The inclusive $B \rightarrow D_{s 1}^{+} X$ decay is studied by reconstructing the decay channels $D_{s 1}^{+} \rightarrow$ $D^{* 0} K^{+}$and $D^{*+} K_{S}^{0}$ using the decay modes $D^{* 0} \rightarrow D^{0} \pi^{0}$ and $D^{*+} \rightarrow D^{0} \pi^{+}$. The $D^{0}$ is reconstructed using the decay modes $D^{0} \rightarrow K^{-} \pi^{+}$and $K^{-} \pi^{+} \pi^{0}$. Hadronic events are required to satisfy the ratio of Fox-Wolfram moments [11] $R_{2}=H_{2} / H_{0}<0.3$ to reduce the background from continuum events.

Charged tracks, except pions from $K_{S}^{0}$ decays, are required to be consistent with coming from the primary interaction point. Charged kaon and pion candidates are identified using specific ionization $(d E / d x)$ and, when available, time-of-flight (TOF) information. For kaon
identification, we consider the relative probability for a charged track to be a kaon, $\mathcal{R}_{K}=$ $\mathcal{P}_{K} /\left(\mathcal{P}_{\pi}+\mathcal{P}_{K}+\mathcal{P}_{p}\right)$, where $\mathcal{P}$ is the $\chi^{2}$ probability for a given particle hypothesis. The requirement on $\mathcal{R}_{K}$ depends on the decay mode of interest. Pion candidates are identified by requiring the $d E / d x$ and, when available, TOF information to be within 3 standard deviations $(\sigma)$ of that expected for pions. We select $K_{S}^{0}$ candidates through the decay to $\pi^{+} \pi^{-}$by requiring a decay vertex displaced from the primary interaction point and a $K_{S}^{0}$ invariant mass within $10 \mathrm{MeV} / \mathrm{c}^{2}$ of its nominal value. We reconstruct $\pi^{0}$ candidates through the decay to $\gamma \gamma$ by requiring candidates to have an invariant mass within 2.5 standard deviations ( $\sigma \approx 5 \mathrm{MeV} / \mathrm{c}^{2}$ ) of the nominal $\pi^{0}$ mass.

The $K^{-} \pi^{+}$and $K^{-} \pi^{+} \pi^{0}$ combinations are required to have a kaon identification of $\mathcal{R}_{K}>$ 0.5 and 0.7 , respectively, and an invariant mass within 15 and $25 \mathrm{MeV} / \mathrm{c}^{2}(\sim 2 \sigma)$ of the nominal $D^{0}$ mass, respectively. In addition, we select regions of the $D^{0} \rightarrow K^{-} \pi^{+} \pi^{0}$ Dalitz plot to take advantage of the known resonant substructure 12 . For the $D_{s 1}^{+} \rightarrow D^{* 0} K^{+}$ mode, the Dalitz cut reduces the signal efficiency by $40 \%$ and the background by $80 \%$. We relax the Dalitz cut for the $D^{*+} K_{S}^{0}$ mode since the combinatoric background is substantially lower.

The $D^{*+} \rightarrow D^{0} \pi^{+}$candidates are required to have a mass difference $M\left(D^{0} \pi^{+}\right)-M\left(D^{0}\right)$ within $1.5 \mathrm{MeV} / \mathrm{c}^{2}(\sim 2 \sigma)$ of the nominal value of $145.4 \mathrm{MeV} / \mathrm{c}^{2}$, where $M(X)$ is the reconstructed invariant mass of $X$. Similarly, the $D^{* 0} \rightarrow D^{0} \pi^{0}$ candidates are required to have a mass difference $M\left(D^{0} \pi^{0}\right)-M\left(D^{0}\right)$ within $1.5 \mathrm{MeV} / \mathrm{c}^{2}(\sim 2 \sigma)$ of the nominal value of $142.1 \mathrm{MeV} / \mathrm{c}^{2}$. To form $D_{s 1}^{+}$candidates charged kaons are combined with $D^{* 0}$ candidates and $K_{S}^{0}$ 's are combined with $D^{*+}$ candidates. Since the primary kaons from $D_{s 1}^{+} \rightarrow D^{* 0} K^{+}$ decays have low momentum, we can impose a stringent $\mathcal{R}_{K}>0.9$ requirement on the $K^{+}$ with negligible loss of efficiency. The $D_{s 1}^{+}$candidates are required to have a scaled momentum $x_{p}=p_{D_{s 1}^{+}} / \sqrt{E_{\text {beam }}^{2}-M_{D_{s 1}^{+}}^{+}}<0.45$, which is the kinematic limit for $B \rightarrow D_{s 1}^{+} X$ decays. (We ignore the negligible contributions from $b \rightarrow u$ decays.) Upper-vertex $D_{s 1}^{+}$production results in a maximum $x_{p}$ of 0.35 , and this requirement is imposed when determining the $D_{s 1}^{+}$ decay constant. The $D_{s 1}^{+}$decay channels with $\pi^{0}$ 's in the final state often have multiple $D_{s 1}^{+}$ candidates per event. We select the candidate with the highest $\chi^{2}$ probability of being a $D_{s 1}^{+}$, which is derived from the invariant masses of the reconstructed $\pi^{0}, D^{0}$ and $D^{*}$ mesons.

## III. RAW YIELDS

The $D_{s 1}^{+}$signal is identified using the $D^{*} K$ mass difference, $\Delta M_{1}=M\left(D^{* 0} K^{+}\right)-$ $M\left(D^{* 0}\right)-M_{K^{+}}$and $\Delta M_{2}=M\left(D^{*+} K_{S}^{0}\right)-M\left(D^{*+}\right)-M_{K_{S}^{0}}$, where $M_{K^{+}}$and $M_{K_{S}^{0}}$ are the known masses [1]. The $D^{*} K$ mass difference signal has a resolution that is two to four times smaller than the corresponding signal in the reconstructed $D^{*} K$ invariant mass distribution. The $\Delta M_{1}$ and $\Delta M_{2}$ distributions are shown in Figure 2, where the $D^{0} \rightarrow K^{-} \pi^{+}$ and $K^{-} \pi^{+} \pi^{0}$ modes have been added together. The data is fit with a Gaussian signal and a threshold background function. The Gaussian width is fixed to that expected from a GEANT-based Monte Carlo simulation [13] $\left(\sigma=2.4-3.6 \mathrm{MeV} / \mathrm{c}^{2}\right.$, depending on the mode) and the mean is fixed to the measured $D_{s 1}^{+}$mass difference from continuum data ( $\Delta M_{1} \approx 35$ $\mathrm{MeV} / \mathrm{c}^{2}$ and $\Delta M_{2} \approx 27 \mathrm{MeV} / \mathrm{c}^{2}$.) We observe $42 \pm 14$ signal events in the $D^{* 0} K^{+}$mode and $9 \pm 6$ events in the $D^{*+} K_{S}^{0}$ mode.

However, when the $D^{* 0} K^{+}$candidates are further subdivided into the $D^{0} \rightarrow K^{-} \pi^{+}$and $K^{-} \pi^{+} \pi^{0}$ decay channels there is a discrepancy in the $D_{s 1}^{+}$yields. As shown in Figure 3, we observe $10 \pm 8$ signal events in the $\Delta M_{1}$ distribution for the $D^{0} \rightarrow K^{-} \pi^{+}$channel and $33 \pm 12 D_{s 1}^{+}$signal events for the $D^{0} \rightarrow K^{-} \pi^{+} \pi^{0}$ channel. After accounting for branching fractions and efficiencies, discussed below, this results in a $2.2 \sigma$ discrepancy in the $D^{* 0} K^{+}$ rates between the two $D^{0}$ modes. We cannot rule out the fact that background sources may be contributing a false $D_{s 1}^{+}$signal in the $D^{0} \rightarrow K^{-} \pi^{+} \pi^{0}$ channel, but not in the $D^{0} \rightarrow K^{-} \pi^{+}$ channel. However, no such mechanism has been uncovered. To be conservative, we choose to quote only an upper limit for the decay $B \rightarrow D_{s 1}^{+} X$.

Since the $D_{s 1}^{+}$reconstruction efficiency increases rapidly with $x_{p}$ and the $D_{s 1}^{+}$momentum distribution from $B$ decays is not known, we compute the inclusive $B \rightarrow D_{s 1}^{+} X$ branching fraction by dividing the data into four equal regions of $x_{p}$ from 0.05 to 0.45 and summing the efficiency corrected yields. The $D_{s 1}^{+} \rightarrow D^{* 0} K^{+}$and $D^{*+} K^{0}$ branching fractions are equal according to isospin, and their ratio has been measured to be within $30 \%$ of unity [14]. We measure the branching fraction $B \rightarrow D_{s 1}^{+} X$ to be ( $0.77 \pm 0.22$ ) \% from the $D^{* 0} K^{+}$mode and $(0.28 \pm 0.37) \%$ from the $D^{*+} K_{S}^{0}$ mode, where the error is statistical only. The two measurements are statistically consistent. The $x_{p}$ distribution for our $D_{s 1}^{+}$candidates is shown in Figure 7.

## IV. CROSS-CHECKS

Several cross-checks, shown in Figure 5, were performed to corroborate the validity of the $D_{s 1}^{+}$signal. The scaled continuum background from data after satisfying all selection cuts is negligible, and there is no excess in the $\Delta M_{1}$ signal region ( $3 \pm 5$ events). The uncertainty in the continuum $D_{s 1}^{+}$contribution is included in the systematic error. There is also no evidence of peaking in the $\Delta M_{1}$ signal region for wrong-sign $D^{* 0} K^{-}$combinations ( $0 \pm 9$ events), $D^{0}$ mass sidebands ( $5 \pm 5$ events), and $D^{* 0}$ mass sidebands ( $-4 \pm 6$ events).

We have also searched for the $D^{0}$ signal from $D_{s 1}^{+} \rightarrow D^{* 0} K^{+}$candidates in the $\Delta M_{1}$ signal region, $\left|\Delta M_{1}-35 \mathrm{MeV} / \mathrm{c}^{2}\right|<10 \mathrm{MeV} / \mathrm{c}^{2}$, by relaxing the $D^{0}$ mass cut and histogramming the invariant mass of all $K^{-} \pi^{+}$and $K^{-} \pi^{+} \pi^{0}$ combinations that satisfy the remaining selection criteria. In events with multiple candidates per $D^{0}$ decay mode we select the candidate with the highest $\chi^{2}$ probability, which is derived from the reconstructed $\pi^{0}$ and $D_{s 1}^{+}$masses. We observe $100 \pm 15 D^{0}$ events. However, there are also real $D^{0}$ 's in the random $D^{* 0} K^{+}$ combinations under the $D_{s 1}^{+}$peak; after a $\Delta M_{1}$ sideband subtraction the $D^{0}$ invariant mass spectrum yields $44 \pm 18$ events (see Figure $6(\mathrm{a})$ ). This is consistent with our $D_{s 1}^{+} \rightarrow D^{* 0} K^{+}$ yield in Figure 2 .

Similarly, we have studied the $D^{* 0}$ signal from $D_{s 1}^{+} \rightarrow D^{* 0} K^{+}$candidates in the $\Delta M_{1}$ signal region. We observe $59 \pm 15 D^{0}$ events. As in the $D^{0}$ case there are also real $D^{* 0}$ 's in the random $D^{* 0} K^{+}$combinations under the $D_{s 1}^{+}$peak. After a $\Delta M_{1}$ sideband subtraction the $D^{* 0}$ mass difference spectrum yields $25 \pm 18$ events (See Figure 6(b)), consistent with our $D_{s 1}^{+} \rightarrow D^{* 0} K^{+}$yield.

Finally, we have studied the $D_{s 1}^{+}$production from continuum $e^{+} e^{-} \rightarrow c \bar{c}$ events. The selection criteria is similar to that used to find $D_{s 1}^{+}$from $B$ decays, but since continuum charm production has a hard fragmentation, we require $x_{p}>0.5$. In addition, we remove
the $R_{2}<0.3$ cut, relax the charged kaon identification to $\mathcal{R}_{K}>0.1$, and remove the Dalitz cut for $D^{0} \rightarrow K^{-} \pi^{+} \pi^{0}$. The mass difference distribution for $D^{* 0} K^{+}$and $D^{*+} K_{S}^{0}$ combinations are shown in Figure 7, where the $D^{0} \rightarrow K^{-} \pi^{+}$and $K^{-} \pi^{+} \pi^{0}$ modes have been added together. We extract the $D_{s 1}^{+}$signal by fitting the data with a Gaussian signal and a threshold background function. The Gaussian width is fixed to the value predicted by Monte Carlo ( $2.1 \mathrm{MeV} / \mathrm{c}^{2}$ ), and the mean is allowed to float. We observe $222 \pm 19$ events in the $D_{s 1}^{+} \rightarrow D^{* 0} K^{+}$mode with a mass difference of $35.0 \pm 0.2 \mathrm{MeV} / \mathrm{c}^{2}$ (statistical error only), and $101 \pm 11$ events in the $D_{s 1}^{+} \rightarrow D^{*+} K_{S}^{0}$ mode with a mass difference of $27.5 \pm 0.3$ $\mathrm{MeV} / \mathrm{c}^{2}$. The results are consistent with the previous CLEO analysis [14].

## V. SYSTEMATIC ERRORS AND FINAL RESULTS

There are several sources of systematic error. We assign a systematic error of $16 \%$ to account for the $2.2 \sigma$ discrepancy between the $D^{* 0} K^{+}$rates for the $D^{0} \rightarrow K^{-} \pi^{+}$and $K^{-} \pi^{+} \pi^{0}$ modes. This accomodates different methods of computing the weighted average of the $B \rightarrow D_{s 1}^{+} X$ branching fraction from the four separate decay chains. Uncertainties due to reconstruction efficiencies include $1.5 \%$ per charged track, $5 \%$ per $\pi^{0}, 5 \%$ for slow pions from $D^{*}$, and $5 \%$ for $K_{S}^{0}$. We also include systematic errors of $7 \%$ for Monte Carlo statistics, $5 \%$ for kaon identification and the Dalitz decay cut efficiency, $4 \%$ for uncertainties in the yield for $x_{p}<0.05$, and $8 \%$ for uncertainties in the continuum $D_{s 1}^{+}$contribution that passes our selection criteria. The total systematic error is $24 \%$.

Averaging the $D^{* 0} K^{+}$and $D^{*+} K_{S}^{0}$ modes together, we obtain $\mathcal{B}\left(B \rightarrow D_{s 1}^{+} X\right)=(0.64 \pm$ $0.19 \pm 0.15) \%$. Since the $D_{s 1}^{+}$signal is observed largely in only one decay mode $D_{s 1}^{+} \rightarrow$ $D^{* 0} K^{+}$with $D^{0} \rightarrow K^{-} \pi^{+} \pi^{0}$, and since there is a discrepancy between this mode and the corresponding mode involving $D^{0} \rightarrow K^{-} \pi^{+}$, we instead prefer to quote an upper limit on the branching fraction to be $\mathcal{B}<0.95 \%$ at the $90 \%$ C.L. [15] This decay rate limit is small relative to the total rate expected for $B \rightarrow \bar{D}^{(*)} D^{(*)} K X$ of about $(7.9 \pm 2.2) \%$ from the wrong-sign $D$ meson yield in $B$ decays [6]. This is not surprising considering the $c \bar{s}$ system has appreciable phase space beyond the $D_{s 1}^{+}$mass [4]. Also, CLEO's [16] recent observation of exclusive $B \rightarrow \bar{D}^{(*)} D^{(*)} K$ decays shows that the $D^{(*)} K$ invariant mass distribution lies mostly above the $D_{s 1}^{+}$mass.

## VI. $D_{S 1}^{+}$DECAY CONSTANT

Measurement of the $B \rightarrow D_{s 1}^{+} X$ decay rate also provides an estimate of the $D_{s 1}^{+}$decay constant, $f_{D_{s 1}^{+}}$, assuming that the $D_{s 1}^{+}$comes dominantly from upper-vertex decays. The inclusive decay rate for $B$ mesons into ground state or excited $D_{s}^{+}$mesons can be calculated assuming factorization [17],

$$
\Gamma\left(B \rightarrow D_{s} X\right)=\frac{G_{F}^{2}\left|V_{c b} V_{c s}\right|^{2}}{16 \pi} M_{b}^{3} a_{1}^{2} f_{D_{s}}^{2} I(x, y)
$$

where $a_{1}$ is the BSW [18] parameter for the effective charged current, and $I(x, y)$ is a kinematic factor with $x=M_{D_{s}}^{2} / M_{b}^{2}$ and $y=M_{c}^{2} / M_{b}^{2}$. For scalar or pseudoscalar $D_{s}$ mesons,
$I(x, y)=\sqrt{(1-x-y)^{2}-4 x y}\left(1-x-2 y-x y+y^{2}\right)$, and for vector or axial-vector $D_{s}$ mesons, $I(x, y)=\sqrt{(1-x-y)^{2}-4 x y}\left(1+x-2 x^{2}-2 y+x y+y^{2}\right)$.

We have tightened the $x_{p}$ requirement to $x_{p}<0.35$ since this is the kinematic limit for upper-vertex $B \rightarrow D_{s 1}^{+} \bar{D} X$ decays. The production of ground state and excited $D_{s}^{+}$ mesons from lower-vertex decays such as $\bar{B} \rightarrow D_{s 1}^{+} \bar{K} X$ is expected to be suppressed. This is certainly true for $B \rightarrow D_{s}^{+} X$ decays where the fraction of $D_{s}^{+}$produced at the lower-vertex is measured to be $0.172 \pm 0.079 \pm 0.026$ [19]. Moreover, there is no evidence of $D_{s 1}^{+}$production in the region $x_{p}=0.35-0.45$ where lower-vertex production is likely to occur (see Figure 7 .)

With the assumption $f_{D_{s}^{+}}=f_{D_{s}^{*+}}$ we can extract $f_{D_{s 1}^{+}}$from the ratio of inclusive rates,

$$
\frac{\mathcal{B}\left(B \rightarrow D_{s 1}^{+} X\right)}{\mathcal{B}\left(B \rightarrow D_{s}^{+} X\right)}=\frac{\Gamma\left(B \rightarrow D_{s 1}^{+} X\right)}{\Gamma\left(B \rightarrow D_{s}^{+} X\right)+\Gamma\left(B \rightarrow D_{s}^{*+} X\right)} \approx 0.49\left(\frac{f_{D_{s 1}^{+}}}{f_{D_{s}^{+}}}\right)^{2}
$$

Many systematic errors cancel in the ratio. When computing the $D_{s 1}^{+}$decay constant from the above equation, we use $(75 \pm 25) \%$ of the measured $B \rightarrow D_{s 1}^{+} X$ branching fraction to account for uncertainties in the upper and lower vertex contributions to $D_{s 1}^{+}$. This accomodates the excess of $B \rightarrow D_{s 1}^{+} X$ candidates observed at low $x_{p}<0.15$ as seen in Figure $\theta$. From our upper limit on $B \rightarrow D_{s 1}^{+} X$ and CLEO's 20] measurement of $\mathcal{B}\left(B \rightarrow D_{s}^{+} X\right)=(12.11 \pm$ $0.39 \pm 0.88 \pm 1.38) \%$, we derive $f_{D_{s 1}} / f_{D_{s}^{+}}<0.40$ at the $90 \%$ C.L. The central value is $f_{D_{s 1}^{+}} / f_{D_{s}^{+}}=0.29 \pm 0.06 \pm 0.06$, where the first error is due to the total error in the inclusive $B \rightarrow D_{s}^{+} X$ and $B \rightarrow D_{s 1}^{+} X$ branching fractions, and the second is the uncertainty in the non-factorizable and lower-vertex contributions to the $B \rightarrow D_{s 1}^{+} X$ decay rate. Using the measured value of $f_{D_{s}^{+}}=280 \pm 40 \mathrm{MeV}$ [20] gives $f_{D_{s 1}^{+}}=81 \pm 26 \mathrm{MeV}$ which corresponds to an upper limit of $f_{D_{s 1}^{+}}<114 \mathrm{MeV}$. This limit accomodates the prediction of $f_{D_{s 1}^{+}}=87 \pm 19$ MeV by Veseli and Dunietz 21].

## VII. CONCLUSIONS

In summary, we have searched for $B$ mesons decaying into the P-wave $D_{s 1}^{+}(2536)$ meson. The upper limit of $\mathcal{B}\left(B \rightarrow D_{s 1}^{+} X\right)<0.95 \%$ at the $90 \%$ C.L. accounts for at most only a fraction of the total wrong-sign $B \rightarrow D X$ rate. Assuming factorization, the decay constant $f_{D_{s 1}^{+}}$is at least a factor of 2.5 times smaller than the decay constant for the pseudoscalar $D_{s}^{+}$.

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## REFERENCES

[1] Particle Data Group, R.M. Barnett et al., Phys. Rev. D 54, 1 (1996).
[2] I. Bigi, B. Blok, M. Shifman and A. Vainshtein, Phys. Lett. B 323, 408 (1994).
[3] A.F. Falk, M.B. Wise, and I. Dunietz, Phys. Rev. D 51, 1183 (1995); E. Bagan, P. Ball, V.M. Braun, and P. Gosdzinsky, Phys. Lett. B 324, 362 (1995); M.B. Voloshin, Phys. Rev. D 51, 3948 (1995).
[4] G. Buchalla, I. Dunietz, and H. Yamamoto, Phys. Lett. B 364, 188 (1995).
[5] B. Blok, M. Shifman, and N. Uraltsev, preprint CERN-TH/96-252.
[6] CLEO Collaboration, T.E. Coan et al., preprint CLNS 97/1516, CLEO 97-23.
[7] ALEPH Collaboration, PA05-060, contributed to the 1996 International Conference on High Energy Physics, Warsaw, Poland.
[8] DELPHI Collaboration, PA01-108, contributed to the 1996 International Conference on High Energy Physics, Warsaw, Poland.
[9] S. Okubo, Phys. Lett. B 5, 165 (1963); G. Zweig, CERN Report 8419/TH412 (1964); I. Iizuka, Prog. Theor. Phys. Suppl. 37, 21 (1966).
[10] CLEO Collaboration, Y. Kubota et al., Nucl. Inst. and Meth. A320, 66 (1992).
[11] G. Fox and S. Wolfram, Phys. Rev. Lett. 41, 1581 (1978).
[12] E691 Collaboration, J.C. Anjos et al., Phys. Rev. D 48, 56 (1993).
[13] R. Brun et al., GEANT 3.15, CERN DD/EE/84-1.
[14] CLEO Collaboration, J. Alexander et al., Phys. Lett. B 303, 377 (1993).
[15] The $90 \%$ upper limit is derived, assuming Gaussian statistics, by adding 1.28 times the total error to the central value.
[16] CLEO Collaboration, M. Bishai et al., CLEO-CONF 97-26, EPS97-337, contributed to the 1997 International Europhysics Conference on High Energy Physics, Jerusalem, Israel.
[17] J.H. Kuhn, S. Nussinov, and R. Ruckl, Z. Phys. C 5, 117 (1980).
[18] M. Bauer, B. Stech, and M. Wirbel, Z. Phys. C 29, 637 (1985).
[19] CLEO Collaboration, X. Fu et al., CLEO CONF-95-11, EPS0169, contributed to the 1995 International Europhysics Conference on High Energy Physics, Brussels, Belgium.
[20] CLEO Collaboration, D. Gibaut et al., Phys. Rev. D 53, 4734 (1996).
[21] S. Veseli and I. Dunietz, Phys. Rev. D 54, 6803 (1996).


FIG. 1. Feynman diagrams for (a) $B \rightarrow D_{s 1}^{+} X$ decays producing $D_{s 1}^{+}$at the upper-vertex and (b) $B \rightarrow D_{s 1}^{-} X$ decays producing $D_{s 1}^{-}$at the lower-vertex.


FIG. 2. The mass difference distribution for (a) $D^{* 0} K^{+}$and (b) $D^{*+} K_{S}^{0}$ candidates from $B$ meson decays.


FIG. 3. The $\Delta M_{1}$ mass difference distribution for $D^{* 0} K^{+}$candidates from the (a) $D^{0} \rightarrow K^{-} \pi^{+}$ and (b) $D^{0} \rightarrow K^{-} \pi^{+} \pi^{0}$ decay channels.


FIG. 4. The efficiency corrected yield for our $B \rightarrow D_{s 1}^{+} X$ candidates as a function of the $D_{s 1}^{+}$ scaled momentum $x_{p}$. The kinematic limit from upper-vertex and lower-vertex $B \rightarrow D_{s 1}^{+} X$ decays is $x_{p}<0.35$ and $x_{p}<0.45$, respectively.


FIG. 5. The normalized $D^{* 0} K^{+}$mass difference distributions from (a) continuum events, (b) $D^{* 0} K^{-}$"wrong-sign" combinations, (c) $D^{0}$ mass sidebands, and (d) $D^{* 0}$ mass sidebands.


FIG. 6. (a) The invariant mass distribution for $K^{-} \pi^{+}$and $K^{-} \pi^{+} \pi^{0}$ combinations from $D^{* 0} K^{+}$ candidates in the $\Delta M_{1}$ signal region, after sideband subtraction. (b) The $D^{* 0}$ mass difference distribution from $D^{* 0} K^{+}$candidates in the $\Delta M_{1}$ signal region, after sideband subtraction.


FIG. 7. The mass difference distribution for (a) $D^{* 0} K^{+}$and (b) $D^{*+} K_{S}^{0}$ candidates from continuum $e^{+} e^{-} \rightarrow c \bar{c}$ events.

