# A Measurement of $\psi(2 S)$ Resonance Parameters 

## (BES Collaboration)

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Cross sections for $e^{+} e^{-} \rightarrow$ hadrons, $\pi^{+} \pi^{-} J / \psi$, and $\mu^{+} \mu^{-}$have been measured in the vicinity of the $\psi(2 S)$ resonance using the BESII detector operated at the BEPC. The $\psi(2 S)$ total width; partial widths to hadrons, $\pi^{+} \pi^{-} J / \psi$, muons; and corresponding branching fractions have been determined to be $\Gamma_{t}=264 \pm 27 \mathrm{keV} ; \Gamma_{h}=$ $258 \pm 26 \mathrm{keV}, \Gamma_{\mu}=2.44 \pm 0.21 \mathrm{keV}$, and $\Gamma_{\pi^{+} \pi^{-} J / \psi}=85.4 \pm 8.7 \mathrm{keV} ;$ and $B_{h}=(97.79 \pm 0.15) \%, B_{\pi^{+} \pi^{-} J / \psi}=$ $(32.3 \pm 1.4) \%, B_{\mu}=(0.93 \pm 0.08) \%$, respectively.

## 1. Introduction

Since the discovery of the $\psi(2 S)$ in 1974 [1], a few measurements of its total width $\left(\Gamma_{t}\right)$, and partial decay widths into hadrons $\left(\Gamma_{h}\right), \pi^{+} \pi^{-} J / \psi$ ( $\Gamma_{\pi^{+} \pi^{-} J / \psi}$ ), and $\mu^{+} \mu^{-}\left(\Gamma_{\mu}\right)$, and the corresponding branching fractions, $B_{h}, B_{\pi^{+} \pi^{-} J / \psi}$, and $B_{\mu}$, have been carried out $[2-9]$. The results of these experiments differ on both decay widths and branching fractions, as shown in Table 1. The parameters are of particular interest because, for instance, $\psi(2 S) \rightarrow \mu^{+} \mu^{-}$is used in reconstructing $B$ mesons for $C P$ violation measurements [11], and $\psi(2 S) \rightarrow \pi^{+} \pi^{-} J / \psi$ is often used to determine the total number of $\psi(2 S)$ events in $\psi(2 S)$ branching fraction measurements due to its large branching fraction and straightforward detection. Therefore, it is important to measure these decay widths and branching fractions with better accuracy.

Twenty four center-of-mass energy points were scanned in the vicinity of the $\psi(2 S)$ peak ranging from 3.67 GeV to 3.71 GeV . The data were collected with the BESII (BEijing Spectrometer) detector at the BEPC (Beijing Electron Positron Collider) storage ring. The BESII detector is described in detail in Ref. 12]. In addition, separated-beam data were taken at the first and the last points for background studies. The total integrated luminosity was $1149 \mathrm{nb}^{-1}$.

## 2. Event selection

The following four reactions are studied:

$$
\begin{array}{ll}
e^{+} e^{-} & \rightarrow e^{+} e^{-} \\
e^{+} e^{-} & \rightarrow \mu^{+} \mu^{-} \\
e^{+} e^{-} & \rightarrow \pi^{+} \pi^{-} J / \psi \\
e^{+} e^{-} & \rightarrow \text { hadrons }
\end{array}
$$

For the selection of lepton-pair final states, two charged tracks with total charge zero are required. For $\mu^{+} \mu^{-}$events, the acollinearity must be less than 10 degrees. In addition, in order to suppress cosmic ray background, the time-of-flight measurements of the two muon-candidates must satisfy $\sqrt{\left(t_{1}-5\right)^{2}+\left(t_{2}-5\right)^{2}}<4.5(\mathrm{~ns})$, as shown

[^0]in Fig. 11. Further, the Muon Counter(MUC) hit information is used to identify di-muon events from other back-to-back two-prong final states, and this requires $\left|\cos \theta_{\mu}\right| \leq 0.65$ due to the limited solid angle coverage.

To separate electrons from muons and hadrons, the energies deposited by the two tracks in the Barrel Shower Counter (BSC) must satisfy $\sqrt{\left(\tilde{E}_{d e p ~} 1-1\right)^{2}+\left(\tilde{E}_{d e p} 2-1\right)^{2}}<0.65$, where $\tilde{E}_{\text {dep }}=\frac{E_{\text {dep }}}{E_{\text {beam }}}$ is the normalized energy deposited. We also require $\left|\cos \theta_{e}\right| \leq 0.72$, and because the Monte Carlo simulation does not model the energy deposited well in the rib region of the BSC, an additional cut is applied on the $z$-coordinate of the first hit layer: $0.03<\left|z_{s c}\right|<0.85$ or $\left|z_{s c}\right|>0.95 \mathrm{~m}$.


Figure 1. Times of flight for $\mu$-pairs. The diagonal bands are due to cosmic ray events. Good events, which cluster at the center of the plot are selected with the circle cut shown.

A potential source of background is leptonpairs coming from $\psi(2 S) \rightarrow X J / \psi, J / \psi \rightarrow l^{+} l^{-}$. To eliminate this background, we make cuts on the track momenta, as shown in Fig. 2 (13].

Using the above criteria to select $\mu^{+} \mu^{-}$and $e^{+} e^{-}$events, we have compared various distributions with Monte Carlo distributions. Good

Table 1
$\psi(2 S)$ decay widths and branching ratios

| Expt. | yr. | $\Gamma_{t}$ <br> $(\mathrm{keV})$ | $\Gamma_{h}$ <br> $(\mathrm{keV})$ | $\Gamma_{\mu}$ <br> $(\mathrm{keV})$ | $B(h a d)$ <br> $(\%)$ | $B(\mu \mu)$ <br> $\left(10^{-3}\right)$ | $B\left(\pi^{+} \pi^{-} J / \psi\right)$ <br> $(\%)$ | ref. <br> MARK I 75 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 75 | $228 \pm 56$ | $224 \pm 56$ | $2.1 \pm 0.3$ | $98.1 \pm 0.3$ | $9.3 \pm 1.6$ |  | $[2]$ |  |
| MARK I | 75 |  |  |  |  |  | $32 \pm 4$ | $[3]$ |
| SPEC | 75 |  |  |  |  | $8 \pm 3$ |  | $[4]$ |
| DASP | 79 | $202 \pm 57$ |  |  |  | $9.9 \pm 3.2$ | $36 \pm 6$ | $[5]$ |
| E760 | 92 | $306 \pm 39$ |  |  |  |  |  | $[6]$ |
| E760 | 97 |  |  |  |  | $8.3 \pm 0.86$ | $28.3 \pm 2.9$ | $[7]$ |
| BES | 02 | $252 \pm 37$ |  |  |  |  |  | $[8]$ |
| BABAR | 02 |  |  |  |  | $6.7 \pm 1.1$ |  | $[9]$ |
| PDG | 02 | $300 \pm 25$ |  |  | $98.1 \pm 0.3$ | $7.0 \pm 0.9$ | $30.5 \pm 1.6$ | $[10]$ |

agreement is found, as illustrated, for example, in Fig. 3 .

For hadron event selection, we are guided by our R-scan experience 14, 15. There is no particular event topology to require; instead we make cuts to reject major backgrounds: cosmic rays, beam-associated background, two-photon processes $\left(\gamma^{*} \gamma^{*}\right)$, mis-identified "hadron" events from QED processes of $e^{+} e^{-} \rightarrow l^{+} l^{-}, l=e$, $\mu, \tau$, and $e^{+} e^{-} \rightarrow \gamma \gamma$ followed by $\gamma$ conversion, etc. Events with at least two well reconstructed charged tracks are selected. The total energy deposited by an event in the BSC is required to be larger than $0.36 E_{\text {beam }}$, in order to suppress contamination from two-photon processes and beam associated background. Events with all tracks pointing to the same hemisphere in the $z$ direction are removed to suppress beam-associated background. For two-prong events, two additional cuts are applied to eliminate possible lepton pair background. The number of photons must be greater than one, and the acollinearity between two charged tracks must be greater than 10 degrees. The background from $\tau^{+} \tau^{-}$decay is difficult to distinguish from direct hadronic decay events, so the contribution from this source, $N_{\tau^{+} \tau^{-}}$, is estimated using $N_{\tau \tau}=L \cdot\left(\varepsilon_{\tau \tau} \cdot \sigma_{\tau \tau}\right)$, where $L$ is the integrated luminosity at each energy point, $\sigma_{\tau \tau}$ the QED production cross section at this energy point, and $\varepsilon_{\tau \tau}$ the acceptance of our hadron event selection criteria for $\tau^{+} \tau^{-}$ events. This is subtracted from the observed
number of hadrons. A similar subtraction is performed for the other surviving backgrounds, such as $e^{+} e^{-} \rightarrow e^{+} e^{-}, \mu^{+} \mu^{-}, \gamma \gamma$, and two-photon process $\left(\gamma^{*} \gamma^{*}\right)$. Therefore, the corrected number of hadron events, $N_{h}^{o b s}$, is

$$
N_{h}^{o b s}=N_{h}-N_{\tau \tau}-N_{e e}-N_{\mu \mu}-N_{\gamma \gamma}-N_{\gamma^{*} \gamma^{*}}
$$

where $N_{h}$ is the number of events that satisfy the hadron selection cuts.

For the selection of $\psi(2 S) \rightarrow \pi^{+} \pi^{-} J / \psi$ events, we select a pair of low energy pions and determine the mass recoiling against these two pions, $m_{\text {recoil }}$, which shows a strong $J / \psi$ peak, corresponding to the decay $\psi(2 S) \rightarrow \pi^{+} \pi^{-} J / \psi$. The $m_{\text {recoil }}$ distribution is fitted with a signal shape plus polynomial background to obtain the number of $\psi(2 S) \rightarrow \pi^{+} \pi^{-} J / \psi$ events at each energy point. The very clean $\psi(2 S) \rightarrow \pi^{+} \pi^{-} J / \psi$, $J / \psi \rightarrow l^{+} l^{-}$channel is used to determine the signal shape. The inclusive $m_{\text {recoil }}$ distribution for all 24 energy points combined is shown in Fig. 4. For more detail, see Ref. [16]. The numbers of events selected for the four final states at the 24 energies are listed in Table 2.

## 3. Acceptance

The acceptance is the product of the trigger efficiency and the reconstruction-selection efficiency. The triggers are the same as those used in our $R$ scan experiment 14, The trigger efficiencies, measured by comparing the responses


Figure 2. Momentum distributions for (a) $e^{+} e^{-}$ events and (b) $\mu^{+} \mu^{-}$events. The solid line indicates the cuts applied to remove background from $\psi(2 S) \rightarrow X J / \psi, J / \psi \rightarrow l^{+} l^{-}$[13].


Figure 3. Normalized momentum distributions for (a) $e^{+} e^{-}$events and (b) $\mu^{+} \mu^{-}$events. (Histogram for M.C. and dots with error bar for Data)
to different trigger requirements in special runs taken at the $J / \psi$ resonance, are determined to be $1.000,0.994$ and 0.998 for $e^{+} e^{-}, \mu^{+} \mu^{-}$and hadronic events respectively, with an uncertainty of 0.005 .

Different generators are used to determine the reconstruction-selection efficiencies. For $e^{+} e^{-}$ and $\mu^{+} \mu^{-}$final states, the efficiencies for QED processes are determined in simulations with the BHABHA and MUPAIR generators 17. The resonance $e^{+} e^{-}$and $\mu^{+} \mu^{-}$efficiencies are determined using the generator V2LL, adapted from MUPAIR, with the initial state radiative correc-


Figure 4. Mass recoiling against $\pi^{+} \pi^{-}$for all 24 energy points combined. The $J / \psi$ peak is due to the signal $\psi(2 S) \rightarrow \pi^{+} \pi^{-} J / \psi, J / \psi \rightarrow$ anything events.
tions removed. For the hadronic processes, an event generator for charmonium inclusive decay [18] is used to obtain the efficiency for the resonance portion, and the JETSET string fragmentation algorithm with parameters modified to fit the experimental data in the BEPC energy region 19 is used to compute the efficiency for the continuum portion. For the $\pi^{+} \pi^{-} J / \psi$ acceptance, a phase space Monte Carlo program, modified to give the correct dipion mass and angular distributions 20], is used.

The acceptances of the four final states for continuum $\left(A^{c}\right)$ and resonance $\left(A^{r}\right)$ processes, together with their relative errors, are listed in Table 3. Here the acceptance for the $e^{+} e^{-}$final state in the table applies to events within a restricted solid angle $\left(\left|\cos \theta_{e}\right| \leq 0.72\right)$, whereas those of the hadron and dimuon final states cover all solid angles. The acceptance error includes the uncertainties estimated by varying selection cuts and using different selection methods and Monte Carlo models.

Table 2
Numbers of events selected.

| $E_{c m}$ | Selected number of events |  |  |  |
| :---: | ---: | ---: | ---: | ---: |
| $(\mathrm{GeV})$ | $N_{e e}^{\text {obs }}$ | $N_{\mu \mu}^{\text {obs }}$ | $N_{h}^{\text {obs }}$ | $N_{\pi \pi J / \psi}$ |
| 3.6668 | 1789 | 110 | 385 | 7.2 |
| 3.6719 | 1752 | 92 | 389 | 10.2 |
| 3.6750 | 1734 | 124 | 391 | 22.3 |
| 3.6781 | 1783 | 102 | 437 | 0.0 |
| 3.6801 | 1771 | 66 | 485 | 12.8 |
| 3.6809 | 1909 | 104 | 588 | 14.2 |
| 3.6820 | 1790 | 91 | 764 | 75.0 |
| 3.6828 | 1773 | 86 | 1538 | 181.0 |
| 3.6832 | 1778 | 69 | 2662 | 426.1 |
| 3.6836 | 1852 | 79 | 4178 | 668.0 |
| 3.6844 | 1774 | 92 | 8169 | 1508.0 |
| 3.6850 | 1845 | 128 | 14684 | 2660.8 |
| 3.6855 | 1720 | 140 | 15073 | 2758.1 |
| 3.6863 | 1703 | 191 | 15621 | 2902.6 |
| 3.6867 | 1715 | 176 | 14980 | 2572.0 |
| 3.6875 | 1711 | 161 | 11658 | 2201.8 |
| 3.6882 | 1758 | 175 | 7047 | 1245.1 |
| 3.6886 | 1738 | 125 | 4960 | 868.9 |
| 3.6893 | 2183 | 188 | 3964 | 707.4 |
| 3.6908 | 1805 | 113 | 1897 | 269.0 |
| 3.6939 | 1989 | 97 | 1318 | 128.8 |
| 3.6979 | 1926 | 132 | 1029 | 82.6 |
| 3.7017 | 1884 | 118 | 876 | 77.2 |
| 3.7068 | 1942 | 120 | 729 | 26.5 |
| sum | 43624 | 2879 | 113823 | 19425.4 |
|  |  |  |  |  |

## 4. Fit of observed cross sections and results

The $e^{+} e^{-} \rightarrow$ hadrons, $\pi^{+} \pi^{-} J / \psi, e^{+} e^{-}$, and $\mu^{+} \mu^{-}$events at the 24 scan points are fitted simultaneously to obtain the partial widths of $\psi(2 S)$ to hadrons, $\pi^{+} \pi^{-} J / \psi$, and $\mu^{+} \mu^{-}$final states. The total width is assumed to be the sum of four partial widths, $\Gamma_{t}=\Gamma_{h}+\Gamma_{\mu}+\Gamma_{e}+\Gamma_{\tau}$, and lepton universality is assumed $\mid$, $\Gamma_{e}=\Gamma_{\mu}=$
${ }^{\dagger}$ BES collaboration has measured the branching fraction of $\psi(2 S)$ decay into $\tau^{+} \tau^{-}$. This value along with those of the branching fractions in $e^{+} e^{-}$and $\mu^{+} \mu^{-}$, satisfies the relation predicted by the sequential lepton hypothesis within errors 8 .

Table 3
Acceptances for continuum, $A^{c}$, and the resonance, $A^{r}$.

| final state | $e^{+} e^{-}$ | $\mu^{+} \mu^{-}$ | Had | $\pi \pi J / \psi$ |
| :---: | :---: | :---: | :---: | :---: |
| $A^{c}(\%)$ | 72.4 | 37.1 | 74.5 | - |
| $\delta A^{c} / A^{c}(\%)$ | 3.2 | 5.0 | 7.1 | - |
| $A^{r}(\%)$ | 76.4 | 41.9 | 77.1 | 43.4 |
| $\delta A^{r} / A^{r}(\%)$ | 8.5 | 4.7 | 2.2 | 3.4 |

$\Gamma_{\tau} / 0.38847$. A likelihood function incorporating correlations due to luminosities and acceptances is constructed 21 and maximized using the MINUIT package [22] to give the best estimates for $\psi(2 S)$ parameters and their uncertainties. The theoretical cross section used in the fit for the hadron channel uses a Breit-Wigner amplitude and a non-resonant direct-channel amplitude plus a $J / \psi$ resonance "tail" cross section, as determined by a previous BES $J / \psi$ scan experiment [23]. The contributions from $\psi(2 S)$ decay into $e^{+} e^{-}, \mu^{+} \mu^{-}, \tau^{+} \tau^{-}$final states mis-identified as hadron events have been taken into account by correcting the resonant hadron event acceptanceff. For the $\pi^{+} \pi^{-} J / \psi$ final state, only a resonant Breit-Wigner amplitude is considered. In the $\mu^{+} \mu^{-}$channel, the $\psi(2 S)$ resonant term, QED term, and their interference are included. The radiative corrections to these three processes are taken into account by the formulation of Refs. (24] and [25]. For the $e^{+} e^{-}$final state, where the QED $t$-channel photon exchange also contributes, a theoretical cross section including radiative corrections is derived using the method of Ref. [26]. The effects on lepton-pair final state cross sections coming from vacuum polarization are also taken into consideration [27]; while for hadronic final states, the vacuum polarization is absorbed into the definition of $\Gamma_{e e}$, that is

$$
\begin{gathered}
\Gamma_{\exp }\left(\psi(2 S) \rightarrow e^{+} e^{-}\right)= \\
\Gamma_{0}\left(\psi(2 S) \rightarrow e^{+} e^{-}\right) \cdot \frac{1}{\left|1-\prod\left(M_{\psi(2 S)}^{2}\right)\right|^{2}},
\end{gathered}
$$

where $\Gamma_{\text {exp }}$ is the experimental width, $\Gamma_{0}$ the low-

[^1]est order in $\alpha$ width, and $\Pi$ the order $\alpha$ vacuum polarization [28]. The theoretical cross sections are convoluted with the energy distribution of the colliding beams, which is treated as Gaussian. The following parameters are allowed to vary in the fit: the $\psi(2 S)$ mass, $M$, the total width, $\Gamma_{t}$, the partial widths, $\Gamma_{\pi^{+} \pi^{-} J / \psi}$ and $\Gamma_{\mu}$, the energy spread of the machine, and the nonresonant hadronic cross section.

As the branching fraction of $\psi(2 S)$ to $e^{+} e^{-}$is small, the cross section for the $e^{+} e^{-}$final state is dominated by the QED process. Therefore this channel is used to calculate the integrated luminosity at each energy point by an iterative method. First, all $e^{+} e^{-}$events within $|\cos \theta| \leq$ 0.72 are taken as "Bhabha" events and used to calculate the integrated luminosity at each energy point. A maximum likelihood fit is performed to the observed cross sections for hadron, $\pi^{+} \pi^{-} J / \psi$, and muon pair final states, and a group of $\psi(2 S)$ parameters is obtained with the assumption of $e-\mu-\tau$ universality. Then, separating the $e^{+} e^{-}$ events into a QED part, a resonance part and their interference, the integrated luminosity for each energy point is recalculated using the QED part only, and the fitting procedures are redone to get new values for the $\psi(2 S)$ parameters. The iterative process is repeated until the value of the integrated luminosity at each energy point is consistent for two successive iterations.
The fitted curves are shown along with the scan points in Fig. 5 . The fitted mass of the $\psi(2 S)$ is corrected to the PDG value 10]. The errors in the other parameters caused by this correction are negligible. The fitted spread in the center-of-mass energy of the machine is $(1.298 \pm 0.007) \mathrm{MeV}$, in agreement with the expectation ( $\sim 1.3 \mathrm{MeV}$ ). The resultant $R$ ratio for the hadronic cross section near the $\psi(2 S)$ resonance is $2.15 \pm 0.16$, which agrees well with the earlier BES $R$ measurements (15].
The results of the fit for decay widths and branching fractions are given in Table $\AA$, together with corresponding PDG 10 values for comparison. The errors are the sum in quadrature of statistical, fitting, and systematic uncertainties, including those from acceptance uncertainties and a center-of-mass energy uncertainty of


Figure 5. The cross section for (a) $e^{+} e^{-} \rightarrow$ hadrons, (b) $e^{+} e^{-} \rightarrow \pi^{+} \pi^{-} J / \psi$, and (c) $e^{+} e^{-} \rightarrow$ $\mu^{+} \mu^{-}$versus center-of-mass energy. The solid curves represent the results of the fit to the data.
0.10 MeV 30]. For $\mathcal{B}_{h}, \mathcal{B}_{\pi \pi J / \psi}$, and $\mathcal{B}_{\mu}$, the error related to the luminosity measurement cancels out.

As a check of the fitting procedure, $\mathcal{B}_{\pi \pi J / \psi}$ was also determined by a simpler approach. In this approach, the distribution of $N_{h}^{\text {obs }}$ versus energy was fit with the shape determined from $N_{\pi \pi J / \psi}$ versus scan energy plus a polynomial to represent the continuum process to determine the number of hadrons coming from $\psi(2 S)$ decays. Using the ratio of the total number of $N_{\pi \pi J / \psi}$ events corrected by their detection efficiency and the number of $\psi(2 S)$ hadronic decays corrected by their detection efficiency, we directly determine $\mathcal{B}_{\pi \pi J / \psi}$, which agrees very well with the result from the full fitting procedure.

The assumption that lepton pairs couple to the $\psi(2 S)$ only via an intermediate photon 29] implies the existence of the decay $\psi(2 S) \rightarrow \gamma \rightarrow$

Table 4
Results and comparison with the PDG2002 10.

| Value | BES | PDG2002 |
| :---: | :---: | :---: |
| $\Gamma_{t}(\mathrm{keV})$ | $264 \pm 27$ | $300 \pm 25$ |
|  | $(10.1 \%)$ | $(8.3 \%)$ |
| $\Gamma_{h}(\mathrm{keV})$ | $258 \pm 26$ |  |
|  | $(10.1 \%)$ |  |
| $\Gamma_{\pi \pi J / \psi}(\mathrm{keV})$ | $85.4 \pm 8.7$ |  |
|  | $(10.1 \%)$ |  |
| $\star \Gamma_{\mu}(\mathrm{keV})$ | $2.44 \pm 0.21$ |  |
|  | $(8.8 \%)$ |  |
| $\mathcal{B}_{h}(\%)$ | $97.79 \pm 0.15$ | $98.10 \pm 0.30$ |
|  | $(0.16 \%)$ | $(0.31 \%)$ |
| $\mathcal{B}_{\pi \pi J / \psi}(\%)$ | $32.3 \pm 1.4$ | $30.5 \pm 1.6$ |
|  | $(4.4 \%)$ | $(5.2 \%)$ |
| $\mathcal{B}_{\mu}(\%)$ | $0.93 \pm 0.08$ | $0.7 \pm 0.09$ |
|  | $(8.5 \%)$ | $(12.9 \%)$ |

Note : The numbers in parenthesis denote the relative errors; $\star$ value given with assumption $\Gamma_{e}=\Gamma_{\mu}$.
hadrons with a branching fraction:

$$
\Gamma_{\gamma h} / \Gamma_{t}=R \Gamma_{\mu} / \Gamma_{t}=0.0199 \pm 0.0019
$$

which corresponds to a width $\Gamma_{\gamma h}$ of $5.26 \pm 0.32$ keV.

The $\psi(2 S)$ total decay width $\Gamma_{t}=264 \pm 27 \mathrm{keV}$ obtained in this measurement agrees with the BES previous value of $(252 \pm 37 \mathrm{keV})$ [8], within the error. In addition, this is the first direct measurement to the decay width of $\psi(2 S) \rightarrow \pi^{+} \pi^{-} J / \psi$, and the precision of $B_{\pi^{+} \pi^{-} J / \psi}$ is much better than previous measurements and the current PDG value.

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13. The track momenta are required to satisfy the following requirements:

$$
\begin{aligned}
& \tilde{p}_{1} \geq 0.95, \quad \text { or } \quad \tilde{p}_{2} \geq 0.95, \quad \text { or } \\
& \sqrt{\left(\tilde{p}_{1}-1\right)^{2}+\left(\tilde{p}_{2}-1\right)^{2}}<0.16,
\end{aligned}
$$

for an $e$-pair, where $\tilde{p}$ is the normalized momentum: $\tilde{p}=p / E_{\text {beam }}$. For a $\mu$-pair, the corresponding cut is:

$$
\text { P-cut. } 1 \cap(P \text {-cut. } 2 \cup P \text {-cut. } 3)
$$

where $P$-cut.1, P-cut.2, and P-cut. 3 are de-
fined as following:
P-cut.1: $\sqrt{\left(\frac{\tilde{p}_{1}-\tilde{p}_{2}}{0.35}\right)^{2}+\left(\frac{\tilde{p}_{1}+\tilde{p}_{2}-1.68}{0.125}\right)^{2}}>1$,
P-cut.2: $\quad\left(\tilde{p}_{1} \geq 0.9\right) \cap\left(\tilde{p}_{2} \geq 0.7\right)$,
P-cut.3: $\quad\left(\tilde{p}_{2} \geq 0.9\right) \cap\left(\tilde{p}_{2} \geq 0.7\right)$.
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[^1]:    ${ }^{\dagger}$ The contaminations from QED processes $e^{+} e^{-} \rightarrow l^{+} l^{-}$ have been already subtracted, see section 2 .

