# $\psi(2 S)$ two- and three-body hadronic decays 

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We report measurements of branching fractions for $\psi(2 S)$ decays into $\omega \pi^{+} \pi^{-}, b_{1} \pi, \omega f_{2}(1270)$, $\omega K^{+} K^{-}, \omega p \bar{p}, \phi \pi^{+} \pi^{-}, \phi f_{0}(980), \phi K^{+} K^{-}$, and an upper limit for $\phi p \bar{p}$ final states based on a data sample of $(4.02 \pm 0.22) \times 10^{6} \psi(2 S)$ events collected with the BESI detector at the Beijing Electron-Positron Collider. The branching fractions for $b_{1} \pi$ and $\omega f_{2}(1270)$ update previous BES results, while those for other decay modes are first measurements. The ratios of $\psi(2 S)$ and $J / \psi$ branching fractions are smaller than what is expected from the $12 \%$ rule by a factor of six for $\omega f_{2}(1270)$, by a factor of two for $\omega \pi^{+} \pi^{-}, \omega p \bar{p}$, and $\phi K^{+} K^{-}$, while for other studied channels the ratios are consistent with expectation within errors.

## I. INTRODUCTION

In perturbative QCD, the charmonium states, $J / \psi$ and $\psi(2 S)$, are considered to be non-relativistic bound states of charm and anticharm quarks, and their decays into light hadrons are expected to be dominated by the annihilation of the constituent $c$ and $\bar{c}$ quarks into three gluons. In this simple picture, the partial width for decays into any exclusive hadronic state $h$ is proportional to the wave function at the origin squared, $|\psi(0)|^{2}$, which is well determined from dilepton decays. Since the strong coupling constant $\alpha_{s}$ does not change much between the $J / \psi$ and $\psi(2 S)$ masses, it is reasonable to expect that, for any exclusive hadronic state $h$, the $J / \psi$ and $\psi(2 S)$ decay branching fractions will scale as (11)

$$
\frac{B(\psi(2 S) \rightarrow h)}{B(J / \psi \rightarrow h)} \simeq \frac{B\left(\psi(2 S) \rightarrow e^{+} e^{-}\right)}{B\left(J / \psi \rightarrow e^{+} e^{-}\right)} \simeq 12 \%
$$

where the leptonic branching fractions are taken from the PDG tables [2]. This relation is known as the " $12 \%$ rule". Although the rule works reasonably well for a number of specific decay modes, it fails severely in the case of the $\psi(2 S)$ two-body decays to the vectorpseudoscalar ( $V P$ ) meson final states, $\rho \pi$ and $K^{*} \bar{K}$ [3,4. This anomaly is commonly called the $\rho \pi$ puzzle. In addition, the BES group has reported violations of the $12 \%$ rule for vector-tensor ( $V T$ ) decay modes [5]. Although a number of theoretical explanations have been proposed to explain this puzzle [1].6], it seems that most of them do not provide a satisfactory solution.

In this paper, the measurements of the branching fractions of $\psi(2 S)$ decays into $\omega \pi^{+} \pi^{-}, b_{1} \pi, \omega f_{2}(1270)$, $\omega K^{+} K^{-}, \omega p \bar{p}, \phi \pi^{+} \pi^{-}, \phi f_{0}(980), \phi K^{+} K^{-}$, and $\phi p \bar{p}$ final states are presented. The results are compared with the corresponding $J / \psi$ branching fractions to test the $12 \%$ rule for these two-body and three-body hadronic decays.

## II. THE BES DETECTOR

The BEijing Spectrometer, BES, is a conventional cylindrical magnetic spectrometer that is coaxial with the colliding $e^{+} e^{-}$beams of the Beijing ElectronPositron Collider, BEPC. BESI is described in detail in ref. [7]. A four-layer central drift chamber (CDC) surrounding the beam pipe provides trigger information. Outside the CDC, the forty-layer main drift chamber (MDC) provides tracking and energyloss $(d E / d x)$ information on charged tracks over $85 \%$ of the total solid angle. The momentum resolution for charged tracks is $\sigma_{p} / p=0.017 \sqrt{1+p^{2}}(p$ in $\mathrm{GeV} / \mathrm{c})$, and the $d E / d x$ resolution for hadron tracks in these measurements is about $9 \%$. An array of 48 scintillation counters surrounding the MDC provides measurements of the time-of-flight (TOF) of charged tracks with a resolution of about 450 ps for hadrons. Outside the TOF system is a 12 radiation length thick leadgas barrel shower counter (BSC) that operates in selfquenching streamer mode and detects electrons and photons over $80 \%$ of the total solid angle. The BSC energy resolution is $\sigma_{E} / E=0.22 / \sqrt{E}(E$ in GeV$)$, and its spatial resolution for photons is $\sigma_{\phi}=4.5 \mathrm{mrad}$ and $\sigma_{\theta}=12 \mathrm{mrad}$. A solenoidal magnet surrounds the BSC and provides a 0.4 Tesla magnetic field in the central tracking region of the detector. Outside the solenoidal coil, there are three double layers of proportional chambers interspersed with the magnet flux return iron to identify muons of momentum greater than $0.5 \mathrm{GeV} / \mathrm{c}$.

## III. EVENT SELECTION

## A. Data sample and event topologies

The data sample used for this analysis consists of $(4.02 \pm 0.22) \times 10^{6} \psi(2 S)$ events collected with BES/BEPC at the center-of-mass energy $\sqrt{s}=$ $M_{\psi(2 S)}$. The decay channels investigated are $\psi(2 S)$ into $\omega \pi^{+} \pi^{-}, b_{1} \pi, \omega f_{2}(1270), \omega K^{+} K^{-}, \omega p \bar{p}, \phi \pi^{+} \pi^{-}$,
$\phi f_{0}(980), \phi K^{+} K^{-}$, and $\phi p \bar{p}$ final states, where $b_{1}$ decays to $\omega \pi, \omega$ to $\pi^{+} \pi^{-} \pi^{0}, \phi$ to $K^{+} K^{-}$, and $f_{2}(1270)$ and $f_{0}(980)$ to $\pi^{+} \pi^{-}$. They are all four-prong events or four-prong plus two photon events.

## B. Photon and charged particle identification

A neutral cluster is considered to be a photon candidate if the following requirements are satisfied: it is located within the BSC fiducial region $(|\cos \theta|<0.8)$, the energy deposited in the BSC is greater than 50 MeV , the first hit appears in the first 6 radiation lengths, the angle in the $x y$ plane (perpendicular to beam direction) between the cluster and the nearest charged track is greater than $16^{\circ}$, and the angle between the cluster development direction in the BSC and the photon emission direction from the beam interaction point (IP) is less than $37^{\circ}$. With these criteria applied to the $\psi(2 S) \rightarrow \pi^{+} \pi^{-} p \bar{p}$ sample selected by four-constraint (4C) kinematic fitting, less than $20 \%$ of events have photon candidates, which indicates an adequate fake-photon rejection (see Fig. 11).


FIG. 1. The distribution of the number of photon candidates found in kinematically selected $\psi(2 S) \rightarrow \pi^{+} \pi^{-} p \bar{p}$ events.

Each charged track is required to be well fit by a three-dimensional helix, to originate from the IP region, $V_{x y}=\sqrt{V_{x}^{2}+V_{y}^{2}}<2 \mathrm{~cm}$ and $\left|V_{z}\right|<20 \mathrm{~cm}$, and to have a polar angle $|\cos \theta|<0.8$. Here $V_{x}, V_{y}$, and $V_{z}$ are the $\mathrm{x}, \mathrm{y}$, and z coordinates of the point of closest approach to the beam axis. The time of flight (TOF) and $d E / d x$ measurements for each charged track are used to calculate $\chi^{2}$ values for the hypotheses that a track is a pion, kaon, or proton, for the purpose of particle identification.

## C. Monte Carlo simulations

Phase space Monte Carlo (MC) event generators and the BES detector simulation package, SOBER (7], are used for simulating events for all channels analyzed. To determine detection efficiencies, MC generated events are subjected to the same reconstruction
and event selection criteria as those applied to the real data. For each channel, $30,000 \mathrm{MC}$ events are generated.

## D. Event selection criteria

For all analyzed decay channels, the candidate events are required to satisfy the following general selection criteria:

1. The number of charged particles must be equal to four with net charge zero.
2. The number of photon candidates must be equal to or greater than two for the decay channels containing $\pi^{0}$.
3. For each charged track in an event, the $\chi_{P I D}^{2}(i)$ and its corresponding $\operatorname{Prob}_{P I D}(i)$ values are calculated based on the measurements of $d E / d x$ in the MDC and the time of flight in the TOF, with definitions

$$
\begin{gathered}
\chi_{P I D}^{2}(i)=\chi_{d E / d x}^{2}(i)+\chi_{T O F}^{2}(i) \\
\operatorname{Prob}_{P I D}(i)=\operatorname{Prob}\left(\chi_{P I D}^{2}(i), n d f_{P I D}\right),
\end{gathered}
$$

where $n d f_{P I D}=2$ is the number of degrees of freedom in the $\chi_{P I D}^{2}(i)$ determination and $\operatorname{Prob}_{P I D}(i)$ signifies the probability of this track having a particle $i$ assignment. For final states containing $p \bar{p}$, we require at least one of the charged tracks satisfy $\operatorname{Prob}_{P I D}(p / \bar{p})>0.01>$ $\operatorname{Prob}_{P I D}(\pi / K)$, while for other channels analyzed, the probability of a charged track for a candidate particle assignment is required to be greater than 0.01 .
4. A 4C (4 prong events) or 5C (4 prong plus two photon events) kinematic fit is performed for each event. To be selected for any candidate final state, the event probability given by the fit must be greater than 0.01 .
5. The combined $\chi^{2}, \chi_{\text {com }}^{2}$, is defined as the sum of the $\chi^{2}$ values of the kinematic fit and those from each of the four particle identification assignments:

$$
\chi_{c o m}^{2}=\sum_{i} \chi_{P I D}^{2}(i)+\chi_{k i n e}^{2}
$$

which corresponds to the combined probability:

$$
\operatorname{Prob}_{c o m}=\operatorname{Prob}\left(\chi_{c o m}^{2}, n d f_{c o m}\right)
$$

where $n d f_{\text {com }}$ is the corresponding total number of degrees of the freedom in the $\chi_{\text {com }}^{2}$ determination. The final state with the largest $\operatorname{Prob}_{\text {com }}$ is taken as the candidate assignment for each event.
6. A cut on $R_{E p}$ is imposed to reject possible contamination from $\psi(2 S) \rightarrow \pi^{+} \pi^{-} J / \psi$ and $\eta J / \psi$, with $J / \psi \rightarrow e^{+} e^{-}$, where

$$
R_{E p}=\left(\frac{E_{s c}^{+}}{p_{+}}-1\right)^{2}+\left(\frac{E_{s c}^{-}}{p_{-}}-1\right)^{2}
$$

and $p_{+}\left(p_{-}\right)$is the momentum of positive (negative) charged track measured with the MDC, and $E_{s c}^{+}\left(E_{s c}^{-}\right)$is the energy deposited in the BSC by the positive (negative) charged track.
7. Hit information from the muon chambers is used to reject possible muon tracks to reduce contamination from $\psi(2 S) \rightarrow \pi^{+} \pi^{-} J / \psi$ and $\eta J / \psi$, where $J / \psi \rightarrow \mu^{+} \mu^{-}$.

$$
\text { 1. } \psi(2 S) \rightarrow \omega p \bar{p}
$$

The combined probability for the assignment of $\psi(2 S) \rightarrow \pi^{+} \pi^{-} \pi^{0} p \bar{p}$ is required to be larger than those of $\psi(2 S) \rightarrow \pi^{+} \pi^{-} \pi^{0} \pi^{+} \pi^{-}$and $\psi(2 S) \rightarrow$ $\pi^{+} \pi^{-} \pi^{0} K^{+} K^{-}$. We impose a cut of $\mid m_{\text {recoil }}^{\pi^{+}-}$ $m_{J / \psi} \mid>0.05 \mathrm{GeV}$ to reject backgrounds from $\psi(2 S) \rightarrow \pi^{+} \pi^{-} J / \psi$, where $m_{\text {recoil }}^{\pi^{+} \pi^{-}}$is the mass recoiling against the assigned $\pi^{+} \pi^{-}$pair. A requirement of $m_{p \bar{p}}<m_{\psi(2 S)}-m_{\omega}=2.9 \mathrm{GeV}$ is applied to reject the backgrounds from $\psi(2 S) \rightarrow \eta J / \psi \rightarrow \pi^{+} \pi^{-} \pi^{0} p \bar{p}$ and $\pi^{+} \pi^{-} \pi^{0} \mu^{+} \mu^{-}$. Possible background could come from the decay of $\psi(2 S) \rightarrow \pi^{0} \pi^{0} J / \psi, J / \psi \rightarrow p \bar{p} \pi^{+} \pi^{-}$, where one of the $\pi^{0} \mathrm{~s}$ is missed in the BES detector. However, MC simulation shows that after our selection criteria, the $\pi^{+} \pi^{-} \pi^{0}$ system from this process has a negligible contribution in the $\omega$ mass region. Also, due to the tiny branching fraction, the contamination from the decay of $\psi(2 S) \rightarrow \pi^{0} J / \psi, J / \psi \rightarrow \pi^{+} \pi^{-} p \bar{p}$ is negligible.

The $\pi^{+} \pi^{-} \pi^{0}$ invariant mass distribution for the events that survive all selection requirements is shown in Fig. 2, where a clean $\omega$ signal can be seen. A BreitWigner resonance convoluted with Gaussian mass resolution function plus a polynomial background is fitted to the data using an unbinned maximum likelihood method. In the fit, the mass resolution is fixed to its MC-determined value, and the width of the $\omega$ is fixed to its PDG value. The fit gives $14.9 \pm 5.8$ signal events with statistical significance $2.6 \sigma$, and with the

MC-determined efficiency of $5.4 \%$, we determine the branching fraction

$$
B(\psi(2 S) \rightarrow \omega p \bar{p})=(0.8 \pm 0.3 \pm 0.1) \times 10^{-4}
$$

where the first error is statistical and the second error systematic. Determination of the systematic errors is described in section IV.


FIG. 2. The $\pi^{+} \pi^{-} \pi^{0}$ invariant mass distribution for candidate $\psi(2 S) \rightarrow \omega p \bar{p}$ events.

$$
\text { 2. } \psi(2 S) \rightarrow \omega K^{+} K^{-}
$$

For this channel, the final state $\left(\pi^{+} \pi^{-} \pi^{0} K^{+} K^{-}\right)$ is similar to that of the previous channel $\left(\pi^{+} \pi^{-} \pi^{0} p \bar{p}\right)$ except $p \bar{p}$ is replaced by $K^{+} K^{-}$. Therefore, similar selection criteria are imposed, but the combined probability for the assignment of $\psi(2 S) \rightarrow \pi^{+} \pi^{-} \pi^{0} K^{+} K^{-}$ must be larger than those of $\psi(2 S) \rightarrow \pi^{+} \pi^{-} \pi^{0} \pi^{+} \pi^{-}$ and $\psi(2 S) \rightarrow \pi^{0} K^{+} K^{-} K^{+} K^{-}$. A cut of $\mid m_{\text {recoil }}^{\pi^{+} \pi^{-}}$ $m_{J / \psi} \mid>0.05 \mathrm{GeV}$ is used to reject backgrounds from $\psi(2 S) \rightarrow \pi^{+} \pi^{-} J / \psi$. We require $m_{K^{+} K^{-}}<m_{\psi(2 S)}-$ $m_{\omega}=2.9 \mathrm{GeV}$ to reject backgrounds from $\psi(2 S) \rightarrow$ $\eta J / \psi \rightarrow \pi^{+} \pi^{-} \pi^{0} K^{+} K^{-}$. The contamination from the decay of $\psi(2 S) \rightarrow \pi^{0} J / \psi, J / \psi \rightarrow \pi^{+} \pi^{-} K^{+} K^{-}$ is negligible due to its tiny branching fraction. Although our selection criteria can not completely eliminate the contamination from $\psi(2 S) \rightarrow K_{s}^{0} K^{ \pm} \pi^{\mp} \pi^{0}$, $K_{s}^{0} \rightarrow \pi^{+} \pi^{-}$decay, the invariant mass distribution of $m_{\pi^{+} \pi^{-} \pi^{0}}$ from this background is smooth, and therefore it will not affect the determination of the signal events.


FIG. 3. The $\pi^{+} \pi^{-} \pi^{0}$ invariant mass distribution for candidate $\psi(2 S) \rightarrow \omega K^{+} K^{-}$events.

Figure 3 shows the $\pi^{+} \pi^{-} \pi^{0}$ invariant mass distribution for $\omega K^{+} K^{-}$candidates. The polynomial backgrounds include the contamination from $\psi(2 S) \rightarrow$ $K_{s}^{0} K^{ \pm} \pi^{\mp} \pi^{0}, K_{s}^{0} \rightarrow \pi^{+} \pi^{-}$. A fit gives $23.0 \pm 5.2$ signal events with a statistical significance of $6.3 \sigma$. The detection efficiency for this decay mode is $4.4 \%$, and we determine the branching fraction

$$
B\left(\psi(2 S) \rightarrow \omega K^{+} K^{-}\right)=(1.5 \pm 0.3 \pm 0.2) \times 10^{-4}
$$

$$
\text { 3. } \psi(2 S) \rightarrow \omega \pi^{+} \pi^{-}
$$

The candidate events for this decay mode have the final state $\pi^{+} \pi^{-} \pi^{0} \pi^{+} \pi^{-}$. To be selected, the combined probability for the assignment of $\psi(2 S) \rightarrow$ $\pi^{+} \pi^{-} \pi^{0} \pi^{+} \pi^{-}$must be larger than that of $\psi(2 S) \rightarrow$ $\pi^{+} \pi^{-} \pi^{0} K^{+} K^{-}$. A cut of $\left|m_{\text {recoil }}^{\pi^{+}-m^{-}}-m_{J / \psi}\right|>0.05 \mathrm{GeV}$ rejects the backgrounds from $\psi(2 S) \rightarrow \pi^{+} \pi^{-} J / \psi$, $J / \psi \rightarrow \pi^{+} \pi^{-} \pi^{0}$. We require $m_{\pi^{+} \pi^{-}}<m_{\psi(2 S)}-m_{\omega}=$ 2.9 GeV to reject the backgrounds from $\psi(2 S) \rightarrow$ $\eta J / \psi \rightarrow \pi^{+} \pi^{-} \pi^{0} \pi^{+} \pi^{-}$and $\pi^{+} \pi^{-} \pi^{0} \mu^{+} \mu^{-}$, where $m_{\pi^{+} \pi^{-}}$is the invariant mass of the $\pi^{+} \pi^{-}$against the $\omega$ determined by the kinematic fit. The contamination from the decay of $\psi(2 S) \rightarrow \pi^{0} J / \psi, J / \psi \rightarrow$ $\pi^{+} \pi^{-} \pi^{+} \pi^{-}$is negligible due to its tiny branching fraction.

Figure shows the the $\pi^{+} \pi^{-} \pi^{0}$ invariant mass distribution for $\omega \pi^{+} \pi^{-}$candidates, where the polynomial backgrounds contain the contamination from $\psi(2 S) \rightarrow K_{s}^{0} K^{ \pm} \pi^{\mp} \pi^{0}, K_{s}^{0} \rightarrow \pi^{+} \pi^{-}$. A fit gives $100 \pm 12$ signal events. The detection efficiency for this decay mode is $5.8 \%$, and we determine the branching fraction

$$
\begin{gathered}
B\left(\psi(2 S) \rightarrow \omega \pi^{+} \pi^{-}\right)=(4.8 \pm 0.6 \pm 0.7) \times 10^{-4} \\
\text { 4. } \psi(2 S) \rightarrow b_{1} \pi
\end{gathered}
$$

The dominant decay mode of the $b_{1}$ is $b_{1} \rightarrow \omega \pi$, and we assume its branching fraction is $100 \%$. Therefore, the final state for this mode is the same as for $\psi(2 S) \rightarrow \omega \pi^{+} \pi^{-}$. We use the same criteria as those for $\psi(2 S) \rightarrow \omega \pi^{+} \pi^{-}$to select candidate events, but an additional cut $\left|m_{\pi^{+} \pi^{-} \pi^{0}}-m_{\omega}\right|<0.03 \mathrm{GeV}$ is applied to select events containing the $\omega$ particle. The Dalitz
 left and in the bottom-right of the scatter plots (d) and (e) indicate a clear $b_{1}$ signal. Figure 6 shows the $\omega \pi$ invariant mass distribution for $b_{1} \pi$ candidates. In
the fit, the mass and width of the $b_{1}$ are fixed to the PDG values. A fit gives $61 \pm 11$ signal events. The detection efficiency for this decay mode is $5.2 \%$, and we determine the branching fraction

$$
B\left(\psi(2 S) \rightarrow b_{1} \pi\right)=(3.2 \pm 0.6 \pm 0.5) \times 10^{-4}
$$



FIG. 4. The $\pi^{+} \pi^{-} \pi^{0}$ invariant mass distribution for candidate $\psi(2 S) \rightarrow \omega \pi^{+} \pi^{-}$events.


FIG. 5. The Dalitz plot (a,d) for $\psi(2 S) \rightarrow \omega \pi^{+} \pi^{-}$ (data); (b,e) for $\psi(2 S) \rightarrow b_{1} \pi$ (MC); and (c,f) for $\psi(2 S) \rightarrow \omega f_{2}(1270)(\mathrm{MC})$ events, respectively.


FIG. 6. The $\omega \pi$ invariant mass distribution for candidate $\psi(2 S) \rightarrow b_{1} \pi$ events.

$$
\text { 5. } \psi(2 S) \rightarrow \omega f_{2}(1270)
$$

The final state for this decay mode is also the same as for $\psi(2 S) \rightarrow \omega \pi^{+} \pi^{-}$. We use the same criteria as those for $\psi(2 S) \rightarrow \omega \pi^{+} \pi^{-}$, but impose an additional cut $\left|m_{\pi^{+} \pi^{-} \pi^{0}}-m_{\omega}\right|<0.03 \mathrm{GeV}$ to select events containing an $\omega$ particle. A requirement of $\left|m_{\omega \pi}-m_{b_{1}}\right|>0.2 \mathrm{GeV}$ is applied to remove contamination from the $b_{1} \pi$ channel. Figure 7 shows the $\pi^{+} \pi^{-}$ invariant mass distribution for $\psi(2 S) \rightarrow \omega f_{2}(1270)$ candidates; it shows a visible bump in the $f_{2}(1270)$ mass region, in addition to the broad distribution in the lower mass region, which is presumably attributed to $f_{0}(400-1200)$ [8] production. A fit gives $10.2 \pm 4.9$ signal events with the mass and width of the $f_{2}$ (1270) fixed to its PDG values, the statistical significance is about $2.1 \sigma$. The detection efficiency for this decay mode is $4.8 \%$, and we determine the branching fraction

$$
B\left(\psi(2 S) \rightarrow \omega f_{2}(1270)\right)=(1.1 \pm 0.5 \pm 0.2) \times 10^{-4}
$$

or an upper limit of $1.5 \times 10^{-4}$ ( $90 \%$ C.L.).


FIG. 7. The $\pi^{+} \pi^{-}$invariant mass distribution for candidate $\psi(2 S) \rightarrow \omega f_{2}(1270)$ events.

$$
\text { 6. } \psi(2 S) \rightarrow \phi \pi^{+} \pi^{-}
$$

The candidate events for this decay mode have a final state $K^{+} K^{-} \pi^{+} \pi^{-}$. The combined probability for the assignment of $\psi(2 S) \rightarrow K^{+} K^{-} \pi^{+} \pi^{-}$ is required to be larger than those of $p \bar{p} \pi^{+} \pi^{-}$, $\pi^{+} \pi^{-} \pi^{+} \pi^{-}, K^{+} K^{-} K^{+} K^{-}$, and $K^{ \pm} \pi^{\mp} \pi^{+} \pi^{-}$. A cut of $\left|m_{\text {recoil }}^{\pi^{+} \pi^{-}}-m_{J / \psi}\right|>0.05 \mathrm{GeV}$ rejects possible backgrounds from $\psi(2 S) \rightarrow \pi^{+} \pi^{-} J / \psi$. The decay of $\psi(2 S) \rightarrow K^{*} K^{-} \pi^{+}(+c . c.) \rightarrow K^{+} K^{-} \pi^{+} \pi^{-}$has a smooth $m_{K^{+} K^{-}}$distribution below 1.06 GeV and therefore does not affect the $\phi \pi^{+} \pi^{-}$signal. No $K_{s}^{0}$ signal is found in the $m_{\pi^{+} \pi^{-}}$invariant mass distribution for the selected data sample, indicating negligible $K_{s}^{0} K^{ \pm} \pi^{\mp}$ background. Figure 8 shows the $K^{+} K^{-}$ invariant mass distribution for $\psi(2 S) \rightarrow \phi \pi^{+} \pi^{-}$candidates, where a prominent $\phi$ signal can be seen. A
fit gives $51.5 \pm 8.3$ signal events with the width of the $\phi$ fixed to its PDG value. The detection efficiency for this decay mode is $17.8 \%$, and we determine the branching fraction

$$
B\left(\psi(2 S) \rightarrow \phi \pi^{+} \pi^{-}\right)=(1.5 \pm 0.2 \pm 0.2) \times 10^{-4}
$$



FIG. 8. The $K^{+} K^{-}$invariant mass distribution for candidate $\psi(2 S) \rightarrow \phi \pi^{+} \pi^{-}$events.

$$
\text { 7. } \psi(2 S) \rightarrow \phi f_{0}(980)
$$

We use the same criteria as those for $\phi \pi^{+} \pi^{-}$for this decay mode, but with an additional requirement $\left|m_{K^{+} K^{-}}-m_{\phi}\right|<0.02 \mathrm{GeV}$ to select events containing a $\phi$ particle. The $\pi^{+} \pi^{-}$invariant mass distribution in Fig. 9 shows a clear $f_{0}(980)$ peak. A fit gives $18.4 \pm 6.4$ signal events with a width of about 45 MeV . The detection efficiency for this decay mode is $17.0 \%$, and we determine the branching fraction

$$
B\left(\psi(2 S) \rightarrow \phi f_{0}(980)\right) \cdot B\left(\phi f_{0}(980) \rightarrow \pi^{+} \pi^{-}\right)
$$

$$
=(0.6 \pm 0.2 \pm 0.1) \times 10^{-4}
$$



FIG. 9. The $\pi^{+} \pi^{-}$invariant mass distribution for candidate $\psi(2 S) \rightarrow \phi f_{0}(980)$ events.

$$
\text { 8. } \psi(2 S) \rightarrow \phi K^{+} K^{-}
$$

Here the combined probability for the assignment of $\psi(2 S) \rightarrow K^{+} K^{-} K^{+} K^{-}$is required to be larger than
those of $p \bar{p} K^{+} K^{-}, K^{+} K^{-} \pi^{+} \pi^{-}$, and $\pi^{+} \pi^{-} \pi^{+} \pi^{-}$. The $K^{+} K^{-}$invariant mass distribution in Fig. 10 shows a clear $\phi$ peak. A fit gives $16.1 \pm 5.0$ signal events with the width of the $\phi$ fixed to its PDG value. The detection efficiency for this decay mode is $13.4 \%$, and we determine the branching fraction

$$
B\left(\psi(2 S) \rightarrow \phi K^{+} K^{-}\right)=(0.6 \pm 0.2 \pm 0.1) \times 10^{-4}
$$



FIG. 10. The $K^{+} K^{-}$invariant mass distribution for candidate $\psi(2 S) \rightarrow \phi K^{+} K^{-}$events.

$$
\text { 9. } \psi(2 S) \rightarrow \phi p \bar{p}
$$

The combined probability for the assignment of $\psi(2 S) \rightarrow K^{+} K^{-} p \bar{p}$ is required to be larger than those of $p \bar{p} \pi^{+} \pi^{-}, K^{+} K^{-} K^{+} K^{-}$, and $\pi^{+} \pi^{-} \pi^{+} \pi^{-}$. The $K^{+} K^{-}$invariant mass plot is shown in Fig. 11. Only four events appear in the $\phi$ mass region. Assuming zero background events and using a detection efficiency of $16.8 \%$, we obtain the upper limit on the branching fraction of

$$
B(\psi(2 S) \rightarrow \phi p \bar{p})<0.26 \times 10^{-4} \quad(90 \% \quad \text { C.L. })
$$



FIG. 11. The $K^{+} K^{-}$invariant mass distribution for candidate $\psi(2 S) \rightarrow \phi p \bar{p}$ events.

## IV. BRANCHING FRACTION DETERMINATION

For a process $\psi(2 S) \rightarrow X$, the branching fraction is determined by the relation

$$
B(\psi(2 S) \rightarrow X)=
$$

$$
\frac{n^{o b s}(\psi(2 S) \rightarrow X \rightarrow Y)}{N_{\psi(2 S)} \cdot B(X \rightarrow Y) \cdot \epsilon(\psi(2 S) \rightarrow X \rightarrow Y)},
$$

where Y stands for the final state, X the intermediate state, and $\epsilon$ the detection efficiency. The branching fraction of $X \rightarrow Y$ is taken from the PDG [2]. The total number of $\psi(2 S)$ events $N_{\psi(2 S)}=(4.02 \pm 0.22) \times$ $10^{6}$ [9] is determined from the number of $\psi(2 S) \rightarrow$ $\pi^{+} \pi^{-} J / \psi$ events corrected for detection efficiency in the BES $\psi(2 S)$ data sample $(1.227 \pm 0.003 \pm 0.017 \times$ $10^{6}$ ) 10] and the PDG branching fraction [2].

## A. Efficiency Corrections and Systematic errors

Because the Monte Carlo does not simulate real events exactly, it is necessary to correct the detection efficiency for the difference that the PID selection has on data and MC events and for the difference that kinematic selection has on data and MC events because of differences in the track fit error matrix elements. To correct for the PID difference, the efficiency is multiplied by a factor ranging from 0.89 to 0.98 with an uncertainty of 0.04 to 0.07 , depending on channel; while the correction factor in kinematic fitting is $0.85 \pm 0.05$ and $0.88 \pm 0.08$ for 4 -prong and 4 -prong plus 2-photon final states, respectively 11].

Beside the uncertainties caused by the particle identification and the kinematic fitting stated above, a systematic error common to all decay modes is the uncertainty in the total number of $\psi(2 S)$ events ( $5.4 \%$ ). The uncertainties of the PDG values of the intermediate state $\omega, \phi, b_{1}, f_{2}(1270)$, and $f_{0}(980)$ decay branching fractions are also sources of systematic error ( $0.8 \%$ to $3.1 \%$ ). The systematic error due to the statistical precision of the MC event samples ranges from $1.2 \%$ to $3.2 \%$, depending on the decay channel. Difficulties in the simulation of low energy photons in the Monte Carlo give rise to a systematic error in the efficiency that varies from $4.5 \%$ to $8.6 \%$ depending on photon energy for the final states containing $\pi^{0}$. The systematic error from $\pi^{0} \rightarrow 2 \gamma$, where at least one photon is converted to a $e^{+} e^{-}$pair is about $1.4 \%$. The variation of branching fraction results for different choices of the fiducial region is about $5 \%$. The total systematic error is taken as the sum of the individual terms added in quadrature and ranges from $12 \%$ to $17 \%$, depending on the channel.

## B. Branching fraction results

The results, including numbers of signal events, detection efficiencies and branching fractions or upper
limits ( $90 \%$ C.L.), are summarized in Table in. The first error of the branching fraction is statistical and the second is systematic for each channel. Among these, the branching fractions for $\omega f_{2}(1270)$ and $b_{1}^{ \pm} \pi^{\mp}$ supersede previous BES results [5]; while all other branching fractions are first measurements for these decays. For $b_{1}^{ \pm} \pi^{\mp}$, the difference is due to an improved understanding of the acceptance; for $\omega f_{2}(1270)$, the difference is due to improved selection criteria to reduce background.

To test the $12 \%$ rule, we also list in Table il the ratio $Q_{h}$ of the $\psi(2 S)$ and $J / \psi$ branching fractions for each channel, where the $J / \psi$ branching fractions are taken from the PDG. Among these channels, the ratio of $\omega f_{2}(1270)$ (VT mode) is suppressed by a factor of six with respect to the PQCD expectation, and those of $\omega \pi^{+} \pi^{-}, \omega p \bar{p}$, and $\phi K^{+} K^{-}$are suppressed by about a factor of two, those of other channels are consistent with PQCD expectation within errors.

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TABLE I. Branching fractions of $\psi(2 S)$ and $Q_{h}$ values for $\psi(2 S)$ and $J / \psi$ hadronic decays.*

| Channel | Number of | Efficiency | $\frac{B_{\psi(2 S) \rightarrow X}}{B_{\psi(2 S) \rightarrow \pi+\pi-J / \psi}}$ | $B_{\psi(2 S) \rightarrow X}$ | $B_{J / \psi \rightarrow X}$ | $Q_{X}(\%)$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| X | Events | $(\%)$ | $\left(10^{-4}\right)$ | $\left(10^{-4}\right)$ | $\left(10^{-4}\right)$ | $(\%)$ |
| $\omega \pi^{+} \pi^{-}$ | $100 \pm 12$ | $5.8 \pm 0.8$ | $15.8 \pm 1.9 \pm 2.2$ | $4.8 \pm 0.6 \pm 0.7$ | $72.0 \pm 12.0$ | $6.7 \pm 1.7$ |
| $b_{1}^{ \pm} \pi^{\mp}$ | $61 \pm 11$ | $5.2 \pm 0.7$ | $10.6 \pm 1.9 \pm 1.5$ | $3.2 \pm 0.6 \pm 0.5$ | $30.0 \pm 5.0$ | $11 \pm 3$ |
| $\omega f_{2}(1270)$ | $10.2 \pm 4.9$ | $4.8 \pm 0.7$ | $3.4 \pm 1.7 \pm 0.5$ | $1.1 \pm 0.5 \pm 0.2$ | $43.0 \pm 6.0$ | $2.4 \pm 1.3$ |
|  |  |  |  | $<1.5$ |  |  |
| $\omega K^{+} K^{-}$ | $23.0 \pm 5.2$ | $4.4 \pm 0.6$ | $4.8 \pm 1.1 \pm 0.7$ | $1.5 \pm 0.3 \pm 0.2$ | $7.4 \pm 2.4$ | $20 \pm 8$ |
| $\omega p \bar{p}$ | $14.9 \pm 5.8$ | $5.4 \pm 0.8$ | $2.5 \pm 1.0 \pm 0.4$ | $0.8 \pm 0.3 \pm 0.1$ | $13.0 \pm 2.5$ | $6.0 \pm 2.8$ |
| $\phi \pi^{+} \pi^{-}$ | $51.5 \pm 8.3$ | $17.8 \pm 2.1$ | $4.8 \pm 0.8 \pm 0.6$ | $1.5 \pm 0.2 \pm 0.2$ | $8.0 \pm 1.2$ | $18 \pm 5$ |
| $\phi f_{0}(980)\left(f_{0} \rightarrow \pi^{+} \pi^{-}\right)$ | $18.4 \pm 6.4$ | $17.0 \pm 2.1$ | $1.8 \pm 0.6 \pm 0.2$ | $0.6 \pm 0.2 \pm 0.1$ |  |  |
| $\phi f_{0}(980)^{* *}$ |  |  | $3.4 \pm 1.2 \pm 0.4$ | $1.1 \pm 0.4 \pm 0.1$ | $3.2 \pm 0.9$ | $33 \pm 15$ |
| $\phi K^{+} K^{-}$ | $16.1 \pm 5.0$ | $13.4 \pm 1.6$ | $2.0 \pm 0.6 \pm 0.2$ | $0.6 \pm 0.2 \pm 0.1$ | $8.3 \pm 1.3$ | $7.3 \pm 2.6$ |
| $\phi p \bar{p}$ | 4 | $16.8 \pm 1.8$ | $<0.85$ | $<0.26$ | $8.3 \pm 1.3$ | $<58$ |
| $T \mathrm{~T}$ |  |  |  |  |  |  |

* The upper limit is at the $90 \%$ confidence level; $B_{J / \psi}$ taken from PDG value.
** $B_{f_{0} \rightarrow \pi^{+} \pi^{-}}=0.521 \pm 0.016\left(\mathrm{PDG}{ }^{\prime} 96\right)$

