# Optimization of NLC machine parameters for specific physics processes* 

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#### Abstract

We examine the optimization of NLC parameters at 500 , 1000 , and 1500 GeV c.m. energy for specific classes of physics processes, in particular, top and stop pair production, and $\mathrm{W}-\mathrm{W}$ scattering processes. Our focus is on optimizing the luminosity spectrum, while maintaining or improving machine operability.


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#### Abstract

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## 1 Introduction

The purpose of this paper is to look at the flexibility in optimizing the event rate for specific classes of physics processes in a future linear collider. We do not address the issue of detector backgrounds, other than to observe that increasing $n_{\gamma}$ (number of beamstrahlung photons per incoming particle) and $\Upsilon$ (the beamstrahlung parameter, which governs the rate of coherent pair production) much higher than the values in the present designs would substantially increase backgrounds in the detector. With this caveat, our working assumption is that when the total rate for the various processes considered is optimized, one will end up with a larger number of useful events even after appropriate cuts are applied to reduce backgrounds.

| Table 1: IP parameters for three $\sim 1 / 2 \mathrm{TeV}$ |  |  |  |  |  | c.m. and three $\sim 1 \mathrm{TeV}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  | c.m. NLC designs ${ }^{2}$ |  |  |  |  |  |
|  | A-500 | B-500 | C-500 | A-1000 | B-1000 | C-1000 |
| $E_{\text {beam }}[\mathrm{GeV}]$ | 267.5 | 257.5 | 250. | 523. | 504. | 489. |
| $\mathrm{~N}\left[10^{10}\right]$ | 0.75 | 0.95 | 1.1 | 0.75 | 0.95 | 1.1 |
| $\gamma \epsilon_{x} / \gamma \epsilon_{y}[\mu \mathrm{~m}-\mathrm{r}]$ | $4 . / 0.06$ | $4.5 / 0.1$ | $5 . / 0.14$ | $4 . / 0.06$ | $4.5 / 0.1$ | $5 . / 0.14$ |
| $\beta_{x} / \beta_{y}[\mathrm{~mm}]$ | $10 / 0.1$ | $12 / 0.12$ | $13 / 0.2$ | $10 / 0.125$ | $12 / 0.15$ | $13 / 0.2$ |
| $\sigma_{z}[\mu \mathrm{~m}]$ | 90. | 120. | 145. | 90. | 120. | 145. |
| $\sigma_{x} / \sigma_{y}[\mathrm{~nm}]$ | $276 / 3.4$ | $327 / 4.9$ | $365 / 7.6$ | $198 / 2.7$ | $234 / 3.9$ | $261 / 5.4$ |
| $\Upsilon_{\text {avg }}$ | 0.14 | 0.11 | 0.09 | 0.39 | 0.30 | 0.25 |
| $H_{D}$ | 1.36 | 1.30 | 1.49 | 1.50 | 1.44 | 1.50 |
| $n_{\gamma}$ | 1.08 | 1.18 | 1.24 | 1.39 | 1.53 | 1.62 |
| $\delta_{B}$ | $4.3 \%$ | $3.9 \%$ | $3.7 \%$ | $9.5 \%$ | $9.2 \%$ | $8.7 \%$ |
| Bunches $/ \mathrm{train}$ | 95 | 95 | 95 | 95 | 95 | 95 |
| Rep. rate | 120 | 120 | 120 | 120 | 120 | 120 |
| $L_{D} / 10^{33} / \mathrm{cm}^{2} / \mathrm{sec}$ | 7.42 | 6.66 | 5.94 | 14.33 | 12.95 | 11.67 |

We focus on processes whose cross sections are increasing over the energy ranges of interest; optimization for a sharp luminosity spectrum at the top threshold is addressed elsewhere at this conference ${ }^{1}$. One factor in maximizing the event rate is obviously to maximize the convolution of the cross section with the beamstrahlungdegraded luminosity spectrum. However, the difficulty of machine operation is an important factor in determining the event rates one will actually obtain. The
vertical spot size is very small in the nominal linear collider designs, which leads to tight vertical machine tolerances. Thus it is also of interest to see how one can relax these tolerances with minimal impact on the luminosity.

We present some interaction region parameters ${ }^{2}$ for the basic NLC designs near $0.5,1.0$, and 1.5 TeV c.m. energy in Tables 1 and 2 . The luminosities, the number of photons $n_{\gamma}$, and the average fractional beamstrahlung energy loss $\delta_{B}$ are obtained from simulations using the beam-beam code Guineapig ${ }^{3}$.

Note that the c.m. energy is assumed to decrease with higher bunch charge $N$ because the beam loading reduces the acceleration gradient in a given linac design; it is possible to compensate the loading by adding additional rf structures, but this increases the cost. There is also variation in other parameters among different design versions near a given energy. We have done systematic studies ${ }^{4}$ where we vary each of the parameters $N, \sigma_{z}, \beta_{x}, \beta_{y}, \gamma \epsilon_{y}$, or $\gamma \epsilon_{x}$. We find that the best "knobs" for increasing luminosity at the high energy end of the spectrum are $\gamma \epsilon_{y}$ and $N$. It is thought difficult to decrease $\gamma \epsilon_{y}$ much, but one may consider increasing $N$ if one is willing either to let the energy drop or compensate for the beam-loading.

One finding of these studies is that doubling $\beta_{y}$ (which relaxes vertical tolerances) does not reduce luminosity very much ${ }^{4}$. We have also examined designs ${ }^{5}$ with equal or near-equal beta functions (see Table 4) which increase the vertical spot size even further and can have much higher total luminosity if one is willing to allow rather high values of $n_{\gamma}$ and $\Upsilon$. To bring $n_{\gamma}$ and $\Upsilon$ down to more conventional values, we can reduce the bunch charge, sacrificing some of the luminosity gain. Note that in the last two designs in Table 4, we assume the bunch spacing is halved, the number of bunches doubled, and the charge per bunch decreased. The design with bunch charge $N=0.475 \times 10^{10}$ has the same beam loading as the nominal NLC-B-1000 design. The total luminosity of this design is comparable to the nominal NLC-B-1000 design but the spectrum is somewhat more degraded to lower energies ( $\delta_{B}=16 \%$ instead of $9 \%$ ). The design with $N=0.55 \times 10^{10}$ has higher luminosity, but it would be necessary to make up for increased beam loading if one wanted to keep the nominal c.m. energy the same.

We show the luminosity spectra for the nominal designs, with effects of both beamstrahlung and initial state radiation (ISR) included, in Table 3. The fractional luminosities are shown, e.g., $L_{99 \%}$ denotes the percentage of the luminosity with c.m. energy greater than or equal to $99 \%$ of the nominal c.m. energy. (These numbers are not significantly different for the $\mathrm{A}, \mathrm{B}$, and C variations of the designs at 500 and 1000 GeV .)

## 2 SUSY scalar production

We compare the rates of top and stop production in a $500-\mathrm{GeV}$ collider, assuming $m_{\tilde{t}}=m_{t}$. The total top and stop pair production cross-sections are plotted in Figure 1.

The production rates (\# events in a running year of $10^{7} \mathrm{sec}$ ) are shown in Table 5 for the three nominal designs near $500-\mathrm{GeV}$ c.m. energy, and also for designs with bunch charge $N$ pushed up from the nominal B- 500 design value. Here we

|  | Table 2: IP parameters for two | $\sim 1.5 \mathrm{TeV}$ c.m |
| :--- | ---: | ---: |
|  | $\mathrm{A}-1500$ | $\mathrm{~B}-1500$ |
| $E_{\text {beam }}[\mathrm{GeV}]$ | 703 | 739 |
| $\mathrm{~N}\left[10^{10}\right]$ | 1.4 | 0.95 |
| $\gamma \epsilon_{x} / \gamma \epsilon_{y}[\mu \mathrm{~m}-\mathrm{r}]$ | $4.5 / 0.14$ | $4.5 / 0.1$ |
| $\beta_{x} / \beta_{y}[\mathrm{~mm}]$ | $15 / 0.2$ | $13 / 0.2$ |
| $\sigma_{z}[\mu \mathrm{~m}]$ | 130. | 150. |
| $\sigma_{x} / \sigma_{y}[\mathrm{~nm}]$ | $222 / 4.5$ | $201 / 3.7$ |
| $\Upsilon_{\text {avg }}$ | 0.60 | 0.41 |
| $H_{D}$ | 1.61 | 1.50 |
| $n_{\gamma}$ | 2.2 | 1.7 |
| $\delta_{B}$ | $17 \%$ | $12 \%$ |
| Bunches $/$ train | 95 | 95 |
| Rep. rate | 60 | 90 |
| $L_{D} / 10^{33} / \mathrm{cm}^{2} / \mathrm{sec}$ | 14.3 | 12.3 |

Table 3: Fractional luminosities for NLC designs $\sim 500 \mathrm{GeV}$ designs $\sim 1000 \mathrm{GeV}$ designs $\quad 1500-\mathrm{A} \quad 1500-\mathrm{B}$

| beamst.+ISR: |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| $L_{99.5 \%}(\operatorname{sim})$ | $37 \%$ | $27 \%$ | $18 \%$ | $23 \%$ |
| $L_{99 \%}(\operatorname{sim})$ | $44 \%$ | $33 \%$ | $22 \%$ | $29 \%$ |
| $L_{98 \%}(\operatorname{sim})$ | $54 \%$ | $41 \%$ | $28 \%$ | $36 \%$ |
| $L_{95 \%}(\operatorname{sim})$ | $69 \%$ | $56 \%$ | $41 \%$ | $50 \%$ |
| $L_{90 \%}(\operatorname{sim})$ | $81 \%$ | $70 \%$ | $55 \%$ | $64 \%$ |
| $L_{80 \%}(\operatorname{sim})$ | $91 \%$ | $84 \%$ | $73 \%$ | $80 \%$ |
| $L_{50 \%}(\operatorname{sim})$ | $98 \%$ | $97 \%$ | $95 \%$ | $97 \%$ |

assume it is reasonable to compensate the extra beam loading to keep the energy fixed.

## 3 WW-scattering processes

The class of processes $e^{+} e^{-} \rightarrow \ell \ell X$ occurring via $W W$ scattering, where one or both $\ell$ 's is a neutrino and $X$ could be for example $t \bar{t}, W$ 's and/or $Z$ 's, have cross sections which rise with energy above threshold and through the TeV energy scale. Taking as a representative example the process $e^{+} e-\rightarrow \nu_{e} \bar{\nu}_{e} W^{+} W^{-}$, we show the number of events in $10^{7}$ seconds of running for designs near 1 TeV in Table 6 . In addition to the nominal $\mathrm{A}, \mathrm{B}$, and C designs, we show the increase in luminosity attainable with $\gamma \epsilon_{y}$ decreased from its nominal value of $0.1 \mu \mathrm{~m}-\mathrm{r}$, or with $N$ increased from its nominal value of $0.95 \times 10^{10}$, with and without compensation of the extra beam-loading. The biggest luminosity gains are obtained by increasing $N$ and keeping the energy fixed, or by going to equal or near-equal beta functions and keeping $N$ near its nominal

Table 4: IP parameters for $\sim 1.0 \mathrm{TeV}$ c.m. NLC designs, with equal or near-equal beta functions
$\left.\begin{array}{llllll} & \begin{array}{lll}\text { A-1000- } \\ \text { bx1by1 }\end{array} & \begin{array}{l}\text { B-1000- } \\ \text { bx1.3by1.3 }\end{array} & \begin{array}{l}\text { A-1000- } \\ \text { bx2.5by1 }\end{array} & \begin{array}{l}\text { B-1000- } \\ \text { bx1.3by1.3 } \\ \text { N.475-b190 }\end{array} & \begin{array}{l}\text { B-1000- } \\ \text { bx1.3by1.3 }\end{array} \\ \text { N.55-b190 }\end{array}\right]$
value; further study is needed to see how high $n_{\gamma}$ and $\Upsilon$ can be allowed to go. Note that there is only a $13 \%$ reduction in the number of events for the case where $\beta_{y}$ is doubled from its nominal value. Also, note that we can get event rates comparable to those for the nominal designs in the equal-beta, reduced charge-per-bunch designs B1000 -bx1.3by $1.3-\mathrm{N} .475-\mathrm{b} 190$ and B-1000-bx1.3by1.3-N.55-b190, which have greatly relaxed vertical tolerances. Similar trends hold for the designs near 1.5 TeV ; some examples are shown in Table 7.

Table 5: Number of top and stop pair production events in a $10^{7}$ second running year, for nominal designs near $1 / 2 \mathrm{TeV}$ c.m. (first three columns) and for modified B-500 design with increased $N$ and energy kept fixed (last three columns).

|  | $\mathrm{A}-500$ | $\mathrm{~B}-500$ | $\mathrm{C}-500$ | $\mathrm{~B}-\mathrm{N} 1.1$ | $\mathrm{~B}-\mathrm{N} 1.3$ | $\mathrm{~B}-\mathrm{N} 1.5$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $e_{L}^{-} e_{R}^{+} \rightarrow t \bar{t}$ | 785000 | 674000 | 581000 | 927000 | 1347000 | 1856000 |
| $e_{R}^{-} e_{L}^{+} \rightarrow t \bar{t}$ | 357000 | 305000 | 262000 | 420000 | 609000 | 837700 |
| $e_{L}^{-} e_{R}^{+} \rightarrow \tilde{t_{R}} \tilde{t_{R}}$ | 22000 | 17500 | 14200 | 23900 | 34000 | 46000 |
| $e_{R}^{-} e_{L}^{+} \rightarrow \tilde{t}_{R} \tilde{t_{R}}$ | 92000 | 74000 | 60200 | 101000 | 144000 | 195000 |
| $e_{L}^{-} e_{R}^{+} \rightarrow \tilde{t}_{L} \tilde{t_{L}}$ | 178000 | 143000 | 116500 | 195000 | 279000 | 377000 |
| $e_{R}^{-} e_{L}^{+} \rightarrow \tilde{t}_{L} \tilde{t_{L}}$ | 4900 | 3900 | 3200 | 5300 | 7600 | 10200 |

Table 6: Rate of events for designs near 1 TeV c.m., for the process $e^{+} e^{-} \rightarrow \nu \bar{\nu} W^{+} W^{-}$(assuming $M_{H}=100 \mathrm{GeV}$ and no polarization)

| No. of <br> events | \% change <br> B-1000 | $n_{\gamma}$ |
| :---: | :---: | :---: |
| 76000 | $+28 \%$ | 1.4 |
| 59300 | $0 \%$ | 1.5 |
| 48300 | $-19 \%$ | 1.6 |
|  |  |  |
| 68200 | $+15 \%$ | 1.5 |
| 80300 | $+35 \%$ | 1.5 |
| 102000 | $+73 \%$ | 1.5 |
|  |  |  |
| 81170 | $+37 \%$ | 1.8 |
| 114000 | $+92 \%$ | 2.0 |
| 152000 | $+157 \%$ | 2.3 |
|  |  |  |
| 72400 | $+22 \%$ | 1.8 |
| 84300 | $+42 \%$ | 2.0 |
| 92600 | $+56 \%$ | 2.3 |
|  |  |  |
| 123000 | $+107 \%$ | 4.7 |
| 95900 | $+62 \%$ | 5.1 |
| 70700 | $+19 \%$ | 2.6 |
|  |  |  |
| 51700 | $-13 \%$ | 1.5 |
|  |  |  |
| 44900 | $-24 \%$ | 2.2 |
| 61700 | $+4 \%$ | 2.7 |
|  |  |  |
| 130400 | $+120 \%$ | 2.3 |
| 71700 | $+21 \%$ | 2.2 |

$\mathrm{B}-1000, \beta_{y} \uparrow 0.30 \mathrm{~mm}, \mathrm{~N} \uparrow 1.5 \cdot 10^{10}, \mathrm{E} \downarrow 891 \mathrm{GeV} \quad 71700 \quad+21 \% \quad 2.2$

Table 7: Rate of events for designs near 1.5 TeV c.m., for the process $e^{+} e^{-} \rightarrow \nu \bar{\nu} W^{+} W^{-}$(assuming $M_{H}=100 \mathrm{GeV}$ and no polarization)

| No. of <br> events | $\%$ change <br> B-1500 | $\%$ change <br> B-1000 | $n_{\gamma}$ |
| :---: | :---: | ---: | :---: |
| 230000 | $-10 \%$ | $290 \%$ | 2.2 |
| 254000 | $0 \%$ | $330 \%$ | 1.7 |
| 345000 | $+36 \%$ | $480 \%$ | 2.0 |
| 483000 | $+90 \%$ | $710 \%$ | 2.3 |
| 646000 | $+154 \%$ | $990 \%$ | 2.6 |
| 235000 | $-8 \%$ | $300 \%$ | 1.7 |



Figure 1: Left-hand plot shows cross sections for $e_{L}^{-} e_{R}^{+} \rightarrow t \bar{t}$ (solid curve) and $e_{R}^{-} e_{L}^{+} \rightarrow t \bar{t}$ (dashed curve). Right-hand plot shows cross sections for $e_{L}^{-} e_{R}^{+} \rightarrow \tilde{t}_{R} \tilde{t_{R}}$ (dot-dashed curve), $e_{R}^{-} e_{L}^{+} \rightarrow \tilde{t}_{R} \tilde{t_{R}}$ (dotted curve), $e_{L}^{-} e_{R}^{+} \rightarrow \tilde{t_{L}} \tilde{t_{L}}$ (solid curve), $e_{R}^{-} e_{L}^{+} \rightarrow \tilde{t}_{L} \tilde{t_{L}}$ (dashed curve).

## Conclusions and Acknowledgments

The examples in this paper, representative of processes whose cross sections increase with energy, illustrate several approaches to increasing event rates beyond those which would be obtained in the nominal designs. The nominal designs appear to be fairly well optimized, although a significant increase in the vertical beta function (accompanied perhaps by some decrease in the horizontal beta function) may be desirable to relax the vertical tolerances in the collider, while maintaining luminosity at levels comparable to the nominal designs. The cases where there is a large (factor two or more) increase in event rate are accompanied by large $n_{\gamma}$ and $\Upsilon$ and thus significantly higher backgrounds; just how much background is acceptable must be examined in more detail for individual physics channels.

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