# Magnetic Moments of the Baryon Decuplet in a Relativistic Quark Model* 

Felix Schlumpf<br>Stanford Linear Accelerator Center<br>Stanford University, Stanford, California 94309


#### Abstract

The magnetic moments of the baryon decuplet are calculated in a relativistic constituent quark model using the light-front formalism. Of particular interest are the magnetic moments of the $\Omega^{-}$and $\Delta^{++}$for which new recent experimental measurements are available. Our calculation for the magnetic moment ratio $\mu\left(\Delta^{++}\right) / \mu(p)$ is in excellent agreement with the experimental ratio, while our ratio $\mu\left(\Omega^{-}\right) / \mu\left(\Lambda^{0}\right)$ is slightly higher than the experimental ratio.


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## I. INTRODUCTION

Already two of the magnetic moments of the baryon decuplet have been measured. The most precise experiment for the $\Delta^{++}$is a pion bremsstrahlung analysis [ $\left[\begin{array}{l}i \\ i\end{array}\right]$. The magnetic moment of the $\Omega^{-}$has been measured by the E756 collaboration [20] where $\Omega^{-}$hyperons are produced by a polarized neutral spin transfer reaction. The final result from the succeeding experiment called E800 is expected within the year [3]i]. Theoretical predictions for the $\Delta^{++}$ and $\Omega^{-}$magnetic moments have been given in many models. In particular, the simple, additive quark model predicts the ratio of the magnetic moment of $\Delta^{++}$and proton to be 2 , and it predicts the ratio of the magnetic moment of $\Omega^{-}$and $\Lambda^{0}$ to be 3 .

The analysis of Ref. 㑑 finds the ratio $\mu\left(\Delta^{++}\right) / \mu(p)$ to be $1.62 \pm 0.18$, which is significantly smaller than the additive quark model. Most models however predict a ratio 2 or higher, a value that is only compatible with older experiments.

We recently investigated the predictive power of a relativistic constituent quark model formulated on the light-front [ $[4]$. It provides a simple model wherein we have overall an excellent and consistent picture of the magnetic moments and the semileptonic decays of the baryon octet. The parameters of this model are the constituent quark mass $m$ and the scale parameter $\beta$, which is a measure for the size of the baryon. All parameters except $\beta$ for $\Omega^{-}$have been determined and fixed in Ref. [ $h_{1}$ ]. We predict the magnetic moments for the baryon decuplet and find that the ratio $\mu\left(\Delta^{++}\right) / \mu(p)$ is in excellent agreement with the experiment, while our ratio $\mu\left(\Omega^{-}\right) / \mu\left(\Lambda^{0}\right)$ is slightly higher than the experimental ratio.

In Sec. TIT we give a brief summary of our model as described in Ref. 槝. Section contains the explicit expressions for the magnetic moments of the baryon decuplet. The numerical results are presented in Sec. $\mathbb{I V}_{b}^{2}$, and are compared with experiment and other calculations. We summarize our investigation in a concluding Sec. 'V̄̄̄'.

## II. QUARK-MODEL WAVE FUNCTION

The constituent quark model that we are going to use is described in a previous paper [4]. In order to fix the notation we repeat here the essential formalism.

We shall formulate our model on the light-front which is specified by the invariant hypersurface $x^{+}=x^{0}+x^{3}=0$. The following notation is used: The four-vector is given by $x=\left(x^{+}, x^{-}, x_{\perp}\right)$, where $x^{ \pm}=x^{0} \pm x^{3}$ and $x_{\perp}=\left(x^{1}, x^{2}\right)$. Light-front vectors are denoted by boldface $\mathbf{x}=\left(x^{+}, x_{\perp}\right)$, and they are covariant under kinematic Lorentz transformations The three momenta $\mathbf{p}_{i}$ of the quarks can be transformed to the total and relative momenta to facilitate the separation of the center of mass motion [6]:

$$
\begin{align*}
& \mathbf{P}=\mathbf{p}_{1}+\mathbf{p}_{2}+\mathbf{p}_{3}, \quad \xi=\frac{p_{1}^{+}}{p_{1}^{+}+p_{2}^{+}}, \quad \eta=\frac{p_{1}^{+}+p_{2}^{+}}{P^{+}},  \tag{2.1}\\
& q_{\perp}=(1-\xi) p_{1 \perp}-\xi p_{2 \perp}, \quad Q_{\perp}=(1-\eta)\left(p_{1 \perp}+p_{2 \perp}\right)-\eta p_{3 \perp} .
\end{align*}
$$

Note that the four-vectors are not conserved, i.e., $p_{1}+p_{2}+p_{3} \neq P$. In the light-front dynamics the Hamiltonian takes the form

$$
\begin{equation*}
H=\frac{P_{\perp}^{2}+M^{2}}{P^{+}} \tag{2.2}
\end{equation*}
$$

where $M$ is the mass operator with the interaction term $W$

$$
\begin{align*}
M & =M_{0}+W \\
M_{0}^{2} & =\frac{Q_{\perp}^{2}}{\eta(1-\eta)}+\frac{M_{3}^{2}}{\eta}+\frac{m_{3}^{2}}{1-\eta}  \tag{2.3}\\
M_{3}^{2} & =\frac{q_{\perp}^{2}}{\xi(1-\xi)}+\frac{m_{1}^{2}}{\xi}+\frac{m_{2}^{2}}{1-\xi},
\end{align*}
$$

with $m_{i}$ being the masses of the constituent quarks. To get a clearer picture of $M_{0}$ we transform to $q_{3}$ and $Q_{3}$ by

$$
\begin{align*}
\xi & =\frac{E_{1}+q_{3}}{E_{1}+E_{2}}, \quad \eta=\frac{E_{12}+Q_{3}}{E_{12}+E_{3}}, \\
E_{1 / 2} & =\left(\mathbf{q}^{2}+m_{1 / 2}^{2}\right)^{1 / 2}, \quad E_{3}=\left(\mathbf{Q}^{2}+m_{3}^{2}\right)^{1 / 2}, \quad E_{12}=\left(\mathbf{Q}^{2}+M_{3}^{2}\right)^{1 / 2}, \tag{2.4}
\end{align*}
$$

where $\mathbf{q}=\left(q_{1}, q_{2}, q_{3}\right)$, and $\mathbf{Q}=\left(Q_{1}, Q_{2}, Q_{3}\right)$. The expression for the mass operator is now simply

$$
\begin{equation*}
M_{0}=E_{12}+E_{3}, \quad M_{3}=E_{1}+E_{2} . \tag{2.5}
\end{equation*}
$$

All relevant matrix elements we investigate are related to

$$
\begin{equation*}
\left\langle\mathbf{p}^{\prime}\right| \bar{q} \gamma^{+} q|\mathbf{p}\rangle \sqrt{p^{\prime+} p^{+}} \equiv \mathcal{M}^{+} \tag{2.6}
\end{equation*}
$$

where the state $|\mathbf{p}\rangle \equiv|p\rangle / \sqrt{p^{+}}$is normalized according to

$$
\begin{equation*}
\left\langle\mathbf{p}^{\prime} \mid \mathbf{p}\right\rangle=\delta\left(\mathbf{p}^{\prime}-\mathbf{p}\right) \tag{2.7}
\end{equation*}
$$

The plus component of the matrix element is [ $\left[\begin{array}{ll}1 \\ \hline\end{array}\right]$ :

$$
\begin{equation*}
\mathcal{M}^{+}=3 \frac{N_{c}}{(2 \pi)^{6}} \int d^{3} q d^{3} Q\left(\frac{E_{3}^{\prime} E_{12}^{\prime} M}{E_{3} E_{12} M^{\prime}}\right)^{1 / 2} \Psi^{\dagger}\left(\mathbf{q}^{\prime}, \mathbf{Q}^{\prime}, \lambda^{\prime}\right) \Psi(\mathbf{q}, \mathbf{Q}, \lambda) \tag{2.8}
\end{equation*}
$$

We can write the $\Delta^{++}$for instance as

$$
\begin{equation*}
\left|\Delta^{++}\right\rangle=(\text {uиu }) \chi \phi \tag{2.9}
\end{equation*}
$$

with $\chi$ being the spin wave function and $\phi$ being the momentum distribution. For the latter we choose a function of $M_{0}^{2}$, in particular we choose the same harmonic oscillator and pole type wave function as in Ref. [4] :

$$
\begin{align*}
\phi_{H} & =N_{H} \exp \left(-M_{0}^{2} / 2 \beta^{2}\right), \\
\phi_{P} & =N_{P}\left(1+M_{0}^{2} / \beta^{2}\right)^{-3.5} . \tag{2.10}
\end{align*}
$$

The normalization constants $N_{H}$ and $N_{P}$ are given by the constraint:

$$
\begin{equation*}
\frac{N_{c}}{(2 \pi)^{6}} \int d^{3} q d^{3} Q|\phi|^{2}=1 \tag{2.11}
\end{equation*}
$$

The spin wave function $\chi$ for the spin $\frac{3}{2}$ and $\frac{1}{2}$ are given by

$$
\begin{align*}
& \chi_{\frac{3}{2}}=\uparrow \uparrow \uparrow \\
& \chi_{\frac{1}{2}}=(\uparrow \uparrow \downarrow+\uparrow \downarrow \uparrow+\downarrow \uparrow \uparrow) / \sqrt{3} . \tag{2.12}
\end{align*}
$$

In order to get the baryon to be an eigenfunction of the spin operator we still have to rotate the quark spins by the Melosh transformation as follows:

$$
\begin{equation*}
\uparrow=\mathcal{R}_{i}\binom{1}{0} \text { and } \downarrow=\mathcal{R}_{i}\binom{0}{1} . \tag{2.13}
\end{equation*}
$$

The Melosh rotation for three particles can be written as

$$
\begin{align*}
& \mathcal{R}_{1}=\frac{1}{\sqrt{a^{2}+Q_{\perp}^{2}} \sqrt{c^{2}+q_{\perp}^{2}}}\left(\begin{array}{cc}
a c-q_{R} Q_{L} & -a q_{L}-c Q_{L} \\
c Q_{R}+a q_{R} & a c-q_{L} Q_{R}
\end{array}\right) \\
& \mathcal{R}_{2}=\frac{1}{\sqrt{a^{2}+Q_{\perp}^{2}} \sqrt{d^{2}+q_{\perp}^{2}}}\left(\begin{array}{cc}
a d+q_{R} Q_{L} & a q_{L}-d Q_{L} \\
d Q_{R}-a q_{R} & a d+q_{L} Q_{R}
\end{array}\right)  \tag{2.14}\\
& \mathcal{R}_{3}=\frac{1}{\sqrt{b^{2}+Q_{\perp}^{2}}}\left(\begin{array}{cc}
b & Q_{L} \\
-Q_{R} & b
\end{array}\right)
\end{align*}
$$

where we have defined the following quantities:

$$
\begin{align*}
a & =M_{3}+\eta M, \quad b=m_{3}+(1-\eta) M, \\
c & =m_{1}+\xi M_{3}, \quad d=m_{2}+(1-\xi) M_{3}, \\
q_{R} & =q_{1}+i q_{2}, \quad q_{L}=q_{1}-i q_{2},  \tag{2.15}\\
Q_{R} & =Q_{1}+i Q_{2}, \quad Q_{L}=Q_{1}-i Q_{2} .
\end{align*}
$$

## III. MAGNETIC MOMENTS FOR THE BARYON DECUPLET

The electromagnetic current matrix element for spin $\frac{3}{2}$ particles can be written as

$$
\begin{equation*}
\left\langle p^{\prime}, s^{\prime}\right| J^{\mu}(0)|p, s\rangle=\bar{u}_{\alpha}\left(p^{\prime}, s^{\prime}\right) \mathcal{O}^{\alpha \mu \beta} u_{\beta}(p, s), \tag{3.1}
\end{equation*}
$$

where $u_{\alpha}(p, s)$ is a Rarita-Schwinger spin-vector with momentum $p$ and spin $s$. The Lorentz covariant form for the tensor $\mathcal{O}^{\alpha \mu \beta}$ may be written as

$$
\begin{equation*}
\mathcal{O}^{\alpha \mu \beta}=g^{\alpha \beta}\left(F_{1} \gamma^{\mu}+\frac{F_{2}}{2 M_{B}} i \sigma^{\mu \nu} K_{\nu}\right)+\frac{K^{\alpha} K^{\beta}}{2 M_{B}^{2}}\left(F_{3} \gamma^{\mu}+\frac{F_{4}}{2 M_{B}} i \sigma^{\mu \nu} K_{\nu}\right) \tag{3.2}
\end{equation*}
$$

with momentum transfer $K=p^{\prime}-p$ and baryon mass $M_{B}$. For $K^{2}=0$ the form factors $F_{1}$ and $F_{2}$ are respectively equal to the charge and the anomalous magnetic moment, and the
magnetic moment is $\mu=F_{1}(0)+F_{2}(0)$. For this analysis we are therefore not interested in the form factors $F_{3}$ and $F_{4}$. In order to use Eq. ( $\left.\overline{2} . \bar{B}_{1}^{\prime}\right)$ we express the form factors $F_{1}$ and $F_{2}$ in terms of the plus component of the current:

$$
\begin{align*}
F_{1}(0) & =\left\langle p, \frac{3}{2}\right| J^{+}\left|p, \frac{3}{2}\right\rangle, \\
K_{\perp} F_{2}(0) & =2\left[\sqrt{3} M_{B}\left\langle p^{\prime}, \frac{1}{2}\right| J^{+}\left|p, \frac{3}{2}\right\rangle+K_{\perp}\left\langle p, \frac{3}{2}\right| J^{+}\left|p, \frac{3}{2}\right\rangle\right] . \tag{3.3}
\end{align*}
$$

By inserting our wave function from Eq. (2,9) into the spin conserving matrix element $\left\langle p, \frac{3}{2}\right| J^{+}\left|p, \frac{3}{2}\right\rangle$ we get the charge of the baryon. For the spin flipping matrix element we get

$$
\begin{equation*}
\left\langle p^{\prime}, \frac{1}{2}\right| J^{+}\left|p, \frac{3}{2}\right\rangle=K_{\perp} f \tag{3.4}
\end{equation*}
$$

where $f$ is given for the different baryons as follows:

$$
\begin{align*}
f\left(\Delta^{++}\right) & =2 I_{\Delta}, \\
f\left(\Delta^{+}\right) & =I_{\Delta}, \\
f\left(\Delta^{0}\right) & =0, \\
f\left(\Delta^{-}\right) & =-I_{\Delta}, \\
f\left(\Sigma^{*+}\right) & =\left(4 I_{\Sigma^{*}}^{(2)}-I_{\Sigma^{*}}^{(3)}\right) / 3, \\
f\left(\Sigma^{* 0}\right) & =\left(I_{\Sigma^{*}}^{(2)}-I_{\Sigma^{*}}^{(3)}\right) / 3, \\
f\left(\Sigma^{*-}\right) & =\left(-2 I_{\Sigma^{*}}^{(2)}-I_{\Sigma^{*}}^{(3)}\right) / 3, \\
f\left(\Xi^{* 0}\right) & =\left(2 I_{\Xi^{*}}^{(3)}-2 I_{\Xi^{*}}^{(2)}\right) / 3, \\
f\left(\Xi^{*-}\right) & =\left(-I_{\Xi^{*}}^{(3)}-2 I_{\Xi^{*}}^{(2)}\right) / 3, \\
f\left(\Omega^{-}\right) & =-I_{\Omega} . \tag{3.5}
\end{align*}
$$

The integral $I$ is given by

$$
\begin{equation*}
I=\frac{N_{c}}{(2 \pi)^{6}} \int d^{3} q d^{3} Q|\phi|^{2}\left(A_{1}+A_{2}+A_{3}\right) / \sqrt{3} \tag{3.6}
\end{equation*}
$$

where the quantities $A_{i}$ are

$$
\begin{aligned}
& A_{1}=\frac{\eta\left(a-\frac{Q_{\perp}^{2}}{2(1-\eta) M}\right)}{a^{2}+Q_{\perp}^{2}} \frac{c^{2}}{c^{2}+q_{\perp}^{2}}, \\
& A_{2}=\frac{\eta\left(a-\frac{Q_{\perp}^{2}}{2(1-\eta) M}\right)}{a^{2}+Q_{\perp}^{2}} \frac{d^{2}}{d^{2}+q_{\perp}^{2}}, \\
& A_{3}=\frac{Q_{\perp}^{2}-\eta b}{b^{2}+Q_{\perp}^{2}} .
\end{aligned}
$$

Note that for equal $u$ and $d$ quark masses there is an equality $A_{1}=A_{2}$ under the integral. The masses $m_{i}$ in our equations are set as follows $\left(m=m_{u}=m_{d}\right)$ :

$$
\begin{aligned}
& I_{\Delta}: \quad m_{1}=m_{2}=m_{3}=m, \\
& I_{\Sigma^{*}}^{(2)}: \quad m_{1}=m_{3}=m, \quad m_{2}=m_{s}, \\
& I_{\Sigma^{*}}^{(3)}: \quad m_{1}=m_{2}=m, \quad m_{3}=m_{s}, \\
& I_{\Xi^{*}}^{(2)}: \quad m_{1}=m_{3}=m_{s}, \quad m_{2}=m, \\
& I_{\Xi^{*}}: \\
& I_{\Omega}: \quad m_{1}=m_{2}=m_{s}, \quad m_{3}=m, \\
& I_{1}=m_{2}=m_{3}=m_{s} .
\end{aligned}
$$

In the nonrelativistic limit, $\beta / m \rightarrow 0$, and for equal quark masses the integral $I$ does vanish.

## IV. RESULTS AND DISCUSSIONS

 The parameters of the model, the constituent quark mass $m$ and the scale parameter $\beta$, have been determined and fixed by a successful fit to the electroweak properties of the baryon octet $\left(\beta_{\Delta}=\beta_{N}, \beta_{\Sigma^{*}}=\beta_{\Sigma}, \beta_{\Xi^{*}}=\beta_{\Xi}\right)$ [ $[\overline{4}]$. The only new parameter $\beta_{\Omega}$ is chosen to fit nicely into the raising pattern of the $\beta_{\mathrm{S}}$. The parameters for both wave functions $\phi_{H}$ and $\phi_{P}$ in Eq. ( $\left.\overline{2} \overline{1} \overline{1} \overline{0}_{1}^{\prime}\right)$ are summarized in Table il
 other calculations.

In the simple nonrelativistic quark model (NQM) [8] baryon is the sum of the magnetic moments of each quark composing the baryon. This is quite different to the fact that the magnetic moment is derived from the elastic electron scattering at non-zero momentum transfer. The lattice result (Latt) is taken from a recent lattice simulation of quenched QCD [ $[\overline{9}]$. The other model calculations include results from a
 [1] 1 , an additive quark model [13] with effective quark masses (EM) and a calculation in which relativistic corrections ( RC ) to the baryon magnetic moments are considered $[174$. experimental value (Expt) for the $\Delta^{++}$is taken from a recent pion bremsstrahlung analysis [i] , and the experimental value for the $\Omega^{-}$is taken from a recent investigation where $\Omega^{-}$ hyperons are produced by a polarized neutral spin transfer reaction [

It is instructive to compare the different results of the ratios of the magnetic moments $\mu\left(\Delta^{++}\right) / \mu(p)$ and $\mu\left(\Omega^{-}\right) / \mu\left(\Lambda^{0}\right)$. In the NQM these ratios are parameter free and given to be 2 and 3 respectively.

The experimental value for $\mu\left(\Delta^{++}\right) / \mu(p)$ of Ref. [in is lower than 2 even if we include the uncertainty of the model dependence of the measurement $( \pm 0.16)$. Only the BS calculation and our result are in excellent agreement with experiment. The results from Latt and CB
 this sense the magnetic moment of the $\Delta^{++}$is a good mean to distinguish between the different models.

The experimental value for $\mu\left(\Omega^{-}\right) / \mu\left(\Lambda^{0}\right)$ of Ref. [2] is slightly higher than 3 . It is interesting to note that every model beyond the NQM gives also a value larger than 3, except for EM. Our value 3.49 is closest to the central value of the experiment, although most of the calculations are within the statistical ( $\pm 0.28$ ) and systematic ( $\pm 0.23$ ) error of
this experiment. We could even reduce our value for the ratio $\mu\left(\Omega^{-}\right) / \mu\left(\Lambda^{0}\right)$ by using a larger value of $\beta_{\Omega}$ or by choosing an appropriate anomalous magnetic moment of the strange quark.

## V. SUMMARY

The magnetic moments of the baryon decuplet are calculated in a relativistic constituent quark model using the light-front formalism. The parameters of the model are fixed by fitting the baryon octet physics, except for $\beta_{\Omega}$ which is chosen in a natural way. It is a challenge for every hadronic model to get consistent values for the magnetic moments for both the $\Delta^{++}$and $\Omega^{-}$. Our calculation for the magnetic moment ratio $\mu\left(\Delta^{++}\right) / \mu(p)$ is in excellent agreement with the experimental ratio, while our ratio $\mu\left(\Omega^{-}\right) / \mu\left(\Lambda^{0}\right)$ is slightly higher than the experimental ratio.

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## TABLES

TABLE I. The parameter of the constituent quark model for the harmonic oscillator wave function $(\mathrm{H})$ and for the pole type $(\mathrm{P})$ wave function. Both the quark masses $m$ and the scale parameter $\beta$ are given in units of GeV .

| Parameters | H | P |
| :---: | :---: | :---: |
| $m_{u}=m_{d}$ | 0.26 | 0.263 |
| $m_{s}$ | 0.38 | 0.38 |
| $\beta_{\Delta}$ | 0.55 | 0.607 |
| $\beta_{\text { }^{*}}$ | 0.60 | 0.75 |
| $\beta_{\Xi^{*}}$ | 0.62 | 0.90 |
| $\beta_{\Omega}$ | 0.70 | 1.05 |

TABLE II. Magnetic moments of the baryon decuplet. The calculations of the present work with the harmonic oscillator wave function $(\mathrm{H})$ and the pole type wave function $(\mathrm{P})$ are compared with the simple nonrelativistic quark model (NQM), with a lattice calculation (Latt) and with the Skyrme model (Skyr). The magnetic moments are given in units of the nuclear magneton. References are given in the text.

| Baryon | H | P | NQM | Latt | Skyr |
| :--- | ---: | ---: | ---: | ---: | ---: |
| $\Delta^{++}$ | 4.76 | 4.93 | 5.56 | 4.91 | 4.53 |
| $\Delta^{+}$ | 2.38 | 2.47 | 2.73 | 2.46 | 2.09 |
| $\Delta^{0}$ | 0.00 | 0.00 | -0.09 | 0.00 | -0.36 |
| $\Delta^{-}$ | -2.38 | -2.47 | -2.92 | -2.46 | -2.80 |
| $\Sigma^{*+}$ | 1.82 | 1.84 | 3.09 | 2.55 | 2.55 |
| $\Sigma^{* 0}$ | -0.27 | -0.28 | 0.27 | 0.27 | -0.02 |
| $\Sigma^{*-}$ | -2.36 | -2.41 | -2.56 | -2.02 | -2.60 |
| $\Xi^{* 0}$ | -0.60 | -0.56 | 0.63 | 0.46 | 0.40 |
| $\Xi^{*-}$ | -2.41 | -2.41 | -2.20 | -1.68 | -2.31 |
| $\Omega^{-}$ | -2.48 | -2.47 | -1.84 | -1.40 | -1.98 |

TABLE III. Comparison of our calculations (H) and (P) of the magnetic moments for the $\Delta^{++}$and $\Omega^{-}$with other calculations and experiment (Expt). The calculations are the simple nonrelativistic quark model (NQM), lattice calculations (Latt), Skyrme model (Skyr), cloudy bag model (CB), Bethe-Salpeter formalism (BS), an additive quark model based on effective quark masses (EM) and a calculation including relativistic corrections (RC). The experimental value given for $\Delta^{++}$has some model dependence. All numbers are given in units of the nuclear magneton. References are given in the text.

| Magnetic Moment | Expt | H | P | NQM | Latt | Skyr | CB | BS | EM | RC |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| $\mu\left(\Delta^{++}\right)$ | $4.52 \pm 0.50$ | 4.76 | 4.93 | 5.56 | 4.91 | 4.53 | 6.54 | 4.44 | - | - |
| $\mu\left(\Delta^{++}\right) / \mu(p)$ | $1.62 \pm 0.18$ | 1.69 | 1.75 | 2.00 | 2.18 | 1.98 | 2.34 | 1.59 | - | - |
| $\mu\left(\Omega^{-}\right)$ | $-1.94 \pm 0.17$ | -2.41 | -2.41 | -1.84 | -1.40 | -1.98 | -2.52 | - | -1.69 | -2.25 |
| $\mu\left(\Omega^{-}\right) / \mu\left(\Lambda^{0}\right)$ | $3.16 \pm 0.28$ | 3.49 | 3.49 | 3.00 | 3.6 | 3.73 | 4.13 | - | 2.77 | 3.66 |


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