# PRODUCTION OF $Q^{2} \bar{Q}^{2}$ STATES* 

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## ABSTRACT

In this talk, the productions of $Q^{2} \bar{Q}^{2}$ states in two-photon collision and $J / \psi$ radiative decays are discussed.

1. Introduction. The spectrum of low-lying hadrons is richer in the mass range of $1-2 \mathrm{GeV}$. Besides the $Q^{2} \bar{Q}^{2}$ mesons, some new types of hadrons, like glueballs and hybrids, are predicted theoretically. It is learned from the MIT bag model ${ }^{1}$ that among the $Q^{2} \bar{Q}^{2}$ mesons, some decay to vector meson pairs dominantly and their masses are just about the threshold of corresponding vector meson pairs. These $Q^{2} \bar{Q}^{2}$ mesons might be observed as mass bumps.

The wave functions of some $Q^{2} \bar{Q}^{2}$ states can be projected to a color-singlet/color-singlet meson pair and a color-octet/color-octet meson pair. The recoupling coefficients for $0^{+}$ $Q^{2} \bar{Q}^{2}$ states are the following (Jaffe's notations are used):

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[^0]|  | $P \mathrm{P}$ | VV | $\mathrm{P} \cdot \mathrm{P}$ | $\mathrm{Y}-\mathrm{Y}$ |
| ---: | ---: | ---: | ---: | ---: |
| 9 | 0.743 | -0.041 | -0.169 | 0.646 |
| 36 | 0.644 | 0.177 | 0.407 | 0.623 |
| $9^{\prime}$ | -0.177 | 0.644 | 0.623 | 0.407 |
| $\mathbf{3 6}^{*}$ | 0.041 | 0.743 | -0.643 | -0.169 |

For $2^{+} Q^{2} \bar{Q}^{2}$ states, the recoupling coeficients are:

|  | VV | $\underline{\mathrm{V}} \cdot \underline{\mathrm{V}}$ |
| :---: | :---: | :---: |
| 9 | $\sqrt{\frac{2}{3}}$ | $-\frac{1}{\sqrt{3}}$ |
| 36 | $\frac{1}{\sqrt{3}}$ | $\sqrt{\frac{2}{3}}$ |

According to the MIT bag model, the relative angular momenta of these states are $s$ waves. From these coefficients, the $0^{+}\left(9^{+}, 36^{+}\right)$and $2^{+}(9,36)$ states decay to vector pairs dominantly through the fall-apart mechanism.

On the other hand, according to the VDM, these states can be produced in two-photon collisions (Fig. 1). Also, due to the fact that there are color-octet-vector/ color-octet-vector ( $\underline{V} \cdot \underline{\mathrm{~V}}$ ) components in these states, we expect these states can be produced via two hard gluon channels in the mechanism, which is analogous to $\mathrm{VDM}^{2}$ (Fig. 2). It is known from perturbative QCD that the $J / \psi$ radia tive decay provides such a two-gluon channel; therefore, the productions of these $Q^{2} \bar{Q}^{2}$ states are predicted in $J / \psi$ radiative decays.
2. $\underline{Q}^{2} \bar{Q}^{2}$ Production in $\boldsymbol{\gamma} \boldsymbol{\gamma}$ Collision. Under the mechanism of VDM, the $Q^{2} \bar{Q}^{2}$ states which decay to two-vector mesons dominantly can be produced in two-photon collisions (Fig. 1). Therefore, we can search for these $Q^{2} \bar{Q}^{2}$ states in the processes $77 \rightarrow \mathrm{VV}$ '.
$\gamma \gamma \rightarrow \rho^{0} \rho^{0}$ and $\rho^{+} \rho^{-}$. The experimental data $^{3}$ show large enhancement around the threshold of $\mathbf{p p}$ in the cross section of $77 \rightarrow \rho^{0} \rho^{0}$. Other observations, ${ }^{4}$ however, reveal large suppression in $77 \rightarrow \rho^{+} \rho^{-}$around the $\rho \rho$ threshold. There are many attempts to explain these results; however, only the scheme of $Q^{2} \bar{Q}^{2}$ (Refs. 5, 6) survives. In the scheme of $Q^{2} \bar{Q}^{2}$, there are three $0^{+}$and three $2^{+} Q^{2} \bar{Q}^{2}$ around the $\rho \rho$ threshold which contribute
to $\boldsymbol{\gamma} \boldsymbol{\gamma} \rightarrow p \boldsymbol{p}$. For $0^{+}$or $2^{+} Q^{2} \bar{Q}^{2}$ states, there are two isoscalars and one isotensor $Q^{2} \bar{Q}^{2}$. In the picture of $Q^{2} \bar{Q}^{2}$, there is a constructive interference between the isoscalar and isotensor amplitudes in the reaction $\boldsymbol{\gamma} \boldsymbol{\gamma} \rightarrow \boldsymbol{\rho}^{0} \boldsymbol{\rho}^{0}$. Consequently, a large cross section for $\boldsymbol{\gamma} \boldsymbol{\gamma} \rightarrow \rho^{0} \rho^{0}$ is obtained. For the reaction $\boldsymbol{\gamma} \boldsymbol{\gamma} \rightarrow \rho^{+} \rho^{-}$, such interference is destructive; thus, the cross 'section for $\boldsymbol{\gamma} \boldsymbol{\gamma} \rightarrow \rho^{+} \rho^{-}$is smaller in comparison to $\boldsymbol{\gamma} \boldsymbol{\gamma} \rightarrow \rho^{0} \rho^{0}$. As a matter of fact, it is easy to obtain a 100 nb cross section for $\boldsymbol{\gamma} \boldsymbol{\gamma} \rightarrow \boldsymbol{\rho}^{0} \boldsymbol{\rho}^{0}$ at peak without any new parameter in the picture of $Q^{2} \bar{Q}^{2}$ states.

On the other hand, the TASSO Collaboration has found that for the reaction $\gamma \gamma \rightarrow \rho^{0} \rho^{0}$, $0^{+}$is-dominant as $W_{\gamma \gamma}<1.8 \mathrm{GeV}$, and $2^{+}$is dominant as $W_{\gamma \gamma}>1.8 \mathrm{GeV}$. This result is consistent with the measurement of TPC/2 . These results are consistent with the $Q^{2} \bar{Q}^{2}$ mechanism (Fig. 3).
$\boldsymbol{\gamma} \boldsymbol{\gamma} \rightarrow \rho^{0} \boldsymbol{\omega}$. In the same sense, the cross section of $\gamma \boldsymbol{\gamma} \rightarrow \rho^{0} \omega$ can be explained by the $Q^{2} \bar{Q}^{2}$ model (Fig. 4). ${ }^{7}$
$\underline{\gamma} \rightarrow K^{*} \bar{K}^{*}, \rho^{0} \phi, \omega \phi . \quad$ Observation' of the reaction $\gamma \gamma \rightarrow K^{*+} K^{*-}$ in the $1.7-2.7-\mathrm{GeV}$ region with a peak value of about 50 nb at about 1.9 GeV has been reported. The structure in the channel $\boldsymbol{K}^{*} \mathbf{K}^{\circ}{ }^{\mathrm{O}}$ is observed ${ }^{9}$ to be smaller than the $K^{*+} K^{*-}$ channel by a factor of $7.8 \pm 3.1 \pm 2.0$. The ARGUS mean upper limit $^{9}$ on the $\boldsymbol{\gamma} \boldsymbol{\gamma} \rightarrow \boldsymbol{\rho}^{\boldsymbol{0}} \boldsymbol{\phi}$ cross section is 1.0 nb in the range of $W_{\gamma \gamma}$ between 1.8 and 2.2 GeV . The corresponding upper limit from TPC/2 (Ref. 10) is about 6 nb in the $W_{\gamma \gamma}$ range of $2-2.5 \mathrm{GeV}$. The upper limit of the $\gamma \boldsymbol{\gamma} \rightarrow \boldsymbol{\omega} \boldsymbol{\phi}$ cross section given by ARGUS" is 1.7 nb in the range of $W_{\boldsymbol{\gamma} \boldsymbol{\gamma}}$ between 1.9 and 2.5 GeV .

In the picture of $Q^{2} \bar{Q}^{2}$ states, there are two isoscalars and two isovectors which contribute to $77 \rightarrow K^{*} \bar{K}^{*}$. Among these four $Q^{2} \bar{Q}^{2}$, the two isovectors $Q^{2} \bar{Q}^{2}$ contribute to $77 \rightarrow \boldsymbol{\rho}^{\mathbf{0}} \boldsymbol{\phi}$ and the two isoscalars contribute to $77 \rightarrow \boldsymbol{\omega} \boldsymbol{\phi}$. Without introducing the mixings between the two $Q^{2} \bar{Q}^{2}$ states with the same isospin, the $Q^{2} \bar{Q}^{2}$ picture ${ }^{5,6}$ predicted very small cross sections for both $K^{*+} K^{*-}$ and $K^{*} K^{0}$ channels and very large cross sections for $77 \rightarrow \rho^{0} \phi^{6}$. On the other hand, there have been other theoretical attempts ${ }^{12,13}$ to predict the $K^{*} \bar{K}^{*}$ productions in 77 collisions, but they are all confronted with difficulties in explaining the data.

In our recent paper, ${ }^{14}$ it is pointed out that the predicted small $K^{*} \bar{K}^{*}$ cross sections in the picture of $Q^{2} \bar{Q}^{2}$ are due to the destructive interferences between two isoscalar states and also two isovector states. Since, in the MIT bag model calculation, all the $2^{+} Q^{2} \bar{Q}^{2}$ which decay to $K^{*} \bar{K}^{*}, \rho^{0} \phi$, and $\omega \phi$ dominantly essentially degenerate at 1.95 GeV , the slightest perturbation will cause them to mix pairwise in the channels. We introduce the mixing mechanism to explore its consequences.

After introducing the mixings, constructive interference is found for $\gamma \gamma \rightarrow K^{*+} K^{*-}$ betwen the isoscalar and isovector amplitudes, and this interference yields a large cross section for $\boldsymbol{\gamma} \boldsymbol{\gamma} \boldsymbol{\gamma} \rightarrow K^{*+} K^{*-}$ around 1.9 GeV . Whereas destructive interference between these two amplitudes is found for the reaction $\gamma \boldsymbol{\gamma} \rightarrow \boldsymbol{K}^{* 0} \overline{\boldsymbol{K}}^{* 0}$, this interference suppresses the cross section of $\gamma \gamma \rightarrow K^{* 0} \bar{K}^{* 0}$. The charged-to-neutral $K^{*} \bar{K}^{*}$ ratio is predicted to be about 4 , which is compatible with the experimental measurement (Figs. 5, 6). By using the same mechanism, the amplitude of $\boldsymbol{\gamma} \boldsymbol{\gamma} \rightarrow \boldsymbol{\rho}^{\boldsymbol{0} \phi}$ is diminished. Consequently, the calculated cross section of this reaction is smaller than the original calculation by one order-of-magnitude. The mean value of the cross section in the range of $W_{\boldsymbol{\gamma} \boldsymbol{\gamma}}$ between 1.8 GeV to 2.2 GeV is 1.45 nb , which is compatible with the upper limits set by ARGUS and TPC/2 . As in the earlier calculation, we still obtain a small cross section for $\gamma \boldsymbol{\gamma} \rightarrow \boldsymbol{\omega} \phi$. The mean yalue of the cross section in the range of $W_{\gamma \gamma}$ between 1.9 GeV and 2.5 GeV is about 0.34 nb , which is below the upper limit set by ARGUS.
3. $J / \psi \rightarrow \gamma+V V^{\prime}$. It is analogous to the VDM that a gluon can couple to a color octet vector quark pair; thus, we expect these $Q^{2} \bar{Q}^{2}$ states having larger $\underline{V} \cdot \underline{V}$ components can be produced in two hard gluon channels easily. Under this picture, these $Q^{2} \bar{Q}^{2}$ states can be produced in $J / \psi$ radiative decays in the processes $J / \psi \rightarrow \gamma+V V^{\prime}$ via the mechanism shown in Fig. 7. By using this mechanism, we compute the decay rates of $J / \psi \rightarrow \gamma \rho \rho, \gamma \omega \omega, \gamma K^{*} \bar{K}^{*}$, and $\gamma \phi \phi .^{15}$

$$
\begin{gathered}
\boldsymbol{B}\left(J / \psi \rightarrow \gamma\left(Q^{2} \bar{Q}^{2}\right)_{2^{+}} \rightarrow \gamma \rho \rho\right)=3 \times(0.8-1.4) \times 10^{-4} \\
\boldsymbol{B}\left(J / \psi \rightarrow \gamma\left(Q^{2} \bar{Q}^{2}\right)_{2^{+}} \rightarrow \gamma \omega \omega\right)=(0.8-1.4) \times 10^{-4} \\
\boldsymbol{B}\left(J / \psi \rightarrow \gamma\left(Q^{2} \bar{Q}^{2}\right)_{2^{+}} \rightarrow \gamma \phi \phi\right)=0.7 \times 10^{-6} \\
B\left(J / \psi \rightarrow \gamma\left(Q^{2} \bar{Q}^{2}\right)_{2^{+}} \rightarrow \gamma K^{*} \bar{K}^{*}\right)=(2.3-3.0) \times 10^{-5}
\end{gathered}
$$

4. Conclusions. The $Q^{2} \bar{Q}^{2}$ picture describes the reactions $\boldsymbol{\gamma} \boldsymbol{\gamma} \rightarrow \boldsymbol{V} \boldsymbol{V}$, very well. In order to verify the existence of these $Q^{2} \bar{Q}^{2}$ states, it is important to search for them via a two-gluon channel; $J / \psi$ radiative decays provide good opportunities for that. Due to the smallness of the decay rate of $J / \psi \rightarrow \gamma\left(Q^{2} \bar{Q}^{2}\right)_{2^{+}} \rightarrow \gamma V V^{\prime}$, an $e^{+} e^{-}$collider with very high luminosity will be of significant assistance.

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## FIGURE CAPTIONS

1. Diagram for the reaction $77 \rightarrow \mathbf{V} \mathbf{V}^{\prime}$ with $Q^{2} \bar{Q}^{2}$ states as the intermediate states.
2. Diagram for the reaction $\mathrm{gg} \rightarrow \mathbf{V} \mathbf{V}^{\prime}$ with $Q^{2} \bar{Q}^{2}$ states as the intermediate states.
3. The calculated $Q^{2} \bar{Q}^{2}$ contributions to the $77 \rightarrow \rho^{0} \rho^{0}$ cross section (solid curve) and the $77 \rightarrow \rho^{+} \rho^{-}$cross section (dashed curve) in comparison with the experimental data.
4. Cross section of $77 \rightarrow \omega \boldsymbol{\pi}^{+} \boldsymbol{\pi}^{-}$. The fitted curve was obtained from a four-quark model prescription.
5. Cross section for $77 \rightarrow K^{*+} K^{*-}$.
6. Cross sections for $77 \rightarrow K^{* 0} \bar{K}^{* 0}$ and $\rho^{0} \phi$.
7. Diagram for $J / \psi \rightarrow \gamma V V^{\prime}$ with $Q^{2} \bar{Q}^{2}$ states as the intermediate states.


Fig. 1


Fig. 2


Fig. 3


Fig. 4


Fig. 5


Fig. 6


Fig. 7


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