# DISCOVERING SUPERSYMMETRIC PARTICLES IN $w$-BOSON DECAY AND $e^{+} e^{-}$ANNIHILATION* 

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#### Abstract

The reported discovery of the $W$-boson may provide the opportunity either to discover the supersymmetric partners of the neutrino and the electron or to set greatly improved limits on their masses. We also discuss searching for scalar neutrinos in $e^{+} e^{-}$annihilation (off and on the $Z^{0}$ ).


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[^0]One of the reasons for the proliferation of supersymmetric models ${ }^{1}$ has been the lack of experimental restraints. Future progress in this field would be aided greatly by the discovery of even a single supersymmetric partner of a presently known particle. Even an improvement of the experimental limits on the masses of such particles would be helpful. At this stage a purely phenomenological study, as model-independent as possible, is indicated ${ }^{2}$.

It is clear that processes involving supersymmetric particles are quite rare, and we therefore believe that one should look for events with very distinctive signatures. We have found that the decays of the scalar neutrino $\nu_{s}$ and the scalar electron $e_{s}$ (or muon) can lead to such signatures. Furthermore, measurements of $\nu_{s}$ decays are interesting since there are no real limits on the masses of the scalar neutrinos. The processes we consider are the supersymmetric analogues of $W \rightarrow e \bar{\nu}$ (in $p \bar{p}$ scattering) and $e^{+} e^{-} \rightarrow \nu \bar{\nu}, \quad$ i. e. $W \rightarrow e_{s} \bar{\nu}_{s}$ and $e^{+} e^{-} \rightarrow \nu_{s} \bar{\nu}_{s}$. We find that these processes either could lead to the discovery of the $\nu_{s}$ or $e_{s}$, or could at least set greatly improved limits for their masses.

For some but not all of our results we make use of our previous work ${ }^{3}$ where we showed that for certain sets of parameters a significant fraction (see Fig. 1) of the $\nu_{s}$ will decay into charged modes such as $\nu_{s} \rightarrow e^{-} u \bar{d} \tilde{g}, \quad \nu_{s} \rightarrow \nu u \bar{u} \tilde{g}$ (where $\tilde{g} \equiv$ gluino) or if kinematically allowed $\nu_{s} \rightarrow e_{s} u \bar{d}$. Otherwise the main decay mode is usually expected ${ }^{4}$ to be $\nu_{s} \rightarrow \nu \tilde{\gamma}$. We assume that the photino $\tilde{\gamma}$ behaves like a neutrino experimentally so that the two-body $\nu_{s}$ decays are invisible.

Let us consider first the process $p \bar{p} \rightarrow W+$ anything with $W \rightarrow e_{s} \nu_{s}$. At the CERN SPS collider several events with $W \rightarrow e \nu$ have been observed by two experiments ${ }^{5}$, and we therefore feel it is reasonable to assume that many more $W$ bosons will be produced in the near future. Of these a significant fraction may decay into $e_{s} \nu_{s}$ (see Fig. 2) depending on their masses:

$$
\begin{equation*}
r \equiv \frac{\Gamma\left(W^{+} \rightarrow e_{s}^{+} \nu_{s}\right)}{\Gamma\left(W^{+} \rightarrow e^{+} \nu\right)}=\frac{1}{2}\left[\left(1-\frac{M_{\nu_{s}}^{2}}{M_{W}^{2}}-\frac{M_{e_{s}}^{2}}{M_{W}^{2}}\right)^{2}-4 \frac{M_{\nu_{s}}^{2} M_{e_{s}}^{2}}{M_{W}^{4}}\right]^{\frac{3}{2}} \tag{1}
\end{equation*}
$$

The identification of these events requires their separation from $e \nu$ events and from other backgrounds (such as the semileptonic decays of a pair of heavy
quarks). To aid in this identification, we have calculated a variety of distributions of $\nu e$ and $\nu_{s} e_{s}$ processes under the assumption that $\nu_{s}$ decays invisibly. We used Monte Carlo techniques to simulate $W$ bosons with appropriate longitudinal and transverse momentum distributions ${ }^{6}$, and to decay the $\boldsymbol{W}$ bosons into either ev or $e_{s} \nu_{s}$ (the $e_{s}$ were then decayed into $e \tilde{\gamma}$ ). Using the standard model of electroweak interactions, we have applied the appropriate angular distributions for the $e \nu$ and for $e_{s} \nu_{s}$. The transverse momentum ( $p_{e}^{\perp}$ ) spectra for the final electrons is shown in Fig. 3. By assuming that the process is $W \rightarrow e \nu$, one can calculate the $p_{\nu}^{\perp}$ spectra for the final neutrino ( $\vec{p}_{\nu}^{\perp}=-\vec{p}_{h a d}^{\perp}-\vec{p}_{e}^{\perp}$ ); the distributions look very similar to those in Fig. 3. For $e^{\mp} \nu$ the $\cos \theta$ distribution ( $\theta$ being the angle between electron and proton beam) still shows the forward-backward asymmetry although the $(1 \pm \cos \theta)^{2}$ dependence of $u d \rightarrow e \nu$ is somewhat modified since the $W$ is not produced at rest. For $e_{g} \nu_{s}$ events the momentum of the parent $W$ changes the center-of-mass $\sin ^{2} \theta$ distribution into a relatively flat distribution which actually $\operatorname{dips}$ at $\cos \theta \approx 0$. Another useful distribution is related to the calculated longitudinal momentum $p_{\nu}^{\prime}$ of the neutrino assuming $W \rightarrow e \nu$. Even if $W$ indeed decays into $e \nu$ there is an often unresolvable ambiguity in the determination of $p_{\nu}$. The two solutions are:

$$
\begin{equation*}
p_{\nu}^{\|}=\frac{M_{W}^{2}+2 \vec{p}_{\nu}^{\perp} \cdot \vec{p}_{e}^{\perp}}{2{p_{e}^{\perp}}^{2}}\left\{p_{e}^{\|} \pm p_{e} \sqrt{1-\frac{4 p_{\nu}^{\perp^{2}} p_{e}^{\perp^{2}}}{\left(M_{W}^{2}+2 \vec{p}_{\nu}^{\perp} \cdot \vec{p}_{e}^{\perp}\right)^{2}}}\right\} \tag{2}
\end{equation*}
$$

We choose a variable $p_{m}$ which is uniquely defined as that solution to Eq. (2) with the smaller absolute value. The sign of this solution is kept. For $e_{s} \nu_{s}$ events $p_{m}$ does not have a simple kinematical interpretation.

We find that we can separate $e_{s} \nu_{s}$ events from $e \nu$ events by making cuts in these four variables. We can then identify the presence of $e_{s} \nu_{s}$ events from the resulting distributions. For example, by eliminating all events with $p_{e}^{\perp}$ or $\stackrel{\perp}{\perp}>35 \mathrm{GeV}$, or $\cos \theta>0.65$, or $-40<p_{m}<20 \mathrm{GeV}$ we find that $00 \%$ of $e \nu$ events but less than half of $e_{s} \nu_{s}$ events are eliminated. This will be discussed in greater detail in a future paper ${ }^{7}$.

We do not wish to minimize the problem of backgrounds (including standard
physics backgrounds such as from dual semi-leptonic heavy quark decays where the leptons carry almost all the energy). It is important for experimentalists to measure backgrounds, determine efficiencies, etc. in order to find out how well they can separate the signal from the noise. Some backgrounds may be eliminated by requiring the absence of accompanying hadronic jets. One clearly must have a minimum $p_{e}^{\perp}$ cut. We chose $p_{e}^{\perp}>12 \mathrm{GeV}$ but a higher cut is possible. The number of events from the background of $W \rightarrow \nu \tau$ with $\tau \rightarrow \nu \nu e$ is precisely calculable given the $W \rightarrow \nu e$ rate. They also have a softer $p_{e}^{\perp}$ spectrum and have the forward-backward asymmetry of $W \rightarrow \nu e$ events.

In order to find particles or set limits in the region $M_{\nu_{0}} \approx M_{e_{g}} \approx 30 \mathrm{GeV}$ or $M_{e_{s}} \approx 40 \mathrm{GeV}, M_{\nu_{g}} \approx 10 \mathrm{GeV}$ (i.e. $r>0.2$ in Fig. 1 ), one will need an integrated luminosity adequate to produce at least 200 to $300 W \rightarrow e \nu$ events (and 40 to $60 e_{s} \nu_{s}$ events).

If the $\nu_{s}$ has a substantial charged-decay mode, then one may in addition look for events with a high energy electron plus a hadron jet plus missing $E^{\perp}$ (from the photino). The hadron jet should have a very high invariant mass which should help separating these events from heavy quark ( b or c ) production.

Let us now consider $e^{+} e^{-} \rightarrow \nu_{s} \nu_{s}$ which occurs via s-channel $Z^{0}$ and $t$ channel wino exchange. If $\nu_{s}$ has only invisible decays, one must rely on neutrino-counting techniques ${ }^{8}$. If the charged-decay modes are significant, then there are some very distinctive signatures in $e^{+} e^{-}$physics. These occur when one $\nu_{s}$ decays invisibly while the other $\nu_{s}$ decays into modes such as $e^{-} u \bar{d} \tilde{g}$ or $\nu u \bar{u} \tilde{g}$. The rate of $\nu_{s} \bar{\nu}_{s}$ production is dependent on $M_{\nu}$ and beam energy as shown in Fig. 4 (where $M_{\text {wino }}=M_{W}$ was assumed). If the wino is significantly lighter ${ }^{9}$ than the $W$, then these rates may be significantly enhanced ${ }^{10}$. If the luminosity for PETRA at $\sqrt{s}=42 \mathrm{GeV}$ is $1.3 \times 10^{31} \mathrm{sec}^{-1} \mathrm{~cm}^{-2}, M_{\nu_{g}}=$ 18 GeV and we count $\nu_{s}^{e} \bar{\nu}_{s}^{e}, \nu_{s}^{\mu} \bar{\nu}_{s}^{\mu}$ and $\nu_{s}^{\tau} \bar{\nu}_{s}^{\tau}$ events, then a year's running (with $50 \%$ uptime) may yield 14 events with one neutral and one charged decay. At TRISTAN ( $\sqrt{s}=60 \mathrm{GeV}$ ) a year's running may yield 450 such events; whereas at SLC and LEP, running on the $Z^{0}$ resonance may yield many more events or could set much higher limits on the masses. Due to the large production cross
section of $\nu_{s} \nu_{s}$ at the $Z^{0}$, one is much more sensitive to rare decay mode of the $\nu_{s}$ which can lead to very dramatic signatures. For example, in $Z^{0} \rightarrow \nu_{s} \nu_{s}$ with $\nu_{s} \rightarrow \nu \mu^{+} e^{-} \tilde{\gamma}$ (and $\tilde{\nu}_{s} \rightarrow$ unobserved neutrals), one will observe $\mu^{+} e^{-}$and considerable missing energy.

The angular distribution of $\nu_{s} \nu_{s}$ events (neglecting electron mass) is

$$
\begin{align*}
\frac{\mathrm{d} \sigma}{\mathrm{~d} \cos \theta}= & \frac{\pi \alpha^{2} s}{32 X^{2}}\left(1-\frac{4 M^{2}}{s}\right)^{\frac{3}{2}} \sin ^{2} \theta \\
& \times\left\{\frac{1}{\left(M_{w i n o}^{2}-t\right)^{2}}+\left(\frac{(4 X-1)^{2}+1}{8(1-X)^{2}}\right)\left(\frac{1}{\left(M_{Z}^{2}-s\right)^{2}+\Gamma^{2} M_{Z}^{2}}\right)\right.  \tag{3}\\
& \left.\quad+\left(\frac{2 X-1}{1-X}\right)\left(\frac{1}{M_{w i n o}^{2}-t}\right)\left(\frac{M_{Z}-s}{\left(M_{Z}-s\right)^{2}+\Gamma^{2} M_{Z}^{2}}\right)\right\}
\end{align*}
$$

where $X \equiv \sin ^{2} \theta_{W}, M \equiv M_{\nu_{s}}$ and $t=M^{2}-\frac{s}{2}+\frac{s}{2}\left(1-\frac{4 M^{2}}{s}\right)^{\frac{1}{2}} \cos \theta$. The threshold behavior and the overall $\sin ^{2} \theta$ dependence reflect the $p$-wave nature of this process and result from the spin of $\nu_{s}$ and its chiral couplings.

This angular dependence is very helpful in separating these events from the primary backgrounds. One background is beam-gas events which can be totally separated. Another is two-photon events in which one electron is missed down the beam pipe and the other electron comes out at a large angle but goes through a "hole" in the detector. Our discussions with experimentalists leave us confident that our events can be isolated from all backgrounds even if the numbers are small. We have generated random events, some of which are displayed in Fig. 5 making use of the $\nu_{s}$ decay matrix elements ${ }^{3}$.

Finally it should be added that $\boldsymbol{W}$-decay and $e^{+} e^{-}$physics can also be used to study the production of other supersymmetric particles ${ }^{11}$. Sometimes the signatures of these events can be quite similar to those discussed here. Consider for example, the case which has been proposed in the literature, that one of the winos $(\omega)$ is light ${ }^{9,10}$. If the two lightest mass eigenstates $\chi_{1}^{0}$ and $\chi_{2}^{0}$ of the neutral gaugino and higgsino mass matrix are also light, the following decays become possible: $W^{ \pm} \rightarrow \omega^{ \pm} \chi_{1,2}^{0}$ and $e^{+} e^{-} \rightarrow \chi_{\mathbf{1}, 2}^{0} \chi_{1,2}^{0}$. In particular, if the decay
$\chi_{2}^{0} \rightarrow \chi_{1}^{0}+$ hadronic jets occurs (where $\chi_{1}^{0}$ behaves like the $\tilde{\gamma}$ ), then $e^{+} e^{-} \rightarrow \chi_{1}^{0} \chi_{2}^{0}$ events will resemble our $e^{+} e^{-} \rightarrow \nu_{s} \bar{\nu}_{s}$ events where one $\nu_{s}$ decays into charged particles and the other decays invisibly. Clearly, the observation of such events would also be a signal of physics beyond the standard model and a hint for supersymmetry.

We believe that the combination of searches in $W$-boson decay and $e^{+} e^{-} \rightarrow$ $\nu_{s} \bar{\nu}_{s}$ has the potential of setting greatly improved limits on supersymmetric scalar leptons and could even lead to their discovery in the next few years.

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## FIGURE CAPTIONS

1. Fraction of $e^{+} e^{-} \rightarrow \nu_{s} \bar{\nu}_{s}$ events where one of the scalar neutrinos decays into charged particles and the other one decays into invisible neutrals (solid line); and fraction of events where both scalar neutrinos decay into charged particles (dashed line). We have assumed that $M_{u_{s}} \approx M_{e_{s}}$, $M_{\text {wino }}=M_{W}$ and $M_{\tilde{\gamma}} \approx M_{\tilde{g}} \approx 0$. We choose $M_{\nu_{s}}=20 \mathrm{GeV}$; however, the curve is nearly independent of the mass-scale as long as $M_{\nu_{\theta}}$, $M_{e^{s}}<M_{W}$. The increase of the dashed line for small $M_{e_{g}}\left(M_{u_{g}}\right)$ corresponds to the production of on-shell scalar electrons (scalar $u$-quarks) which then decay into charged modes.
2. Curves of constant $r$ are shown. $r \equiv \Gamma\left(W \rightarrow e_{s} \nu_{s}\right) / \Gamma(W \rightarrow e \nu)$ is a function of $M_{\nu_{g}}$ and $M_{e_{g}}$ (cf. Eq. 1). There is a large range of mass parameters for which the decay of the $W$ into scalar leptons would have a significant branching ratio. Since there is virtually no limit on $M_{\nu_{s}}$ and the limit on $M_{e^{8}}$ is only 17 GeV , even a value of $r=0.4$ is not yet excluded.
3. The shape of the transverse momentum $p_{e}^{\perp}$ distribution of the electron resulting from the decay of a $W$ produced in $p \bar{p}$ collisions. The curves are normalized to equal area. The solid curve refers to $W \rightarrow e \nu$. The Jacobian peak is clearly visible. The two other curves show the $p_{e}^{\perp}$ distribution for $W \rightarrow e_{s} \nu_{s}$ where $e_{s} \rightarrow e \tilde{\gamma}$. The dashed curve corresponds to $M_{e_{\theta}}=40 \mathrm{GeV}$ and $M_{\nu_{g}}=10 \mathrm{GeV}$. The dotted curve corresponds to $M_{e_{g}}=M_{\nu_{s}}=30 \mathrm{GeV}$.
4. The ratio $R \equiv \sigma\left(\nu_{s} \bar{\nu}_{s}\right) / \sigma^{e m}\left(\mu^{+} \mu^{-}\right)$as a function of the mass of the scalar neutrino. We have assumed that $M_{\text {wino }}=M_{W}$. In some models with lighter winos, the values of $R$ could be significantly enhanced (below the $Z^{0}$ resonance). Note that this cross section will be difficult to detect unless (at least) one of the $\nu_{s}$ decays via charged modes.
5. Simulated events of $e^{+} e^{-} \rightarrow \nu_{s} \nu_{s}$. One of the scalar neutrinos decays into eu $\bar{d} \tilde{g}$ and the other one decays invisibly. In these "typical events"
$\sqrt{s}=42 \mathrm{GeV}$, and $M_{\nu_{0}}=18 \mathrm{GeV}$. Each event is shown in two views. First with the beam-pipe perpendicular to the plane of the projection and secondly with the beam-pipe going from top to bottom of the plane of projection. The beam-pipe has been marked in both views. The dotted lines correspond to the electron whereas the solid lines represent the gluino and the two quarks. The resultant hadron jets will usually be relatively narrow.


Fig. 1


Fig. 2


Fig. 3


Fig. 4


Fig. 5


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