

$B \rightarrow K^{(*)}\ell^+\ell^-$ from B-factories and Tevatron

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BABAR and Belle measurements of branching fractions, rate asymmetries and angular observables in the decay modes $B \rightarrow K^{(*)}\ell^+\ell^-$ are reviewed and new results from CDF on $B \rightarrow K^{(*)}\mu^+\mu^-$ branching fractions and angular observables are discussed. A first search for $B^+ \rightarrow K^+\tau^+\tau^-$ is presented.

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1 Introduction

The decays $b \rightarrow s\ell^+\ell^-$, where $\ell^+\ell^-$ is an e^+e^- , $\mu^+\mu^-$ or $\tau^+\tau^-$ pair, are flavor-changing neutral current (FCNC) processes, which are forbidden in the Standard Model (SM) at tree level but are allowed to proceed via electroweak loops and weak box diagrams. An effective Hamiltonian is used to calculate decay amplitudes [1], which depend on three effective Wilson coefficients, C_7^{eff} , C_9^{eff} , and C_{10}^{eff} . The first is extracted from the $B \rightarrow X_s\gamma$ branching fraction, the latter two respectively represent the vector and axial vector part of the weak penguin and box diagrams. New Physics effects involve new loops that interfere with the SM processes modifying the measured values of C_7^{eff} , C_9^{eff} , and C_{10}^{eff} with respect to the SM predictions [2]. In addition, scalar and pseudoscalar processes may contribute that introduce new Wilson coefficients C_s and C_p that are forbidden in the SM. Thus, it is important to measure many observables in order to overconstrain the complex Wilson coefficients [3]. These electroweak penguin modes contribute in probing New Physics at a scale of a few TeV [4]. In this review, we focus on exclusive decays presenting results from *BABAR*, Belle and CDF. The data samples are based on luminosities of 349 fb^{-1} , 605 fb^{-1} and 4.4 fb^{-1} corresponding to 384 million $B\bar{B}$ events, 656 Million $B\bar{B}$ events and $2 \times 10^{10} b\bar{b}$ events, respectively.

2 Selection of $B \rightarrow K^{(*)}e^+e^-$ and $B \rightarrow K^{(*)}\mu^+\mu^-$ Events

BABAR and Belle fully reconstruct ten $B \rightarrow K^{(*)}e^+e^-$ and $B \rightarrow K^{(*)}\mu^+\mu^-$ final states, in which a K^+ , K_S^0 , $K^+\pi^-$, $K^+\pi^0$ or $K_S^0\pi^+$ recoils against the lepton pair*, while CDF reconstructs $K^+\mu^+\mu^-$ and $K^+\pi^-\mu^+\mu^-$ final states. *BABAR* (Belle) selects lepton candidates with momenta $p_e > 0.3(0.4) \text{ GeV}/c$ and $p_\mu > 0.7(0.7) \text{ GeV}/c$. *BABAR* and Belle require good particle identification (PID) for e , μ , K , and π , and select K_S^0 in the $\pi^+\pi^-$ channel. CDF requires muons with $p_T(\mu) > 0.4 \text{ GeV}/c$, kaons and pions with $p_T(K, \pi) > 1 \text{ GeV}/c$ and B -mesons with $p_T(B) > 6 \text{ GeV}/c$. Both, muons and hadrons must have good PID and the muon pair must originate from a secondary vertex. All three experiments suppress combinatorial $B\bar{B}$ and $q\bar{q}$ continuum backgrounds ($q = u, d, s, c$). Here, the leptons dominantly originate from semileptonic b and c decays. *BABAR* trains neural networks (NN) using event shape variables, vertex information, missing energy, and lepton separation near the interaction region (IR) optimized in each mode and each q^2 bin[†]. Belle trains a Fisher discriminant using event shape variables, missing mass, B flavor tagging, and lepton separation in z near the IR. CDF trains NNs using vertex information, the angle between the signed vertex displacement with respect to the B momentum, and the μ

*Charge conjugation is implied unless otherwise stated.

[†]This is the squared momentum transfer into the dilepton system.

Experiment	Mode	\mathcal{B} [10^{-6}]	\mathcal{A}_{CP}	$\mathcal{R}_{K^{(*)}}$
<i>BABAR</i> [6]	$K\ell^+\ell^-$	$0.394_{-0.069}^{+0.073} \pm 0.02$	$-0.18_{-0.18}^{+0.18} \pm 0.01$	$0.96_{-0.34}^{+0.44} \pm 0.05$
<i>BABAR</i> [6]	$K^*\ell^+\ell^-$	$1.11_{-0.18}^{+0.19} \pm 0.07$	$-0.01_{-0.15}^{+0.16} \pm 0.01$	$1.10_{-0.32}^{+0.42} \pm 0.07$
Belle [7]	$K\ell^+\ell^-$	$0.48_{-0.04}^{+0.05} \pm 0.03$	$0.04 \pm 0.1 \pm 0.02$	$1.03 \pm 0.19 \pm 0.06$
Belle [7]	$K^*\ell^+\ell^-$	$1.07_{-0.10}^{+0.11} \pm 0.09$	$-0.10 \pm 0.1 \pm 0.01$	$0.83 \pm 0.17 \pm 0.8$
CDF [8]	$K\mu^+\mu^-$	$0.38_{-0.05}^{+0.05} \pm 0.03$		
CDF [8]	$K^*\mu^+\mu^-$	$1.06_{-0.14}^{+0.14} \pm 0.09$		

Table 1: Branching fractions, CP asymmetries and lepton flavor ratios for $B \rightarrow K^{(*)}\ell^+\ell^-$ modes in the entire q^2 region from *BABAR*, Belle, and CDF. Uncertainties are statistical and systematic, respectively.

separation. *BABAR* and Belle select signal candidates using the beam-energy substituted mass $m_{ES} = \sqrt{E_{beam}^{*2} - p_B^{*2}}$ and the energy difference $\Delta E = E_B^* - E_{beam}^*$, where E_{beam}^* , E_B^* and p_B^* are the beam energy, B-meson energy and B-meson momentum in the $\Upsilon(4S)$ center-of-mass frame, respectively. *BABAR* extracts the signal yield from a one-dimensional unbinned extended maximum log-likelihood fit in m_{ES} , while Belle performs a one (two) dimensional unbinned extended maximum log-likelihood fit in m_{ES} (and $m_{K\pi}$) for $K^{(*)}\ell^+\ell^-$ modes. CDF selects signal candidates from an unbinned maximum log-likelihood fit in the B invariant-mass distribution. All experiments reject events in the J/ψ and $\psi(2S)$ mass regions and require that $K\mu$ and $K\pi\mu$ masses are not consistent with a D mass to reject background from $B \rightarrow DX$ decays. The rejected charmonium events are used as control samples for various cross checks.

3 Results for $B \rightarrow K^{(*)}e^+e^-$ and $B \rightarrow K^{(*)}\mu^+\mu^-$ Modes

Figure 1 (left) shows total branching fractions for $B \rightarrow K^{(*)}\ell^+\ell^-$ (e^+e^- and $\mu^+\mu^-$ modes combined) [6, 7, 8] and $B \rightarrow X_s\ell^+\ell^-$ [9, 7] in comparison to the SM predictions [5]. The individual exclusive measurements are summarized in Table 1. The Belle inclusive measurement is a recent update based on a luminosity of 605 fb^{-1} , yielding $\mathcal{B}(B \rightarrow X_s\ell^+\ell^-) = 3.33 \pm 0.8_{-0.24}^{+0.19} \times 10^{-6}$ [10]. The partial branching fractions measured in the three experiments are also consistent with the SM predictions.

Rate asymmetries are more precisely measured than branching fractions, since many uncertainties cancel [11]. The isospin asymmetry [12]

$$\mathcal{A}_I(q^2) = \frac{d\mathcal{B}(B^0 \rightarrow K^{(*)0}\ell^+\ell^-)/dq^2 - (\tau_{B^0}/\tau_{B^+})d\mathcal{B}(B^+ \rightarrow K^{(*)+}\ell^+\ell^-)/dq^2}{d\mathcal{B}(B^0 \rightarrow K^{(*)0}\ell^+\ell^-)/dq^2 + (\tau_{B^0}/\tau_{B^+})d\mathcal{B}(B^+ \rightarrow K^{(*)+}\ell^+\ell^-)/dq^2}, \quad (1)$$

corrected for the different B^0 and B^+ lifetimes (τ_{B^0}/τ_{B^+}), is expected to be small in the SM ($\mathcal{A}_I(q^2)/dq^2$ is -0.01 for $q^2 = 2.7 - 6 \text{ GeV}^2/c^4$ after dropping from \simeq

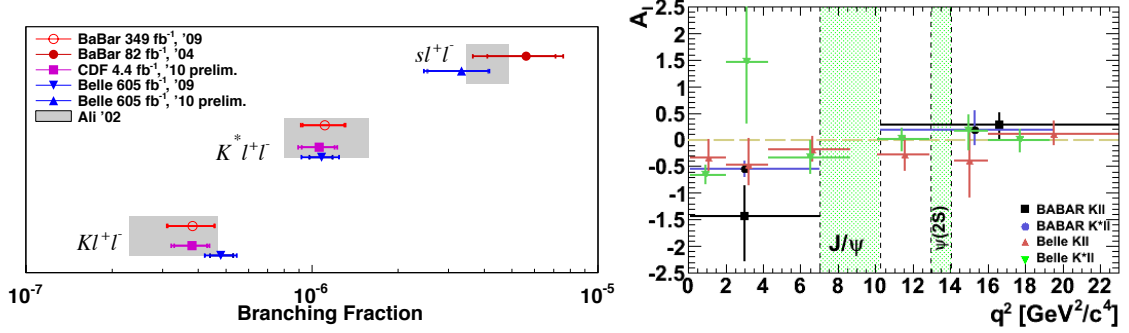


Figure 1: (Left) Total branching fractions measurements of $B \rightarrow K^{(*)}\ell^+\ell^-$ and $B \rightarrow X_s\ell^+\ell^-$ modes from *BABAR* (red dots), Belle (blue triangles) and CDF (magenta squares) in comparison to the SM prediction (grey-shaded region). For *BABAR* and Belle, $\ell^+\ell^-$ is a combination of e^+e^- and $\mu^+\mu^-$ modes, for CDF it is $\mu^+\mu^-$. (Right) Isospin asymmetry measurements for $B \rightarrow K^{(*)}\ell^+\ell^-$ versus q^2 from *BABAR* (black squares, blue dots) and Belle (red triangles, green triangles).

0.075 at $q^2 = 0.1 \text{ GeV}^2/c^4$ and crossing zero near $q^2 = 1.7 \text{ GeV}^2/c^4$) [12]. Figure 1 (right) shows the *BABAR* and Belle \mathcal{A}_I measurements for different q^2 regions. The q^2 integrated isospin asymmetry and \mathcal{A}_I for q^2 values above the J/ψ are consistent with the SM prediction. Below the J/ψ , however, *BABAR* observes a negative \mathcal{A}_I that deviates significantly from the SM prediction (3.9σ from $\mathcal{A}_I = 0$). For models in which the sign in C_7^{eff} is flipped with respect to the value in the SM, a small negative \mathcal{A}_I is expected [12, 13], but it is too small to explain the *BABAR* measurement. For low q^2 , the Belle results are consistent with both *BABAR* and the SM.

In the SM, the direct CP asymmetry

$$\mathcal{A}_{CP} = \frac{\mathcal{B}(\bar{B} \rightarrow K^{(*)}\ell^+\ell^-) - \mathcal{B}(B \rightarrow K^{(*)}\ell^+\ell^-)}{\mathcal{B}(\bar{B} \rightarrow K^{(*)}\ell^+\ell^-) + \mathcal{B}(B \rightarrow K^{(*)}\ell^+\ell^-)}. \quad (2)$$

is expected to be $\mathcal{O}(10^{-3})$, and new physics at the electroweak scale may provide significant enhancements [14]. *BABAR* performs a simultaneous fit to $B^+ \rightarrow K^+\ell^+\ell^-$ and $B \rightarrow K^*\ell^+\ell^-$ modes. The results summarized in Table 1 together with Belle's measurements are consistent with the SM expectations.

In the SM, the lepton flavor ratios $\mathcal{R}_K = \mathcal{B}(B \rightarrow K\mu^+\mu^-)/\mathcal{B}(B \rightarrow Ke^+e^-)$ and $\mathcal{R}_{K^*} = \mathcal{B}(B \rightarrow K^*\mu^+\mu^-)/\mathcal{B}(B \rightarrow K^*e^+e^-)$ integrated over all q^2 are predicted to be one and 0.75, respectively. The theoretical uncertainties are just a few percent. For example, in two-Higgs-doublet models the presence of a SUSY Higgs might give $\sim 10\%$ corrections to $\mathcal{R}_{K^{(*)}}$ for large $\tan\beta$ [13]. The *BABAR* and Belle measurements summarized in Table 1 are consistent with the SM expectations.

The $B \rightarrow K^*\ell^+\ell^-$ angular distribution depends on three angles: θ_K , the angle between the K momentum and the B momentum in the K^* rest frame, θ_ℓ , the angle

Experiment	q^2 bin [GeV^2/c^4]	\mathcal{F}_L	\mathcal{A}_{FB}
<i>BABAR</i> [17]	0.1-6.25	$0.35 \pm 0.16 \pm 0.04$	$0.24_{-0.23}^{+0.18} \pm 0.05$
Belle [7]	1-6	$0.67 \pm 0.23 \pm 0.04$	$0.26_{-0.30}^{+0.27} \pm 0.07$
CDF [8]	1-6	$0.5_{-0.30}^{+0.27} \pm 0.04$	$0.43_{-0.37}^{+0.36} \pm 0.06$
SM [24]	1-6	$0.73_{-0.23}^{+0.13}$	$-0.05_{-0.04}^{+0.03}$

Table 2: *BABAR*, Belle, and CDF measurements of \mathcal{F}_L and \mathcal{A}_{FB} from $B \rightarrow K^* \ell^+ \ell^-$ modes in the low q^2 region.

between the $\ell^+ (\ell^-)$ momentum and the $B (\bar{B})$ momentum in the $\ell^+ \ell^-$ rest frame, and ϕ , the angle between the two decay planes. The angular distribution involves 12 q^2 -dependent coefficients J_i [15, 16] that can be extracted from a full angular fit in individual bins of q^2 . Since large data samples are necessary for this study, *BABAR*, Belle and CDF have analyzed only the one-dimensional angular distributions

$$W(\cos \theta_K) = \frac{3}{2} \mathcal{F}_L \cos^2 \theta_K + \frac{3}{4} (1 - \mathcal{F}_L) \sin^2 \theta_K, \quad (3)$$

$$W(\cos \theta_\ell) = \frac{3}{4} \mathcal{F}_L \sin^2 \theta_\ell + \frac{3}{8} (1 - \mathcal{F}_L) (1 + \cos^2 \theta_\ell) + \mathcal{A}_{FB} \cos \theta_\ell, \quad (4)$$

where \mathcal{F}_L is the K^* longitudinal polarization and \mathcal{A}_{FB} is the lepton forward-backward asymmetry. While Belle and CDF measure \mathcal{F}_L and \mathcal{A}_{FB} in six q^2 bins, *BABAR* measured \mathcal{F}_L and \mathcal{A}_{FB} in two q^2 bins due to the limited data sample. An update with the full *BABAR* data set in six q^2 bins is in progress. The measured m_{ES} and angular distributions are fitted with signal, combinatorial background and peaking background components. After determining the signal yield from the m_{ES} spectrum, \mathcal{F}_L is extracted from a fit to the $\cos \theta_K$ distribution for fixed signal yield. Finally, \mathcal{A}_{FB} is extracted from the $\cos \theta_\ell$ distribution for fixed signal yield and fixed \mathcal{F}_L .

Figure 2 shows the *BABAR*, Belle, and CDF results for \mathcal{F}_L (left) and \mathcal{A}_{FB} (right) in comparison to the SM prediction (lower red curve) [18] and for flipped-sign C_7^{eff} models (upper blue curve) [20, 23]. In the SM, \mathcal{A}_{FB} is negative for small q^2 , crosses zero at $q_0^2 = (4.2 \pm 0.6) \text{ GeV}^2/c^4$ and is positive for large q^2 , while for flipped-sign C_7^{eff} models \mathcal{A}_{FB} is positive for all q^2 . Table 2 summarized the \mathcal{F}_L and \mathcal{A}_{FB} measurements from $B \rightarrow K^* \ell^+ \ell^-$ in the low q^2 region in comparison to the SM prediction. For \mathcal{F}_L , the three measurements are consistent with each other and the SM prediction. For \mathcal{A}_{FB} , the three measurements are in good agreement. Though they are in better agreement with the flipped-sign C_7^{eff} model, they are consistent with the SM prediction. For $B \rightarrow K \ell^+ \ell^-$, \mathcal{A}_{FB} is consistent with zero as expected in the SM.

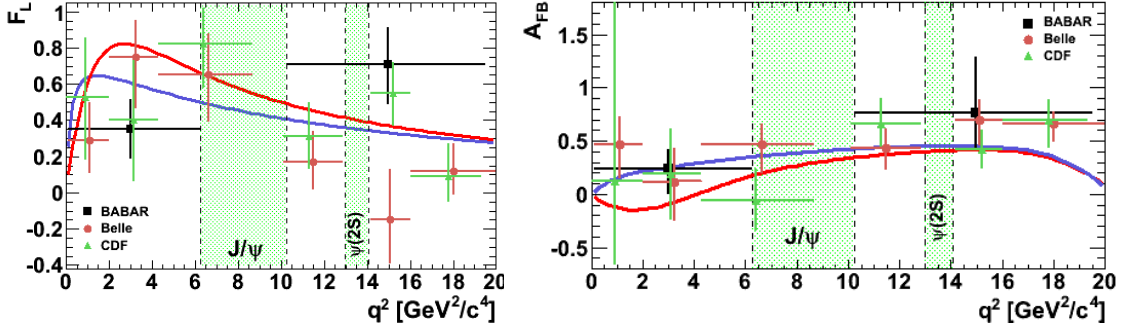


Figure 2: (left) Measurements of \mathcal{F}_L and (right) Measurements of \mathcal{A}_{FB} in $B \rightarrow K^{(*)}\ell^+\ell^-$ modes by *BABAR* (black squares), *Belle* (brown dots) and *CDF* (green triangles). The SM prediction (flipped-sign C_7^{eff} model) is shown by the upper red (lower blue) curve for \mathcal{F}_L and the lower red (upper blue) curve for \mathcal{A}_{FB} .

4 Search for $B^+ \rightarrow K^+\tau^+\tau^-$

In the SM, the q^2 dependence of the $B \rightarrow X_s\tau^+\tau^-$ decay rate has a shape similar to that of $B \rightarrow X_s\mu^+\mu^-$ in the high q^2 region. The $B^+ \rightarrow K^+\tau^+\tau^-$ branching fraction is predicted to be $\sim 2 \times 10^{-7}$ in the SM, which is 50 – 60% of the total inclusive branching fraction [21]. Enhancements are predicted in models beyond the SM. In the next-to-minimal supersymmetric models (NMSSM), for example, the rate may be enhanced by the squared tau-to-muon mass ratio $(m_\tau/m_\mu)^2 \sim 280$. Since signal final states contain 2-4 ν , a different analysis strategy is needed here to control backgrounds.

BABAR has performed the first search for $B^+ \rightarrow K^+\tau^+\tau^-$ using an integrated luminosity of 423 fb^{-1} which corresponds to 465 $B\bar{B}$ events. The recoiling ("tag") B is reconstructed in many hadronic final states, $B^- \rightarrow D^{(*)0,+}X$, where X represents up to six hadrons ($\pi^\pm, \pi^0, K^\pm, K_S^0$). Using m_{ES} and ΔE the tag is selected with an efficiency of $\sim 0.2\%$. The single-prong τ decays $\tau \rightarrow e\nu\bar{\nu}, \tau \rightarrow \mu\nu\bar{\nu}$ and $\tau \rightarrow \pi\nu$ are selected as signal modes. Thus, signal candidates are required to have only three charged particles of which one is an identified kaon with charge opposite to the tag B and $0.44 < p_K < 1.4 \text{ GeV}/c$ in the center-of-mass frame. The two remaining particles must have opposite charge, be consistent with the signal τ decays, have $p < 1.59 \text{ GeV}/c$ and a mass $M_{pair} < 2.89 \text{ GeV}/c^2$. Further requirements are $q^2 = (\vec{p}_{r(4S)} - \vec{p}_{tag} - \vec{p}_K)^2/c^2 > 14.23 \text{ GeV}^2/c^4$, a missing energy (*i.e.* the energy carried off by neutrinos estimated as the difference between $\Upsilon(4S)$ energy and that of all observed particles) of $1.39 < E_{miss} < 3.38 \text{ GeV}$, and neutral energy deposited in the electromagnetic calorimeter $E_{extra} < 0.74 \text{ GeV}$. Continuum background is suppressed by $|\cos\theta_T| < 0.8$, where θ_T is the opening angle between the thrust axis of the tag and that of the rest of the event. The largest remaining background originates

from $B^+ \rightarrow D^0 X^+$, which is suppressed by combining the signal K^+ with the τ daughter of opposite charge assigned the π mass hypothesis and requiring a mass $M_{K\pi} > 1.96 \text{ GeV}/c^2$.

BABAR observes 47 events with an expected background of 64.7 ± 7.3 events. Including systematic uncertainties a branching fraction upper limit of $\mathcal{B}(B \rightarrow K^+ \tau^+ \tau^-) < 3.3 \times 10^{-3}$ is set at 90% confidence level (CL).

5 Conclusion

BABAR and Belle have measured branching fractions, rate asymmetries and angular observables in $B \rightarrow K^{(*)} \ell^+ \ell^-$ final states. Recently, CDF contributed new measurements on branching fractions and angular observables in $B \rightarrow K^{(*)} \mu^+ \mu^-$. Except for the isospin asymmetry at low values of q^2 all other measurements are consistent with the SM, though \mathcal{F}_L and \mathcal{A}_{FB} agree also with the flipped-sign C_7^{eff} model. *BABAR* has performed the first search for $B^+ \rightarrow K^+ \tau^+ \tau^-$ setting a branching fraction upper limit of $\mathcal{B}(B^+ \rightarrow K^+ \tau^+ \tau^-) < 3.3 \times 10^{-3}$ at 90% CL. Although all experiments are expected to update results with the final data sets, significant improvement in precision will come from LHCb and the Super B-factories. In these new experiments, sufficiently large data samples will be collected to measure the full angular distribution from which the 12 observables J_i [15] can be measured with high precision in different bins of q^2 . In turn, the Wilson coefficients can be determined with high precision to reveal small discrepancies with respect to the SM predictions [3, 23].

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