

Dark matter profiles and annihilation in dwarf spheroidal galaxies: perspectives for present and future γ -ray observatories

I. The classical dSphs

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Accepted XXXX. Received XXXX; in original form XXXX

ABSTRACT

Due to their large dynamical mass-to-light ratios, dwarf spheroidal galaxies (dSphs) are promising targets for the indirect detection of dark matter (DM) in γ -rays. We examine their detectability by present and future γ -ray observatories. The key innovative features of our analysis are: (i) We take into account the *angular size* of the dSphs; while nearby objects have higher γ ray flux, their larger angular extent can make them less attractive targets for background-dominated instruments. (ii) We derive DM profiles and the astrophysical J -factor (which parameterises the expected γ -ray flux, independently of the choice of DM particle model) for the classical dSphs *directly* from photometric and kinematic data. We assume very little about the DM profile, modelling this as a smooth split-power law distribution, with and without sub-clumps. (iii) We use a Markov Chain Monte Carlo (MCMC) technique to marginalise over unknown parameters and determine the sensitivity of our derived J -factors to both model and measurement uncertainties. (iv) We use simulated DM profiles to demonstrate that our J -factor determinations recover the correct solution within our quoted uncertainties.

Our key findings are: (i) Sub-clumps in the dSphs do *not* usefully boost the signal; (ii) The sensitivity of atmospheric Cherenkov telescopes to dSphs within ~ 20 kpc with cored halos can be up to ~ 50 times worse than when estimated assuming them to be point-like. Even for the satellite-borne Fermi-LAT the sensitivity is significantly degraded on the relevant angular scales for long exposures, hence it is vital to consider the angular extent of the dSphs when selecting targets; (iii) *No* DM profile has been ruled out by current data, but using a prior on the inner dark matter cusp slope $0 \leq \gamma_{\text{prior}} \leq 1$ provides J -factor estimates accurate to a factor of a few if an appropriate angular scale is chosen; (iv) The J -factor is best constrained at a critical integration angle $\alpha_c = 2r_{\text{half}}/d$ (where r_{half} is the half light radius and d is the distance to the dwarf) and we estimate the corresponding sensitivity of γ -ray observatories; (v) The ‘classical’ dSphs can be grouped into three categories: well-constrained and promising (Ursa Minor, Sculptor, and Draco), well-constrained but less promising (Carina, Fornax, and Leo I), and poorly constrained (Sextans and Leo II); (vi) Observations of classical dSphs with Fermi-LAT integrated over the mission lifetime are more promising than observations with the planned Cherenkov Telescope Array for DM particle mass $\lesssim 700$ GeV. However, even Fermi-LAT will *not* have sufficient integrated signal from the classical dwarfs to detect DM in the ‘vanilla’ Minimal Supersymmetric Standard Model. Both the Galactic centre and the ‘ultra-faint’ dwarfs are likely to be better targets and will be considered in future work.

Key words: astroparticle physics — (cosmology:) dark matter — Galaxy: kinematics and dynamics — γ -rays: general — methods: miscellaneous

1 INTRODUCTION

The detection of γ -rays from dark matter (DM) annihilation is one of the most promising channels for indirect detection (Gunn et al. 1978; Stecker 1978). Since the signal goes as the DM density squared, the Galactic centre seems to be the obvious location to search for such a signal (Silk & Bloemen 1987). However, it is plagued by a confusing background of astrophysical sources (e.g. Aharonian et al. 2004). For this reason, the dwarf spheroidal galaxies (dSphs) orbiting the Milky Way have been flagged as favoured targets given their potentially high DM densities and small astrophysical backgrounds (Lake 1990; Evans et al. 2004).

Despite the growing amount of kinematic data from the classical dSphs, the inner parts of their DM profiles remain poorly constrained and can generally accommodate both cored or cuspy solutions (e.g. Koch et al. 2007; Strigari et al. 2007; Walker et al. 2009). There are two dSphs—Fornax and Ursa Minor—that show indirect hints of a cored distribution (Kleyna et al. 2003; Goerdt et al. 2006); however, in both cases the presence of a core is inferred based on a timing argument that assumes we are not catching the dSph at a special moment. Theoretical expectations remain similarly uncertain. Cusps are favoured by cosmological models that model the DM alone, assuming it is cold and collisionless (e.g. Navarro, Frenk & White 1996). However, the complex dynamical interplay between stars, gas and DM during galaxy formation could erase such cusps leading to cored distributions (e.g. Navarro et al. 1996; Read & Gilmore 2005; Mashchenko et al. 2008; Goerdt et al. 2010; Governato et al. 2010; Cole et al. 2011). Cores could also be an indication of other possibilities such as self-interacting dark matter (e.g. Hogan & Dalcanton 2000; Moore et al. 2000).

Knowledge of the inner slope of the DM profile is of critical importance as most of the annihilation flux comes from that region. Lacking this information, several studies have focused on the detectability of these dSphs by current γ -ray observatories such as the satellite-borne Fermi-LAT and atmospheric Cherenkov telescopes (ACTs) such as H.E.S.S., MAGIC and VERITAS, using a small sample of cusped and cored profiles (generally one of each). Most studies rely on standard core and cusp profiles fitted to the kinematic data of the dSph of interest (Bergström & Hooper 2006; Sánchez-Conde et al. 2007; Bringmann et al. 2009; Pieri et al. 2009; Pieri et al. 2009). Other authors use a ‘cosmological prior’ from large scale cosmological simulations (e.g. Kuhlen 2010). Both approaches may be combined, such as in Strigari et al. (2007) and Martinez et al. (2009) who rely partially on the results of structure formation simulations to constrain the inner slope and then perform a fit to the data to derive the other parameters. However such cosmological priors remain sufficiently uncertain that their use is inappropriate for guiding observational strategies. There have been only a few studies (e.g., Essig et al. 2009) which have *not* assumed strong priors for the DM profiles.

In this work, we revisit the question of the detectability of dark matter annihilation in the classical Milky Way dSphs, motivated by ambitious plans for next-generation ACTs such as the Cherenkov Telescope Array (CTA). We rely *solely* on published kinematic data to derive the properties of the dSphs, making minimal assumptions about the underlying DM distribution. Most importantly, we do not restrict our survey of DM profiles to those suggested by cosmological simulations. We also consider the effect of the spatial extent of the dSphs, which becomes important for nearby systems observed by background-limited instruments such as ACTs.

This paper extends the earlier study of Walker et al. (2011) which showed that there is a critical integration angle (twice the half-light radius divided by the dSph distance) where we can obtain a robust estimate of the J -factor (that parameterises the expected γ -ray flux from a dSph independently of the choice of dark matter particle model; see Section 2), regardless of the value of the central DM cusp slope γ . Here, we focus on the full radial dependence of the J -factor. We consider the effect of DM sub-lumps within the dSphs, discuss which dSphs are the best candidates for an observing programme, and examine the competitiveness of next-generation ACTs as dark matter probes.

This paper is organised as follows. In Section 2, we present a study of the annihilation γ -ray flux, focusing on which parameters critically affect the expected signal. In Section 3, we discuss the sensitivity of present/future γ -ray observatories. In Section 4, we present our method for the dynamical modelling of the observed kinematics of stars in dSphs. In Section 5, we derive DM density profiles for the classical dSphs using an MCMC analysis, from which the detection potential of future γ -ray observatories can be assessed. We present our conclusions in Section 6.¹

This paper includes detailed analyses from both high-energy astrophysics and stellar dynamical modelling. To assist readers from these different fields in navigating the key sections, we suggest that those who are primarily interested in the high-energy calculations may wish to focus their attention on Sections 2, 3 and 5 before moving to the conclusions. Readers from the dynamics community may instead prefer to read Sections 2, 4 and 5. Finally, those who are willing to trust the underlying modelling should proceed to Section 5 where our main results regarding the detectability of dSphs are presented in Figs. 12, 15, 16 and 17.

2 THE DARK MATTER ANNIHILATION SIGNAL: KEY PARAMETERS

2.1 The γ -ray flux

The γ -ray flux Φ_γ (photons $\text{cm}^{-2} \text{s}^{-1} \text{GeV}^{-1}$) from DM annihilations in a dSph, as seen within a solid angle $\Delta\Omega$, is given by (see Appendix A for definitions and conventions used in the literature):

$$\frac{d\Phi_\gamma}{dE_\gamma}(E_\gamma, \Delta\Omega) = \Phi^{\text{PP}}(E_\gamma) \times J(\Delta\Omega), \quad (1)$$

The first factor encodes the (unknown) particle physics of DM annihilations which we wish to measure. The second factor encodes the astrophysics *viz.* the l.o.s. integral of the DM density-squared over solid angle $\Delta\Omega$ in the dSph — this is called the ‘ J -factor’. We now discuss each factor in turn.

¹ Technical details are deferred to Appendices. In Appendix A, we comment on the various notations used in similar studies and provide conversion factors to help compare results. In Appendix B, we provide a toy model for quick estimates of the J -factor. In Appendix D, we calculate in a more systematic fashion the range of the possible ‘boost factor’ (due to DM clumps within the dSphs) for generic dSphs. In Appendix E, we show that convolving the signal by the PSF of the instrument is equivalent to a cruder quadrature sum approximation. In Appendix F, we discuss some technical issues related to confidence level determination from the MCMC analysis. In Appendix G, the reconstruction method is validated on simulated dSphs. In Appendix H, we discuss the impact of the choice of the binning of the stars and of the shape of the light profile on the J -factor determination.

2.1.1 The particle physics factor

The particle physics factor (Φ^{PP}) is given by:

$$\Phi^{\text{PP}}(E_\gamma) \equiv \frac{d\Phi_\gamma}{dE_\gamma} = \frac{1}{4\pi} \frac{\langle \sigma_{\text{ann}} v \rangle}{2m_\chi^2} \times \frac{dN_\gamma}{dE_\gamma}, \quad (2)$$

where m_χ is the mass of the DM particle, σ_{ann} is its self-annihilation cross-section and $\langle \sigma_{\text{ann}} v \rangle$ the average over its velocity distribution, and dN_γ/dE_γ is the differential photon yield per annihilation. A benchmark value is $\langle \sigma_{\text{ann}} v \rangle \sim 3 \times 10^{-26} \text{ cm}^3 \text{ s}^{-1}$ (Jungman et al. 1996), which would result in a present-day DM abundance satisfying cosmological constraints.

Unlike the annihilation cross section and particle mass, the differential annihilation spectrum ($dN_\gamma/dE_\gamma(E_\gamma)$) requires us to adopt a specific DM particle model. We focus on a well-motivated class of models that are within reach of up-coming direct and indirect experiments: the Minimal Supersymmetric Standard Model (MSSM). In this framework, the neutralino is typically the lightest stable particle and therefore one of the most favoured DM candidates (see e.g. Bertone et al. 2005). A γ -ray continuum is produced from the decay of hadrons (e.g. $\pi^0 \rightarrow \gamma\gamma$) resulting from the DM annihilation. Neutralino annihilations can also directly produce mono-energetic γ -ray lines through loop processes, with the formation of either a pair of γ -rays ($\chi\chi \rightarrow \gamma\gamma$; Bergström & Ullio 1997), or a Z^0 boson and a γ -ray ($\chi\chi \rightarrow \gamma Z^0$; Ullio & Bergström 1998). We do not take into account such line production processes since they are usually sub-dominant and very model dependent (Bringmann et al. 2008). The differential photon spectrum we use is restricted to the continuum contribution and is written as:

$$\frac{dN_\gamma}{dE_\gamma}(E_\gamma) = \sum_i b_i \frac{dN_\gamma^i}{dE_\gamma}(E_\gamma, m_\chi), \quad (3)$$

where the different annihilation final states i are characterised by a branching ratio b_i .

Using the parameters in Fornengo et al. (2004), we plot the continuum spectra calculated for a 1 TeV mass neutralino in Fig. 1. Apart from the $\tau^+\tau^-$ channel (dash-dotted line), all the annihilation channels in the continuum result in very similar spectra of γ -rays (dashed lines). For charged annihilation products, internal bremsstrahlung (IB) has recently been investigated and found to enhance the spectrum close to the kinematic cut-off (e.g., Bringmann et al. 2008). As an illustration, the long-dashed line in Fig. 1 corresponds to the benchmark configuration for a wino-like neutralino taken from Bringmann et al. (2008). However, the shape and amplitude of this spectrum are strongly model dependent (Bringmann et al. 2009) and, as argued in Cannoni et al. (2010), this contribution is relevant only for models (and at energies) where the line contribution is dominant over the secondary photons.

We wish to be as model-independent as possible, and so do not consider internal bremsstrahlung. In the remainder of this paper, all our results will be based on an *average* spectrum taken from the parametrisation (Bergström et al. 1998, solid line in Fig. 1):

$$\frac{dN_\gamma}{dE_\gamma} = \frac{1}{m_\chi} \frac{dN_\gamma}{dx} = \frac{1}{m_\chi} \frac{0.73 e^{-7.8x}}{x^{1.5}}, \quad (4)$$

with $x \equiv E_\gamma/m_\chi$. Finally, in order to be conservative in deriving detection limits, we also do not consider the possible ‘Sommerfeld enhancement’ of the DM annihilation cross-section (Hisano et al.

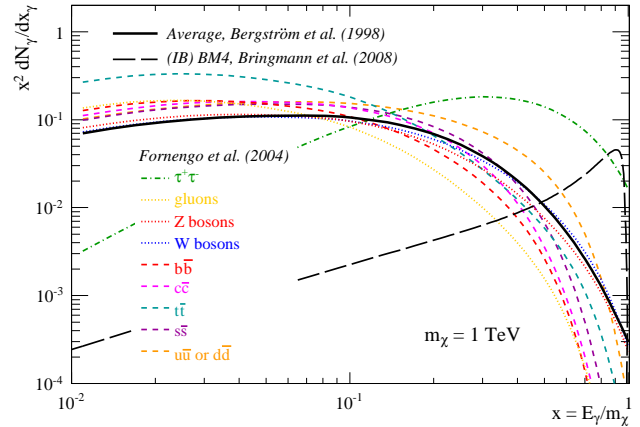


Figure 1. Differential spectra (multiplied by x^2) of γ -rays from the fragmentation of neutrino annihilation products (here for a DM particle mass of $m_\chi = 1 \text{ TeV}$). Several different channels are shown, taken from Fornengo et al. (2004) and an average parametrisation Bergström et al. (1998) is marked by the black solid line; this is what we adopt throughout this paper. The black dashed line is the benchmark model BM4 (Bringmann et al. 2008) which includes internal bremsstrahlung and serves to illustrate that very different spectra are possible. However, the example shown here is dominated by line emission and therefore highly model dependent; for this reason, we do not consider such effects in this paper.

2004, 2005).² This depends inversely on the DM particle velocity, and thus requires precise modelling of the velocity distribution of the DM within the dSph; we will investigate this in a separate study.

2.1.2 The J -factor

The second term in Eq. (1) is the astrophysical J -factor which depends on the spatial distribution of DM as well as on the beam size. It corresponds to the l.o.s. integration of the DM density squared over solid angle $\Delta\Omega$ in the dSph:

$$J = \int_{\Delta\Omega} \int \rho_{\text{DM}}^2(l, \Omega) dl d\Omega. \quad (5)$$

The solid angle is simply related to the integration angle α_{int} by

$$\Delta\Omega = 2\pi \cdot (1 - \cos(\alpha_{\text{int}})).$$

The J -factor is useful because it allows us to rank the dSphs by their expected γ -ray flux, independently of any assumed DM particle physics model. Moreover, the knowledge of the relative J -factors would also help us to evaluate the validity of any potential detection of a given dSph, because for a given particle physics model we could then scale the signal to what we should expect to see in the other dSphs.

All calculations of J presented in this paper were performed using the publicly available CLUMPY package (Charbonnier, Combet, Maurin, in preparation) which includes models for a smooth DM density profile for the dSph, clumpy dark matter sub-structures inside the dSph, and a smooth and clumpy Galactic DM distribution.³

² This effect depends on the mass and the velocity of the particle; the resulting boost of the signal and the impact on detectability of the dSphs has been discussed, e.g., in Pieri et al. (2009).

³ In Appendix B, we provide approximate formulae for quick estimates of the J -factor and cross-checks with the numerical results.

2.1.3 DM profiles

For the DM halo we use a generalised (α, β, γ) Hernquist profile given by (Hernquist 1990; Dehnen 1993; Zhao 1996):

$$\rho(r) = \rho_s \left(\frac{r}{r_s} \right)^{-\gamma} \left[1 + \left(\frac{r}{r_s} \right)^\alpha \right]^{\frac{\gamma-\beta}{\alpha}}, \quad (6)$$

where the parameter α controls the sharpness of the transition from inner slope, $\lim_{r \rightarrow 0} d \ln(\rho) / d \ln(r) = -\gamma$, to outer slope $\lim_{r \rightarrow \infty} d \ln(\rho) / d \ln(r) = -\beta$, and r_s is a characteristic scale. In principle we could add an additional parameter in order to introduce an exponential cut-off in the profile of Eq (6) to mimic the effects of tidal truncation, as proposed in e.g., the Aquarius (Springel et al. 2008) or Via Lactea II (Diemand et al. 2008) simulations. However, the freedom to vary parameters r_s , α and β in Eq (6) already allows for density profiles that fall arbitrarily steeply at large radius. Moreover, given that our MCMC analysis later shows that the outer slope β is unconstrained by the available data and that the J-factor does not correlate with β , we choose not to add further shape parameters.

For profiles such as $\gamma \geq 1.5$, the quantity J from the inner regions diverges. This can be avoided by introducing a saturation scale r_{sat} , that corresponds physically to the typical scale where the annihilation rate $[\langle \sigma v \rangle \rho(r_{\text{sat}}) / m_\chi]^2$ balances the gravitational infall rate of DM particles $(G\bar{\rho})^{-1/2}$ (Berezinsky et al. 1992). Taking $\bar{\rho}$ to be about 200 times the critical density gives

$$\rho_{\text{sat}} \approx 3 \times 10^{18} \left(\frac{m_\chi}{100 \text{ GeV}} \right) \times \left(\frac{10^{-26} \text{ cm}^3 \text{ s}^{-1}}{\langle \sigma v \rangle} \right) M_\odot \text{ kpc}^{-3}. \quad (7)$$

The associated saturation radius is given by

$$r_{\text{sat}} = r_s \left(\frac{\rho_s}{\rho_{\text{sat}}} \right)^{1/\gamma} \ll r_s. \quad (8)$$

This limit is used for all of our calculations.

2.2 Motivation for a generic approach and reference models

In many studies, the γ -ray flux (from DM annihilations) is calculated using the point-source approximation (e.g., Bergström & Hooper 2006; Kuhlen 2010). This is valid so long as the inner profile is steep, in which case the total luminosity of the dSph is dominated by a very small central region. However, if the profile is shallow and/or the dSph is nearby, the effective size of the dSph on the sky is larger than the point spread function (PSF) of the detector, and the point-source approximation breaks down. For upcoming instruments and particularly shallow DM profiles, the effective size of the dSph may even be comparable to the field of view of the instrument. This difference in the radial extent of the signal does matter in terms of detection (see Section 3). Hence we do not assume that the dSph is a point-source but rather derive sky-maps for the expected γ -ray flux.

2.2.1 Illustration: a cored vs cusped profile

Fig. 2 shows J as a function of the integration angle α_{int} for a dSph at 20 kpc (looking towards its centre). The black solid line is for a cored profile ($\gamma = 0$) and the green dashed line is for a cuspy profile ($\gamma = 1.5$); both are normalised to unity at $\alpha_{\text{int}} = 5^\circ$. For the cuspy profile, $\sim 100\%$ of the signal is in the first bin while for the cored profile, J builds up slowly with α_{int} , and 80% of the signal (w.r.t. the value for $\alpha_{\text{int}} = 5^\circ$) is obtained for $\alpha \approx 3^\circ$. This is

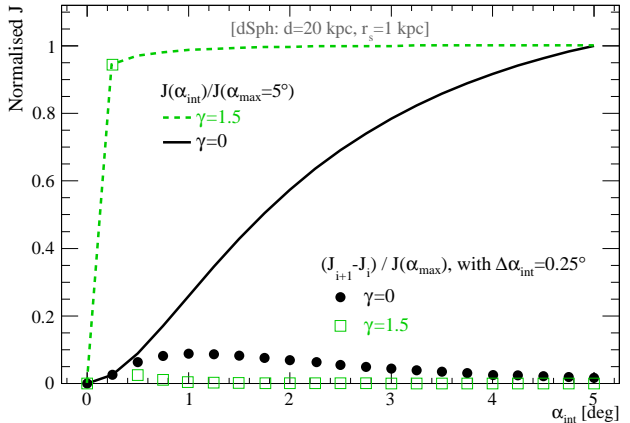


Figure 2. Finite size effects: J as a function of the integration angle α_{int} for a dSph at 20 kpc (pointing towards the centre of the dSph). The black solid line is for a cored profile ($\gamma = 0$) and the green dashed line is for a cuspy profile ($\gamma = 1.5$); both are normalised to unity at $\alpha_{\text{int}} = 5^\circ$.

also indicated by the symbols which show the contribution of DM shells in two angular bins — whereas the (green) hollow squares have a spiky distribution in the first bin ($\gamma = 1.5$), the (black) filled circles ($\gamma = 0$) show a very broad distribution for J .

The integration angle required to have a sizeable fraction of the signal depends on several parameters: the distance d of the dSph, the inner profile slope γ , and the scale radius r_s . Small integration angles are desirable since this minimises contaminating background γ -ray photons and maximises the signal to noise. Thus the true detectability of a dSph will depend on its spatial extent on the sky, and thus also on d , γ and r_s .

2.2.2 Generic dSph profiles

As will be seen in Section 5, the errors on the density profiles of the Milky Way dSphs are large, making it difficult to disentangle the interplay between the key parameters for detectability. Hence we select some ‘generic profiles’ to illustrate the key dependencies.

The most constrained quantity is the mass within the half-light radius r_{half} (typically a few tenths of a kpc), as this is where most of the kinematic data come from (e.g., Walker et al. 2009; Wolf et al. 2010). For the classical Milky Way dSphs, the typical mass within $r_{\text{half}} \sim 300 \text{ pc}$ is found to be $M_{300} \sim 10^7 M_\odot$ (Strigari et al. 2008, — see also the bottom panel of Fig. 13). If the DM scale radius is significantly larger than this ($r_s \gg r_{\text{half}}$) and the inner slope $\gamma \gtrsim 0.5$, we can approximate the enclosed mass by:

$$M_{300} \simeq \frac{4\pi \rho_s r_s^3}{3 - \gamma} \left(\frac{300 \text{ pc}}{r_s} \right)^{3-\gamma} \approx 10^7 M_\odot. \quad (9)$$

The parameter ρ_s is thus determined completely by the above condition, if we choose the scale radius r_s and cusp slope γ .

Table 1 shows, for several values of r_s and γ , the value required for ρ_s to obtain the assumed M_{300} mass. We fix $\alpha = 1, \beta = 3$ but our results are not sensitive to these choices.⁴ The values of r_s are chosen to encompass the range of r_s found in the MCMC analysis (see Section 5). To further convince ourselves that the generic

⁴ For a different mass for the dSph, the results for J below have to be rescaled by a factor $(M_{300}^{\text{new}} / 10^7 M_\odot)^2$ since the density is proportional to M_{300} , while J goes as the density squared.

Table 1. The required normalisation ρ_s to have $M_{300} = 10^7 M_\odot$ for a sample of $(1, 3, \gamma)$ profiles with varying scale radius r_s .

$\gamma \setminus r_s$ [kpc]	$\rho_s (10^7 M_\odot \text{ kpc}^{-3})$		
	0.10	0.50	1.0
0.00	224	25.8	16.02
0.25	196	18.6	10.22
0.50	170	13.4	6.47
0.75	146	9.5	4.06
1.00	125	6.7	2.52
1.25	106	4.7	1.54
1.50	88	3.2	0.92

profiles we present here are a possible description of real dSphs, we checked (not shown) using typical stellar profiles and properties of these objects (i.e., half-light radius of a few 100 pc), that a flat $\sim 10 \text{ km s}^{-1}$ velocity dispersion profile within the error bars is recovered. We also study below the effect of moving these dSphs from a distance of 10 kpc to 300 kpc, corresponding to the typical range covered by these objects.

2.2.3 Sub-structures within the dSph

Structure formation simulations in the currently favoured Λ CDM (cold DM plus a cosmological constant) cosmology find that DM halos are self-similar, containing a wealth of smaller ‘sub-structure’ halos down to Earth-mass halos (e.g. Diemand et al. 2005). However, as emphasised in the introduction, such simulations typically neglect the influence of the baryonic matter during galaxy formation. It is not clear what effect these have on the DM sub-structure distribution. For this reason, we adopt a more generic approach. We assess the importance of clumps using the following recipe:⁵

- (i) we take a fraction $f = 20\%$ of DM mass in the form of clumps;
- (ii) the spatial distribution of clumps follows the smooth one;
- (iii) the clump profiles are calculated *à la* Bullock et al. (2001) (hereafter B01), i.e. an ‘NFW’ profile (Navarro, Frenk & White 1996) with concentration related to the mass of the clumps.
- (iv) the clump mass distribution is $\propto M^{-a}$ ($a = -1.9$), within a mass range $M_{\min} - M_{\max} = [10^{-6} - 10^6] M_\odot$.

Although these parameters are very uncertain, they allow us to investigate the impact of substructures on the J-factor. They are varied within reasonable bounds in Section 2.3.2 (and Appendix D) to determine whether the sub-clump contribution can boost the signal. Note that a 20% clump mass fraction is about twice as large as the fraction obtained from numerical simulations (see, e.g., Springel et al. 2008). This generous fraction does not affect our conclusions, as discussed below.

2.3 J_{sm} and J_{subcl} for the generic models

As an illustration, we show in Fig. 3 one realisation of the 2D distribution of J from a generic core profile ($\gamma = 0$) with $r_s = 1$ kpc (sub-clump parameters are as described in Section 2.2.3). The

dSph is at $d = 100$ kpc. We note that our consideration of a $\gamma = 0$ smooth component with NFW sub-clumps is plausible if, e.g., baryon-dynamical processes erase cusps in the smooth halo but cannot do so in the sub-subhalos. The total J is the sum of the smooth and sub-clump distributions. The centre is dominated by the smooth component, whereas some graininess appears in the outskirts of the dSph. In this particular configuration, the ‘extended’ signal from the core profile, when integrated over a very small solid angle, could be sub-dominant compared with the signal of NFW sub-clumps that it hosts. The discussion of cross-constraints between detectability of sub-halos of the Galaxy vs. sub-clumps in the dSph is left for a future study.

In the remainder of the paper, we will replace for simplicity the calculation of $J_{\text{subcl}}(\alpha_{\text{int}})$ by its mean value, as we are primarily interested in ‘unresolved’ observations. Hence clumps are not drawn from their distribution function, but rather $\langle J_{\text{subcl}} \rangle$ is calculated from the integration of the spatial and luminosity (as a function of the mass) distributions (see Appendix B2).

2.3.1 Radial dependence $J(\theta)$

The radial dependence of J is shown in Fig. 4 for four values of γ (for an integration angle $\alpha_{\text{int}} = 0.01^\circ$). The dashed lines show the result for the smooth distribution; the dotted lines show the sub-clump contribution; and the solid lines are the sum of the two. The peak of the signal is towards the dSph centre. As long as the distribution of clumps is assumed to follow the smooth one, regardless of the value of γ , the quantity $(1 - f)^2 J_{\text{sm}}(0)$ always dominates (at least by a factor of a few) over $\langle J_{\text{subcl}}(0) \rangle$. (Recall that in our generic models, all dSphs have the same M_{300} .) The scatter in $J_{\text{tot}}(0)$ is about 4 orders of magnitude for $\gamma \in [0.0 - 1.5]$, but only a factor of 20 for $\gamma \in [0.0 - 1.0]$. Beyond a few tenths of degrees, $\langle J_{\text{subcl}} \rangle$ dominates. The crossing point depends on a combination of the clump mass fraction f , γ , r_s , d , α_{int} . The dependence of J on the two latter parameters are discussed in Appendix C. The radial dependence is as expected: the smooth contribution decreases faster than that of the sub-clump one, because the signal is proportional to the squared spatial distribution in the first case, but directly proportional to the spatial distribution in the second case. Halving f to match the fraction from N-body simulations would have a 25% effect on $(1 - f)^2 J_{\text{sm}}$, but decrease J_{subcl} by a factor 4, so that the cross-over between the two components would occur at a larger angle in Fig. 4.

2.3.2 Boost factor

Whether or not the signal is boosted by the sub-clump population is still debated in the literature (Strigari et al. 2007; Kuhlen et al. 2008; Pieri et al. 2008; Pieri et al. 2009). As underlined in the previous sections, the sub-clump contribution towards the dSph centre never dominates over the smooth one if the spatial profile of the sub-clumps follows that of the smooth distribution, and if the integration angle remains below some critical angle discussed below.

Let us first define properly the parameters with respect to which this boost is calculated, as there is sometimes some confusion about this. Here, we define it with respect to the integration angle α_{int} (the pointing direction is still towards the dSph centre):

$$B(\alpha_{\text{int}}) \equiv \frac{(1 - f)^2 J_{\text{sm}}(\alpha_{\text{int}}) + J_{\text{subcl}}(\alpha_{\text{int}})}{J_{\text{sm}}(\alpha_{\text{int}})}. \quad (10)$$

In most studies, the boost has been calculated by integrating out to the clump boundary (i.e., $\alpha_{\text{int}}^{\text{all}} = R_{\text{vir}}/d$). But the boost depends

⁵ More details about the clump distributions can be found in Appendix B2. See also, e.g., Section 2 in Lavalley et al. (2008) and references therein, as we use the same definitions as those given in that paper.

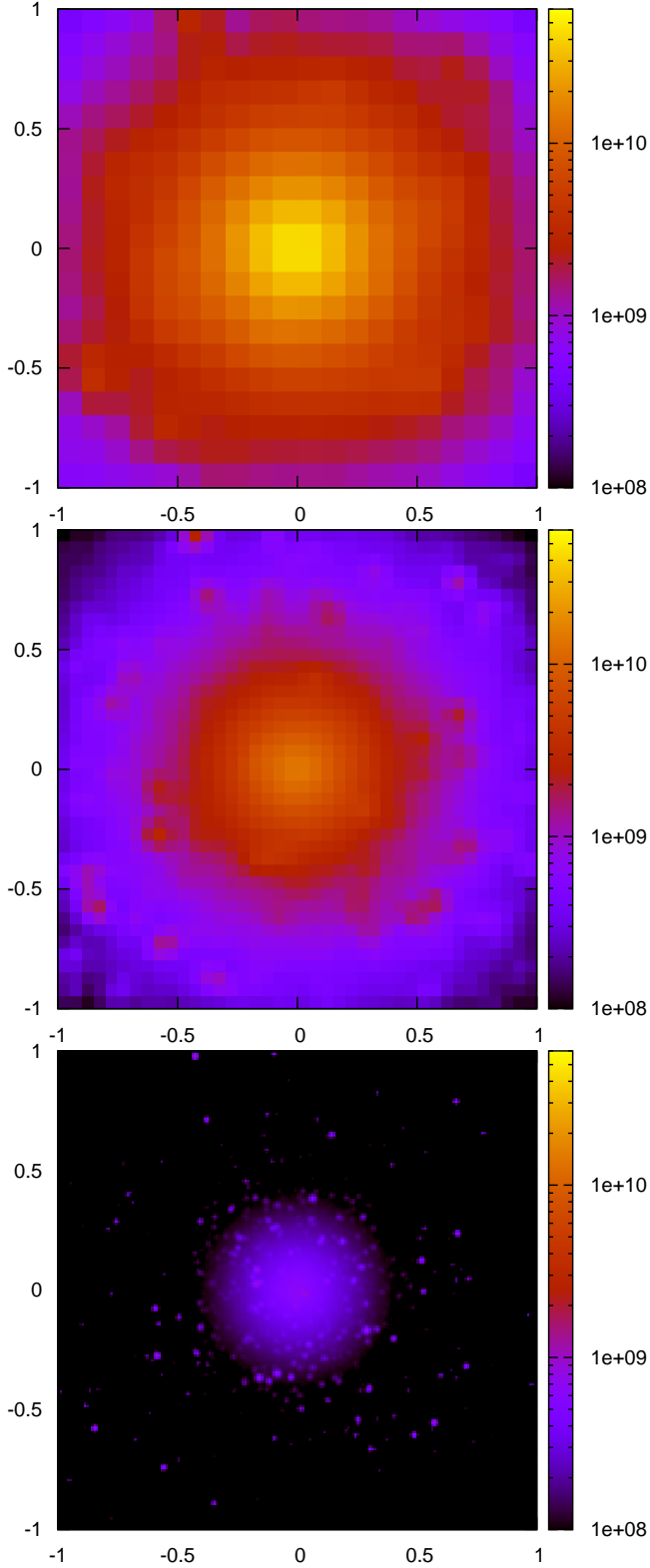


Figure 3. 2D view (x and y axis are in degrees) of J for the generic dSph with $\gamma = 0$ and $r_s = 1$ kpc at $d = 100$ kpc ($M_{300} = 10^7 M_\odot$). The sub-clumps are drawn from the reference model described in Section 2.2.3, i.e. $f=20\%$, sub-clump distribution follows smooth, and sub-clump inner profiles have NFW with B01 concentration. From top to bottom panel: $\alpha_{\text{int}} = 0.1^\circ$, 0.05° , and 0.01° . For the sake of comparison, the same colour scale is taken for the three integration angles (J is in units of $M_\odot^2 \text{ kpc}^{-5}$).

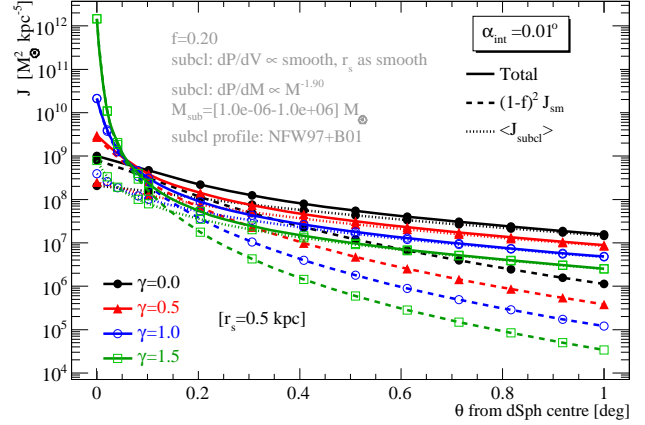


Figure 4. J as a function of the angle θ away from the dSph centre for a dSph at 100 kpc with $r_s = 0.5$ kpc (ρ_s is given in Table 1). The integration angle is $\alpha_{\text{int}} = 0.01^\circ$. For the four inner slope values γ , the various contributions to J are shown as solid (total), dashed (smooth), and dotted lines (sub-clumps).

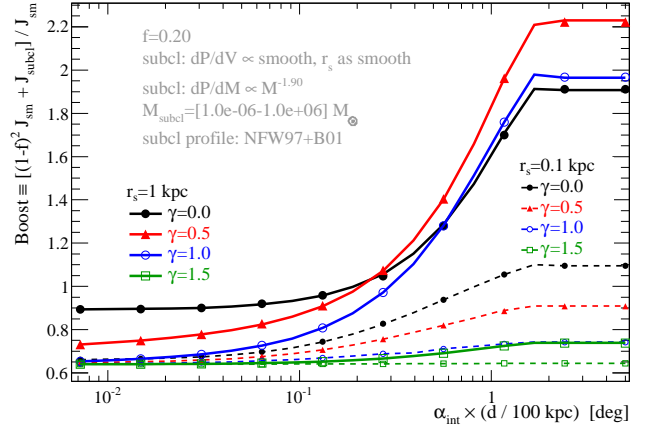


Figure 5. Boost factor as a function of $\alpha_{\text{int}} \times (d/100 \text{ kpc})$ for profiles sub-clumps follow smooth (see Section 2.2.3): the dSph is at $d = 100$ kpc (lines) or $d = 10$ kpc (symbols).

crucially on α_{int} (the radial dependence of the smooth and sub-clump contributions differ, see Section 2.3.1).

We plot in Fig. 5 the boost for different inner slopes γ , where a direct consequence of Eq. (C7) is the $\alpha_{\text{int}} \times d$ rescaling. For $r_s \lesssim 0.1$ kpc (regardless of γ), or for $\gamma \gtrsim 1.5$ (regardless of r_s), the signal is never boosted.⁶ For small enough α_{int} , B is smaller than unity, and if γ is steep enough, $B \approx (1-f)^2$. For large values, a plateau is reached as soon as $\alpha_{\text{int}} d \gtrsim R_{\text{vir}}$ (taken to be 3 kpc here). In between, the value of the boost depends on r_s and γ of the smooth component. Going beyond this qualitative description is difficult, as the toy model formulae of Appendix B2 gives results

⁶ The difference between the level of boost observed for $r_s = 0.1$ kpc or $r_s = 1$ kpc can be understood if we recall that the total mass of the clump is fixed at 300 pc, regardless of the value of γ or r_s . For $r_s = 0.1$ kpc, $\rho_s \sim \mathcal{O}(10^9 M_\odot \text{ kpc}^{-3})$, whereas for $r_s = 1$ kpc, $\rho_s \sim \mathcal{O}(10^7 M_\odot \text{ kpc}^{-3})$. As $J_{\text{sm}} \propto \rho_s^2$ whereas $J_{\text{sub}} \propto \rho_s$, the relative amount of J_{sub} with respect to J_{sm} is expected to decrease with smaller r_s . This is indeed what we observe in the figure (solid vs dashed lines).

correct to only a factor of ~ 2 (which is inadequate to evaluate the boost properly).

To conclude, the maximum value for sub-clump *follows* smooth is $\lesssim 2$, and this value is reached only when integrating the signal out to R_{vir}/d . The boost could still be increased by varying the sub-clump properties (e.g., taking a higher concentration). Conversely, if dynamical friction has caused the sub-clump population to become much more centrally concentrated than the smooth component, then the boost is decreased. This is detailed in Appendix D. For the most realistic configurations, there is *no* significant boost when a clump mass fraction $f = 20\%$ is used. Naturally this result is even more true for the smaller f found in N-body simulations so we disregard the boost for the rest of this paper and consider only the smooth contribution.

3 SENSITIVITY OF PRESENT/FUTURE γ -RAY OBSERVATORIES

Major new ground-based γ -ray observatories are in the planning stage, with CTA (CTA Consortium 2010) and AGIS (AGIS Collaboration 2010) as the main concepts. As the designs of these instruments are still evolving, we adopt here generic performance curves (described below), close to the stated goals of these projects. For the Large Area Telescope (LAT) of the Fermi γ -ray satellite, the performance for 1 year observations of point-like, high Galactic latitude sources is known (Fermi-LAT Collaboration 2010), but no information is yet available for longer exposures or for extended objects. We therefore adopt a toy likelihood-based model for the Fermi sensitivity, tuned to reproduce the 1 year point-source curves. We note that whilst this approach results in approximate performance curves for both the ground- and space-based instruments, it captures the key differences (in particular the differences in collection area and angular resolution) and illustrates the advantages and limitations of the two instrument types, as well as the prospects for the discovery of DM annihilation in dSphs within the next decade.

3.1 Detector models

The sensitivity of a major future γ -ray observatory based on an array of Cherenkov Telescopes (FCA in the following, for ‘Future Cherenkov Array’) is approximated based on the point-source differential sensitivity curve (for a 5σ detection in 50 hours of observations) presented by Bernlöhner et al. (2008). Under the assumption that the angular resolution of such a detector is a factor 2 better than HESS (Funk et al. 2008) and has the same energy-dependence, and that the effective collection area for γ -rays grows from 10^4 m^2 at 30 GeV to 1 km^2 at 1 TeV, the implied cosmic-ray (hadron and electron) background rate per square degree can be inferred and the sensitivity thus adapted to different observation times, spectral shapes and source extensions. Given that the design of instruments such as CTA are not yet fixed, we consider that such a simplified response, characterised by the following functions is a useful tool to explore the capabilities of a generic next-generation instrument:

$$\text{LS} = -13.1 - 0.33 X + 0.72 X^2, \quad (11)$$

$$\text{LA} = 6 + 0.46 X - 0.56 X^2, \quad (12)$$

$$\psi_{68} = 0.038 + \exp(-(X + 2.9)/0.61), \quad (13)$$

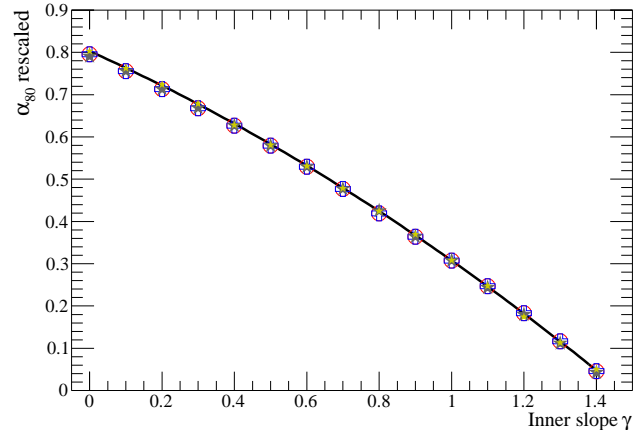


Figure 6. The cone angle encompassing 80% of the annihilation flux at as function of the inner slope γ . Several different values of r_s and distance d are shown for each γ , all scaled by $(1 \text{ kpc}/r_s$ and $100 \text{ kpc}/d)$. The best-fit curve is also shown, corresponding to Eq. (16).

where

$$X = \log_{10}(\text{PhotonEnergy}/\text{TeV}), \quad (14)$$

$\text{LS} = \log_{10}(\text{Differential Sensitivity}/\text{erg cm}^{-2} \text{ s}^{-1})$, $\text{LA} = \log_{10}(\text{EffectiveArea}/\text{m}^2)$, and ψ_{68} is the 68% containment radius of the point-spread-function (PSF) in degrees.

For the Fermi detector a similar simplified approach is taken, the numbers used below being those provided by Fermi-LAT Collaboration (2010). The effective area changes as a function of energy and incident angle to the detector, reaching a maximum of $\approx 8000 \text{ cm}^2$. The effective time-averaged area is then $\epsilon A \Omega / 4\pi$ and the data-taking efficiency $\epsilon \approx 0.8$ (due to instrument dead-time and passages through the South Atlantic Anomaly). The point spread function again varies as a function of energy (with a much smaller dependence as a function of incidence angle) varying from 10 degrees to a few tenths of a degree over the LAT energy range. A rate of $1.5 \times 10^{-5} \text{ cm}^{-2} \text{ s}^{-1} \text{ sr}^{-1}$ ($> 100 \text{ MeV}$) and a photon index of 2.1 are assumed for the background. The sensitivity is then estimated using a simplified likelihood method which provides results within 20% of the sensitivity for a one year observation of a point-like source given by Fermi-LAT Collaboration (2010).

Whilst both detector responses are approximate, the comparison is still useful. Our work incorporates several key aspects not considered in earlier studies, including the strong energy dependence of the angular resolution of both ground and space based instruments in the relevant energy range of 1 GeV to 1 TeV and hence the energy-dependent impact of the angular size of the target region.

3.2 Relative performance for generic halos

Using the results from Section 2.2.2 and the detector performance models defined above we can begin to investigate the sensitivity of future ACT arrays and the Fermi-LAT detector (over long observation times) to DM annihilation in dSphs. The detectability of a source depends primarily on its flux, but also on its angular extent. The impact of source extension on detectability is dealt with approximately (in each energy bin independently) by assuming that the opening angle of a cone which incorporates 80% of the signal

is given by

$$\theta_{80} = \sqrt{\psi_{80}^2 + \alpha_{80}^2}, \quad (15)$$

where $\psi_{80} = 1.25 \psi_{68}$ is assumed for the FCA and interpolated from values given for 68% and 95% containment for the LAT Fermi-LAT Collaboration (2010); here α_{80} is the 80% containment angle of the halo emission. The validity of this approximation (at the level of a few percent) has been tested (see Appendix E) by convolving realistic halo profiles with a double Gaussian PSF as found for HESS (Horns 2005). An 80% integration circle is close to optimum for a Gaussian source on a flat background (in the background limited regime). Fig. 6 shows the 80% containment radius of the annihilation flux of generic halos as a function of the inner slope γ . This result can be parametrised as:

$$\alpha_{80} = 0.8^\circ (1 - 0.48\gamma - 0.137\gamma^2) \left(\frac{r_s}{1 \text{ kpc}}\right) \left(\frac{d}{100 \text{ kpc}}\right)^{-1}. \quad (16)$$

It is clear that for a broad range of d , γ and r_s the characteristic angular size of the emission region is *larger* than the angular resolution of the instruments under consideration. It is therefore critical to assess the performance as a function of the angular size of the dSph as well as the mass of the annihilating particle.

Fig. 7 shows the relative sensitivity of Fermi and an FCA within our framework as a function of the mass of the annihilating particle, adopting the annihilation spectrum given in Eq. (4), with the several panels illustrating different points. From Fig. 7 top (the case of a point-like signal for different observation times) it is clear that Fermi-LAT has a considerable advantage for lower mass DM particles ($m_\chi \ll 1$ TeV) on the timescale for construction of an FCA (i.e. over a 5-10 year mission lifetime) in comparison to a deep ACT observation of 200 hours. Furthermore, Fermi-LAT is less adversely affected by the angular extent of the target regions (see Fig. 7 bottom), due to its modest angular resolution in the energy range where it is limited by background, meaning that the source extension is well matched to the PSF of the instrument. The middle panel of this figure illustrates the impact of different approaches to the analysis. In the case that there is a DM candidate inferred from the discovery of supersymmetry at the LHC (quite possible on the relevant timescale) a search optimised on an assumed mass and spectral shape can be made (solid curves). However, all instruments are less sensitive when a generic search is undertaken. Simple analyses using all the photon flux above a fixed energy threshold (arbitrarily set to reduce background) are effective only in a relatively narrow range of particle mass. For example keeping only >100 GeV photons works well for ACTs for 0.3-3 TeV particles; whereas keeping all photons >1 GeV works moderately well in the 0.1-0.2 TeV range, but is much less sensitive than the higher threshold cut over the rest of the candidate dark matter particle mass range. The features of these curves are dictated by the expected shape of the annihilation spectrum. From Eq. (4) the peak photon output (adopting the average spectrum for DM annihilation) occurs at an energy which is an order of magnitude below the particle mass – effective detection requires that this peak occurs within (or close to) the energy range of the instrument concerned.

The total annihilation flux from a dSph increases at smaller distances as $1/d^2$ for fixed halo mass, making nearby dSphs attractive for DM detection. However, as Fig. 7 shows, the increased angular size of such nearby sources raises the required detection flux. Fig. 8 illustrates the reduction in sensitivity for an FCA with respect to a point-like source for generic dSph halos as a function of distance, for inner slopes, γ , of zero and one and with r_s fixed to

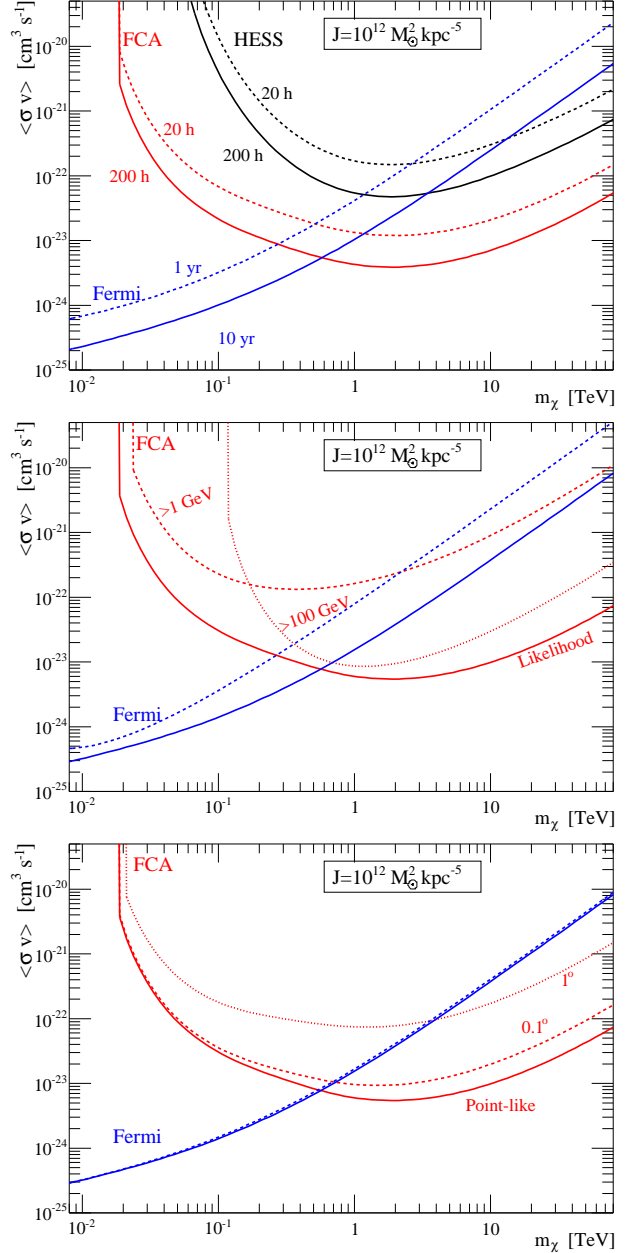


Figure 7. Approximate sensitivities of Fermi-LAT (blue lines), HESS (black lines) and the FCA described above (red lines) to a generic halo with $J = 10^{12} M_\odot^2 \text{ kpc}^{-5}$, as a function of the mass of the annihilating particle and for the annihilation spectrum of Eq. (4). **Top:** The impact of observation time is illustrated: dashed lines give the 1 year and 20 hour sensitivities for Fermi and FCA/HESS respectively while the solid lines refer to 10 year (200 hour) observations. **Middle:** the impact of analysis methods is considered for 5 year (100 hour) observations using Fermi (FCA). Solid lines show likelihood analyses in which the mass and spectrum of the annihilating particle are known in advance, while dashed and dotted lines show simple integral flux measurements above fixed thresholds of 1 GeV (dashed) and 100 GeV (dotted). Note that the 1 GeV cut implies accepting all events for the FCA (where the trigger threshold is ≈ 20 GeV). **Bottom:** the impact of the angular extension of target sources, as given by the halo profile in Fig. 6 is illustrated. The solid lines reproduce the likelihood case from the middle panel for a point-like source, and with values of α_{80} of 0.1° (dashed) and 1° also shown.

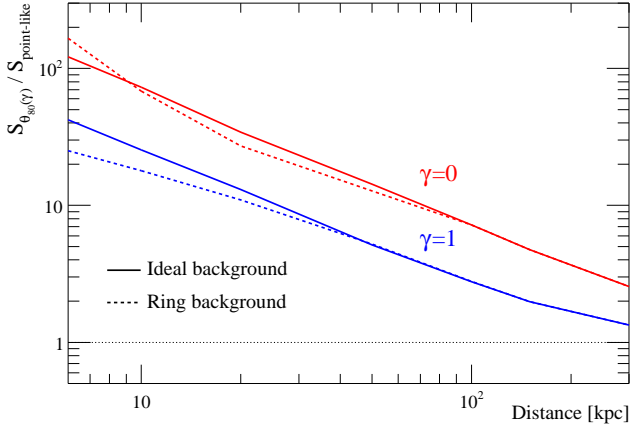


Figure 8. Relative DM annihilation detection sensitivity for a 100 hour FCA observation, as a function of dSph distance for different inner slopes γ and with r_s fixed to 1 kpc. The sensitivity for a realistic approach using θ_{80} is given relative to the sensitivity to a point-like source with the same flux. Larger values correspond to poorer performance (larger values of the minimum detectable flux). The assumed spectral shape is again as given by Eq. (4) with $m_\chi = 300$ GeV. This sensitivity ratio depends on the strategy used to estimate the background level at the dSph position. The dashed lines show the impact of using an annulus between 3.5° and 4.0° of the dSph centre as a background control region. The solid line assumes that the background control region lies completely outside the region of emission from the dSph.

1 kpc, relative to the assumption of the full annihilation signal and a point-like source. Even for $\gamma = 1$, the point-like approximation leads to an order of magnitude overestimate of the detection sensitivity for nearby (~ 20 kpc) dSphs. A further complication is how to establish the level of background emission arising from the residual non- γ -ray background. A common method in ground-based γ -ray astronomy is to estimate this background from an annulus around the target source (see, e.g., Berge et al. 2007). The dashed lines in Fig. 8 show the impact of estimating the background using an annulus between 3.5° and 4.0° from the target. This approach has a modest impact on sensitivity and is ignored in the following discussions as it reduces the detectable flux but also θ_{80} and leads to a small improvement in some cases.

4 JEANS/MCMC ANALYSIS OF DSPH KINEMATICS

4.1 dSph kinematics with the spherical Jeans equation

Extensive kinematic surveys of the stellar components of dSphs have shown that these systems have negligible rotational support (with the possible exception of the Sculptor dSph, see Battaglia et al. 2008). If we assume that the dSphs are in virial equilibrium, then their internal gravitational potentials balance the random motions of their stars. In order to estimate dSph masses, we consider here the behaviour of dSph stellar velocity dispersion as a function of distance from the dSph centre (analogous to rotation curves of spiral galaxies). Specifically, we use the stellar kinematic data of Walker et al. (2009) for the Carina, Fornax, Sculptor and Sextans dSphs, the data of Mateo et al. (2008) for the Leo I dSph, and data from Mateo et al. (in preparation) for the Draco, Leo II and Ursa Minor dSphs. Walker et al. (2009, W09 hereafter) have calculated velocity dispersion profiles from these same data under the assumption that l.o.s. velocity distributions are Gaussian.

Here we re-calculate these profiles without adopting any particular form for the velocity distributions. Specifically, for a given dSph we divide the velocity sample into circular bins containing approximately equal numbers of member stars,⁷ and within each bin we estimate the second velocity moment (squared velocity dispersion) as:

$$\langle \hat{V}^2 \rangle = \frac{1}{N-1} \sum_{i=1}^N [(V_i - \langle \hat{V} \rangle)^2 - \sigma_i^2], \quad (17)$$

where N is the number of member stars in the bin. We hold $\langle V \rangle$ fixed for all bins at the median velocity over the entire sample. For each bin we use a standard bootstrap re-sampling to estimate the associated error distribution for $\langle \hat{V}^2 \rangle$, which is approximately Gaussian. Fig. 9 displays the resulting velocity dispersion profiles, $\langle \hat{V}^2 \rangle^{1/2}(R)$, which are similar to previously published profiles.

In order to relate these velocity dispersion profiles to dSph masses, we follow W09 in assuming that the data sample in each dSph a single, pressure-supported stellar population that is in dynamical equilibrium and traces an underlying gravitational potential dominated by dark matter. Implicit is the assumption that the orbital motions of stellar binary systems contribute negligibly to the measured velocity dispersions.⁸ Furthermore, assuming spherical symmetry, the mass profile, $M(r)$, of the DM halo relates to (moments of) the stellar distribution function via the Jeans equation:

$$\frac{1}{\nu} \frac{d}{dr} (\nu \bar{v}_r^2) + 2 \frac{\beta(r) \bar{v}_r^2}{r} = - \frac{GM(r)}{r^2}, \quad (18)$$

where $\nu(r)$, $\bar{v}_r^2(r)$, and $\beta_r \equiv \beta(r) \equiv 1 - \bar{v}_\theta^2 / \bar{v}_r^2$ describe the 3-dimensional density, radial velocity dispersion, and orbital anisotropy, respectively, of the stellar component. Projecting along the l.o.s., the mass profile relates to observable profiles, the projected stellar density $I(R)$ and velocity dispersion $\sigma_p(R)$, according to (Binney & Tremaine 2008, BT08 hereafter)

$$\sigma_p^2(R) = \frac{2}{I(R)} \int_R^\infty \left(1 - \beta_r \frac{R^2}{r^2} \right) \frac{\nu \bar{v}_r^2 r}{\sqrt{r^2 - R^2}} dr. \quad (19)$$

Notice that while we observe the projected velocity dispersion and stellar density profiles directly, the l.o.s. velocity dispersion profiles provide *no* information about the anisotropy, $\beta(r)$. Therefore we require an assumption about $\beta(r)$; here we assume $\beta = \text{constant}$, allowing for nonzero anisotropy in the simplest way. For constant anisotropy, the Jeans equation has the solution (e.g., Mamon & Łokas 2005):

$$\nu \bar{v}_r^2 = Gr^{-2\beta_r} \int_r^\infty s^{2\beta_r-2} \nu(s) M(s) ds. \quad (20)$$

We shall adopt parametric models for $I(R)$ and $M(r)$ and then find values of the parameters of $M(r)$ that, via Eqs. (19) and (20), best reproduce the observed velocity dispersion profiles.

⁷ Kinematic samples are often contaminated by interlopers from the Milky Way foreground. Following W09, we discard all stars for which the algorithm described by Walker et al. (2009) returns a membership probability less than 0.95.

⁸ Olszewski et al. (1996) and Hargreaves et al. (1996) conclude that this assumption is valid for the classical dSphs studied here, which have measured velocity dispersions of ~ 10 km s⁻¹. This conclusion does not necessarily apply to recently-discovered ‘ultra-faint’ Milky Way satellites, which have measured velocity dispersions as small as ~ 3 km s⁻¹ (McConnachie & Côté 2010).

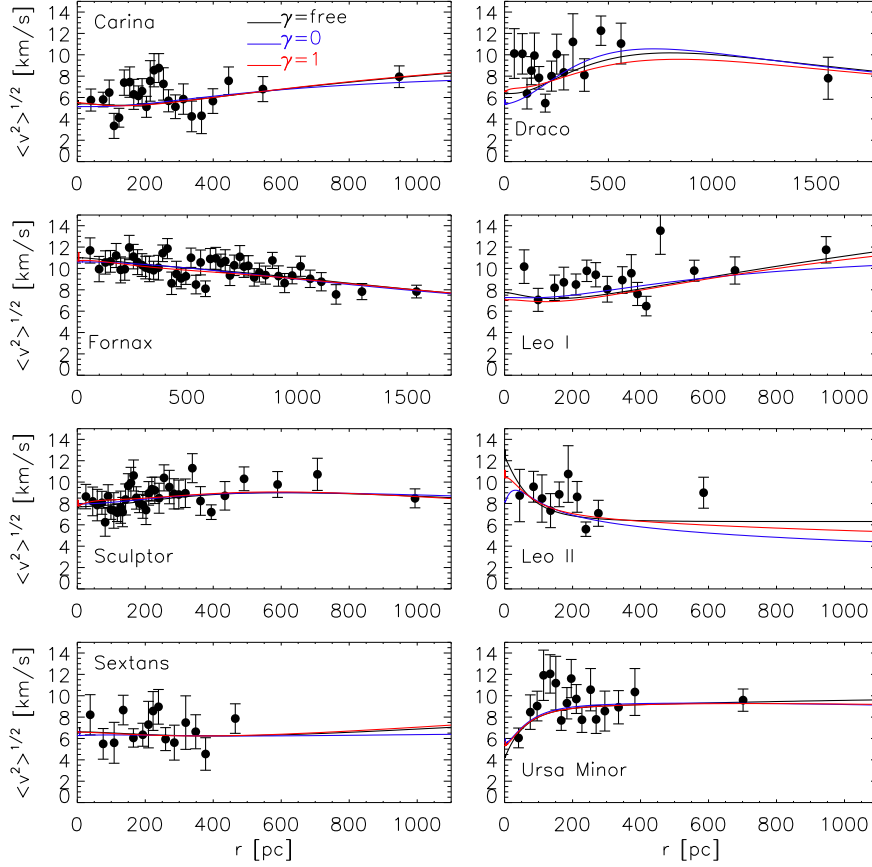


Figure 9. Velocity dispersion profile data for the 8 classical dSphs, obtained as described in the text (the impact of the binning choice is discussed in Appendix H1). The solid lines correspond to the best-fit models for the inner slope when γ is left free (dark), γ is fixed to 1 (blue), and γ is fixed to 0 (red). Because of the large degeneracies among the halo parameters (see Section 5.1 for a list), we do not list the corresponding best-fit parameters. The motivation for showing these profiles is to illustrate that our halo model is capable of describing the kinematic data, and that the inner profile is not constrained by the data.

4.1.1 Stellar Density

Stellar surface densities of dSphs are typically fit by Plummer (1911), King (1962) and/or Sersic (1968), profiles (e.g., Irwin & Hatzidimitriou 1995). For simplicity, we adopt here the Plummer profile:

$$I(R) = \frac{L}{\pi r_{\text{half}}^2} \frac{1}{[1 + R^2/r_{\text{half}}^2]^2}, \quad (21)$$

which has just two free parameters: the total luminosity L and the projected⁹ half-light radius r_{half} . Given spherical symmetry, the Plummer profile implies a 3-dimensional stellar density (BT08) of:

$$\nu(r) = -\frac{1}{\pi} \int_r^\infty \frac{dI}{dR} \frac{dR}{\sqrt{R^2 - r^2}} = \frac{3L}{4\pi r_{\text{half}}^3} \frac{1}{[1 + r^2/r_{\text{half}}^2]^{5/2}}. \quad (22)$$

Since we assume that DM dominates the gravitational potential at all radii (all measured dSphs have central mass-to-light ratios $\gtrsim 10$, e.g., Mateo 1998), the value of L has no bearing on our analysis. We adopt values of r_{half} (and associated errors) from Table 1 in the published erratum to W09; these data originally come from the star count study of Irwin & Hatzidimitriou (1995). We have checked

⁹ For consistency with Walker et al. (2009) we define r_{half} as the radius of the circle enclosing half of the dSph stellar light as seen in projection. Elsewhere this radius is commonly referred to as the ‘effective radius’.

that a steeper outer slope or a steeper inner slope for the light profile leaves unchanged the conclusions (see Appendix H2).

4.1.2 Dark matter halo

For the DM halo we follow W09 in using a generalised Hernquist profile, as given by Eq. (6). In terms of these parameters, i.e. the density ρ_s at scale radius r_s , plus the (outer, transition, inner) slopes (α, β, γ), the mass profile is:

$$M(r) = 4\pi \int_0^r s^2 \rho(s) ds = \frac{4\pi \rho_s r_s^3}{3 - \gamma} \left(\frac{r}{r_s}\right)^{3-\gamma} {}_2F_1 \left[\frac{3-\gamma}{\alpha}, \frac{\beta-\gamma}{\alpha}; \frac{3-\gamma+\alpha}{\alpha}; -\left(\frac{r}{r_s}\right)^\alpha \right], \quad (23)$$

where ${}_2F_1(a, b; c; z)$ is Gauss’ hypergeometric function.

Eq. (6) includes plausible halo shapes ranging from the constant-density ‘cores’ ($\gamma = 0$) that seem to describe rotation curves of spiral and low-surface-brightness galaxies (e.g., de Blok 2010 and references therein) to the centrally divergent ‘cusps’ ($\gamma > 0$) motivated by cosmological N-body simulations that model only the DM component. For $(\alpha, \beta, \gamma) = (1, 3, 1)$ Eq. (6) is just the cuspy NFW (Navarro, Frenk & White 1996, 1997) profile.

4.2 Markov-Chain Monte Carlo Method

For a given halo model we compare the projected (squared) velocity dispersion profile $\sigma_p^2(R)$ (obtained from Eq. 19) to the empirical profile $\langle \hat{V}^2 \rangle(R)$ (displayed in Fig. 9) using the likelihood function

$$\zeta = \prod_{i=1}^N \frac{1}{\sqrt{2\pi \text{Var}[\langle \hat{V}^2 \rangle(R_i)]}} \exp \left[-\frac{1}{2} \frac{(\langle \hat{V}^2 \rangle(R_i) - \sigma_p^2(R_i))^2}{\text{Var}[\langle \hat{V}^2 \rangle(R_i)]} \right], \quad (24)$$

where $\text{Var}[\langle \hat{V}^2 \rangle(R_i)]$ is the variance associated with the empirical mean square velocity, as estimated from our bootstrap re-sampling.

In order to explore the large parameter space efficiently, we employ Markov-chain Monte Carlo (MCMC) techniques. That is, we use the standard Metropolis-Hastings algorithm (Metropolis et al. 1953; Hastings 1970) to generate posterior distributions according to the following prescription: 1) from the current location in parameter space, S_n , draw a prospective new location, S' , from a Gaussian probability density centred on S_n ; 2) evaluate the ratio of likelihoods at S_n and S' ; and 3) if $\zeta(S')/\zeta(S_n) \geq 1$, accept such that $S_{n+1} = S'$, else accept with probability $\zeta(S')/\zeta(S_n)$ and $S_{n+1} = S_n$ with probability $1 - \zeta(S')/\zeta(S_n)$. In order to account for the observational uncertainty associated with the half-light radius adopted from Irwin & Hatzidimitriou (1995), for each new point we scatter the adopted value of r_{half} by a random deviate drawn from a Gaussian distribution with standard deviation equal to the published error. This method effectively propagates the observational uncertainty associated with the half-light radius to the posterior distributions for our model parameters.

Solutions of the Jeans equations are not guaranteed to correspond to physical models, as the associated phase-space distribution functions may not be everywhere positive. An & Evans (2006) have derived a necessary relation between the asymptotic values of the logarithmic slope of the gravitational potential, the tracer density distribution and the velocity anisotropy at small radii. Models which do not satisfy this relation will not give rise to physical distribution functions. In terms of our parametrisation, this relation becomes

$$\gamma_{\text{tracer}} \gtrsim 2\beta_{\text{aniso}}. \quad (25)$$

We therefore exclude from the Markov Chain those models which do not satisfy this condition. Because the Plummer profiles we use to describe dSph surface brightness profiles have $\gamma_{\text{tracer}} = 0$, this restriction implies $\beta_{\text{aniso}} \lesssim 0$. Given our assumption of constant velocity anisotropy, this disqualifies all radially anisotropic models. Relaxing this condition affects the results on the J -factors, but the difference is contained within their CLs (see Appendix H2).

For this procedure we use the adaptive MCMC engine CosmoMC (Lewis & Bridle 2002).¹⁰ Although it was developed specifically for analysis of cosmic microwave background data, CosmoMC provides a generic sampler that continually updates the probability density according to the parameter covariances in order to optimise the acceptance rate. For each galaxy and parametrisation we run four chains simultaneously, allowing each to proceed until the variances of parameter values across the four chains become less than 1% of the mean of the variances. Satisfying this convergence criterion typically requires $\sim 10^4$ steps for our chains. We then estimate the posterior distribution in parameter space using the last half of all accepted points (we discard the first half of

points, which we conservatively assume corresponds to the ‘burn-in’ period).

5 DETECTABILITY OF MILKY WAY DSPHS

This section provides our key results. For the benefit of readers who start reading here, we summarise our findings so far.

In Section 2, we focused on generic $(1, 3, \gamma)$ profiles, to show that, most of the time, the sub-structure contribution is negligible, and to check that the only relevant dSph halo parameters are the density normalisation ρ_s , the scale radius r_s , and the inner slope γ (because $J_{\text{dSph}} \propto r_s^{2\gamma} \times (\alpha_{\text{int}} d)^{3-2\gamma}$, see also Appendix B).

In Section 3, we provided the sensitivity of present and future γ -ray observatories, showing how it is degraded when considering ‘extended’ sources (e.g. a flat profile for close dSphs), and an instrument response that varies with energy.

In Section 4, we presented our method to perform a Markov-Chain Monte Carlo analysis of the observed stellar kinematics in the 8 classical Milky Way dSphs under the assumptions of virial equilibrium, spherical symmetry, constant velocity anisotropy, and a Plummer light distribution. The analysis uses the observed velocity dispersion profiles of the dSphs to constrain their underlying dark matter halo potentials, parametrised using the five parameter models of Eq. (6).

5.1 6-parameter MCMC analysis—varying γ

Our kinematic models have six free parameters, for which we adopt uniform priors over the following ranges:

$$\begin{aligned} -\log_{10}[1 - \beta_{\text{ani}}] &: [-1, +1]; \\ \log_{10}[\rho_s / (M_{\odot} \text{pc}^{-3})] &: [-10, +4]; \\ \log_{10}[r_s / \text{pc}] &: [0, 4]; \\ \alpha &: [0.5, 3]; \\ \beta &: [3, 7]; \\ \gamma &: [0, 2] \text{ or } [0, 1]; \end{aligned}$$

The anisotropy parameter β_{ani} does not enter directly the profile/mass/ J calculation, although it is of fundamental importance for the fit as it can correlate with the DM profile structure parameters (so with the mass and the J -factor). We have not checked explicitly the details of these correlations, but we have checked that restricting the range of possible β_{ani} does not significantly impact on the results for the J calculation. Hence, we do not discuss this parameter further below.

5.1.1 Parameter correlations

Fig. 10 shows the marginalised probability density functions (PDFs) of the profile parameters and the joint distributions of pairs of parameters. The features of these plots are driven by the fact that most of the stellar kinematic data lie at radii of up to few hundred parsecs (see Fig. 9). For instance, the outer slope β is not at all constrained (i.e. the fit is insensitive to the value of β), because only tracers beyond a radius of $r \gtrsim 1$ kpc are sensitive to this parameter and these radii are sparsely sampled by the observations. The transition slope α and then the inner slope γ are the two other least constrained parameters. In terms of best-fit models, as seen in Fig. 9, the match to kinematics data is equally good for varying

¹⁰ available at <http://cosmologist.info/cosmomc>

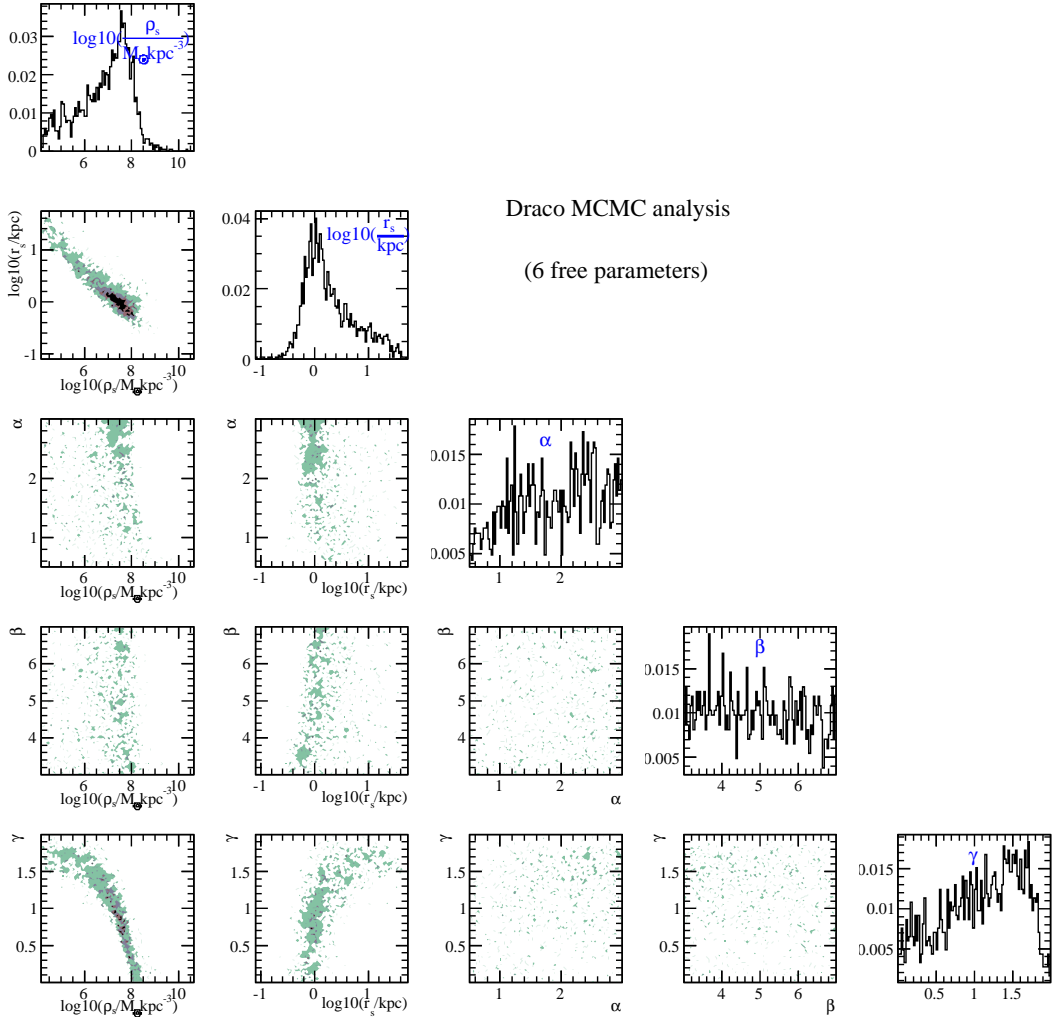


Figure 10. Joint distributions and marginalised PDFs of parameters entering the MCMC for the Draco dSph. The off-diagonal plots show joint distributions that highlight correlations between the parameters, while the on-diagonal plots are the marginalised PDFs of the parameters. This marginalisation includes the marginalisation over the velocity anisotropy parameter β_{ani} . (We do not plot a marginalised PDF or correlation for β_{ani} since it is a nuisance parameter for our analysis here.)

γ (black) models and models in which we fix the value to $\gamma = 0$ (blue), or $\gamma = 1$ (red). In the following, we will not discuss further the best-fit values. The more meaningful quantity, in the context of an MCMC analysis providing PDFs, is the *median* of the distribution.

Several groups have shown recently that in a Jeans analysis, the observed flatness of dSph velocity dispersion profiles (Walker et al. 2007) leads to a constraint on $M(r_{\text{half}})$ —the mass enclosed within a sphere of radius r_{half} —that is insensitive to assumptions about either anisotropy or the structural parameters of the DM halo (Walker et al. 2009; Wolf et al. 2010). Using for the appropriate radius the mass estimate Eq. (9) and the above constraint leads to a relation between the profile parameters

$$\log(\rho_s) + \gamma \log(r_s) \approx \text{constant}.$$

This relation explains the approximately linear correlations between these parameters seen, for instance, in the bottom left panel of Fig. 10.

5.1.2 From $\rho(r)$ to $J(\alpha_{\text{int}})$: uncertainty and impact of γ_{prior}

Fig. F1 shows the density profile for Draco as recovered by our MCMC analysis. It is noticeable that the confidence limits are narrower for radial scales of a few hundreds pc—this is a common feature of the density profile confidence limits for all the dSphs we have considered. As discussed above, this is partly due to the fact that these are the radii at which the majority of the kinematic data lie. The least constrained $\rho(r)$ (less pronounced narrowing of the confidence limits) is that of Sextans, for which the range where useful data can be found is clearly the smallest compared to other dSphs (see Fig. 9).

The variation of the constraints on $\rho(r)$ as a function of radius impacts directly on the behaviour of J . Complications arise because it is the profile squared that is now integrated along a l.o.s. (given the integration angle α_{int} , see Eq. 5). The median value and 95% CL on J as a function of the integration angle α_{int} is plotted in Fig. 11 (top), for two different priors on γ_{prior} . The bottom panel gives the corresponding PDF for two integration angles. The prior has a strong impact on the result: the median (thick solid

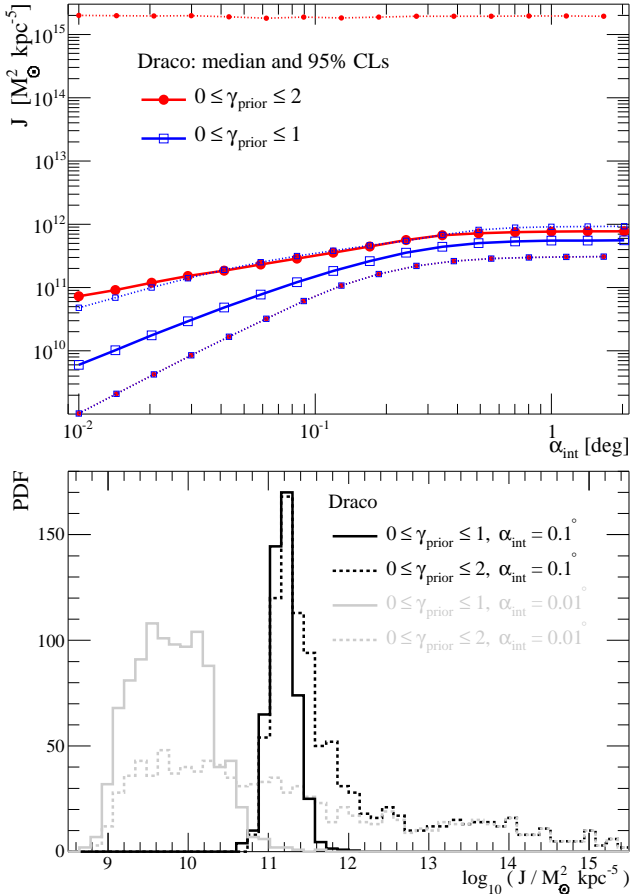


Figure 11. *Top:* $J(\alpha_{\text{int}})$ for Draco as a function of the integration angle. Solid lines correspond to the median model, dotted lines to the 95% lower and upper CL. The two sets of curves correspond to two different γ_{prior} for the MCMC analysis on the same data. *Bottom:* PDF of the J-factor for $\alpha_{\text{int}} = 0.01^\circ$ (grey) and $\alpha_{\text{int}} = 0.1^\circ$ (black), when the range of the inner slope prior is $[0 - 1]$ (solid lines) or $[0 - 2]$ (dashed lines).

curves and large symbols – top panel) is changed by $\sim 50\%$ for $\alpha_{\text{int}} \gtrsim 0.1^\circ$, but by a factor of ten for $\alpha_{\text{int}} \sim 0.01^\circ$. However, the most striking feature is the difference between the CLs: for the prior $0 \leq \gamma_{\text{prior}} \leq 2$, the typical uncertainty is 3 to 4 orders of magnitude (red dotted curves), whereas it is only \lesssim than one order of magnitude for the prior $0 \leq \gamma_{\text{prior}} \leq 1$ (blue dotted curves).¹¹ The bottom panel of Fig. 11 shows that $\log_{10} J$ has a long and flat tail (associated to large γ values). This tail is responsible for the large upper limit of the J -factor CLs for $0 \leq \gamma_{\text{prior}} \leq 2$.

In Appendix G2, a detailed analysis of the impact of these two priors is carried on artificial data (for which the true profile is known). We find that the prior $0 \leq \gamma_{\text{prior}} \leq 2$ satisfactorily reconstructs $\rho(r)$ and $J(\alpha_{\text{int}})$, i.e. the MCMC CLs bracket the true value. This is also the case when using the prior $0 \leq \gamma_{\text{prior}} \leq 1$. However, two important points are noteworthy:

- this prior obviously performs better for $0 \leq \gamma_{\text{true}} \leq 1$ profiles where it gives much tighter constraints on J ;
- for cuspy profiles (e.g., $\gamma_{\text{true}} = 1.5$), this prior succeeds slightly less (than the prior $0 \leq \gamma_{\text{prior}} \leq 2$) in reconstructing $\rho(r)$, but it does surprisingly better on J in terms of providing a value closer to the true one (see details and explanations in Appendix G2).

DM simulations and observations do not favour $\gamma > 1$, although steeper profiles can still fit the kinematic data in a Jeans analysis. Indeed, the Aquarius simulations indicate values of γ slightly smaller than 1, and although some recent simulations (Ishiyama et al. 2010) have argued for cuspy profiles, this happens for micro-haloes only. Given that the J -factor for the cuspy profiles are only marginally more (or even less) reliable when using the prior $0 \leq \gamma_{\text{prior}} \leq 2$, we restrict ourselves to the $0 \leq \gamma_{\text{prior}} \leq 1$ prior below.

Note that other sources of bias exist. First, the reconstruction of $\rho(r)$ or $J(\alpha_{\text{int}})$ is affected by the choice of binning used in the estimation of the empirical velocity dispersion profiles. Appendix H1 shows that we obtain slightly different results when we apply our method to empirical velocity dispersion profiles calculated from the same raw kinematic data, but using different numbers of bins. We find that the effects of binning add an extra factor of a few uncertainty on J for the least well measured (in terms of radial coverage) dSphs, for which more measurements are desirable. (On the other hand, Fornax and Sculptor are found to provide robust results against different binnings.) Second, we note that the analysis presented here uses a fixed profile for the light distribution which, when combined with our assumption of constant velocity anisotropy, restricts the possible halo profiles we can recover. Our constraints on $\rho(r)$ and $J(\alpha_{\text{int}})$ are therefore sensitive to these assumptions (see, e.g., Strigari et al. 2010, for an example of fitting the dSph kinematic data with cusped profiles when the light profile is also allowed to be cusped), although this does not change our conclusions (see Appendix H2 where different light profiles are used). This situation is set to change over the coming years as new distribution function-based models will permit constraints to be placed on the slope of the DM density profiles (Wilkinson et al. 2011, in prep.).

5.1.3 Best constraints on J : median value and CLs

As validated by the simulated data, we are now able to provide robust (although possibly not the best achievable with current data) and model-independent constraints on $J(\alpha_{\text{int}})$ for the 8 classical dSphs. The results are summarised in Table 2 in terms of the median, and 68% and 95% CLs. The J -factor is calculated for $\alpha_{\text{int}} = 0.01^\circ$ (an angle slightly better than what can be achieved with FCA), $\alpha_{\text{int}} = 0.1^\circ$ (typical of the angular resolution of existing GeV and TeV γ -ray instruments), and for $\alpha_c = 2r_{\text{half}}/d$ (as proposed in Walker et al. 2011). We do not report the values of ρ_s and r_s as these vary across a large range—and therefore do not give additional useful information—nor the value of γ as it is forced in the range $0 \leq \gamma_{\text{prior}} \leq 1$ to give the least biased J value.

There is no simple way to provide unambiguously the best target, as their relative merit depends non trivially on their distance, their mass and the integration angle selected. As proposed in Walker et al. (2011), since the most robust constraint on J is obtained for $\alpha_{\text{int}} = \alpha_c$, having different integration angles for each dSph can be a good starting point to establish a relative ranking. The situation is complicated further for background-limited instru-

¹¹ Note that this behaviour is grossly representative of all dSphs, although the integration angle for which the uncertainty is the smallest, and the amplitude of this uncertainty depend, respectively, on the dSph distance (see Section 2.3 for the generic dependence), and on the range/precision of the kinematic data (see above).

Table 2. Positions of the classical dSphs (Mateo 1998) sorted according to their distance: longitude, latitude, distance, $2r_{\text{half}}$ (taken from Irwin & Hatzidimitriou 1995), the galactic angle away from centre $\phi = \cos^{-1}[\cos(\text{long.})\cos(\text{lat.})]$, and $\alpha_c \approx 2r_{\text{half}}/d$ (see Walker et al. 2011). The remaining columns are the median value with 68% (95%) CLs for M_{300} and $\log_{10}[J(\alpha_{\text{int}})]$ from the six-parameter MCMC analysis ($0 \leq \gamma_{\text{prior}} \leq 1$). For conversion factors to units used in other studies, please refer to numbers given in Appendix A.

dSph	long. [deg]	lat. [deg]	d [kpc]	$2r_h$ [kpc]	ϕ [deg]	α_c [deg]	M_{300} [$10^7 M_\odot$]	$\log_{10}[J(0.01^\circ)]$	$\log_{10}[J(0.1^\circ)]$ [$M_\odot^2 \text{kpc}^{-5}$]	$\log_{10}[J^*(\alpha_c)]$
Ursa Minor	105.0	+44.8	66	0.56	100.6	0.49	$1.54^{+0.18(+0.33)}_{-0.21(-0.42)}$	$10.5^{+0.8(+1.5)}_{-0.6(-1.2)}$	$11.7^{+0.5(+0.8)}_{-0.3(-0.6)}$	$12.0^{+0.3(+0.5)}_{-0.1(-0.2)}$
Sculptor	287.5	-83.2	79	0.52	88.0	0.38	$1.34^{+0.12(+0.23)}_{-0.13(-0.23)}$	$10.0^{+0.5(+0.9)}_{-0.5(-0.8)}$	$11.3^{+0.2(+0.4)}_{-0.2(-0.3)}$	$11.7^{+0.1(+0.2)}_{-0.1(-0.1)}$
Draco	86.4	+34.7	82	0.40	87.0	0.28	$1.22^{+0.15(+0.28)}_{-0.14(-0.28)}$	$9.8^{+0.5(+0.9)}_{-0.5(-0.8)}$	$11.2^{+0.2(+0.4)}_{-0.2(-0.3)}$	$11.6^{+0.1(+0.2)}_{-0.1(-0.2)}$
Sextans	243.5	+42.3	86	1.36	109.3	0.91	$0.61^{+0.38(+0.96)}_{-0.31(-0.43)}$	$9.4^{+1.7(+2.9)}_{-1.2(-1.8)}$	$10.7^{+1.1(+1.9)}_{-0.8(-1.1)}$	$11.1^{+0.7(+1.5)}_{-0.4(-0.6)}$
Carina	260.1	-22.2	101	0.48	99.2	0.27	$0.59^{+0.10(+0.60)}_{-0.07(-0.14)}$	$9.3^{+0.3(+0.8)}_{-0.4(-0.8)}$	$10.5^{+0.2(+0.4)}_{-0.1(-0.2)}$	$10.9^{+0.1(+0.1)}_{-0.1(-0.1)}$
Fornax	237.1	-65.7	138	1.34	102.9	0.56	$1.01^{+0.30(+0.60)}_{-0.17(-0.28)}$	$9.5^{+0.5(+1.1)}_{-0.5(-0.8)}$	$10.8^{+0.2(+0.5)}_{-0.2(-0.3)}$	$10.5^{+0.3(+0.7)}_{-0.2(-0.4)}$
LeoII	220.2	+67.2	205	0.30	107.2	0.08	$0.94^{+0.26(+0.50)}_{-0.18(-0.29)}$	$11.6^{+0.8(+1.7)}_{-0.8(-1.5)}$	$11.7^{+0.7(+1.6)}_{-0.6(-0.9)}$	$11.7^{+0.7(+1.6)}_{-0.6(-0.9)}$
LeoI	226.0	+49.1	250	0.50	117.1	0.11	$1.22^{+0.24(+2.52)}_{-0.21(-0.36)}$	$9.7^{+0.3(+1.0)}_{-0.2(-0.5)}$	$10.7^{+0.1(+0.3)}_{-0.1(-0.2)}$	$10.7^{+0.1(+0.3)}_{-0.1(-0.2)}$

* Note that the values for $\log_{10}[J(\alpha_c)]$ differ from those quoted in Walker et al. (2011) as the MCMC analysis is slightly different here.

ments such as CTA, as some loss of sensitivity can occur (see, e.g. Figure 4 of Walker et al. 2011). This is discussed, taking into account the full detail of the instruments, in Section 5.3. However, in this respect, the best target for future instrument may eventually become Leo II, which despite a quite large uncertainty outshines all other dSphs at $\alpha_{\text{int}} = 0.01^\circ$ (see also Fig. 12). We note however that it is the dsph with the smallest amount of kinematic data at present (so it has the most uncertain J -factor).

5.1.4 dSphs in the diffuse galactic DM signal: contrast

The uncertainties in J are illustrated from a different viewpoint in Fig.12. It shows, in addition to the mean, 68% and 98% CLs on the J s, the latitudinal dependence of the Galactic DM background (smooth and galactic clump contribution) for the same integration angle.¹² For a typical present-day instrument resolution (integration angle $\alpha_{\text{int}} \sim 0.1^\circ$), we recover the standard result that the Galactic Centre outshines all dSphs.

The three panels illustrate the loss of contrast (signal from the dSph w.r.t. to the diffuse Galactic DM signal) as the integration angle is increased. This is understood as follows: the integrand appearing in Eqs. (C4) and (C5) is mostly insensitive to the l.o.s. direction a few tens of degree away from the Galactic centre, so that Eq. (C6) holds, giving an α_{int}^2 dependence.

For detectability (see also Sec 3), the naïve approach of maximising the integration angle (to maximise J_{dSph}) must be weighed against the fact that an increased integration angle means more

astrophysical γ -ray and cosmic-ray background. For large integration angles, dSphs also have poor contrast against the diffuse Galactic DM annihilation signal, indicating that the Galactic halo is a better target for any search on angular scales $\gtrsim 1$ (see e.g. Abramowski et al. 2011b for such a search with H.E.S.S.).

5.1.5 Comparison to other works

Comparison between different works can be difficult as every author uses different definition, notations and units for the astrophysical factor. To ease the comparison, we provide in Appendix A conversion factors between standard units (we also point out issues to be aware of when performing such comparisons).

Below is a comparison to just a few of the works published on the subject, and only for the objects that these studies and the present one have in common:

- The Evans et al. (2004) values of $J/\Delta\Omega$ for Draco (with $\Delta\Omega = 10^{-5}$ i.e. $\alpha_{\text{int}} = 0.1^\circ$) for all the profiles they explored (cored, $\gamma = 0.5$, $\gamma = 1$, $\gamma = 1.5$) are larger (after correction by $\Delta\Omega$, given their definition of the astrophysical factor) than our 95% CL upper limit for this object shown in Table 2. The difference is probably related to our data set which is about twice as large as that used by Evans et al. (2004).

- Strigari et al. (2007) provide directly the γ -ray flux (i.e. including the particle physics term), so that we can only compare our respective rankings. These agree in general but for Sculptor we find a larger flux than Draco, conversely to these authors.

- Pieri et al. (2009) focused on Sextans, Carina, Draco and Ursa Minor. They found the latter to have the largest J (Φ_{cosmo} in their notation) of these 4 objects, followed by Draco, Carina and Sextans. But for the last two, this ranking is similar to ours. However, while their values of J fall within our 68% (UMi, Sextans) or 95% (Carina) CL, their value for Draco is above our 95% CL upper limit.

- Essig et al. (2009) also performed a statistical study on Draco and Ursa Minor, to determine their profiles from kinematic data and to derive the confidence levels on the J -factor. Given that their integration is performed on a slightly larger opening angle (0.14°),

¹² The smooth profile is taken to be an Einasto profile, the clump distribution is a core one, whereas their inner profile are Einasto with concentration and parameters *à la* Bullock et al. (2001) Normalising the mass distribution to have 100 clumps more massive than $10^8 M_\odot$, and taking $dP/dM \propto M^{-1.9}$ leads to a DM fraction into clumps of $\sim 10\%$ for clumps distributed in the range $10^{-6} - 10^{10} M_\odot$ (see, e.g., Lavalley et al. 2008, and references therein). The local DM distribution is fixed to the fiducial value $\rho_\odot = 0.3 \text{ GeV cm}^{-3}$. The exact configuration is unimportant here as this plot is mostly used for illustration purpose.

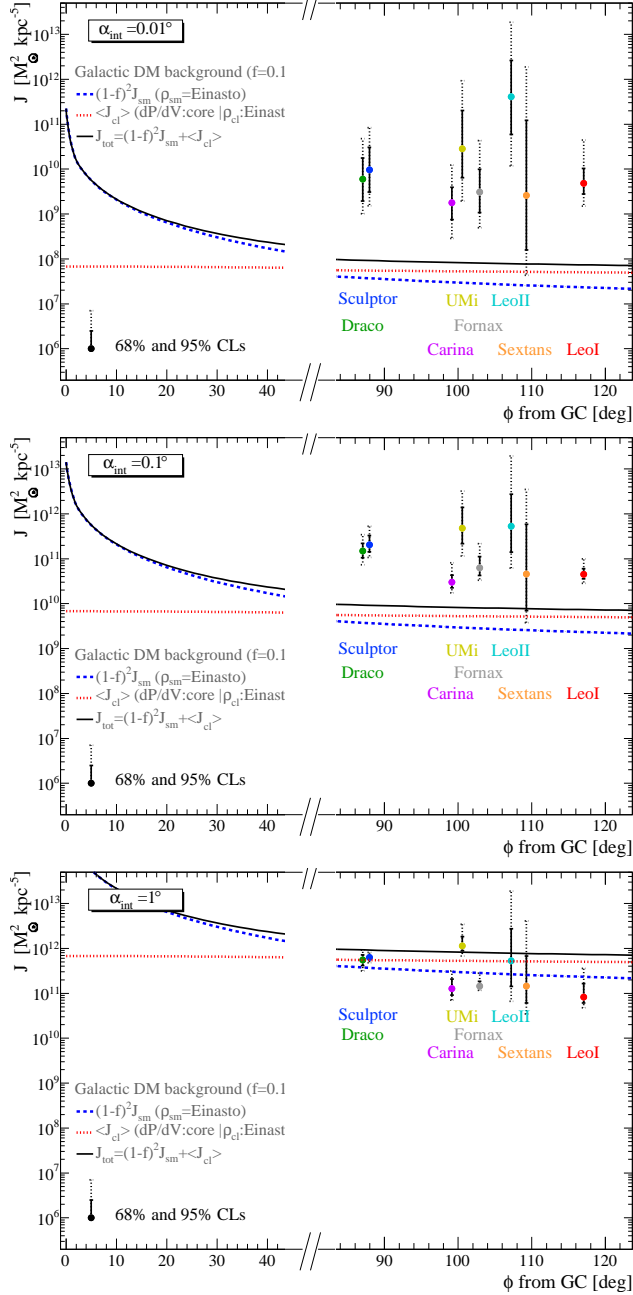


Figure 12. Galactic contributions to J for the smooth (blue-dashed line), mean clump (red-dotted line) and sum (black-solid line) vs the angle from the Galactic centre. The symbols show J for the dSphs, assuming a prior of $0 \leq \gamma_{\text{prior}} \leq 1$ on the central DM slope. The central point corresponds to the median values, the solid bars to the 68% CLs, and the dotted bars to the 95% CLs. The integration angle is, from top to bottom 0.01° , 0.1° , and 1° . The Galactic contributions J_{sm} and $\langle J_{\text{subcl}} \rangle$ scale as α_{int}^2 , but J_{dSph} does not, changing the contrast of the dSphs w.r.t. to the DM Galactic background (see text for details).

our results appear to be in agreement. Their 90% CL limits are 2-3 times larger than the 95% CL limits given in Table 2 but this may be due to the larger range they adopt for the prior on the inner slope (see App. G1).

• Kuhlen (2010) gives the astrophysical factors of all the dSphs using a point-like approximation and a NFW DM profile, and integrated with a $\alpha_{\text{int}} = 0.15^\circ$ angular resolution. These can be

compared to the median and confidence levels we derived in Table 2 for $\alpha_{\text{int}} = 0.1^\circ$. The values of Kuhlen (2010) (multiplied by 4π to match our definition of J) generally fall inside our 68% CL intervals, but for Leo II his value is just within our 95% CI while Draco and Carina cannot be accommodated at all. For these two objects, the values of Kuhlen (2010) are much larger than the ones we find, and this is unlikely to be explained by the 0.05° difference in integration angles. A simple explanation is that Kuhlen (2010) does not use stellar kinematic data directly in his analysis, but stacks suitable Via Lactea halos ($M_{300} \approx 10^7 M_\odot$ and appropriate distances) and uses those averages to estimate J . Focusing on the ranking (without worrying about contrast to the background and the other instrumental constraints), both we and Kuhlen (2010) agree that among the classical dSph UMi is a most promising target. However, while we find Sculptor and Draco to be the next most favorable targets, Kuhlen (2010) names Draco and Carina from his ‘simulation-based’ approach.

For completeness, we also compare our median values with the J values used by different experimental groups:

- The MAGIC collaboration published point source limits for Draco (Albert et al. 2008) adopting the scheme of Sánchez-Conde et al. (2007) of a power law density profile, with an exponential cut-off. They examine two scenarios, a cored and a cusped model, but find no discernable difference when calculating J for integration angles $< 0.4^\circ$, i.e. larger than the MAGIC PSF. The value of J they calculate for Draco is a higher than ours (after appropriate scaling of the integration region and unit conversion) by about a factor of 2.
- The VERITAS collaboration also published limits on Draco and Ursa Minor (Acciari et al. 2010). They assume a NFW profile, take the density profiles from Strigari et al. (2007) and follow Bergström et al. (1998) for the calculation of J . Whilst the range of density values in Strigari et al. (2007) have a physical motivation the values used in Acciari et al. (2010) are rather arbitrarily chosen to be the midpoint of that range, which leads to consistently higher J -values than ours (by a factor of 3 for Draco and a factor of 1.2 for UMi).
- The H.E.S.S. collaboration (Abramowski et al. 2011a) published limits on the southern sources Sculptor and Carina using NFW and isothermal profiles with a number of varying assumptions. This leads to a range of calculated J -values (rather than a single solution) that are consistent with our median value and estimated uncertainties.
- The Fermi collaboration (Abdo et al. 2010) has published limits for a number of the sources studied here. They adopted a NFW profile within the tidal radius and following Martinez et al. (2009) they calculated the J -value (using an MCMC approach on the observed stellar velocities) for a 1° integration angle which is compatible with their high energy PSF. From this they find Draco to have a larger J compared to the other dwarfs (a factor of ~ 2 higher than the next dwarf which is Ursa Minor), contrary to what we find in this study.

5.2 5-parameter MCMC analysis: γ_{prior} fixed

Higher resolution numerical simulations following both DM and gas, additional kinematic data and new modelling techniques may help constraining the value of γ in the near future. With the knowledge of γ , we should better constrain the radial-dependence of J , which is crucial to disentangle, e.g. dark matter annihilation from DM decay (Boyarisky et al. 2006;

Palomares-Ruiz & Siegal-Gaskins 2010). The topic of decaying dark matter goes beyond the scope of this paper, and it will be discussed elsewhere. Below, we merely inspect the gain obtained on the J prediction when having a strong prior on γ , and briefly comment on the possibility to disentangle $\gamma = 0$ profiles from $\gamma = 1.0$ profile in the case of annihilation (if this cannot be achieved, hopes for disentangling decay from annihilation would be quite low on a single object).

5.2.1 Parameter correlations

We repeat the MCMC analysis for fixed value of the inner slope $\gamma_{\text{prior}} = 0., 0.5, 1., \text{ and } 1.5$. The priors for the five other parameters are as given in Section 5.1.

Using Eq. (9) for the mass having a robust estimate of $M(r_{\text{half}})$ (Walker et al. 2009; Wolf et al. 2010; Amorisco & Evans 2011) gives $\log(\rho_s) + \gamma \log(r_s) \approx \text{constant}$ which reduces to $\log(\rho_s) \approx \text{constant}$ for $\gamma = 0$. As a result, we expect a strong correlation between ρ_s and r_s when $\gamma_{\text{prior}} = 1$ and none when $\gamma_{\text{prior}} = 0$. This is confirmed by the result of our MCMC analysis shown in Fig. 13 (here, for the Draco case). The half-light radius r_{half} for Draco is ~ 200 pc, but we choose to show the PDF for M_{300} in the bottom panel of Fig. 13 as we wish to compare the mass of the dSphs among themselves (see Table 2). It confirms that the mass within an appropriate radius can be reliably constrained by the data regardless of the value of γ .

5.2.2 Uncertainties on the profile and on J

For any given γ , the uncertainty on $\rho(r)$ at small radii is related to the range of r_s values at which the asymptotic slope is reached (for each profile accepted by the MCMC analysis). For $\gamma_{\text{prior}} = 0$, the maximum uncertainty on $\rho(r)$ is directly related to the maximum uncertainty on ρ_s (since for $r \ll r_s$, $\rho(r)$ is constant) which can be read off the PDF (top-left panel of Fig. 13). This leads to an order of magnitude uncertainty on $\rho(r)$ for small r , which is consistent with the 95% CL shown in top panel of Fig. 14. For $\gamma > 0$, the uncertainty has to be read from the dispersion in the values of $\rho_s r_s^\gamma$, or equivalently, the mass M_{300} . The bottom panel of Fig. 13 shows that this mass is well-constrained, independently of γ for the case of Draco (see however in Table 2 for a larger spread for some dSphs), resulting in a smaller uncertainty for $\gamma_{\text{prior}} = 1.5$ than for $\gamma_{\text{prior}} = 0$ (top panel of Fig. 13). We checked that the CLs obtained in Fig. 14 (in Appendix G2) for the artificial data enclose correctly the range of reconstructed values: they are consistent with a larger reconstruction bias for $\gamma_{\text{prior}} = 0$ than for $\gamma_{\text{prior}} = 1.5$ at small radii.

For the uncertainty on J , we can obtain a crude estimate by relying on the approximate formulae given in Appendix B. For $\gamma > 0$, $J \propto \rho_s^2 r_s^3$, and substituting the constant M_{300} relationship leads to $J \propto r_s^{3-2\gamma}$. The value of r_s , as seen in its PDF in the top and middle panels of Fig. 13, varies by roughly a factor of 10. Because of the weighting power $3 - 2\gamma$, the uncertainty on J is expected to be the smallest for $\gamma = 1.5$, which is in agreement with the curves in Fig. 14 (bottom panel). However, the analysis of the artificial data in Appendix G2 shows that the typical CL on J obtained in the bottom panel of Fig. 14 is likely to be underestimated for $\gamma_{\text{prior}} = 1.5$ (up to factor $\mathcal{O}(2)$, see Fig. G2).¹³ This happens

¹³ This is understood as for the latter, the inner region ($r \ll r_s$) contribute the most to J , and even small differences for $\rho(r \sim r_s)$ are bound to trans-

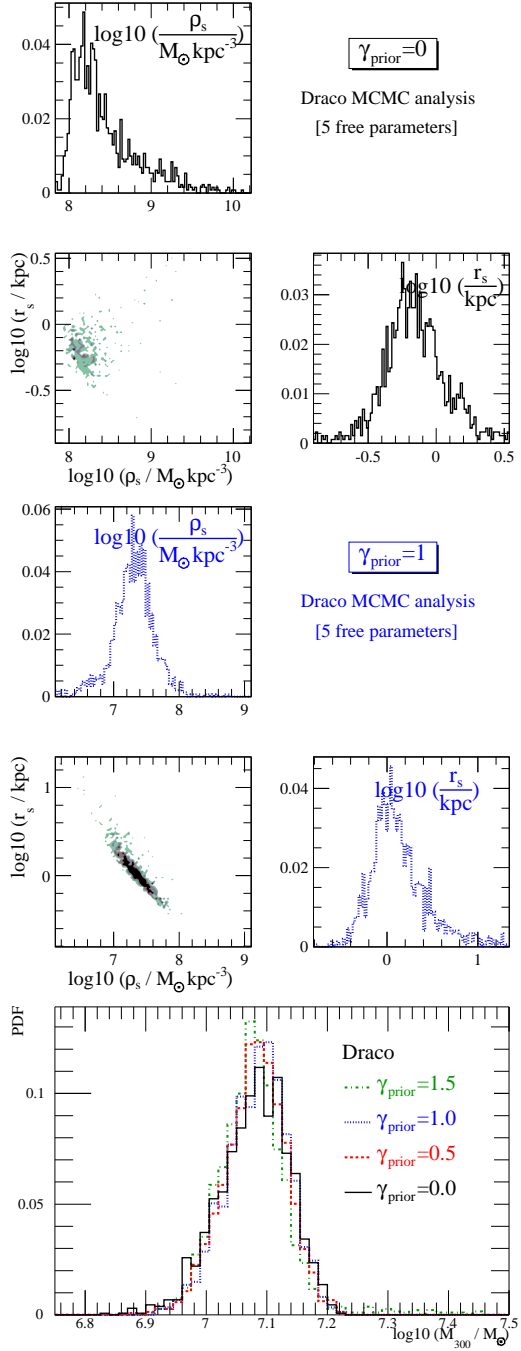


Figure 13. **Top:** correlation and PDF of the profile parameters ρ_s and r_s from the 5-parameter MCMC analysis $\gamma_{\text{prior}} = 0.0$. **Middle:** same, but for $\gamma_{\text{prior}} = 1.0$. **Bottom:** PDF of M_{300} , the mass at 300 pc.

for any integration angle. For this reason, we cannot rely of the J value for $\gamma_{\text{prior}} = 1.5$ and focus only on the three cases $\gamma_{\text{prior}} = 0$, $\gamma_{\text{prior}} = 0.5$, and $\gamma_{\text{prior}} = 1.0$ below.

late in sizeable differences for $\rho(r \rightarrow 0)$. Conversely, similar differences on ρ for shallower profiles is not an issue as their inner parts do not contribute to J .

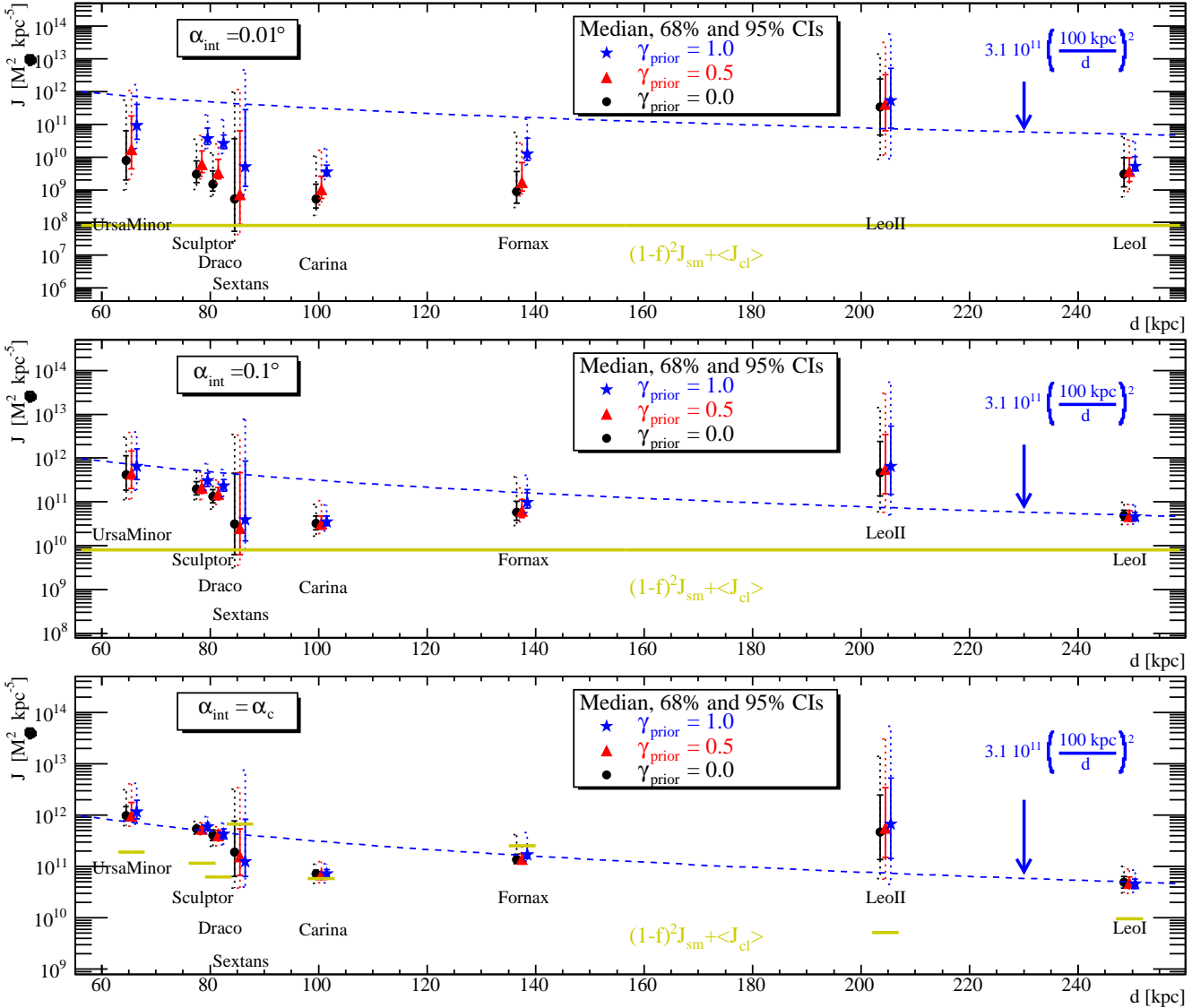


Figure 15. Median J -factor values (symbols) and 68%/95% CLs (solid bars; dashed bars) for the fixed γ_{prior} analysis (the result for $\gamma_{\text{prior}} = 1.5$ is not shown because it is not reliable, see Sect. G2). The blue dashed line shows the expected scaling with distance for point sources: $3.1 \cdot 10^{15} d^{-2} [\text{M}_{\odot}^2 \text{kpc}^{-5}]$. The panels show, from top to bottom, three integration angles $\alpha_{\text{int}} = 0.01^{\circ}$, 0.1° , and $\alpha_c \approx 2r_h/d$ (an angle very similar to the angle enclosing 80% of the flux, see Fig. 16) that optimises the determination of the J -factor for a given dSph (hence the error bars are smaller in this plot than in the other two). The yellow solid lines (and broken lines in the bottom panel) correspond to the Galactic DM background including both the smooth and clumpy distributions. For the bottom panel, this is not a smooth curve since it depends on the integration angle α_{int} that varies from dSph to dSph in this figure. Note that the choice of using the critical angle $\alpha_{\text{int}} = \alpha_c$ is optimal in the sense that it gives the most constrained value for J . But where the Galactic background annihilation signal approaches that of the dSphs (see for example, Sextans and Fornax), the motivation for staring at the dSphs rather than simply looking at the Galactic halo is gone.

5.2.3 $J(d)$ and departure from the $1/d^2$ scaling

Fig. 15 shows the J median values, 65% and 95% CIs as symbols, dashed and solid error bars respectively, for an integration angle of 0.01° (top), 0.1° (middle), and $\alpha_c \approx 2r_{\text{half}}/d$ (Walker et al. 2011). The x -axis is the distance to the dSph (in kpc). For point-like sources, the J -factor of a single dSph scales as $1/d^2$, as illustrated by the blue-dashed line. Departure from this scaling is interpreted as a combination of a mass effect and/or a profile effect. For instance, Sextans and Carina are dSphs with smaller M_{300} with respect to the other ones (see Tab. 2); consequently they are located below the dashed blue line in the top panel of Fig. 15. The exception is Leo II, which has a ‘small’ mass but is nevertheless above

the dashed line. Although this analysis cannot constrain γ , we are tempted to interpret this oddity in terms of a ‘cuspier’ profile (w.r.t. those for other dSphs), which would be consistent with the fact that its J remains similar in moving from $\alpha_{\text{int}} = 0.1^{\circ}$ (middle panel) to 0.01° (top panel). However, an alternative explanation (which would be more consistent with the results obtained in this paper) could be the fact that Leo II has the smallest amount of kinematic data at present, and that its J is overestimated (see Appendix H1 to support this line of argument). We repeat that the relative brightness of the dSphs is further affected for background-dominated instruments (as described in Sec. 3), so that the ranking has to be based on Fig 16 discussed in the next section.

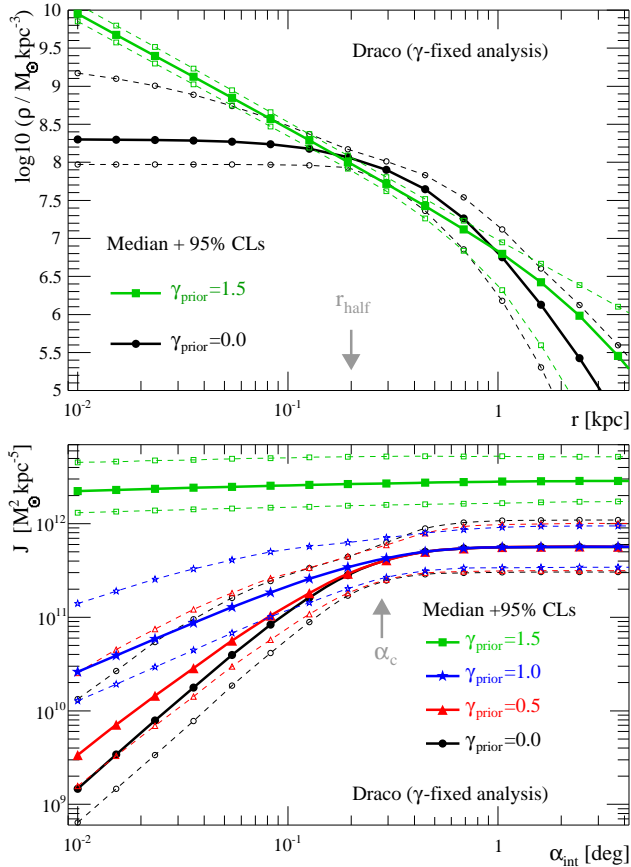


Figure 14. Median values (solid lines, filled symbols) and 95% CLs (dashed lines, empty symbols) from the fixed γ_{prior} MCMC analysis on Draco. **Top:** density profiles (the gray arrow indicates the value of r_{half}). **Bottom:** J -factor (the gray arrow indicates $\alpha_c \approx 2r_{\text{half}}/d$).

The bottom panel of Fig. 15 shows the J value for an ‘optimal’ integration angle α_c that is twice the half-light radius divided by the dSph distance¹⁴ (this corresponds to the integration angle that minimises the CLs on J ; see Walker et al. 2011). The yellow broken solid lines show the expected signal from the diffuse Galactic DM annihilation background, including a contribution from clumpy sub-structures (the extragalactic background, which also scales as α_{int}^2 , has not been included). The total background may be uncertain by a factor of a few (depending on the exact Galactic (smooth) profile and local DM density). Its exact level—which depends on the chosen integration angle—determines the condition for the loss of contrast of the dSph signal, i.e. the condition for which looking at the DM halo (rather than at dSphs) becomes a better strategy.

5.2.4 Conclusion for the fixed γ_{prior} analysis

The analysis of simulated data shows that the analysis for $\gamma_{\text{prior}} = 1.5$ is biased by a factor of $\mathcal{O}(10)$ and that the CLs obtained on the real data are likely to be severely under-estimated in that case. But such steeply cusped profiles are neither supported by observations nor motivated by current cosmological simulations. For values of

¹⁴ CLs for $J(\alpha_{\text{int}})$ are provided along with the paper for readers interested in applying our analysis to existing and future observatories.

$\gamma_{\text{prior}} \leq 1$, this bias is a factor of a few only, so that it shows that the results from a fixed γ_{prior} analysis of the 8 classical dSphs are robust. However, this analysis shows that unless very small integration angles $\alpha_{\text{int}} \lesssim 0.01^\circ$ are chosen (or if $\gamma_{\text{true}} \gtrsim 1$), knowing the exact value of γ does not help in improving the determination of J . Indeed, even using Draco, the stellar population of which is one of the most studied, the CLs of the three reconstructed fluxes ($\gamma_{\text{prior}} = 0$ in black full circles, $\gamma_{\text{prior}} = 0.5$ in red triangles, and $\gamma_{\text{prior}} = 1.0$ in blue stars) in Fig. 14 (bottom), overlap. Reversing the argument, if we do not know the inner slope, and if a γ -ray signal is detected from just one dSph in future, there will be little hope of recovering the slope of the DM halo from that measurement only.

This means that the best way to improve the prediction of the J -factor in the future relies on obtaining more *data* and a more refined MCMC analysis; an improved prior on the DM distribution makes little difference.

5.3 Sensitivity of γ -ray observatories to DM annihilation in the dSphs

The potential for using the classical dSph to place constraints on the DM annihilation cross-section, given the uncertainties in the astrophysical J -factor, can be seen in Fig. 16. Previous analyses have adopted the solid angle for calculation of the J -factor to be the angular resolution of the telescope for a point-like source, typically assuming a NFW-like profile (Acciari et al. 2010; Abdo et al. 2010; Abramowski et al. 2011a). By contrast our sensitivity plots take into account finite size effects: i) the J values are based on the MCMC analysis with the prior $0 \leq \gamma_{\text{prior}} \leq 1$, where the corresponding J are shown in Fig. 12; ii) the energy dependent angular resolution has also been taken into account assuming a standard γ -ray annihilation spectrum (see Section 2.1.1). Moreover for Fermi-LAT the background level assumed has been increased (resulting in a 25% worsening of the sensitivity above 100 MeV) to reflect the average situation in the directions of the classical dSph (the variation between the individual dSph is only 7% rms). A likelihood based analysis is used for both FCA and Fermi and a nominal observation zenith angle of 20° assumed for the FCA¹⁵ (see Section 3.2).

The panels from top to bottom correspond to increasing DM (neutralino) masses. At low values, Fermi has a better sensitivity than FCA; at a mass of about 1 TeV the two are comparable, and for higher masses the FCA becomes the more sensitive instrument due to the vastly greater effective area at the photon energies at which the annihilation spectrum is expected to peak. Note that the precise value of $\langle\sigma v\rangle$ where the relative sensitivities of the two instruments cross depends on the form of the DM annihilation spectrum. Since we are examining the uncertainties in the astrophysical J -factor to the detectability of dSphs, we have used a conservative spectrum averaged over a number of possible annihilation channels (see Fig. 1) which results in the majority of produced γ -ray photons having energies $\simeq 10\%$ of the DM particle mass. If we were to move from a relatively soft spectrum, such as $b\bar{b}$ to a harder one, such as $\tau^+\tau^-$, this would benefit both instruments in different ways. For Fermi-LAT a harder spectrum makes the signal easier to distinguish above the diffuse γ -ray background; indeed the

¹⁵ The energy threshold for a ground based instrument is dependent on the zenith angle of observation. This means that the actual energy threshold for a given object will depend on the object’s declination and the latitude of the, yet to be determined FCA site.

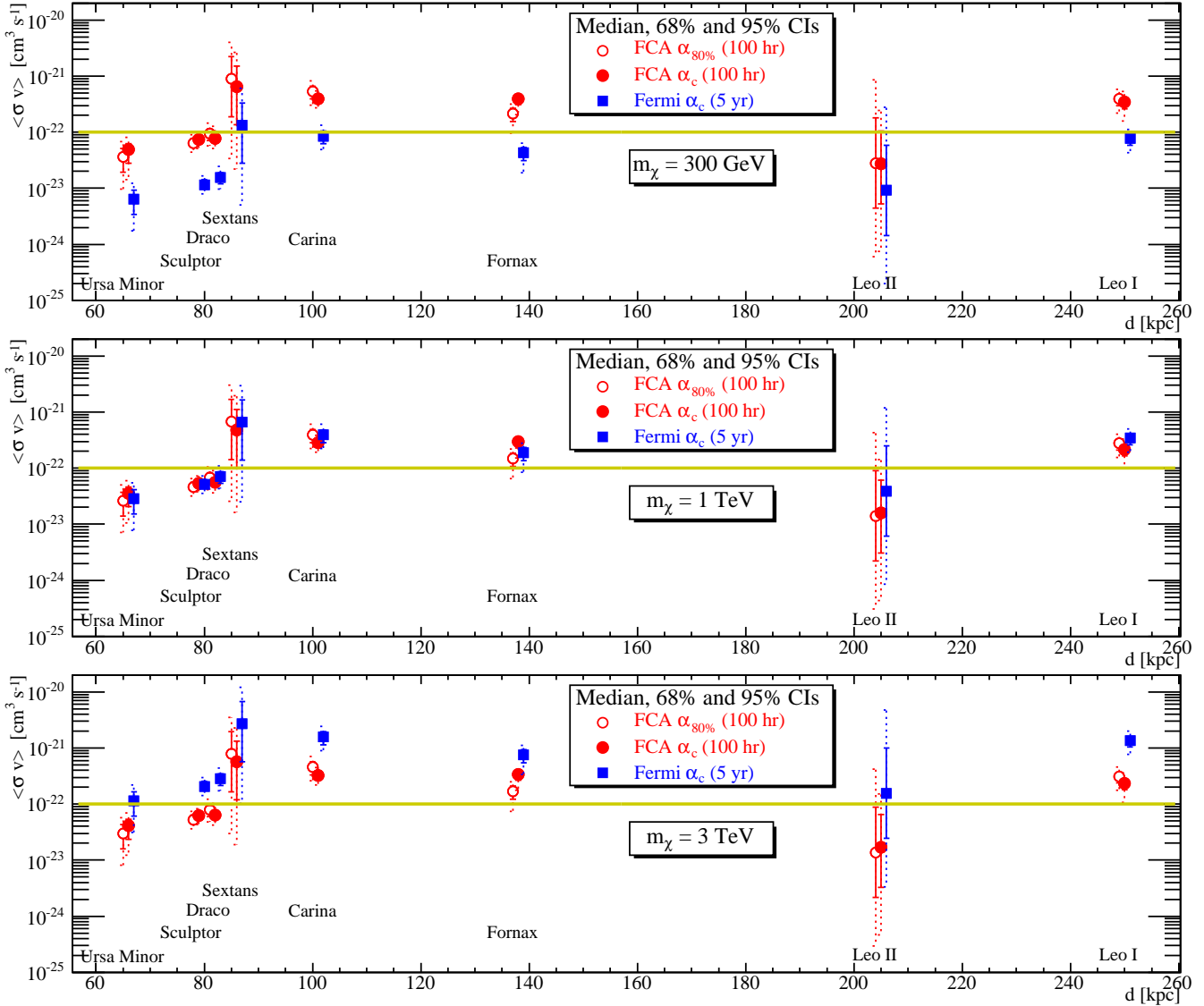


Figure 16. Minimum detectable $\langle \sigma v \rangle$ for known dSphs shown as a function of their distance, for different assumed DM masses (separate panels). 100 hour observations with an FCA (red circles) are compared to 5 years of Fermi observations (blue squares). Error bars indicate 65% (solid lines) and 95% (dotted lines) confidence limits. The integration angle is adapted to the α_c of each dSph and the energy-dependent PSF of the two instruments. The strategy of using α_{80} , rather than α_c , is indicated with hollow symbols for the FCA case. The line for $\langle \sigma v \rangle = 10^{-22} \text{ cm}^3 \text{ s}^{-1}$ is drawn for comparison purpose between the panels.

Abdo et al. (2010) found that the detectable flux limit from a potential source could vary by a factor of 2–20 (with lower particle masses benefiting the most) between these different annihilation spectra. For the FCA, which has a very large effective area to photons $\geq 100 \text{ GeV}$, the benefits of having more high energy photons is very apparent when it comes to flux sensitivity. For both observatories, an increased number of high energy photons needs to be balanced with the correspondingly better angular resolution, particularly if (e.g. for Fermi-LAT) a point-like source becomes spatially resolved.

Our analysis places Ursa Minor as the best candidate for the northern sky (marginally better than Draco, which has long been a favourite target of northern hemisphere observatories) and Sculptor for the southern sky, when it comes to a favourable median and low uncertainty in the J -factor. It should be noted, however, that although the closest objects seem to be favoured, Leo II has the po-

tential to yield a stronger signal, however more kinematic data are needed in order to constrain better its J -factor. In addition, it should be noted that the uneven sensitivity of the Fermi-LAT across the sky, caused in particular by the proximity of bright sources¹⁶ as well as the galactic diffuse background can change what is considered the favorite candidate.

We emphasise that in our analysis the inner slope γ has not been constrained, but that a better independent determination of γ in future will not help providing a better determination of J (see Fig. 15); this is discussed further in the Appendices. Carina, Fornax and Leo I are the targets least favoured. When compared to existing limits from Fermi-LAT (Abdo et al. 2010) or the current generation

¹⁶ In particular there is a bright GeV emitter 1FGL J0058.4-3235 only $\sim 1.1^\circ$ away from Sculptor which significantly worsens the upper limit on that object as discussed by Abdo et al. (2010).

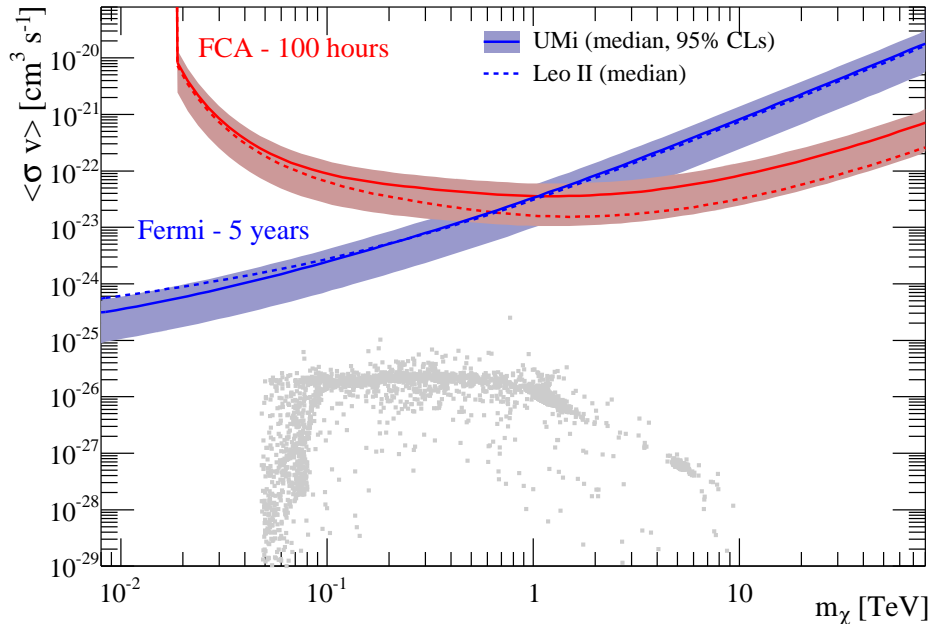


Figure 17. Sensitivity reach in the $m_\chi - \langle\sigma v\rangle$ plan for FCA (100 hr) and Fermi (5 yr), for our best candidates UMi (median value and 95% CIs) and Leo II (median only). Black asterisks represent points from MSSM models that fall within 3 standard deviations of the relic density measured in the 3 year WMAP data set (taken from Acciari et al. 2010).

of ACTs (Acciari et al. 2010; Abramowski et al. 2011a) it can be seen that our limits are not dissimilar from those that have already been published. For Fermi this is not surprising, since the source is unresolved and any difference should relate only to the assumed increase in exposure from 1 to 5 years, resulting in a factor of a few at best. The similarity in sensitivity between current and future ACTs is perhaps more surprising, but this as stated earlier relates to the naïve assumptions made on the form for the J -factor and the solid angle integrated over; in order to reach the currently claimed limits requires a deep exposure with an instrument as sensitive as CTA.

One last thing to note is that a common way to synthesise a deeper exposure is to stack observations of different sources together to provide an effective long exposure of a generic source. For a common universal halo profile this may be fine, however any analysis will have to take into account the different integration angles for each individual source correctly. If all dSphs do not share a common halo profile and hence have different γ values, we have to rely on the varying- γ analysis presented in the previous section and the relative ranking of potential targets would then be different.

6 DISCUSSION AND CONCLUSIONS

We have revisited the expected DM annihilation signal from dSph galaxies for current (Fermi-LAT) and future (e.g. CTA) γ -ray observatories. The main innovative features of our analysis are that: (i) We have considered the effect of the *angular size* of the dSphs for the first time. This is important since, while nearby dSphs have higher γ ray flux, their larger angular extent can make them sub-prime targets if the sensitivity is limited by cosmic ray and γ -ray backgrounds. (ii) We determined the astrophysical J -factor for the classical dSphs directly from photometric and kinematic data. We assumed very little about their underlying DM distribution, modelling the dSph DM profile as a smooth split-power law, both with

and without DM sub-clumps. (iii) We used a MCMC technique to marginalise over unknown parameters and determine the sensitivity of our derived J -factors to both model and measurement uncertainties. (iv) We used simulated DM profiles to demonstrate that our J -factor determinations recover the correct solution within our quoted uncertainties.

Our key findings are as follows:

(i) Sub-clumps in the dSphs do *not* usefully boost the signal. For all configurations where the sub-clump distribution follows the underlying smooth DM halo, the boost factor is at most $\sim 2 - 3$. Moreover, to obtain even this mild boost, one has to integrate the signal over the whole angular extent of the dSph. This is unlikely to be an effective strategy as the diffuse Galactic DM signal will dominate for integration angles $\alpha_{\text{int}} \gtrsim 1^\circ$.

(ii) Point-like emission from a dSph is a very poor approximation for high angular resolution instruments, such as the next-generation CTA. For a nearby dSph, using the point-like approximation can lead to an order of magnitude overestimate of the detection sensitivity. In the case of a nearby cored profile consisting of very high mass DM particles, a point source approximation can be unsatisfactory even for the modest angular resolution of Fermi-LAT.

(iii) With the Jeans' analysis, no DM profile can be ruled out by current data. The use of the MCMC technique on artificial data also shows that such an analysis is unable to provide reliable values for J if the profiles are cuspy ($\gamma = 1.5$). However, using a prior on the inner DM cusp slope $0 \leq \gamma_{\text{prior}} \leq 1$ provides J -factor estimates accurate to a factor of a few.

(iv) The best dSph targets are not simply those closest to us, as might naively be expected. A good candidate has to combine high mass, close proximity, small angular size ($\lesssim 1^\circ$; i.e. not too close); and a well-constrained DM profile. With these criteria in mind, we find three categories: well-constrained and promising (Ursa Minor, Sculptor and Draco), well-constrained but less promising (Carina,

Fornax and Leo I), and poorly constrained (Sextans and Leo II). Leo II may yet prove to be a viable target as it has a larger median J -factor than UMi, however more data are required to confirm its status.

(v) A search based on a known DM candidate (from, e.g., forthcoming discoveries at the LHC) will do much to optimise the search strategy and, ultimately, the detection sensitivity for all γ -ray observatories. This is because the shape of the annihilation spectrum is a strong driver of the photon energy range that can provide the best information on the candidate DM particle mass. Fermi-LAT has great potential to probe down to the expected annihilation cross-section for particles of mass $\ll 700$ GeV, whereas a ground based instrument is more suited for probing particle masses above a few hundred GeV with a sufficiently deep exposure. However, even for 5 yr of observation with Fermi-LAT or 100 hrs with FCA, the sensitivity reach (Fig. 17) remains anywhere between 4 to 10 orders of magnitude above the expected annihilation cross-section for a cosmological relic (depending on the mass of the DM particle candidate). Improving these limits will require a harder annihilation spectrum than the conservative average we have adopted in this study, or a significant boost (e.g. from the Sommerfeld enhancement) to the γ -ray production.

Finally, the ultra-faint dSphs have received a lot of interest in the community lately, as they could be the most-DM dominated systems in the Galaxy. We emphasise that the MCMC analysis we have performed for the classical dSphs cannot be applied ‘as is’ for these objects. First, the sample of stars observed is smaller. Second, the velocity dispersion is smaller and suffers from larger uncertainties than those for the classical dSphs. The robustness and systematic biases of the MCMC analysis will be discussed elsewhere (Walker et al., 2011, in preparation). Results concerning J for the ultra-faint dSphs will be presented in a companion paper.

ACKNOWLEDGMENTS

We thank the anonymous referee for their careful reading of the manuscript and useful comments. We thank Walter Dehnen for providing his code for use in generating artificial dSph data sets. MGW is supported by NASA through Hubble Fellowship grant HST-HF-51283, awarded by the Space Telescope Science Institute, which is operated by the Association of Universities for Research in Astronomy, Inc., for NASA, under contract NAS 5-26555. CC acknowledges support from an STFC rolling grant at the University of Leicester. JAH acknowledges the support of an STFC Advanced Fellowship. MIW acknowledges the Royal Society for support through a University Research Fellowship. JIR acknowledges support from SNF grant PP00P2_128540/1. SS acknowledges support by the EU Research & Training Network ‘Unification in the LHC era’ (PITN-GA-2009-237920). Part of this work used the ALICE High Performance Computing Facility at the University of Leicester. Some resources on ALICE form part of the DiRAC Facility jointly funded by STFC and the Large Facilities Capital Fund of BIS.

APPENDIX A: DEFINITIONS, NOTATION, CONVERSION FACTORS

Studies of DM annihilations in the context of dSphs involves both particle physics and astrophysics. The obvious difference of scales between the two fields and habits among the two communities have given rise to a plethora of notations and unit choices throughout the

literature. In this Appendix, we provide some explanatory elements and conversion factors to ease comparison between the different works published on the subject.

As mentioned in §2, we define the differential γ -ray flux as integrated over the solid angle $\Delta\Omega$ as

$$\frac{d\Phi_\gamma}{dE_\gamma}(E_\gamma, \Delta\Omega) = \Phi^{\text{PP}}(E_\gamma) \times J(\Delta\Omega),$$

where

$$\Phi^{\text{PP}}(E_\gamma) \equiv \frac{d\Phi_\gamma}{dE_\gamma} = \frac{1}{4\pi} \frac{\langle \sigma_{\text{ann}} v \rangle}{2m_\chi^2} \cdot \frac{dN_\gamma}{dE_\gamma},$$

and

$$J(\Delta\Omega) = \int_{\Delta\Omega} \int \rho_{\text{DM}}^2(l, \Omega) dl d\Omega.$$

The solid angle is simply related to the integration angle α_{int} by

$$\Delta\Omega = 2\pi \cdot (1 - \cos(\alpha_{\text{int}})).$$

In our work, the units of these quantities are as follows:

- $[d\Phi_\gamma/dE_\gamma] = \text{cm}^{-2} \text{s}^{-1} \text{GeV}^{-1}$;
- $[\Phi^{\text{PP}}(E_\gamma)] = \text{cm}^3 \text{s}^{-1} \text{GeV}^{-3} (\text{sr}^{-1})$;
- $[J] = M_\odot^2 \text{kpc}^{-5} (\text{sr})$.

First of all, note that the location of the $1/4\pi$ factor appearing in Φ^{PP} is arbitrary. We followed Pieri et al. (2009) and included it in the particle physics factor. In other works, it can appear in the astrophysical factor J (e.g., Bringmann et al. 2009). Therefore, to compare the astrophysical factors between several studies, one must first ensure to correct the value of J by 4π if needed. In the text, we did not explicitly stated the solid angle dependence in the units of J as it is dimensionless quantity.¹⁷ The conversion factor (once the 4π issue is resolved) from our J units to that traditionally found in the literature are:

- $1 M_\odot^2 \text{kpc}^{-5} = 10^{-15} M_\odot^2 \text{pc}^{-5}$
- $1 M_\odot^2 \text{kpc}^{-5} = 4.45 \times 10^6 \text{GeV}^2 \text{cm}^{-5}$
- $1 M_\odot^2 \text{kpc}^{-5} (\text{sr}) = 1.44 \times 10^{-15} \text{GeV}^2 \text{cm}^{-6} \text{kpc} (\text{sr})$

Before comparing any number, one must also ensure that the solid angle $\Delta\Omega$ over which the integration is performed is the same. In most works, a $\alpha_{\text{int}} = 0.1^\circ$ angular resolution is chosen, corresponding to $\Delta\Omega = 10^{-5} \text{sr}$. However this is not always the case, as in the present study where we explore several angular resolutions. Note that the quantity $\bar{J} \equiv J/\Delta\Omega$ (in $\text{GeV}^2 \text{cm}^{-5} \text{sr}^{-1}$ for example) is also in use and the astrophysical factor is can be found under this form in some articles (e.g., Evans et al. 2004).

APPENDIX B: TOY MODEL FOR J (IN DSPHS)

The volume of the dSph is not always fully encompassed in the integration solid angle, as sketched in Fig. B1 (vertical hatched region) so that a numerical integration is required in general. However, a reasonable approximation for estimating the dependence of J on the parameters of the problem, i.e. the distance to

¹⁷ Some authors do however explicitly express the solid angle dependence in their units, e.g. Pieri et al. (2009), who express J (Φ_{cosmo} in their notation) in $\text{GeV}^2 \text{cm}^{-6} \text{kpc} \text{sr}$. This is completely equivalent to our $M_\odot^2 \text{kpc}^{-5}$ but for the unit numerical conversion factor.

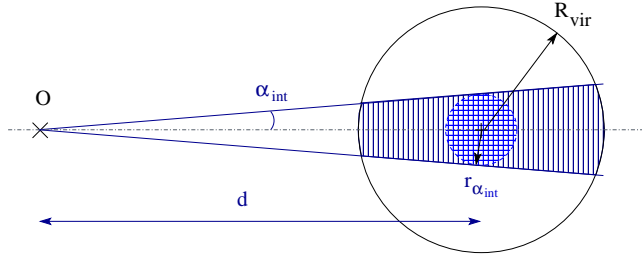


Figure B1. Sketch of the integration regions contributing to the J factor: shown are the full integration region (vertical hatched) or a sub-region (cross-hatched) used for the toy calculations. The letter O shows the observer position, α_{int} is the integration angle, d is the distance of the dSph and R_{vir} its virial radius.

the dSph d , the integration angle α_{int} , and the profile parameters ρ_s , r_s and γ), is to consider only the volume within the radius

$$r_{\alpha_{\text{int}}} = d \times \sin(\alpha_{\text{int}}) \approx d \times \alpha_{\text{int}}, \quad (\text{B1})$$

where the approximation is valid for typical integration angles $\alpha_{\text{int}} \lesssim 0.1^\circ$. This volume corresponds to the spherical cross-hatched region in Fig. B1.

The toy model proposed below to calculate J allows us to cross-check the results of the numerical integration for both the smooth and sub-clump contribution. We find that the model is accurate enough up to a factor of 2 for $\gamma = 0$ and $\gamma > 0.5$, so can be used for gross estimates of any signal from a DM clump.

B1 For the smooth distribution

About 90% of the clump luminosity is usually contained in a few r_s , whatever the profile. The consequences are twofold. First, as can be read off Table 2, $r_s/d \ll 1$, so that the J factor amounts to a point like contribution

$$J_{\text{point-like}} = \frac{4\pi}{d^2} \int_0^{\min(r_{\alpha_{\text{int}}}, r_s)} r^2 \rho^2(r) dr. \quad (\text{B2})$$

Secondly, it means that Eq. (6) for the profile can be simplified into the approximate expression

$$\rho_{\text{approx}}(r) = \begin{cases} \rho_{\text{sat}} & \text{if } r \leq r_{\text{sat}}; \\ \rho_s \times \left(\frac{r}{r_s}\right)^{-\gamma} & \text{if } r_{\text{sat}} < r \leq r_s; \\ 0 & \text{otherwise.} \end{cases} \quad (\text{B3})$$

However, for all applications of our toy model, we will keep $\gamma < 3/2$, so that the saturation density above is never reached in the dSphs considered below.

Various regimes The approximate formulae for J is obtained by combining Eqs. (B2) and (B3):

$$J_{\text{approx}} = \frac{4\pi}{d^2} \int_0^{\min(r_{\alpha_{\text{int}}}, r_s)} r^2 \rho_{\text{approx}}^2(r) dr. \quad (\text{B4})$$

Using Eq. (B1), this leads to

$$J_{\text{approx}} = \frac{4\pi}{d^2} \cdot \frac{\rho_s^2 r_s^{2\gamma}}{3-2\gamma} \cdot [\min(r_{\alpha_{\text{int}}}, r_s)]^{3-2\gamma}. \quad (\text{B5})$$

This formula gives satisfactory results for cuspy profiles (see below), but has to be modified in the following cases:

- If $r_{\alpha_{\text{int}}} \gtrsim r_s$, the integration region encompasses r_s . The $(1, 3, \gamma)$ profiles decrease faster than $r^{-\gamma}$ for $r \sim r_s$ hence integrating the toy model up to r_s is bound to overshoot the true result. We thus stop the integration at the radius r_x such that $\rho_{\text{true}}(r_x) = \rho_{\text{approx}}(r_x)/x$, i.e.

$$r_x = r_s \cdot [x^{1/(3-\gamma)} - 1].$$

Taking $x = 2$ gives a satisfactory fit to the full numerical calculation (see below).

- If $r_{\alpha_{\text{int}}} \gtrsim r_s$ and $\gamma = 0$, the integration can be performed analytically up to R_{vir} and is used instead.

- If $r_{\alpha_{\text{int}}} \lesssim r_s$ and $\gamma = 0$, the profile is constant, and integrating on the cross-hatched region (instead of the vertical hatched one, see Fig. B1) undershoots the true result. A better approximation is to integrate on a conic section. For the same reason as given for the first item, we replace r_s by r_x (with $x = 2$) in the calculation of the cone volume.

Resulting formula To summarise, the final toy-model formula proposed for the smooth contribution of the dSph is:

$$J_{\text{toy}} = \frac{4\pi\rho_s^2}{d^2} \times \begin{cases} r_s^{2\gamma} \cdot \frac{\min(r_x, r_{\alpha_{\text{int}}})^{3-2\gamma}}{3-2\gamma} & \text{if } \gamma > 0; \\ [I(r_{\alpha_{\text{int}}}) - I(0)] & \text{if } \gamma = 0, r_{\alpha_{\text{int}}} > r_x; \\ \frac{r_{\alpha_{\text{int}}}^2 \cdot r_s}{2} & \text{if } \gamma = 0, r_{\alpha_{\text{int}}} < r_x; \end{cases} \quad (\text{B6})$$

where

$$\begin{aligned} r_{\alpha_{\text{int}}} &= \alpha_{\text{int}} \cdot d, \\ r_x &= r_s \cdot [x^{1/(3-\gamma)} - 1], \\ I(x) &= -r_s^6 (r_s^2 + 5r_s x + 10x^2) / (30(r_s + x)^5). \end{aligned} \quad (\text{B7})$$

Toy model vs numerical integration Finally, we check the validity of this toy model by confronting it with the full numerical integration. Various inner slope γ of the profile are considered as provided in Table 1. Defining the critical distance d_{crit} for which the dSph is fully encompassed by the integration region, i.e.,

$$d_{\text{crit}} = \frac{r_s}{\alpha_{\text{int}}}.$$

we find $d_{\text{crit}} \sim 50$ kpc and 500 kpc for $r_s = 0.1$ and 1 kpc respectively (the integration range is $\alpha_{\text{int}} = 0.1^\circ$). If r_x is used instead of r_s , this distance is even smaller. This allows us to test the toy model for the two regimes. The result is shown in Fig. B2. The symbols show the full numerical integration while the lines show the toy-model calculations. For profiles steeper than 0.5, the agreement is better than a factor of 2 for all distances. For flatter profiles, the toy model only gives results within an order of magnitude. However, for $\gamma = 0$, the fix applied to the toy-model allows to regain the correct results within a factor of 2.

Hence, given the current uncertainties on the profiles, the set of formulae (B7) and (B7) can safely be used for quick inspection of the J value of any profile with an inner slope γ of 0, or greater than 0.5.

B2 For the sub-clumps

The influence of DM sub-structures on the γ -ray production has been widely discussed in the literature. These sub-structures may enhance the detectability by boosting the γ -ray signal. In this appendix, we give an analytical estimation of the effect of sub-clumps

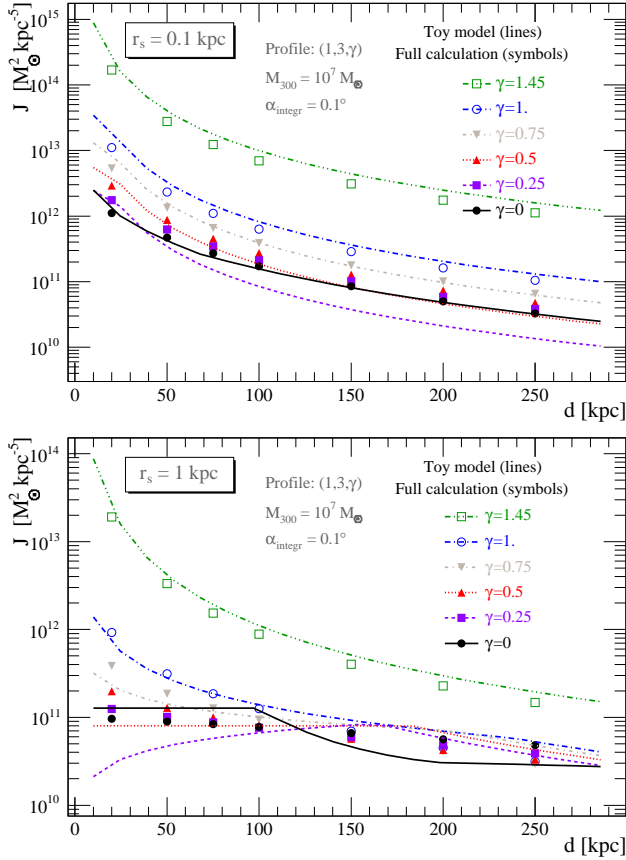


Figure B2. Toy-model calculation (lines) vs full numerical integration (symbols) of J as a function of the distance to the dSph. The integration angle is fixed to $\alpha_{\text{int}} = 0.1^\circ$ and the $(1, 3, \gamma)$ profiles are taken to vary from $\gamma = 0$ to $\gamma = 1.45$. For each model, ρ_s is calculated such as to provide $M_{300} = 10^7 M_\odot$. **Top:** dSphs for which $r_s = 0.1$ kpc. **Bottom:** dSphs for which $r_s = 1$ kpc. .

in dSph spheroidal galaxies, in the same spirit as the toy model developed in the previous section for the smooth component. For simplicity, we restrict ourselves to one cored $(\alpha, \beta, \gamma) = (1, 3, 0)$ and one cusped $(1, 3, 1)$ profile. To characterise the clump distribution, we use the formalism given in Lavalley et al. (2008).

Sub-structure distribution The clump spatial distribution is assumed to follow the dSph DM profile, namely

$$\frac{dP(r)}{dV} \propto \left(\frac{r}{r_s}\right)^{-\gamma} \left[1 + \left(\frac{r}{r_s}\right)^{-\alpha}\right]^{\frac{\gamma-\beta}{\alpha}}. \quad (\text{B8})$$

The mass distribution of the clumps is taken to be independent of the spatial distribution and takes the usual form,

$$\frac{dP}{dM} = AM^{-a}, \quad (\text{B9})$$

with $M \in [M_{\text{min}}, M_{\text{max}}]$ and $a \sim 1.9$ from cosmological N-body simulations (A is the normalisation constant for dP/dM to be a probability).

Clump luminosity Defining L_i the *intrinsic luminosity* of the sub-clump i to be

$$L_i \equiv \int_{V_{\text{cl}}} \rho^2 dV, \quad (\text{B10})$$

the astrophysical contribution to the γ -ray flux from the sub-structures of the dSph is

$$J_{\text{clumps}} = \frac{1}{d^2} \cdot \sum_{i=1}^{N^{\text{cl}}} L_i, \quad (\text{B11})$$

where N^{cl} is the number of clumps contained within the integration angle α and d is the distance of dSph. The luminosity depends only on the mass of the clump, once a concentration-mass ($c_{\text{vir}} - M_{\text{vir}}$) relationship is chosen (see, e.g., Lavalley et al. 2008, and references therein), so that $L_i = L(M_i)$. Moving to the continuous limit, Eq. (B11) reads

$$J_{\text{clumps}} = \frac{1}{d^2} \cdot N^{\text{cl}} \cdot \int_{M_{\text{min}}}^{M_{\text{max}}} L(M) \frac{dP}{dM} dM. \quad (\text{B12})$$

Fitting the results from Lavalley et al. (2008), the intrinsic luminosity¹⁸ varies almost linearly with the mass of the clump, as

$$L^{\text{NFW}}(M) = 1.17 \times 10^8 (M/M_\odot)^{0.91} M_\odot^2 \text{kpc}^{-3}, \quad (\text{B13})$$

so we have

$$J_{\text{clumps}} = \frac{N^{\text{cl}} A}{d^2} \left(\frac{1.17 \times 10^8}{1.91 - a} \right) (M_{\text{max}}^{1.91-a} - M_{\text{min}}^{1.91-a}). \quad (\text{B14})$$

Number of clumps The fraction F of clumps in the spherical integration region $r_{\alpha_{\text{int}}} \approx \alpha_{\text{int}} d$ (cross-hatched region in Fig. B1) is given by

$$F = \frac{N^{\text{cl}}}{N_{\text{tot}}^{\text{cl}}} = \int_0^{r_{\alpha_{\text{int}}}} 4\pi r^2 \frac{dP}{dV} dr, \quad (\text{B15})$$

where $N_{\text{tot}}^{\text{cl}}$ is the total number of clumps within the dSph. Upon integration and defining $x_{\text{int}} = r_{\alpha_{\text{int}}}/r_s$ and $x_{\text{vir}} = R_{\text{vir}}/r_s$ this becomes:

$$F_{\text{core}} = \left[\frac{4x_\alpha + 3}{2(x_\alpha + 1)^2} + \ln(x_\alpha + 1) - \frac{3}{2} \right] \times \left[\frac{4x_{\text{vir}} + 3}{2(x_{\text{vir}} + 1)^2} + \ln(x_{\text{vir}} + 1) - \frac{3}{2} \right]^{-1} \text{ for } (1, 3, 0), \quad (\text{B16})$$

and

$$F_{\text{cusp}} = \left[\frac{1}{(x_\alpha + 1)} + \ln(x_\alpha + 1) - 1 \right] \times \left[\frac{1}{(x_{\text{vir}} + 1)} + \ln(x_{\text{vir}} + 1) - 1 \right]^{-1} \text{ for NFW}. \quad (\text{B17})$$

Some care is necessary when evaluating the number of clumps $N^{\text{cl}} = F \times N_{\text{tot}}^{\text{cl}}$ in the integration region. Whatever the profile, most of the clumps are located within r_s so when $r_{\alpha_{\text{int}}} > r_s$, the spherical integration region of our toy model (cross-hatched region in Fig. B1) is a good enough approximation, and Eq. (B16) and (B17) hold. However, if $r_{\alpha_{\text{int}}} < r_s$ then the remainder of the intersecting cone (vertically hatched region in Fig. B1) could amount to a significant contribution to the number of clumps. Cuspy distributions should only be marginally affected given their high central concentration. However, this effect may be important for cored profiles. Whenever $r_{\alpha_{\text{int}}} < r_s$, as for the smooth contribution, Eq. (B16) is therefore multiplied by the ratio of the intersecting

¹⁸ In this toy model, we limit ourselves to the NFW profiles for the sub-clumps in the dSph, and a $c_{\text{vir}} - M_{\text{vir}}$ relation taken from Bullock et al. (2001).

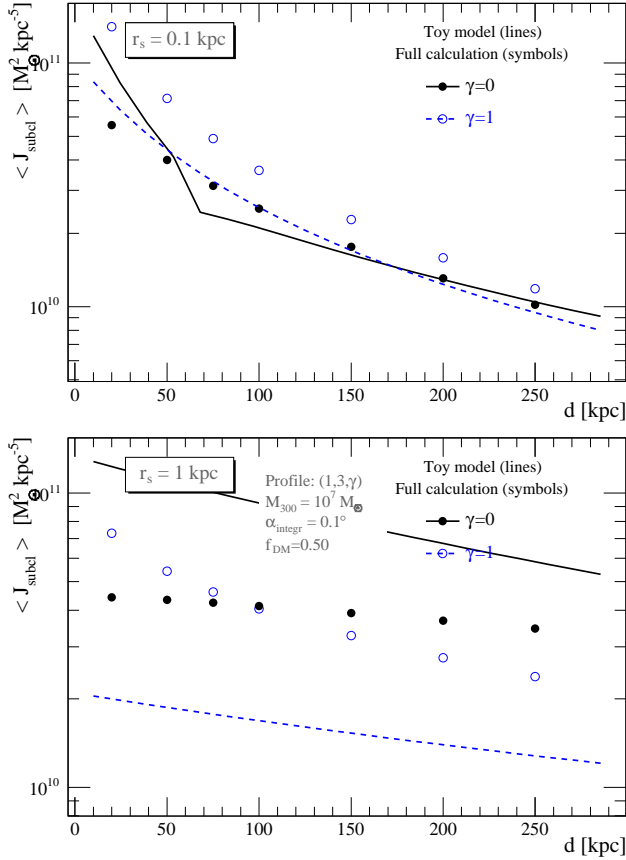


Figure B3. Toy-model calculation (lines) vs full numerical integration (symbols) of J as a function of the distance to the dSph. The integration angle is fixed to $\alpha_{\text{int}} = 0.1^{\circ}$ and the two $(1, 3, \gamma)$ sub-clump spatial distribution are $\gamma = 0$ and $\gamma = 1$ (their inner profile is a NFW with a $c_{\text{vir}} - M_{\text{vir}}$ relation taken from Bullock et al. (2001)). The calculations assume the fraction of DM in sub-clumps to be $f = 50\%$ of the total mass of the dSphs, where the smooth profile is taken as in Fig. B2. **Top:** $r_s = 0.1$ kpc. **Bottom:** $r_s = 1$ kpc.

cone volume to the integration sphere volume, in order to account for that effect.

If the mass of the dSph is M_{vir} and assuming a fraction f of this mass is in the form of clumps, one gets using Eq. (B9)

$$N_{\text{tot}}^{\text{cl}} = f \frac{2-a}{A} M_{\text{vir}} (M_{\text{max}}^{2-a} - M_{\text{min}}^{2-a})^{-1}.$$

Resulting formulae Adding all ingredients together, the contribution of the sub-structures to the flux is

$$J_{\text{clumps}} = 1.17 \times 10^8 \frac{F_{\text{core/cusp}}}{d^2} \left(\frac{2-a}{1.91-a} \right) \times \left(\frac{M_{\text{max}}^{1.91-a} - M_{\text{min}}^{1.91-a}}{M_{\text{max}}^{2-a} - M_{\text{min}}^{2-a}} \right) f M_{\text{vir}}. \quad (\text{B18})$$

Toy model vs numerical integration The comparison between the two is shown in Fig. B3. The symbols show the full numerical integration while the lines show the toy-model calculations. For $r_s = 100$ pc, the agreement is better than a factor of 2 for all distances. For $r_s = 1$ kpc, the toy model only gives results correct to within a factor of 4 for $\gamma = 1$.

Hence, given the current uncertainties on the profiles,

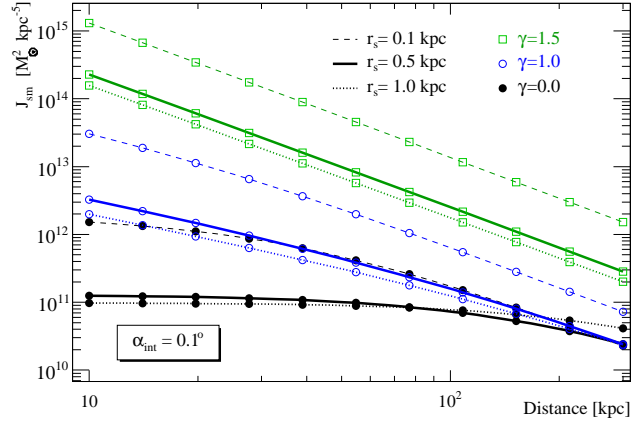


Figure C1. $J_{\text{sm}}(\theta = 0)$ as a function of the distance to the dSph for three profiles γ and three values of r_s . The corresponding values for ρ_s are given in Table 1.

Eq. (B19) can be used for quick inspection of the J value for the sub-clump contribution.

APPENDIX C: DISTANCE AND INTEGRATION ANGLE DEPENDENCE ON J FOR GENERIC DSPHS

This Appendix completes the study of the J -factor dependences started in Section 2.3. All the plots and discussions below rely on the generic profiles given in Table 1, and the sub-structure reference configuration given in Section 2.2.3.

C1 Distance dependence $J(d)$

Fig. C1 shows J_{sm} as a function of the distance to the dSph (we assume $\alpha_{\text{int}} = 0.1^{\circ}$ here and that we are pointing towards the dSph centre, i.e. $\theta = 0$). As we have checked earlier, the sub-clump contribution for the reference model at $\theta = 0$ is always sub-dominant, so for clarity only J_{sm} is displayed ($f = 0$) in the figure.

If the angular size of the signal is smaller than the integration angle, the distance dependence is expected to be $J_{\text{sm}} \propto d^{-2}$. This is the case for $\gamma = 1.5$ for any value of r_s (hollow squares curves). Actually, the three curves follow the point-like source toy formula (B6) appropriate for steep γ , i.e.

$$J(\theta = 0) \propto \rho_s^2 \times \frac{r_s^3}{d^2}. \quad (\text{C1})$$

However, when the angular size of the emitting region becomes larger than the integration angle, the above relationship fails. As most of the flux is emitted within r_s , this happens for a critical distance

$$d_{\text{crit}} \approx \frac{r_s}{\alpha_{\text{int}}}. \quad (\text{C2})$$

For $r_s = 0.1$ kpc, this corresponds to $d_{\text{crit}} \approx 60$ kpc (see the full circles dashed curve for $\gamma = 0$). Having a dSph closer than this critical distance does not increase further the signal (see, e.g., the solid and dotted full circles curves for $\gamma = 0$ and $r_s \gtrsim 0.5$ kpc). In the latter case, taking a larger integration region is not always the best strategy as, from an experimental point of view, a larger integration region increases not only the signal but also the background. In this case, the gain in sensitivity from having a dSph close by is not as

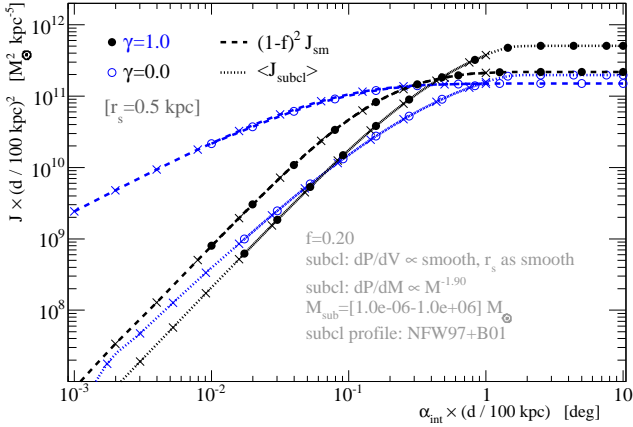


Figure C2. $J \times (d/100 \text{ kpc})^2$ as a function of $\alpha_{\text{int}} \times (d/100 \text{ kpc})$ for a generic dSph with $r_s=0.5 \text{ kpc}$: smooth (thick dashed lines) and sub-clumps (thin dotted lines). With this rescaling, the case $d = 10 \text{ kpc}$ (stars) superimposes on the case $d = 100 \text{ kpc}$ (empty and full circles).

important as what might naïvely be expected from the point-like approximation (see Section 3).

C2 Integration angle dependence $J(\alpha_{\text{int}})$

We recall that $\int_{\Delta\Omega} d\Omega = \int_0^{2\pi} d\beta_{\text{int}} \int_0^{\alpha_{\text{int}}} \sin(\alpha_{\text{int}}) d\alpha_{\text{int}}$, where $\Delta\Omega = 2\pi(1 - \cos(\alpha_{\text{int}}))$, so that the J -factor from Eq. (5) can be rewritten in the symbolic notation

$$J(\psi, \theta, \Delta\Omega) = \int_0^{2\pi} F_{[\beta_{\text{int}}]} d\beta_{\text{int}} \quad (\text{C3})$$

with

$$F_{[\beta_{\text{int}}]} = \int_0^{\alpha_{\text{int}}} F_{[\beta_{\text{int}}, \alpha_{\text{int}}]} d\alpha'_{\text{int}} \quad (\text{C4})$$

and

$$F_{[\beta_{\text{int}}, \alpha_{\text{int}}]} = \sin(\alpha_{\text{int}}) \int_0^{l_{\text{max}}} \mathcal{F}[r(l, \beta_{\text{int}}, \alpha_{\text{int}})] dl. \quad (\text{C5})$$

For small integration angles and the case of a flat enough profile, the integrand in Eqs. (C4) and (C5) does not vary much with α_{int} , so that for the smooth ($\mathcal{F} \equiv \rho^2$) and the mean sub-clumps ($\mathcal{F} \equiv \rho$), we have

$$J_{\text{sm}} \propto \alpha_{\text{int}}^2 \quad \text{and} \quad \langle J_{\text{subcl}} \rangle \propto \alpha_{\text{int}}^2. \quad (\text{C6})$$

Fig. C2 shows the integration angle dependence for the smooth $(1-f)^2 J_{\text{sm}}$ (dashed lines) and the sub-clump mean $\langle J_{\text{subcl}} \rangle$ (dotted lines) contributions. (The pointing direction is towards the dSph centre.) For $\gamma = 0$ (solid black circles), the α_{int}^2 scaling holds up to $\alpha_{\text{int}}^{\text{crit}} \sim 3^\circ$ if $d = 10 \text{ kpc}$ (as given by Eq. C2). A plateau is reached when the entire emitting region of the dSph is encompassed (i.e. for a few r_s/d). For $\gamma = 1$ (blue empty circles), the curves are slightly more difficult to interpret, as the profile is not steep enough for it to be considered fully point-like (and thus ‘independent’ of α_{int}) given the integration angles considered.¹⁹

¹⁹ The dependence can be understood by means of the toy model formulae (B6) and (B7). For $\alpha_{\text{int}} < \alpha_{\text{int}}^{\text{crit}}$, we have

$$J_{[\gamma \geq 0.5]} \propto r_s^{2\gamma} \times (\alpha_{\text{int}} d)^{3-2\gamma}.$$

For $\gamma = 1$ (empty blue circles), J is then expected to scale linearly with

Table D1. Maximum boost and transition regime, i.e. $(\alpha_{\text{int}} d)_{B=1}$ in deg kpc, for which $B = 1$, for various smooth/sub-clump parameters for three inner slope γ (for the smooth).

Config. [†]	$\gamma = 0$	$\gamma = 0.5$	$\gamma = 1$
reference [‡]	1.9 19	2.2 21	2.0 30
[global parameters]			
$\alpha = 1$	1.0 40	1.3 60	1.6 160
$\beta = 5$	2.3 11	2.0 18	1.3 36
$R_{\text{vir}} = 6 \text{ kpc}$	3.0 15	3.5 20	2.9 29
$M_{300} = 2 \cdot 10^7 M_\odot$	1.3 66	1.4 52	1.3 64
[sub-clump parameters]			
$dP/dV = \text{Einasto}^*$	1.4 ...	1.7 ...	1.7 22
$a = 1.7$	1.3 62	1.5 50	1.3 61
$a = 2.0$	2.8 0.2	3.4 8	2.9 16
$M_{\text{min}} = 1 M_\odot$	1.5 43	1.7 37	1.5 47
$M_{\text{max}} = 10^4 M_\odot$	2.4 4	2.8 14	2.5 22
$f = 0.5$	3.4 10	4.2 16	3.5 25
$\rho_{\text{subcl}} = \text{Einasto}$	8.7 0.05	10.6 0.35	9.0 4
$c_{\text{vir}} \times 2$	7.6 0.06	9.3 0.4	7.9 4.5

[†] All parameters are as for *reference*, except those quoted.

[‡] Reference configuration ($M_{300} = 10^7 M_\odot$):

- ρ_{sm} with $(\alpha, \beta, \gamma) = (1, 3, \gamma)$ and $dP/dV \propto \rho_{\text{sm}}$;
- $R_{\text{vir}} = 3 \text{ kpc}$ and $r_s = 1 \text{ kpc}$ (for ρ_{sm} and dP/dV);
- $dP/dM = M^{-a}$ ($a = 1.9$), and $M_{\text{sub}} \in [10^{-6} - 10^6] M_\odot$;
- $f = 0.2$, $\rho_{\text{subcl}} = \text{NFW}$, and $c_{\text{vir}} = M_{\text{vir}} = \text{B01}$.

* Einasto parameters taken from Merritt et al. (2006).

Finally, the rescaling used in Fig. C2 implies:

$$J_{\text{d1}}(\alpha_{\text{int}}) = J_{\text{d2}} \left(\alpha_{\text{int}} \frac{d_2}{d_1} \right) \times \left(\frac{d_2}{d_1} \right)^2. \quad (\text{C7})$$

APPENDIX D: COMPLEMENTARY STUDY OF THE BOOST FACTOR

In Section 2.3.2, we concluded that the boost could not be larger than a factor of 2 for all configurations where the sub-clump spatial distribution follows that of the smooth halo in the dSph. The calculations were also made for a ‘reference’ configuration of the sub-clumps. However, the boost can be smaller (or larger) when the latter parameters are varied.

In Tab. D1, we systematically vary all the parameters entering the calculation in order to compare with the reference model case. The two quantities of importance are the maximum boost possible (which is obtained when α_{int} fully encompasses the clump), and the transition point $\alpha_{\text{int}} d$ for which the boost equals 1 (the minimum value is always given by $(1-f)^2$). The *reference* results correspond to the numbers obtained from the dotted lines in Fig. 5, i.e. for $r_s = 1 \text{ kpc}$. Note that most of the values for B_{max} in the Table would be close to unity if $r_s = 0.1 \text{ kpc}$ were to be selected.

α_{int} , which is observed for the smooth (dashed blue line), and to some extent for the sub-clump contribution (dotted blue line). However, for the latter, the transition region (around r_s) falls from a slope $\alpha = 1$ towards an outer slope $\beta = 3$ (instead of falling from $\alpha^2 = 1$ to $\beta^2 = 6$). Hence, for $\alpha_{\text{int}} > \alpha_{\text{int}}^{\text{crit}}$, the sub-clump contribution continues to build up gradually.

D1 Varying the [global parameters]

The four lines under '[global parameters]' keeps the recipe of $dP/dV \propto \rho_{\text{sm}}$, but some previously fixed parameters are now varied. The trend is that a sharper transition zone (larger α), a larger radius of the dSph, or a smaller mass imply a larger B_{max} . The impact of the outer slope β depends on the value of the inner slope γ . However, the maximum boost factor reached for these parameters is never larger than ~ 3 . The typical transition value lies around 20° kpc, which corresponds, for a dSphs located 100 kpc away, to an integration angle of 0.2° . Hence, for all these configuration, large integration angle should be preferred (this is even worse for closer dSph).

D2 Varying the [sub-clump parameters]

The remaining lines under [sub-clump parameters] show the impact of the choice of the distribution of sub-clumps, the mass distribution parameters (minimal mass and maximal mass of the sub-clumps, slope a of dP/dM), and the density profile of the sub-clumps. Relaxing the condition $dP/dV \propto \rho_{\text{sm}}$ has no major impact. In Springel et al. (2008), a simple Einasto profile with universal parameters was found to fit all halos (from the Aquarius simulation) independently of the halo mass. For that specific case, we use the values found for the Galaxy in Merritt et al. (2006). The Einasto profile is steeper than $\gamma = 0$ but it decreases logarithmically inwards. Only for $\gamma \gtrsim 1$ (for the smooth component) such a model is able to marginally increase the maximum boost w.r.t. the reference model (instead of decreasing it), which is not unexpected.²⁰ Varying the mass distribution slope a is understood as follows: for $a \approx 1.9$, all decades in mass contribute about the same amount. When a is decreased, the less massive sub-halos dominate, whereas for $a \gtrsim 1.9$, the most massive sub-halos dominate the luminosity (e.g. Fig. 4 of Laval et al. 2008). This has to be balanced by the fact that the fraction of DM going into sub-clumps remain the same ($f = 0.2$), regardless of the value of a , so that the total number of clumps in a mass decade also changes. The net result is a smaller boost when a is decreased, and a larger boost from the more massive sub-structure when α is increased. In a similar way (a is now fixed to 1.9 again), the mass also impact on B , but in a marginal way. The only sizeable impact comes from varying the fraction of mass into clumps, the sub-clump profile or the concentration of sub-clumps. In the first case, when f increases, the smooth signal decreases by $(1-f)^2$ whereas the sub-clump signal increases as f . Even if f is increased up to 50%, which is very unlikely (recent simulations such as Springel et al. (2008) tend to give an upper limit of $f \lesssim 10\%$) this gives only a mild enhancement. In the second configuration, the NFW profile for the sub-clumps is replaced by an Einasto one. Despite its logarithmic slope decreasing faster than the NFW slope $\gamma = 1$ below some critical radius, the latter profile is known to give slightly more signal than the NFW one ($\rho_{\text{Einasto}}(r) > \rho_{\text{NFW}}(r)$ for a region that matters for the J calculation). This results in a boost close to 10, regardless of the dSph's smooth profile. Finally, we recall that the B01 $c_{\text{vir}} - M_{\text{vir}}$ relation is used to calculate the value of the scale parameter for any sub-clump mass. In the last configuration, the concentration

²⁰ For smaller γ , the smooth distribution, in that case, is flatter than the sub-clump one, so that the boost is larger than one for small α_{int} and the transition where $B = 1$ is ill-defined. However, such a configuration is highly unlikely as it is exactly the opposite of what is observed in all N-body simulations.

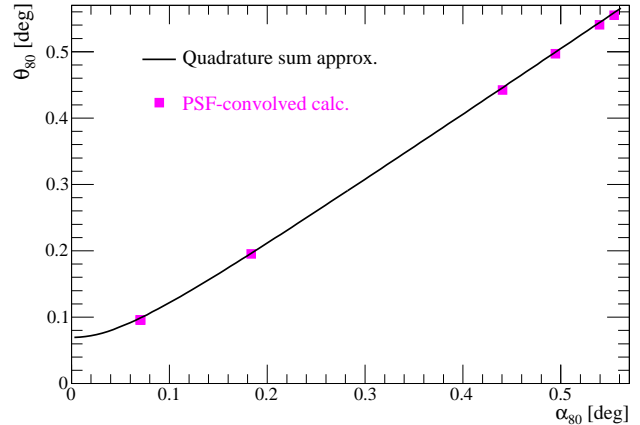


Figure E1. 80% containment radius (θ_{80}) of PSF-convolved DM annihilation halo models versus α_{80} .

parameter is simply multiplied by a factor of 2, which is probably not realistic. Again, the same boost of ~ 10 is observed. Accordingly, for these last two cases, the transition angle is reduced, and corresponds to $\alpha_{\text{int}} < 0.01^\circ$ (for a dSphs at 100 kpc).

To conclude, although boosts by as large as a factor of 10 can be obtained through suitable combinations of parameters, most of these combinations are unlikely and require the signal to be integrated on large angles.

APPENDIX E: IMPACT OF THE PSF OF THE INSTRUMENT

Fig. E1 shows the impact of the instrument angular resolution on the 80% containment radius for J (for the generic dSphs studied in Sec. 3). The solid line corresponds to the quadrature approximation given by Eq. (15), whereas the symbols correspond to the convolved PSF*halo profile. The PSF is described by the sum of two Gaussians and is a scaled (factor two improved) version of the PSF appropriate for H.E.S.S. at 200 GeV. Calculated halos for a range of α , β , γ models consistent with the stellar kinematics of the classical dSphs are shown as gray squares. The quadrature sum approximation used in this work is shown as a solid line.

APPENDIX F: CONFIDENCE LEVELS AND PRIORS

In this Appendix, we describe how confidence intervals for the quantities such as $\rho(r)$ or J are chosen.

F1 Sensitivity of the result to the choice of prior

In the Bayesian approach, the PDF of a parameter x is given by the product of the MCMC output PDF $\mathcal{P}(x)$ and the prior $p(x)$. The resulting PDF is therefore subjective, since it depends on the adoption of a prior. However, whenever the latter are not strongly dependent on x , or if $\mathcal{P}(x)$ falls in a range where $p(x)$ does not strongly varies, the PDF of the parameter becomes insensitive to the prior. This happens for instance if the data give tight constraints on the parameters.

In our MCMC analysis, we assumed a flat prior for all our halo parameters, as there is no observationally motivated reason for doing otherwise. Note, however, that flat priors on the model

parameters do not necessarily translate into flat priors on quantities derived from those parameters. Specifically, the flat priors on our model parameters imply a non-flat prior on the DM density (and also on its logarithm) at a given radius, and hence a non-flat prior on J . In principle it is possible to choose a combination of priors for the parameters that would translate into flat priors on $\rho(r)$, but we have not done so here. The general impact of such choices, and the methodology to study the prior-dependent results, has been discussed in the context of cosmological studies by Valkenburg et al. (2008). In this study, we only use a flat prior on the parameters (or on the log for r_s and ρ_s). The test with artificial data demonstrate that our reconstructed ρ and J values are sound.

F2 Confidence intervals for $\rho(r)$ and cross-checks

F2.1 Definition

Confidence intervals Δ_x (CI), associated with a confidence level $x\%$ (CL), are constructed from the PDF. The asymmetric interval $\Delta_x \equiv [\theta_x^-, \theta_x^+]$ such as

$$\text{CL}(x) \equiv \int_{\Delta_x} \mathcal{P}(\theta) d\theta = 1 - \gamma,$$

defines the $1 - \gamma$ confidence level (CL), along with the CI of the parameter θ . We rely on two standard practises for the CI selection. The first one (used only in this Appendix) is to fix θ_x^- to be the lowest value of the PDF. The CLs correspond then to quantiles. This is useful for CI selection of χ^2 values, to ensure that the best-fit value of a model (i.e. the lowest χ^2) falls in the CI (see, e.g., Fig. 7 of Putze et al. 2009). In the second approach, the CI, i.e. θ_x^- (resp. θ_x^+), is found by starting from the median θ^{med} of the PDF and decrease (resp. increase) θ_x until we get $x\%/2$ of the integral of the PDF. This approach ensures that the median value of the parameters falls in the CI, any asymmetry in the CI illustrating the departure from a Gaussian PDF: this is the one used throughout the paper.

F2.2 Comparison of several choices for the PDF of $\rho(r)$

Fig. F1 shows the projection for each r of the PDF calculated from the output MCMC file. To do so, $\rho(r)$ is calculated for each entry of the thinned chains and then stored as an histogram. This results in 'boxes': the larger the box, the more likely the value of $\rho(r)$. From this distribution, we can calculate the median (thick solid black line), the most probable value (thick dotted black line). The thick solid red line correspond to the model having the smallest χ^2 value. We see that the latter differ from the median one for this dSph, though they can be close for other dSph in our sample. In this paper, as our analysis is based on the Bayesian approach, we disregard the best-fit model and only retain the median value.

In the first approach, the 68% and 95% CLs are calculated from the distribution ρ_r (at each r) They are shown as dashed and dotted thick black lines. Note that none of all the above lines corresponds to a *physical* configuration of $\rho(r)$.

A second approach is to construct the 68% CLs from a sampling of the (still) correlated parameters. This is achieved by using all sets of parameters $\{\vec{\theta}\}_{x\% \text{ CL}} = \{\vec{\theta}_i\}_{i=1 \dots p}$, for which $\chi^2(\vec{\theta}_i)$ falls in the 68% CL of the χ^2 PDF (see above). Once these sets are found, we calculate $\rho(r)$ for each of them, and keep the maximum and minimum values for each position r . This defines envelopes of $\rho(r)$ (CIs are found for each r). This is shown as dotted and dashed red lines. Such an approach was used in Putze et al. (2009).

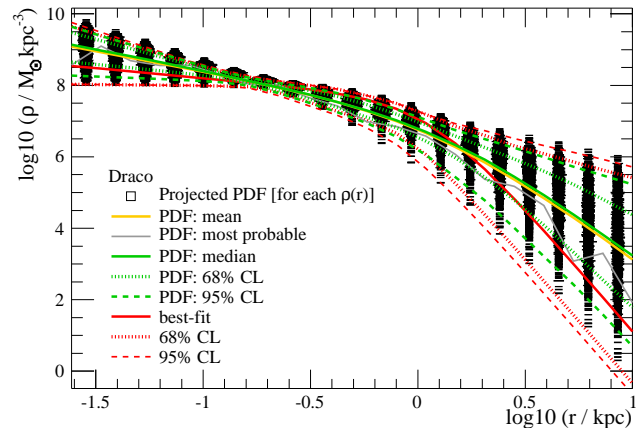


Figure F1. Projected distribution of $\log_{10}(\rho)$ along with the value of several other estimators for the MCMC analysis of Draco. In this box projection, the larger the box, the most likely the probability of $\log_{10}(\rho)$. For instance, on the top panel, for $\log_{10}(r) = -1.5$ the probability density function of $\log_{10}(\rho)$ is distributed in the range $[8 - 10]$ and peaks around 9.5).

The CLs obtained from it are larger than the previous one. In the above paper, the uncertainties were small even with that method, so that was not an issue. However, in this study, this makes a huge difference in the resulting value CL of J .

In order to check which approach was the correct one, we bootstrapped the Draco kinematic data and calculate from the collection of $\rho(r)$ from each bootstrap sample the median value and the uncertainty. The first approach, where the CLs are directly calculated from the full set of MCMC samples was in agreement with the bootstrap approach, meaning that the second one biases the results toward too large uncertainties. The results of the paper rely thus on the first and correct approach.

APPENDIX G: ARTIFICIAL DATA SETS: VALIDATION OF THE MCMC ANALYSIS

In this section, we examine the reliability of the Jeans/MCMC analysis by applying it to artificial data sets of 1000 stellar positions and velocities drawn directly from distribution functions with constant velocity anisotropy. We assume the form $L^{-2\beta_{\text{aniso}}} f(\varepsilon)$ for the distribution functions, where the (constant) velocity anisotropy is given by $\beta_{\text{aniso}} = 1 - \sigma_t^2/\sigma_r^2$, with σ_t^2 and σ_r^2 being the second moments of the velocity distribution in the radial and tangential directions, respectively. The function $f(\varepsilon)$ is an unspecified function of energy ε which we determine numerically using an Abel inversion once the halo model and stellar density are specified (Cuddeford 1991). We used the same models in Walker et al. (2011), but we present here a more general study. The set of artificial data covers a grid of models with $\gamma = 0.1, 0.5, 1.0$, $r_h/r_s = 0.1, 0.5, 1.0$ and $\beta = 3.1$. For each halo model, we assume β_{aniso} values of 0 (isotropic), 0.25 (radial) or -0.75 (tangential): the β_{aniso} values for the anisotropic models are chosen to give models with roughly equivalent levels of anisotropy (in terms of the ratios of the velocity dispersions in the radial and tangential directions). We also generate a grid of models with a steeper inner slope $\gamma = 1.5$ and $\beta = 4.0$. In all cases, the haloes contain $\sim 10^7 M_\odot$ within 300pc. We mimic the effects of observational errors by adding Gaussian noise with a dispersion of 2 km s^{-1} to each

individual stellar velocity generated from the distribution function. The reconstruction depends on the choice of the prior γ_{prior} , and this effect is explored in the two sections below.

G1 Prior: $0 \leq \gamma_{\text{prior}} \leq 1$ versus $0 \leq \gamma_{\text{prior}} \leq 2$

We start with the free γ_{prior} analysis (see Sec. 5.1) based on two different priors. Top panels of Fig. G1 show the ratio of the reconstructed median profile to the true profile. There is no significant differences for $\rho(r \gtrsim 1 \text{ kpc})$ when using the prior $0 \leq \gamma_{\text{prior}} \leq 2$ (top right) or $0 \leq \gamma_{\text{prior}} \leq 1$ (top left): at large radii, the profile does not depend any longer on the γ parameter. However, it is striking to see that restricting the prior to $0 \leq \gamma_{\text{prior}} \leq 1$ greatly improves the determination of the inner regions for the profile, regardless of the value of γ_{true} . Even for $\gamma_{\text{true}} = 1.5$ (green curves), using an incorrect prior does not degrade to much the reconstruction of the profile.

This results is further emphasised when looking at J . The bottom panels of Fig. G1 are plotted with the same scale to emphasise the difference. As J integrates over the inner parts of the profile, the median MCMC value can strongly differ from the true value for cuspy profiles. This difference can reach up to 5 orders of magnitude (over the whole range of α_{int}) for $\gamma_{\text{true}} \gtrsim 0.5$ when using the prior $0 \leq \gamma_{\text{prior}} \leq 2$. The prior $0 \leq \gamma_{\text{prior}} \leq 1$ does generally better, and accordingly, the confidence intervals are much smaller than for the other prior (for any integration angle).

The behaviour of the $\gamma_{\text{true}} = 1.5$ case is unexpected. Using the prior $0 \leq \gamma_{\text{prior}} \leq 1$ does better than the other one for any integration angle. Indeed, even if the reconstructed median value is shifted by a factor of 10, its CLs correctly encompass the true value. It does better than the $0 \leq \gamma_{\text{prior}} \leq 1$ prior, which correctly provides CLs (that bracket the true value), but which are completely useless as these CLs can vary on ~ 8 orders of magnitude.

G2 Strong prior: γ_{prior} fixed

In Fig. G2 below, we use a prior $\gamma_{\text{prior}} = 0$ for models having $\gamma_{\text{true}} = 0$, a prior $\gamma_{\text{prior}} = 0.5$ for models having $\gamma_{\text{true}} = 0.5$, etc.

A comparison of Figs. G1 (using $0 \leq \gamma_{\text{prior}} \leq 1$ or $0 \leq \gamma_{\text{prior}} \leq 2$) and G2 (fixed γ_{prior}) shows that the latter prior only slightly improves the precision of the J -factor reconstruction for $\gamma_{\text{true}} = 0$, $\gamma_{\text{true}} = 0.5$, and $\gamma_{\text{true}} = 1$. However, if $\gamma_{\text{true}} = 1.5$ (green curves), although the corresponding J -factor is now better reconstructed than when using the prior $0 \leq \gamma_{\text{prior}} \leq 2$ (Figs G1, top panel), it is surprisingly less reliable than the strongly biased $0 \leq \gamma_{\text{prior}} \leq 1$ prior.

The main conclusion is that the knowledge of γ_{true} does not help providing tighter constraints on J : the uncertainty remains a factor of a few, except when the inner profile is really cuspy ($\gamma_{\text{true}} = 1.5$), in which case it becomes strongly biased/unreliable.

APPENDIX H: OTHER RECONSTRUCTION 'BIASES' ON THE J -FACTOR

In this Appendix, the MCMC analysis is performed based on the prior $0 \leq \gamma_{\text{prior}} \leq 1$, for which the analysis is found to be the most robust (see previous Appendix).

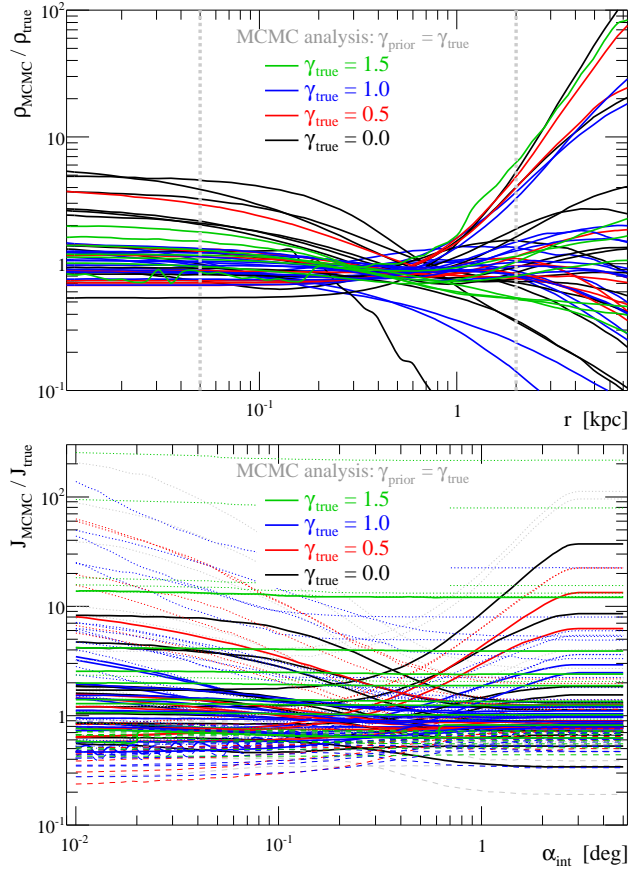


Figure G2. Fixed γ_{prior} MCMC analysis. **Top:** $\rho(r)$. **Bottom:** $J(\alpha_{\text{int}})$.

H1 Impact of the binning of the stars

Figure H1 shows the impact of using different binnings in the MCMC analysis. The left panel shows the reconstructed (median) value of the velocity dispersion as a function of the logarithm of r (to emphasise the differences at small radii), for a binning used in this paper (black; where each of \sqrt{N} bins has \sqrt{N} member stars, where N is the total number of members), a binning with two times (red) and four times (blue) fewer bins. For Fornax and Sculptor, the profiles are insensitive to the binning chosen, so that the reconstruction of the J values median and 68% CLs (right panel) is robust. For other dSphs, either the adjusted velocity dispersion profile is affected at small radii, or at large radii. In the latter case, the J calculation should not be affected, as the outer part does not contribute much to the annihilation signal. In the former case, a deviation even at small radii can affect the associated J by a factor of a few. The exact impact depends on the integration angle, the distance to the dSph (which corresponds to a given radius), and the 'cuspiness' of the reconstructed profile (the J value of a core profile will be less sensitive to differences in the inner parts than would be a cuspy profile). For instance, Draco and Leo1 both have a 2 km/s uncertainty below 100 pc, but Draco is three times closer than Leo1: their J for a given α_{int} have different behaviours (right panel). The strongest impact is for Leo1 that have the fewest data. The flatness of the J curve seems to indicate a cuspy profile (all the signal in the very inner parts), which we know are the least well reconstructed ones (see Appendix G1). Leo1 is thus the most sensitive dSph to the binning, for which a balance between a sufficient coverage over r and small error bars cannot be achieved. The ultra-faints dSphs are expected

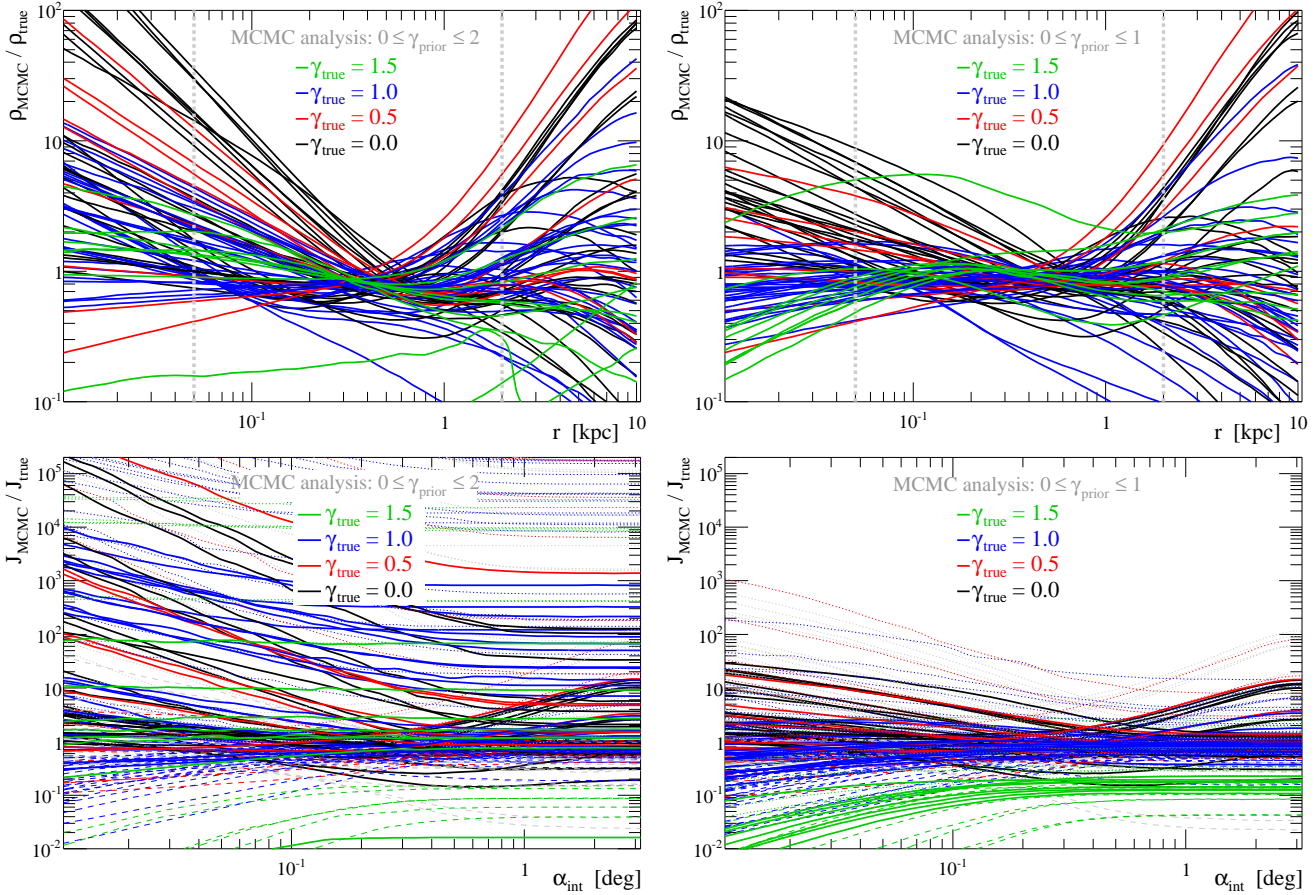


Figure G1. Ratio of the MCMC profile to the true profile. The lines are colour-coded with respect to the value of the true inner slope γ_{true} of the artificial data. **Top panels:** ratio of the median $\rho(r)$. The two vertical gray dashed lines correspond to the typical range within which the artificial data bin are taken. **Bottom panels:** ratio of $J(\alpha_{\text{int}})$ for the artificial dSphs located at 100 kpc. **Left panels:** MCMC analysis with the prior $0 \leq \gamma_{\text{prior}} \leq 2$. **Right panels:** the prior is $0 \leq \gamma_{\text{prior}} \leq 1$.

to have even fewer stars, so that their J calculation is expected to be even more uncertain.

Overall, the choice of the binning can produce an additional bias of a few on the J reconstruction. This is an extra uncertainty factor that makes Fornax and Sculptor the more robust targets with respect to their annihilation signal. Surveys in the inner parts and outer parts of Carina, Draco, Sextans, Leo I, Leo II and Ursa Minor are desired to get rid of this binning bias.

H2 Impact of the choice of the light profile

Figure H2 shows the various median values and 68% CIs of J when changing the assumptions made on the light profile. The black lines labeled ‘physical’ correspond to the Plummer model used for the main analysis (see Eq. 21); the red lines labeled ‘unphysical’ are also Plummer, but the physical constraint given by Eq. (25) is relaxed; the blue lines and green lines correspond respectively to a light profile modeled with an (α, β, γ) profile in order to get a steeper outer slope (2, 6, 0) or a steeper inner slope (2, 5, 1) with respect to the Plummer profile. Regardless of the light profile used, we recover similar critical angles for which J is the most constrained. The impact on the J value is strongest for the least-well measured profiles (Leo 2 and Sextans), but is contained within the 95% CI and marginally within the 68% CL.

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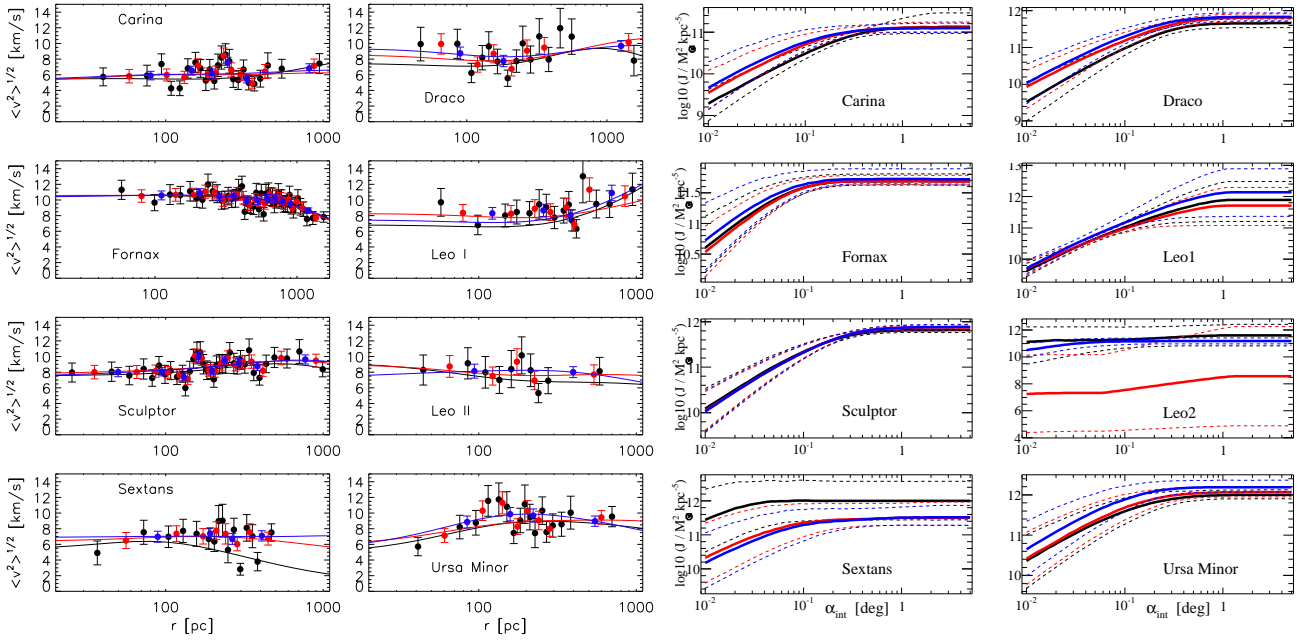


Figure H1. For the 8 classical dSphs, impact of using several binnings of the stars: black is the binning used throughout this paper (i.e. \sqrt{N} bins), red has $\sqrt{N}/2$ bins, and blue has $\sqrt{N}/4$ bins. **Left:** velocity dispersion as a function of $\log(r)$ (symbols are data, lines are the MCMC median values based on the data). **Right:** corresponding median values and 68% CI for $J(\alpha_{\text{int}})$.

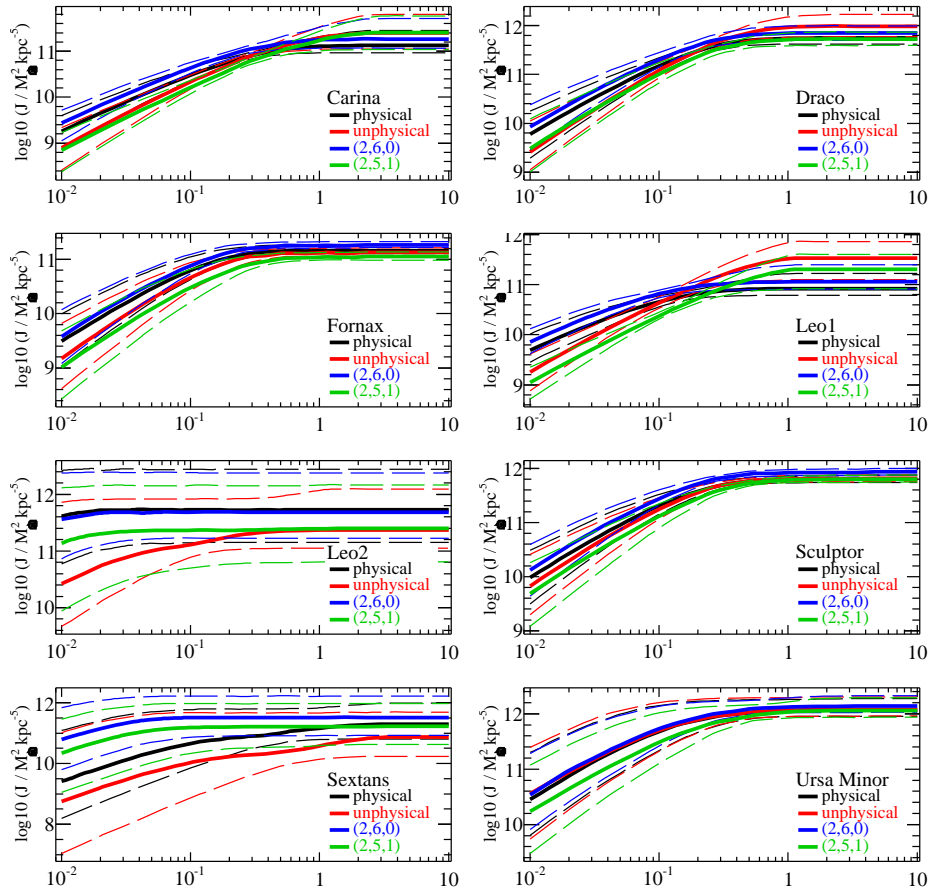


Figure H2. For the 8 classical dSphs, impact of using different light-profiles (see text). Solid lines are the MCMC median values and dashed lines the 68% CI for $J(\alpha_{\text{int}})$.

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