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New observables in the decay mode $\bar{B}_d \rightarrow \bar{K}^{*0} \ell^+ \ell^-$

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Abstract

We discuss the large set of observables available from the angular distributions of the decay $\bar{B}_d \rightarrow \bar{K}^{*0} \ell^+ \ell^-$. We present a NLO analysis of all observables based on the QCD factorization approach in the low-dilepton mass region and an estimate of Λ/m_b corrections. Moreover, we discuss their sensitivity to new physics. We explore the experimental sensitivities at LHCb (10 fb⁻¹) and SuperLHCb (100 fb⁻¹) based on a full-angular fit method and explore the sensitivity to right handed currents. We also show that the previously discussed transversity amplitude $A_T^{(1)}$ cannot be measured at the LHCb experiment or at future B factory experiments as it requires a measurement of the spin of the final state particles.

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1 Introduction

A major aim of particle physics in the LHC era is the discovery of new degrees of freedom at the TeV energy scale which might contribute to our understanding of the origin of electroweak symmetry breaking. Rare B and kaon decays (for reviews see [1–3]) representing loop-induced processes are highly sensitive probes for new degrees of freedom beyond the Standard Model (SM) and will be used when making indirect searches for these unknown effects. It is well-known that the indirect constraints on new physics (NP) from the present flavour data indicate a NP scale much higher than the electroweak scale when such new effects are naturally parameterised by higher-dimensional operators. Thus, if there is NP at the electroweak scale, then its flavour structure has to be highly non-trivial and the experimental measurement of flavour-violating couplings is mandatory. This ‘flavour problem’, namely why flavour-changing neutral currents are suppressed, has to be solved by any NP scenario at the electroweak scale.

In this article we discuss theoretical and experimental preparations for an indirect NP search using the rare decay $\bar{B}_d \rightarrow \bar{K}^{*0} \mu^+ \mu^-$. This exclusive decay was first observed at Belle [4]. It offers a rich phenomenology of various kinematical distributions beyond the measurement of the branching ratio. Some experimental analyses of those angular distributions are already presented by the B factories [5–8] but only the large increase in statistics at LHCb [9–11] for $\bar{B}_d \rightarrow \bar{K}^{*0} \mu^+ \mu^-$ will make much higher precision measurements possible. There are also great opportunities at the future (Super-) B factories in this respect [12–15]. A careful choice of observables needs to be made to take full advantage of this exclusive decay as only in certain ratios such as CP and forward-backward asymmetries, the hadronic uncertainties cancel out in specific observables making such ratios the only observables that are sensitive to NP. In this respect the by now standard theoretical tools like QCD factorization (QCDF) and its quantum field theoretical formulation, soft-collinear effective theory (SCET), are crucial. They imply form factor relations which simplify the theoretical structure of various kinematical distributions such that at least at the leading order (LO) level any hadronic uncertainties cancel out. A well-known example of this is the zero-crossing of the forward-backward asymmetry.

We construct new observables of this kind in the $\bar{B}_d \rightarrow \bar{K}^{*0} \mu^+ \mu^-$ decay which have very small theoretical uncertainties and good experimental resolution. Moreover, it is possible to design the new observables for a specific kind of NP operator within the model-independent analysis using the effective field theory approach.

Previously proposed angular distributions and CP violating observables in $\bar{B}_d \rightarrow \bar{K}^{*0} \mu^+ \mu^-$ are reviewed in Ref. [16], and more recently QCDF analyses of such angular distributions [17, 18] and CP violating observables [19] were presented.

The paper is organised as follows: in Sec. 2 we recall the differential decay distribution in the $\bar{B}_d \rightarrow \bar{K}^{*0} \mu^+ \mu^-$ decay; in Sec. 3 we recall the basic theoretical formulae which are crucial for our construction of new observables; in Sec. 4 we discuss the basic properties and symmetries of potential observables and propose a new set of observables which are sensitive to new right-handed currents and we also discuss the previously proposed quantity $A_T^{(1)}$; in Sec. 5 we explain our method to calculate the experimental sensitivity obtainable with the statistics of LHCb to new and old observables; and finally in Sec. 6 we present our phenomenological analysis, in particular we analyse the theoretical and experimental sensitivity to NP. We also comment very briefly on recent *BABAR* measurements of certain angular distributions. In appendices we make angular definitions explicit, provide the theoretical framework for the derivation of the spin amplitudes, and present the theoretical NLO expressions.

2 Differential decay distribution

The decay $\bar{B}_d \rightarrow \bar{K}^{*0} \ell^+ \ell^-$ with $\bar{K}^{*0} \rightarrow K^- \pi^+$ on the mass shell, is completely described by four independent kinematic variables, the lepton-pair invariant mass squared, q^2 , and the three angles θ_l , θ_K , ϕ . Summing over the spins of the final particles, the differential decay distribution of $\bar{B}_d \rightarrow \bar{K}^{*0} \ell^+ \ell^-$ can be written as

$$\frac{d^4 \Gamma_{\bar{B}_d}}{dq^2 d\theta_l d\theta_K d\phi} = \frac{9}{32\pi} I(q^2, \theta_l, \theta_K, \phi) \sin \theta_l \sin \theta_K, \quad (2.1)$$

with the physical region of phase space $4m_l^2 \leq q^2 \leq (m_B - m_{K^*})^2$ and

$$\begin{aligned} I = & I_1 + I_2 \cos 2\theta_l + I_3 \sin^2 \theta_l \cos 2\phi + I_4 \sin 2\theta_l \cos \phi + I_5 \sin \theta_l \cos \phi + I_6 \cos \theta_l \\ & + I_7 \sin \theta_l \sin \phi + I_8 \sin 2\theta_l \sin \phi + I_9 \sin^2 \theta_l \sin 2\phi. \end{aligned} \quad (2.2)$$

The I_i depend on products of the seven complex K^* spin amplitudes, $A_{\perp L/R}$, $A_{\parallel L/R}$, $A_{0L/R}$, A_t (see next section) with each of these a function of q^2 . A_t is related to the time-like component of the virtual K^* , which does not contribute in the case of massless leptons and can be neglected if the lepton mass is small in comparison to the mass of the lepton

pair. We will consider this case in our present analysis. For $m_l = 0$, one finds [20–23]:

$$\begin{aligned} I_1 &= \frac{3}{4} (|A_{\perp L}|^2 + |A_{\parallel L}|^2 + (L \rightarrow R)) \sin^2 \theta_K + (|A_{0L}|^2 + |A_{0R}|^2) \cos^2 \theta_K \\ &\equiv a \sin^2 \theta_K + b \cos^2 \theta_K, \end{aligned} \quad (2.3a)$$

$$\begin{aligned} I_2 &= \frac{1}{4} (|A_{\perp L}|^2 + |A_{\parallel L}|^2) \sin^2 \theta_K - |A_{0L}|^2 \cos^2 \theta_K + (L \rightarrow R) \\ &\equiv c \sin^2 \theta_K + d \cos^2 \theta_K, \end{aligned} \quad (2.3b)$$

$$I_3 = \frac{1}{2} \left[(|A_{\perp L}|^2 - |A_{\parallel L}|^2) \sin^2 \theta_K + (L \rightarrow R) \right] \equiv e \sin^2 \theta_K, \quad (2.3c)$$

$$I_4 = \frac{1}{\sqrt{2}} \left[\text{Re}(A_{0L} A_{\parallel L}^*) \sin 2\theta_K + (L \rightarrow R) \right] \equiv f \sin 2\theta_K, \quad (2.3d)$$

$$I_5 = \sqrt{2} \left[\text{Re}(A_{0L} A_{\perp L}^*) \sin 2\theta_K - (L \rightarrow R) \right] \equiv g \sin 2\theta_K, \quad (2.3e)$$

$$I_6 = 2 \left[\text{Re}(A_{\parallel L} A_{\perp L}^*) \sin^2 \theta_K - (L \rightarrow R) \right] \equiv h \sin^2 \theta_K, \quad (2.3f)$$

$$I_7 = \sqrt{2} \left[\text{Im}(A_{0L} A_{\parallel L}^*) \sin 2\theta_K - (L \rightarrow R) \right] \equiv j \sin 2\theta_K, \quad (2.3g)$$

$$I_8 = \frac{1}{\sqrt{2}} \left[\text{Im}(A_{0L} A_{\perp L}^*) \sin 2\theta_K + (L \rightarrow R) \right] \equiv k \sin 2\theta_K, \quad (2.3h)$$

$$I_9 = \left[\text{Im}(A_{\parallel L}^* A_{\perp L}) \sin^2 \theta_K + (L \rightarrow R) \right] \equiv m \sin^2 \theta_K. \quad (2.3i)$$

The exact equations presented here depend on the definition of the angles which we for this reason have made explicit in Appendix A.

From comparing the amplitude terms in Eq. (2.3), we see that $a = 3c$ and $b = -d$ thus leaving nine independent parameters which can be fixed experimentally in a full angular fit. The 9 independent parameters do not seem to correspond to the 12 parameters from the six complex \bar{K}^{*0} spin amplitudes, $A_{\perp L/R}$, $A_{\parallel L/R}$, $A_{0L/R}$, in the massless case on the theory side. However, we will in Sec. 4 see that this comparison is too naive.

3 K^* spin amplitudes

The six complex K^* spin amplitudes of the massless case are related to the well-known helicity amplitudes (used for example in [21, 22, 24]) through

$$A_{\perp, \parallel} = (H_{+1} \mp H_{-1})/\sqrt{2}, \quad A_0 = H_0. \quad (3.4)$$

The amplitudes describe the $B \rightarrow K\pi$ transition and can be parameterised in terms of the seven $B \rightarrow K^*$ form factors by means of a narrow-width approximation. They also depend on the short-distance Wilson coefficients C_i corresponding to the various operators

of the effective electroweak Hamiltonian. The precise definitions of the form factors and of the effective operators are given in Appendix B. One obtains [17]

$$A_{\perp L,R} = N\sqrt{2}\lambda^{1/2} \left[(\mathcal{C}_9^{(\text{eff})} \mp \mathcal{C}_{10}) \frac{V(s)}{m_B + m_{K^*}} + \frac{2m_b}{q^2} (\mathcal{C}_7^{(\text{eff})} + \mathcal{C}'_7^{(\text{eff})}) T_1(q^2) \right], \quad (3.5)$$

$$A_{\parallel L,R} = -N\sqrt{2}(m_B^2 - m_{K^*}^2) \left[(\mathcal{C}_9^{(\text{eff})} \mp \mathcal{C}_{10}) \frac{A_1(q^2)}{m_B - m_{K^*}} + \frac{2m_b}{q^2} (\mathcal{C}_7^{(\text{eff})} - \mathcal{C}'_7^{(\text{eff})}) T_2(q^2) \right], \quad (3.6)$$

$$A_{0L,R} = -\frac{N}{2m_{K^*}\sqrt{q^2}} \left[(\mathcal{C}_9^{(\text{eff})} \mp \mathcal{C}_{10}) \left\{ (m_B^2 - m_{K^*}^2 - q^2)(m_B + m_{K^*})A_1(q^2) - \lambda \frac{A_2(q^2)}{m_B + m_{K^*}} \right\} + 2m_b(\mathcal{C}_7^{(\text{eff})} - \mathcal{C}'_7^{(\text{eff})}) \left\{ (m_B^2 + 3m_{K^*}^2 - q^2)T_2(q^2) - \frac{\lambda}{m_B^2 - m_{K^*}^2} T_3(q^2) \right\} \right] \quad (3.7)$$

where $\lambda = m_B^4 + m_{K^*}^4 + q^4 - 2(m_B^2 m_{K^*}^2 + m_{K^*}^2 q^2 + m_B^2 q^2)$ and

$$N = \left[\frac{G_F^2 \alpha^2}{3 \cdot 2^{10} \pi^5 m_B^3} |V_{tb} V_{ts}^*|^2 q^2 \lambda^{1/2} \left(1 - \frac{4m_t^2}{q^2} \right)^{1/2} \right]^{1/2}. \quad (3.8)$$

The crucial theoretical input we use in our analysis is the observation that in the limit where the initial hadron is heavy and the final meson has a large energy [25] the hadronic form factors can be expanded in the small ratios Λ_{QCD}/m_b and Λ_{QCD}/E , where E is the energy of the light meson. Neglecting corrections of order $1/m_b$ and α_s , the seven a priori independent $B \rightarrow K^*$ form factors reduce to two universal form factors ξ_{\perp} and ξ_{\parallel} [25, 26]. These relations can be strictly derived within the QCDf and SCET approach and are given in the appendix. Using those simplifications the spin amplitudes at leading order in $1/m_b$ and α_s have a very simple form:

$$A_{\perp L,R} = \sqrt{2} N m_B (1 - \hat{s}) \left[(\mathcal{C}_9^{(\text{eff})} \mp \mathcal{C}_{10}) + \frac{2\hat{m}_b}{\hat{s}} (\mathcal{C}_7^{(\text{eff})} + \mathcal{C}'_7^{(\text{eff})}) \right] \xi_{\perp}(E_{K^*}), \quad (3.9)$$

$$A_{\parallel L,R} = -\sqrt{2} N m_B (1 - \hat{s}) \left[(\mathcal{C}_9^{(\text{eff})} \mp \mathcal{C}_{10}) + \frac{2\hat{m}_b}{\hat{s}} (\mathcal{C}_7^{(\text{eff})} - \mathcal{C}'_7^{(\text{eff})}) \right] \xi_{\perp}(E_{K^*}), \quad (3.10)$$

$$A_{0L,R} = -\frac{N m_B}{2\hat{m}_{K^*}\sqrt{\hat{s}}} (1 - \hat{s})^2 \left[(\mathcal{C}_9^{(\text{eff})} \mp \mathcal{C}_{10}) + 2\hat{m}_b (\mathcal{C}_7^{(\text{eff})} - \mathcal{C}'_7^{(\text{eff})}) \right] \xi_{\parallel}(E_{K^*}), \quad (3.11)$$

with $\hat{s} = q^2/m_B^2$, $\hat{m}_i = m_i/m_B$. Here we neglected terms of $O(\hat{m}_{K^*}^2)$.

Some remarks are in order:

- The theoretical simplifications are restricted to the kinematic region in which the energy of the K^* is of the order of the heavy quark mass, i.e. $q^2 \ll m_B^2$. Moreover, the influences of very light resonances below 1 GeV GeV question the QCD factorization results in that region. Thus, we will confine our analysis of all observables to the dilepton mass in the range, $1 \text{ GeV}^2 \leq q^2 \leq 6 \text{ GeV}^2$.
- Within the SM, we recover the naive quark-model prediction of $A_\perp = -A_\parallel$ [28, 29] in the $m_B \rightarrow \infty$ and $E_{K^*} \rightarrow \infty$ limit (equivalently $\hat{m}_{K^*}^2 \rightarrow 0$). In this case, the s quark is produced in helicity $-1/2$ by weak interactions in the limit $m_s \rightarrow 0$, which is not affected by strong interactions in the massless case [27]. Thus, the strange quark combines with a light quark to form a K^* with helicity either -1 or 0 but not $+1$. Consequently, the SM predicts at quark level $H_{+1} = 0$, and hence $A_\perp = -A_\parallel$ [cf. Eq. (3.4)], which is revealed as $|H_{-1}| \gg |H_{+1}|$ (or $A_\perp \approx -A_\parallel$) at the hadron level.
- As noted in Ref. [17], the contributions of the chirality-flipped operators $\mathcal{O}'_{9,10} = \mathcal{O}_{9,10}(P_L \rightarrow P_R)$ can be included in the above amplitudes by the replacements $\mathcal{C}_{9,10}^{(\text{eff})} \rightarrow \mathcal{C}_{9,10}^{(\text{eff})} + \mathcal{C}'_{9,10}{}^{(\text{eff})}$ in Eq. (3.9), $\mathcal{C}_{9,10}^{(\text{eff})} \rightarrow \mathcal{C}_{9,10}^{(\text{eff})} - \mathcal{C}'_{9,10}{}^{(\text{eff})}$ in Eqs. (3.10) and (3.11). However, they play a sub-dominant role in our NP analysis presented here.
- The symmetry breaking corrections of order α_s can be calculated in the QCDf/SCET approach. Those NLO corrections are included in our numerical analysis following Ref. [30]. The corresponding formulae for the case $\mathcal{C}'_7{}^{(\text{eff})} \neq 0$ are given in Appendix C.
- In general we have no means to calculate Λ/m_b corrections to the QCDf amplitudes so they are treated as unknown corrections. This leads to a large uncertainty of theoretical predictions based on the QCDf/SCET approach. However, in specific examples one can combine QCDf/SCET results with calculations based on the QCD sum rule approach in order to estimate the leading power corrections.

To take into account the present situation, we introduce a set of extra parameters, one for each spin amplitude, to explore what the effect of a possible Λ/m_b correction could be:

$$A_{\perp,\parallel,0} = A_{\perp,\parallel,0}^0 (1 + c_{\perp,\parallel,0}) \quad (3.12)$$

where the ‘0’ superscript stands for the QCD NLO Factorisation amplitude and $c_{\perp,\parallel,0}$ are taken to vary in a range $\pm 10\%$ which corresponds to a naive dimensional estimate. Furthermore, we also give our final predictions taking into account further

improvements on the power corrections and varying the independent parameters in a less conservative range of $\pm 5\%$.

4 Theoretically clean observables

4.1 General criteria

We recall again that 2 of the 11 measurable distribution functions a, b, \dots, m of the differential decay distribution in the limit $m_\ell^2 \ll q^2$, defined in Eq. 2.3, include redundant information due to the relations $a = 3c$ and $b = -d$. So in principle there are 9 independent observables. However, the dependence of those functions on the six complex theoretical spin amplitudes, $A_{\perp L/R}, A_{\parallel L/R}, A_{0L/R}$, is special. By inspection one finds that the distribution functions are *invariant* under the following three independent symmetry transformations of the spin amplitudes: global phase transformation of the L -amplitudes

$$A'_{\perp L} = e^{i\phi_L} A_{\perp L}, \quad A'_{\parallel L} = e^{i\phi_L} A_{\parallel L}, \quad A'_{0L} = e^{i\phi_L} A_{0L}, \quad (4.13)$$

global phase transformation of the R -amplitudes

$$A'_{\perp R} = e^{i\phi_R} A_{\perp R}, \quad A'_{\parallel R} = e^{i\phi_R} A_{\parallel R}, \quad A'_{0R} = e^{i\phi_R} A_{0R}, \quad (4.14)$$

and a continuous $L \leftrightarrow R$ rotation

$$A'_{\perp L} = +\cos\theta A_{\perp L} - \sin\theta A_{\perp R}^* \quad (4.15a)$$

$$A'_{\perp R} = +\sin\theta A_{\perp L} + \cos\theta A_{\perp R}^* \quad (4.15b)$$

$$A'_{0L} = +\cos\theta A_{0L} - \sin\theta A_{0R}^* \quad (4.15c)$$

$$A'_{0R} = +\sin\theta A_{0L} + \cos\theta A_{0R}^* \quad (4.15d)$$

$$A'_{\parallel L} = +\cos\theta A_{\parallel L} + \sin\theta A_{\parallel R}^* \quad (4.15e)$$

$$A'_{\parallel R} = -\sin\theta A_{\parallel L} + \cos\theta A_{\parallel R}^*. \quad (4.15f)$$

Normally, there is the freedom to pick a single global phase, but as L and R amplitudes do not interfere here, two phases can be chosen arbitrarily as reflected in the first two transformations. The third symmetry reflects that an average is made over the spin amplitudes to obtain the angular distribution. So it is clear that only 9 out of the 12 parameters arising from the 6 complex amplitudes are independent which fits exactly with the 9 independent measurable distribution functions.

A consequence of the three symmetries is that any observable based on the differential decay distribution has also to be invariant under the same symmetry transformations. Or differently stated, the 9 coefficient functions in the differential decay rate form a basis in

the space of invariant strings that can be built out of two spin amplitudes. The invariance under the three symmetries is then necessary and sufficient criterium for any quantity built out these to be an observable.

Besides the mandatory criterium above there are further criteria required for an interesting observable:

Simplicity: A simple functional dependence on the 9 independent measurable distribution functions; at best it should depend only from one or two in the numerator and denominator of an asymmetry.

Cleanliness: At leading order in Λ/m_b and in α_s the observable should be independent of any form factor, at best for all q^2 . Also the influence of symmetry-breaking corrections at order α_s and at order Λ/m_b should be minimal.

Sensitivity: The sensitivity to the $\mathcal{C}_7^{(\text{eff})}$ Wilson coefficient representing NP with another chirality than in the SM should be maximal;

Precision: The experimental precision obtainable should be good enough to distinguish different NP models.

In the limit where the \bar{K}^{*0} meson has a large energy, only two independent form factors occur in $A_{0L/R}$ and in $A_{\perp L/R}$ and $A_{\parallel L/R}$. Clearly, any ratio of two of the nine measurable distribution functions proportional to the same form factor fulfil the criterium of symmetry, simplicity, and theoretical cleanliness up to Λ/m_b corrections. However, the third criterium, a sensitivity to a special kind of NP and the subsequent requirement of experimental precision, singles out particular combinations. In this paper we focus on new right-handed currents. Other NP sensitivities may single out other observables as will be analysed in a forthcoming paper [32].

4.2 Observables

There are some proposals for theoretical clean observables already in the literature which we should briefly discuss in view of the above criteria:

- The forward backward asymmetry is the most popular quantity in the $\bar{B}_d \rightarrow \bar{K}^{*0} \mu^+ \mu^-$ decay [33]. In terms of the \bar{K}^{*0} spin amplitudes it can be written as [34, 35]

$$A_{\text{FB}} = \frac{3}{2} \frac{\text{Re}(A_{\parallel L} A_{\perp L}^*) - \text{Re}(A_{\parallel R} A_{\perp R}^*)}{|A_0|^2 + |A_{\parallel}|^2 + |A_{\perp}|^2} \quad (4.16)$$

where

$$A_i A_j^* \equiv A_{iL}(q^2) A_{jL}^*(q^2) + A_{iR}(q^2) A_{jR}^*(q^2) \quad (i, j = 0, \parallel, \perp). \quad (4.17)$$

While the criteria of symmetry and simplicity are fulfilled, the form factors cancel out only at the specific value of q^2 where $A_{\text{FB}} = 0$. Thus the measurement provide only a single clean number, the zero crossing point, rather than a theoretically clean distribution.

- The fractions of the \bar{K}^{*0} polarisation

$$F_L(q^2) = \frac{|A_0|^2}{|A_0|^2 + |A_{\parallel}|^2 + |A_{\perp}|^2}, \quad (4.18)$$

$$F_T(q^2) = 1 - F_L(q^2) = \frac{|A_{\perp}|^2 + |A_{\parallel}|^2}{|A_0|^2 + |A_{\parallel}|^2 + |A_{\perp}|^2}, \quad (4.19)$$

and the K^* polarisation parameter

$$\alpha_{K^*}(q^2) = \frac{2F_L}{F_T} - 1 = \frac{2|A_0|^2}{|A_{\parallel}|^2 + |A_{\perp}|^2} - 1. \quad (4.20)$$

All fulfil the criteria of symmetry and simplicity, but the form factors do not cancel in the LO approximation; thus, suffering from larger hadronic uncertainties. The fraction of the \bar{K}^{*} polarisation can be measured from the angular projections alone and the first experimental measurements of F_L with limited accuracy are available [6, 8].

- Defining the helicity distributions $\Gamma_{\pm} = |H_{\pm 1}^L|^2 + |H_{\pm 1}^R|^2$ one can construct [21]

$$A_T^{(1)} = \frac{\Gamma_- - \Gamma_+}{\Gamma_- + \Gamma_+} = \frac{-2\text{Re}(A_{\parallel}A_{\perp}^*)}{|A_{\perp}|^2 + |A_{\parallel}|^2}. \quad (4.21)$$

It has been shown [17, 18] that this quantity shows an adequate cleanliness and is very sensitive to right-handed currents, making an ideal observable of it if just these two criteria were sufficient. However, the quantity $A_T^{(1)}$ does not fulfil the most important criterium of symmetry. The important consequences out of this observation are briefly discussed in the next subsection.

- The other transversity amplitude, first proposed in [17], is defined as

$$A_T^{(2)} = \frac{|A_{\perp}|^2 - |A_{\parallel}|^2}{|A_{\perp}|^2 + |A_{\parallel}|^2}. \quad (4.22)$$

It obviously fulfils all three criteria of symmetry, simplicity and theoretical cleanliness. It is also rather sensitivity to $\mathcal{C}'_7^{(\text{eff})}$ as one can see by inspection of the LO formulae of the \bar{K}^{*0} amplitudes in Eqs. (3.9-3.11); in this approximation it is directly proportional to $\mathcal{C}'_7^{(\text{eff})}$, thus vanishes in the SM.

By inspection of the formulae of the K^* spin amplitudes in terms of the Wilson coefficients and the SCET form factors at the LO approximation, Eqs. (3.9-3.11), one is led to some new observables which fulfil the first three criteria *and* have an enhanced sensitivity to $\mathcal{C}'_7^{(\text{eff})}$. They are defined as

$$A_T^{(3)} = \frac{|A_{0L}A_{\parallel L}^* - A_{0R}^*A_{\parallel R}|}{\sqrt{|A_0|^2|A_\perp|^2}}, \quad (4.23)$$

and

$$A_T^{(4)} = \frac{|A_{0L}A_{\perp L}^* - A_{0R}^*A_{\perp R}|}{|A_{0L}^*A_{\parallel L} + A_{0R}A_{\parallel R}^*|}, \quad (4.24)$$

One could also consider the real and imaginary parts of $A_T^{(3)}$.

There are no further independent quantities which fulfil the criteria we have set out. However, when we will consider NP sensitivities beyond $\mathcal{C}'_7^{(\text{eff})}$ further observables may be singled out [32].

4.3 The problem with $A_T^{(1)}$

Contrary to the case of $A_T^{(i)}$ with $i = 2, 3, 4$, it is not possible to extract $A_T^{(1)}$ from the full angular distribution. This is a direct consequence of the fact that the quantity $A_T^{(1)}$ is not invariant under the symmetry (4.15) of the distribution function (2.1) which represent the complete set of observables in the case spins of the final states are summed up. Let us elaborate further on this surprising observation; it seems practically not possible to measure the helicity of the final states on a *event-by-event* basis. At the forthcoming LHCb experiment for example one only measures the charge, the three-momentum of the final state particles and its nature through different types of particle identification. So one has the four-momentum for each particle and its charge. The situation does not look different for the present B factories and their future upgrades. While the e^+e^- environment is much simpler there is still no practical way to measure the spin of the muons on an *event-by-event* basis. We should emphasise that this is a practical and not a principle problem; in a *gedanken* experiment where the helicity of the individual final state leptons are measured, it would indeed be possible to measure $A_T^{(1)}$. So while $A_T^{(1)}$ is in principle a good observable, we cannot see any way it can be measured at either LHCb or at a Super- B factory with electrons or muons in the final state.

5 Method to calculate experimental sensitivity

In this section we explain how to investigate the sensitivity to the angular observables presented in Sec. 4 using a toy Monte Carlo model. We estimate the statistical uncertainty

on all observables with statistics corresponding to 5 years of nominal running at LHC***b*** (10 fb^{-1}) and comment on the experimental prospects for a measurement at the end of an upgrade to LHC***b*** (100 fb^{-1}). For the estimates here we are only considering the final state with muons.

5.1 $\bar{B}_d \rightarrow \bar{K}^{*0} \ell^+ \ell^-$ decay model

The angles θ_l , θ_K and ϕ , as well as the q^2 of the lepton pair can be measured with small uncertainty and no experimental resolution effects needs to be considered. A toy Monte Carlo model of the decay was created using Eq. (2.1) as a probability density function (PDF) normalised to the width,

$$\int_{q_{\text{min}}^2}^{q_{\text{max}}^2} \frac{d\Gamma}{dq^2} dq^2. \quad (5.25)$$

It is parameterised in terms of the real and imaginary parts of the spin amplitudes where each of these amplitudes is q^2 dependent. A simple approach, where the data is divided into regions of q^2 and the spin amplitudes determined within these, will not work; the coefficients in front of the different angular components as seen in Eq. (2.1) depend in a non-linear way on the spin amplitudes meaning that the angular distribution after integration over a bin in q^2 cannot be expressed in terms of Eq. (2.1) with some q^2 -averaged spin amplitudes. Instead an approach is used where the q^2 dependence of each of the spin amplitudes is parameterised as a function of q^2 .

A special choice of the symmetry transformations described in Sec. 4 can be used to reduce the number of parameters. Here we use the first two symmetry transformations Eqs. (4.13) and (4.14) to get rid of the two phases in A_{0R} and A_{0L} . Then the third transformation Eq. (4.15) is used with $\theta = \arctan(-A_{0R}/A_{0L})$ leading to A_{0L} being real and $A_{0R} = 0$ thus disappearing completely from the parametrisation. At a given value of q^2 we are thus left with 9 parameters corresponding to the real and imaginary components of $A_{\parallel L,R}$ and $A_{\perp L,R}$ and the real component of A_{0L} . We now parameterise each of these spin amplitudes as a 2nd order polynomial. Through the polynomial ansatz we are introducing a weak model dependence; we checked that the error introduced by this was significantly smaller than the corresponding experimental errors across the squared dimuon mass range $1 \text{ GeV}^2 < q^2 < 6 \text{ GeV}^2$. To describe the full q^2 and angular dependence of the decay we thus need 27 parameters. As a final step we recognise that an absolute measurement of the total width is difficult to obtain in a hadronic environment such as LHC***b*** and fix the value of A_{0L} to 1 at a reference value of q^2 thus reducing the number of free parameters to 26. This last step has no influence on the experimental determination of any of the

observables discussed in this paper as they are all formed as ratios where the total width cancels out. While no longer sensitive to the absolute width we are still sensitive to the shape of the differential width as a function of q^2 .

We follow the resolution, yield and background numbers in [9] to construct a model that includes a realistic level of background. The signal is assumed to have a Gaussian distribution in m_B with a width of 14 MeV in a window of $m_B \pm 50$ MeV and a Breit-Wigner in $m_{K\pi}$ with width 48 MeV in a window of $m_{K^*0} \pm 100$ MeV. A simplified background model is included; it is flat in all angles, effectively treating all background as combinatorial, but follows the q^2 distribution of the signal. Acceptance and CP violation effects are neglected allowing us to treat $\bar{B}_d \rightarrow \bar{K}^{*0} \mu^+ \mu^-$ and its charge conjugate simultaneously. We do not include any contributions from non-resonant $\bar{B}_d \rightarrow K^- \pi^+ \mu^+ \mu^-$.

Using the toy Monte Carlo model, a dataset for the observables θ_l , θ_K , ϕ and q^2 can be generated with the calculated values of the spin amplitudes as input without making use of the polynomial ansatz. Physics beyond the SM can be included in a straightforward way by providing the relevant spin amplitudes. Using the yield and background estimates from [9] and assuming a flat efficiency for the signal as a function of q^2 we use on average 4032 signal events and 1168 background events in the q^2 interval from $4m_\mu^2$ to 9 GeV^2 in a dataset of 2 fb^{-1} . These are scaled lineally in order to obtain 10 fb^{-1} and 100 fb^{-1} yield estimates. For each dataset we generate, the signal and background numbers are varied according to Poisson statistics.

5.2 Full angular fit

With the model above we can generate an ensemble of experiments corresponding to a given integrated luminosity. In each of these experiments we can use a general minimiser to find the spin value parametrisation that best corresponds to the data. Each fit has in total 27 parameters; 26 from the signal described above and a single parameter to describe the level of the simplified background model. From the ensemble of experiments, estimates of the experimental uncertainties can be made and any biases introduced can be studied. For each dataset, the extracted spin amplitude components were used to calculate the value of each angular observable as a function of q^2 . In total we created an ensemble of 1000 experiments and will thus at a given value of q^2 get 1000 different determinations of a given observable. By looking at the point where 33% and 47.5% of results lie within either side of the median of the results we can form asymmetric 1σ and 2σ errors. Connecting these at different q^2 values gives us 1σ and 2σ bands for the experimental errors on the observable. An illustration of the method in Fig. 1 shows the experimental sensitivity to the width distribution relative to the normalisation point which was arbitrarily chosen

as 3.5 GeV^2 . The experimental sensitivity to the observables will be presented in Sec. 6 within the phenomenological analysis to allow for an easy comparison of experimental and theoretical errors.

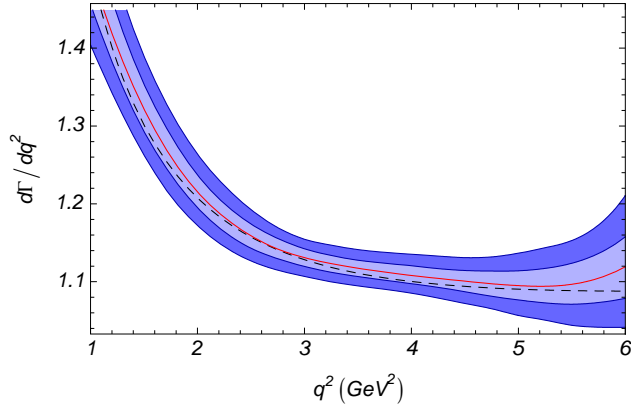


Figure 1: The experimental sensitivity to $\frac{d\Gamma}{dq^2}$ with the SM as input. The inner and outer bands correspond to 1σ and 2σ experimental errors with statistics corresponding to a 10 fb^{-1} dataset from LHC**b**.

5.3 Comparisons with fits to projections

The full angular fit gives access to angular observables not accessible in other ways. However, A_{FB} , $A_T^{(2)}$, F_L and A_{im}^1 can be extracted from distributions in just a single angle after integration over the other 2 in Eq. (2.1):

$$\frac{d\Gamma'}{d\phi} = \frac{\Gamma'}{2\pi} \left(1 + \frac{1}{2}(1 - F_L)A_T^{(2)} \cos 2\phi + A_{\text{im}} \sin 2\phi \right), \quad (5.26a)$$

$$\frac{d\Gamma'}{d\theta_l} = \Gamma' \left(\frac{3}{4}F_L \sin^2 \theta_l + \frac{3}{8}(1 - F_L)(1 + \cos^2 \theta_l) + A_{\text{FB}} \cos \theta_l \right) \sin \theta_l, \quad (5.26b)$$

$$\frac{d\Gamma'}{d\theta_K} = \frac{3\Gamma'}{4} \sin \theta_K (2F_L \cos^2 \theta_K + (1 - F_L) \sin^2 \theta_K), \quad (5.26c)$$

where $\Gamma' = b + 4c$. This method was investigated for LHC**b** in [11]. The observables appear linearly in the expressions so the fits can be performed on data binned in q^2 . The value extracted from these fits is then a $\frac{d\Gamma}{dq^2}$ weighted average of each parameter.

The full angular model described in Sec. 5.2 was used to generate data sets which were then fit simultaneously using the distributions in Eq. (5.26). The treatment of background and the $m_{B,K\pi}$ distributions were the same as in the full angular model. For a direct

¹ A_{im} is defined as $A_{\text{im}} = \frac{\text{Im}(A_{\perp L} A_{\parallel L}^*) + \text{Im}(A_{\perp R} A_{\parallel R}^*)}{|A_0|^2 + |A_{\perp}|^2 + |A_{\parallel}|^2}$ and is included for completeness here. It is not of importance for the measurement of right handed currents.

comparison between this method and the full angular fit, the q^2 dependent values of the observables were averaged using a weighted mean,

$$A_T^{(i)} = \frac{\int_{q_{\min}^2}^{q_{\max}^2} \frac{d\Gamma}{dq^2} A_T^{(i)}(q^2)}{\int_{q_{\min}^2}^{q_{\max}^2} \frac{d\Gamma}{dq^2}}. \quad (5.27)$$

The central values produced for the full angular approach in this case show some small biases due to the breakdown of the polynomial ansatz at the edges of the q^2 distribution, however this is still well below the statistical error expected with 10 fb^{-1} of data from *LHCb*. The power of the full angular fit is striking for $A_T^{(2)}$ where the resolution is above a factor 2 better compared to fitting the projections. This can easily be understood in terms of the $(1 - F_L)$ factor in Eq. (5.26a), where F_L is large in the SM.

For all the observables where a comparison can be made, we see that the full angular fit provides improvements in the resolution of between 15% and 60%.

In the full angular fit we can calculate the position of the zero crossing for the forward-backward asymmetry, q_0^2 . We illustrate the distribution of results obtained from the ensemble of datasets in Fig. 2 where a resolution, assuming the SM as input, of 0.17 GeV^2 is obtained. Alternatively we can perform the simpler task of binning the data in 1 GeV^2 bins and then in each bin perform simultaneous fits to the three angular projections. The value of A_{FB} is extracted by performing a straight line fit in the range $2 - 6 \text{ GeV}^2$ to the A_{FB} values found in each q^2 bin. This gives us, with exactly the same assumptions for how background and acceptance are treated, a resolution of 0.24 GeV^2 . So also in this case we see an improvement of 30% in the statistical power by performing a full angular fit.

The comparisons made here demonstrate that there is significant advantage in performing the full angular fit once the data sets are large enough. Using the simplified model described here it is possible to use this approach even with a smaller 2 fb^{-1} data set. In reality, detector effects not accounted for such as angular acceptance will complicate the process and a proper full angular analysis may not be possible with data sets this small. However, we have shown that with the signal and background statistics at *LHCb* a full angular analysis is possible once the detector effects have been properly understood.

6 Phenomenological analysis

In this section we present our phenomenological analysis of the old and new observables in the SM and in extensions of the SM with new right-handed currents. The latter can be done in a model-independent way by introducing the chiral partners of the SM Wilson

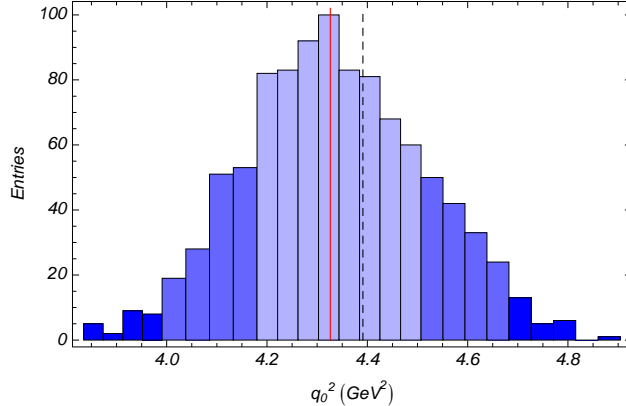


Figure 2: The distribution in the determination of the zero crossing of A_{FB} from an ensemble of datasets created from the toy Monte Carlo model with statistics corresponding to 10 fb^{-1} at LHC**b**. The edge of the inner (light blue) and middle (medium blue) regions correspond to 1σ and 2σ experimental errors. The solid (red) line is the median of the fitted values and the dashed (black) line is the input value from the SM theory predictions. From the figure we see a resolution of 0.17 GeV^2 .

coefficients $\mathcal{C}_7^{(\text{eff})}$, $\mathcal{C}_9^{(\text{eff})}$, and \mathcal{C}_{10}^2 . This general new-physics scenario can be realized for example via gluino-mediated FCNC in the general R-parity conserving MSSM.

6.1 Preliminaries

Our analysis is based on the numerical input as summarized in Table 1. Moreover, we introduce four representative benchmark points of supersymmetry with non-minimal flavour violation in the down squark sector which were already used in Ref. [18]. The most important flavour diagonal parameters are fixed as follows: $\tan\beta = 5$, $\mu = M_1 = M_2 = M_{H^\pm} = m_{\tilde{u}_R} = 1 \text{ TeV}$. Note that we choose a low value for $\tan\beta$; this shows that we do not need to rely on a large- $\tan\beta$ to see an effect, and ensures automatic fulfilment of the constraint coming from $B_s \rightarrow \mu^+\mu^-$. Furthermore, we make the assumption that all the entries in $m_{u,LR}^2$ and $m_{d,LR}^2$ vanish, with the exception of the one that corresponds to $(\delta_{LR}^d)_{32}$. The remaining parameters of the four benchmark points correspond to two different scenarios and are fixed as follows:

- Scenario A: $m_{\tilde{g}} = 1 \text{ TeV}$ and $m_{\tilde{d}} \in [200, 1000] \text{ GeV}$. The only non-zero mass insertion is varied between $-0.1 \leq (\delta_{LR}^d)_{32} \leq 0.1$. For all parameter sets the compatibility

²We note here that the impact of $\mathcal{C}_9^{(\text{eff})}$ and \mathcal{C}_{10} and their chiral partners is rather small compared with $\mathcal{C}'_7^{(\text{eff})}$ in the low- q^2 region, due to the $2 \hat{m}_b/\hat{s}$ factor in the matrix element and the experimental constraints from the inclusive decay $B \rightarrow X_s \ell^+ \ell^-$.

Table 1: Summary of input parameters and estimated uncertainties.

m_B	$5.27950 \pm 0.00033 \text{ GeV}$	λ	0.2262 ± 0.0014
m_K	$0.896 \pm 0.040 \text{ GeV}$	A	0.815 ± 0.013
M_W	$80.403 \pm 0.029 \text{ GeV}$	$\bar{\rho}$	0.235 ± 0.031
M_Z	$91.1876 \pm 0.0021 \text{ GeV}$	$\bar{\eta}$	0.349 ± 0.020
$\hat{m}_t(\hat{m}_t)$	$167 \pm 5 \text{ GeV}$	$\Lambda_{\text{QCD}}^{(n_f=5)}$	$220 \pm 40 \text{ MeV}$
$m_{b,\text{PS}}(2 \text{ GeV})$	$4.6 \pm 0.1 \text{ GeV}$	$\alpha_s(M_Z)$	0.1176 ± 0.0002
m_c	$1.5 \pm 0.2 \text{ GeV}$	α_{em}	$1/137$
f_B	$200 \pm 30 \text{ MeV}$	$a_1(K^*)_{\perp, \parallel}$	0.10 ± 0.07
$f_{K^*,\perp}$	$175 \pm 25 \text{ MeV}$	$a_2(K^*)_{\perp}$	0.13 ± 0.08
$f_{K^*,\parallel}$	$217 \pm 5 \text{ MeV}$	$a_2(K^*)_{\parallel}$	0.09 ± 0.05
$m_B \xi_{K^*,\parallel}(0)/(2m_{K^*})$	0.47 ± 0.09	$\lambda_{B,+}(1.5\text{GeV})$	$0.485 \pm 0.115 \text{ GeV}$
$\xi_{K^*,\perp}(0)$	0.26 ± 0.02		

with other B physics constraints, the electroweak constraints, constraints from particle searches, and also with the vacuum stability bounds is verified [18]. The curves denoted by “a” and “b” correspond respectively to $m_{\tilde{g}}/m_{\tilde{d}} = 2.5$, $(\delta_{LR}^d)_{32} = 0.016$ and $m_{\tilde{g}}/m_{\tilde{d}} = 4$, $(\delta_{LR}^d)_{32} = 0.036$. We will refer to this case as the large-gluino and positive mass insertion scenario.

- Scenario B: $m_{\tilde{d}} = 1 \text{ TeV}$ and $m_{\tilde{g}} \in [200, 800] \text{ GeV}$. The mass insertion is varied in the same range as Scenario A. The curves denoted by “c” and “d”, correspond, respectively to $m_{\tilde{g}}/m_{\tilde{d}} = 0.7$, $(\delta_{LR}^d)_{32} = -0.004$ and $m_{\tilde{g}}/m_{\tilde{d}} = 0.6$, $(\delta_{LR}^d)_{32} = -0.006$. We will refer to this case as the low-gluino mass (although large squark mass would be more appropriate) and negative mass insertion scenario.

Notice that we have changed curve “c” with respect to Ref. [18] reducing its corresponding mass insertion to avoid any conflict with vacuum stability or colour breaking constraints [31].

Finally, we emphasize again that the validity of our theoretical predictions is restricted to the kinematic region in which the energy of the K^* is of the order of the heavy quark mass. So we restrict our analysis to the low- q^2 region from 1 GeV^2 to 6 GeV^2 . In the region below 1 GeV^2 the QCDf/SCET results are questioned by the presence of very light resonances.

6.2 Results

We present our results on the observables, F_L , A_{FB} , $A_T^{(2)}$, $A_T^{(3)}$, and $A_T^{(4)}$ (for definitions see Sec. 4) in the following form:

- For all the observables we plot the theoretical sensitivity on the left hand side of each Figure.

The thin dark line is the central NLO result for the SM and the narrow inner dark (orange) band that surrounds it corresponds to the NLO SM uncertainties due to both input parameters and perturbative scale dependence. Light grey (green) bands are the estimated $\Lambda/m_b \pm 5\%$ corrections for each spin amplitude (as given in Eq. 3.12) while darker grey (green) ones are the more conservative $\Lambda/m_b \pm 10\%$ corrections. The curves labelled (a)–(d) correspond to the four different benchmark points in the MSSM introduced above.

- The experimental sensitivity for a dataset corresponding to 10 fb^{-1} of LHC***b*** data is given in each figure on the right hand side. Here the solid (red) line shows the median extracted from the fit to the ensemble of data and the dashed (black) line shows the theoretical input distribution. The inner and outer bands correspond to 1σ and 2σ experimental errors.

Let us start with some concrete observations on the new observables $A_T^{(3)}$ and $A_T^{(4)}$. They offer sensitivity to the longitudinal spin amplitude $A_{0L,R}$ in a controlled way compared to the old observables F_L and α_K^* : the dependence on both the parallel and perpendicular soft form factors $\xi_{\parallel}(0)$ and $\xi_{\perp}(0)$ cancels at LO. A residual of this dependence may appear at NLO, but as shown in Figs. 4 and 5, it is basically negligible. It is also remarkable that for $A_T^{(3)}$ and $A_T^{(4)}$ at low q^2 the impact of this uncertainty is less important than the uncertainties due to input parameters and scale dependence.

The new observables $A_T^{(3)}$ and $A_T^{(4)}$ also present a different sensitivity to \mathcal{C}'_7 via their dependence on $A_{0L,R}$ compared with $A_T^{(2)}$. This may allow for a particularly interesting cross check of the sensitivity to this chirality flipped operator \mathcal{O}'_7 ; for instance, new contributions coming from tensor scalars and pseudo-scalars will behave differently among the set of observables.

Another remarkable point that comes clear when comparing the set of clean observables $A_T^{(2)}$, $A_T^{(3)}$ and $A_T^{(4)}$ versus the old observables like F_L concerns the potential discovery of NP, in particular of new right-handed currents. The new observables share the nice feature of $A_T^{(2)}$ that there are large deviations from the SM curve from the ones of the four supersymmetric benchmark points. In case of $A_T^{(2)}$ this is caused by the balance between

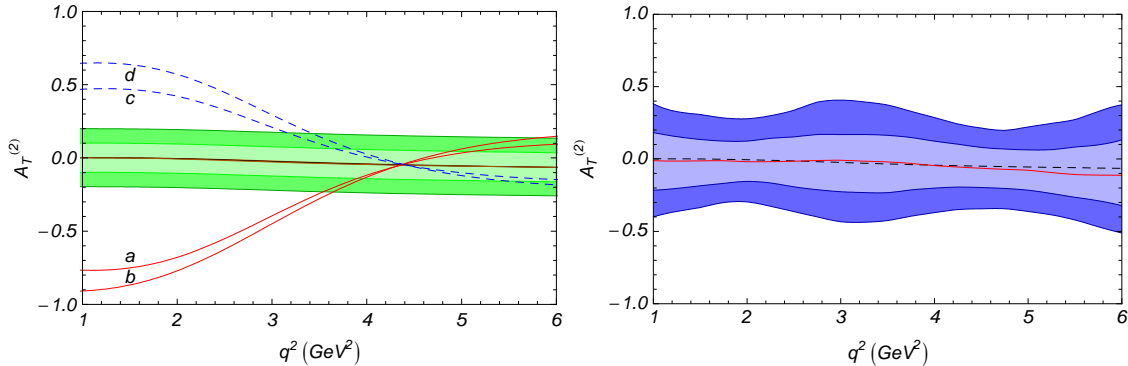


Figure 3: For $A_T^{(2)}$ we compare the theoretical errors (left) with the experimental errors (right) as a function of the squared dimuon mass. For the theory, the narrow inner dark (orange) bands correspond to the NLO result for the SM including all uncertainties (except for Λ/m_b) as explained in the text. Light grey (green) bands include the estimated Λ/m_b uncertainty at a $\pm 5\%$ level and the external dark grey (green) bands correspond to a $\pm 10\%$ correction for each spin amplitude. The curves labelled (a)–(d) correspond to different SUSY scenarios as explained in the text. For the experimental aspects the inner and outer bands correspond to 1σ and 2σ statistical errors with a yield corresponding to a 10 fb^{-1} dataset from LHC**b**.

the competing contributions of order $1/q^2$ and $1/q^4$ originating from the photon pole in the numerator and denominator of $A_T^{(2)}$, providing a strong sensitivity to $\mathcal{C}_7^{(\text{eff})}$. This sensitivity is near maximal around the 1 GeV^2 region precisely inside the theoretically well controlled area. A large deviation from the SM for $A_T^{(2)}$, $A_T^{(3)}$ or $A_T^{(4)}$ can thus show the presence of right-handed currents in a way that is not possible with F_L or A_{FB} . In the latter cases the deviations from the SM prediction of the same four representative curves are marginal.

In the experimental plots we find a good agreement between the central values extracted from the fits and the theoretical input. Any deviations seen are small compared to the statistical uncertainties, however the weakness of the polynomial parametrisation, particularly at the extremes of the q^2 range, can be seen. For much larger data sets this could be addressed by increasing the order of the polynomials used. The experimental resolution for F_L is very good but with the small deviations from the SM expected this is not helpful in the discovery of new right-handed currents. Comparing the theoretical and experimental figures for the other observables it can be seen that in particular $A_T^{(3)}$ show great promise to distinguish between NP models.

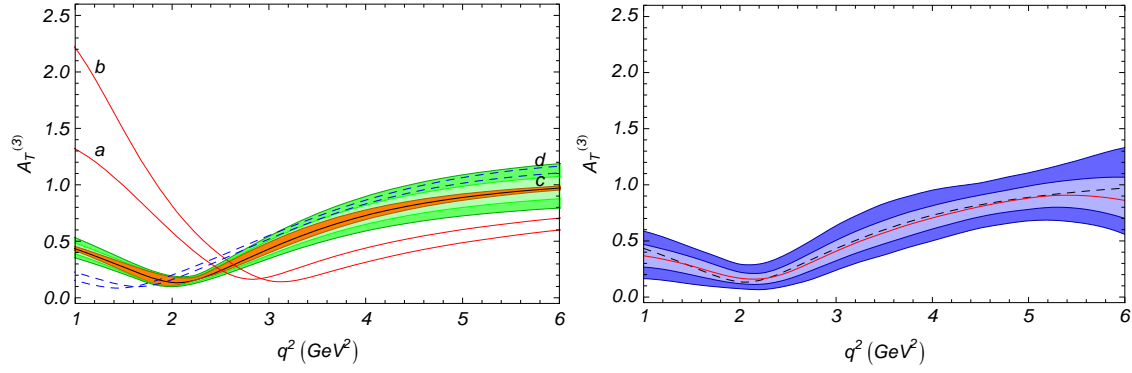


Figure 4: For the new observable $A_T^{(3)}$ we compare the theoretical errors (left) with the experimental errors (right). See the caption of Fig. 3 for details.

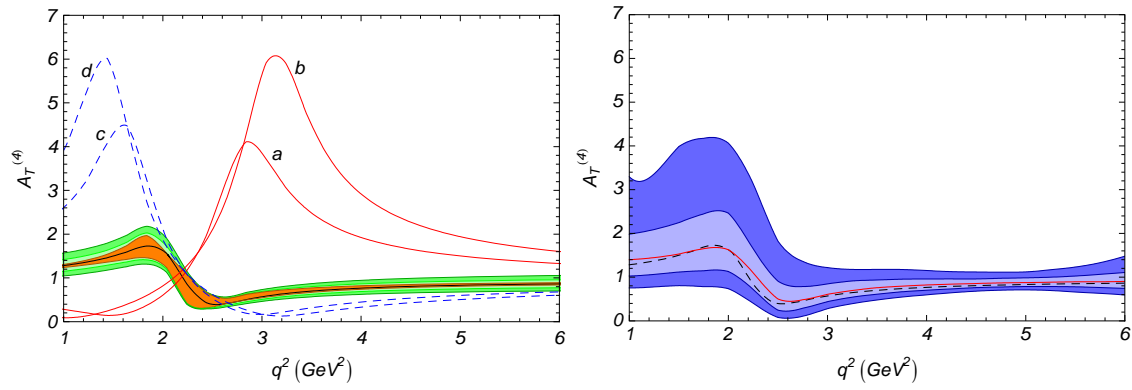


Figure 5: For the new observable $A_T^{(4)}$ we compare the theoretical errors (left) with the experimental errors (right). See the caption of Fig. 3 for details.

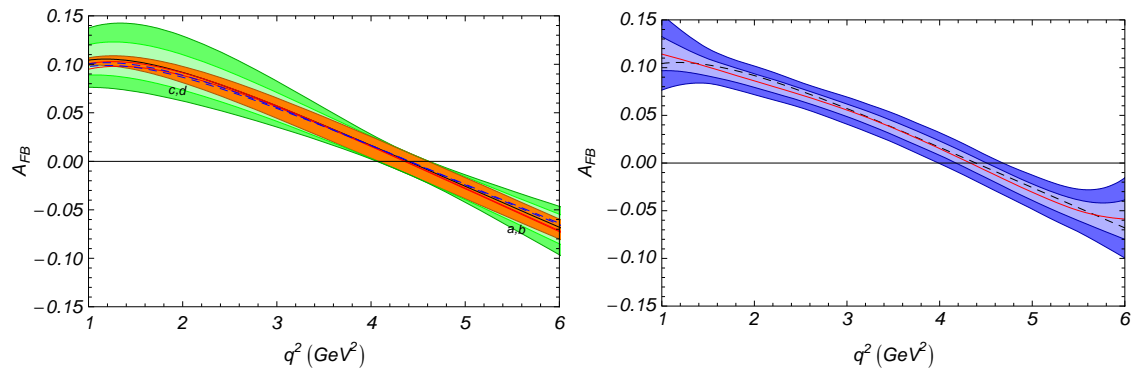


Figure 6: For A_{FB} we compare the theoretical errors (left) with the experimental errors (right). See the caption of Fig. 3 for details.

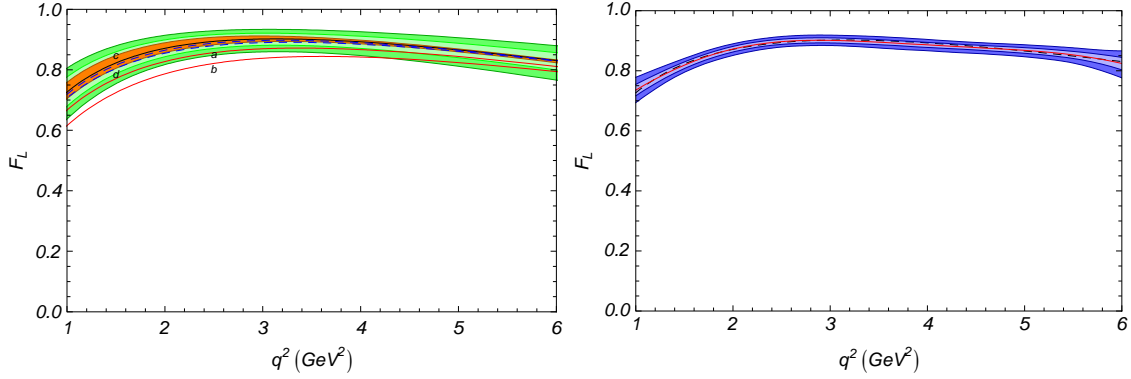


Figure 7: For F_L we compare the theoretical errors (left) with the experimental errors (right). See the caption of Fig. 3 for details.

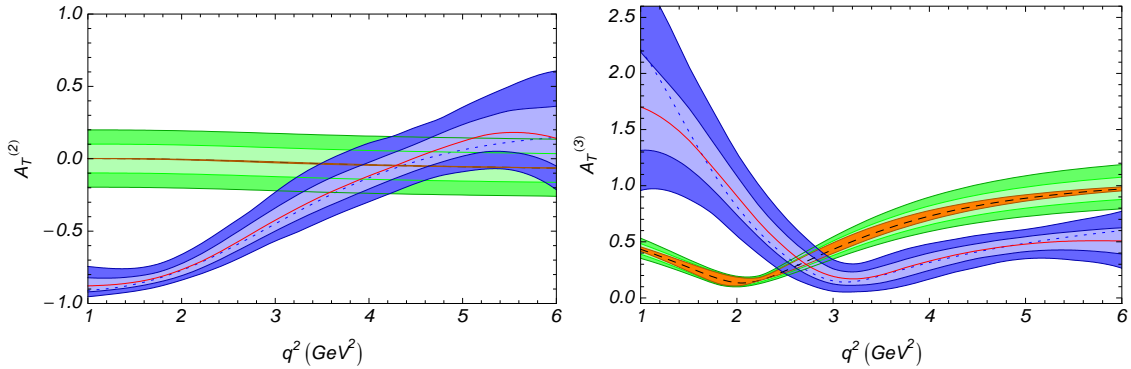


Figure 8: The experimental errors (blue, on top) assuming SUSY scenario (b) with large-gluino mass and positive mass insertion, is compared to the theoretical errors (green, below) assuming the SM. To the left for $A_T^{(2)}$ and the right for $A_T^{(3)}$.

To further explore the power of the observables we can imagine that nature corresponds to SUSY scenario (b). We create an ensemble of datasets from the toy Monte Carlo model assuming model (b) as input and compare the results to the SM prediction including the theoretical errors to get a feeling for how significantly different from the SM prediction the results are. The results of this are presented in Figs. 8-10: It can be seen that $A_T^{(2)}$, $A_T^{(3)}$ and $A_T^{(4)}$ all show a remarkable separation between the experimental error band and the SM prediction thus providing high sensitivity to NP. For the SUSY scenario (b) chosen here, the deviation for A_{FB} and F_L on the other hand is minor.

As mentioned in the introduction, the B factories can already access some of the angular observables using the projection-fit method described in Sec. 5. For example, recently the *BABAR* collaboration announced the first measurement of the longitudinal

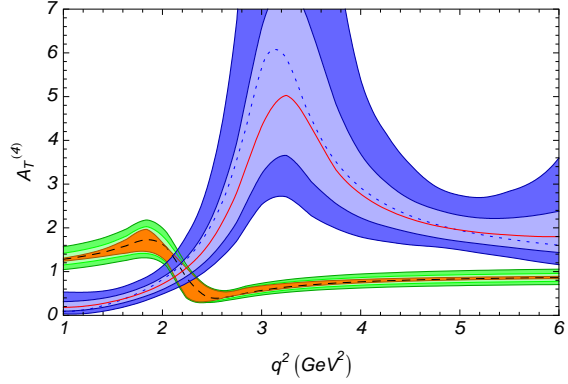


Figure 9: The experimental errors (blue, on top) assuming SUSY scenario (b) with large-gluino mass and positive mass insertion, is compared to the theoretical errors (green, below) assuming the SM. Here the observable $A_T^{(4)}$ is considered.

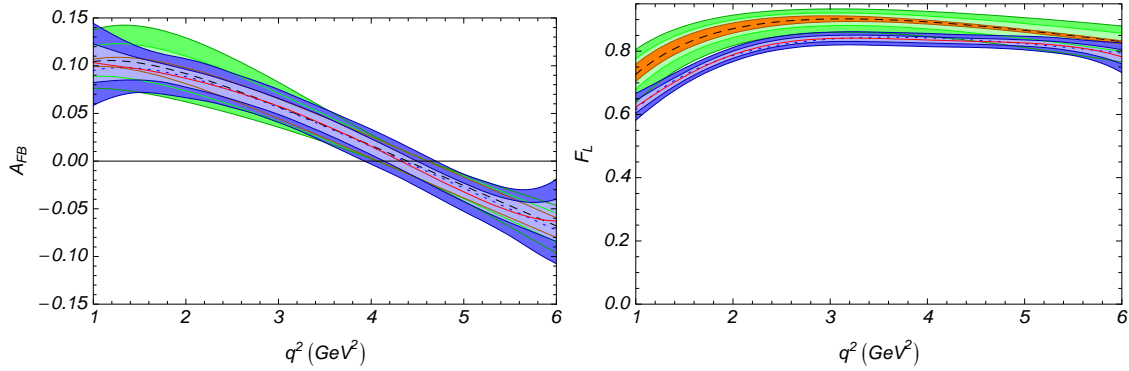


Figure 10: The experimental errors (blue, on top) assuming SUSY scenario (b) with large-gluino mass and positive mass insertion, is compared to the theoretical errors (green, below) assuming the SM. To the left for A_{FB} and the right for F_L .

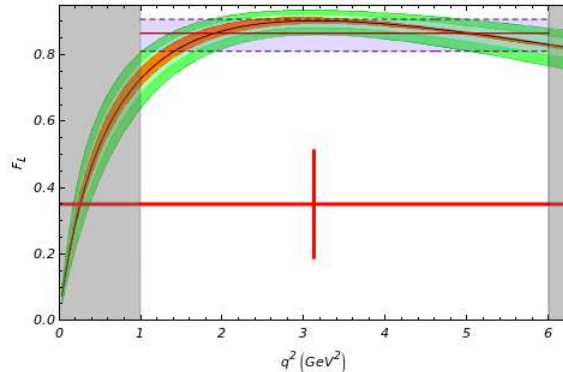


Figure 11: Weighted SM average over the bin $q^2 \in [1 \text{ GeV}^2, 6 \text{ GeV}^2]$ and recent *BABAR* measurement using the extended bin $q^2 \in [4m_\mu^2, 6.25 \text{ GeV}^2]$ (shown in grey).

polarisation in the low q^2 region as an average over the bin $q^2 \in [4m_\mu^2, 6.25 \text{ GeV}^2]$ [8] (see Fig. 11):

$$F_L(q^2 \in [4m_\mu^2, 6.25 \text{ GeV}^2]) = 0.35 \pm 0.16_{\text{stat}} \pm 0.04_{\text{sys}}. \quad (6.28)$$

However, as mentioned before, the spectrum below 1 GeV^2 is theoretically problematic; moreover the rate and also the polarisation F_L are changing dramatically around 1 GeV^2 . Therefore, we strongly recommend to use the standard bin from 1 GeV^2 to 6 GeV^2 . For future comparison we give here the theoretical average, weighted over the rate, using the bin, $q^2 \in [1 \text{ GeV}^2, 6 \text{ GeV}^2]$, based on our results:

$$F_L(q^2 \in [1 \text{ GeV}^2, 6 \text{ GeV}^2]) = 0.86^{+0.04}_{-0.05}. \quad (6.29)$$

and refer to Fig. 7 for the future experimental sensitivity of the *LHCb* experiment. In Fig. 11 we see the theoretical q^2 distribution of F_L with the rate average overlaid.

Finally we might ask what happens if we consider the situation with 100 fb^{-1} of experimental data corresponding to the full dataset from an upgrade to *LHCb*. We assume the same performance of the experiment so simply scale the statistics by a factor 10 compared to the 10 fb^{-1} study. The experimental errors are shown in Fig. 12 and are in general just a factor $\sqrt{10}$ smaller as expected. Comparing to Figs. 4 and 5 it can be seen that the Λ/m_b uncertainties will dominate unless progress is made on the theoretical side.

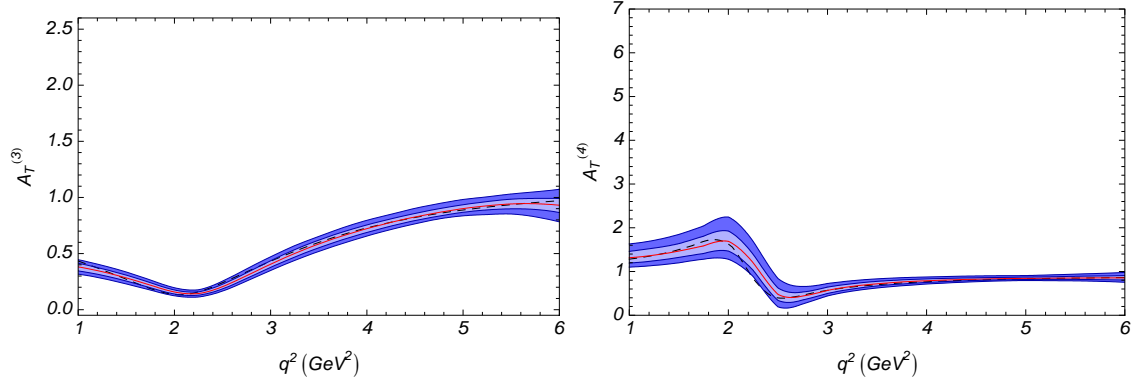


Figure 12: The experimental errors in $A_T^{(3)}$ (right) and $A_T^{(4)}$ left assuming the SM for statistics equivalent to 100 fb^{-1} at the end of an upgrade to LHC**b**.

7 Summary

We have constructed two new observables $A_T^{(3)}$ and $A_T^{(4)}$ out of the K^* spin amplitudes of the $\bar{B}_d \rightarrow \bar{K}^{*0} \mu^+ \mu^-$ decay, that fulfil the criteria of being theoretically clean and can be experimentally extracted from the angular distribution of this decay with good precision. We have shown how to design the new observables for a specific kind of NP operator within the model-independent analysis using the effective field theory approach.

We have presented a complete calculation of all observables in QCD factorisation and have made the impact of unknown Λ/m_b corrections to the various observables explicit. Subsequently, we demonstrated the high sensitivity of $A_T^{(2)}$, $A_T^{(3)}$ and $A_T^{(4)}$ to right handed currents. Clearly theoretical progress on the Λ/m_b corrections would enhance that sensitivity significantly and would be desirable in view of an upgrade of the LHC**b** experiment.

The new observables $A_T^{(3)}$ and $A_T^{(4)}$ exhibit the important property of presenting a direct sensitivity to the longitudinal spin amplitude, while reducing at maximum the sensitivity to the poorly known longitudinal soft form factors within the whole low dilepton mass spectrum. Previously defined F_L or A_{FB} does not exhibit this behaviour. This same idea was behind the construction of $A_T^{(2)}$ using the transverse amplitudes.

The combination of the three observables offer a full view of the sensitivity to NP of the three spin amplitudes with a good control of hadronic uncertainties.

Using a toy Monte Carlo approach we have estimated the statistical uncertainty of all observables for statistics corresponding to LHC**b** and also for Super-LHC**b**. The model performs a fit to the full angular and q^2 distribution. $A_T^{(3)}$ and $A_T^{(4)}$ require a full angular fit and for $A_T^{(2)}$ we have demonstrated that the resolution improves by more than a factor 2 compared to extracting $A_T^{(2)}$ from angular projection. The experimental errors are such

that measuring these new observables will be a powerful way to detect the presence of right handed currents. For the well known measurement of the zero point of the forward-backward asymmetry we see an improvement of 30% in the resolution from a full angular fit compared to fitting the angular projections.

Finally we have shown that the previously discussed angular distribution $A_T^{(1)}$ cannot be measured at either LHC*b* or at a Super-*B* factory.

Acknowledgements

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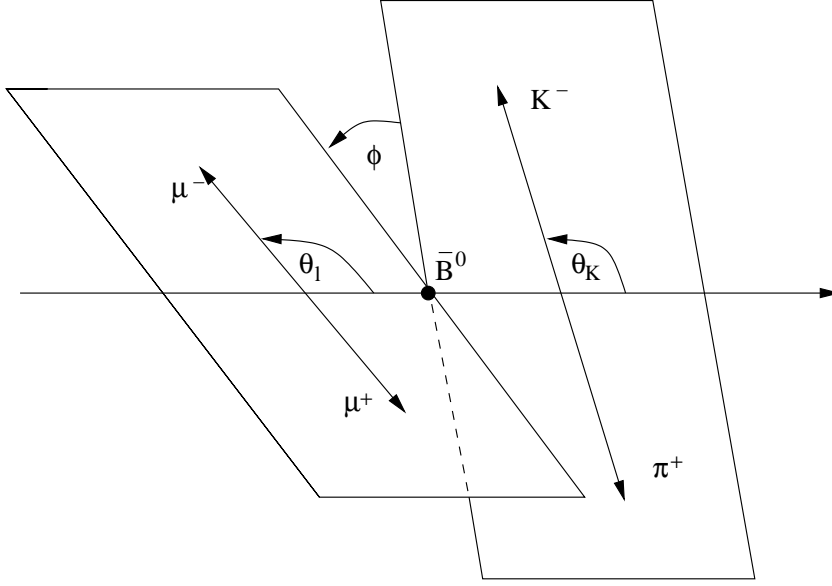


Figure 13: Definition of kinematic variables in the decay $\bar{B}_d \rightarrow \bar{K}^{*0} \mu^+ \mu^-$: The z -axis is the direction in which the B meson flies in the rest frame of the $\mu^+ \mu^-$. θ_l is the angle between the μ^- and the z -axis in the $\mu^+ \mu^-$ rest frame, θ_K is the angle between the K^- and the z -axis in the \bar{K}^* rest frame, and ϕ is the angle between the normals to the $\mu^+ \mu^-$ and $K\pi$ decay planes in the B rest frame. For the $B_d \rightarrow K^{*0} \mu^+ \mu^-$ decay the angles are measured with respect to the μ^+ and the K^+ .

A Kinematics

Assuming the K^* to be on the mass shell, the decay $\bar{B}^0 \rightarrow \bar{K}^{*0} (\rightarrow K^- \pi^+) \ell^+ \ell^-$ is completely described by four independent kinematic variables; namely, the lepton-pair invariant mass, q^2 , and the three angles θ_l , θ_{K^*} , ϕ as illustrated in Fig. 13. The sign of the angles for the \bar{B}_d decay shows great variation in the literature. Therefore we present here the most explicit definition of our conventions. Here \mathbf{p} denote three momentum vectors in the \bar{B}_d rest frame, \mathbf{q} the same in the di-muon rest frame, and \mathbf{r} in the \bar{K}^{*0} rest frame, the z -axis is defined as the direction of the \bar{K}^{*0} in the \bar{B}_d rest frame. Three unit vectors are given in the following way: The first one is defined as the z -axis where the θ angles are measured with respect to, and the other two are perpendicular to the di-muon and \bar{K}^{*0} decay planes.

$$\mathbf{e}_z = \frac{\mathbf{p}_{K^-} + \mathbf{p}_{\pi^+}}{|\mathbf{p}_{K^-} + \mathbf{p}_{\pi^+}|}, \quad \mathbf{e}_l = \frac{\mathbf{p}_{\mu^-} \times \mathbf{p}_{\mu^+}}{|\mathbf{p}_{\mu^-} \times \mathbf{p}_{\mu^+}|}, \quad \mathbf{e}_K = \frac{\mathbf{p}_{K^-} \times \mathbf{p}_{\pi^+}}{|\mathbf{p}_{K^-} \times \mathbf{p}_{\pi^+}|}. \quad (\text{A.30})$$

It follows for the \bar{B}_d

$$\cos \theta_l = \frac{\mathbf{q}_{\mu^-} \cdot \mathbf{e}_z}{|\mathbf{q}_{\mu^-}|}, \quad \cos \theta_K = \frac{\mathbf{r}_{K^-} \cdot \mathbf{e}_z}{|\mathbf{r}_{K^-}|} \quad (\text{A.31})$$

and

$$\sin \phi = (\mathbf{e}_l \times \mathbf{e}_K) \cdot \mathbf{e}_z, \quad \cos \phi = \mathbf{e}_K \cdot \mathbf{e}_l. \quad (\text{A.32})$$

The angles are defined in the intervals

$$-1 \leq \cos \theta_l \leq 1, \quad -1 \leq \cos \theta_K \leq 1, \quad -\pi \leq \phi < \pi, \quad (\text{A.33})$$

where in particular it should be noted that the ϕ angle is signed.

In words, for the \bar{B}_d the angle θ_l is measured as the angle between the μ^- and the z -axis in the dimuon rest frame. As the \bar{B}_d flies in the direction of the z -axis in the dimuon rest frame this is equivalent to measuring θ_l as the angle between the muon and the \bar{B}_d in the di-muon rest frame. The angle θ_K is measured as the angle between the kaon and the z -axis measured in the \bar{K}^{*0} rest frame. Finally ϕ is the angle between the normals to the planes defined by the $K\pi$ system and the $\mu^+\mu^-$ system in the rest frame of the \bar{B}_d meson.

B Theoretical framework

The coefficient functions I_i in the differential decay rate are given in terms of the K^* spin amplitudes (see Eq. (2.3)) discussed in Sec. 3. The theoretical expressions of those spin amplitudes can be derived using the following standard steps:

- The effective Hamiltonian describing the quark transition $b \rightarrow s\ell^+\ell^-$ is given by

$$\mathcal{H}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \sum_{i=1}^{10} [C_i(\mu) \mathcal{O}_i(\mu) + C'_i(\mu) \mathcal{O}'_i(\mu)], \quad (\text{B.34})$$

where in addition to the SM operators we have also added the chirally flipped partners. In what follows, the same conventions are used as in [17]. In the NP analysis, we will focus on the the chirally flipped \mathcal{O}'_7 operator in addition to the most important SM operators \mathcal{O}_7 , \mathcal{O}_9 , and \mathcal{O}_{10} :

$$\mathcal{O}_7 = \frac{e}{16\pi^2} m_b (\bar{s} \sigma_{\mu\nu} P_R b) F^{\mu\nu}, \quad \mathcal{O}'_7 = \frac{e}{16\pi^2} m_b (\bar{s} \sigma_{\mu\nu} P_L b) F^{\mu\nu} \quad (\text{B.35})$$

$$\mathcal{O}_9 = \frac{e^2}{16\pi^2} (\bar{s} \gamma_\mu P_L b) (\bar{\ell} \gamma^\mu \ell), \quad \mathcal{O}_{10} = \frac{e^2}{16\pi^2} (\bar{s} \gamma_\mu P_L b) (\bar{\ell} \gamma^\mu \gamma_5 \ell), \quad (\text{B.36})$$

where $P_{L,R} = (1 \mp \gamma_5)/2$ and $m_b \equiv m_b(\mu)$ is the running mass in the $\overline{\text{MS}}$ scheme.

- From the effective Hamiltonian it is straightforward to compute the matrix element for the decay $\bar{B}_d \rightarrow \bar{K}^{*0} \ell^+ \ell^-$ with $\bar{K}^{*0} \rightarrow K^- \pi^+$:

$$\begin{aligned} \mathcal{M} = & \frac{G_F \alpha}{\sqrt{2} \pi} V_{tb} V_{ts}^* \left\{ \left[\mathcal{C}_9^{(\text{eff})} \langle K \pi | (\bar{s} \gamma^\mu P_L b) | B \rangle \right. \right. \\ & \left. \left. - \frac{2m_b}{q^2} \langle K \pi | \bar{s} i \sigma^{\mu\nu} q_\nu (\mathcal{C}_7^{(\text{eff})} P_R + \mathcal{C}_7'^{(\text{eff})} P_L) b | B \rangle \right] (\bar{\ell} \gamma_\mu \ell) \right. \\ & \left. + \mathcal{C}_{10} \langle K \pi | (\bar{s} \gamma^\mu P_L b) | B \rangle (\bar{\ell} \gamma_\mu \gamma_5 \ell) \right\}, \end{aligned} \quad (\text{B.37})$$

where q is the four-momentum of the lepton pair.

- The hadronic part of the matrix element describing the $B \rightarrow K \pi$ transition can be parameterised in terms of $B \rightarrow K^*$ form factors by means of a narrow-width approximation (see for example [20]). The relevant form factors are defined as:

$$\begin{aligned} \langle K^*(p_{K^*}) | \bar{s} \gamma_\mu P_{L,R} b | B(p) \rangle = & i \epsilon_{\mu\nu\alpha\beta} \epsilon^{\nu*} p^\alpha q^\beta \frac{V(q^2)}{m_B + m_{K^*}} \mp \frac{1}{2} \left\{ \epsilon_\mu^*(m_B + m_{K^*}) A_1(q^2) \right. \\ & \left. - (\epsilon^* \cdot q) (2p - q)_\mu \frac{A_2(q^2)}{m_B + m_{K^*}} - \frac{2m_{K^*}}{q^2} (\epsilon^* \cdot q) [A_3(q^2) - A_0(q^2)] q_\mu \right\}, \end{aligned} \quad (\text{B.38})$$

where

$$A_3(q^2) = \frac{m_B + m_{K^*}}{2m_{K^*}} A_1(q^2) - \frac{m_B - m_{K^*}}{2m_{K^*}} A_2(q^2), \quad (\text{B.39})$$

and

$$\begin{aligned} \langle K^*(p_{K^*}) | \bar{s} i \sigma_{\mu\nu} q^\nu P_{R,L} b | B(p) \rangle = & -i \epsilon_{\mu\nu\alpha\beta} \epsilon^{\nu*} p^\alpha q^\beta T_1(q^2) \pm \frac{1}{2} \left\{ [\epsilon_\mu^*(m_B^2 - m_{K^*}^2) \right. \\ & \left. - (\epsilon^* \cdot q) (2p - q)_\mu] T_2(q^2) + (\epsilon^* \cdot q) \left[q_\mu - \frac{q^2}{m_B^2 - m_{K^*}^2} (2p - q)_\mu \right] T_3(q^2) \right\}. \end{aligned} \quad (\text{B.40})$$

In the above, $q = p_{l^+} + p_{l^-}$ and ϵ^μ is the K^* polarisation vector.

- In the heavy-quark and large-energy limit the seven a priori independent $B \rightarrow K^*$ form factors in Eqs. (B.38) and (B.40) reduce to two universal form factors ξ_\perp and ξ_\parallel in the leading order [25, 26]:³

$$A_1(q^2) = \frac{2E_{K^*}}{m_B + m_{K^*}} \xi_\perp(E_{K^*}), \quad (\text{B.41a})$$

$$A_2(q^2) = \frac{m_B}{m_B - m_{K^*}} \left[\xi_\perp(E_{K^*}) - \xi_\parallel(E_{K^*}) \right], \quad (\text{B.41b})$$

³Following Ref. [26], the longitudinal form factor ξ_\parallel is related to that of Ref. [25] by $\xi_\parallel = (m_{K^*}/E_{K^*}) \zeta_\parallel$.

$$A_0(q^2) = \frac{E_{K^*}}{m_{K^*}} \xi_{\parallel}(E_{K^*}), \quad (\text{B.41c})$$

$$V(q^2) = \frac{m_B + m_{K^*}}{m_B} \xi_{\perp}(E_{K^*}), \quad (\text{B.41d})$$

$$T_1(q^2) = \xi_{\perp}(E_{K^*}), \quad (\text{B.41e})$$

$$T_2(q^2) = \frac{2E_{K^*}}{m_B} \xi_{\perp}(E_{K^*}), \quad (\text{B.41f})$$

$$T_3(q^2) = \xi_{\perp}(E_{K^*}) - \xi_{\parallel}(E_{K^*}). \quad (\text{B.41g})$$

Here, E_{K^*} is the energy of the final vector meson in the B rest frame,

$$E_{K^*} \simeq \frac{m_B}{2} \left(1 - \frac{q^2}{m_B^2} \right). \quad (\text{B.42})$$

These relations valid in the low- q^2 region allow to simplify the spin amplitudes to arrive at the Eqs. (3.9–3.11) which are crucial for the construction of our new observables. They are violated by symmetry breaking corrections of order α_s and $1/m_b$.

C NLO corrections to the spin amplitudes

The NLO corrections to the form factors at order α_s are given in Ref. [30]. In the presence of right-handed currents ($C_7^{\text{eff}} \neq 0$), the spin amplitudes read [17, 18]

$$A_{\perp L,R} = N\sqrt{2} \lambda^{1/2} \left[(\mathcal{C}_9 \mp \mathcal{C}_{10}) \frac{V(q^2)}{m_B + m_{K^*}} + \frac{2m_b}{q^2} \mathcal{T}_{\perp \text{NLO}}^+(q^2) \right], \quad (\text{C.43})$$

$$A_{\parallel L,R} = -N\sqrt{2} (m_B^2 - m_{K^*}^2) \left[(\mathcal{C}_9 \mp \mathcal{C}_{10}) \frac{A_1(q^2)}{m_B - m_{K^*}} + \frac{4m_b E_{K^*}}{m_B \cdot s} \mathcal{T}_{\perp \text{NLO}}^-(q^2) \right], \quad (\text{C.44})$$

$$\begin{aligned} A_{0L,R} = & -\frac{N}{2m_{K^*}q} \left[(\mathcal{C}_9 \mp \mathcal{C}_{10}) \left\{ (m_B^2 - m_{K^*}^2 - q^2)(m_B + m_{K^*})A_1(q^2) - \lambda \frac{A_2(q^2)}{m_B + m_{K^*}} \right\} \right. \\ & + 2m_b \left\{ (m_B^2 + 3m_{K^*}^2 - q^2) \frac{2E_{K^*}}{m_B} \mathcal{T}_{\perp \text{NLO}}^-(q^2) \right. \\ & \left. \left. - \frac{\lambda}{m_B^2 - m_{K^*}^2} \left(\mathcal{T}_{\perp \text{NLO}}^-(q^2) + \mathcal{T}_{\parallel \text{NLO}}^-(q^2) \right) \right\} \right], \quad (\text{C.45}) \end{aligned}$$

where the form factor relations for $V(q^2)$, $A_0(q^2)$ and $A_1(q^2)$ are as in Eq. 3.9, while $A_2(q^2)$ is given by

$$A_2(q^2) = \frac{m_B}{m_B - m_{K^*}} [\xi_{\perp}(q^2) - \xi_{\parallel}(q^2)(1 + C)], \quad (\text{C.46})$$

being C the $\mathcal{O}(\alpha_s)$ correction to the form factor A_2 computed in [26, 30, 36].

$$C = \frac{\alpha_s}{3\pi} \left[(2 - 2L) + 8 \frac{m_{K^*}}{E_{K^*}} \frac{m_B(m_B - 2E_{K^*})}{4E_{K^*}^2} \kappa_{\parallel}(q^2) \lambda_{B,+}^{-1} \int_0^1 du \frac{\Phi_{K^*,\parallel}(u)}{1-u} \right] \quad (\text{C.47})$$

Moreover, we have

$$\begin{aligned} \mathcal{T}_{\perp\text{NLO}}^{\pm} = \xi_{\perp}(q^2) & \left\{ C_{\perp}^{(0,\pm)} + \frac{\alpha_s}{3\pi} \left[C_{\perp}^{(1,\pm)} \right. \right. \\ & \left. \left. + \kappa_{\perp}(q^2) \lambda_{B,+}^{-1} \int_0^1 du \Phi_{K^*,\perp}(u) \left[T_{\perp,+}^{(\text{f}\pm)}(u) + T_{\perp,+}^{(\text{nf})}(u) \right] \right] \right\} \end{aligned}$$

and

$$\begin{aligned} \mathcal{T}_{\parallel\text{NLO}}^{\pm} = \xi_{\parallel}(q^2) & \left\{ C_{\parallel}^{(0,\pm)} + \kappa_{\parallel}(q^2) \frac{m_{K^*}^*}{E_{K^*}} \lambda_{B,-}^{-1}(q^2) \int_0^1 du \Phi_{K^*,\parallel}(u) \hat{T}_{\parallel,-}^{(0)}(u) \right. \\ & + \frac{\alpha_s}{3\pi} \left[C_{\parallel}^{(1,\pm)} + \kappa_{\parallel}(q^2) \frac{m_{K^*}^*}{E_{K^*}} \left(\lambda_{B,+}^{-1} \int_0^1 du \Phi_{K^*,\parallel}(u) \left[T_{\parallel,+}^{(\text{f}\pm)}(u) + T_{\parallel,+}^{(\text{nf})}(u) \right] \right. \right. \\ & \left. \left. + \lambda_{B,-}^{-1}(q^2) \int_0^1 du \Phi_{K^*,\parallel}(u) \hat{T}_{\parallel,-}^{(\text{nf})}(u) \right) \right] \right\} \quad (\text{C.48}) \end{aligned}$$

where $\kappa_z \equiv \pi^2 f_B f_{K^*,z}(\mu) / (N_c m_B \xi_z(q^2))$ (with $z = \perp, \parallel$). The symbol $+$ stands for the substitution of $\mathcal{C}_7^{(\text{eff})} \rightarrow \mathcal{C}_7^{(\text{eff})} + \mathcal{C}_7^{\prime(\text{eff})}$ and $-$ for $\mathcal{C}_7^{(\text{eff})} \rightarrow \mathcal{C}_7^{(\text{eff})} - \mathcal{C}_7^{\prime(\text{eff})}$, wherever $\mathcal{C}_7^{(\text{eff})}$ appears. For instance, in the definition of $C_z^{(1,\pm)} = C_z^{(\text{f}\pm)} + C_z^{(\text{nf})}$ (with $z = \perp, \parallel$), the factorizable correction reads [26, 30].

$$C_{\perp}^{(\text{f}\pm)} = \left(C_7^{\text{eff}} \pm C_7^{\text{eff}\prime} \right) \left(4 \ln \frac{m_b^2}{\mu^2} - 4 - L \right), \quad (\text{C.49})$$

$$C_{\parallel}^{(\text{f}\pm)} = - \left(C_7^{\text{eff}} \pm C_7^{\text{eff}\prime} \right) \left(4 \ln \frac{m_b^2}{\mu^2} - 6 + 4L \right) + \frac{m_B}{2m_b} Y(q^2) (2 - 2L) \quad (\text{C.50})$$

$$\text{with } L \equiv - \frac{m_b^2 - s}{q^2} \ln \left(1 - \frac{q^2}{m_b^2} \right).$$

while the non-factorizable contribution $C_z^{(\text{nf})}$ is common to both. In the definition of the hard scattering functions with $T_{z,\pm}^{(1\pm)} = T_{z,\pm}^{(\text{f}\pm)} + T_{z,\pm}^{(\text{nf})}$ (with $z = \perp, \parallel$), the factorizable correction reads [26, 30]:

$$T_{\perp,+}^{(\text{f}\pm)}(u, \omega) = \left(C_7^{\text{eff}} \pm C_7^{\text{eff}\prime} \right) \frac{2m_B}{\bar{u}E_{K^*}}, \quad (\text{C.51})$$

$$T_{\parallel,+}^{(\text{f}\pm)}(u, \omega) = \left[\left(C_7^{\text{eff}} \pm C_7^{\text{eff}\prime} \right) + \frac{q^2}{2m_b m_B} Y(q^2) \right] \frac{2m_B^2}{(1-u)E_{K^*}^2} \quad (\text{C.52})$$

$$T_{\perp,-}^{(\text{f})}(u, \omega) = T_{\parallel,-}^{(\text{f})}(u, \omega) = 0; \quad (\text{C.53})$$

again the non-factorizable part is common to both cases, because it does not received contributions from \mathcal{O}_7 . For the definition of the function $Y(q^2)$ and for the non-factorizable contributions we refer the reader to [26, 30].

References

- [1] M. Artuso *et al.*, arXiv:0801.1833 [hep-ph].
- [2] T. Hurth, Rev. Mod. Phys. **75** (2003) 1159 [arXiv:hep-ph/0212304].
- [3] T. Hurth, Int. J. Mod. Phys. A **22** (2007) 1781 [arXiv:hep-ph/0703226].
- [4] A. Ishikawa *et al.* [Belle Collaboration], Phys. Rev. Lett. **91** (2003) 261601 [arXiv:hep-ex/0308044].
- [5] B. Aubert *et al.* [BABAR Collaboration], Phys. Rev. Lett. **91** (2003) 221802 [arXiv:hep-ex/0308042].
- [6] A. Ishikawa *et al.*, Phys. Rev. Lett. **96** (2006) 251801 [arXiv:hep-ex/0603018].
- [7] B. Aubert *et al.* [BABAR Collaboration], Phys. Rev. D **73** (2006) 092001 [arXiv:hep-ex/0604007].
- [8] B. Aubert *et al.* [BABAR Collaboration], arXiv:0804.4412 [hep-ex].
- [9] J. Dickens, V. Gibson, C. Lazzeroni and M. Patel, CERN-LHCB-2007-038.
- [10] J. Dickens, V. Gibson, C. Lazzeroni and M. Patel, CERN-LHCB-2007-039.
- [11] U. Egede, CERN-LHCB-2007-057.
- [12] T. Browder, M. Ciuchini, T. Gershon, M. Hazumi, T. Hurth, Y. Okada and A. Stocchi, JHEP **0802** (2008) 110 [arXiv:0710.3799 [hep-ph]].
- [13] M. Bona *et al.*, arXiv:0709.0451 [hep-ex].
- [14] J. L. . Hewett *et al.*, arXiv:hep-ph/0503261.
- [15] A. G. Akeroyd *et al.* [SuperKEKB Physics Working Group], arXiv:hep-ex/0406071.
- [16] F. Krüger, Chapter 2.17 of Ref. [14].
- [17] F. Kruger and J. Matias, Phys. Rev. D **71**, 094009 (2005); J. Matias, PoS **HEP2005** (2006) 281 [arXiv:hep-ph/0511274].
- [18] E. Lunghi and J. Matias, JHEP **0704** (2007) 058 [arXiv:hep-ph/0612166].
- [19] C. Bobeth, G. Hiller and G. Piranishvili, arXiv:0805.2525 [hep-ph].

- [20] F. Krüger, L. M. Sehgal, N. Sinha, and R. Sinha, Phys. Rev. D **61**, 114028 (2000); **63**, 019901(E) (2001).
- [21] D. Melikhov, N. Nikitin, and S. Simula, Phys. Lett. B **442**, 381 (1998).
- [22] C. S. Kim, Y. G. Kim, C.-D. Lü, and T. Morozumi, Phys. Rev. D **62**, 034013 (2000); C. S. Kim, Y. G. Kim, and C.-D. Lü, *ibid.* **64**, 094014 (2001).
- [23] A. Faessler, T. Gutsche, M. A. Ivanov, J. G. Körner, and V. E. Lyubovitskij, EPJdirect **C4**, 18 (2002).
- [24] A. Ali and A. S. Safir, Eur. Phys. J. C **25**, 583 (2002).
- [25] J. Charles, A. Le Yaouanc, L. Oliver, O. Pène, and J.-C. Raynal, Phys. Rev. D **60**, 014001 (1999); Phys. Lett. B **451**, 187 (1999). See also M. J. Dugan and B. Grinstein, *ibid.* **255**, 583 (1991).
- [26] M. Beneke and T. Feldmann, Nucl. Phys. B **592** (2001) 3 [hep-ph/0008255].
- [27] G. Burdman and G. Hiller, Phys. Rev. D **63**, 113008 (2001).
- [28] B. Stech, Phys. Lett. B **354**, 447 (1995); J. M. Soares, Phys. Rev. D **54**, 6837 (1996); [arXiv:hep-ph/9810402].
- [29] J. M. Soares, arXiv:hep-ph/9810421.
- [30] M. Beneke, T. Feldmann, and D. Seidel, Nucl. Phys. **B612**, 25 (2001).
- [31] J. A. Casas and S. Dimopoulos, Phys. Lett. B **387** (1996) 107 [arXiv:hep-ph/9606237].
- [32] U. Egede, T. Hurth, J. Matias, M. Ramon and W. Reece, in preparation.
- [33] A. Ali, T. Mannel and T. Morozumi, Phys. Lett. B **273** (1991) 505.
- [34] M. Beneke, T. Feldmann and D. Seidel, Nucl. Phys. B **612** (2001) 25 [arXiv:hep-ph/0106067].
- [35] T. Feldmann and J. Matias, JHEP **0301** (2003) 074 [arXiv:hep-ph/0212158].
- [36] M. Beneke, T. Feldmann and D. Seidel, Eur. Phys. J. C **41** (2005) 173 [arXiv:hep-ph/0412400].