# Recent Results in Charmless Hadronic B Decays from BABAR 

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#### Abstract

We report results from five analyses based on data taken with the $B A B A R$ detector at the PEP-II asymmetric $e^{+} e^{-}$collider. Included are branching fraction measurements for many $B$-meson decays involving $\eta, \eta^{\prime}, \omega, \phi$ or $a_{0}$ mesons and the final state $K_{S}^{0} \pi^{+} \pi^{-}$, and a full angular analysis of the decay $B^{0} \rightarrow \phi K^{* 0}$.


## 1 Introduction

Many interesting new results from $B A B A R$ for charmless hadronic $B$ decays were presented previously at the Electroweak session of the XXXIXth Rencontres de Moriond. For new measurements of $\sin 2 \beta$ from four final states $\left(\phi K^{0}, K^{+} K^{-} K_{S}^{0}, \pi^{0} K_{S}^{0}, f_{0} K_{S}^{0}\right.$ ), see the writeup by Marc Verderi. Also a new preliminary result for the decay $B^{0} \rightarrow \rho^{+} \rho^{-}$, with a measurement of the CKM angle $\alpha$ was presented in a talk by Lydia Roos. Finally a measurement of the time-dependent asymmetry of the decay $B^{0} \rightarrow \pi^{0} K_{S}^{0} \gamma$ was shown by Eugenio Paoloni. With adequate data, the latter mode can provide interesting constraints on new physics.

In this paper I will report on five other new analyses of charmless hadronic $B$ decays. The first involves $B$ decays to $\eta^{(\prime)} K^{*}, \eta^{(\prime)} \rho, \eta^{(\prime)} \pi^{0}, \omega \pi^{0}$, and $\phi \pi^{01]}$ Substantial signals are seen for $B \rightarrow$ $\eta K^{*}$ and limits are provided for the other modes. The decay $B \rightarrow \eta^{\prime} K^{*}$ is particularly interesting since it provides limits on a flavor-singlet amplitude ${ }^{233}$ The second analysis searches for eight isoscalar final states $\frac{4}{4}$ In addition to the interest in observing signals should the branching fractions be large enough, these channels are interesting because they can provide constraints on the expected value of $\sin 2 \beta$ for the modes $B^{0} \rightarrow \eta^{\prime} K^{0}$ and $B^{0} \rightarrow \phi K^{0} 516$ These channels provide constraints on the size of the color-suppressed tree amplitudes for these penguin-dominated channels. The third analysis involves a search for $B$ decays to the scalar $a_{0}$ meson accompanied by pions or kaons. Little is known about decays involving scalars. The fourth analysis is a fairly precise measurement of the decay $B \rightarrow K_{S}^{0} \pi^{+} \pi^{-}$. The last analysis measures the polarization and potential $C P$-violating terms in the full angular analysis of the decay $B \rightarrow \phi K^{* 0}$.

## 2 Datasets and analysis details

The results presented here are based on data collected with the BABAR detector ${ }^{[7]}$ at the PEP-II asymmetric $e^{+} e^{-}$collider located at the Stanford Linear Accelerator Center. Most analyses
use a sample of 89 million $B \bar{B}$ pairs, recorded at the $\Upsilon(4 S)$ resonance (center-of-mass energy $\sqrt{s}=10.58 \mathrm{GeV}$ ). The $B \rightarrow \phi K^{* 0}$ analysis uses a sample of 124 million $B \bar{B}$ pairs.

A $B$-meson candidate is characterized kinematically by the energy-substituted mass $m_{\mathrm{ES}}$ and by the energy difference $\Delta E$, defined as

$$
\begin{align*}
m_{\mathrm{ES}} & =\sqrt{\frac{1}{4} s-\mathbf{p}_{B}^{* 2}} \quad \text { and }  \tag{1}\\
\Delta E & =E_{B}^{*}-\frac{1}{2} \sqrt{s} \tag{2}
\end{align*}
$$

where $\left(E_{B}, \mathbf{p}_{B}\right)$ is the $B$-candidate four vector and $s$ is the square of the invariant mass of the electron-positron system; the asterisk denotes the value in the $\Upsilon(4 S)$ frame. All analyses use these two quantities in unbinned maximum-likelihood fits which also have invariant masses of quasi-two-body resonances in the final states and a Fisher discriminant that is sensitive to event shape.

## 3 Measurements of $\eta^{(\prime)} K^{*}$ and related decays

We have searched for the $B$ decays to $\eta^{(\prime)} K^{*}, \eta^{(\prime)} \rho, \eta^{(\prime)} \pi^{0}, \omega \pi^{0}$, and $\phi \pi^{0}$. We find a substantial signal for both charge states of the $B \rightarrow \eta K^{*}$ decay as shown in the projection plots in Fig. $\mathbb{\square}$ These results are tabulated in Table $\square$ along with previous results for the $\eta^{(1)} K$ and $\eta^{(1)} \pi$ decays. Thus we have completed the measurement of the four $\left(\eta, \eta^{\prime}\right)\left(K, K^{*}\right)$ final states with a sensitivity in the branching fraction of a few times $10^{-6}$. We find no significant signal for $B \rightarrow \eta^{\prime} K^{*}$; the $90 \%$ C.L. upper limit is not yet precise enough to determine whether a flavor-singlet component is present for this decay, though we do restrict the size of such a contribution. See Ref. 2 and references therein for a discussion of this issue. We also have evidence for the decay $B^{+} \rightarrow \eta \rho^{+}$ with a significance of $3.5 \sigma$.


Figure 1: Projections of the $B$-candidate $m_{\mathrm{ES}}$ and $\Delta E$ distributions for (a),(b) $B^{0} \rightarrow \eta K^{* 0}$ and (c),(d) $B^{+} \rightarrow$ $\eta K^{*+}$. Not all events are shown since these plots are made with a requirement on the likelihood.

Table 1: We show the significance $\mathcal{S}(\sigma)$ (including systematic errors), fit branching fractions $\mathcal{B}, 90 \%$ C.L. upper limits, and charge asymmetries for the 12 new measurements as well as six related measurements (above the line) that were published recently $\frac{89}{9}$

| Mode | $\mathcal{S}(\sigma)$ | $\mathcal{B}\left(10^{-6}\right)$ | UL $\left(10^{-6}\right)$ | $\mathcal{A}_{c h}$ |
| :--- | :---: | :---: | :---: | :---: |
| $B^{+} \rightarrow \eta^{\prime} K^{+}$ | $>10$ | $76.9 \pm 3.5$ |  | $0.037 \pm 0.045$ |
| $B^{0} \rightarrow \eta^{\prime} K^{0}$ | $>10$ | $60.6 \pm 5.6$ |  |  |
| $B^{+} \rightarrow \eta \pi^{+}$ | 7.9 | $5.3 \pm 1.0 \pm 0.3$ |  | $-0.44 \pm 0.18 \pm 0.01$ |
| $B^{+} \rightarrow \eta K^{+}$ | 6.1 | $3.4 \pm 0.8 \pm 0.2$ |  | $-0.52 \pm 0.24 \pm 0.01$ |
| $B^{0} \rightarrow \eta K^{0}$ | 3.3 | $2.9 \pm 1.0 \pm 0.2$ | $<5.2$ |  |
| $B^{+} \rightarrow \eta^{\prime} \pi^{+}$ | 3.4 | $2.7 \pm 1.2 \pm 0.3$ | $<4.5$ |  |
| $B^{+} \rightarrow \eta K^{*+}$ | 9 | $25.6 \pm 4.0 \pm 2.4$ |  | $+0.13 \pm 0.14 \pm 0.02$ |
| $B^{0} \rightarrow \eta K^{* 0}$ | 11 | $18.6 \pm 2.3 \pm 1.2$ |  | $+0.02 \pm 0.11 \pm 0.02$ |
| $B^{+} \rightarrow \eta \rho^{+}$ | 3.5 | $9.2 \pm 3.4 \pm 1.0$ | $<14$ |  |
| $B^{0} \rightarrow \eta \rho^{0}$ | - | $-1.1_{-0.9}^{+0.7} \pm 0.4$ | $<1.5$ |  |
| $B^{0} \rightarrow \eta \pi^{0}$ | 0.8 | $0.7_{-0.9}^{+1.1} \pm 0.3$ | $<2.5$ |  |
| $B^{+} \rightarrow \eta^{\prime} K^{*+}$ | 1.9 | $6.3_{-3.6}^{+4.6} \pm 1.8$ | $<14$ |  |
| $B^{0} \rightarrow \eta^{\prime} K^{* 0}$ | 2.1 | $4.1_{-1.8}^{+2.1} \pm 1.2$ | $<7.6$ |  |
| $B^{+} \rightarrow \eta^{\prime} \rho^{+}$ | 2.6 | $12.9_{-5.5}^{+6.2} \pm 2.0$ | $<22$ |  |
| $B^{0} \rightarrow \eta^{\prime} \rho^{0}$ | 0.5 | $0.8_{-1.2}^{+1.7} \pm 0.9$ | $<4.3$ |  |
| $B^{0} \rightarrow \eta^{\prime} \pi^{0}$ | 0.7 | $1.0_{-1.0}^{+1.4} \pm 0.8$ | $<3.7$ |  |
| $B^{0} \rightarrow \omega \pi^{0}$ | - | $-0.6_{-0.5}^{+0.7} \pm 0.2$ | $<1.2$ |  |
| $B^{0} \rightarrow \phi \pi^{0}$ | 0.7 | $0.2_{-0.3}^{+0.4} \pm 0.1$ | $<1.0$ |  |

## 4 Search for isoscalar charmless decays

We have searched for eight isoscalar charmless decays. These decays are particularly interesting because they can provide constraints on the expected value of $\sin 2 \beta$ for the modes $B^{0} \rightarrow \eta^{\prime} K^{0}$ and $B^{0} \rightarrow \phi K^{0.56]}$ Results are summarized in Table2. The $4.3 \sigma$ signal in $B^{0} \rightarrow \eta \omega$ is unexpected and may be a fluctuation; more data will be required to see if this is interesting. The limits on all of these modes have improved the understanding of the expected value of $\sin 2 \beta$ for $B^{0} \rightarrow \eta^{\prime} K^{0}$ so that the model-independent precision is now 0.10 . ${ }^{6}$ This is an improvement of about a factor of five on the previous limits 5

Table 2: Significance $\mathcal{S}(\sigma)$ (including systematic uncertainties), measured branching fraction $\mathcal{B}$, and $90 \%$ C.L. upper limits (UL) from this and previous measurements by CLEO.

| Mode | $\mathrm{S}(\sigma)$ | $\mathcal{B}\left(10^{-6}\right)$ | $\mathrm{UL}\left(10^{-6}\right)$ | CLEO UL $\left(10^{-6}\right)^{\underline{10}]}$ |
| :--- | :--- | :---: | :---: | :---: |
| $B^{0} \rightarrow \eta \eta$ | 0.0 | $-0.9_{-1.4}^{+1.6} \pm 0.7$ | $<2.8$ | $<18$ |
| $B^{0} \rightarrow \eta \eta^{\prime}$ | 0.3 | $0.6_{-1.7}^{+2.1} \pm 1.1$ | $<4.6$ | $<27$ |
| $B^{0} \rightarrow \eta^{\prime} \eta^{\prime}$ | 0.4 | $1.7_{-3.7}^{+4.8} \pm 0.6$ | $<10$ | $<47$ |
| $B^{0} \rightarrow \eta \omega$ | 4.3 | $4.0_{-1.2}^{+1.3} \pm 0.4$ | $<6.2$ | $<12$ |
| $B^{0} \rightarrow \eta^{\prime} \omega$ | 0.0 | $-0.2_{-0.9}^{+1.3} \pm 0.4$ | $<2.8$ | $<60$ |
| $B^{0} \rightarrow \eta \phi$ | 0.0 | $-1.4_{-0.4}^{+0.7} \pm 0.2$ | $<1.0$ | $<9$ |
| $B^{0} \rightarrow \eta^{\prime} \phi$ | 0.8 | $1.5_{-1.5}^{+1.8} \pm 0.4$ | $<4.5$ | $<31$ |
| $B^{0} \rightarrow \phi \phi$ | 0.3 | $0.3_{-0.4}^{+0.7} \pm 0.1$ | $<1.5$ | $<12$ |

## 5 Search for $B$ decays involving $a_{0}$ mesons

Very little is known about charmless $B$ decays with a scalar meson in the final state. There are also few predictions for these decays. $\frac{1112}{}$ We have searched for quasi-two-body $B$ decays with an $a_{0}$ meson and a pion or kaon. This follows a previous preliminary search where evidence for the decay $B^{0} \rightarrow a_{0}^{-} \pi^{+}$was found ${ }^{13}$ The results of the present search are summarized in Table 3 We do not confirm the previous result which was obtained with one-quarter of this data sample. The difference appears to be a fluctuation. We provide preliminary upper limits on this and five related decay channels. This are the first measurements for these decays and seem to rule out the largest predictions for the $B^{-} \rightarrow a_{0}^{-} K^{0}$ decay from one recent paper $\frac{12}{}$

Table 3: Significance $\mathcal{S}(\sigma)$ (including systematic uncertainties), measured branching fraction $\mathcal{B}$, and $90 \%$ C.L. upper limits (UL) for $B$ decays involving $a_{0}$ mesons.

| Mode | $\mathcal{S}(\sigma)$ | $\mathcal{B}\left(10^{-6}\right)$ | UL $\left(10^{-6}\right)$ |
| :--- | :---: | :---: | :---: |
| $B^{0} \rightarrow a_{0}^{-} \pi^{+}$ | 2.0 | $2.8_{-1.3}^{+1.5} \pm 0.7$ | $<5.1$ |
| $B^{0} \rightarrow a_{0}^{-} K^{+}$ | 0.4 | $0.4_{-0.8}^{+1.0} \pm 0.2$ | $<2.1$ |
| $B^{-} \rightarrow a_{0}^{-} K^{0}$ | 0.6 | $-1.5_{-1.8}^{+2.4} \pm 0.8$ | $<3.9$ |
| $B^{+} \rightarrow a_{0}^{0} \pi^{+}$ | 1.9 | $3.6_{-1.9}^{2+1 .} \pm 0.8$ | $<6.7$ |
| $B^{+} \rightarrow a_{0}^{0} K^{+}$ | 0.0 | $-3.7_{-1.3}^{+1.6} \pm 0.5$ | $<1.8$ |
| $B^{0} \rightarrow a_{0}^{0} K^{0}$ | 1.0 | $2.8_{-2.4}^{+3.1} \pm 1.1$ | $<7.8$ |

## 6 Measurement of the branching fraction for the decay $B \rightarrow K^{0} \pi^{+} \pi^{-}$

We measure the branching fraction of the decay $B \rightarrow K^{0} \pi^{+} \pi^{-}$. Corrections are made for the efficiency variation across the Dalitz plot. From $310 \pm 27$ signal events, we measure $\mathcal{B}(B \rightarrow$ $\left.K^{0} \pi^{+} \pi^{-}\right)=43.8 \pm 3.8 \pm 3.4 \times 10^{-6}$. This is in good agreement with, but more precise than, previous results. ${ }^{14} \mathrm{An}$ analysis of the Dalitz plot structure is in progress.

7 Measurement of polarization and $C P$-violating terms in a full angular analysis of $B \rightarrow \phi K^{* 0}$

We present a full angular analysis of the decay $B \rightarrow \phi K^{* 0}$. The angular distribution of the $B \rightarrow \phi K^{*}$ decay products can be expressed in the helicity representation with $\mathcal{H}_{i}=\cos \theta_{i}$ and $\Phi$, where $\theta_{i}$ is the angle between the direction of one of the vector meson daughters ( $i=1$ for the $K^{*} \rightarrow K \pi, i=2$ for the $\left.\phi \rightarrow K \bar{K}\right)$ and the direction opposite the $B$ in the resonance rest frame, and $\Phi$ is the angle between the two resonance decay planes. The differential decay width has three complex amplitudes $A_{\lambda}$ for the vector meson helicity $\lambda=0$ or $\pm 1 \frac{1516}{}$ The decay width can be written, in terms of $A_{\|}=\left(A_{+}+A_{-}\right) / \sqrt{2}$, and $A_{\perp}=\left(A_{+}-A_{-}\right) / \sqrt{2}$, as

$$
\begin{array}{r}
\frac{8 \pi}{9 \Gamma} \cdot \frac{d^{3} \Gamma}{d \mathcal{H}_{1} d \mathcal{H}_{2} d \Phi}=\frac{1}{\left|A_{0}\right|^{2}+\left|A_{\|}\right|^{2}+\left|A_{\perp}\right|^{2}} \times\left[\left|A_{0}\right|^{2} \mathcal{H}_{1}^{2} \mathcal{H}_{2}^{2}+\frac{1}{4}\left(\left|A_{\|}\right|^{2}+\left|A_{\perp}\right|^{2}\right)\left(1-\mathcal{H}_{1}^{2}\right)\left(1-\mathcal{H}_{2}^{2}\right)\right. \\
+\frac{1}{4}\left(\left|A_{\|}\right|^{2}-\left|A_{\perp}\right|^{2}\right)\left(1-\mathcal{H}_{1}^{2}\right)\left(1-\mathcal{H}_{2}^{2}\right) \cos 2 \Phi-\operatorname{Im}\left(A_{\perp} A_{\|}^{*}\right)\left(1-\mathcal{H}_{1}^{2}\right)\left(1-\mathcal{H}_{2}^{2}\right) \sin 2 \Phi \\
\left.+\sqrt{2} \operatorname{Re}\left(A_{\|} A_{0}^{*}\right) \sqrt{1-\mathcal{H}_{1}^{2}} \mathcal{H}_{1} \sqrt{1-\mathcal{H}_{2}^{2}} \mathcal{H}_{2} \cos \Phi-\sqrt{2} \operatorname{Im}\left(A_{\perp} A_{0}^{*}\right) \sqrt{1-\mathcal{H}_{1}^{2}} \mathcal{H}_{1} \sqrt{1-\mathcal{H}_{2}^{2}} \mathcal{H}_{2} \sin \Phi\right]
\end{array}
$$

We measure the polarization parameters $f_{L}=\left|A_{0}\right|^{2} / \Sigma\left|A_{\lambda}\right|^{2}, f_{\perp}=\left|A_{\perp}\right|^{2} / \Sigma\left|A_{\lambda}\right|^{2}, \phi_{\|}=$ $\arg \left(A_{\|} / A_{0}\right)$, and $\phi_{\perp}=\arg \left(A_{\perp} / A_{0}\right)$. We also allow for $C P$-violating differences between the $\bar{B}^{0}$

Table 4: We show results for the ten primary signal fit parameters and the secondary triple-product asymmetries. All results include systematic errors quoted last. The dominant correlations coefficients are also shown.

| Fit param. | Fit result | Corr. | Fit param. | Fit result | Corr. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $n_{\text {sig }}($ events $)$ | $129 \pm 14 \pm 9$ |  | $\mathcal{A}_{C P}$ | $-0.12 \pm 0.10 \pm 0.03$ |  |
| $f_{L}$ | $0.52 \pm 0.07 \pm 0.02$ | $\}-52 \%$ | $\mathcal{A}_{C P}^{0}$ | $-0.02 \pm 0.12 \pm 0.01$ |  |
| $f_{\perp}$ | $0.27 \pm 0.07 \pm 0.02$ | $\}$ | $\mathcal{A}_{C P}$ | $-0.10_{-0.27}^{+0.25} \pm 0.04$ | $\}-52 \%$ |
| $\phi_{\\|}(\mathrm{rad})$ | $2.63_{-0.23}^{+0.24} \pm 0.04$ | $+59 \%$ | $\Delta \phi_{\\|}(\mathrm{rad})$ | $0.38_{-0.24}^{+0.23} \pm 0.04$ | $\}+59 \%$ |
| $\phi_{\perp}(\mathrm{rad})$ | $2.71_{-0.24}^{+0.22} \pm 0.03$ |  | $\Delta \phi_{\perp}(\mathrm{rad})$ | $0.30_{-0.22}^{+0.24} \pm 0.03$ |  |
| $\mathcal{A}_{T}^{\\|}$ | $+0.02 \pm 0.05 \pm 0.01$ |  | $\mathcal{A}_{T}^{0}$ | $+0.11 \pm 0.07 \pm 0.01$ |  |

$(Q=+1)$ and the $B^{0}(Q=-1)$ decay amplitudes, where the flavor $\operatorname{sign} Q$ is determined in the self-tagging final state with a $\bar{K}^{*}$ or $K^{*}$ :

$$
\begin{gathered}
n_{\text {sig }}^{Q}=n_{\text {sig }}\left(1+Q \mathcal{A}_{C P}\right) / 2 ; \quad f_{L}^{Q}=f_{L}\left(1+Q \mathcal{A}_{C P}^{0}\right) ; \quad f_{\perp}^{Q}=f_{\perp}\left(1+Q \mathcal{A}_{C P}^{\perp}\right) ; \\
\phi_{\|}^{Q}=\phi_{\|}+Q \Delta \phi_{\|} ; \quad \phi_{\perp}^{Q}=\phi_{\perp}+\frac{\pi}{2}+Q\left(\Delta \phi_{\perp}+\frac{\pi}{2}\right) .
\end{gathered}
$$

From the above parameters one can derive triple-product asymmetries $\mathcal{A}_{T}^{\|}$and $\mathcal{A}_{T}^{0}$ as discussed in Ref. 15

$$
\mathcal{A}_{T}^{\|, 0}=\frac{1}{2}\left(\frac{\operatorname{Im}\left(A_{\perp} A_{\|, 0}^{*}\right)}{\Sigma\left|A_{m}\right|^{2}}+\frac{\operatorname{Im}\left(\bar{A}_{\perp} \bar{A}_{\|, 0}^{*}\right)}{\Sigma\left|\bar{A}_{m}\right|^{2}}\right) .
$$

The longitudinal polarization in this decay is found to be $0.52 \pm 0.07 \pm 0.02$ as seen in Table 4 and Fig. 2(a); this value is surprising since naive expectations and measurements for $B \rightarrow \rho \rho$ indicate a value very close to 1 . This confirms earlier measurements by $B A B A R^{[17]}$ and Belle $\frac{18}{18}$ and is still not understood theoretically. Also shown in Fig. 2 (b)-(d) are measurements involving the other quantities determined in the fit.

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## References

1. BABAR Collaboration, B. Aubert et al., hep-ex/0403025 (2004).
2. C.-W. Chiang and J. L. Rosner, Phys. Rev. D 65, 074035 (2002).
3. M. Beneke and M. Neubert, Nucl. Phys. B 651, 225 (2003).
4. BABAR Collaboration, B. Aubert et al., hep-ex/0403046 (2004).
5. Y. Grossman et al., Phys. Rev. D 68015004 (2003).
6. M. Gronau, J. L. Rosner, and J. Zupan, hep-ph/0403287 (2004).
7. BABAR Collaboration, B. Aubert et al., Nucl. Instr. Meth. A 479, 1 (2002).
8. BABAR Collaboration, B. Aubert et al., Phys. Rev. Lett. 91, 161801 (2003).
9. BABAR Collaboration, B. Aubert et al., Phys. Rev. Lett. 92, 061801 (2004).
10. CLEO Collaboration, B. Behrens et al., Phys. Rev. Lett. 80, 3710 (1998); CLEO Collaboration, T. Bergfeld et al., Phys. Rev. Lett. 81, 272 (1998).
11. V. Chernyak, Phys. Lett. B 509, 273 (2001).
12. P. Minkowski and W. Ochs, hep-ph/0404194 (2004).
13. BABAR Collaboration, B. Aubert et al., hep-ex/0107075 (2001).
14. CLEO Collaboration, E. Eckhart et al., Phys. Rev. Lett. 89, 251801 (2002). Belle Collaboration, A. Garmash et al., Phys. Rev. D 69, 012001 (2004);
15. G. Valencia, Phys. Rev. D 39, 3339 (1989); W. Bensalem, D. London, Phys. Rev. D 64, 116003 (2001); A. Datta and D. London, hep-ph/0303159 (2003).
16. G. Kramer, W.F. Palmer, Phys. Rev. D 45, 193 (1992); H.-Y. Cheng, K.-C. Yang, Phys. Lett. B 511, 40 (2001); C.-H. Chen, Y.-Y. Keum, H-n. Li, Phys. Rev. D 66, 054013 (2002).
17. BABAR Collaboration, B. Aubert et al., Phys. Rev. Lett. 91, 171802 (2003).
18. Belle Collaboration, K.-F. Chen et al., Phys. Rev. Lett. 91, 201801 (2003).


Figure 2: Contour plots with $1 \sigma$ intervals derived from the fit $-2 \ln \mathcal{L}$ distributions for (a) polarization fractions $f_{\perp}$ and $f_{L}$, (b) $C P$-even and $C P$-odd transverse phases ( $[\pi, \pi]$ point expected if no final-state interactions), (c) asymmetry parameters sensitive to direct $C P$ violation; (d) phases of the triple-product asymmetries that are sensitive to new physics. 15

