STUDY OF $\gamma \mathrm{p} \rightarrow \mathrm{p} \omega$ WITH LINEARLY POLARIZ ED PHOTONS AT 2.8 AND 4.7 GEV*
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## ERRATUM

1. Vertical scales for the density matrix elements $\rho_{00}^{0}$, $\operatorname{Re} \rho_{10}^{0}$ and $\rho_{1-1}^{0}$ are incorrectly labeled in Fig. 4. Change 0.4 to 0.2 and -0.4 to -0.2 . Other density matrix elements and $P_{\sigma}$ are correctly labeled.
2. There are two typographical errors in Table IV: In IV-a $(2.8 \mathrm{GeV}$ Gottfried-Jackson system) for $0.06 \leq|t| \leq 0.15 \mathrm{GeV}^{2}$, the value of $\operatorname{Re} \rho_{10}^{\circ}$ is given as $-0.14 \pm 0.04$; it should be $+0.14 \pm 0.04$. In IV-e ( 4.7 GeV helicity system) for $0.014 \leq|t| \leq 0.06$ the value of $\rho_{1-1}^{1}$ should be $-0.04 \pm 0.12$; it is shown correctly in Fig. 4 .
[^0]
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#### Abstract

The reaction $\gamma \mathrm{p} \rightarrow \mathrm{p} \omega$ was studied in a hydrogen bubble chamber using a linearly polarized photon beam. The total cross section was found to be $5.8 \pm 0.5 \mu \mathrm{~b}$ at 2.8 GeV and $3.2 \pm 0.3 \mu \mathrm{~b}$ at 4.7 GeV . From the decay angular distributions these cross sections have been separated into contributions from natural and unnatural parity exchange $\sigma^{N}, \sigma^{U}$ in the $t$ channel. For $|\mathrm{t}|<1 \mathrm{GeV}^{2} \sigma^{\mathrm{N}}=2.5 \pm 0.4 \mu \mathrm{~b}, \sigma^{\mathrm{U}}=2.7 \pm 0.4 \mu \mathrm{~b}$ at 2.8 GeV and $\sigma^{\mathrm{N}}=1.8 \pm 0.3 \mu \mathrm{~b}, \sigma^{\mathrm{U}}=1.3 \pm 0.3 \mu \mathrm{~b}$ at 4.7 GeV . The contributions from unnatural parity exchange are consistent with the predictions of the onepion exchange model.


[^1]The energy dependence and the magnitude of the cross section for $\omega$ production by unpolarized photons mensured ${ }^{1,2}$ in the reaction

$$
\begin{equation*}
\gamma \mathrm{p} \rightarrow \mathrm{p} \pi^{+} \pi^{-} \pi^{\mathrm{o}} \tag{1}
\end{equation*}
$$

suggests that $\omega$ production proceeds partly via one-pion exchange (OPE) and partly via diffraction scattering, with the dominant contribution at low energies ( $\sim 2-4 \mathrm{GeV}$ ) coming from OPE. Using polarized photons, the contributions from natural parity $\left(P=(-1)^{J}\right)$ and unnatural parity $\left(P=-(-1)^{J}\right)$ exchange in the $t-$ channel can be separated, and the above conjecture can be tested.

We have analyzed $\omega$ production in reaction (1) at 2.8 and 4.7 GeV exposing the 82-inch hydrogen bubble chamber at SLAC to the linearly polarized Compton backscattered laser beam. Table I summarizes the details of the beam and of the exposure.

In Table I we list the number of events which gave a OC "fit" to reaction (1) (the photon energy $\mathrm{E}_{\gamma}$ not being constrained) and which satisfied the following criteria: the mass assignments are consistent with ionization, and the event has no accepted fit to the hypothesis $\gamma \mathrm{p} \rightarrow \mathrm{p} \pi^{+} \pi^{-}$. Most of the multineutral events are removed by requiring the reconstructed photon energy to lie within the limits specified in Table I.

In Fig. 1 the $\pi^{+} \pi^{-} \pi^{\circ}$ mass distributions show a clear $\omega$ signal. In order to determine the cross section for $\omega$ production corrections were made for $\omega$ events which: (a) were excluded because they fit the 3 C hypothesis $\gamma \mathrm{p} \rightarrow \mathrm{p} \pi^{+} \pi^{-}\left(X^{2}<25\right)$; (b) have a reconstructed photon energy outside the specified energy interval or a $\pi^{+} \pi^{-} \pi^{\circ}$ mass outside the $\omega$ region ( $0.67-0.90 \mathrm{GeV}$ ); (c) were lost because of short recoil protons; or (d) have a decay mode other than $\pi^{+} \pi^{-} \pi^{\circ}{ }^{7}$ Corrections (a) and (b) were determined using the track and event simulation program PHONY ${ }^{8}$ and amounted to $1.09 \pm 0.02$ at 2.8 GeV and $1.22 \pm 0.06$ at 4.7 GeV . For (c), because events with short recoil protons cannot be measured reliably, we disregarded all events with $|\mathrm{t}|<0.014 \mathrm{GeV}^{2}$ ( t is
the square of the four-momentum transfer between incoming and outgoing proton). At 2.8 GeV the minimum value of $|\mathrm{t}|$ is $0.014 \mathrm{GeV}^{2}$ and no correction of type (c) was applied. At 4.7 GcV we estimate the loss to be $6 \pm 2 \%$ by extrapolating the $t$ distribution according to Eq. (4) below. The scanning efficiency for events with $|t|>0.02 \mathrm{GeV}^{2}$ was found to be greater than $99 \%$.

The corrected total $\omega$ production cross sections are given in Table II and Fig. 2 together with those of other experiments. 1.2.9-11 The differential cross sections $\mathrm{d} \sigma / \mathrm{dt}$ are shown in Fig. 3 and Table III. A fit of $\mathrm{d} \sigma / \mathrm{dt}$ for $0.02<|t|<0.4 \mathrm{GeV}^{2}$ to the form $C \exp (A t)$ leads to the values for $A$ and $C$ given in Table II.

For the analysis of the $\omega$ decay angular distributions we adopt the formalism of Ref. 12. Results will be presented in the helicity system, which was found to be the preferred system for the analysis of $\rho^{0}$ photoproduction. ${ }^{5}$ In this frame the z axis is given by the $\omega$ direction of flight in the total c . m. system. The angles $\theta$ and $\phi$ are defined as the polar and azimuthal angles of the normal to the $\omega$-decay plane in the $\omega$-rest system. The photon polarization plane in the total c.m.s. makes an angle $\Phi$ with the production plane. ${ }^{13}$ The decay angular distribution of the $\omega$ in terms of its spin density matrix is ${ }^{12,14}$ :

$$
\begin{align*}
& \mathrm{W}(\cos \theta, \phi, \phi)= \frac{3}{4 \pi}\left\{\frac{1}{2}\left(1-\rho_{00}^{\mathrm{o}}\right)+\frac{1}{2}\left(3 \rho_{00}^{0}-1\right) \cos ^{2} \theta-\sqrt{2} \operatorname{Re} \rho_{10}^{0} \sin 2 \theta \cos \phi\right. \\
&-\rho_{1-1}^{\mathrm{o}} \sin ^{2} \theta \cos 2 \phi \\
&-\mathrm{P}_{\gamma} \cos 2 \Phi\left[\rho_{11}^{1} \sin ^{2} \theta+\rho_{00}^{1} \cos ^{2} \theta-\sqrt{2} \operatorname{Re} \rho_{10}^{1} \sin 2 \theta \cos \phi-\rho_{1-1}^{1} \sin ^{2} \theta \cos 2 \phi\right] \\
&\left.-\mathrm{P}_{\gamma} \sin 2 \Phi\left[\sqrt{2} \operatorname{Im} \rho_{10}^{2} \sin 2 \theta \sin \phi+\operatorname{Im} \rho_{1-1}^{2} \sin ^{2} \theta \sin 2 \phi\right]\right\} \tag{2}
\end{align*}
$$

where $P_{\gamma}$ is the degree of linear polarization. The nine independent measurable density matrix parameters, which were determined by a moment analysis, are
shown in Fig. 4 as a function of $t$. In $\rho^{\circ}$ photoproduction ${ }^{5}$ we foind for $|t|<0.4$ $\mathrm{GeV}^{2}$ that by choosing the helicity frame all $\rho_{\mathrm{ik}}^{\alpha}$ in Eq. (2) reduced to zoro exeept for two, $\left(\rho_{1-1}^{1}=-\operatorname{Im} \rho_{1-1}^{2}=0.5\right)$ indicating no helicity flip. In contrast, for $\omega$ photoproduction our values for $\rho_{00}^{\circ}$ show that there is considerable helicity flip.

The density matrix parameters are listed in Table IV. For comparison their values are also given in the Gottfried-Jackson and Adair systems. (For the distribution of these systems, see e.g., Ref. 5.)

From the density matrix parameters one can deduce the parity asymmetry, $\mathbf{P}_{\sigma}, \mathbf{P}_{\sigma}=\left(\sigma^{\mathrm{N}}-\sigma^{\mathrm{U}}\right) /\left(\sigma^{\mathrm{N}}+\sigma^{\mathrm{U}}\right)$, which mcasures the cross section contributions $\sigma^{N}, \sigma^{U}$ from natural parity and unnatural parity exchange in the t-channel. In the high energy limit $P_{\sigma}$ is given by ${ }^{12,15}$

$$
\begin{equation*}
\mathrm{P}_{\sigma}=2 \rho_{1-1}^{1}-\rho_{00}^{1} \tag{3}
\end{equation*}
$$

In Table II the values of $\mathrm{P}_{\sigma}, \sigma_{\omega}^{\mathrm{N}}$ and $\sigma_{\omega}^{\mathrm{U}}$ are given for $\omega$ production for $|t|<1.0 \mathrm{GeV}^{2}$ (see also Figs. 2 and 4). Natural and unnatural parity exchanges contribute in approximately equal amounts. The unnatural cross section, $\sigma_{\omega}^{\mathrm{U}}$, decreases from 2.8 to 4.7 GeV whereas $\sigma_{\omega}^{\mathrm{N}}$ does not change significantly. The natural differential cross section, $d \sigma^{N} / \mathrm{dt}$, for $0.02<|\mathrm{t}|<0.4 \mathrm{GeV}^{2}$ is shown in Fig. 3. A fit of $d \sigma / d t$ to the form $C_{N} \exp \left(A_{N} t\right)$ gave the values for $A_{N}$ and $C_{N}$ shown in Table II.

One can compare $\sigma_{\omega}^{N}$ to the corresponding quantity, $\sigma_{\rho}^{N}$, for $\rho^{o}$ production in the reaction $\gamma \mathrm{p} \rightarrow \mathrm{p} \rho^{\circ}$. ${ }^{4,5}$ For $|t|<1 \mathrm{GeV}^{2}$, we found the ratio $\sigma_{\rho}^{N} / \sigma_{\omega}^{N}$ to be between 6 and 9 depending on the models used to determine the $\rho^{\circ}$ cross section. Using the combination of VDM, quark model and SU(6) this ratio has been predicted $^{16}$ to be 9. However, there could be a large positive contribution ( $\sim 40 \%$ ) from $A_{2}$ exchange to $\sigma_{\omega}{ }_{\omega}$ which would reduce the value of this ratio ${ }^{17}$ (the $\mathrm{A}_{2}$ exchange contribution to $\sigma_{\rho}^{N}$ is expected to be small).

Next we compare the contributions from unnatural parity exchange with the predictions of one-pion exchange (OPE). A similar analysis has been given by Schilling and Storim ${ }^{18}$ for $\omega$ production by unpolarized photons. The OPE model
predicts a decrease of the $\omega$ cross section for $|t|<1 \mathrm{GeV}^{2}$ by a factor 2.5 between 2.8 and 4.7 GeV . This ratio is practically independent of whether form factor or absorption corrections are used. Experimentally we found a value of $2.2 \pm 0.6$ for this ratio in agreement with the OPE prediction. The magnitude of the OPE cross section is proportional to the radiative decay width of the $\omega, \Gamma_{\omega \pi}$; it also depends on the vertex or absorption corrections employed. From the values of $\sigma_{\omega}^{\mathrm{U}}$ at 2.8 and 4.7 GeV in the interval $|\mathrm{t}|<1 \mathrm{GeV}^{2}$ and using the parametrization of Benecke and Dürr ${ }^{19}$ we obtained $\Gamma_{\omega \pi \gamma}=0.98 \pm 0.12 \mathrm{MeV}$. This value is consistent with the value obtained from the $\omega$ width and branching ratio, ${ }^{7}$
$\Gamma_{\omega \pi \gamma}=1.19 \pm 0.24 \mathrm{MeV}$. On the other hand the absorption-corrected OPE model $^{18}$ with the absorption coefficient $\mathrm{C}=0.9$ led to $\Gamma_{\omega \pi \gamma}=0.58 \pm 0.07 \mathrm{MeV}$ for our data.

Assuming that $\sigma_{\omega}^{\mathrm{U}}$ is accounted for by OPE we fitted the differential cross section for $0.02<|t|<0.4 \mathrm{GeV}^{2}$ to the form

$$
\begin{equation*}
\mathrm{D} \exp (\mathrm{Bt})+\mathrm{d} \sigma^{\mathrm{OPE}} / \mathrm{dt} \tag{4}
\end{equation*}
$$

to obtain more information on the t-dependence of $\sigma_{\omega}^{N}$. The OPE cross section, was calculated using the Benecke-Dürr parameterization. The fitted variables were $\Gamma_{\omega \pi \gamma}$, D and B and were assumed to be the same at both energies. The result of the fit was $\mathrm{D}=12.1 \pm 2.1 \mu \mathrm{~b} / \mathrm{GeV}^{2}, \mathrm{~B}=5.6 \pm 1.2 \mathrm{GeV}^{-2}$ and $\Gamma_{\omega \pi \gamma}=0.98 \pm 0.10 \mathrm{MeV}$. The value of B is consistent with the slope for $\rho^{0}$ production ${ }^{4}$ in the reaction $\gamma \mathrm{p} \rightarrow \mathrm{p} \rho^{\circ}$.

Finally, we calculate the predictions for the $\omega$ density matrix elements assuming that the natural parity exchange contributions conserve helicity in the total c.m. system as in the reaction ${ }^{5} \gamma \mathrm{p} \rightarrow \mathrm{p} \rho^{\circ}$ and that the contributions from unnatural parity exchange are due to OPE. As a function of $t$ the $\omega$ density matrix is then
given by

$$
\begin{equation*}
\rho_{i k}=\frac{\mathrm{d} \sigma^{\mathrm{N}} / \mathrm{dt} \rho_{i k}^{(\mathrm{N})}+\mathrm{d} \sigma^{\mathrm{OPE}} / \mathrm{dt} \rho_{\mathrm{ik}}^{(\mathrm{OPE})}}{\mathrm{d} \sigma^{\mathrm{N}} / \mathrm{dt}+\mathrm{d} \sigma^{\mathrm{OPE}} / \mathrm{dt}} \tag{5}
\end{equation*}
$$

In the helicity system $\rho_{1-1}^{1(N)}=-\operatorname{Im} \rho_{1-1}^{2(N)}=1 / 2$, and all other density matrix parameters in Eq. (2) are zero; for $\rho(\mathrm{OPE})$ we use the predictions of elementary OPE, which in the Gottfried-Jackson system ${ }^{12}$ are $\rho_{1-1}^{1(O P E)}=-\operatorname{Im} \rho_{1-1}^{2(O P E)}=-1 / 2$, and all other density matrix parameters in Eq. (2) equal to zero. The absorption corrections for $\rho_{i k}^{(O P E)}$ were neglected. For $d \sigma^{N} / d t$ and $d \sigma^{O P E} / d t$ we used the results of the fit to Eq. (4). The curves in Fig. 4 show the values of the $\rho_{\mathrm{ik}}$ predicted by Eq. (5).

## Conclusion:

The $\omega$ production cross section decreases from $5.8 \pm 0.5 \mu \mathrm{~b}$ at 2.8 GeV to $3.2 \pm 0.3 \mu \mathrm{~b}$ at 4.7 GeV . Both natural and unnatural parity exchanges contribute to $\omega$ production. The energy dependence and the magnitude of the unnatural parity exchange cross section agree with the predictions for one-pion exchange. The natural parity exchange cross sections do not change significantly from 2.8 to 4.7 GeV .

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TABLE I: Beam parameters and exposure statistics

| Avg. beam energy, Ery (GeV) | $\begin{gathered} \text { FWHM } \\ (\mathrm{GeV}) \end{gathered}$ | Avg. Linear Polarization $\mathrm{P}_{\gamma}$ | No. of Pictures | Events $/ \mu \mathrm{b}$ | $\begin{aligned} & \text { Events } \\ & \text { fitting } \\ & \gamma \mathrm{p} \rightarrow \mathrm{p} \pi \pi^{\circ}-\pi^{o} \end{aligned}$ | Eylimits accepted (GeV) | $\begin{gathered} \text { Fits to } \\ \gamma \mathrm{p} \rightarrow \mathrm{p} \pi^{-} \mathrm{o}^{\mathrm{o}} \\ \text { within } \mathrm{E}_{\gamma} \\ \operatorname{limits} \end{gathered}$ | No. of $\omega$ events |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.8 | 0.15 | 94\% | 292,000 | $90 \pm 4$ | 3950 | 2.4-3.3 | 2687 | $411 \pm 31$ |
| 4.7 | 0.3 | 92\% | 454,000 | $149 \pm 6$ | 7660 | 4.1-5.3 | 3083 | $315 \pm 24$ |

TABLE II: Parameters of the reaction $\gamma \mathrm{p} \rightarrow \mathrm{p} \omega$. Cross sections, $\mathrm{I}_{\sigma}$, and production angular dependence for $0.02<|t|<0.4 \mathrm{GeV}^{2}$ assuming $\mathrm{d} \sigma / \mathrm{dt}=\mathrm{C} \exp (\mathrm{At})$ for all events, and for the contributions from natural parity exchange in the $t$-channel. Cross section errors include statistical, flux, background and loss correction uncertainties.

|  | $\mathrm{E}_{\gamma}=2.8 \mathrm{GeV}$ | $\mathrm{E}_{\gamma}=4.7 \mathrm{GeV}$ |
| :--- | :--- | :--- |
| $\sigma_{\text {total }}$ | $5.8 \pm 0.5 \mu \mathrm{~b}$ | $3.2 \pm 0.3 \mu \mathrm{~b}$ |
| C | $34 \pm 4 \mu \mathrm{~b} / \mathrm{GeV}^{2}$ | $25 \pm 3 \mu \mathrm{~b} / \mathrm{GeV}^{2}$ |
| A | $6.2 \pm 0.7 \mathrm{GeV}^{-2}$ | $8.0 \pm 0.8 \mathrm{GeV}^{-2}$ |
| $\mathrm{P}_{\sigma}\left(\|\mathrm{t}\|<1 \mathrm{GeV}^{2}\right)$ | $-0.04 \pm 0.13$ | $0.19 \pm 0.14$ |
| $\sigma^{\mathrm{N}}\left(\|\mathrm{t}\|<1 \mathrm{GeV}^{2}\right)$ | $2.50 \pm 0.37 \mu \mathrm{~b}$ | $1.84 \pm 0.28 \mu \mathrm{~b}$ |
| $\sigma^{\mathrm{U}}\left(\|\mathrm{t}\|<1 \mathrm{GeV}^{2}\right)$ | $2.70 \pm 0.39 \mu \mathrm{~b}$ | $1.25 \pm 0.27 \mu \mathrm{~b}$ |
| $\mathrm{C}_{\mathrm{N}}$ | $13.1 \pm 4.1 \mu \mathrm{~b} / \mathrm{GeV}^{2}$ | $15.2 \pm 3.8 \mu \mathrm{~b} / \mathrm{GeV}^{2}$ |
| $\mathrm{~A}_{\mathrm{N}}$ | $5.5 \pm 1.6 \mathrm{GeV}^{-2}$ | $7.5 \pm 1.5 \mathrm{GeV}^{-2}$. |

TABLE III: Differential cross sections $\mathrm{d} \sigma / \mathrm{dt}\left(\mu \mathrm{b} / \mathrm{GeV}^{2}\right)$ for $\omega$ production. The errors given are only statistical.

| $\|t\|\left(\mathrm{GeV}^{2}\right)$ | $\mathrm{E}_{\gamma}=2.8 \mathrm{GeV}$ | $\mathrm{E}_{\gamma}=4.7 \mathrm{GeV}$ |
| :---: | :---: | :---: |
| $0.014-0.06$ | $27.3 \pm 3.1$ | $20.1 \pm 2.1$ |
| $0.06-0.10$ | $22.5 \pm 3.1$ | $11.7 \pm 1.7$ |
| $0.10-0.15$ | $16.6 \pm 2.3$ | $9.0 \pm 1.3$ |
| $0.15-0.20$ | $8.7 \pm 1.8$ | $5.9 \pm 1.1$ |
| $0.20-0.30$ | $7.3 \pm 1.1$ | $2.9 \pm 0.6$ |
| $0.30-0.40$ | $4.1 \pm 0.8$ | $2.2 \pm 0.5$ |
| $0.40-0.50$ | $2.0 \pm 0.6$ | $1.1 \pm 0.4$ |
| $0.5-1.0$ | $0.9 \pm 0.2$ | $0.27 \pm 0.09$ |
| $1.0-2.0$ | $0.28 \pm 0.08$ | 0 |
| $2.0-\|t\| \max$ | $0.15+0.15$ |  |
| $2.0-5.5$ |  | 0.08 |
| $5.5-\|t\| \max$ |  | $0.05 \pm 0.02$ |

TABLE IV: $\omega$ density matrix elements for the reaction $\gamma p \rightarrow p \omega$ 。
a) $\mathrm{E}_{\gamma}=2.8 \mathrm{GeV}$, Gottfried-Jackson system.

|  | $0.014-0.06$ | $0.06-0.15$ | $0.15-0.4$ | $0.4-1.0$ |
| :--- | :--- | :--- | :--- | :--- |
| $\rho_{00}^{0}$ | $0.15 \pm 0.07$ | $0.24 \pm 0.06$ | $0.36 \pm 0.07$ | $0.36 \pm 0.12$ |
| $\operatorname{Re} \rho_{10}^{0}$ | $0.06 \pm 0.05$ | $-0.14 \pm 0.04$ | $0.04 \pm 0.04$ | $-0.25 \pm 0.08$ |
| $\rho_{1-1}^{0}$ | $-0.01 \pm 0.08$ | $-0.04 \pm 0.06$ | $0.15 \pm 0.06$ | $-0.16 \pm 0.10$ |
| $\rho_{00}^{1}$ | $0.10 \pm 0.12$ | $-0.03 \pm 0.10$ | $-0.05 \pm 0.2$ | $-0.41 \pm 0.20$ |
| $\rho_{11}^{1}$ | $0.09 \pm 0.08$ | $0.02 \pm 0.07$ | $0.07 \pm 0.07$ | $0.12 \pm 0.13$ |
| $\operatorname{Re} \rho_{10}^{1}$ | $-0.10 \pm 0.07$ | $0.03 \pm 0.06$ | $0.03 \pm 0.06$ | $0.23 \pm 0.14$ |
| $\rho_{1-1}^{1}$ | $-0.03 \pm 0.12$ | $-0.10 \pm 0.10$ | $-0.07 \pm 0.09$ | $0.19 \pm 0.16$ |
| $\operatorname{Im} \rho_{10}^{2}$ | $0.01 \pm 0.08$ | $0.13 \pm 0.06$ | $0.19 \pm 0.07$ | $0.03 \pm 0.09$ |
| $\operatorname{Im} \rho_{1-1}^{2}$ | $-0.05 \pm 0.13$ | $0.09 \pm 0.09$ | $0.05 \pm 0.10$ | $0.13 \pm 0.14$ |

b) $\mathrm{E}_{\gamma}=2.8 \mathrm{GeV}$, helicity system.

| $\rho_{00}^{0}$ | $0.15 \pm 0.07$ | $0.10 \pm 0.06$ | $0.17 \pm 0.06$ | $0.38 \pm 0.11$ |
| :--- | :---: | :---: | :---: | :---: |
| $\operatorname{Re} \rho_{10}^{0}$ | $-0.02 \pm 0.05$ | $-0.04 \pm 0.04$ | $0.03 \pm 0.05$ | $0.25 \pm 0.08$ |
| $\rho_{1-1}^{0}$ | $-0.01 \pm 0.08$ | $-0.11 \pm 0.07$ | $0.05 \pm 0.07$ | $-0.15 \pm 0.11$ |
| $\rho_{00}^{1}$ | $0.21 \pm 0.13$ | $0.01 \pm 0.12$ | $0.08 \pm 0.11$ | $0.03 \pm 0.20$ |
| $\rho_{11}^{1}$ | $0.02 \pm 0.09$ | $0.00 \pm 0.08$ | $0.01 \pm 0.09$ | $-0.10 \pm 0.13$ |
| $\operatorname{Re} \rho_{10}^{1}$ | $-0.06 \pm 0.08$ | $-0.06 \pm 0.06$ | $-0.06 \pm 0.06$ | $-0.21 \pm 0.13$ |
| $\rho_{1-1}^{1}$ | $0.03 \pm 0.12$ | $-0.08 \pm 0.10$ | $-0.01 \pm 0.10$ | $0.41 \pm 0.17$ |
| $\operatorname{Im} \rho_{10}^{2}$ | $-0.01 \pm 0.08$ | $0.13 \pm 0.05$ | $0.10 \pm 0.06$ | $0.09 \pm 0.10$ |
| $\operatorname{Im} \rho_{1-1}^{2}$ | $-0.04 \pm 0.13$ | $-0.05 \pm 0.10$ | $-0.25 \pm 0.09$ | $-0.04 \pm 0.13$ |

Table IV (cont ${ }^{\prime} \mathrm{d}_{\text {。 }}$ )
c) $\mathrm{E}_{\gamma}=2.8 \mathrm{GeV}$, Adair system.

|  | $0.014-0.06$ | $0.06-0.15$ | $0.15-0.4$ | $0.4-1.0$ |
| :--- | :--- | :--- | :--- | :--- |
| $\rho_{00}^{0}$ | $0.14 \pm 0.07$ | $0.11 \pm 0.06$ | $0.24 \pm 0.07$ | $0.77 \pm 0.14$ |
| $\operatorname{Re} \rho_{10}^{0}$ | $0.01 \pm 0.05$ | $0.05 \pm 0.04$ | $0.07 \pm 0.04$ | $0.01 \pm 0.08$ |
| $\rho_{1-1}^{0}$ | $-0.01 \pm 0.08$ | $-0.10 \pm 0.07$ | $0.08 \pm 0.07$ | $0.05 \pm 0.09$ |
| $\rho_{00}^{1}$ | $0.17 \pm 0.11$ | $-0.03 \pm 0.10$ | $-0.01 \pm 0.11$ | $-0.53 \pm 0.29$ |
| $\rho_{11}^{1}$ | $0.05 \pm 0.08$ | $0.01 \pm 0.08$ | $0.05 \pm 0.08$ | $0.18 \pm 0.12$ |
| $\operatorname{Re} \rho_{10}^{1}$ | $-0.09 \pm 0.08$ | $-0.03 \pm 0.06$ | $-0.06 \pm 0.06$ | $-0.17 \pm 0.11$ |
| $\rho_{1-1}^{1}$ | $0.01 \pm 0.12$ | $-0.10 \pm 0.10$ | $-0.05 \pm 0.10$ | $0.13 \pm 0.16$ |
| $\operatorname{Im} \rho_{10}^{2}$ | $-0.01 \pm 0.08$ | $0.14 \pm 0.06$ | $0.17 \pm 0.06$ | $0.09 \pm 0.11$ |
| $\operatorname{Im} \rho_{1-1}^{2}$ | $-0.05 \pm 0.13$ | $-0.00 \pm 0.10$ | $-0.14 \pm 0.10$ | $0.06 \pm 0.12$ |

d) $\mathrm{E}_{\gamma}=4.7 \mathrm{GeV}$, Gottfried-Jackson system.

| $\rho_{00}^{0}$ | $0.14 \pm 0.06$ | $0.16 \pm 0.07$ | $0.46 \pm 0.09$ | $0.61 \pm 0.15$ |
| :--- | ---: | ---: | ---: | ---: |
| $\operatorname{Re} \rho_{10}^{0}$ | $0.15 \pm 0.04$ | $0.09 \pm 0.05$ | $0.07 \pm 0.05$ | $-0.21 \pm 0.11$ |
| $\rho_{1-1}^{0}$ | $0.12 \pm 0.07$ | $-0.08 \pm 0.07$ | $0.14 \pm 0.07$ | $-0.09 \pm 0.10$ |
| $\rho_{00}^{1}$ | $-0.23 \pm 0.10$ | $-0.24 \pm 0.10$ | $-0.42 \pm 0.15$ | $0.16 \pm 0.32$ |
| $\rho_{11}^{1}$ | $0.20 \pm 0.09$ | $0.11 \pm 0.09$ | $0.19 \pm 0.08$ | $-0.02 \pm 0.15$ |
| $\operatorname{Re} \rho_{10}^{1}$ | $0.02 \pm 0.07$ | $-0.06 \pm 0.08$ | $0.00 \pm 0.07$ | $-0.16 \pm 0.20$ |
| $\rho_{1-1}^{1}$ | $-0.09 \pm 0.12$ | $0.08 \pm 0.12$ | $-0.09 \pm 0.11$ | $-0.04 \pm 0.20$ |
| $\operatorname{Im} \rho_{10}^{2}$ | $-0.04 \pm 0.06$ | $0.09 \pm 0.06$ | $0.13 \pm 0.09$ | $-0.22 \pm 0.13$ |
| $\operatorname{Im} \rho_{1-1}^{2}$ | $-0.10 \pm 0.10$ | $-0.01 \pm 0.11$ | $-0.00 \pm 0.12$ | $-0.15 \pm 0.18$ |

Table IV (cont ${ }^{1} \mathrm{~d}_{0}$ )
e) $\mathrm{E}_{\gamma}=4.7 \mathrm{GeV}$, helicity system.
$|t|\left(\mathrm{GeV}^{2}\right)$

|  | $0.014-0.06$ | $0.06-0.15$ | $0.15-0.4$ | $0.4-1.0$ |
| :--- | :---: | :---: | :---: | :---: |
| $\rho_{00}^{0}$ | $0.02 \pm 0.06$ | $0.18 \pm 0.07$ | $0.09 \pm 0.07$ | $0.34 \pm 0.14$ |
| $\operatorname{Re} \rho_{10}^{0}$ | $0.05 \pm 0.04$ | $-0.10 \pm 0.05$ | $0.03 \pm 0.05$ | $0.24 \pm 0.10$ |
| $\rho_{1-1}^{0}$ | $0.06 \pm 0.07$ | $-0.07 \pm 0.07$ | $-0.05 \pm 0.08$ | $-0.22 \pm .11$ |
| $\rho_{00}^{1}$ | $-0.12 \pm 0.12$ | $-0.05 \pm 0.13$ | $0.17 \pm 0.13$ | $-0.16 \pm .29$ |
| $\rho_{11}^{1}$ | $0.14 \pm 0.10$ | $0.01 \pm 0.11$ | $-0.11 \pm 0.10$ | $0.14 \pm .18$ |
| $\operatorname{Re} \rho_{10}^{1}$ | $-0.15 \pm 0.06$ | $-0.07 \pm 0.07$ | $-0.17 \pm 0.07$ | $0.17 \pm .20$ |
| $\rho_{1-1}^{1}$ | $-0.14 \pm 0.10$ | $0.18 \pm 0.11$ | $0.20 \pm 0.11$ | $-0.20 \pm .18$ |
| $\operatorname{Im} \rho_{10}^{2}$ | $-0.07 \pm 0.06$ | $0.07 \pm 0.07$ | $0.05 \pm 0.08$ | $-0.11 \pm .14$ |
| $\operatorname{Im} \rho_{1-1}^{2}$ | $-0.08 \pm 0.10$ | $-0.09 \pm 0.10$ | $-0.18 \pm 0.13$ | $0.32 \pm .18$ |

f) $\mathrm{E}_{\gamma}=4.7 \mathrm{GeV}$, Adair system.

| $\rho_{00}^{0}$ | $0.04 \pm 0.06$ | $0.13 \pm 0.07$ | $0.18 \pm 0.08$ | $0.66 \pm 0.16$ |
| :--- | :---: | :---: | :---: | :---: |
| $\operatorname{Re} \rho_{10}^{0}$ | $0.08 \pm 0.04$ | $-0.05 \pm 0.05$ | $0.12 \pm 0.05$ | $0.19 \pm 0.09$ |
| $\rho_{1-1}^{0}$ | $0.07 \pm 0.07$ | $-0.09 \pm 0.07$ | $-0.01 \pm 0.08$ | $-0.06 \pm 0.11$ |
| $\rho_{00}^{1}$ | $-0.18 \pm 0.09$ | $-0.10 \pm 0.10$ | $-0.06 \pm 0.12$ | $0.25 \pm 0.36$ |
| $\rho_{11}^{1}$ | $0.17 \pm 0.09$ | $0.04 \pm 0.10$ | $0.01 \pm 0.09$ | $-0.06 \pm 0.15$ |
| $\operatorname{Re} \rho_{10}^{1}$ | $-0.11 \pm 0.07$ | $-0.09 \pm 0.07$ | $-0.25 \pm 0.08$ | $0.17 \pm 0.17$ |
| $\rho_{1-1}^{1}$ | $-0.07 \pm 0.12$ | $0.16 \pm 0.12$ | $0.09 \pm 0.11$ | $0.00 \pm 0.20$ |
| $\operatorname{Im} \rho_{10}^{2}$ | $-0.06 \pm 0.06$ | $0.08 \pm 0.06$ | $0.08 \pm 0.08$ | $-0.21 \pm 0.15$ |
| $\operatorname{Im} \rho_{1-1}^{2}$ | $-0.09 \pm 0.10$ | $-0.08 \pm 0.11$ | $-0.14 \pm 0.14$ | $0.19 \pm 0.16$ |

## FIGURE CAPTIONS

1. $\pi^{+} \pi^{-} \pi^{\circ}$ mass distributions for the reaction $\gamma \mathrm{p} \rightarrow \mathrm{p} \pi^{+} \pi^{-} \pi^{\ominus}$ at 2.8 and 4.7 GeV. There are 2687 and 3083 fits from 2678 and 2912 events at 2.8 and 4.7 GeV respectively.
2. Total cross sections for reaction $\gamma p \rightarrow p \omega$, from this experiment together with the values of Ref. $1,2,9-11$. Cross section contributions $\sigma^{N}, \sigma^{\mathrm{U}}$ from natural parity and unnatural parity exchanges in the $t$-channel for $|\mathrm{t}|<1 \mathrm{GeV}^{2}$.
3. Reaction $\gamma p \rightarrow p \omega$. Total differential cross sections and differential cross sections for contributions from natural parity exchange at 2.8 and 4.7 GeV .
4. Reaction $\gamma \mathrm{p} \rightarrow \mathrm{p} \omega$. The spin density matrix parameters in the helicity system and $\mathrm{P}_{\sigma}$ as a function of $t$ at 2.8 and 4.7 GeV . The curves are calculated according to Eq. (5).


Fig. 1


Fig. 2


Fig. 3

$$
\gamma p \longrightarrow p \omega
$$

HELICITY FRAME

$\operatorname{Re} \rho_{10}^{1} 0_{-0.2}^{02}\left[\frac{1}{4}\right.$


$|t|\left(\mathrm{GeV}^{2}\right)$


Fig. 4


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    (A condensed version has been submitted to Phys. Rev. Letters.)

