UNIVERSITY OF CALIFORNIA

Los Angeles

Hosing Instability of the Drive Electron Beam in the

E157 Plasma-Wakefield Acceleration Experiment

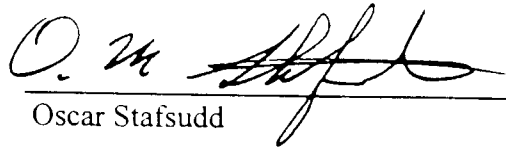at the Stanford Linear Accelerator

A thesis submitted in partial satisfaction

of the requirements for the degree Master of Science
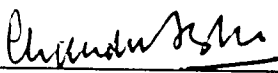
in Electrical Engineering

by

Brent Edward Blue

2000

The thesis of Brent Edward Blue is approved.

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Chandrasekhar J. Joshi, Committee Chair

University of California, Los Angeles

2000

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ABSTRACT OF THE THESIS

Hosing Instability of the Drive Electron Beam in the

E157 Plasma-Wakefield Acceleration Experiment

at the Stanford Linear Accelerator

by

Brent Edward Blue

Master of Science in Electrical Engineering

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Professor Chandrasekhar J. Joshi, Chair

In the plasma-wakefield experiment at SLAC, known as E157, an ultra-relativistic electron beam is used to both excite and witness a plasma wave for advanced accelerator applications. If the beam is tilted, then it will undergo transverse oscillations inside of the plasma. These oscillations can grow exponentially via an instability know as the electron hose instability. The linear theory of electron-hose instability in a uniform ion column predicts that for the parameters of the E157 experiment (beam charge, bunch length, and plasma density) a growth of the centroid offset should occur. Analysis of the E157 data has provided four critical results. The

first was that the incoming beam did have a tilt. The tilt was much smaller than the radius and was measured to be $5.3\,\mu m/\sigma_z$ at the entrance of the plasma (IP1.) The second was the beam centroid oscillates in the ion channel at half the frequency of the beam radius (betatron beam oscillations), and these oscillations can be predicted by the envelope equation. Third, up to the maximum operating plasma density of E157 ($\sim 2\times 10^{14}$ cm^{-3}), no growth of the centroid offset was measured. Finally, time-resolved data of the beam shows that up to this density, no significant growth of the tail of the beam (up to 8ps from the centroid) occurred even though the beam had an initial tilt.

1 Introduction

1.1 What is the PWFA?

Plasma based accelerators are of great interest because of their potential to accelerate charged particles at high gradients. Conventional radio frequency accelerators are limited to approximately 100 MV/m. This limit is partly due to breakdown in the walls of the structure. On the other hand, a plasma can sustain electron plasma waves with electric fields on the order of the nonrelativistic wave breaking field [1], $E_o = c m_e \omega_p / e$, where $\omega_p = (4 \pi n_o e^2 / m_e)^{1/2}$ is the electron plasma frequency and n_o is the electron plasma density. Since the electric field scales as the square root of density, electric fields are on the order of 1-100 GV/m for plasma densities in the range of 10^{14}-10^{18} cm^{-3}.

Plasma based accelerators utilize a laser or a charged particle beam to drive a relativistically propagating plasma wave [2]. Laser driven accelerator schemes include the beat-wave accelerator [3], the laser-wake field accelerator [4], and the self-modulated wake field accelerator [5]. These schemes possess the ability to generate high density plasma waves (~10^{18} cm^{-3}), and therefore, high electric field gradients (~100 GV/m.) The shortcoming of these schemes is that the length of the accelerator is limited to a few Rayleigh lengths of the laser beam (< 1cm.) Charged particle beam driven plasma wake field accelerators (PWFA) are capable of long interaction

lengths (on the order of meters), at the expense of a decreased accelerating gradient (~ 10 – 1000 MV/m.)

In the PWFA, the space-charge force of the drive beam excites plasma waves (figure 1.1.1). For the case of an electron drive beam, the plasma electrons will be expelled radially. If the beam density n_b is greater than the plasma density n_p ("blow-out" regime), then all plasma electrons will be expelled, leaving behind an ion column. After passage of the beam, the ion column space charge will pull back the expelled electrons. These electrons rush back in to the ion column and create a large density spike. The strong fields in front of the density spike are used to accelerate the electron beam.
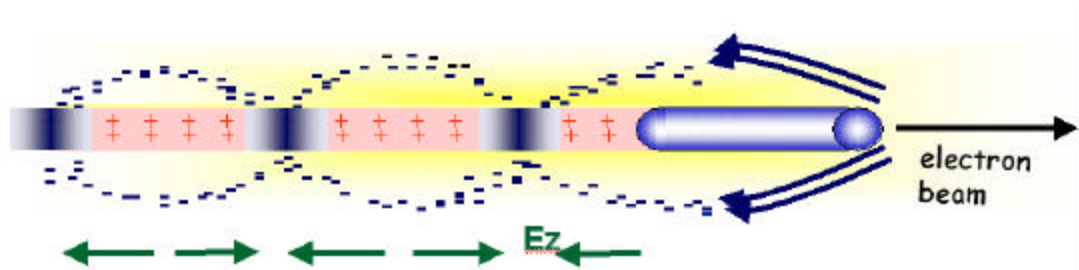
Figure 1.1.1   Cartoon of the electron beam displacing

electrons and generating a plasma wave

1.2 What is E157?

E157 was an experiment to study acceleration of 30 GeV electrons over 1.4 meters in a plasma wakefield accelerator [6]. The experiment was run at the Stanford Linear Accelerator (SLAC.)   It was a collaboration between the University of

California – Los Angeles, the University of Southern California, Lawrence Berkeley National Laboratory, and Stanford University. The goal of the experiment was to explore and develop techniques needed to implement a high-gradient PWFA in a large-scale accelerator. With respect to the electron beam, the goals were to study the longitudinal effects (acceleration of the tail and deceleration of the beam centroid) and the transverse effects (betatron oscillations, emission of betatron radiation, and hosing).

The motivation for this experiment is to not only explore new physics, but to also investigate technology for future high-energy colliders. High-energy colliders are used to study the fundamental building block of nature. The higher the energy of the beams, the more closely we can probe the structure of matter. The highest obtained collision energy was 104.5 GeV electrons on 104.5 GeV positrons in the Large Electron Positron Collider (LEP) at the European Organization for Nuclear Research (CERN.) At SLAC, the collision energies are on the order of 50 GeV on 50 GeV. The next generation accelerators are designed to be 500 GeV on 500 GeV. One design in development is the Next Linear Collider (NLC) [7]. The NLC is over 30 km long (SLAC is 4km long, see figure 1.2.2) since it relies on conventional RF accelerator technology. Clearly new technology must be developed which increases accelerating gradients into the GeV per meter range. Beam driven plasma wakefield accelerators are the most attractive advanced accelerator concept because they can support GeV/m accelerating gradients over meter lengths.
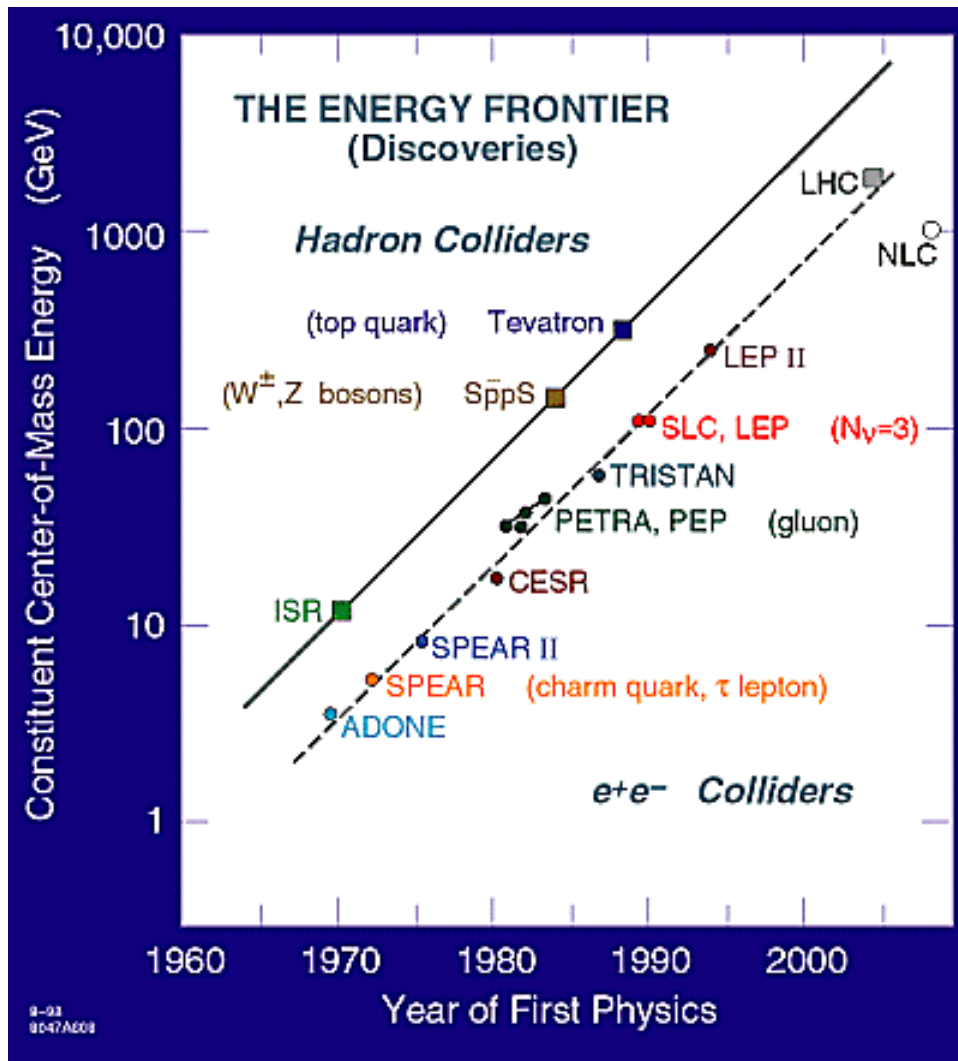
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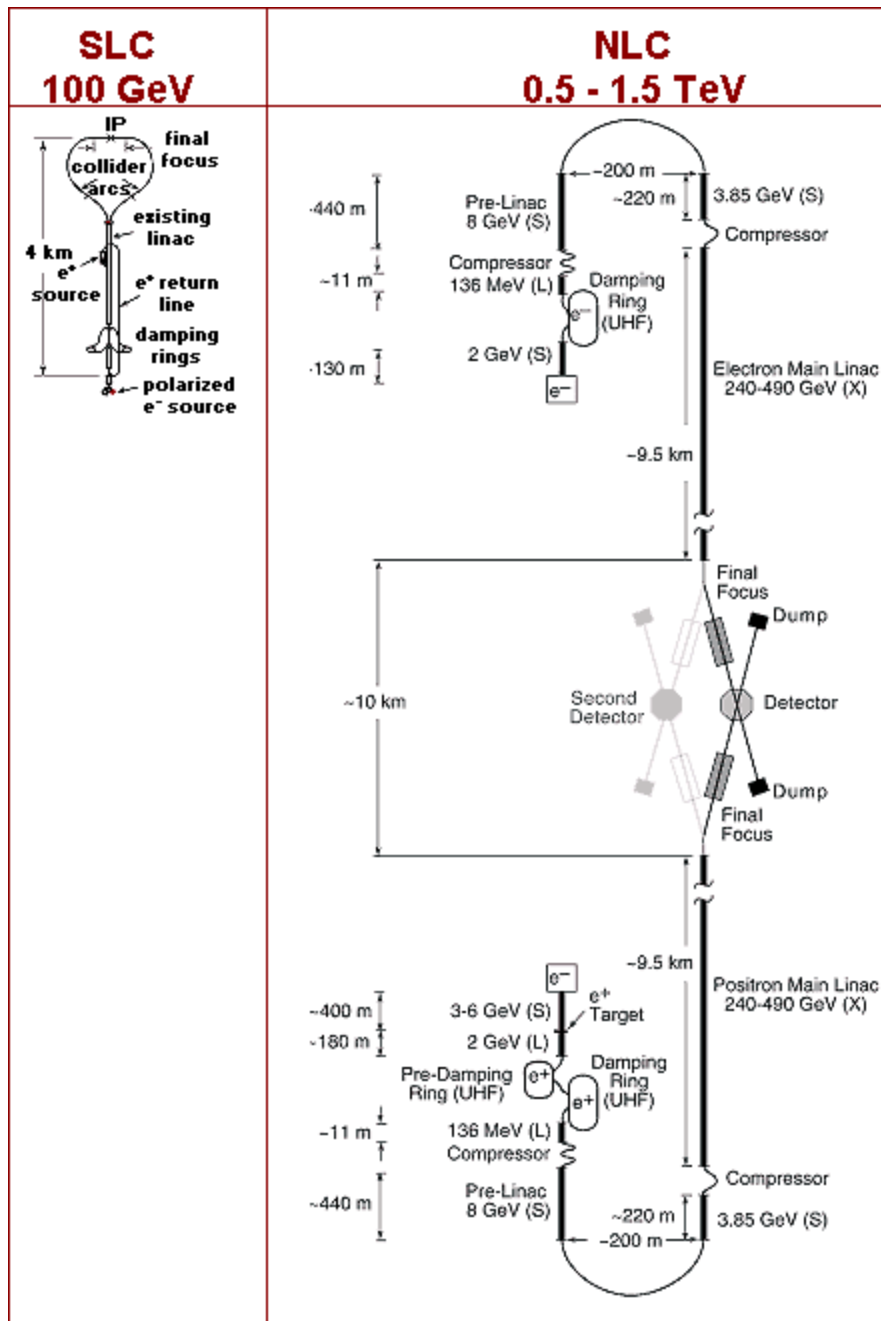
Figure 1.2.2 Schematic for the NLC with SLAC drawn for size comparison

The basic idea of the E157 experiment is to use a single electron bunch where the front of the beam excites a plasma wave and the tail of the beam witnesses the resulting accelerating field. The nominal beam parameters were $2x10^{10}$, 30 GeV electrons, a bunch length of 0.7mm, and a transverse spot size of 40 μm. This beam was propagated through a 1.4m long Lithium plasma of a density up to $2x10^{14}$ e^-/cm^{-3}. The plasma source is positioned at interaction point 1 in the Final Focus Test Beam (FFTB) at SLAC. The FFTB is a straight shot down the 3km long accelerator and was designed to investigate the factors that limit the size and stability of the beam at the collision point of a linear collider. The importance of the FFTB design to our experiment is that the beam optics and diagnostics are capable of delivering a high quality beam to our experiment. In addition to the diagnostics built into the FFTP (beam position monitors, current measuring torroids, and wire scanners), the experiment required single shot beam profile measurements before and after the plasma and time resolved measurements after an energy dispersive bend magnet. These diagnostics allowed the E157 collaboration to study the transverse and longitudinal dynamics of a high peak current (>100A), ultra-relativistic electron bunch in a 1.4m of $0-2x10^{14}$ cm^{-3} underdense plasma.

1.3 What is the hosing instability?

Propagation of intense charged beams in an under-dense plasma (also known as the ion-focused regime, IFR) has drawn considerable interest from both the accelerator and radiation research communities. Some of the accelerator applications are, in addition to the PWFA, the plasma lens [8], the continuous plasma focus [9], and the plasma emittance damper [10]. In addition, both theoretical [11] and experimental work [12] have looked at the generation of coherent radiation from beams in the IFR. Both theoretical [13] and experimental [14] work have shown that a transverse instability exists.

These transverse instabilities arise when a non-uniform transverse force acts upon the beam. Such a situation can occur when an electron beam is offset in a uniform ion column. The term hose instability is used whenever a flexible confinement system is used. Hose instabilities were first observed with long pulse electron beams ($t_b \geq 1ns$.) Stable beam transport was shown to be disrupted by the ion-hose instability [15]. For such long pulses, the ions are mobile and a feedback occurs between the displaced electrons and ions. If the electron pulse length is short enough so that the ions can be considered immobile, another hose instability is predicted to occur, the electron hose instability. In this instability the relativistic electron beam exhibits a transverse instability due to the coupling of the beam centroid to the plasma electrons at the ion-channel edge.
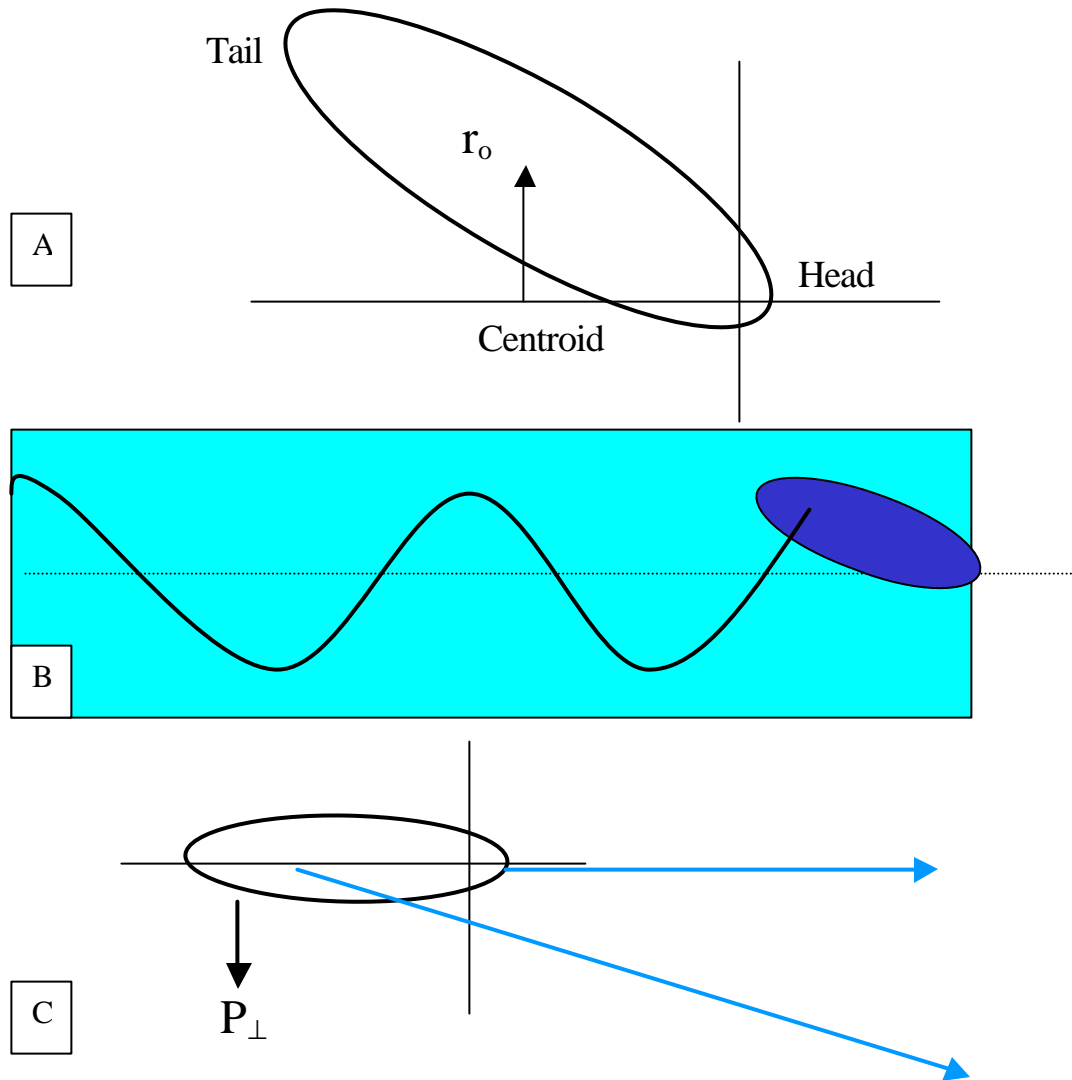
Figure 1.3.1   Cartoon of tilted beam before plasma (A), inside the plasma (B), and after the plasma (C). The nomenclature for our tilted beam (A) is the head defines the axis and the centroid is displaced from the axis by r_o. In the plasma, the head goes straight while the body oscillates. As the beam exists the plasma, the head continues straight while the body, with some perpendicular momentum, travels off at some angle.

Growth rates for the electron hose instability have been calculated based on a simplified model [16]. For the E157 beam parameters, the growth rate of the instability was predicted to be very rapid and therefore deleterious to the experiment. The beam centroid offset was predicted to witness an amplification of 10^0-10^2x [17]. If these predictions were correct, the electron hose instability would not only increase the difficulty of interpreting our experimental results, but it would also hinder the use of PWFAs in future accelerators.

1.4 How might one look for the hose instability?

In the E157 experiment, the head of the beam blows out the plasma electrons to form the ion column. If the beam enters the plasma with a tilt, then the centroid of the beam will be offset in the ion column. If the electron hose instability exists, then this offset will grow inside of the plasma. There exist two diagnostics that can resolve the effects of the electron hose instability. They are the beam position monitors (BPMs) and the streak camera. The BPMs will track the location of the beam centroid, while the streak camera will temporally resolve the relative position of each beam segment. Each diagnostic has its own advantages and disadvantages.

The BPMs track the position of the beam centroid as it drifts out of the plasma. In order to look for hosing using this method, an energy scan data run must be taken. An energy scan data run is when the plasma density is varied from 0 to $2x10^{14}$ cm^{-3} over 200 shots by varying the laser energy needed to ionize the Lithium vapor. By

plotting the centroid displacement as a function of distance after the plasma, the trajectory of the centroid exiting the plasma can be calculated for each shot. Next you plot the slope of the centroid's trajectory vs. plasma density. If a hosing instability exists, the slope of the trajectory will increase nonlinearly with plasma density.

The streak camera can be used to measure the head-tail offset for every shot. If the laser is turned off (i.e. no plasma) then the initial tilt on the beam can be measured. With the plasma turned on, the resultant beam tilt can be measured. This will allow us to analyze how the plasma affects the entire beam, not just the centroid. One difficulty with this measurement is keeping the beam aligned to the slit of the streak camera. If the plasma imparts a large deflection to the beam, it can move the image off of the slit.

One limitation of the current experimental setup is that the streak camera diagnostic and four (out of five) BPMs are located after a large bending magnet. This large bending magnet adds dispersion to the vertical plane that is used for the experiment's energy gain diagnostic. However, this magnet hampers the hosing diagnostics because the analysis requires a pure drift space after the plasma. This limits the analysis to the horizontal plane (x-axis) which does not gain dispersion through the bending magnet. Results will show that a tail is in the x-y plane (section 4.1), but only the horizontal component of the tail will be quantified.

2 Theory of the Hosing Instability

2.1 Theory of the hose instability – Offset Oscillations.

The first step towards looking for the hosing instability is to calculate the transverse motion of the beam in the absence of hosing. We will look at the special case of a relativistic electron beam confined by an ion channel. The initial conditions will be an electron beam and ion column with equal radii r_o and uniform densities. The electron beam density is denoted by n_b and the ion column density is

$$n_p = f n_b. \tag{2.1.1}$$

The neutralization fraction, f, is less than unity and it accounts for the under-dense condition of the plasma density. We will assume that the ions are infinitely massive (i.e. they are rigid) and that the ion column is centered on the z-axis. The beam displacement, y(z,t), will have an initial displacement

$$y_o = y(0,t). \tag{2.1.2}$$

In the limit of small displacement, $|y_o| \ll r_o$, the electric field of the displaced charge cylinders in the area region occupied by the cylinders is uniform with a magnitude linearly proportional to the displacement. The electric field is given by

$$E_y(z,t) = -4p \ e \ n_b \ y(z,t). \tag{2.1.3}$$

This gives rise to a restoring force that is given by

$$F_y(z,t) = 4p \ e^2 \ n_b \ y(z,t). \tag{2.1.4}$$

In addition to the force between the beam and the ion column, the beam position can also change by convection. The net change in the transverse velocity of the beam is

$$\frac{\partial \boldsymbol{n}_y}{\partial t} = -\boldsymbol{b}c\frac{\partial \boldsymbol{n}_y}{\partial z} - \left(\frac{4\boldsymbol{p}e^2 n_p}{\boldsymbol{g}n_e}\right)y \qquad (2.1.5)$$

Rearranging terms and defining the convective derivative and beam plasma frequency

$$\frac{D}{Dt} = \frac{\partial}{\partial t} + \boldsymbol{b}c\frac{\partial}{\partial z} \qquad (2.1.6)$$

$$\boldsymbol{w}_b = \left(\frac{4\boldsymbol{p}e^2 n_b}{\boldsymbol{g}n_e}\right)^{1/2} \qquad (2.1.7)$$

we get

$$\frac{D\boldsymbol{n}_y}{Dt} = -\left(f\boldsymbol{w}_b^2\right)y \qquad (2.1.8)$$

We can similarly derive an expression for the change in y at a point

$$\frac{dy}{dt} = -\boldsymbol{b}c\frac{dy}{dz} + \boldsymbol{n}_y \qquad (2.1.9)$$

or

$$\frac{Dy}{Dt} = \boldsymbol{n}_y \qquad (2.1.10)$$

Combining equations (2.1.8) and (2.1.10) in order to solve for the displacement as a function of initial displacement gives

$$\frac{D^2 y}{Dt^2} = -\left(f\boldsymbol{w}_b^2\right)y \qquad (2.1.11)$$

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or

$$\frac{d^2 y}{dt^2} + 2\boldsymbol{bc}\frac{\boldsymbol{d}}{\boldsymbol{dt}}\frac{dy}{dz} + \boldsymbol{b}^2 c^2 \frac{\boldsymbol{d}^2 y}{\boldsymbol{dz}^2} = -\left(f\boldsymbol{w}_\mathrm{b}^2\right)y \qquad (2.1.12)$$

Calculating a steady state solution by setting the time derivative to zero yields

$$\frac{\boldsymbol{d}^2 y}{\boldsymbol{dz}^2} = -f\left(\frac{\boldsymbol{w}_b}{\boldsymbol{bc}}\right)^2 y \qquad (2.1.13)$$

The solution to this equation is

$$y = y_o \cos(k_b z) \qquad (2.1.14)$$

where

$$k_b = \sqrt{f}\,(\boldsymbol{w}_b / \boldsymbol{bc}) \qquad (2.1.15)$$

This shows that if the electron beam enters the plasma with an offset, it will oscillate harmonically about the center of the ion channel.

The plasma column in the E157 experiment, L, was 140cm long. The head of the beam blows out the electrons and defines the plasma channel. If the beam has a longitudinal-transverse correlation (i.e. tails or tilt), then the beam centroid is displaced from the center of the plasma column. If the beam enters the plasma with an offset of y_o, then it will exit the plasma with an offset of

$$y_L = y_0 \cos(k_b L) \qquad (2.1.16)$$

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If $k_b L$ does not equal an integer number of pi, then the centroid will gain some perpendicular momentum as it exists the plasma. The slope of the centroid's exit trajectory is given by

$$\dot{y}_L = y_0 k_b \sin(k_b L) \qquad (2.1.17)$$

If an instability were present, we would expect to see a growth term in equation (2.1.14).

$$y = y_o e^A \cos(k_b z) \qquad (2.1.18)$$

The basic form of the solution is correct, but now we will go into a more rigorous derivation for electron hosing.

2.2 Theory of Hosing II [16]

We will consider the relativistic beam propagation in an infinite, unmagnitized, preionized, and uniform plasma of density n_p. The plasma is under-dense in relation to the beam density, $n_p < n_b$. We assume that the Budker condition, $n_p \gg n_b/?^2$ is satisfied. This implies that all beam electrons will undergo transverse oscillations at a single "betatron frequency", $w_b = w_p /(2g)^{1/2}$. We will further assume a collisionless plasma and that the plasma skin depth, $c/?_p$, is much larger than the channel radius. By using the "rigid beam" model and the "frozen field" approximation, we find that the system response to a small perturbation, $?_x(s,t)$, is described by a beam breakup equation, where s is the longitudinal position of the beam in the laboratory frame and t

can be thought of as an index that labels a given slice of the beam (i.e. the head of the beam is t = 0ps, and t = 4ps refers to the beam slice 4ps behind the head).

$$\left(\frac{d}{ds} g \frac{d}{ds} + g k_b^2 \right) x_x(s,t) = \int_0^t W(t-t') x(s,t') dt' \qquad (2.2.1)$$

where the wakefield, W, is given by

$$W(t) = \frac{w_o^3}{c^2} \sin(w_o t) \qquad (2.2.2)$$

k_β is the betatron wave number and $?_o = ?_p/(2)^{1/2}$. An asymptotic form for the solution of equation (2.2.1) in the limit of strong focusing and a short bunch (i.e. picosecond pulses) is obtained by the method of steepest descents [18]

$$x(s,t) \approx 0.263 \frac{x_o}{A^{1/2}} e^A \cos\left(k_b s - \frac{A}{\sqrt{3}} + \frac{p}{12} \right) \qquad (2.2.3)$$

where

$$A(s,t) = \frac{3^{3/2}}{4} \left[(k_b s)(w_o t)^2 \right]^{1/3} \qquad (2.2.4)$$

The solution in equation (2.2.3) is for the case when then entire beam is offset in the plasma column. If the beam is tilted, the solution becomes [18]

$$x(s,t) \approx 0.341 \frac{x_o}{A^{3/2}} e^A \cos\left(k_b s - \frac{A}{\sqrt{3}} + \frac{p}{12} \right) \qquad (2.2.5)$$

Figures 2.2.1 and 2.2.2 show how the centroid offset grows for different plasma densities and how the instability grows for beam slices farther from the beam head (i.e. increasing t). Notice how the growth factor, $x(s = 140cm, t)/x_o$, is significantly

reduced for the tilted case. Results from section 4.5 indicate that the beam centroid is about 2ps back from the point of channel formation. The electrons that were to be accelerated were about 4-6ps behind the beam centroid. Figure 2.2.3 shows how the centroid and tail oscillates (t = 2, 4, and 6ps) inside of the plasma column and figure 2.2.4 shows how the centroid and tail oscillations will look downstream of the plasma during a plasma density scan.
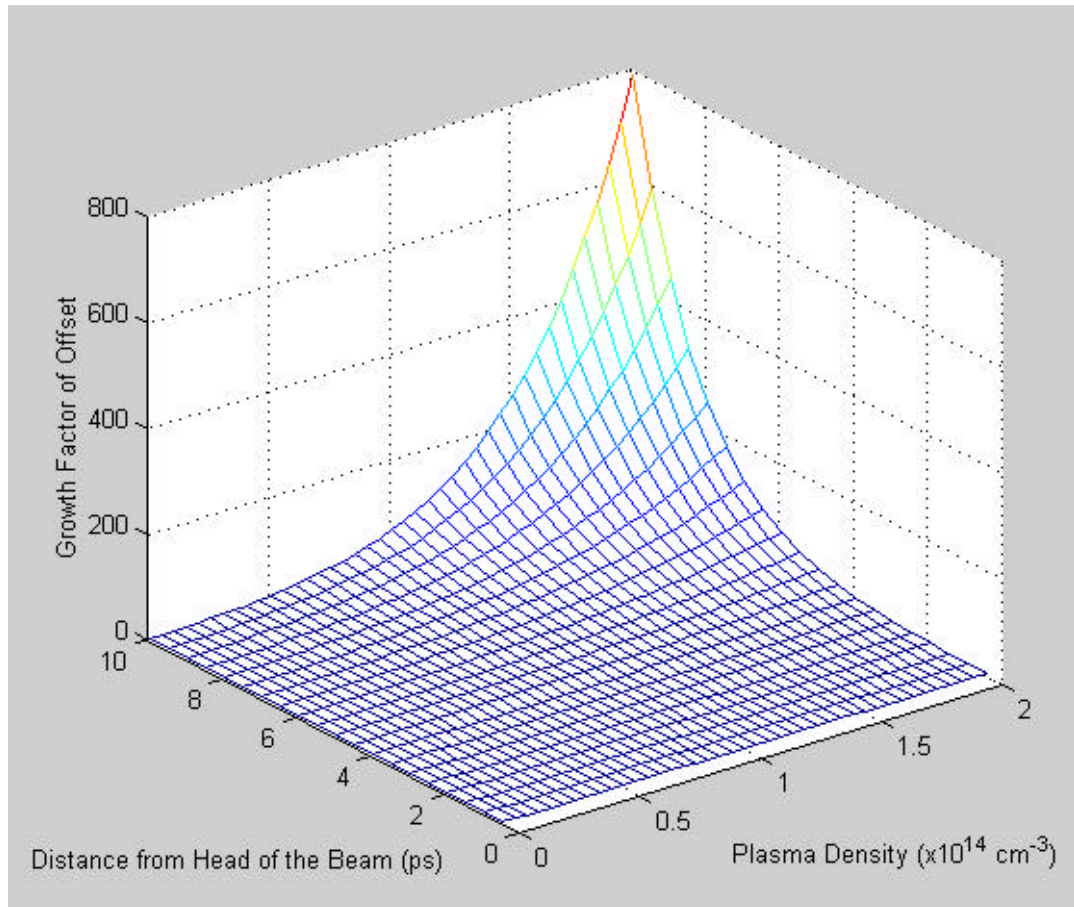
Figure 2.2.1 Parameter Space of Growth Factor for an Offset Beam in a

140cm long plasma
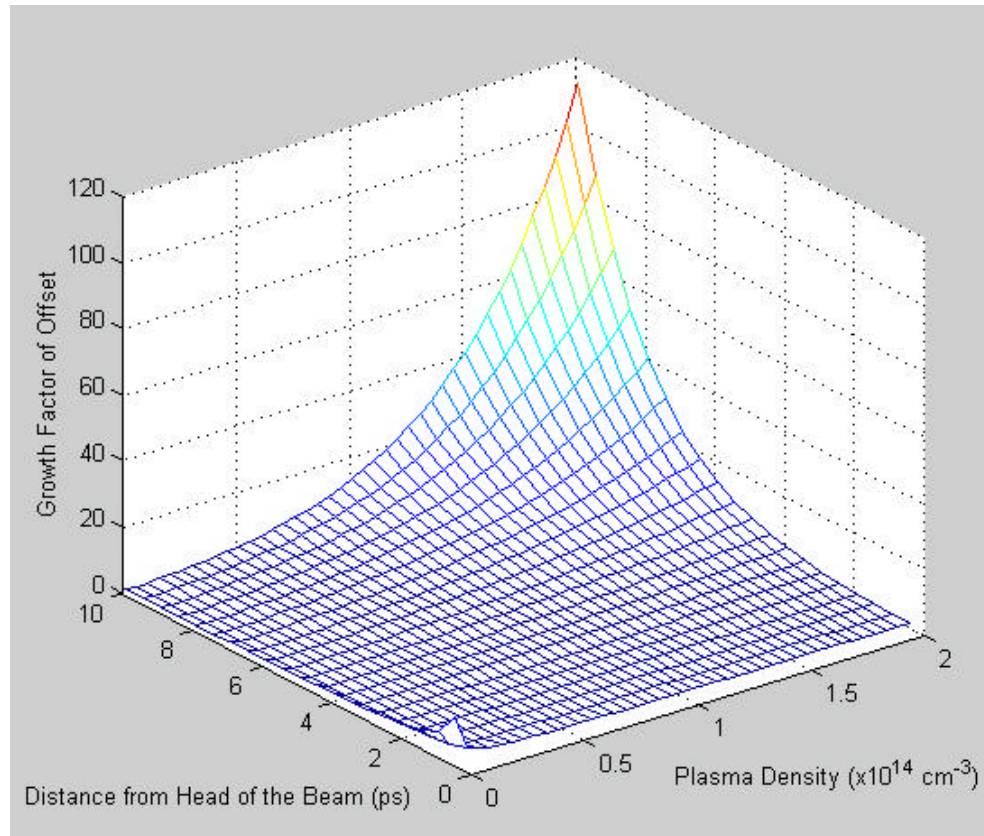
Figure 2.2.2 Parameter Space of Growth Factor for a Tilted Beam in

a 140cm long plasma

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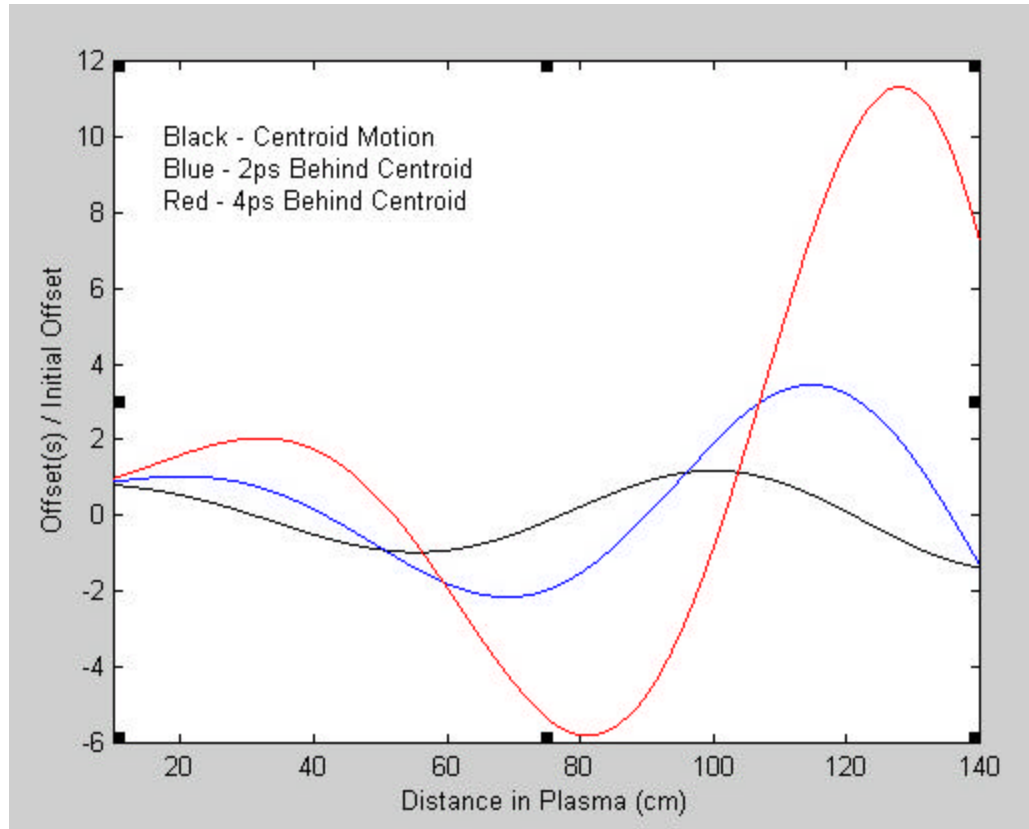
Figure 2.2.3 Oscillation of a tilted beam in a 2×10^{14} cm^{-3} plasma for a channel which is formed 2ps before the centroid
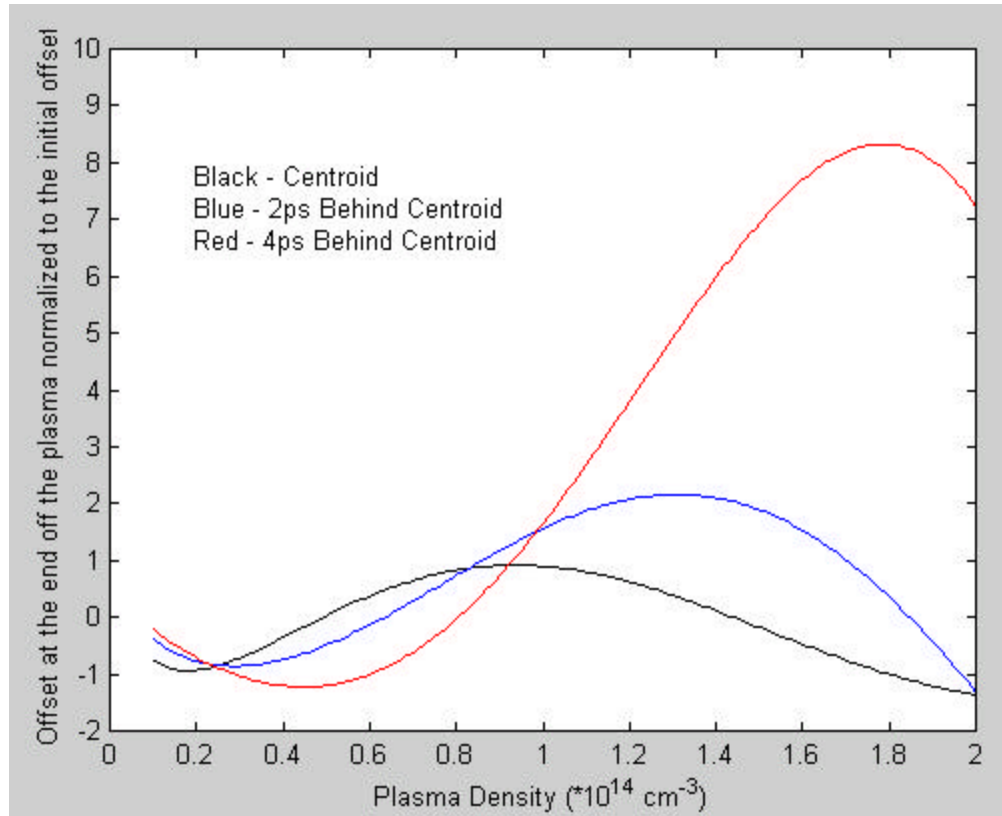
Figure 2.2.4 Oscillation of a tilted beam at the end of a 140cm long plasma for

a channel that is formed 2ps before the centroid

2.3 Limitations to the Theory of Hosing

In the E157 experiment, the beam propagates in an underdense plasma and both excites and witnesses the plasma wave. If two beams were used, one to drive the wave and a second to witness the acceleration, the second beam would be propagating in the ion-focused regime. The subtle difference is that a beam in under-dense plasma creates an ion channel, as opposed to the ion-focused regime that assumes a pre-formed ion channel. Although subtle, no hosing theory exists for the under-dense regime; all have assumed the ion-focused regime. In the past, this approximation was valid since the pulse length was greater than the plasma wavelength. In E157, the pulse length is on the order of the plasma wavelength, therefore the dynamics of the expelled electrons are important and the assumption of a preformed ion column is not a valid one.

Valuable insight can still be gained from the equations, but they need to be modified to take into account the formation of the ion column. A first approximation is to modify the beam position parameter, t. t will no longer correspond to the distance from the head of the beam, rather the distance from channel formation. Since the channel can form near the beam centroid (figure 2.3.1) [19], the growth factor of hosing is significantly reduced (e.g. reduce t from 8ps to 2ps in figure 2.2.2). Therefore, one may not observe significant growth of the hosing instability in the centroid motion of the beam. However, the tail of the beam could still suffer a significant growth as seen in figures 2.2.3 and 2.2.4.
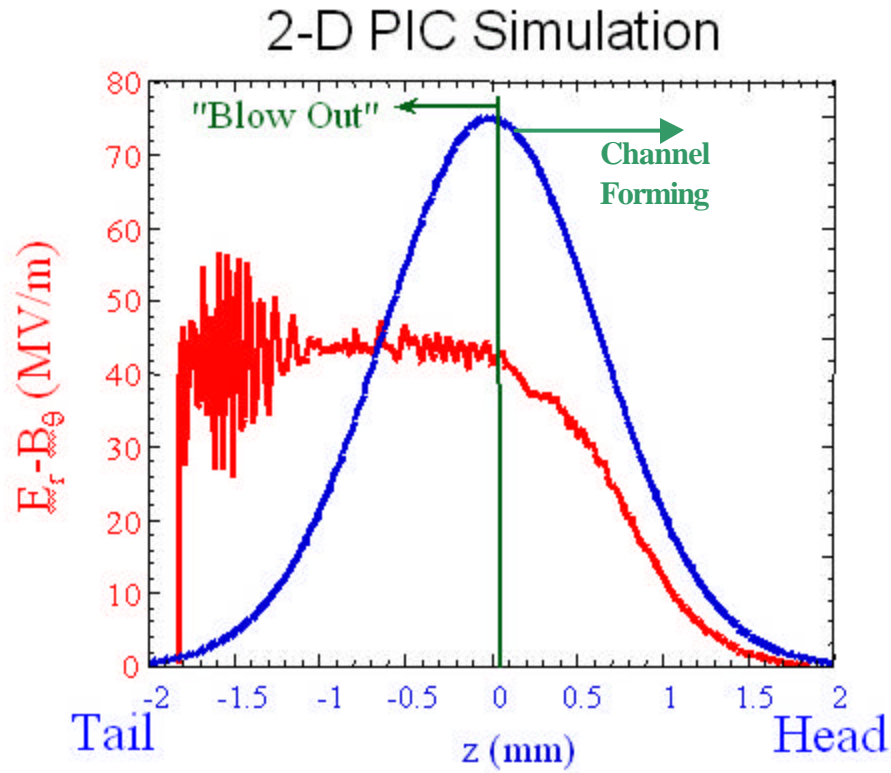
Figure 2.3.1 Dynamics of Ion Channel Formation.   This is a 2-D Particle in Cell simulation of an electron beam (shown in blue) propagating in a plasma.   The space charge of the beam expels plasma electrons radially to form an ion column.   The radial electric field associated with the ion column is show in red.   The magnitude of the field increases until all plasma electrons have been expelled and a pure ion column is left behind.   At this point, known as "blow out", the magnitude of the radial field is constant.   As one can see, the point of channel formation (t = 0) is not the head of the beam, rather it is located part way into the beam.

3 Experimental Setup

The principle components of the experimental apparatus are the Lithium plasma source [20, 24], the optical transition radiators [21, 22, 24], the beam position monitors [23], and an aerogel Cherenkov radiator [24]. A brief description of each component will now be given. For a more detailed view of any specific component, refer to the references given above.
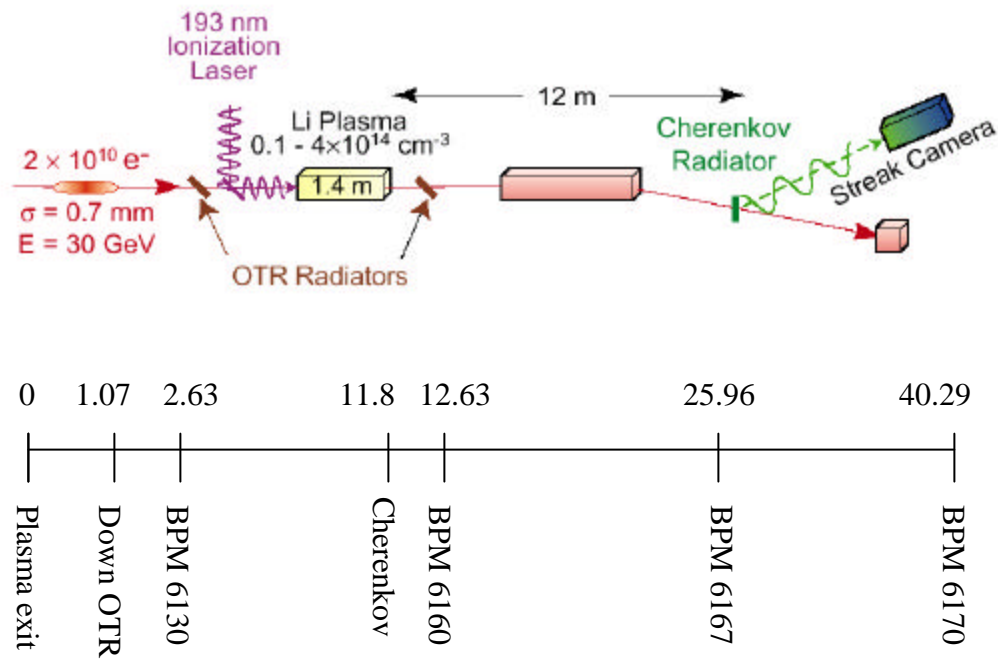
Figure 3.0.1 Experimental Setup and Diagnostic Locations

3.1 Stanford Linear Accelerator (SLAC)

Before a description of the E157 experimental components is given, a brief introduction to SLAC is necessitated. SLAC is operated under contract from the United States Department of Energy (DOE) as a national basic research laboratory. Its function is to probe the structure of matter at the atomic scale with x-rays and at much smaller scales with electron and positron beams. The major facilities at SLAC are the linac, End Station A, SPEAR and SSRL, PEP II, SLC, and the FFTB. The linac is a three kilometer long accelerator capable of producing electron and positron beams with energies up to 50 GeV. End Station A is for fixed target experiments. Early work in End Station A showed that the constituents of the atomic nucleus, the proton and neutron, are themselves composed of smaller, more fundamental objects called quarks. The Stanford Synchrotron Radiation Laboratory (SSRL) uses the SPEAR storage ring to produce intense x-ray and ultraviolet beams for probing matter on the atomic scale. PEP II is a storage ring for a B meson factory in which an experiment, BaBar, is seeking to answer why the universe is made of matter and not anti-matter. The Stanford Linear Collider (SLC) in conjunction with the Stanford Large Detector (SLD), analyzed collisions of 50 GeV electrons on 50 GeV positrons in order to determine the mass and other properties of the Z^0 particle, which is a carrier of the weak force of subatomic physics. The Final Focus Test Beam (FFTB) is a facility for research on future accelerator design. The E157 experiment is located inside the FFTB.

3.2 Final Focus Test Beam (FFTB)

The FFTB was designed to be a facility to be used for the development and study of optical systems, instrumentation, and techniques needed to produce the small beam spot sizes required for future electron-positron colliders. The design consists of five key sections. The first part is a matching section to match the beam that appears at the end of the linac to the lattice of the FFTB beamline. This matching section also has lens to match the betatron space of the beam to the second section, the chromatic correction section. The second, third, and fourth sections are used to correct chromatic and geometric aberrations on the beam. The final section is a telescope that focus the beam down to a small spot size.

The optics of the FFTB consist of dipoles, quadrupoles, and sextapoles. In order to focus the beam down to nanometer spot sizes, the optics needed to be aligned to an accuracy on the order of a micron. The optics were mounted on 3-axis positioners that allowed the optics to be moved ±1mm with 300nm resolution. To complement these optics, diagnostics were needed to determine the spot size and position of the beam along the beamline. These include torroids (to measure the beam's charge), wire scanners (to measure spot size), and BPMs (to measure the beam's posistion, Sec. 3.5). A diagram of the elements of the FFTB near interaction point 1 is given in figure 3.2.1 while a full diagram of the FFTB elements is given in appendix A.
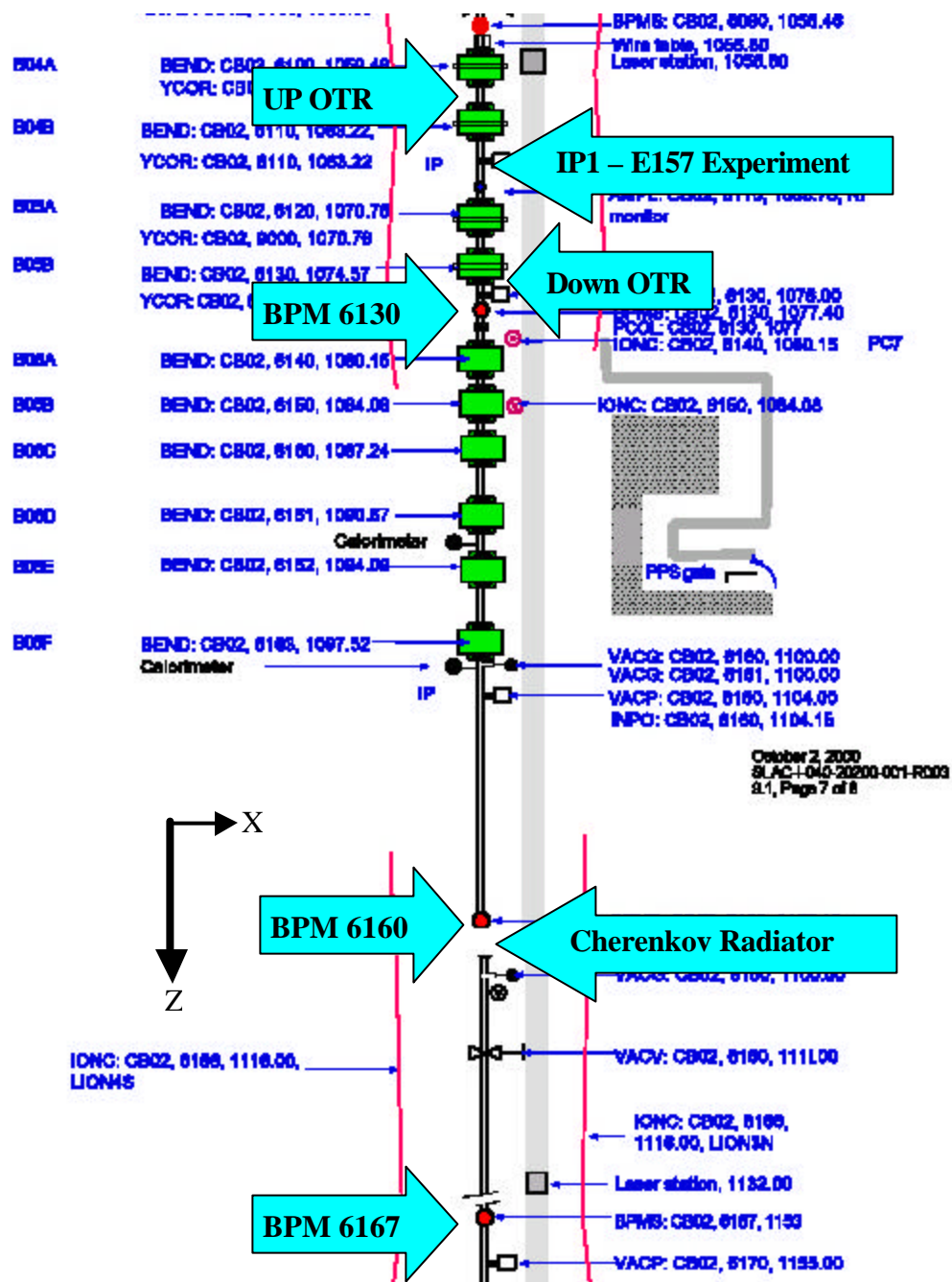
Figure 3.2.1 Diagram of the FFTB near IP1 with relevant diagnostic locations marked

The E157 Experiment

3.3 Lithium plasma source

The two main components of the Li plasma source are the heat pipe oven and the ionizing laser. The heat pipe oven consists of a stainless steel tube wrapped in heater tapes. The inside is lined with a wire mesh and is partially filled with solid (at room temperature) Lithium. Water jackets are placed at each end of the oven. A helium buffer gas is used to constrain the Li vapor. The oven is heated to ~750°C and a Li vapor is formed. The vapor flows from the center of the oven (where it is the hottest) to the water jackets (where it is the coolest). The mesh acts as a wick and transports the Li back towards the center of the oven. The Helium gas, in conjunction with the water jackets, constrains the Li vapor into a uniform column with sharp boundaries. The end product of this heat pipe is a 1.4m long, uniform column of Li vapor at a density of ~$2x10^{15}$ cm^{-3}.

An argon-fluoride excimer laser provides an ultraviolet pulse (193nm, 6.45eV) to ionize the Li vapor via single photon absorption. The first ionization energy of Li is 5.392eV [25] with an ionization cross section of $1.8x10^{-18}$ cm^{-2}. A 10-20ns laser pulse is focused down the vapor column so that laser fluence is constant (photon absorption is counteracted by reduced spot size). At the entrance of the plasma the laser cross-section is approximately 16 mm^2 whereas at the end it is approximately 8 mm^2. Because the laser fluence determines the plasma density, simply changing the output pulse energy on the laser can vary the oven's plasma density. This results in a 1.4m

long plasma column of with a variable density up to 6×10^{14} cm^{-3} as the laser energy is varied from 0-40 mJ.
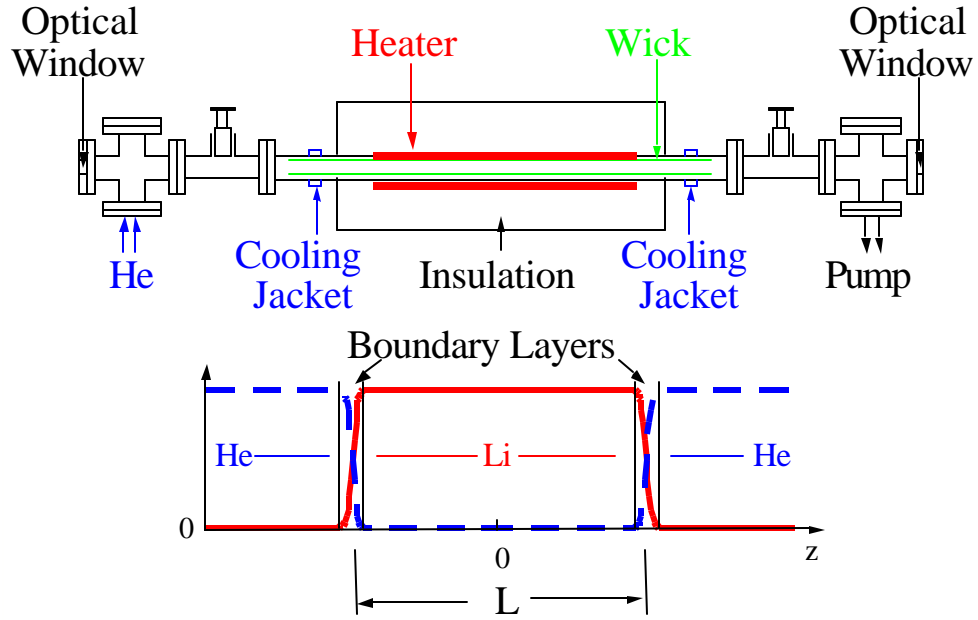
Figure 3.3.1 Diagram of Lithium Oven Setup and Depiction of Lithium Column

3.4 Optical Transition Radiators (OTR)

Two OTR diagnostics are employed in the E157 experiment, one 1 m before the plasma and one 1m after the plasma. These diagnostics give us a single shot time-integrated picture of the beam that allow us to measure the beam's spot size in both the x and y planes. The setup consists of a thin titanium foil placed at a 45° angle in the beam line. An AF Micro-Nikkor 105mm f/2.8D lens is used to image the OTR

from the foil on to a 12-bit Photometrics Sensys CCD camera. The CCD has a pixel size of 9µm x 9µm with an array size of 768 x 512. The spatial resolution of the setup is approximately 20 µm. A computer is used to read out the images and it can acquire date at 1 Hz.

OTR is one mechanism by which a charged particle can emit radiation. The radiation is emitted when a charged particle passes from one medium into another. For our case, the electron beam is propagating in a vacuum and then it enters a titanium foil. When the beam is in vacuum it has certain field characteristics, and when it is inside the titanium foil it has different field characteristics. As the beam makes the transition into the foil, the fields must reorganize themselves. In the process of reorganization, some of the field is "shed" off. Optical transition radiation is this "shed" field [26].

OTR has been used extensively on low energy (MeV) beams, but people thought that it would not be a viable diagnostic for high energy (GeV) beams. The OTR has a peak at angles $\theta=1/\gamma$, which is small for 30 GeV beams ($\gamma=60000$). Because diffraction limited resolution goes as λ/θ, the assumption was that high energy beams could not be resolved. The misconception was that θ is the numerical aperture of the lens, not the radiation source, and that there is significant radiation in the wings of the OTR distribution profile. The E157 collaboration has proved this to be correct by measuring spot sizes on the order of 30 µm. Figures 3.3.1 shows typical upstream and downstream OTR images. The graininess of the downstream OTR

image is not from the beam, rather it results from the grain structure of the titanium foil. Figure 3.3.2 shows how the image analysis routines in Matlab extract spot size information from the images.

Upstream OTR
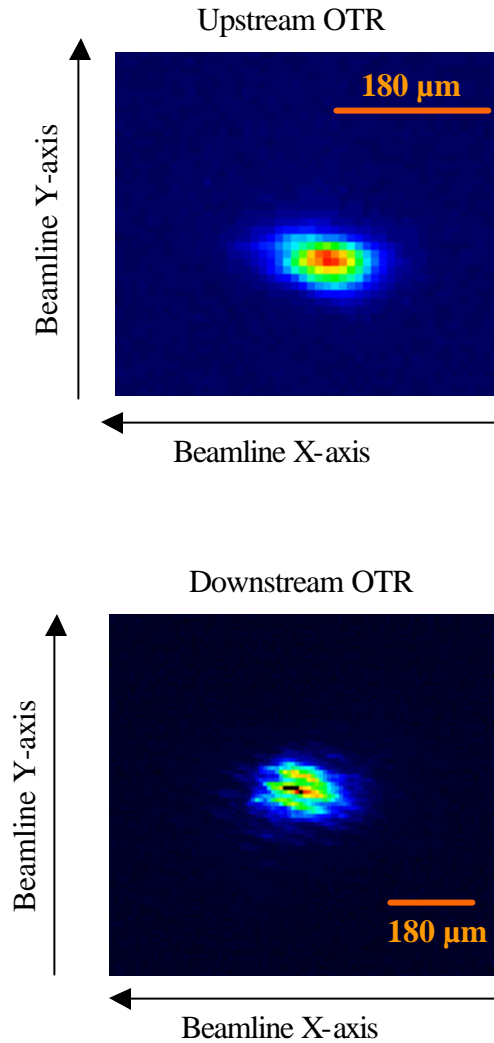
Downstream OTR

Figure 3.4.1 Upstream and Downstream OTR Images

Upstream OTR Image
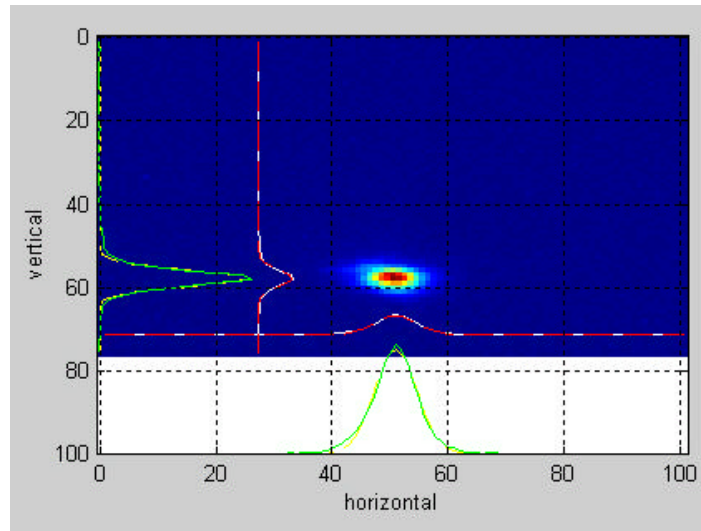
Downstream OTR Image
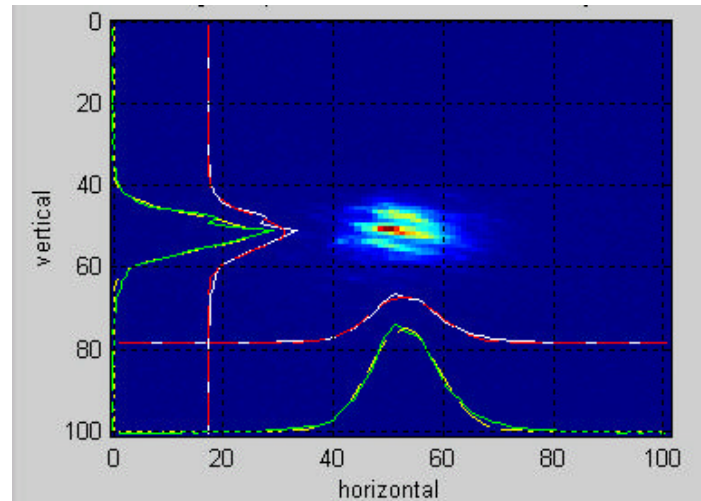
Figure 3.4.2 Image analysis of upstream and downstream OTR images. The white dashed line is the background level. The red line is a gaussian fit to the background level. The dashed yellow line is either a summation of the columns (for the vertical plane) or a summation of the rows (for the horizontal plane). The green lines are gaussian fits to the summation. The upstream image has a vertical spot size of 33.3 µm (3.7 pixels) and a horizontal spot size of 18 µm (2 pixels). The downstream image has a vertical spot size of 37.8 µm (4.2 pixels) and a horizontal spot size of 55.8 µm (6.2 pixels).

3.5 Beam Position Monitors (BPMs)

BPMs measure the beam's position by coupling to the beams electromagnetic field. They use four stripline antennas mounted in quadrature inside the beam pipe as shown in figure 3.5.1.
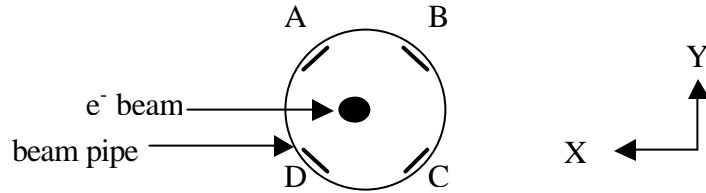
Figure 3.5.1. Typical Stripline BPM

The most common measurement is called the "difference over sum" method. In this method, the radio frequency signal is peak rectified and stretched. The output is then fed into circuitry that calculates positions from

$$X = \frac{(A+D)-(B+C)}{A+B+C+D} \frac{1}{S_x} \tag{3.5.1}$$

$$Y = \frac{(A+B)-(C+D)}{A+B+C+D} \frac{1}{S_y} \tag{3.5.2}$$

where

$$S_x(0,0) = S_y(0,0) = \begin{cases} \dfrac{\sqrt{2}}{r} ; @\ 45^o \\ \dfrac{1}{r} ; @\ 0^o \end{cases} \tag{3.5.3}$$

In addition to calculating position, the BPMs can also be used to measure the beam current.

BPMs are positioned all along the beam line in the FFTB. Several are upstream of the plasma chamber and are used to align the beam with quadrupole magnets and our plasma chamber. Five BPMs located downstream of the plasma chamber are used to measure the trajectory of the beam as it exists the plasma.

3.6 Aerogel Cherenkov Radiator

Cherenkov radiation is emitted whenever charged particles pass through a medium with a velocity that exceeds the velocity of light in that medium.

$$v > v_t = c/n \tag{3.6.1}$$

where v is the particle's velocity (in our case v=c), v_t is the threshold velocity, and n is the index of refraction of the medium. One can see that Cherenkov radiation will be emitted anytime a relativistic beam passes through any medium (n>1). The light is emitted at a constant angle with respect to the particle's trajectory.

$$\cos(\boldsymbol{d}) = \frac{v_t}{v} = \frac{c}{vn} = \frac{1}{n\boldsymbol{b}} = \frac{1}{n}(\text{for } v = c) \tag{3.6.2}$$

This emission is similar to the bow shock created during supersonic flight.

In our experiment, we use the Cherenkov light as part of our energy gain diagnostic. The electron beam exists the plasma and drifts through an energy dispersive magnet. The beam then passes through the aerogel and emits Cherenkov

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radiation. The light is transported approximately 15m to an optical table outside of the FFTB. The light passes through a beam splitter and a small fraction of the light is sent to a CCD camera for time-integrated images of the beam figure 3.6.1 (similar to the OTR images). The remaining light passes through a beam splitter again and one arm is rotated 90 degrees. The two paths are recombined and sent to the streak camera. The 90 degree rotation allows us to streak both the energy dispersive plane (y-axis) and the non-dispersive plane (x-axis) simultaneously figure 3.6.2. Figure 3.6.3 shows the layout of the optical table. The streak camera has a temporal resolution of one picosecond and a spatial resolution of ~100 µm. My analysis will use the non-dispersive plane on the streak camera in order to resolve head-tail offsets.
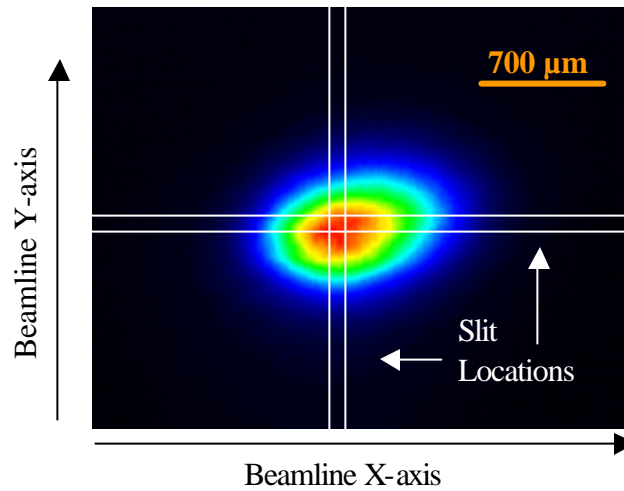
Figure 3.6.1   Time Integrated Cherenkov Image depicting the parts of the beam seen by the horizontal and vertical slits on the streak camera
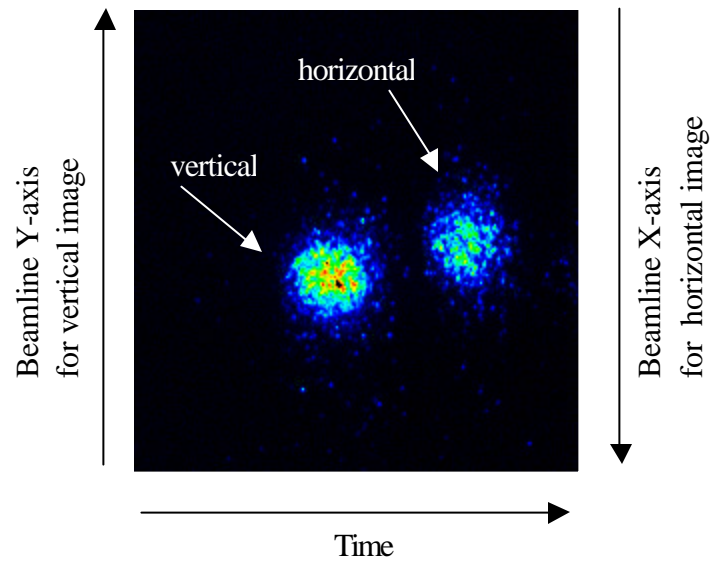
Figure 3.6.2   Typical Streak Camera image showing both the horizontal and vertical streaks
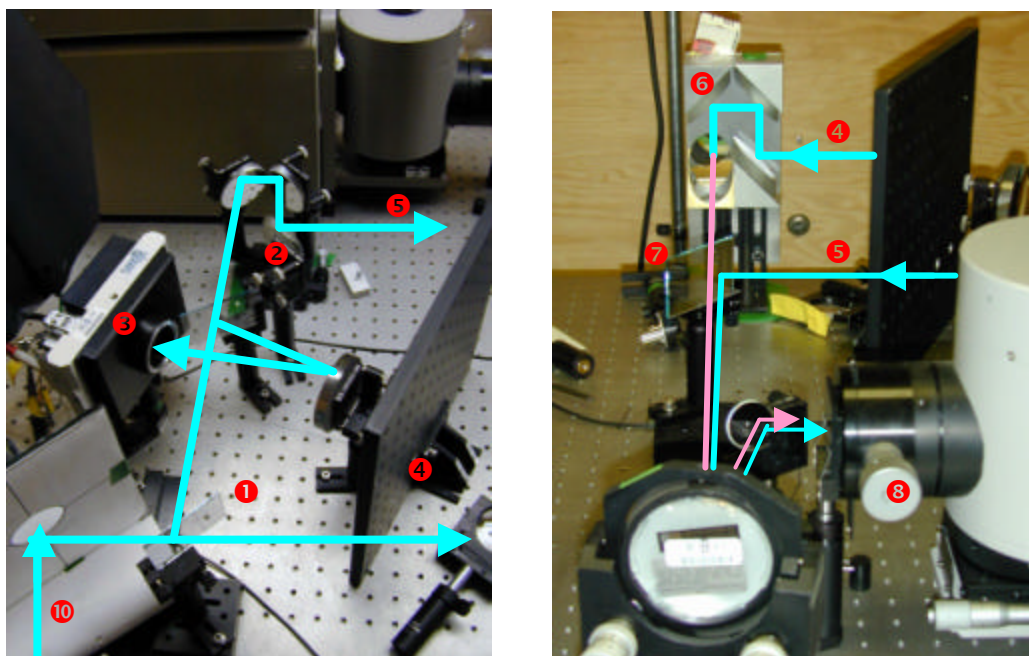
Figure 3.6.3 Diagram of Cherenkov radiation detector setup. The light radiated from the aerogel enters the setup at ❿. It is reflected off of a mirror towards beam splitter ❶. Part of the light is sent to the image rotator ❻ via path ❹ while the other part is directed towards beam splitter ❷. Part of light off of beam splitter ❷ is sent to a CCD camera ❸ for time integrated Cherenkov images while the rest is directed towards beam splitter ❼ via path ❺. The image on path ❹ passes through an image rotator ❻ where it is rotated 90 degrees (the unrotated path is shown in light blue while the rotated image path is shown in purple). Both the unrotated and rotated images are combined at beam splitter ❼. The combined images (slightly delayed in time from each other) are then sent to the streak camera ❽ for time-resolved analysis.

4 Results

4.1 Initial Beam Condition

One of the major highlights of the E157 experiment was the advance made in beam diagnostics. These diagnostics allowed the accelerator physicists to see details of the beam dynamics they had not seen before. The lowest order concern for the experiment was delivering a beam to our plasma with a specified energy and spot size. These requirements were readily attainable since the energy was determined by the linac settings and the spot size was determined by adjusting the beam optics to focus the beam at the plasma entrance. With the knowledge that the electron hosing instability might be a problem for our experiment, we were also concerned about a longitudinal transverse correlation on the beam.

With the available E157 diagnostics, a beam tilt could be quantified by time resolving laser off (i.e. no plasma) data. Because the streak camera is located after the energy (or vertical plane) dispersive bend magnet, we will look at streak data from the horizontal plane (no dispersion). The first step is to slice up the streaked image in 1ps bins. Next, analyze each slice to find its mean position. Finally, a tilt implies that the mean position of each slice will change in time. Figure 4.1.1 shows a streak camera image, where the horizontal streak image has been selected. The lines on the image illustrate how the data analysis software slices up the time-resolved image.

Horizontal Laser Off Streak Data
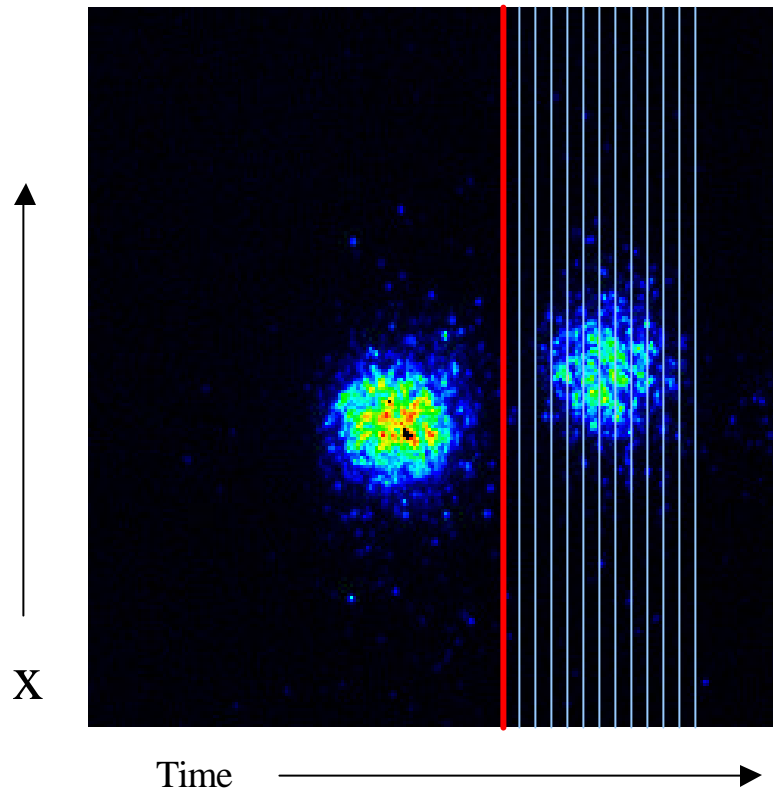
> ➢ Cut beam up into slices
>> ➢ Analyze each slice to find <x>
>>> ➢ A tilt implies <x> will move in time

Figure 4.1.1 Streak Camera Data

The results of the analysis for two single events are plotted with the x-axis being time and the y-axis being mean position. –4ps is the head of the beam, and +5ps is the tail end of the beam. To help visualize the beam tilt, imagine that you are flying down the

beam line looking down at the electron bunch. You will see the back of the bunch is not in line with the head of the bunch, rather it is displaced to the side.

Analysis of Single Shots
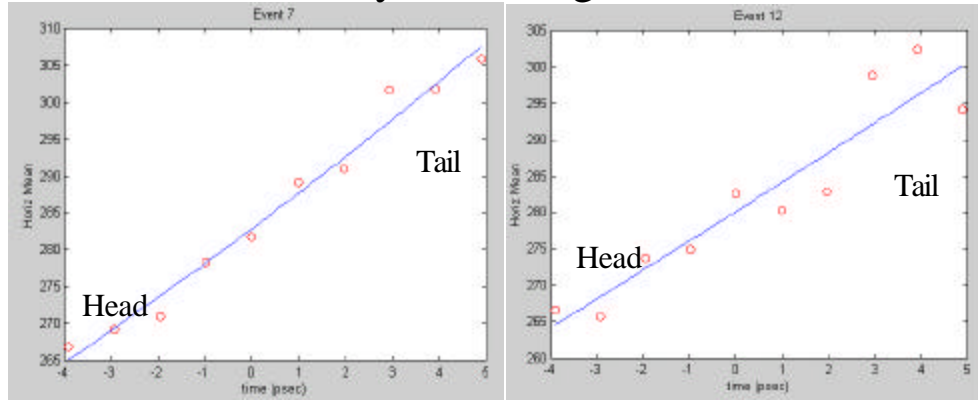
Figure 4.1.2 Tilted Beams (N=2x10^{10} e$^-$; s$_{xDN}$=110μm)

The total results for a single run of 25 consecutive shots are given in figure 4.1.3. Every data point is plotted for each picosecond bin. The solid line drawn through the points represent the mean of all 25 shots for each time step. The two dashed lines represent the mean ± rms for each time step.
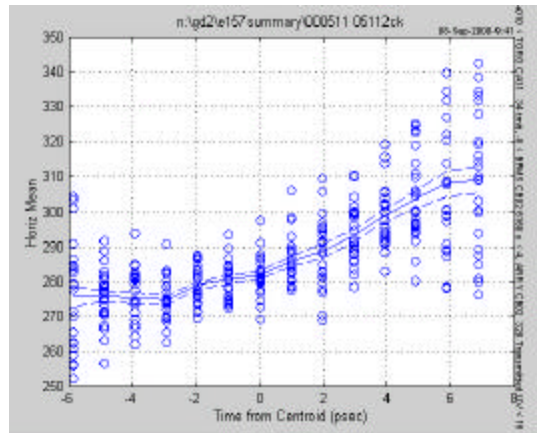
Figure 4.1.3 Average of 25 laser off shots (N=2x10^{10} e$^-$; s$_{xDN}$=110μm)

The bunch length corresponds to a s_z of about 2ps. This gives a beam tilt of 84 μm/s or 197 μm at FWHM. The beam spot size, measured from the time integrated Cherenkov image, was s_x=560 μm or FWHM = 1316 μm. The conclusion we draw from this is that the beam is tilted.

The measured tilt corresponds to the beam parameters at the aerogel that is 12 meters downstream from the plasma chamber. What we are interested in is the beam tilt at the entrance of the plasma. Ideally we would move the aerogel and the streak camera to the plasma entrance. This was not possible, so we approximate the beam tilt at the plasma entrance. We do this by fitting the beam envelope equation

$$\frac{\partial^2 \mathbf{s}(z)}{\partial z^2} + \left[K^2 - \frac{\mathbf{e}_N^2}{\mathbf{g}^2 \mathbf{s}^4(z)} \right] \mathbf{s}(z) = 0$$

$$K = \begin{cases} 0 & \text{no plasma} \\ \dfrac{\mathbf{v}_p}{c\sqrt{2\mathbf{g}}} & \text{in a plasma} \end{cases} \qquad 4.1.1$$

$$\mathbf{e}_N \qquad \text{Normalized emittance}$$

to the three known spot sizes (upstream OTR, downstream OTR, and time-integrated Cherenkov) in order to find the spot size at the plasma entrance. From the fitting procedure, the minimum spot size turns out to be 32 μm. The location of the beam waist is approximately 20 cm from the plasma entrance. This is shown in figure 4.1.4.
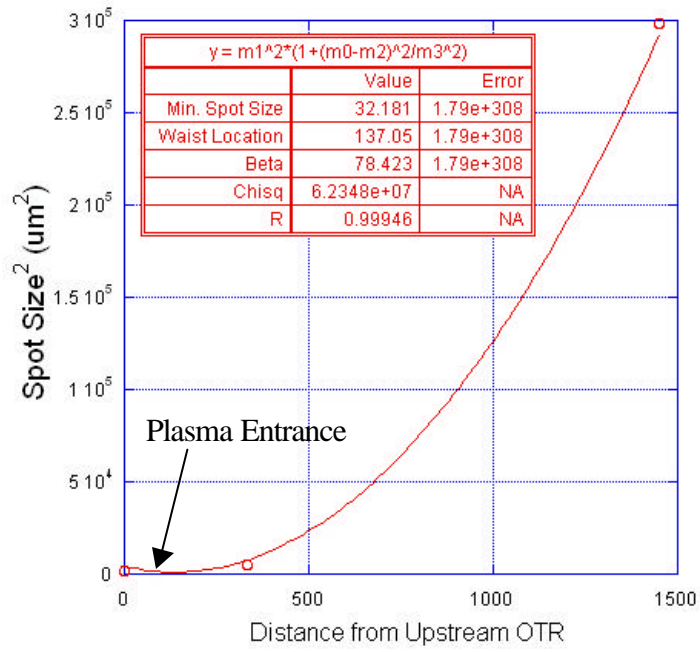
Figure 4.1.4 Fit to envelope equation

After determining the spot size at the plasma entrance, we determine the tilt at the plasma entrance, R_o, by scaling the tilt at the aerogel, R_1, by the ratio of the two beam spot sizes.

$$R_o = R_1 \frac{\sigma_o}{\sigma_1}$$
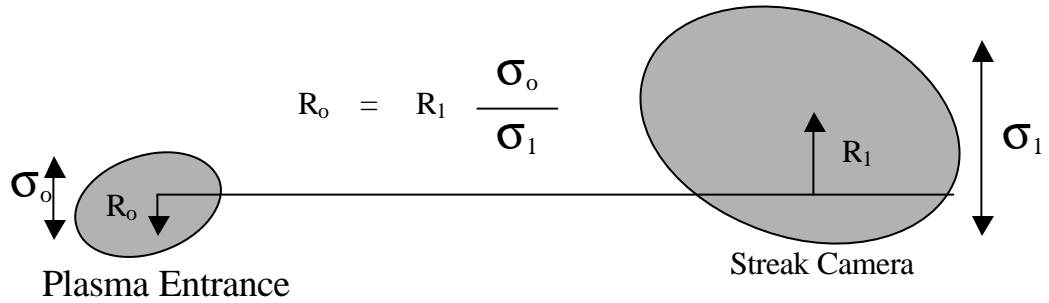
Figure 4.1.5 Scaling of Beam Tilt

The values for the offset at the plasma entrance for the 25 shots are
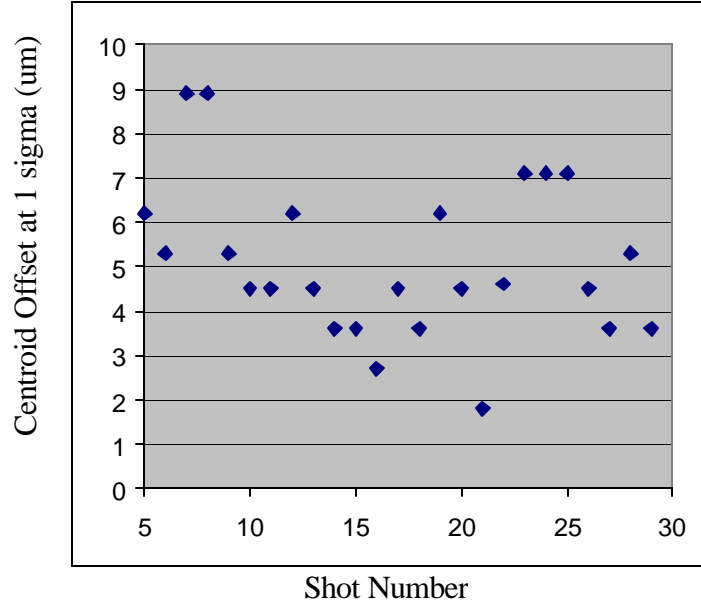
Figure 4.1.6 Centroid offset at plasma entrance (N=2x10^{10} e$^-$; s$_{xUP}$=36µm)

4.2 Centroid Oscillations

Although our analysis is limited to the horizontal plane (due to the dispersive bending magnet), a beam tail generally lies in both the vertical and horizontal planes. Figure 4.2.1 shows two upstream OTR images of beams with large tails.   With the knowledge that the beam coming into the plasma is tilted, we would expect the trajectory of the exiting beam centroid to oscillate (equation 2.1.17).   The data in figures 4.2.2 and 4.2.3 was energy scan data.   The plasma density (x-axis) was varied by varying the ionizing laser energy.   Figure 4.2.2 shows centroid oscillations in both the horizontal and vertical planes just after the plasma on BPM 6130.   Figure 4.2.3

shows the horizontal deviation of the beam centroid from the laser off position on the downstream OTR (DNOTR). In general, neither the spot size nor the centroid oscillations in both the horizontal (x) nor the vertical (y) planes were in exact phase with respect to each other because of the large difference in the beam emittance in these two planes.
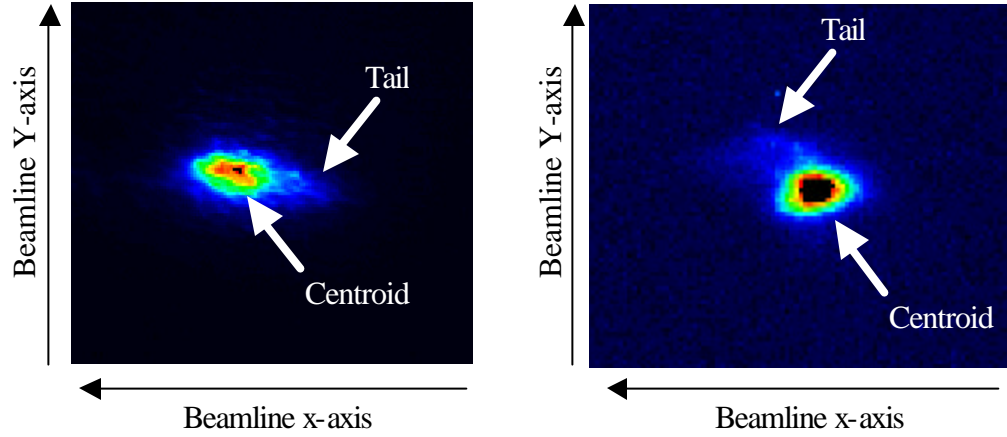
Figure 4.2.1 Upstream OTR images showing a tail that lies in both the horizontal and vertical plane (with respect to the beam centroid).
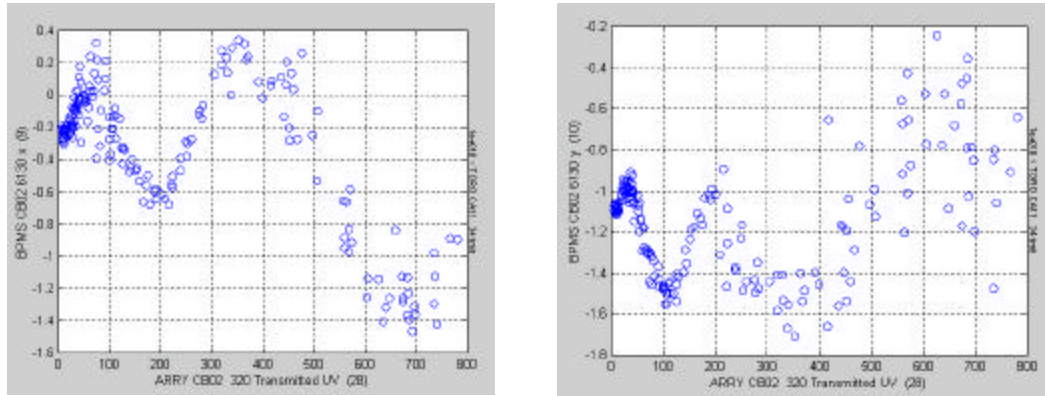
Figure 4.2.2 Centroid Oscillations on BPM 6130 for both the horizontal and vertical planes. The x-axis is the laser energy (plasma density) and the y-axis is the position of the beam centroid measured by the BPM.

Centroid Displacement at DNOTR
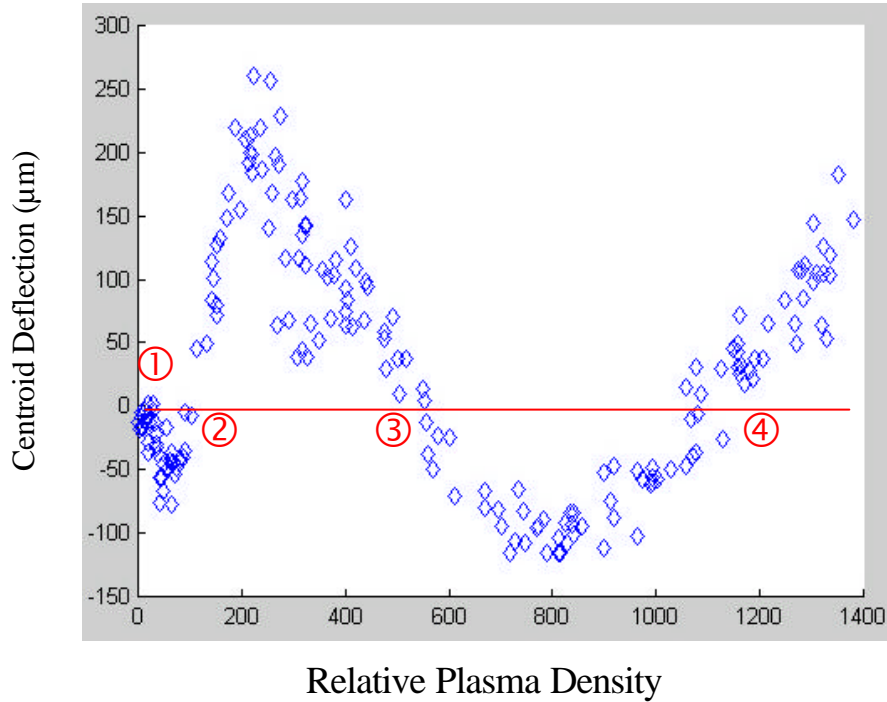
Figure 4.2.3 Centroid Oscillations (N=2.1x10^{10} e$^-$; s $_{xUP}$=55μm)

The centroid starts out in the same position as laser off, and then it goes through oscillations as the plasma density is increased. The four locations numbered 1-4 correspond to the zero crossings of the centroid oscillation.

In addition to the centroid oscillations, the beam experiences a transverse focusing force called betatron oscillations [27]. The plasma column acts as a thick lens whose focusing force is a function of plasma density. In the energy scan data, the beam underwent multiple betatron oscillations as can be seen from figure 4.2.4.

Spot Size at DNOTR vs. Plasma Density
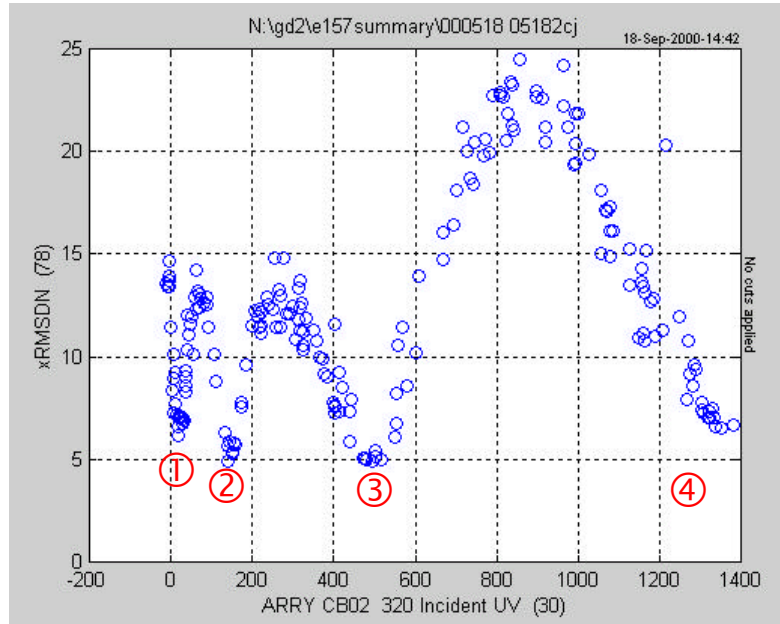
Figure 4.2.4 Betatron oscillations (N=2.1×10^{10} e$^-$; s $_{xUP}$=55μm)

The x-axis is plasma density and the y-axis is the beam's spot size 1m after the plasma. As the plasma density is increased, the beam goes through multiple focii that are numbered 1-4. You can see that the pinch (or focus) densities shown in figure 4.2.4 correspond to the zero crossings of the centroid oscillations shown in figure 4.2.3. This is as expected since the betatron oscillations are at twice the frequency of the offset centroid oscillations. The cartoon in figure 4.2.5 will describe why these two phenomena are related.

Tail

Head

1) Initial Beam Condition at the plasma exit. Note red electrons start off above the axis and blue ones below

2) At the first pinch – all electrons moved towards the axis. Notice the zero crossing of the centroid oscillation. The electrons have a maximum transverse or perpendicular momentum. This beam will defocus at the Cherenkov detector

3) Moving away from the pinch. The beam has blown back up to its original size (one oscillation) and the centroid (tail) has made half an oscillation. This is the "so called" p phase advance condition. The tail is now below the axis and the electrons have a minimum transverse or perpendicular momentum.

4) The beam goes through a second pinch and the centroid goes through a second zero crossing. Again the electrons have a large perpendicular momentum at the plasma exit.

Figure 4.2.5 Single electron motion within the beam at the plasma exit

As one can see, all electrons are oscillating across the axis. The difference is that when there are electrons on both sides of the axis, the beam appears to be focusing and defocusing whereas the tail electrons only appear to oscillate across the axis.

4.3 Tail Flipping

Following the above discussion, the dynamics of the beam can be studied by temporally resolving the beam near a pinch at the Cherenkov detector. This corresponds to a multiple of p phase advance for the beam envelope as it goes through the plasma since a well focused beam at the Cherenkov is only obtained when the beam exits the plasma more-or-less as it entered. As the beam passes through a pinch, the tail should flip from one side of the head to the other. Data was analyzed from both the 4th pinch and the 3rd pinch. The data was divided into bins according to proximity to the pinch. In each bin, the shots were analyzed to determine the horizontal mean position vs. position in the beam (head, tail, centroid, etc.) The data shows the tail moving from one side of the head to the other at the 3rd pinch. At the 4th pinch, the tail goes back to its original side.

Figures 4.3.1 and 4.3.2 show how the data was binned for analysis. The bottom red line corresponding to xRMS of 36 denotes the laser off spot size. Shots with spot sizes below this line are considered to be at the transparency condition. The upper horizontal red line is an arbitrarily chosen criteria to say that any shots with a spot size above this line are defocusing. The vertical lines separate defocused shot into group that are either coming into or exiting the pinch. Figure 4.3.3 gives justification for the 3rd and 4th pinch locations. Figures 4.3.5 and 4.3.6 show the tail flipping at the different pinches.
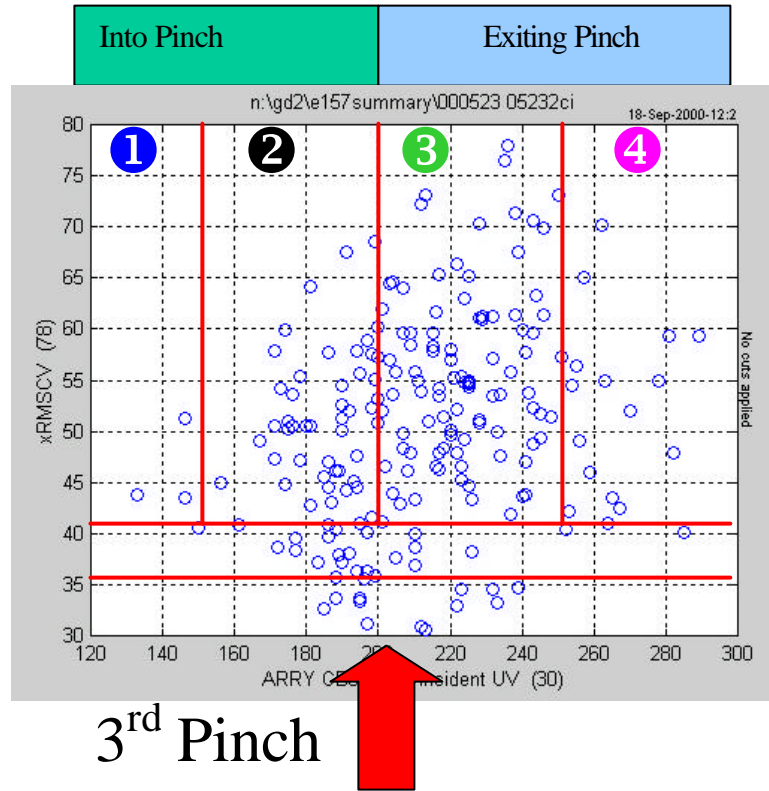
Figure 4.3.1 Spot size data from the 3rd pinch showing the bins numbered 1-4. These bins are used in figure 4.3.5 ($N=1.95 \times 10^{10}$ e^-; $s_{xUP}=56\mu m$) Nominal plasma density for the 3rd pinch is about 1×10^{14} cm^{-3}.
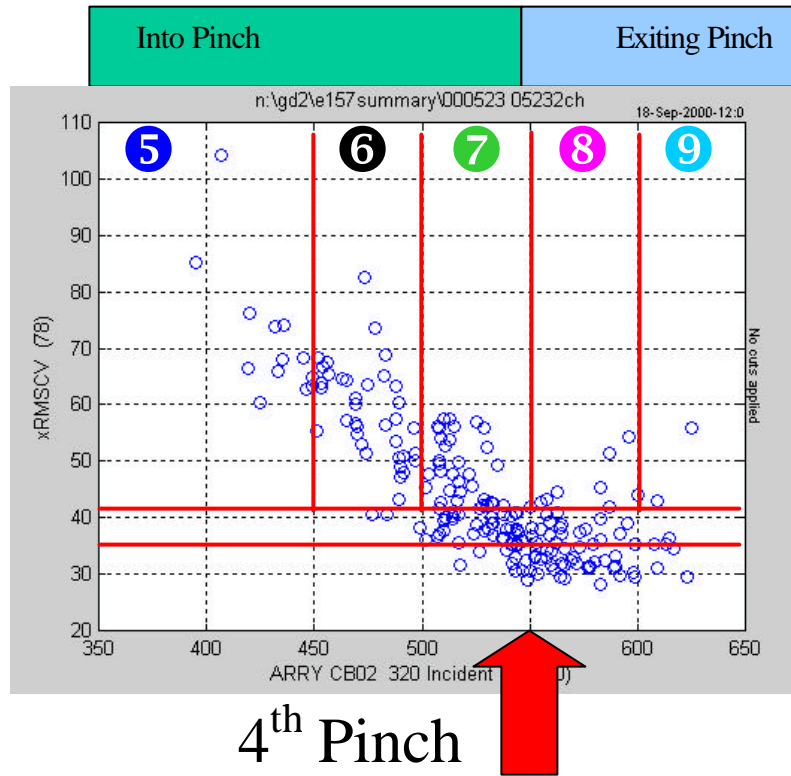
Figure 4.3.2 Spot size data from the 4th pinch showing the bins numbered 5-9. These bins are used in figure 4.3.6. $(N=1.95 \times 10^{10}$ e-; $s_{xUP}=54\mu m)$ Nominal plasma density for the 4th pinch is about 2×10^{14} cm-3.
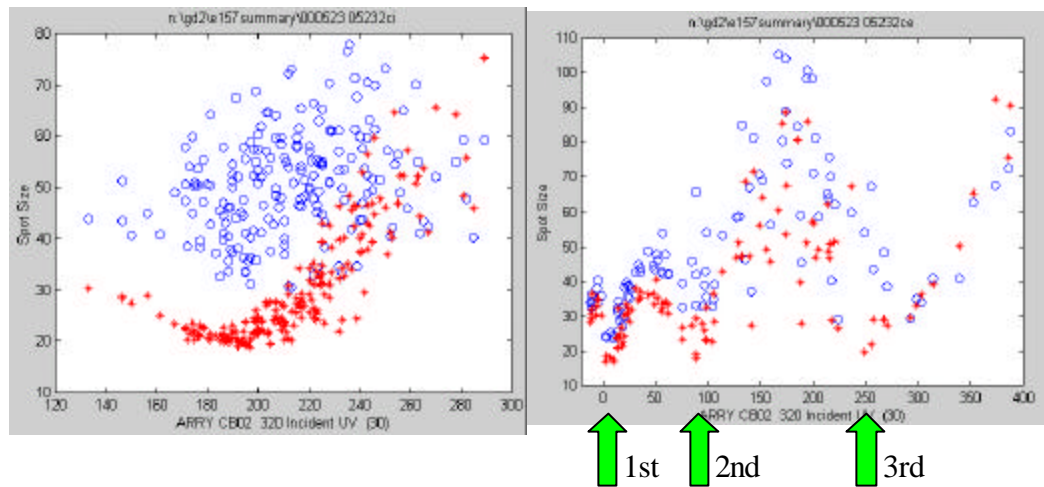
Figure 4.3.3 Justification of pinch location. The both images show the xRMS spot size (blue) and the yRMS spot size (red) at the aerogel vs. incident UV laser energy. The figure on the right shows that the 3rd pinch is located around a GADC reading of 250 and that the pinch location is nearly the same for both the horizontal and vertical planes. The left image is figure 4.3.1 with the yRMS data superposed to show the pinch location.
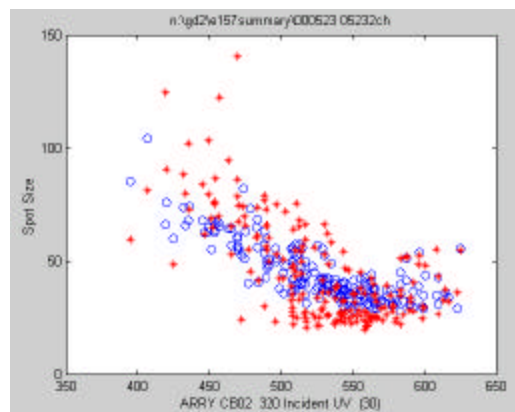
Figure 4.3.4 Fourth pinch data showing the location of the horizontal (blue) and vertical (red) pinches correspond to the same laser energy.

Figure 4.3.5 Tail motion at the 3rd pinch with the pinch located between bins 2 and 3. (N=1.95x10^10 e⁻; s xUP=56μm) Nominal plasma density for the 3rd pinch is about 1x10^14 cm⁻³.

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Bin5
Bin6
Bin7

Bin8
Bin9

4th Pinch

Tail going down
through the pinch
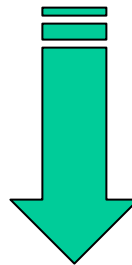
Figure 4.3.6 Tail motion at the 4th pinch
with the pinch located between bins 7 and
8. (N=1.95x10^{10} e$^-$; s$_{xUP}$=56µm)
Nominal plasma density for the 4th pinch
is about 2x10^{14} cm^{-3}.

4.4 Tail Growth on Streak Camera Diagnostic

After showing that the beam is tilted and that this tilt results in tail flipping, we now want to determine if we are experiencing a hosing instability. We will do this by looking at the streak camera data for three cases. The first case will be laser off data. This will determine the initial tilt on the beam. The other two cases are at two different plasma densities; the second and fourth pinches at the Cherenkov detector. The second and fourth pinches were chosen because they are both an integer number of betatron oscillations and an integer number of tail oscillations. Only data that satisfied a transparency condition, where the beam spot size was equal to or slightly smaller than the laser off spot size, was chosen. The laser off spot size was ~36 pixels and the data cut at the 4th pinch can be seen as the lower red bar in figure 4.3.2. The hypothesis is if an instability exists, then the magnitude of the head tail offset should rapidly grow with increasing plasma density (i.e. laser off ? 2nd pinch ? 4th pinch). Figures 4.4.1 shows the time slice analysis of the beam at the laser off, 2nd, and 4th pinches respectively. The results show that there are not signs of significant growth up to the fourth pinch, the operating point of the experiment.
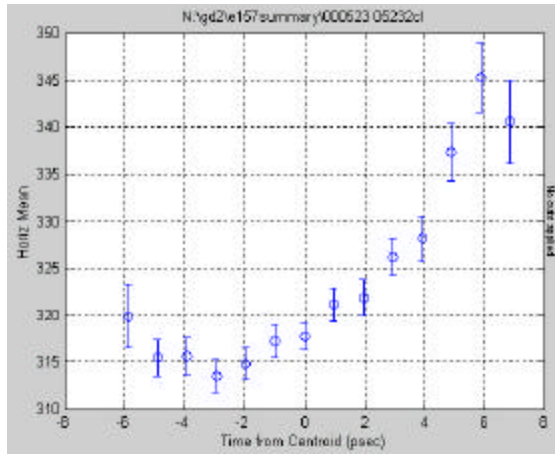
Laser Off
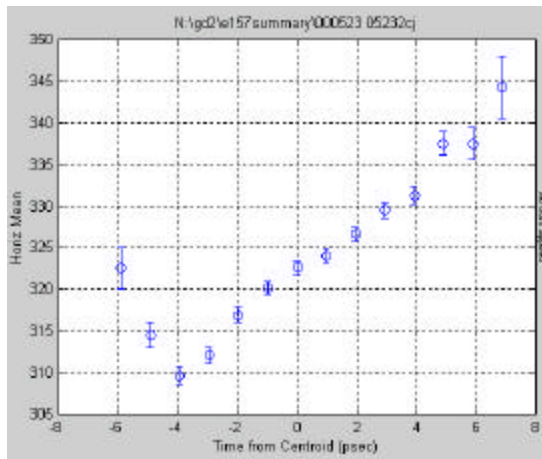
Second Pinch
$n_e \sim 0.3 \times 10^{14} \ cm^{-3}$.
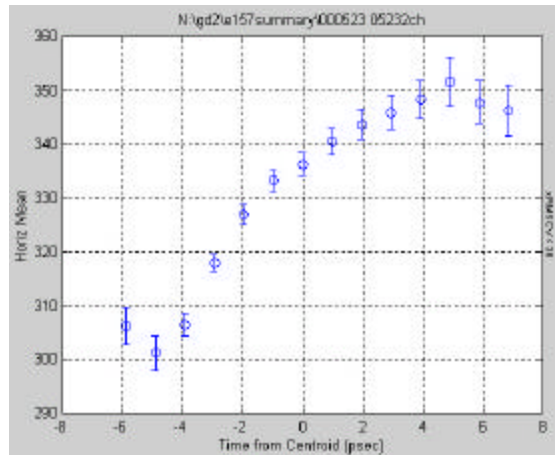
Fourth Pinch
$n_e \sim 2 \times 10^{14} \ cm^{-3}$.

Figure 4.4.1 Time slice analysis at laser off, second, and fourth pinch

Figure 4.4.2 shows the measured growth of the offset normalized to the initial offset (laser off) at the 4th pinch. Both the initial and final offsets are measured with respect to the blow out time. In our case the blow out time was chosen to be 1 and 2 ps before the centroid. For the 2ps case, the mean position of the –2ps slice in the fourth pinch data in figure 4.4.1 is 315. The mean position of the slice 4ps after the centroid is 328. This implies the measured offset is 13 (328-315). The offset is calculated for each slice after blowout and plotted vs. a theoretical curve of a 140cm long, $2x10^{14}$ cm^{-3} plasma.
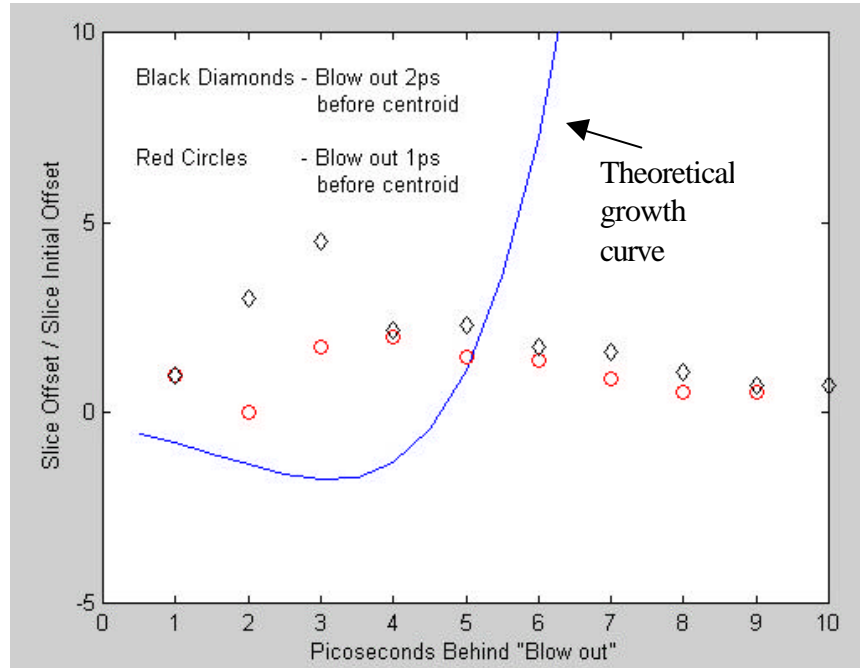
Figure 4.4.2 Growth of normalized slice offsets vs. theoretical hosing curve. (N=1.95x10^{10} e$^-$; s$_{xUP}$=56μm)

4.5 BPM Data for a High Density Run

One data run in the E157 experiment achieved a density higher than any other run. Whereas most runs could only achieve a density of $2x10^{14}$ cm^{-3}, one run achieved a density of approximately $6x10^{14}$ cm^{-3}. This is important because the hosing growth rate increases rapidly with increasing density. Because this run was energy scan data, the centroid motion experienced large displacements. These kicks were large enough to steer the beam off of the streak camera slit, rendering the streak camera data unusable. This mandated the use of BPMs to look for the hosing instability.

To analyze this data, we follow the oscillations of the beam exiting the plasma as measured by the downstream OTR and the beam position monitors 6130, 6160, 6167, and 6170 (figure 4.5.1). For each shot, the deviation from laser off position is calculated and this deviation is plotted versus the BPM's (or downstream OTR) position relative to the exit of the plasma. Figure 4.5.2 shows typical beam trajectory leaving the plasma. A straight line fit is made to the five points (a straight line indicates that upon leaving the plasma, the beam centroid travels ballistically), and the slope of the exit trajectory is found. Figure 4.5.3 shows a plot of the slope of the beam's exit trajectory versus incident laser energy for all 200 shots.
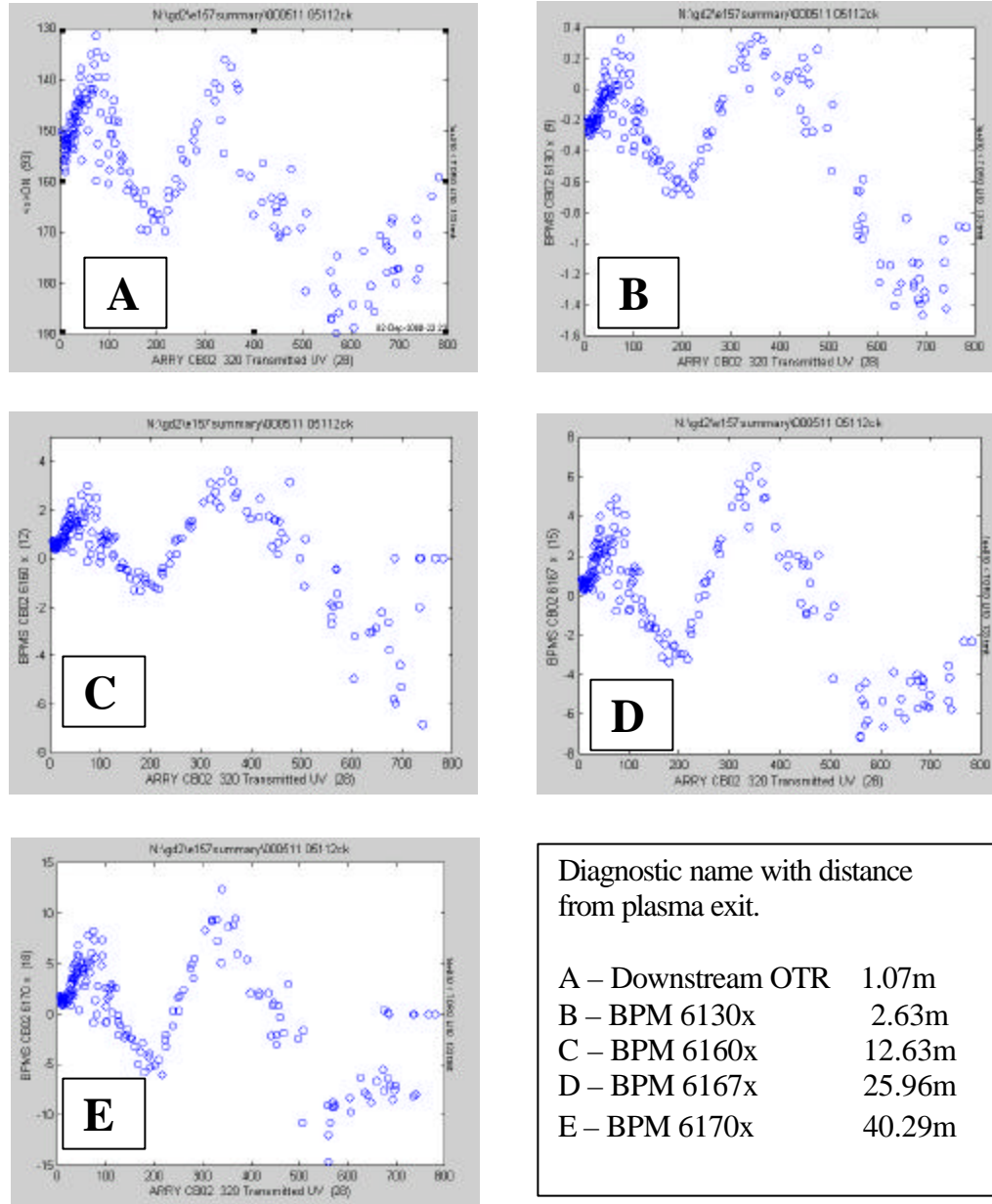
Figure 4.5.1 Oscillations of beam centroid after plasma exit as measured on downstream OTR and on BPMs 6130, 6160, 6167, and 6170. The x-axis is the incident UV laser energy and the y-axis is the transverse position of the beam centroid. ($N=2\times10^{10}$ e$^-$; s$_{xUP}$=36μm)
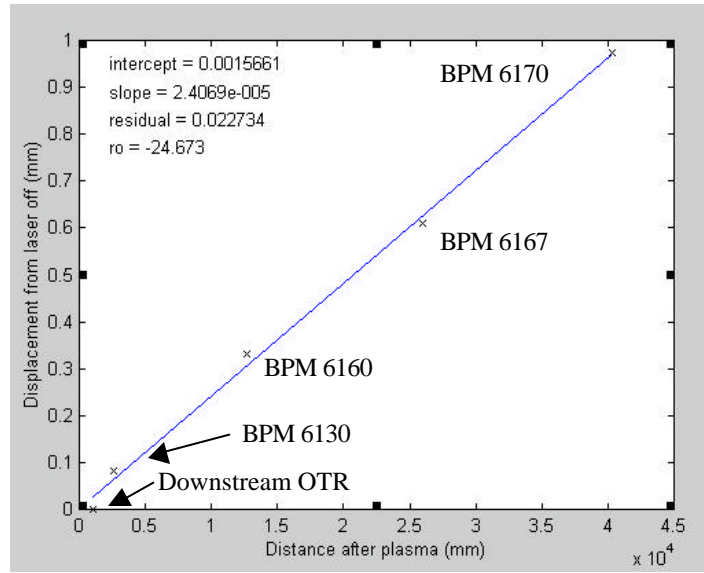
Figure 4.5.2 Beam trajectory exiting plasma
$(N=2x10^{10}$ e$^-$; s $_{xUP}=36\mu m)$
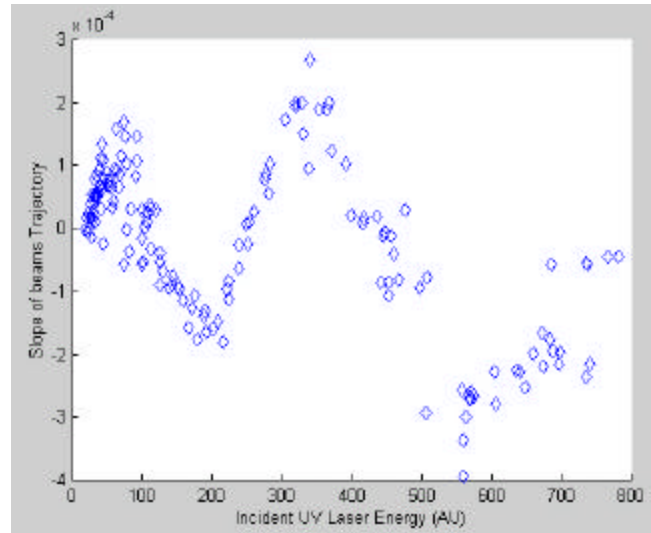
Figure 4.5.3 Slope of the beams exit trajectory as a function of laser
energy (plasma density) $(N=2x10^{10}$ e$^-$; s $_{xUP}=36\mu m)$

Figure 4.5.3 show the slope versus laser energy, but it is more insightful to convert the incident laser energy into plasma density. This is done by fitting the beam envelope equation (4.1.1) to the betatron oscillation data (i.e. spot size fluctuations) as shown in figure 4.5.4.
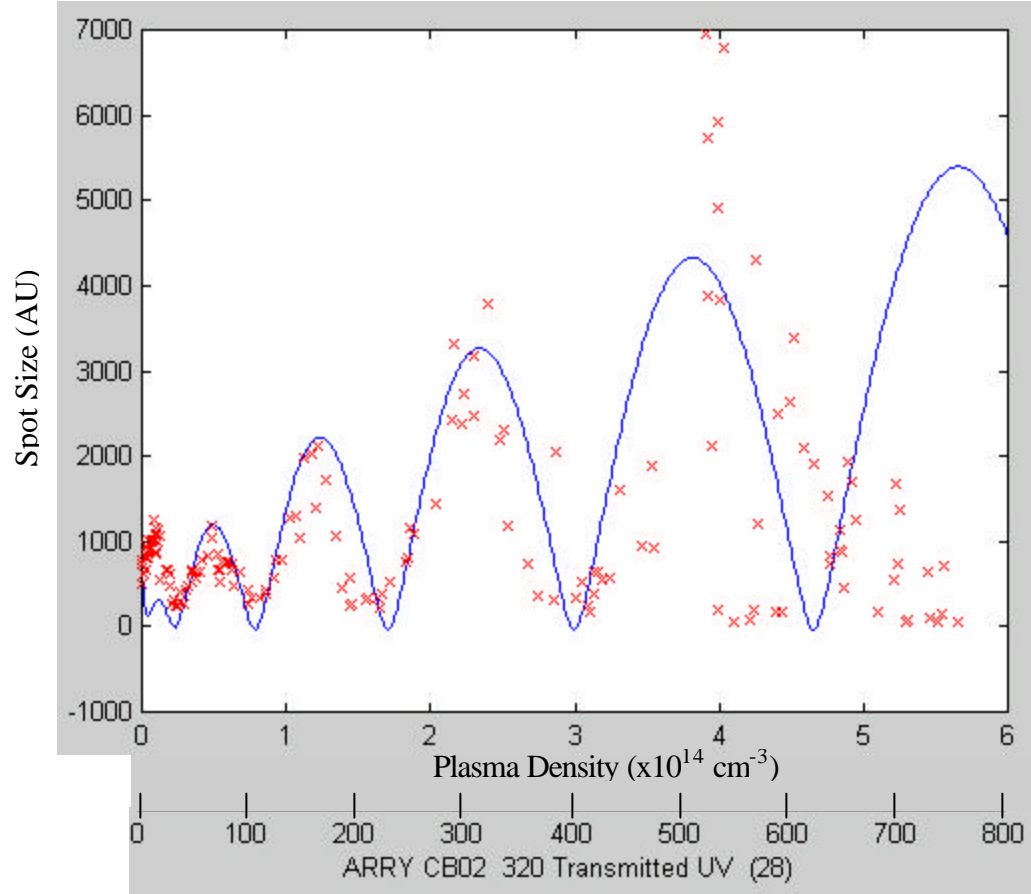
Figure 4.5.4 Plot of envelope equation (shown in blue) versus plasma density superimposed on a plot of the beams spot size (red diamonds) versus incident UV laser energy. This fit is used to convert the incident UV laser energy into plasma density.

The equation for the exit trajectories slope in the absence of hosing (2.1.17) has four variables: the slope, r'; the initial offset, r_o; the plasma density, k_β; and the plasma column length, s. The only unknown is the initial offset. By applying the formula for centroid oscillations with no growth (2.1.17) and solving for r_o at low densities, we find that the initial offset is about 24 μm.

The slope is the ratio of the beams transverse energy to its longitudinal energy.

$$r' = \frac{m_e c^2 \boldsymbol{g}_\perp}{m_e c^2 \boldsymbol{g}_\|} = \frac{\boldsymbol{g}_\perp}{\boldsymbol{g}_\|} \qquad\qquad 4.5.1$$

Figure 4.5.2 shows the calculated perpendicular energy of the beam (found from the slope trajectory) plotted vs. plasma density. The blue diamonds represent calculated values and the black x's represents a theoretical envelope (neglecting the sinusoidal term for clarity) curve of perpendicular energy in absence of hosing .

$$E_\perp = r_o k_b mc^2 \qquad\qquad 4.5.2$$

The red circles represent a theoretical envelope (neglecting the sinusoidal term for clarity) curve for perpendicular energy with hosing.

$$E_\perp = 0.341 \frac{e^A}{A^{3/2}} r_o k_b mc^2$$

The slice index t was chosen to be 1.25ps so that the theoretical curve matched a data point at the plasma density of $4*10^{14}$ cm^{-3}. A small value of t is expected since "blow out" occurs near the centroid and BPMs measure the position of the centroid.
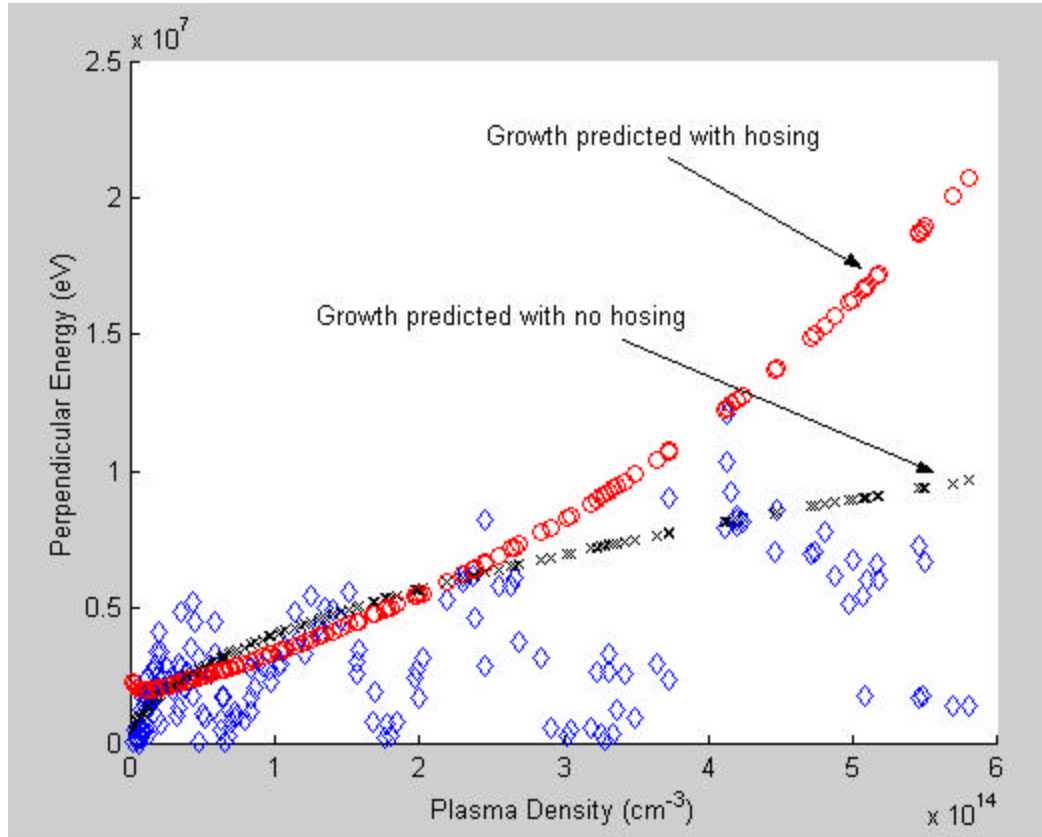
Figure 4.5.2 Perpendicular Energy of Beam in a High Density Plasma
($N=2x10^{10}$ e^-; s_{xUP}=36µm)

The large discrepancy at the low plasma density is due to beam jitter and a divide by zero numerical error. We also know from the time slice analysis that hosing is not present at these low densities. On the other hand, a few of the data points around $4x10^{14}$ cm^{-3} show evidence of growth on the order of 1.5x. This value is consistent with the growth factor predicted by the tilted beam hosing equation 2.2.5 for a t = 1.25ps.

5 Conclusion

5.1 Summary

A subset of the transverse dynamics of an ultra-relativistic electron beam propagating through a meter long plasma has been experimentally measured. The electron hosing instability arises when electrons are offset in an ion column. In a single bunch PWFA experiment, a beam tilt will result in offset electrons. Time-slice analysis of the electron bunch has quantified a head-tail offset (i.e. tilt). Further analysis has shown the tail off the beam oscillating inside the plasma. Finally, the magnitude of the oscillation was not observed to significantly grow up to the operating plasma density of the E157 experiment. In other words, there is no evidence of the electron hosing instability at the operating parameters of the E157 experiment. Recent simulations by E. Dodd corroborate the above statement [28]. There is possible evidence of the hosing instability in a single high-density plasma run, but further data is needed at such a high density to be conclusive.

5.2 Future Directions

An upcoming experiment at SLAC will provide the opportunity to expand on these results [29]. First, an imaging spectrometer will be constructed that will image the beam from the output of the plasma onto the aerogel. This will allow us to analyze the beam at the exit of the plasma as opposed to analyzing it after 12 meters of drift.

A second benefit will be the analysis of positron beams. In an analogous situation to ion channel formation with electron beams, positron beams will create a channel where electrons rush in. The transverse dynamics of a positron beam will be rich with physics that will be both challenging and rewarding to analyze.

Appendix A FFTB beamline

QA1   QUAD: CB00, 1040, 576.91
V1C   YCOR: CB00, 1040, 580.69
  WIRE: CB02, 1040, 581.88
QBM2   QUAD: CB00, 1050, 583.73
QA2   QUAD: CB00, 1060, 585.46
  VACG: CB02, 1068, 588.97

B01A   BEND: CB00, 1070, 592.72
H1C   XCOR: CB00, 1070, 597.74
B01A+B   BTRM: CB00, 1075, 597.91
VB1   YCOR: CB00, 1076, 598.26
B01B   BEND: CB00, 1080, 603.10

QM3A   QUAD: CB00, 1080, 614.38

X-Chromatic correction section begins
H2C   XCOR: CB00, 1090, 828.58
V2C   YCOR: CB00, 1090, 830.16
QN3A   QUAD: CB00, 1100, 832.02
SF1A   SEXT: CB00, 2010, 835.54,
QN3B   QUAD: CB00, 2020, 835.66

QN2A   QUAD: CB00, 2030, 854.92

VACV: CB02, 1040, 576.74
VACP: CB02, 1040, 577.47
BPMB: CB00, 1040, 576.91

BPMB: CB00, 1060, 585.46
VACG: CB02, 1065, 586.67

BBCFT01

Laser station: 597.90

Laser alignment pipe

PCOL: CB02, 1090, 612.80
IONC: CB02, 1090, 612.78
BPMB: CB00, 1090, 614.38

PROF: CB00, 1090, 618.63   PR 620

VACP: CB02, 1090

STPR: CB00, 1090, 823.88
STEP: CB00, 1090, 826.89
STEP: CB00, 1091, 826.89
IONC: CB02, 1090, 827.10

BPMB: CB00, 1100, 832.02

BPMB: CB00, 2020, 835.66

VACG: CB02, 2020, 840.00

Laser station, 851.50
VACP: CB02, 2020, 852.00
BPMB: CB00, 2030, 854.92

B01C   BEND and BTRM: CB00, 2030,   ○ BSCFTB02
                 660.96

B01D   BEND: CB00, 2035, 670.68

                             MASK: CB00, 2040, 675.83
      XCOR: CB00, 2040, 676.75
QN1   QUAD: CB00, 2040, 676.75
                             BPMB: CB00, 2040, 676.75
      YCOR: CB00, 2040, 676.75
      YCOR: CB00, 2045, 676.17

B01E   BEND and BTRM : CB00,
              2050, 683.13

                             Wire table, 687.8

B01F   BEND: CB00, 2060, 692.55

                             MASK: CB00, 2070, 697.67
QN2B   QUAD: CB00, 2070, 698.59   BPMB: CB00, 2070, 698.59

                             Laser station, 703.56

Fermilab Collimator
COL 2077 (Top)   YMOV: CB02, 2077   COL 2075 (North)
COL 2076 (South)   XMOV: B02, 2076   XMOV: CB02, 2075   COL 2074 (Bottom)
Beta exchanger section begins ➡   YMOV: CB02, 2076
                               IONC: CB02, 2080, 716.26
QN3C   QUAD: CB00, 2080, 717.54   PCOL: CB00, 2080, 716.27
                               BPMB: CB00, 2080, 717.54
SPIB   SEXT: CB50, 3010, 719.67
QT1   QUAD: CB00, 3020, 721.49   BPMR: CB00, 3020, 721.49
V2D   YCOR: CB00, 3020, 722.96
H2D   XCOR: CB00, 3020, 723.90

                             VACP: CB02, 3020, 727.06   VP 727

QT2A   QUAD: CB00, 3030, 732.58   BPMB: CB00, 3030, 732.58
QT2B   QUAD: CB01, 3040, 734.75   BPMB: CB01, 3040, 734.75

                             BPMB: CB01, 3041, 737.86
                             WIRE: CB02, 3042, 739.66   WS2
                             BPMB: CB01, 3042, 741.48
H3C   XCOR: CB01, 3042, 743.81
V3CA   YCOR: CB01, 30454747.87

WIRE: CB02, 3046, 749.03, — WS3
YCOR: CB01, 3046, 750.90 — V3CD
BPM8: CB01, 3049, 760.84
YCOR: CB01, 3047, 750.08 — V3CB

PCOL: CB02, 3050, 757.24
IONC: CB02, 3050, 757.77
QUAD: CB01, 3050, 758.82 — QT3
BPM8: CB01, 3050, 758.82
YCOR: CB01, 3050, 758.82
XCOR: CB01, 3050, 758.82

Laser station, 770.00

Y-Chromatic correction section begins ➤

VACV: CB02, 3050, 776.00
VACG: CB02, 3050, 777.00
VACG: CB02, 3051, 777.00
XCOR: CB01, 3051, 780.31, — H4C
YCOR: CB01, 3052, 781.89 — V4C
IONC: CB02, 3051, 780.00
QUAD: CB01, 3060, 783.75 — QT4
BPM8: CB01, 3060, 783.75
SEXT: CB01, 4010, 785.57 — SD1A
QUAD: CB01, 4020, 787.39 — QM3B
BPM8: CB01, 4020, 787.39

VACP: CB02, 4020, 802.00 — VP802

QUAD: CB01, 4030, 806.86 — QM1A
BPM8: CB01, 4030, 806.86

BEND: CB00, 4040, 812.89 — B02A

BTRM: CB01, 4045, 817.40 — B02A+B
Wire table, 817.40 — WT3

BEND: CB00, 4050, 822.11 — B02B
Laser station, 817.40

WSDS: CB02, 4050, 827.53
MASK: CB02, 4050, 827.81
IONC: CB02, 4050, 827.81
QUAD: CB01, 4060, 828.46 — QM2+
BPM8: CB01, 4060, 828.46
YCOR: CB01, 4061, 829.69 — VB4

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B02C   BEND: CB00, 4070, 834.85

B02C, D   BTRM: CB01, 4075, 839.56

B02D   BEND: CB00, 4080, 844.28

    MASK: CB02, 4080, 849.40

QM1B   QUAD: CB01, 4090, 850.32   IONC: CB02, 4090, 849.40

    BPMS: CB01, 4090, 850.32

Final transformer section begins ➝

QM3C   QUAD: CB01, 4100, 869.58   BPMS: CB01, 4100, 869.58

SD1B   SEXT: CB01, 5010, 871.40   IONC: CB02, 5010, 870.00

QM3D   QUAD: CB01, 5020, 873.22   Laser station, 872.51

    BPMS: CB01, 5020, 873.22

    VACP: CB02, 5020, 877.00

    VACG: CB02, 5020, 895.00

    PCOL: CB02, 5030, 897.63

    IONC: CB02, 5030, 898.65

    BPMS: CB01, 5021, 899.40

V5D   YCOR: CB01, 5020, 899.83

QM1C   QUAD: CB01, 5030, 903.41   BPMS: CB01, 5030, 903.41

V5C   YCOR: CB02, 5030, 905.75

H5C   XCOR: CB02, 5060, 913.

    YCOR: CB02, 5050, 915.02

    XCOR: CB02, 5050, 915.02

QC5   QUAD: CB02, 5050, 915.02   BPMS: CB02, 5050, 915.02

    Laser station, 5060, 915.60

B02E   BEND: CB00, 5060, 921.72

VB5   YCOR: CB02, 5060, 926.58

    Wire table, 926.80

B02E, F   BTRM: CB02, 5065, 926.91

H5D   XCOR: CB02, 5066, 927.04

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B02F   BEND: CB00, 5070, 932.10

IONC: C500;5061, 933.00   LION1-N

WSCS: CB02, 5060, 937.22

B03A   BEND: CB02, 5080, 941.55   LION2-S

IONC: C500: 5061, 953.00
IONC: CB02, 5100, 956.28

B03B   BEND: CB02, 5090, 951.01

WSCS: CB02, 5100, 956.45
MASK: CB02, 5100, 956.28
QC4   QUAD: CB02, 5100, 957.20   BPMS: CB02, 5100, 957.20

VACP: CB02, 5100, 960.00   VP960

SK1   SEXT: CB02, 5110, 974.02   IONC: CB02, 5110, 973.56
PCOL: CB02, 5110, 973.23   PC6

SX1   SEXT: CB02, 5120, 975.00

QB3   QUAD: CB02, 5130, 976.16

BSOKI7

QC3   QUAD: CB02, 5140, 992.91   BPMS: CB02, 5140, 992.91

VACV: CB02, 5140, 1050.00

VACG: CB02, 5140, 1000.32
VACG: CB02, 5141, 1000.32
SK2   SEXT: CB02, 5148, 1005.87   VACP: CB02, 5140, 1002.00

SX2   SEXT: CB02, 5150, 1006.66

H6C   XCOR: CB02, 5150, 1007.91   Laser station, 1004.50

QC2   QUAD: CB02, 5160, 1012.93   VACG: CB02, 5160, 1006.17

QTRM: CB02, 5161, 5162, 5163, 5164, 1012.93   BPMS: CB02, 5160, 1012.93

V6C   YCOR: CB02, 5160, 1017.64   VACP: CB02, 5170, 1015.00

H6D   XCOR: CB02, 5160, 1017.64   PCOL: CB0002, 5170, 1015.16

V6D   YCOR: CB02, 5170, 1018.73   IONC: CB02, 5170, 1015.61

QX1   QUAD: CB02, 5170, 1019.88
QTRM: CB02, 5171, 5172, 5173, 5174, 1019.88

Dump line section begins

WIRE: CB02, 5021, 1025.53 KEK beam size

QC1 — QUAD: CB02, 5180, 1022.69 QTRIM:CB02, 5181, 5182, 5183, 5184

WIRE: CB02, 5031, 1025.69 monitor
SIZE: CB02, 5201, 1027.54
WIRE: CB02, 5199, 1025.69 Ozwy beam size
WIRE: CB02, 5250, 1026.60 monitor

FP

QP1A — QUAD: CB02, 6010, 1030.69

WIRE: CB02, 5201, 1029.196
VACV: CB02, 5205, 1029.33
BPMS: CB02, 6010, 1030.69

QP1AH, QP1AV — XYCOR: CB02, 6010, 1031.6
QP1B — QUAD: CB02, 6020, 1032.56
QP2A — QUAD: CB02, 6030, 1034.44
QP2AH, QP2AV — XYCOR: CB02, 6030, 1035.45
QP2B — QUAD: CB02, 6040, 1036.34

IONC: CB02, 5200, 1028.00, LION5 N

QP3A — QUAD: CB02, 6050, 1039.40
QP3AH — XCOR: CB02, 6050, 1039.40
QP3B — QUAD: CB02, 6060, 1043.34

IONC: CB02, 5200, 1028.00, LION5 S

QP4 — QUAD: CB02, 6070, 1047.27

VACP: CB02, 6070, 1049.00

H7C — XCOR: CB02, 6070, 1049.66
V7C — YCOR: CB02, 6070, 1051.13
QP5 — QUAD: CB02, 6080, 1055.66

BPMS: CB02, 6080, 1056.46

B04A — BEND: CB02, 6100, 1059.48 YCOR: CB02, 6100, 1059.

Wire table, 1055.60
Laser station, 1056.60

B04B — BEND: CB02, 6110, 1063.22 YCOR: CB02, 6110, 1063.22

IP

VACP: CB02, 6110, 1066.5
INPO: CB02, 6110, 1066.99
AMPL: CB02, 6110, 1066.76, Rf monitor

B05A — BEND: CB02, 6120, 1070.78 YCOR: CB02, 9000, 1070.78

B05B — BEND: CB02, 6130, 1074.57 YCOR: CB02, 6130, 1074.57

VACP: CB02, 6130, 1076.00
BPMS: CB02, 6130, 1077.40
PCOL: CB02, 6130, 1077
IONC: CB02, 6140, 1080.15   PC7

B06A — BEND: CB02, 6140, 1080.15

B06B — BEND: CB02, 6150, 1084.08

IONC: CB02, 6150, 1084.08

B06C — BEND: CB02, 6160, 1087.24

B06D — BEND: CB02, 6151, 1090.57

Calorimeter

B06E — BEND: CB02, 6152, 1094.08

PPS gate

B06F — BEND: CB02, 6163, 1097.52
Calorimeter

IP

VACG: CB02, 6160, 1100.00
VACG: CB02, 6161, 1100.00
VACP: CB02, 6160, 1104.00
INPO: CB02, 6160, 1104.15

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BPMS: CB02, 5150, 1107.12

VACG: CB02, 6160, 1100.00

IONC: CB02, 6166, 1116.00, LION4S

VACV: CB02, 6160, 1111.00

IONC: CB02, 6166, 1116.00, LION3N

Laser station, 1132.00

BPMS: CB02, 6167, 1153

VACP: CB02, 6170, 1155.00

VACG: CB02, 6170, 1155.00

IONC: CB02, 6170, 1196.0

PC6

TORO: CB02, 6171, 1198.50

BPMS: CB02, 6170, 1200.37

WIRE: :CB02, 6180, 1202.22

PROF: CB02, 6200, 1204.0 Fixed screen

FFTB Dump

IC6   IONC: CB02, 6300, 1216.49

DUMP: CB00, 6300, 1216.49

DM

DMON: CB02, 6300, 1220.0

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Appendix B Typical Electron Beam Parameters

Number of electrons per bunch	$1.8\text{-}2.0\text{x}10^{10}$
Bunch Energy	28.5 GeV
Gamma	55773
Bunch Radius	50 µm
Bunch Length	0.7 mm
	2.3 ps
Normalized Emittance x	$5\text{x}10^{-5}$ m rad
Normalized Emittance y	$0.5\text{x}10^{-5}$ m rad

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