

# T-Violation in $K^+ \rightarrow \pi^0 \mu^+ \nu$ at KEK

J. Imazato  
(E246 collaboration)

XXVI SLAC Summer Institute  
Topical Conference

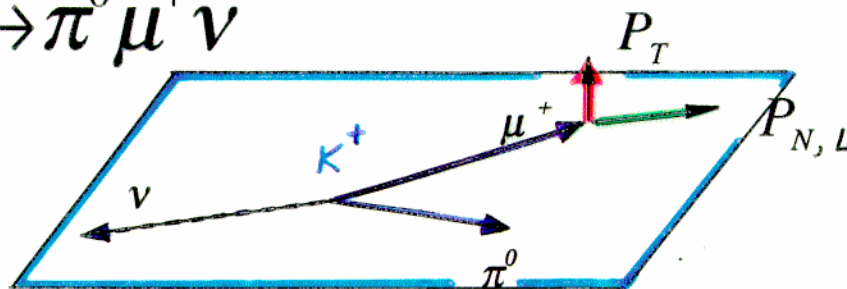
August 14, 1998

1. Transverse polarization in  $K^+ \rightarrow \pi^0 \mu^+ \nu$  ( $K_{\mu 3}$ )
2. KEK-PS E246 experiment
3. Preliminary result from 1996-97 data

## E246 Collaboration

Japan	KEK Univ. of Tsukuba Tokyo Institute of Technology Univ. of Tokyo Osaka Univ.
Russia	Institute for Nuclear Research
Canada	TRIUMF Univ. of British Columbia Univ. of Saskatchewan Univ. of Montreal
Korea	Yonsei Univ. Korea Univ.
U.S.A.	Virginia Polytech Institute Princeton Univ.
Taiwan	National Taiwan Univ.

# Transverse $\mu^+$ polarization in $K^+ \rightarrow \pi^0 \mu^+ \nu$



$$P_T = \vec{\sigma}_\mu \cdot (\vec{p}_\mu \times \vec{p}_{\pi^0})$$

**T-odd correlation**

$P_T^{\text{spurious}}$  (Final State Interaction)  $\approx 10^{-6}$  (Zhitnitskii, 1980)

$P_T \neq 0 (> 10^{-6}) \rightarrow$  T-violation

## Decay amplitude of $K_{\mu 3}$ and $P_T$

$$M = \frac{G_F}{2} \sin\theta_c [ \underline{f_+(q^2)} (p_K^\lambda + p_\pi^\lambda) + \underline{f_-(q^2)} (p_K^\lambda - p_\pi^\lambda) ] \cdot [u_\mu \gamma_\lambda (1 - \gamma_5) u_\nu]$$

$$\underline{\xi(q^2)} = \underline{f_-(q^2)} / \underline{f_+(q^2)}$$

$$P_T = \text{Im} \underline{\xi} \frac{m_\mu}{m_K} \frac{|p_\mu|}{\{ E_\mu + |p_\mu| n_\mu \cdot n_\nu - m_\mu^2 / m_K \}}$$

$\text{Im} \underline{\xi} \neq 0 \leftrightarrow$  T-violation

# Search for $P_T$ in $K_{\mu 3}$ decay

$$P_T \text{ (Standard Model)} = 0 \rightarrow$$

$P_T \neq 0$  means other sources of CP-violation

- three Higgs doublet models [1,2]
- leptoquark models [1,2]
- some supersymmetric models [3,4]

*may give a sizable contribution to  $P_T$  without conflicting with other experimental constraints.*

$$P_T \approx 10^{-3}$$

## <recent theories>

- [1] R.Garisto and G.Kane; PR D44, 2038 (1991)
- [2] G.Bélanger and C.Q.Geng; PR D44, 2789 (1991)
- [3] M.Fabbrichesesi and F.Vassani; PR D, 5334 (1997)
- [4] G.H. Wu and J.N. Ng; PR D56, 93 (1997)

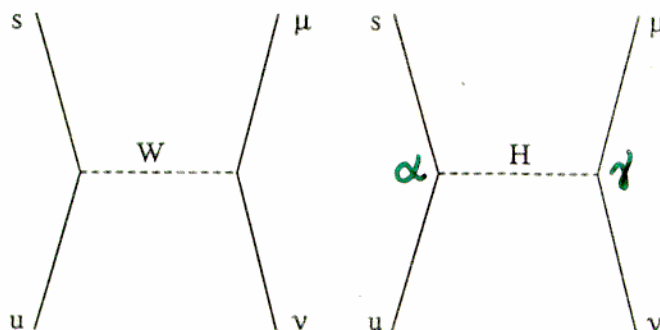
## <Previous data>

	$P_T$	$\text{Im}\xi$	
$K^+ \rightarrow \pi^0 \mu^+ \nu$	$-0.0031 \pm 0.0053$ ( <i>in-flight decay</i> )	$-0.016 \pm 0.025$	BNL-AGS Blatt <i>et al.</i> 1983
$K_L^0 \rightarrow \pi \mu \nu$	$0.0021 \pm 0.0048$ ( $P_T^{\text{spurious}}(\text{FSI}) \approx 0.01$ )	$0.009 \pm 0.030$	BNL-AGS Morse <i>et al.</i> 1979

# Theoretical Models for $P_T$

## (1) Three Higgs doublet model

exchange of  $H^+$

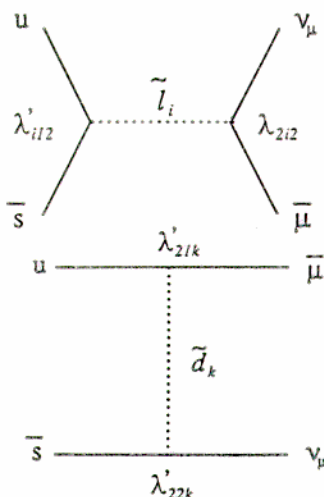


$$\text{Im}\xi^K = -\text{Im}(\gamma_1\alpha_1^*) \cdot \left(\frac{m_K}{m_{H_1^+}}\right)^2 = \text{Im}(\alpha_1\beta_1^*) \cdot \left(\frac{v_2}{v_3}\right)^2 \cdot \left(\frac{m_K}{m_{H_1^+}}\right)^2$$

• constraint on  $\text{Im}(\alpha_1\beta_1^*)$  and  $(v_2/v_3)$

## (2) R-parity violating SUSY

exchange of sleptons and down-type squarks



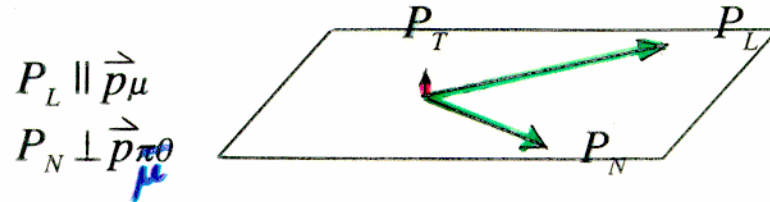
$$\text{Im}\xi^l = \sum_i \frac{\text{Im}[\lambda_{2i2}(\lambda'_{i12})^*]}{4\sqrt{2}G_F \sin\theta_c (m_{\tilde{l}_i})^2} \cdot \frac{m_K^2}{m_\mu m_s}$$

$$\text{Im}\xi^d = \sum_k \frac{\text{Im}[\lambda'_{21k}(\lambda'_{22k})^*]}{4\sqrt{2}G_F \sin\theta_c (m_{\tilde{d}_k})^2} \cdot \frac{m_K^2}{m_\mu m_s}$$

• constraint on  $\text{Im}[\lambda_{2i2}(\lambda'_{i12})^*]$  and  $\text{Im}[\lambda'_{21k}(\lambda'_{22k})^*]$

# How to detect small $P_T$ ?

- *in the presence of large in-plane components  $P_L$  and  $P_N$*
- *by suppressing systematic errors.*



## KEK-PS E246 experiment

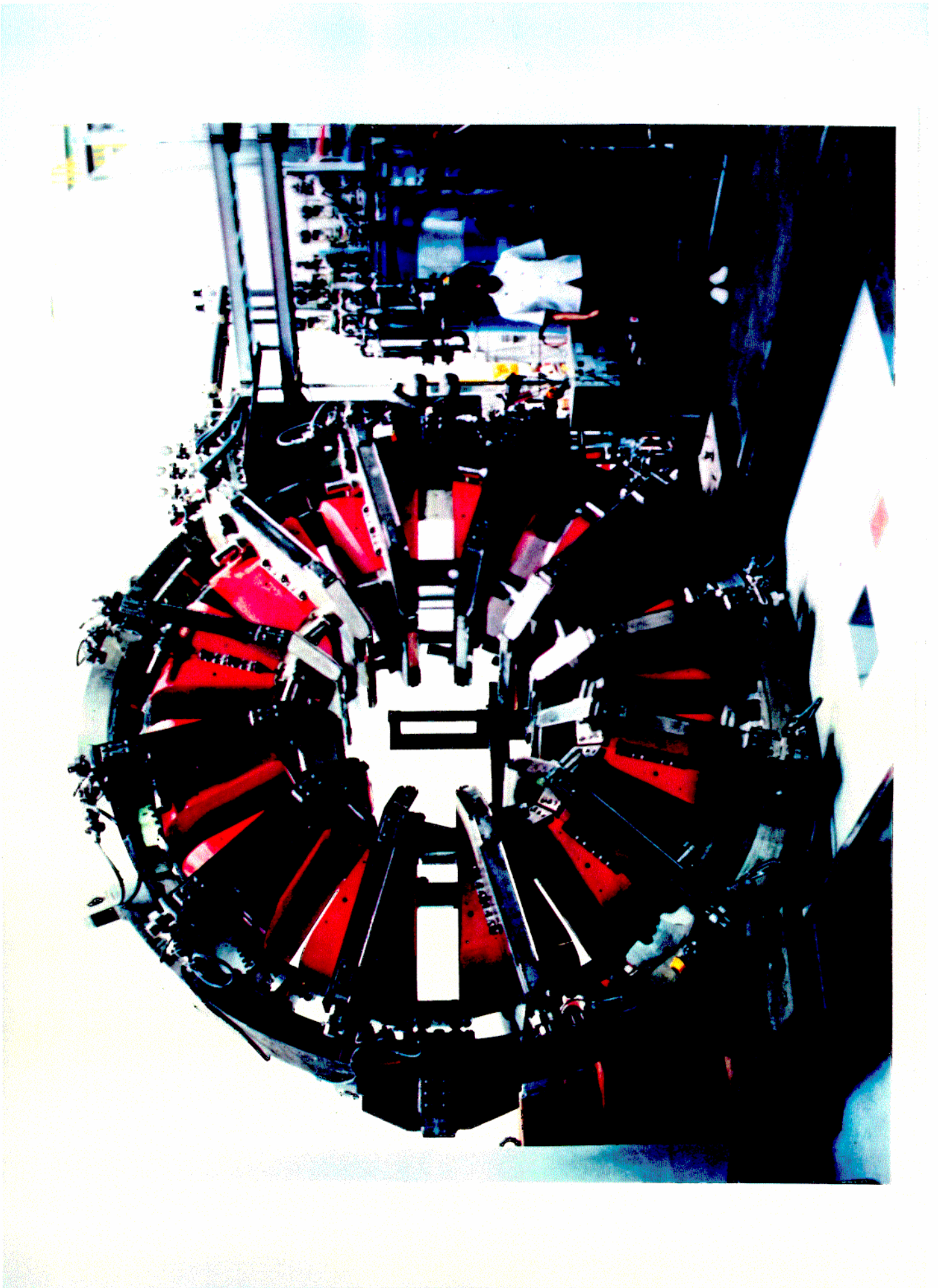
- stopped  $K^+$  method
- Superconducting Toroidal Spectrometer
- $\Delta P_T(\text{stat}) \approx 10^{-3}$ ,  $\Delta P_T(\text{sys}) < \Delta P_T(\text{stat})$

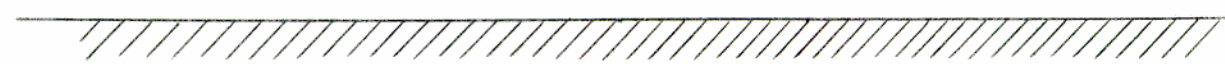
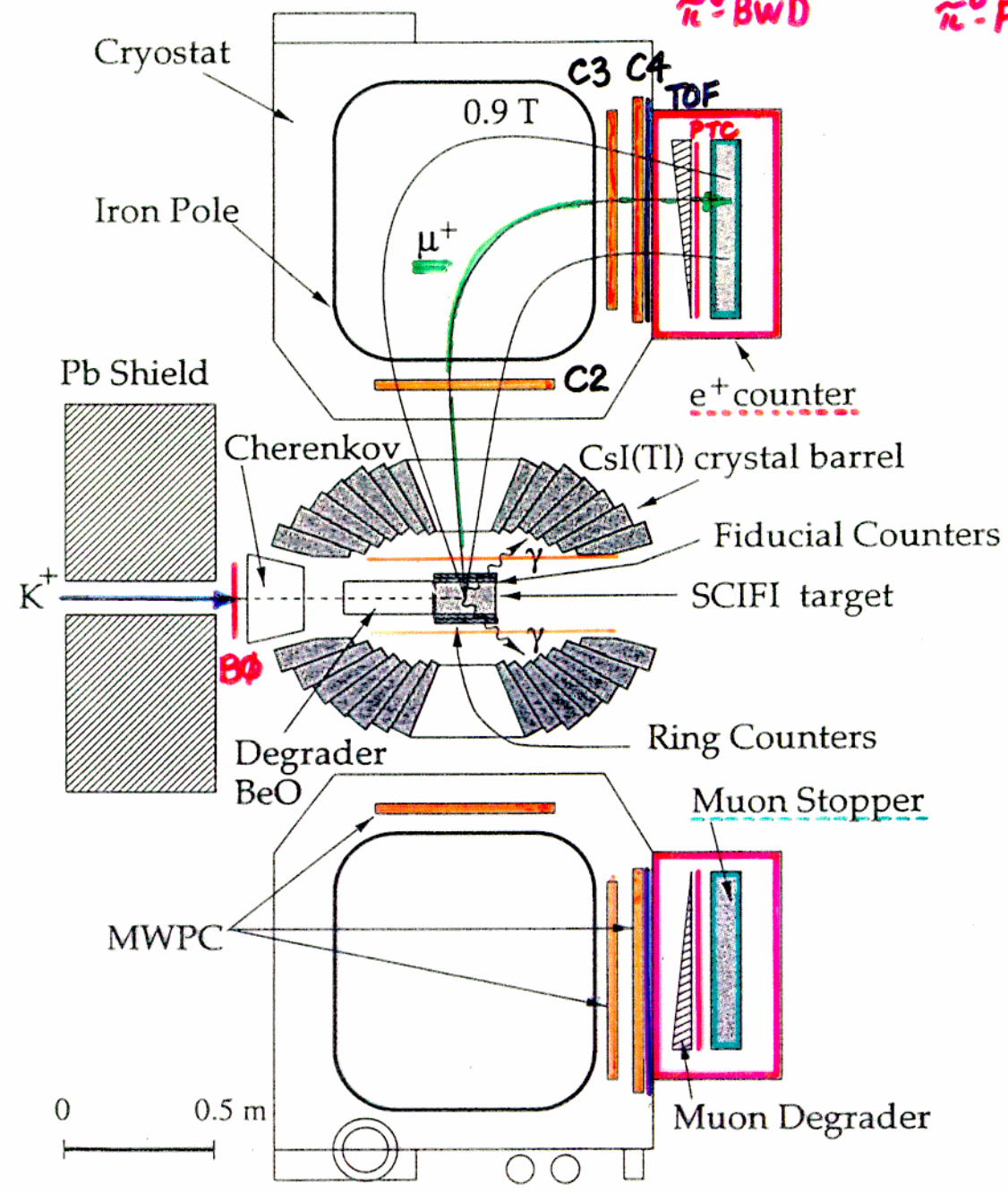
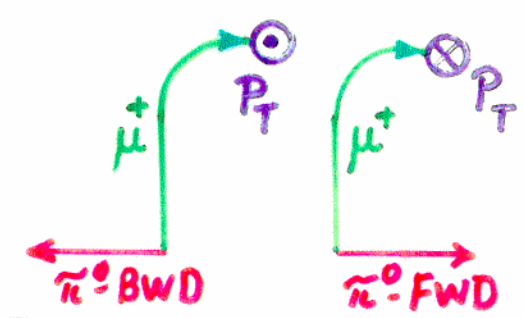
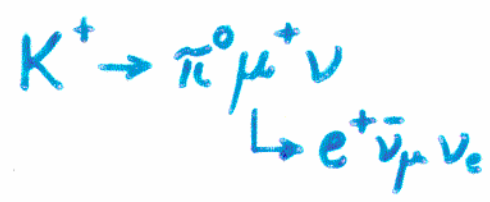
## Advantage of stopped $K^+$ method

- 1) total coverage of decay kinematics
  - double ratio measurement
- 2) detectors located off beam
  - *lower rate and lower background*
- 3) smaller size of setup
  - *controllable systematics*

## Superconducting Toroidal Spectrometer

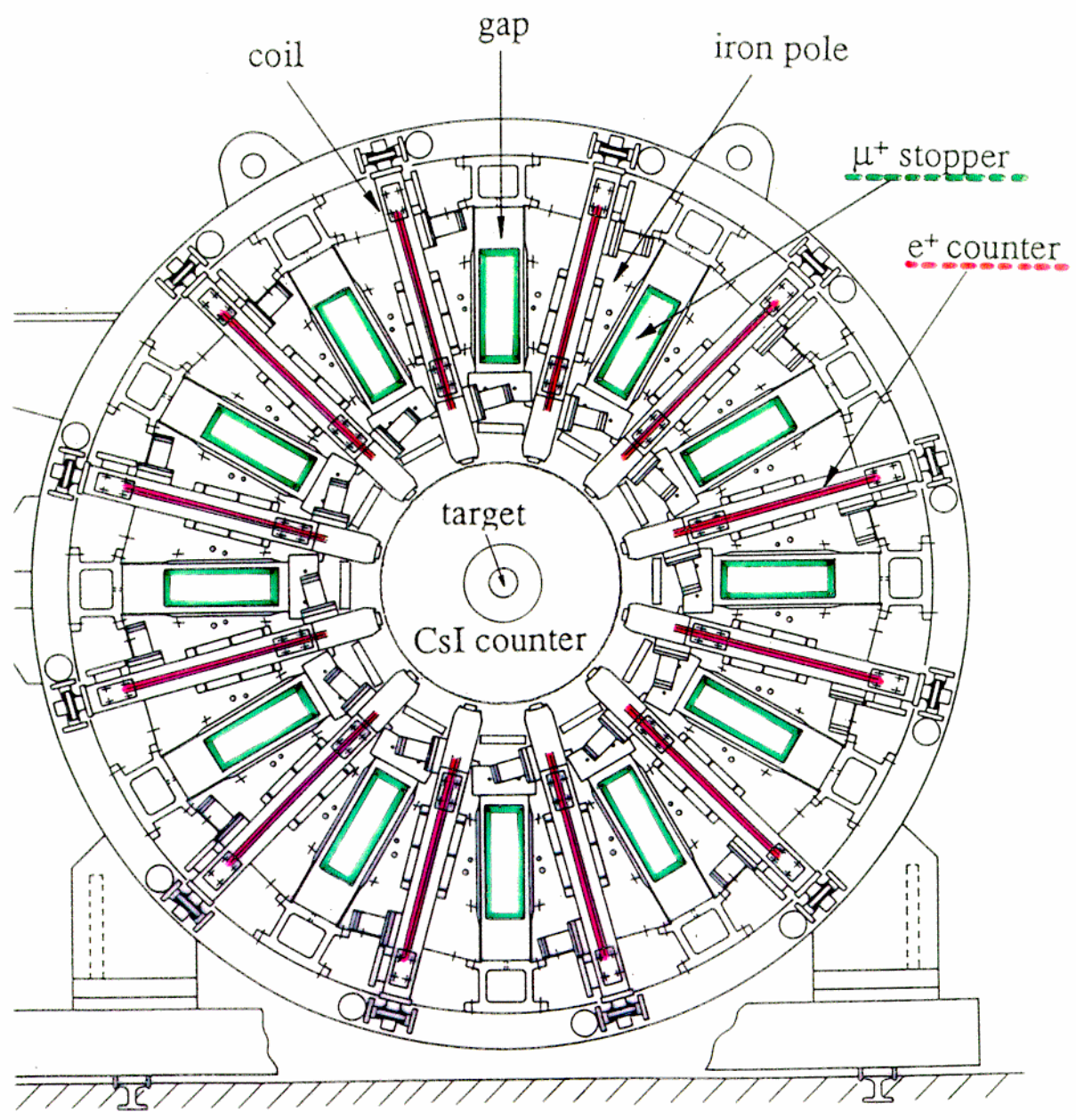
- *large acceptance for stopped decay*
- *high momentum resolution*
- *30° rotational symmetry*





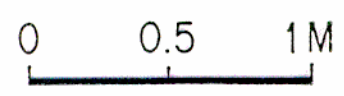


# Superconducting Toroidal Magnet

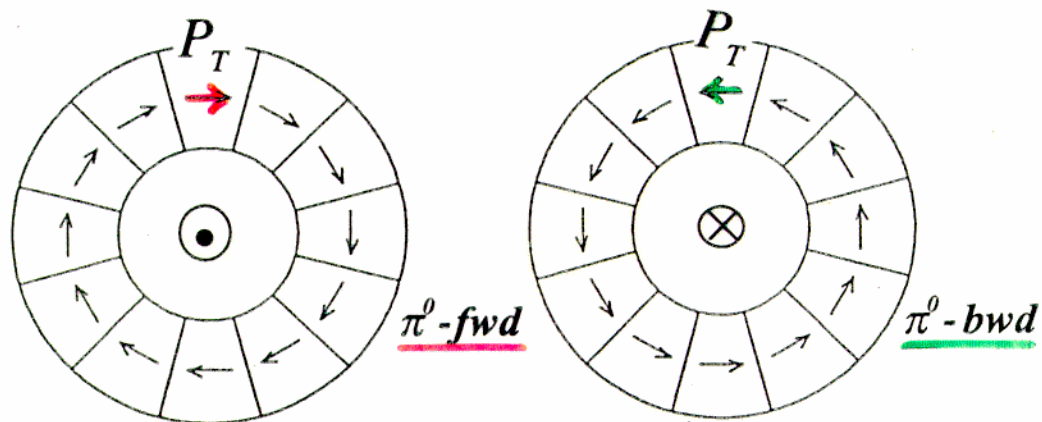


$$\mu^+ \rightarrow e^+ \bar{\nu}_\mu \nu_e$$

$$W(\theta_{e^+}) \sim 1 + A P_\mu \cos \theta_{e^+}$$



# Double ratio experiment E246



$e^+$  cw/ccw asymmetry

$$\frac{\sum_{i=1}^{12} N_i(cw)}{\sum_{i=1}^{12} N_i(ccw)} = 1 \pm 2\alpha \langle \cos\theta_T \rangle P_T$$

$\alpha$  : analyzing power

$\langle \cos\theta_T \rangle$  : kinematical attenuation

• *most of systematics are cancelled by  $\sum_{i=1}^{12}$ .*

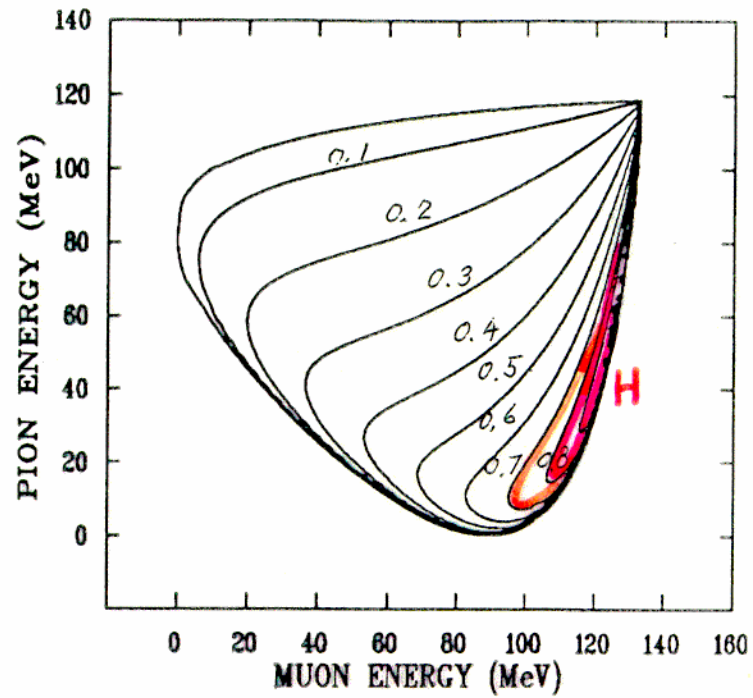
- 1)  $K^+$  stopping distribution in target
- 2)  $e^+$  counter efficiency
- 3) azimuthal distribution of  $\pi^0$  detection efficiency

Ratio of asymmetry between  $fwd$  and  $bwd$

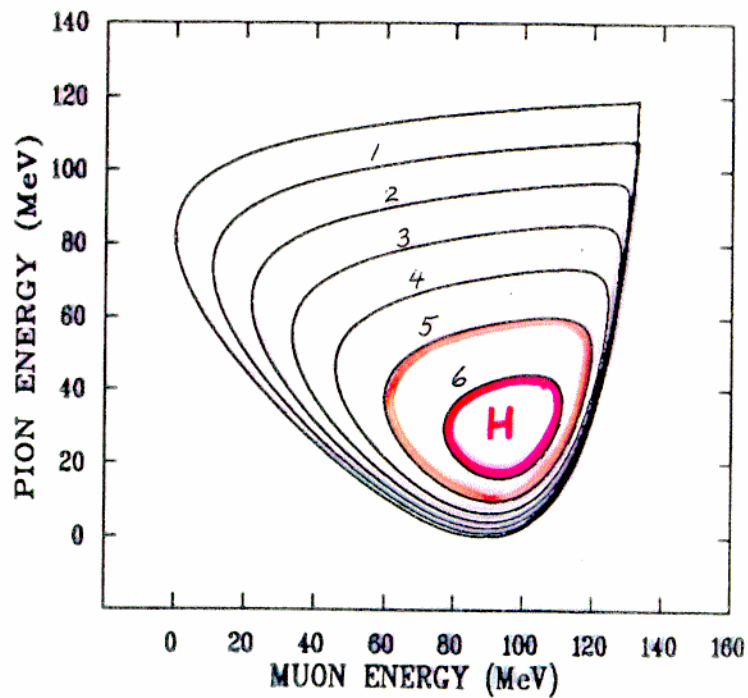
$$\frac{[\sum_{i=1}^{12} N_i(cw) / \sum_{i=1}^{12} N_i(ccw)]_{fwd}}{[\sum_{i=1}^{12} N_i(cw) / \sum_{i=1}^{12} N_i(ccw)]_{bwd}} = 1 + 4\alpha \langle \cos\theta_T \rangle P_T$$

• *most of the systematic errors are cancelled further*

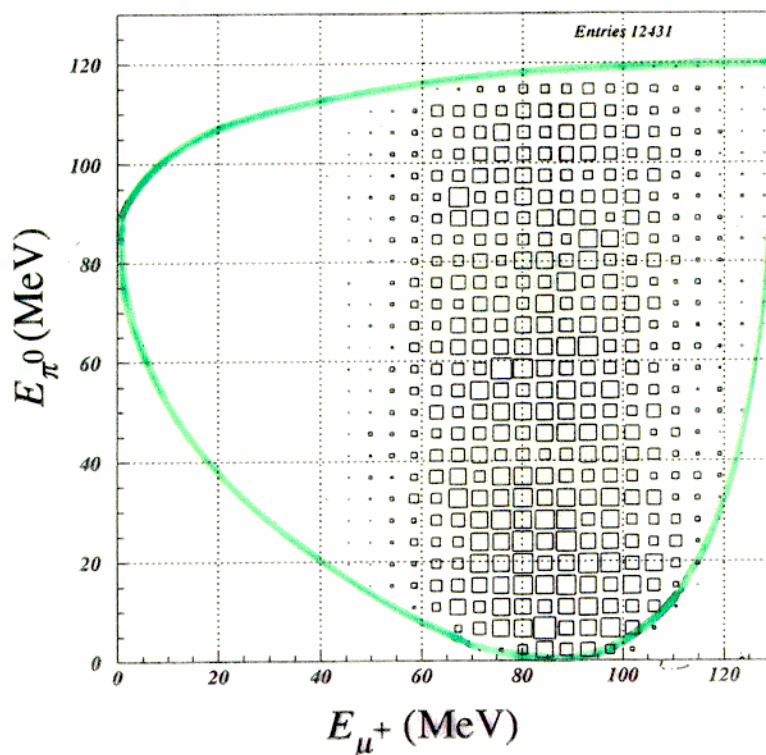
### Sensitivity ( $P_T/Im\xi$ ) distribution



### Figure of Merit ( $P_T/Im\xi \cdot \sqrt{N}$ ) distribution

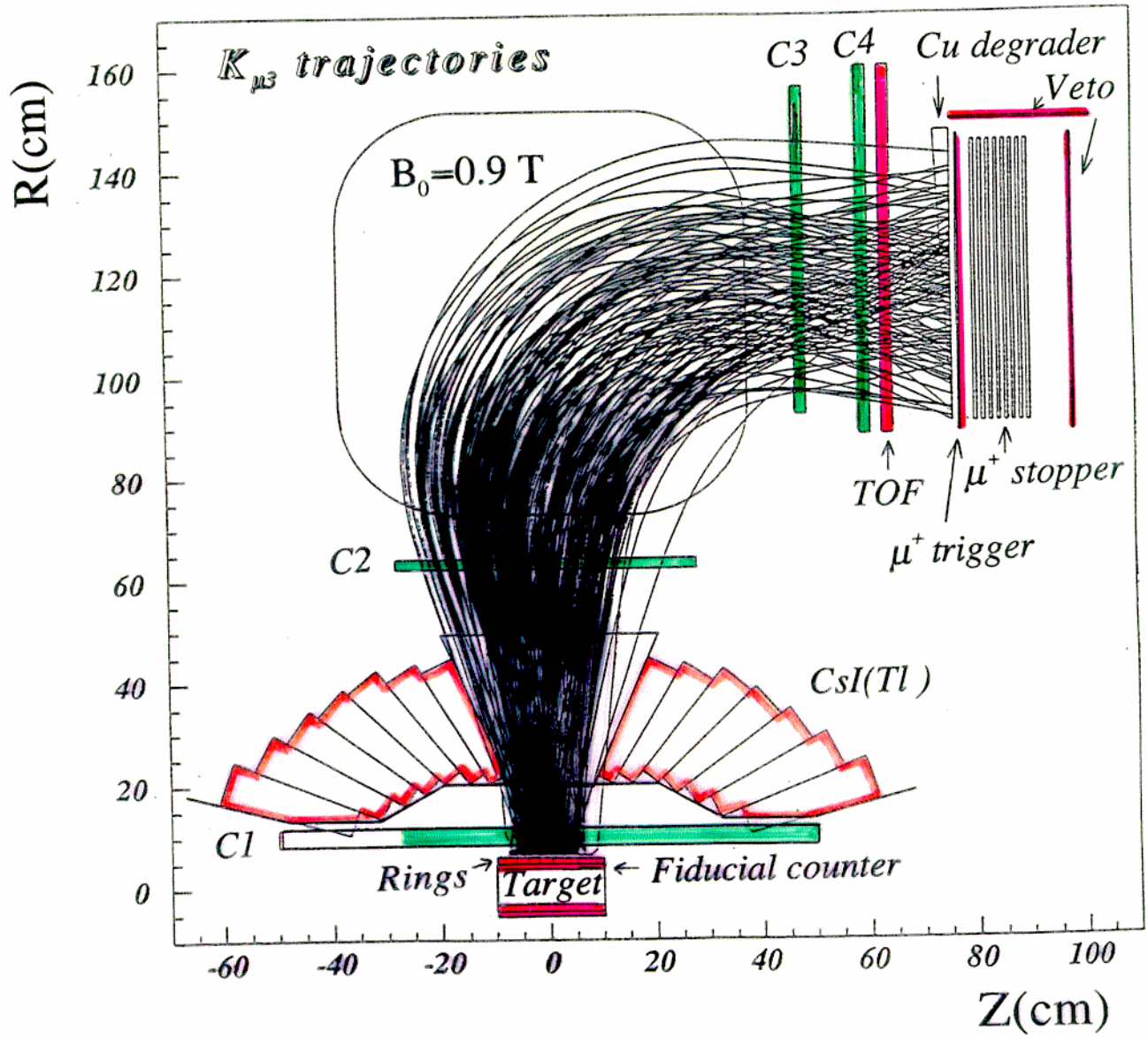


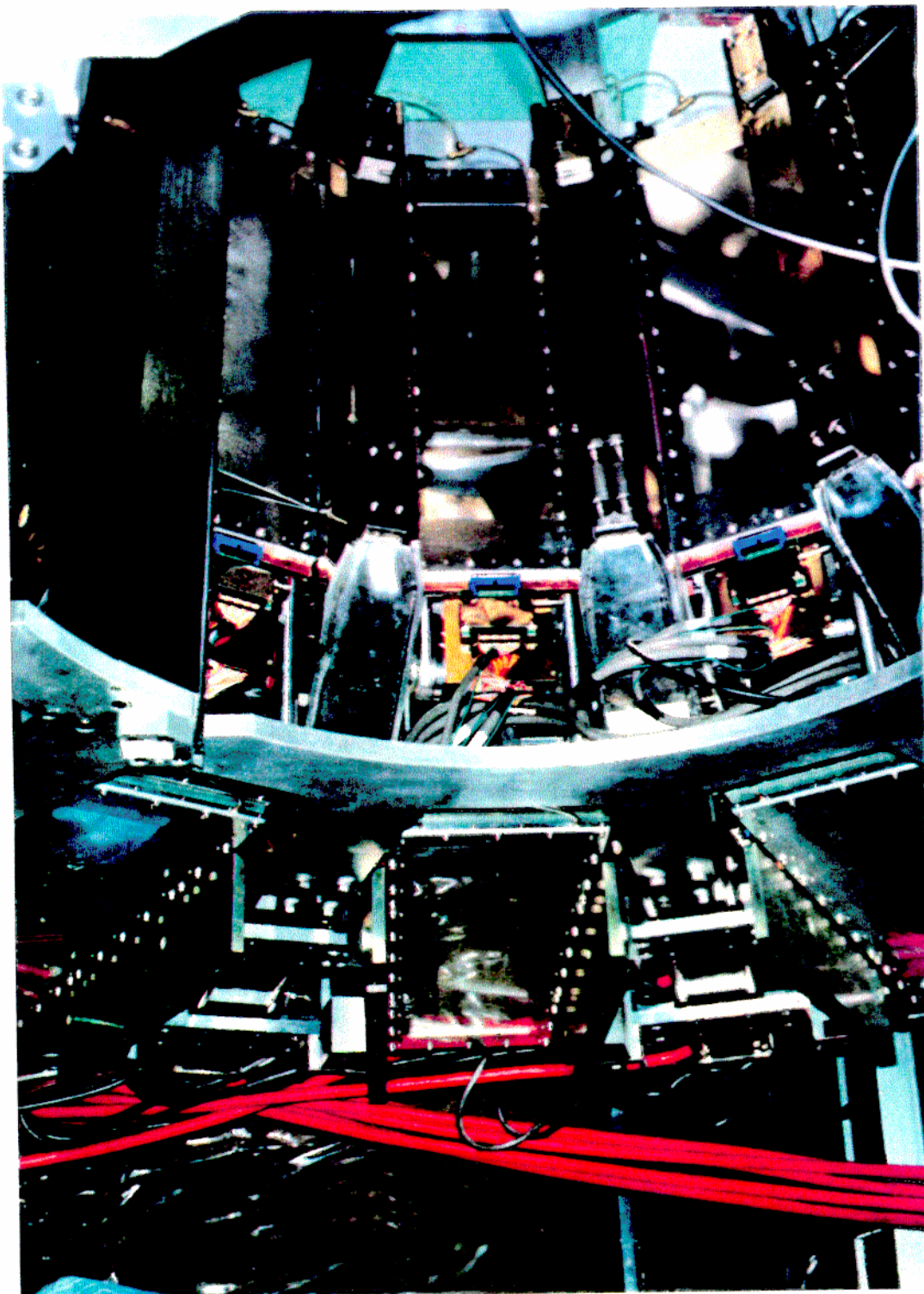
# Detector Acceptance



- $K^+$  beam intensity  $1.0 \times 10^5$  /sec  
@ KEK-PS K5 channel ( 660 MeV/c)
- $K^+$  stopping efficiency 0.40
- $K_{\mu^3}$  branching ratio 0.032
- Detector acceptance
  - spectrometer and  $\mu^+$  stopping 0.022
  - $\pi^0$  detection 0.54
  - $e^+$  detection 0.12
  - data taking 0.8
  - analysis 0.9
- Event rate  $\approx 1.0$  /sec

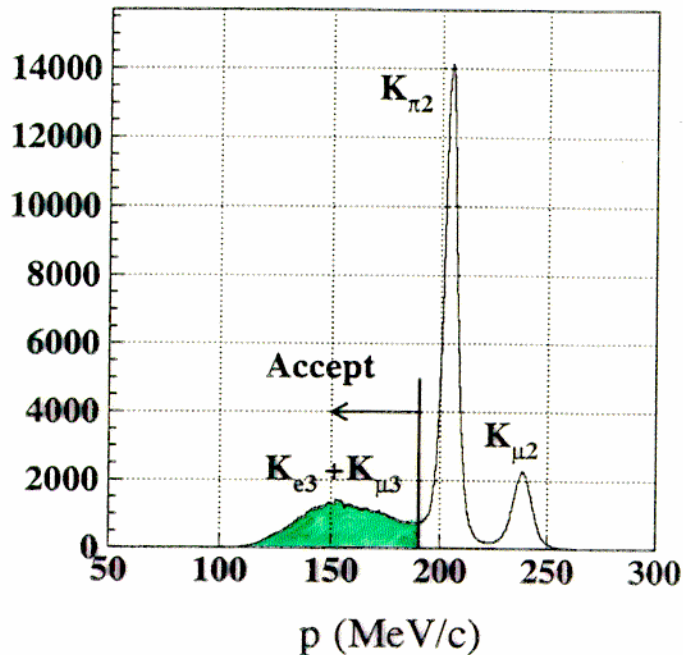
# $\mu^+$ tracking



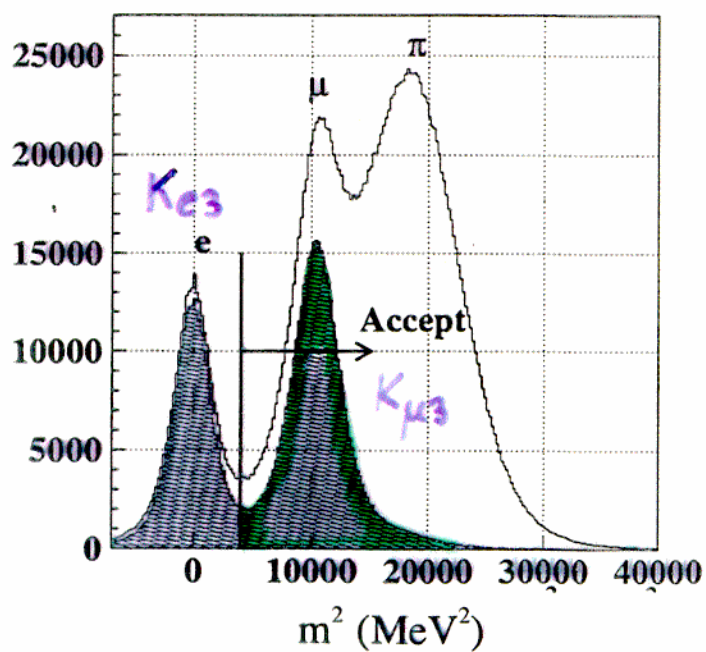


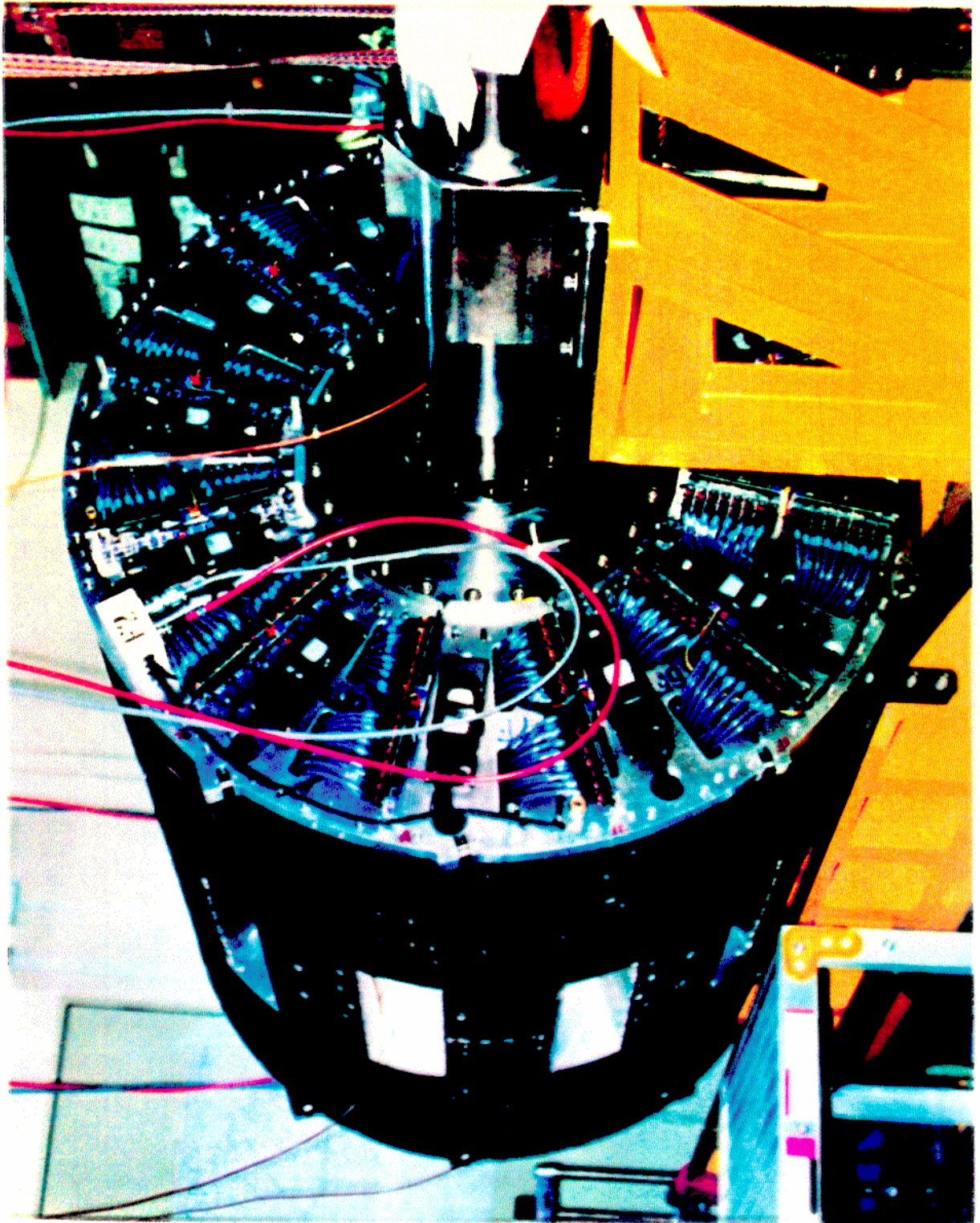
# $\mu^+$ from $K_{\mu 3}$

## Momentum spectrum



## TOF mass spectrum

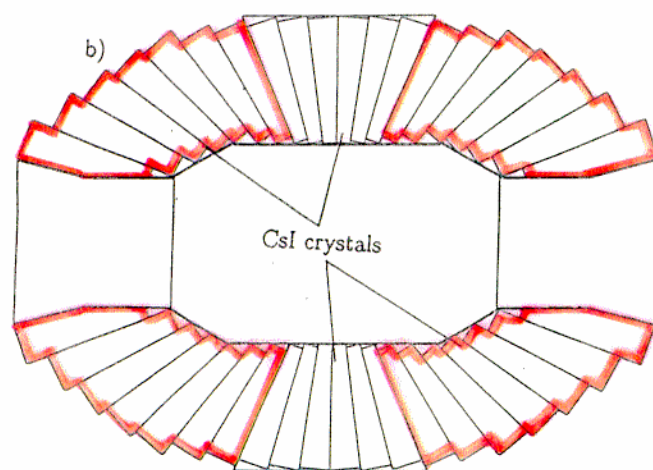
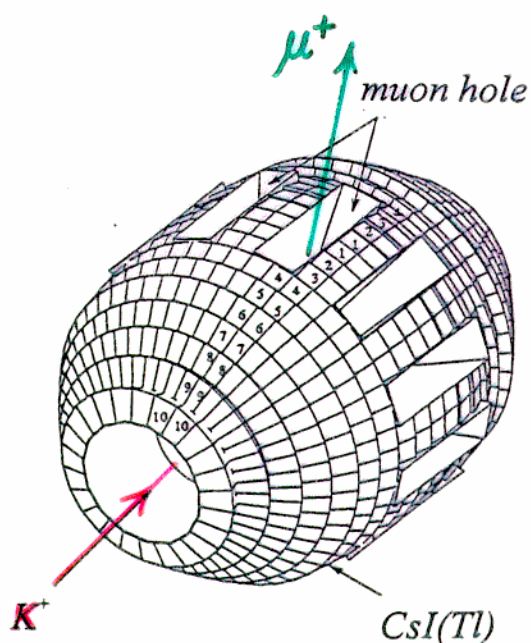




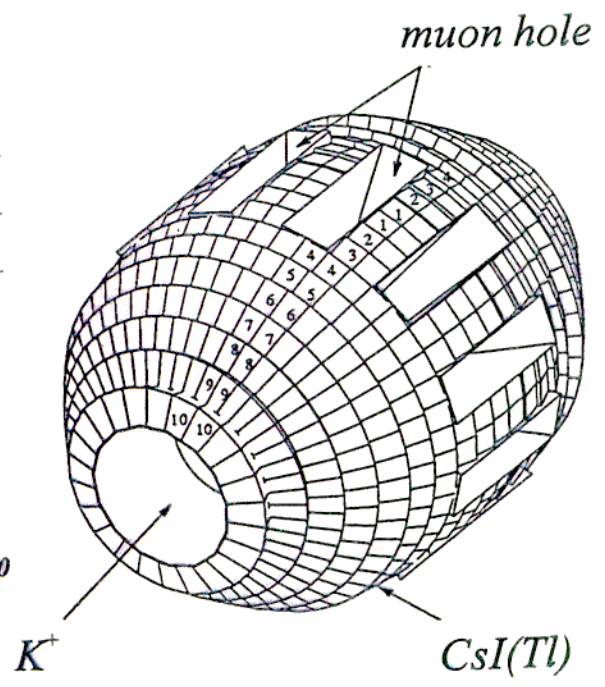
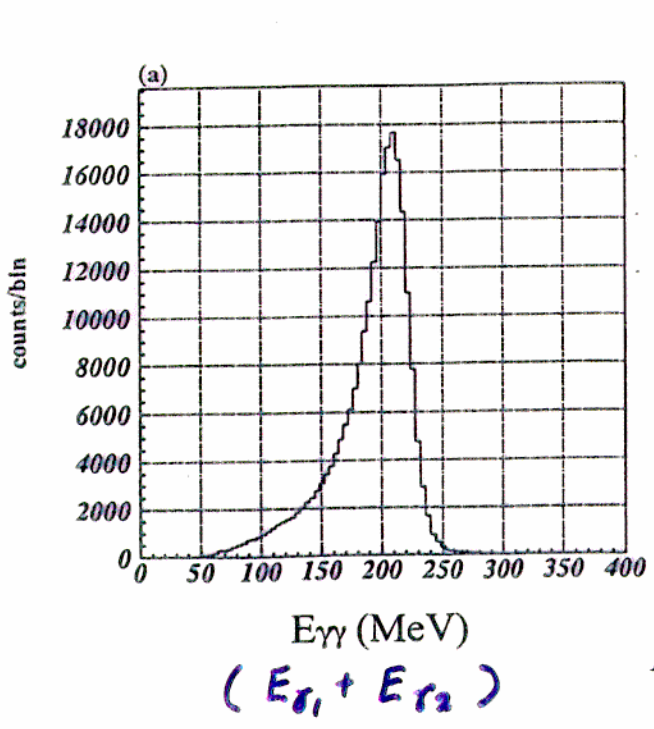
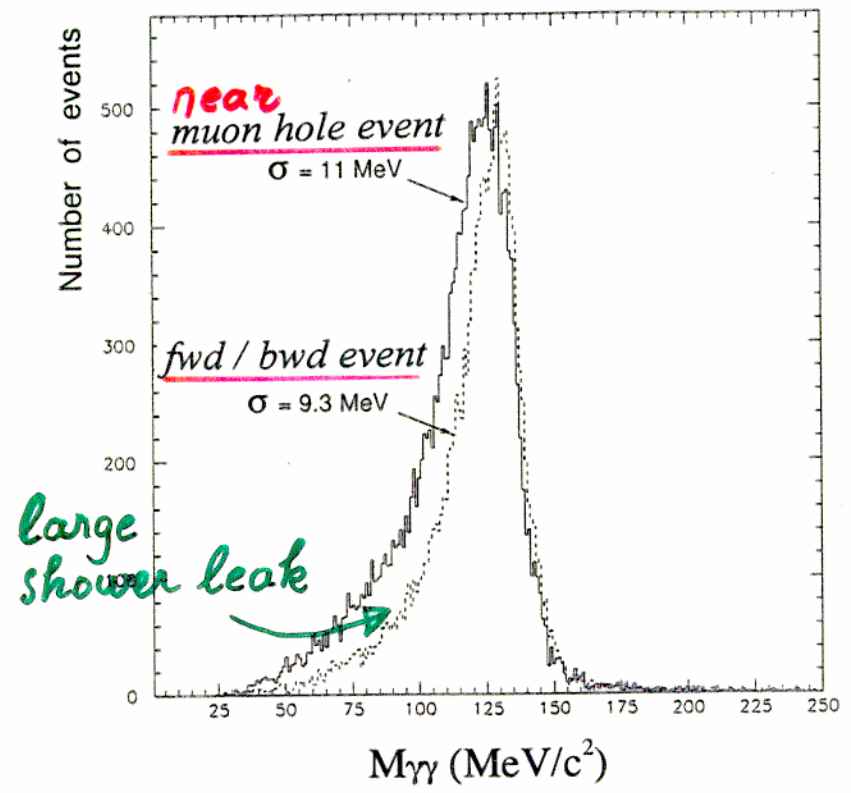


# Main Parameters of CsI(Tl) $\pi^0$ Detector

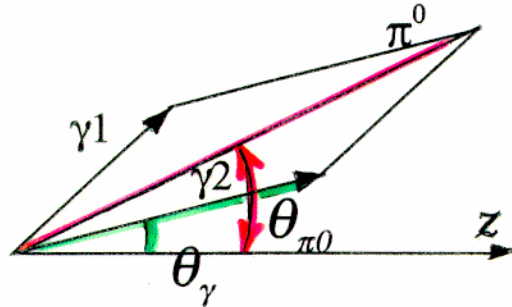
Segmentation	$\Delta\theta = \Delta\phi = 7.5^\circ$
Number of crystals	768
Length of crystals	25 cm (13.5 $X_0$ )
Inner radius	20 cm
Outer radius	50 cm
Solid angle	<u>75 % of <math>4\pi</math></u> $\pi^0 \rightarrow 2\gamma, 1\gamma$
Readout	PIN diode (18x18, 28x28 mm)
<u>Light yield</u>	<u>11000 pe / MeV</u>
<u>Equiv. noise level</u>	<u>65 keV (one module)</u>
Energy resolution	$\sigma_E/E = 3.0 \% @ 200 \text{ MeV}$
Position resolution	$\sigma_p = 1.0 \text{ cm}$
<u>Time resolution</u>	<u><math>\sigma_T = 6.5 \text{ ns}</math> for 10-220 MeV</u>
$\pi^0$ -mass resolution	$\sigma_{\pi^0\text{-mass}} = 14 \text{ MeV}/c^2$



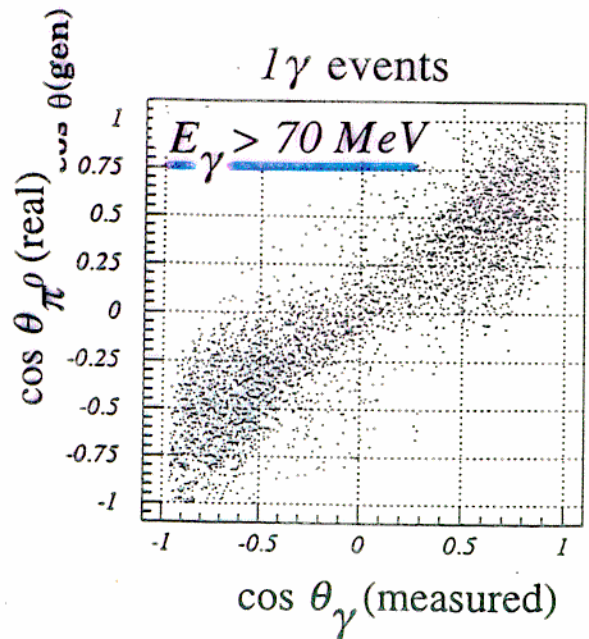
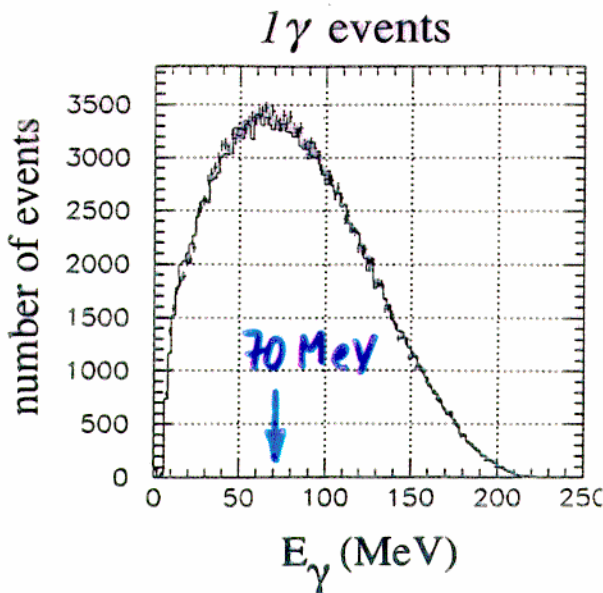
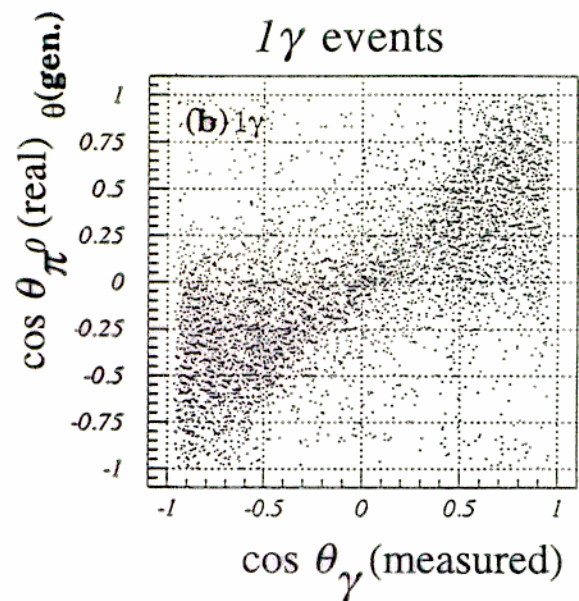
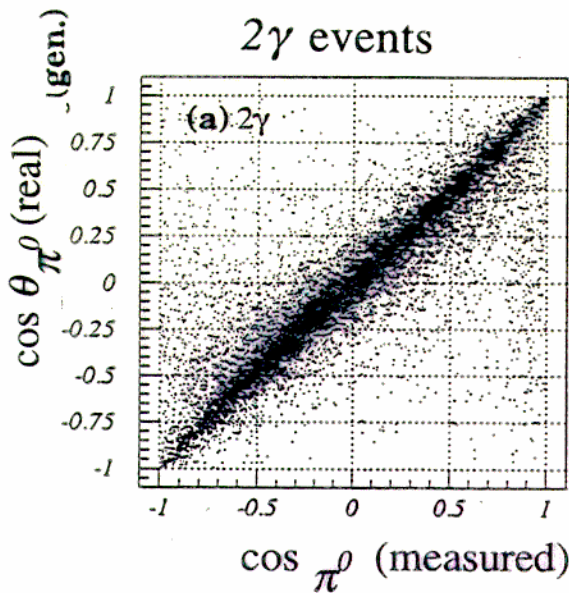
# $\pi^0$ from $K_{\mu 3} - 2\gamma$ events -



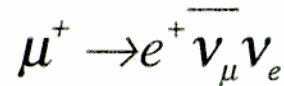
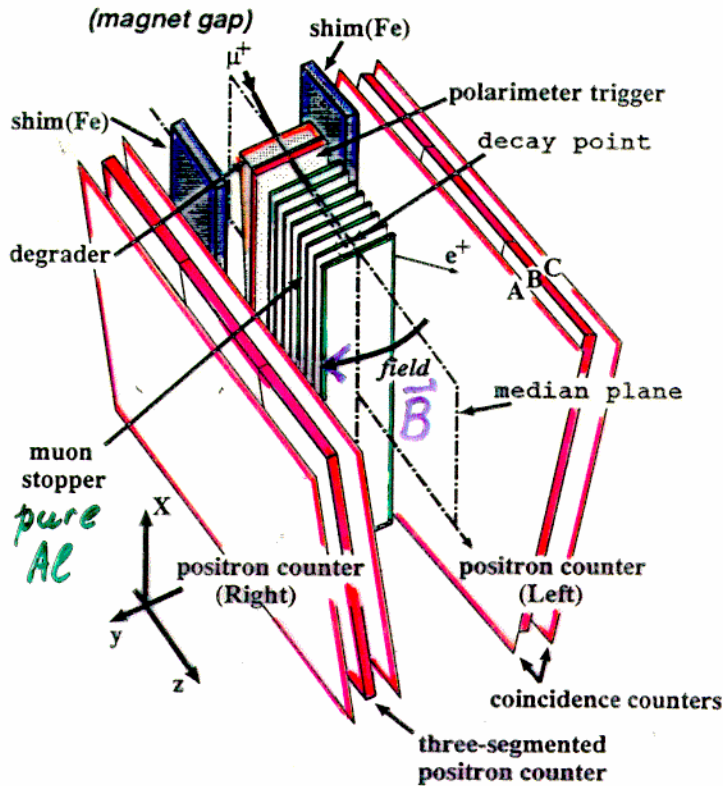
# $\pi^0$ from $K_{\mu 3} - 1\gamma$ events -



- strong correlation between  $\theta_{\pi^0}$  and  $\theta_{\gamma}$
- high sensitivity also in  $1\gamma$  events



# $\mu^+$ Polarimeter



$$\frac{N(cw) - N(ccw)}{N(cw) + N(ccw)} = A_T$$

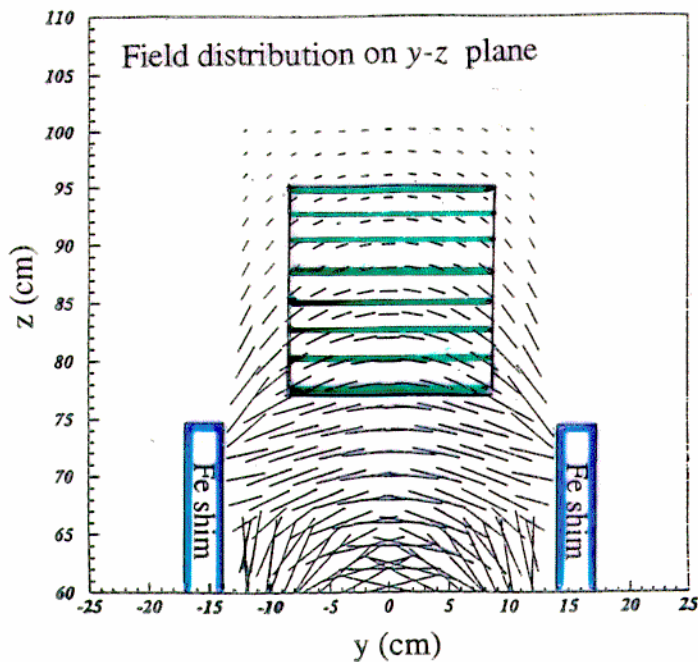
$$P_T = A_T / \alpha \langle \cos \theta_T \rangle$$

$\alpha$  : analyzing power  
 $\langle \cos \theta_T \rangle$  : kinematic attenuation

$\langle P_T \rangle \parallel B \approx 150$  Gauss

$\langle P_T \rangle$  : preserved

$P_L, P_N$  : precess

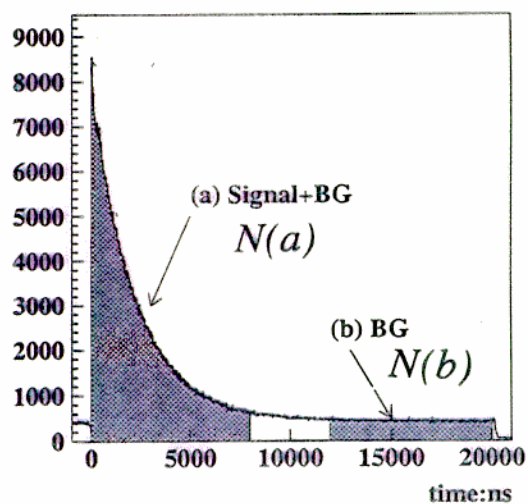
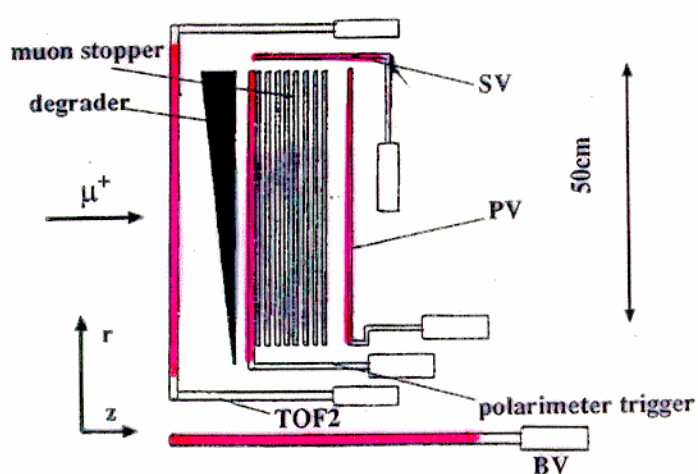
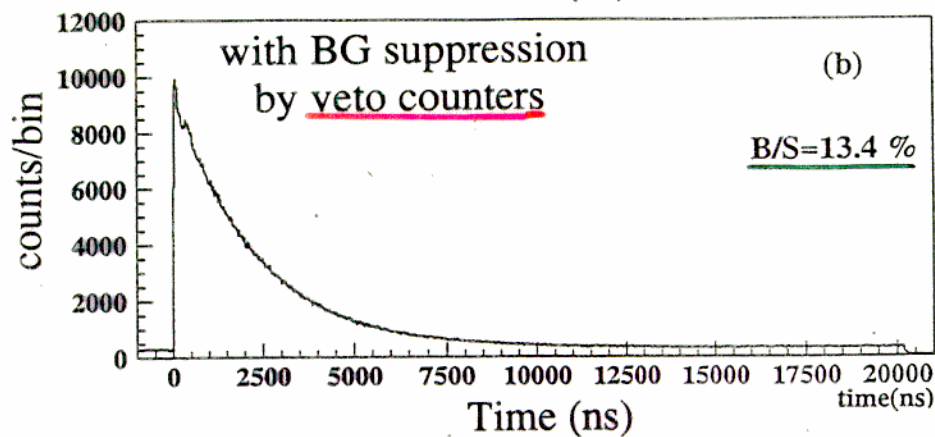
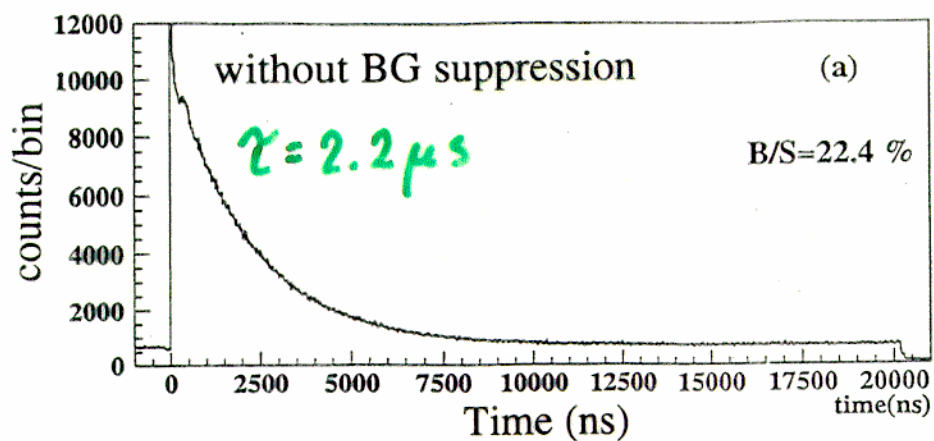


Symmetric field distribution required

- precise field trimming with iron shim plates
- accurate field mapping

Precise alignment of counters and stopper

# $e^+$ time spectrum

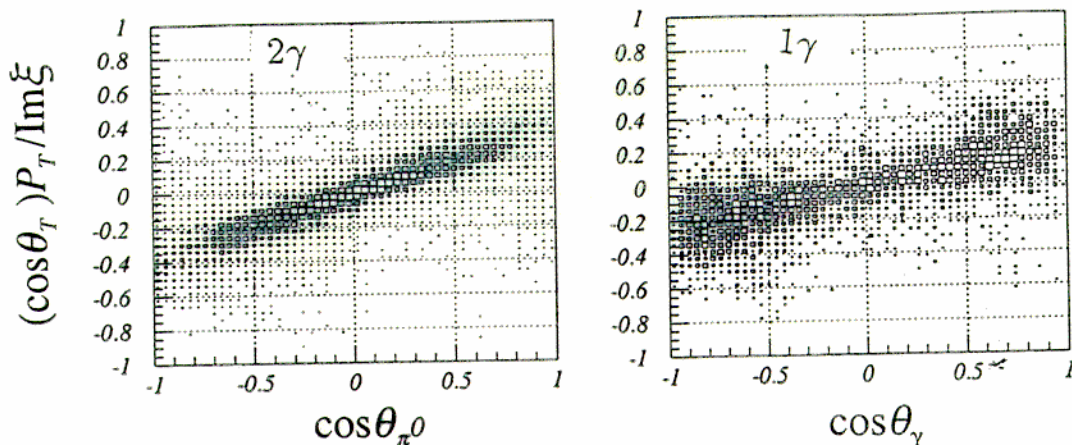


$$N(S) = N(a) - N(b)$$

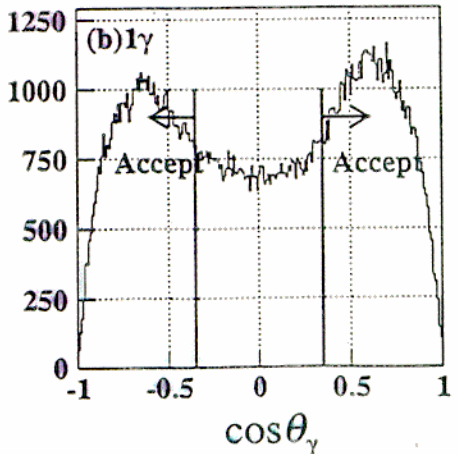
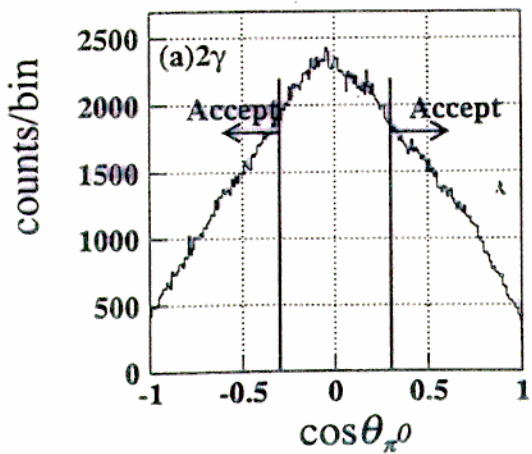
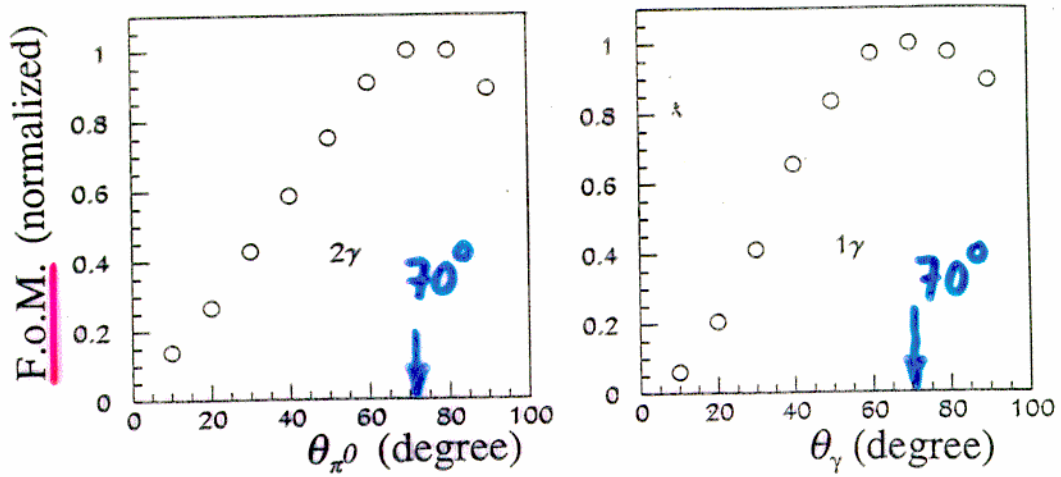
$$\Delta N(S) = \sqrt{N(S) \{1 + 2N(b) / N(S)\}}$$

# Optimum fwd/bwd region

Sensitivity distribution



$$F.o.M. = \langle \cos(\theta_T) \times \frac{P_T}{\text{Im}\xi} \rangle \times \sqrt{N}$$



# $A_T, P_T$ and $\text{Im}\xi$

$$A_T = \frac{1}{4} \left\{ \frac{[\sum_{i=1}^{12} N_i(cw) / \sum_{i=1}^{12} N_i(ccw)]_{fwd}}{[\sum_{i=1}^{12} N_i(cw) / \sum_{i=1}^{12} N_i(ccw)]_{bwd}} - 1 \right\}$$

$$P_T = A_T / \alpha \langle \cos\theta_T \rangle$$

- $\alpha$  : analyzing power

Estimate using  $P_N$  and  $A_N$

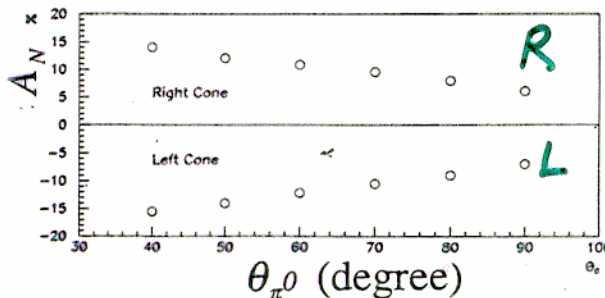
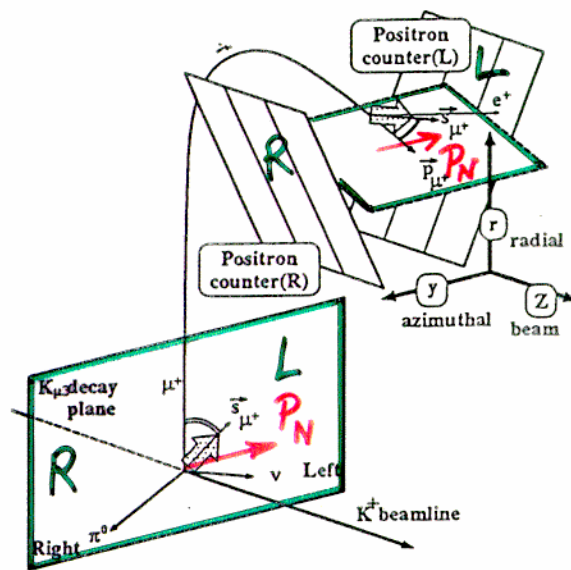
- $\langle \cos\theta_T \rangle$  : kinematical attenuation

Estimate by MC calculation taking into account acc. BG

$$\text{Im}\xi = \frac{P_T}{\langle P_T / \text{Im}\xi \rangle}$$

- $\langle P_T / \text{Im}\xi \rangle$  : aver. sensitivity

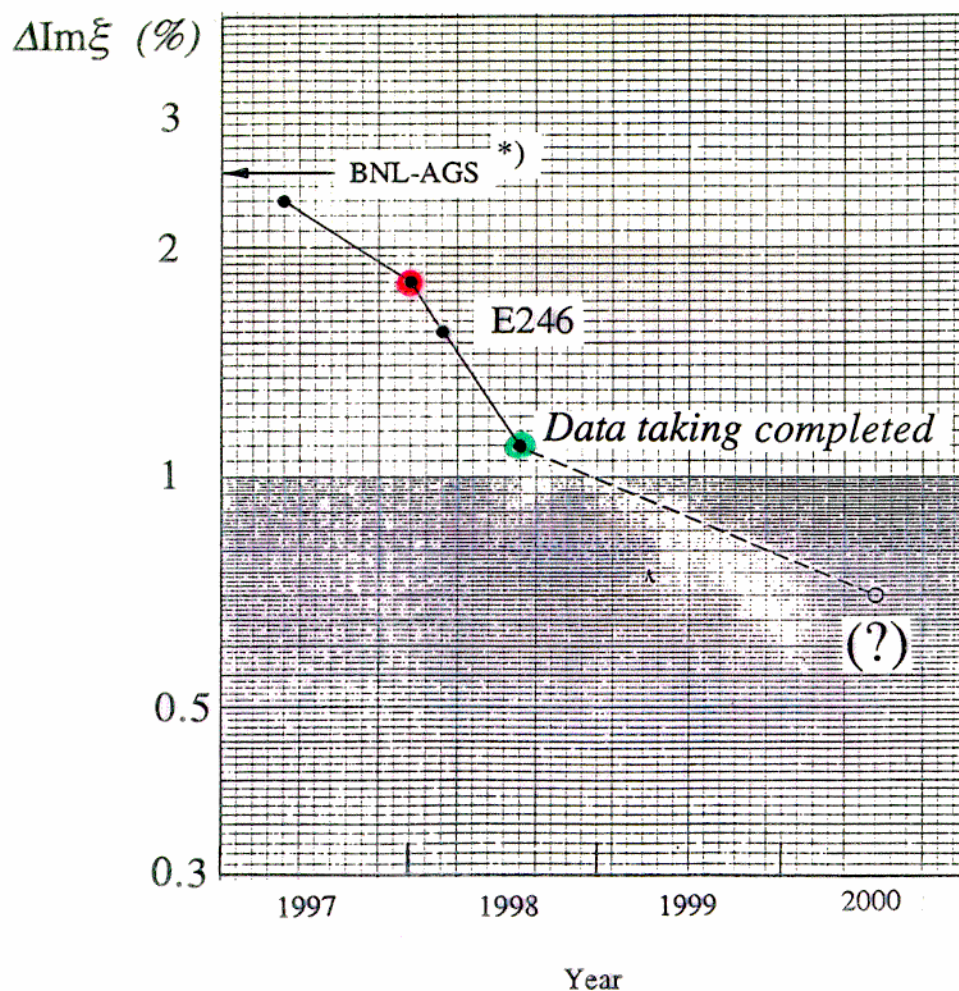
Estimate by MC calculation taking into account acc. BG



	Analysis-1	Analysis-2
$\alpha$	0.198	0.194
$\langle \cos\theta_T \rangle$	0.733 (2 $\gamma$ ) / 0.637 (1 $\gamma$ )	0.770 (2 $\gamma$ ) / 0.649 (1 $\gamma$ )
$\langle P_T / \text{Im}\xi \rangle$	0.314 (2 $\gamma$ ) / 0.284 (1 $\gamma$ )	0.337 (2 $\gamma$ ) / 0.288 (1 $\gamma$ )

# Current status of E246

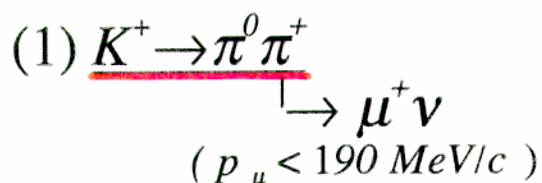
- The 1998 run was completed in June. One  $\sigma$  sensitivity of  $\Delta\text{Im}\xi = 1.1 \times 10^{-2}$  is expected.
- 70 days of further running is planned in next years. The final sensitivity will be  $\Delta\text{Im}\xi = 7 \times 10^{-3}$ .



\*) S.R. Blatt et al.; Phys. Rev. D27 (1983) 1056  
( in-flight decay experiment )



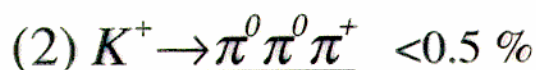
# Physics Background



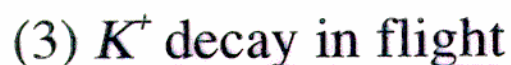
[ Rejection by angle  $\theta_{\mu\pi}$  ]

Analysis-1 : 3.0 %  
 Analysis-2 : <1.0 %

- There is  $P_T$  but  $\langle P_T \rangle = 0$
- $fwd/bwd$  cancellation



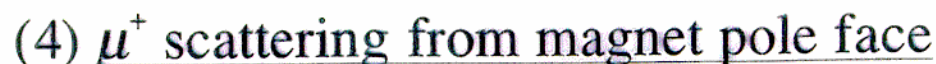
- no  $P_T$
- $fwd/bwd$  cancellation



[ Rejection by missing mass ]

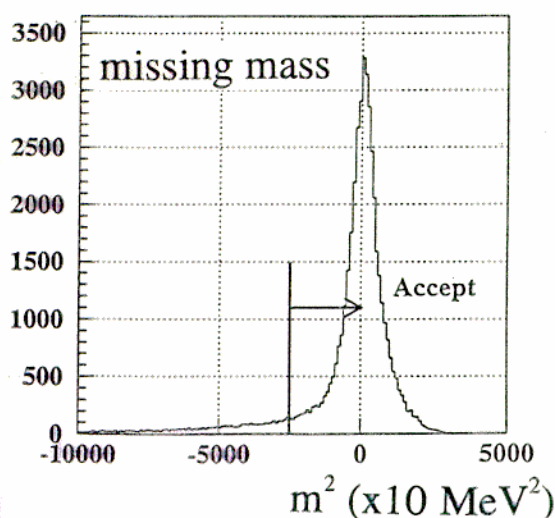
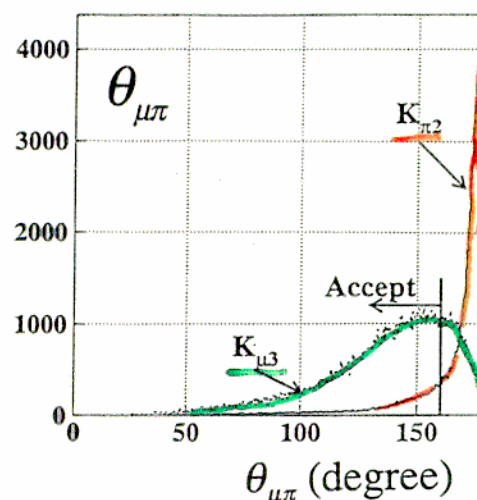
Analysis-1 : <1.0 % ( $2\gamma$ ), = 2.5 % ( $1\gamma$ )  
 Analysis-2 : =1.2 % ( $2\gamma$ ), = 4.5 % ( $1\gamma$ )

- no spurious  $P_T$  was observed in data

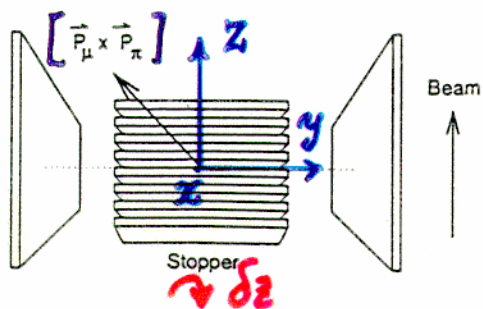


[ Tracking ]

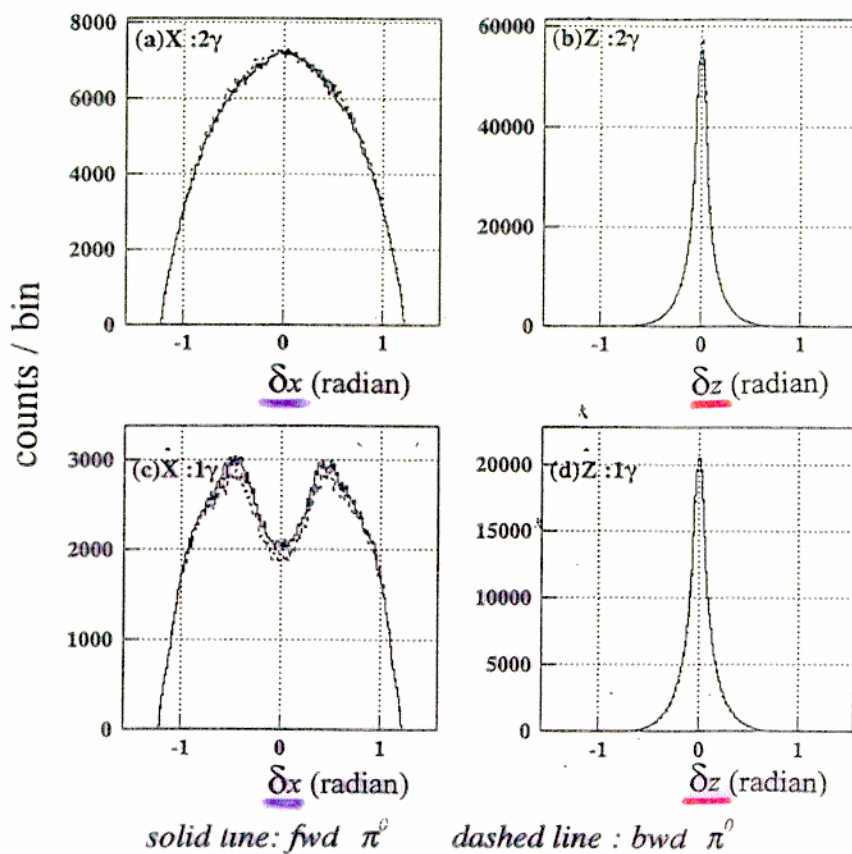
- $\delta P_T < 10^{-5}$  (calculation) <1.0 %



# Systematics - Decay plane rotation - reflecting CsI and chamber alignment



- Rotation around x-axis  $\delta_x$  induces  $P_L$  mixing  
fwd/bwd cancellation
- Rotation around z-axis  $\delta_z$  induces  $P_N$  mixing  
No fwd/bwd cancellation!



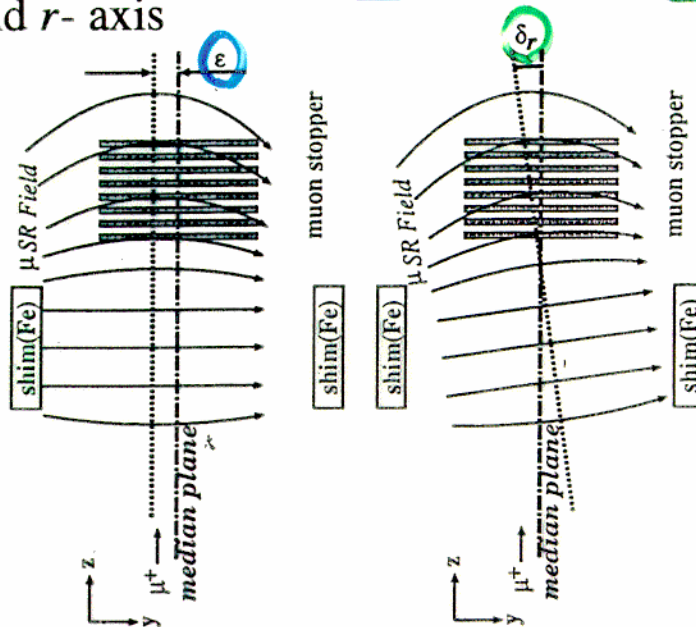
	$1\gamma$	$2\gamma$
$(\delta_x^{fwd} - \delta_x^{bwd}) / 2$	$1.01 \pm 0.55$ mr	$0.06 \pm 0.35$ mr
$(\delta_z^{fwd} + \delta_z^{bwd}) / 2$	$0.45 \pm 0.15$ mr	$0.58 \pm 0.10$ mr

$\delta P_T$   
 $4 \times 10^{-4}$   
 $3 \times 10^{-4}$

# Systematics

## - Asymmetry of magnetic field -

(1) Field distribution offset ( $\epsilon$ ) and rotation ( $\delta_r$ ) around  $r$ - axis



- They introduce  $P_L$  admixture, but
- $fwd/bwd$  cancellation works.

$$\delta P_T \approx 3.5 \times 10^{-4}$$

(2) Field rotation around  $z$ - axis ( $\delta_z$ )

- introduces  $P_N$  admixture.
- There is no  $fwd/bwd$  cancellation

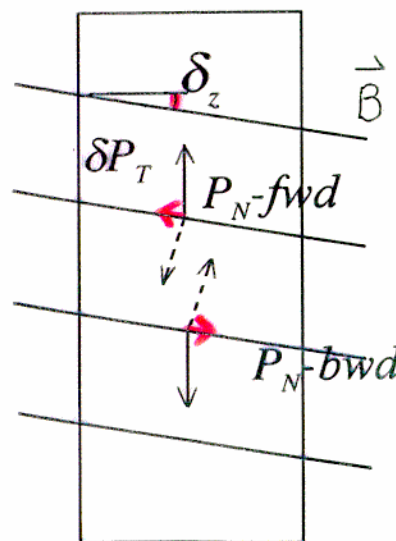
$$\langle \sigma \delta_z \rangle = 1.0 \text{ mr}$$

$$\langle \sigma \delta_z \rangle_{\text{meas.}} \leq 1.0 \text{ mr}$$

$$\langle \sigma \delta_z \rangle^{\text{total}} \leq 1.4 \text{ mr}$$

$$\delta P_T \approx 0.8 P_N \delta_z$$

$$\leq 6 \times 10^{-4}$$



# Summary of systematic errors

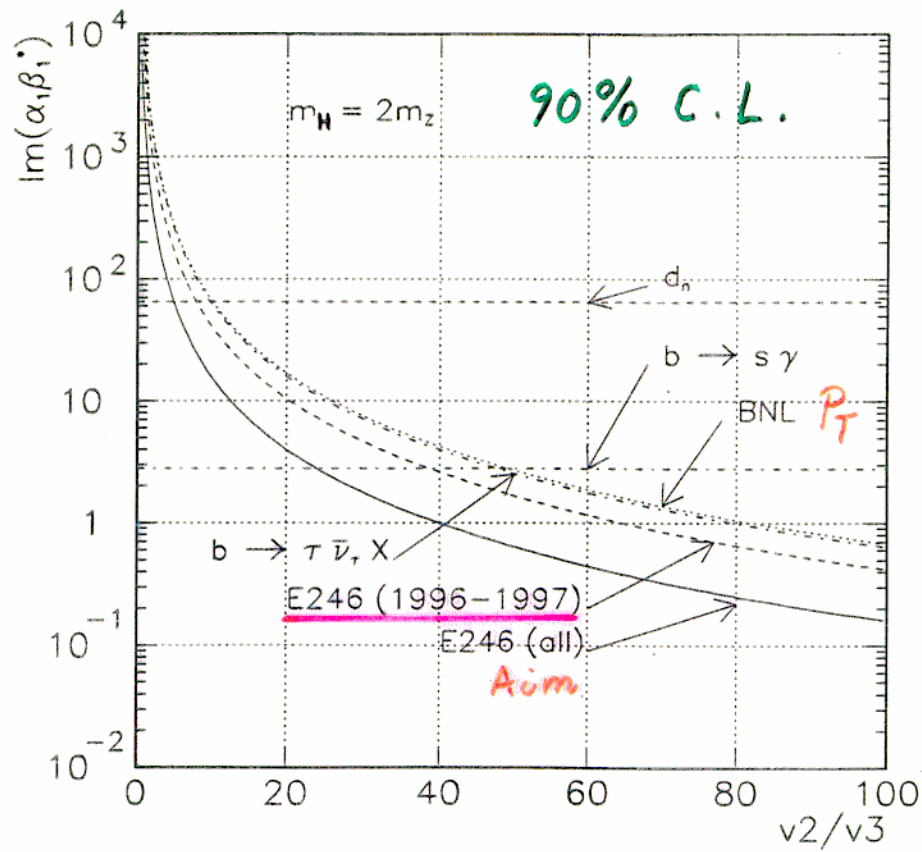
Source of error	$\delta A_T$ after $\Sigma_{12}$	$\delta A_T$ after F/B
Target shift	o $2 \times 10^{-4}$	o $< 10^{-5}$
$e^+$ counter $r$ -rotation	o $1.6 \times 10^{-4}$	o $5 \times 10^{-6}$
$e^+$ counter $z$ -rotation	o $5.2 \times 10^{-5}$	o $2 \times 10^{-6}$
$e^+$ counter $\phi$ -offset	x $5.7 \times 10^{-3}$	o $1.9 \times 10^{-5}$
$e^+$ counter $r$ -offset	o $< 1.5 \times 10^{-6}$	o $< 10^{-6}$
$e^+$ counter $z$ -offset	o $< 1.0 \times 10^{-3}$	o $< 10^{-6}$
B $y$ -offset ( $\epsilon$ )	x $5.2 \times 10^{-4}$	o $5 \times 10^{-5}$
B $r$ -rotation ( $\delta_r$ )	x $1.0 \times 10^{-4}$	o $< 10^{-5}$
<u>B <math>z</math>-rotation (<math>\delta_z</math>)</u>	<u>x</u> $8 \times 10^{-5}$	<u>x</u> $8 \times 10^{-5}$
CsI(Tl) efficiency	o $< 8 \times 10^{-4}$	o $< 5 \times 10^{-5}$
$\mu^+$ counter $y$ -offset	x $< 10^{-4}$	o $< 10^{-5}$
MWPC $y$ -offset	x -	ox $3.5 \times 10^{-5}$
$[\underline{n}_{\pi^0} \times \underline{n}_{\mu^+}]$ rotation ( $\delta_r$ )	ox -	o $6 \times 10^{-5}$
<u><math>[\underline{n}_{\pi^0} \times \underline{n}_{\mu^+}]</math> rotation (<math>\delta_z</math>)</u>	<u>x</u> -	<u>x</u> $4 \times 10^{-5}$
beam background	x $< 2 \times 10^{-3}$	o $< 5 \times 10^{-5}$
x : no cancellation o : cancellation		
TOTAL		$1.4 \times 10^{-4}$

$$\delta P_T \approx 1 \times 10^{-3}$$

# Constraint on Models

## (1) Three Higgs doublet model

$$\text{Im}\xi^K = \text{Im}(\alpha_1\beta_1^*) \cdot \left(\frac{v_2}{v_3}\right)^2 \cdot \left(\frac{m_K}{m_{H_1^+}}\right)^2$$

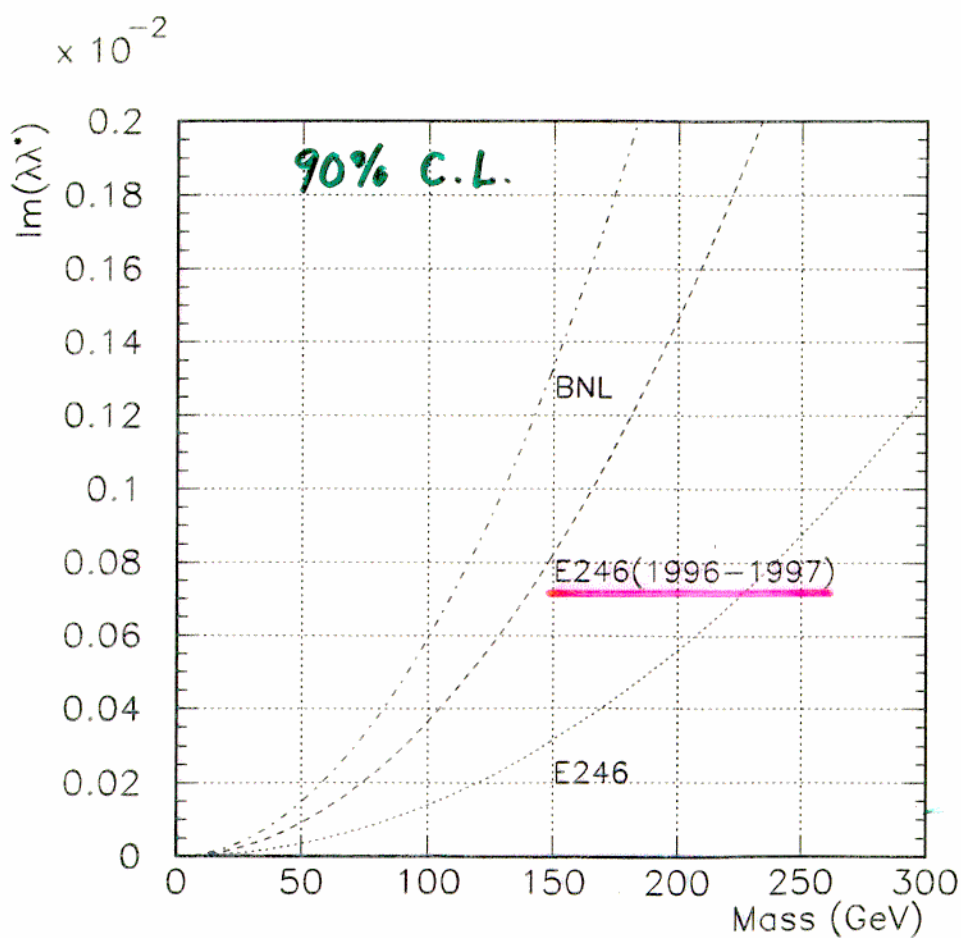


# Constraint on Models

## (2) *R*-parity violating SUSY

$$\text{Im}\xi^l = \sum_i \frac{\text{Im}[\lambda_{2i2}(\lambda'_{i12})^*]}{4\sqrt{2}G_F \sin\theta_c (m_{\tilde{l}_i})^2} \cdot \frac{m_K^2}{m_\mu m_s}$$

$$\text{Im}\xi^d = \sum_k \frac{\text{Im}[\lambda'_{21k}(\lambda'_{22k})^*]}{4\sqrt{2}G_F \sin\theta_c (m_{\tilde{d}_k})^2} \cdot \frac{m_K^2}{m_\mu m_s}$$



## CONCLUSIONS

- Transverse  $\mu^+$  polarization ( $P_T$ ) probes new physics such as 1) multi-Higgs doublet models and 2) a class of SUSY.
- E246 experiment is searching for  $P_T$  with a potential sensitivity of  $\Delta P_T \approx 10^{-3}$ . (Systematic error is of this magnitude.)
- No evidence for  $P_T$  has been found from the 96 and 97 data. Analysis of 98 data is now in progress.
- After 70 days of data taking in the future, we will achieve the sensitivity of  $\Delta \text{Im} \xi = 0.007$ .