

# **SLAC-PROPOSAL-E159**

## **Proposal to Measure $\Delta\sigma^{\gamma N}(k)$ and the High Energy Contribution to the Gerasimov-Drell-Hearn Sum Rule**

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# OUTLINE

- Introduction
- The GDH Sum Rule
- High energy behavior of  $\Delta\sigma^{\gamma N}(k)$
- Connection of virtual photon results
- Experimental Overview
- Beam and Compton Polarimeter
- Target and Detectors
- Backgrounds
- Anticipated Results

# INTRODUCTION

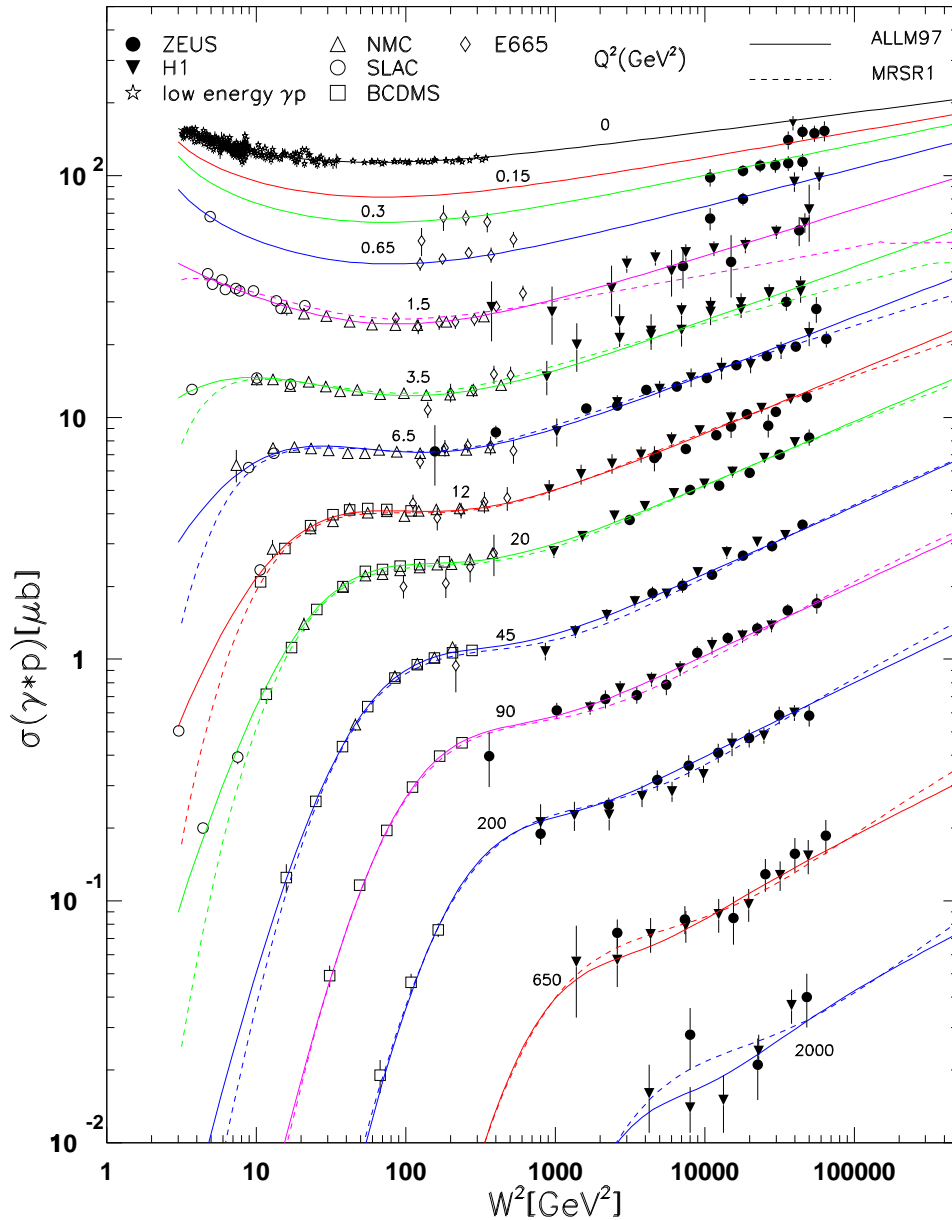
- Total photoabsorption cross section  $\sigma^{\gamma N}(k)$  depends only on **photon energy  $k$**  for real photons.
- Can be decomposed into **spin 1/2 and 3/2** final states  $\sigma_{3/2}$  and  $\sigma_{1/2}$ , corresponding to helicity of photon aligned or anti-aligned with spin of nucleon.
- Spin-averaged  $\sigma^{\gamma N}(k) = (\sigma_{1/2} + \sigma_{3/2})/2$  well-measured (including SLAC early 1970's). Roughly **constant** at **120  $\mu\text{b}$** .
- We propose to measure

$$\Delta\sigma^{\gamma N}(k) = \sigma_{3/2} - \sigma_{1/2}$$

using circularly polarized photons and longitudinally polarized nucleons.

# SPIN-AVERAGED $\sigma^{\gamma N}(k, Q^2)$

Large body of data: explore connection perturbative and non-perturbative regimes of QCD.



# The GDH SUM RULE

- Relates integral over  $\Delta\sigma(k)$  to anomalous magnetic moment  $\kappa$  of target with spin  $S$  (composite or elementary).

$$\int_{k_\pi}^{\infty} \frac{dk}{k} \Delta\sigma^{\gamma N}(k) = \frac{2\pi^2 \alpha \kappa^2}{M^2}$$

- Follows from **general principles** of causality, universality, Lorentz and electromagnetic gauge invariance.
- One **assumption**: that unsubtracted dispersion relation can be used for  $f_2(\nu)$  (the spin-dependent part of the forward Compton amplitude).
- Theorists debate whether a  $J = 1$  fixed pole (violating GDH Sum Rule and possibly Bjorken Sum Rule also) is likely, unlikely, or ruled out in QCD.

- **Scale** of convergence gives scale of highest spin-flip excitations of target.
- Oscillations in  $\Delta\sigma^{\gamma N}(k)$  signal important excitations (such as  $\Delta(1232)$  Resonance). Are there any oscillations above 4 GeV?
- $\Delta\sigma^{\gamma N}(k)$  must **decrease** with  $k$  at high  $k$  for integral to converge. Contrast to  $\sigma^{\gamma N}(k)$ , known to **increase** with  $k$  at high energies.
- Direct measurements only exist up to 800 MeV for proton, but various resonance region multi-pole analyses have made estimates of integrals.

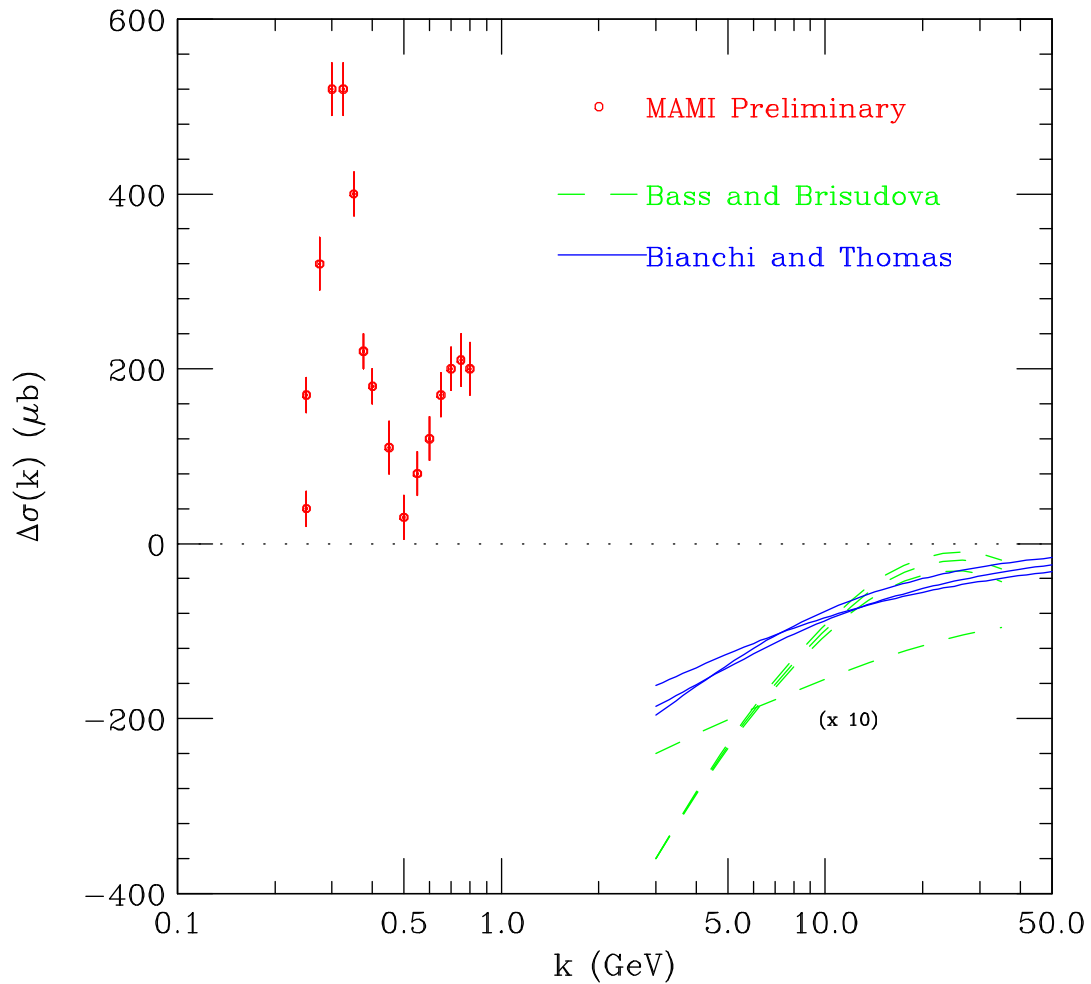
| target            | $2\pi^2\alpha\kappa^2/M^2$ | Analyses                 |
|-------------------|----------------------------|--------------------------|
| proton            | 204 $\mu\text{b}$          | 257 to 289 $\mu\text{b}$ |
| neutron           | 232 $\mu\text{b}$          | 169 to 189 $\mu\text{b}$ |
| isoscalar (p+n)/2 | 219 $\mu\text{b}$          | 213 to 239 $\mu\text{b}$ |
| isovector (p-n)/2 | -15 $\mu\text{b}$          | 34 to 65 $\mu\text{b}$   |

- Large discrepancy, especially **isovector** case.
- **Non-resonant** contribution important?
- **High energy** contributions important?
- Need **data** on both proton and neutron to find out.
- Worldwide program at Mainz, Bonn, GRAAL, SPIN8, LEGS, Jefferson Lab, TUNL, other, but limited to 5 GeV.

# LOW ENERGY BEHAVIOR OF $\Delta\sigma(k)$

Preliminary data from Mainz on [proton](#).

Resonant excitations are evident (especially  $\Delta(1232)$ ).



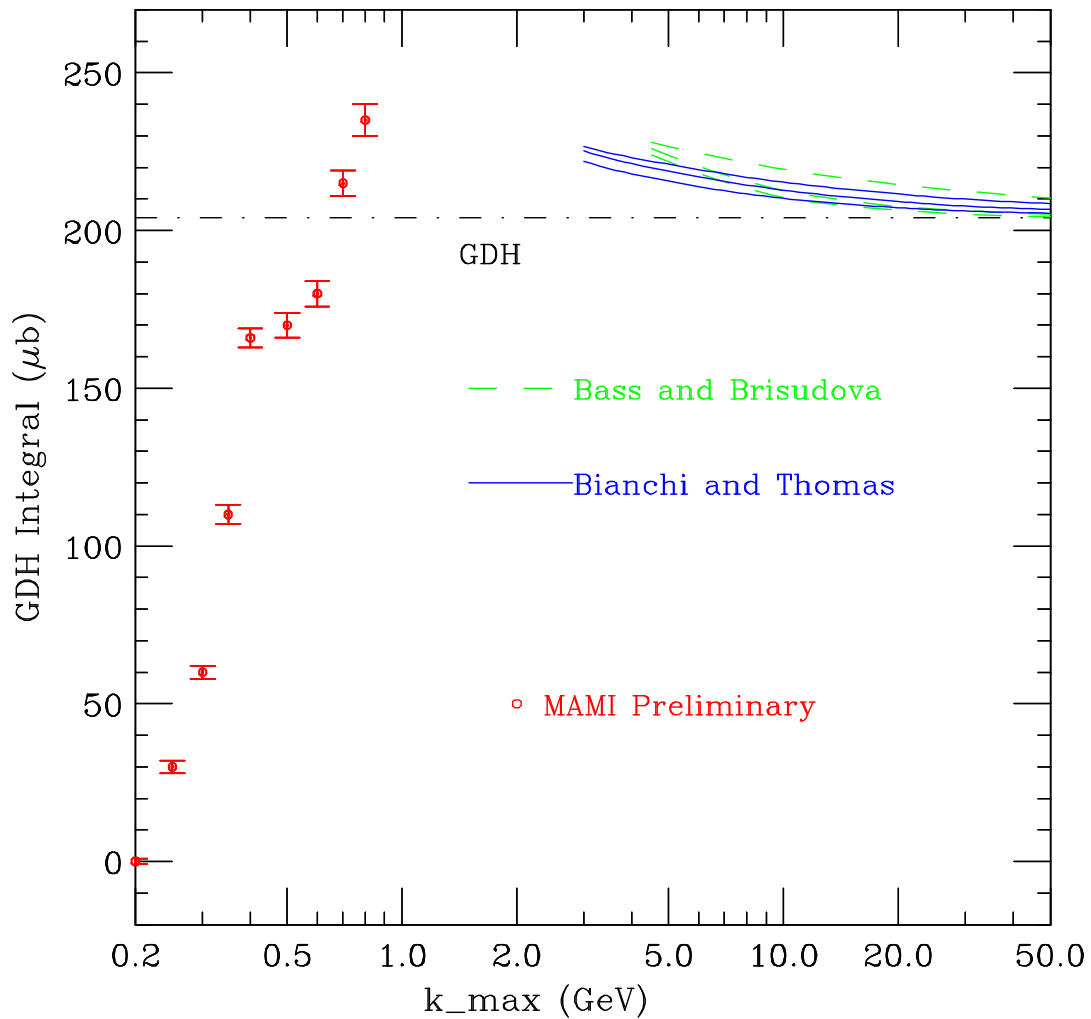


## HIGH ENERGY BEHAVIOR OF $\Delta\sigma(k)$

- **Regge theory** describes many reactions. Has been applied to measurements using virtual photons  $\Delta\sigma(k, Q^2)$ . Can fit SLAC data for  $Q^2 > 0$  quite well.
- **Isovector** contribution dominated by poorly known  $a_1(1260)$  axial vector meson trajectory.
- **Isoscalar** dominated by better known  $f_1(1285)$  meson trajectory.
- Isoscalar non-perturbative gluon exchange  $[(\ln s)/s]$ ?
- Pomeron-pomeron cut contributions  $[1/\ln s^2)]$ ?

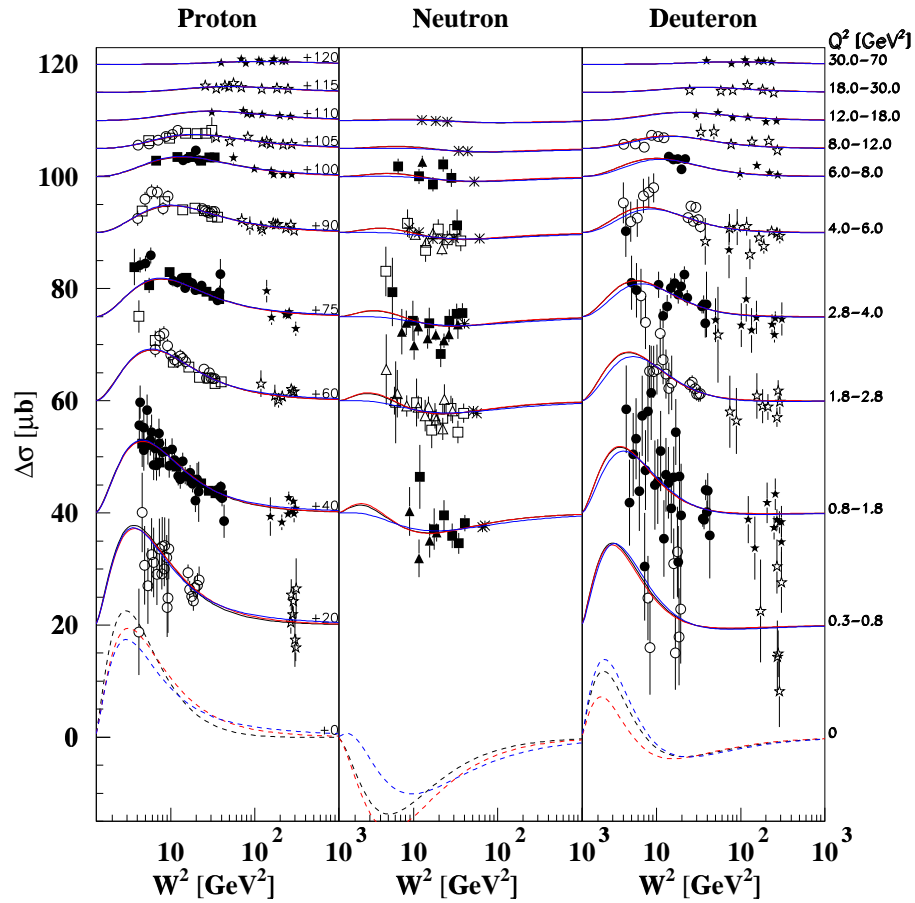
# INTEGRAL CONVERGENCE?

Curves are various Regge theory fits to virtual photoproduction data, plotted **assuming** **proton** integral converges.



# FIT OF BIANCHI AND THOMAS

Regge theory fits virtual photon data well:  
predicts dramatic change in **neutron** at  $Q^2 = 0$   
compared to  $Q^2 \geq 1 \text{ GeV}^2$ .



## WHY MEASURE $\Delta\sigma(k)$ AT SLAC?

- Measures a very **fundamental** quantity.
- Test **convergence** GDH Sum Rule.
- Compare isoscalar and isovector: latter has connection to **Bjorken Sum Rule**.
- Help in understanding of  $g_1(x, Q^2)$  at low  $x$ , and convergence of integrals over  $g_1$ .
- Look for unexpected spin-flip strength: probe relevant energy **scale**.
- No existing data: field wide open for **surprises**.
- Drell and Hearn suggested SLAC should measure this in 1966. **Now** technology exists to do a good job.

## EXPERIMENTAL OVERVIEW

- Coherent bremsstrahlung provides circularly polarized photons  $4 < k < 40$  GeV.
- Subtract incoherent contributions to obtain  $\Delta\sigma(k)$  at discrete values of  $k$ .
- Longitudinally polarized  $NH_3$  and  $ND_3$  targets.
- Measure total cross section asymmetry with large calorimeters.
- Reject E.M. backgrounds with cuts, longitudinal segmentation of detector, and/or calculations
- Measure in Counting Mode for lower systematic error (each hadronic interaction is individually counted)
- Use Flux Integration Mode for smaller statistical errors (total hadronic energy summed over many interactions).

## PHOTON BEAM

Described earlier. [Summary](#) of important parameters for four of 10 to 12 settings that will be used:

|                                                   |                   |                   |                   |                   |
|---------------------------------------------------|-------------------|-------------------|-------------------|-------------------|
| Electron Energy (GeV)                             | 9.9               | 13.2              | 26.6              | 48.3              |
| $k_0/E$ of Main Coherent Peak                     | 0.5               | 0.77              | 0.50              | 0.77              |
| Incident Electrons/spill                          | $5 \times 10^9$   | $8 \times 10^9$   | $1.5 \times 10^9$ | $2 \times 10^9$   |
| collimator Radius (mm)                            | 3                 | 3                 | 1                 | 1                 |
| Total photons/spill                               | $1.5 \times 10^5$ | $3.0 \times 10^5$ | $5 \times 10^4$   | $1.1 \times 10^5$ |
| Coherent NI/spill                                 | 6.8               | 3.2               | 3.7               | 2.7               |
| Coherent $\langle P_\gamma/P_e \rangle$           | 0.59              | 0.87              | 0.57              | 0.82              |
| $r$ with energy cut                               | 0.59              | 0.31              | 0.80              | 0.58              |
| $\delta\Delta\sigma^{\gamma p}$ ( $\mu\text{b}$ ) | 0.5               | 0.7               | 0.6               | 0.6               |

# COMPTON POLARIMETER

- Designed to measure flux, energy distribution, and circular polarization of beam photons.

- Use Atomic Compton scattering  $\gamma e \rightarrow \gamma e$ .

- Helicity-dependent cross section:

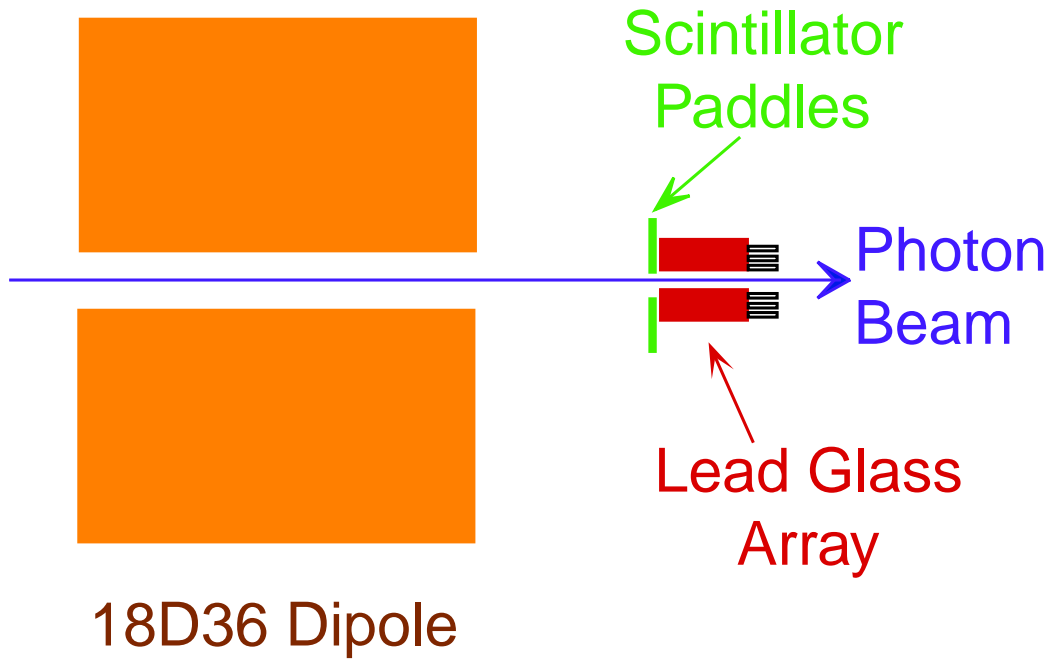
$$\frac{d\sigma}{d\Omega} = \frac{\alpha^2}{2m_e^2} \left(\frac{k}{k_0}\right)^2 \left[ \frac{k}{k_0} + \frac{k_0}{k} - \sin^2 \theta - P_\gamma P_e (1 - \cos \theta) \cos \theta \frac{(k + k_0)}{m_e} \right],$$

- For flux measurements, electrons in  $\text{NH}_3$  and  $\text{ND}_3$  targets can be used for continuous monitoring.

- For circular polarization measurements, use special purpose iron target (similar to that used in E155, etc. for Møller measurements).

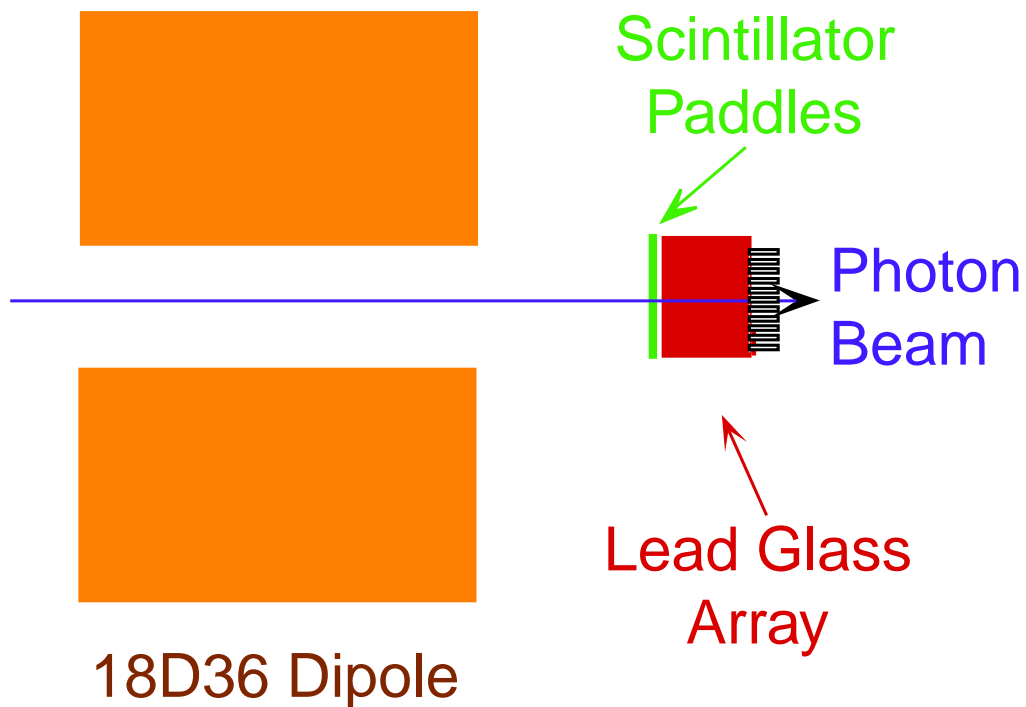
- Electrons in foil polarized using same magnet as for  $\text{NH}_3$  (5 T). Expect average  $P_e$  about 0.08.

## SIDE VIEW



## TOP VIEW

1 M





- Polarimeter uses **dipole** magnet ( 1-m-long 18D36) to bend electrons to north.
- Electrons and photon energies measured in 3 by 10 arrays of **lead glass blocks**, one below, one above the beam line.
- Small scintillator **hodoscope** used to separate scattered electrons and photons.
- Allows **energy measurement** of primary photon to 3%-5%.
- Polarimeter is **movable** on a cart to accommodate opening angle decrease with increasing photon energy.
- With reasonable counting rates (a few per spill), **polarization** can be measured to 3% in about 1 hour.

| $z_{det}$ (m) | $\theta$ range | $\gamma_{coh}/\text{spill}$ | $k$ -range | $C/\text{spl}$ | time(hr) |
|---------------|----------------|-----------------------------|------------|----------------|----------|
| 4.5           | 6-20 mr        | $3 \times 10^5$             | 8-14       | 1.5            | 0.5      |
| 9.0           | 3-10 mr        | $2 \times 10^6$             | 20-40      | 1.0            | 0.9      |

# TARGETS

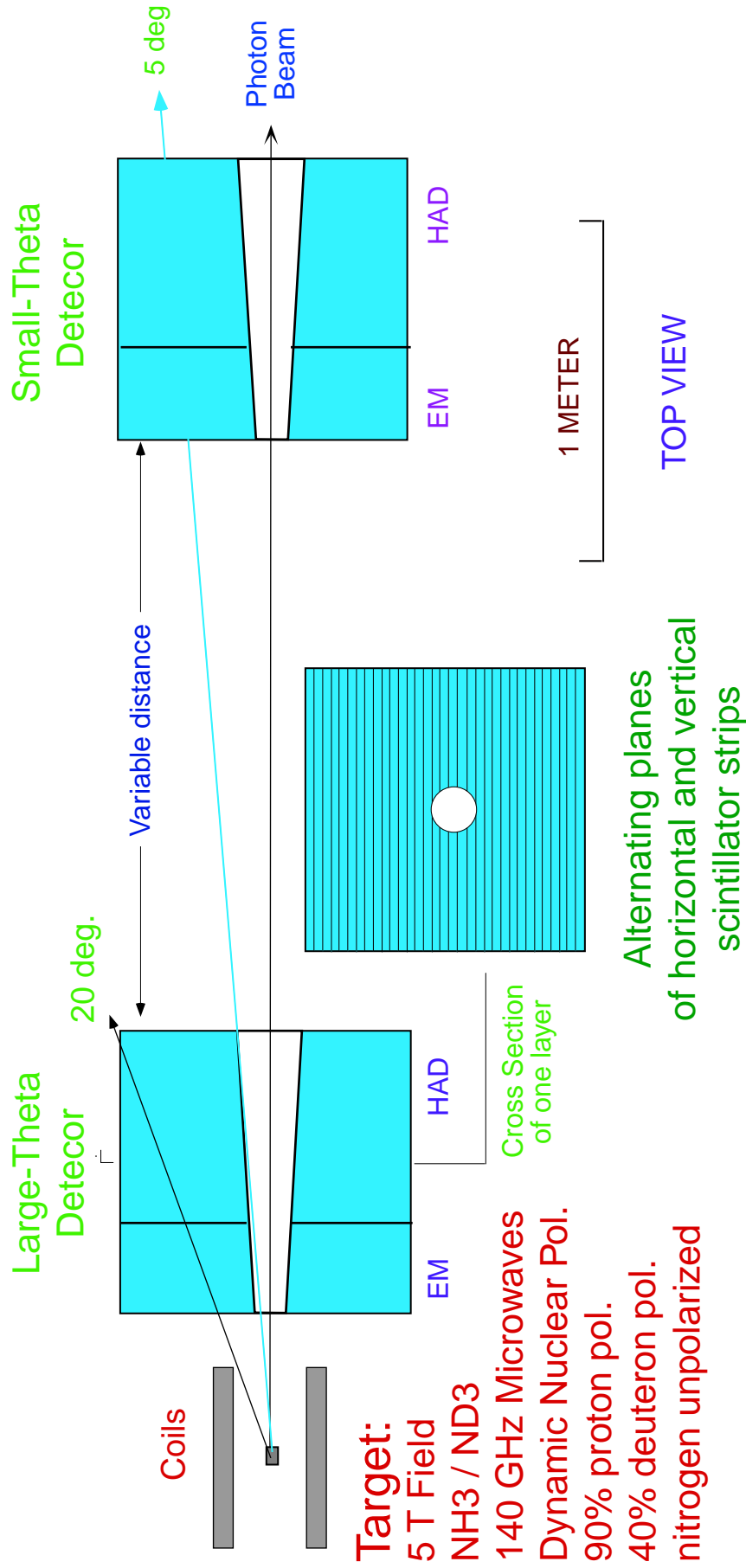
- Very similar to those used in E143, E155, and E155x.
- Will use 3-cm-long cells with  $\text{NH}_3$  for longitudinally polarized protons. Expect polarization  $P_t = 0.9$  and dilution factor  $f = 0.18$ .
- Will use  $\text{ND}_3$  for longitudinally polarized deuterons. Expect polarization  $P_t = 0.4$  and dilution factor  $f = 0.30$ .
- Beam heating and radiation damage very low compared to E155: expect higher average polarizations, less time for annealing, etc.

- Will use **5T** field (new magnet) and **140 GHz microwaves** (existing klystrons), as in E155. **Dilution refrigerator** will be used for cooler temperatures.
- Magnet allows front calorimeter to be **close**, and accept particles up to  **$\pm 20$  degrees**.
- Will extract **neutron** results with small corrections for D-state and shadowing.
- Deuteron photodisintegration, coherent  $\pi^0$  production, relativistic effects, etc. expected to be **very small** at high energies of this experiment (have big effects only for  $k < 500$  MeV).

# DETECTORS

- Based on **concept** of previous SLAC experiment which measured **spin-averaged** cross section: **D.O. Caldwell *et al.*, Phys. Rev. D7 (1973) 1362.**
- **No** Magnetic Field or Tracking
- **Two identical** detectors: **Small Angle** for as low as 0.5 to 5 degrees (moves): **Large Angle** for 5 to 20 degrees (does not move).
- Detectors are sampling **calorimeters**, made from 80 alternating layers of 3-mm-thick **scintillator hodoscopes and lead plates** 6 mm (1 r.l.) thick.

# Target and Detectors



27 EM and 53 Had layers summed with longitudinal wave-shifter bars

- Scintillator **hodoscopes** alternate **horizontal and vertical**, with about 40 elements/plane.
- **Longitudinal segmentation** of each detector: separate read-out of first **27 r.l. (E.M.)** and subsequent **53 r.l. (HAD)**.
- Readout uses longitudinal **wave-shifter bars** with PMT's down-beam ends. Total is **640 PMTs**.
- **Electronics:** each PMT output to **ADC**, discriminator, and multi-hit **TDC** (as in E155).
- **Large- $\theta$**  calorimeter at **fixed** distance from target, **Small- $\theta$**  moves on cart so  **$\theta_{min} = 10\sqrt{40/k_0}$  mr**

## DETECTOR RATES

- In Counting mode, 30 to 50 hadrons/spill in Small- $\theta$  detector. This establishes luminosity limit, given 500 nsec beam pulse length.
- About 4 to 12 hadrons/spill in Large- $\theta$  detector.
- Several 100 low energy (10 to 50 MeV) electrons and photons/spill. Most will be below discriminator threshold. Tolerable “sprinkle hit” rate remaining.
- Estimate 100 neutrons/spill, most with kinetic energy less than 50 MeV. Most below detector threshold.
- In Flux Integration mode, total energy from neutrons estimated to be less than 1% of hadronic energy.

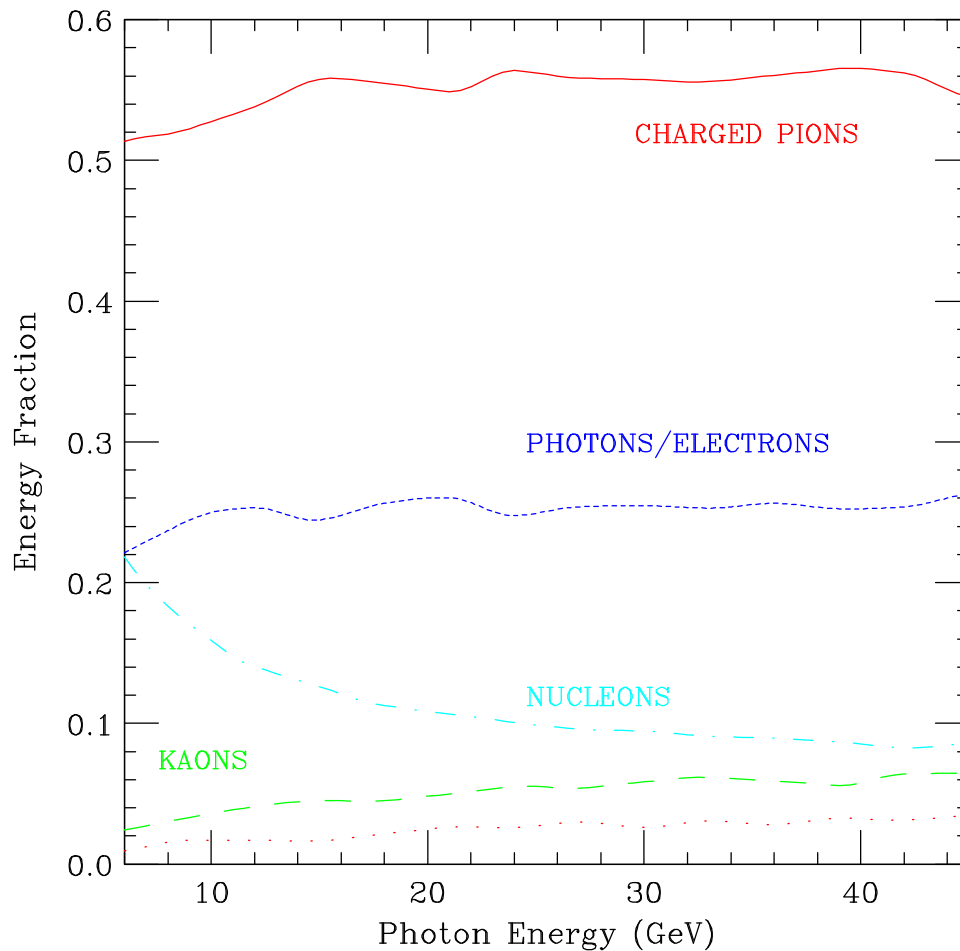
## HADRONIC SIGNAL

- Using PYTHIA, find 99.5% (99%) probability, at least one final state “hadron” (includes photon from  $\pi^0$  decay) has  $p_T > 0.05$  GeV ( $p_T > 0.1$  GeV).
- Most ( $> 80\%$ ) events have a charged pion or kaon in final state with  $P > 1$  GeV
- Good efficiency ( $> 97\%$ ) obtained in counting mode with requirements  $p_T > 0.1$  GeV or  $E_{min} = 0.6 \ln(k_0)$  and  $p_T^{HAD} > 0.05$  GeV.
- Efficiency slightly lower if count only energy in HAD calorimeter [flux integration method B].



# HADRONIC EVENTS

Fractional energy into **charged pions** (solid), photons/electrons (short dashed), **nucleons/anti-nucleons** (dot-dashed), **kaons** (long dashed), and **neutrinos** (dotted).



## Hadronic Efficiency

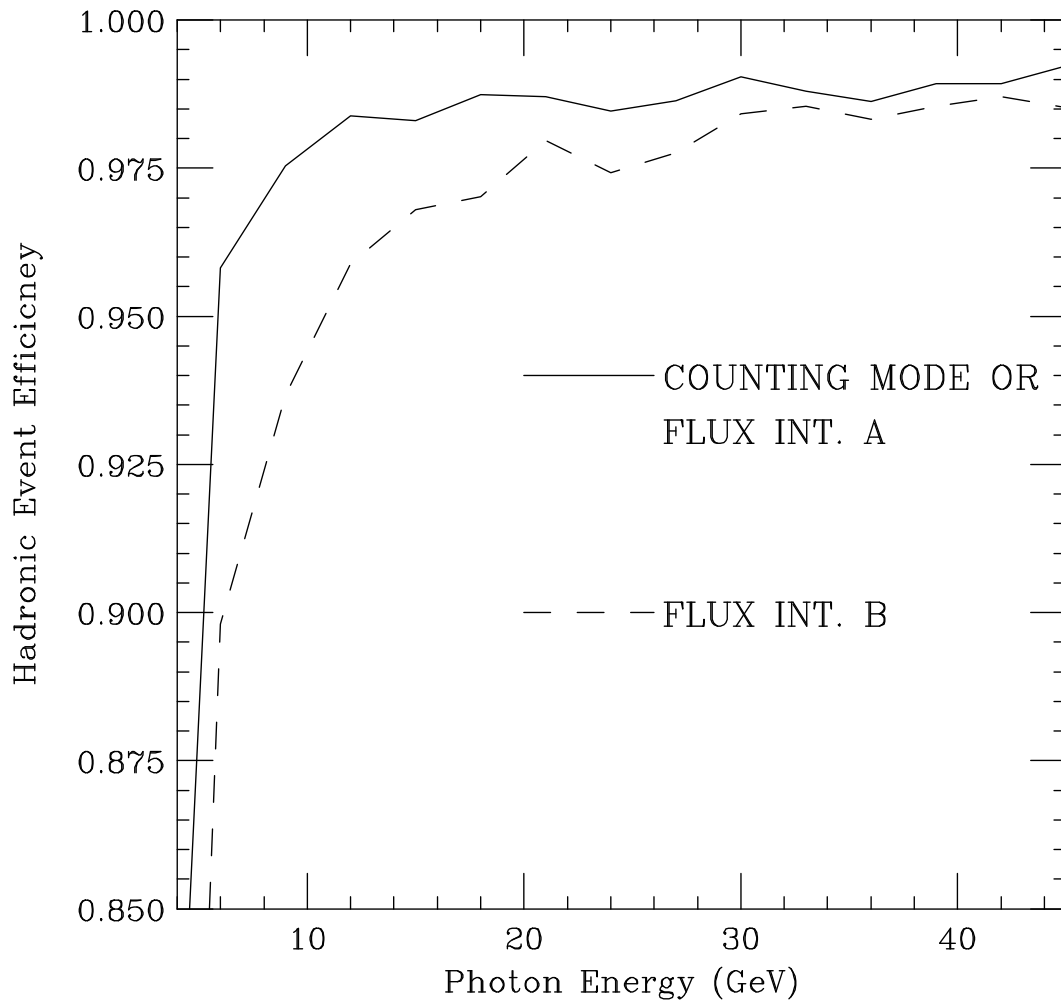
- Less than 1% of events lost using  $\theta_{min} = 0.010\sqrt{40/k}$  mr. Similar to  $\theta_{min} = 400/k$  mr cut used by Caldwell.
- Find  $\theta_{max} = 20$  degrees gives good efficiency for  $k > 10$  GeV. Some loss at lower energies, but need this compromise to keep reasonable target costs.
- Find using energy cut  $E_{min} = 0.6 \ln(k_0)$  preserves almost all events from coherent peak.

# EFFICIENCY VERSUS $K$

Flux integration Methods:

A: E.M. background subtracted;

B: only energy in HAD calorimeter



# PHYSICS BACKGROUND SUMMARY

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| Data Analysis      | B.H. Rates | Compton Rates |
|--------------------|------------|---------------|
| Counting Mode      | < 1%       | negligible    |
| Flux Integration A | 50%        | 10% to 20%    |
| Flux Integration B | negligible | negligible    |

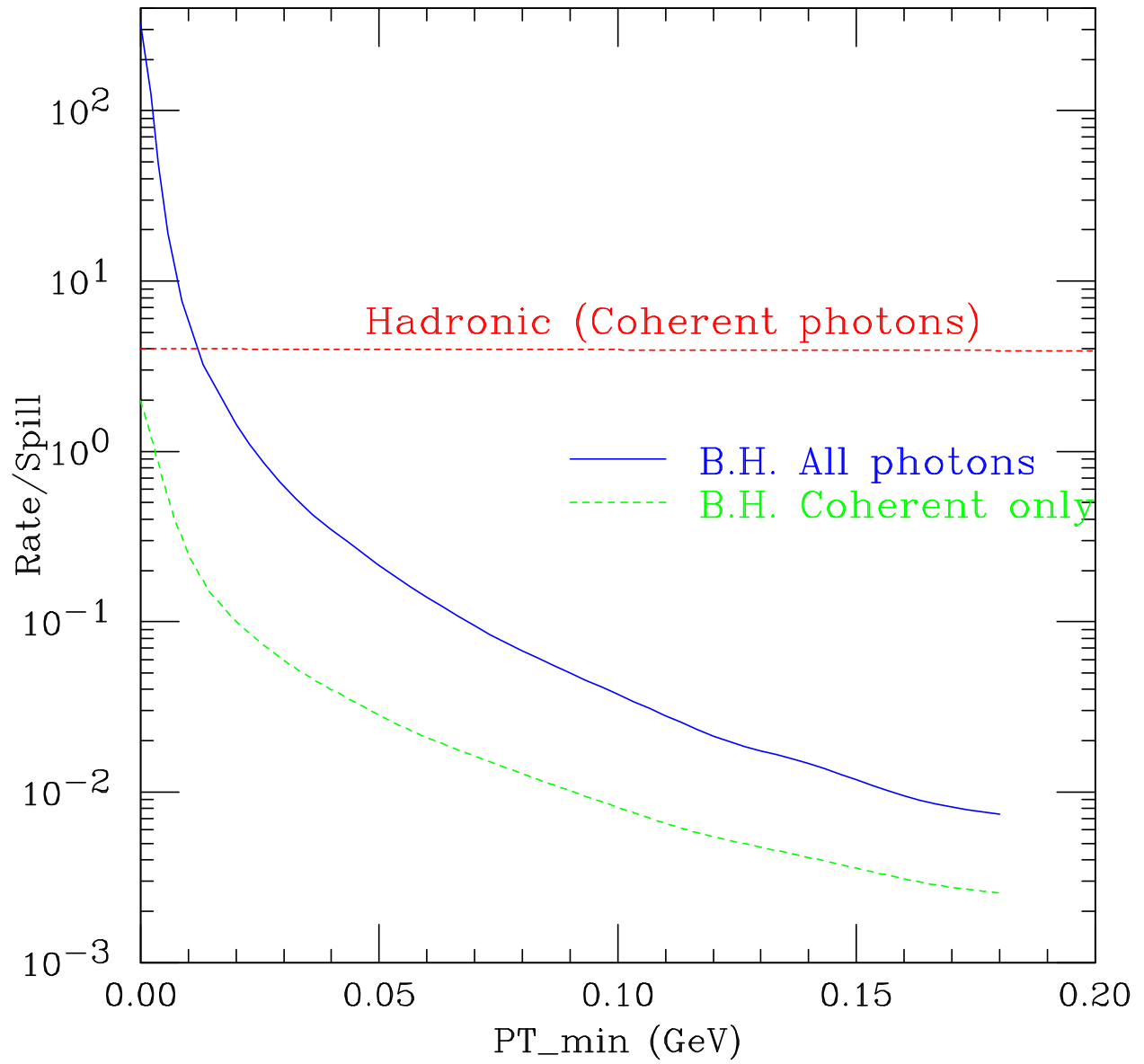
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Rates and physics asymmetry for both backgrounds well-known and [calculable](#).

## BETHE-HEITLER BACKGROUND

- Calculations include quasi-elastic and nuclear elastic  $e^+e^-$  pair production.
- Inelastic not included (part of GDH).
- Cross sections and asymmetry readily calculated in terms of  $F_1$ ,  $F_2$ ,  $g_1$ , and  $g_2$ .
- Find several 100/spill, but have low energy and mainly come from low energy incoherent photons. Total energy/spill similar to total hadronic energy per spill, with asymmetry close to zero. Applies to flux integration method A.
- Rate very low ( $< 1\%$ ) with  $p_T > 0.1$  GeV cut and subtraction of incoherent photon contribution (applies to counting mode).
- Negligible contribution to flux integration method B since all of energy absorbed in EM calorimeter.

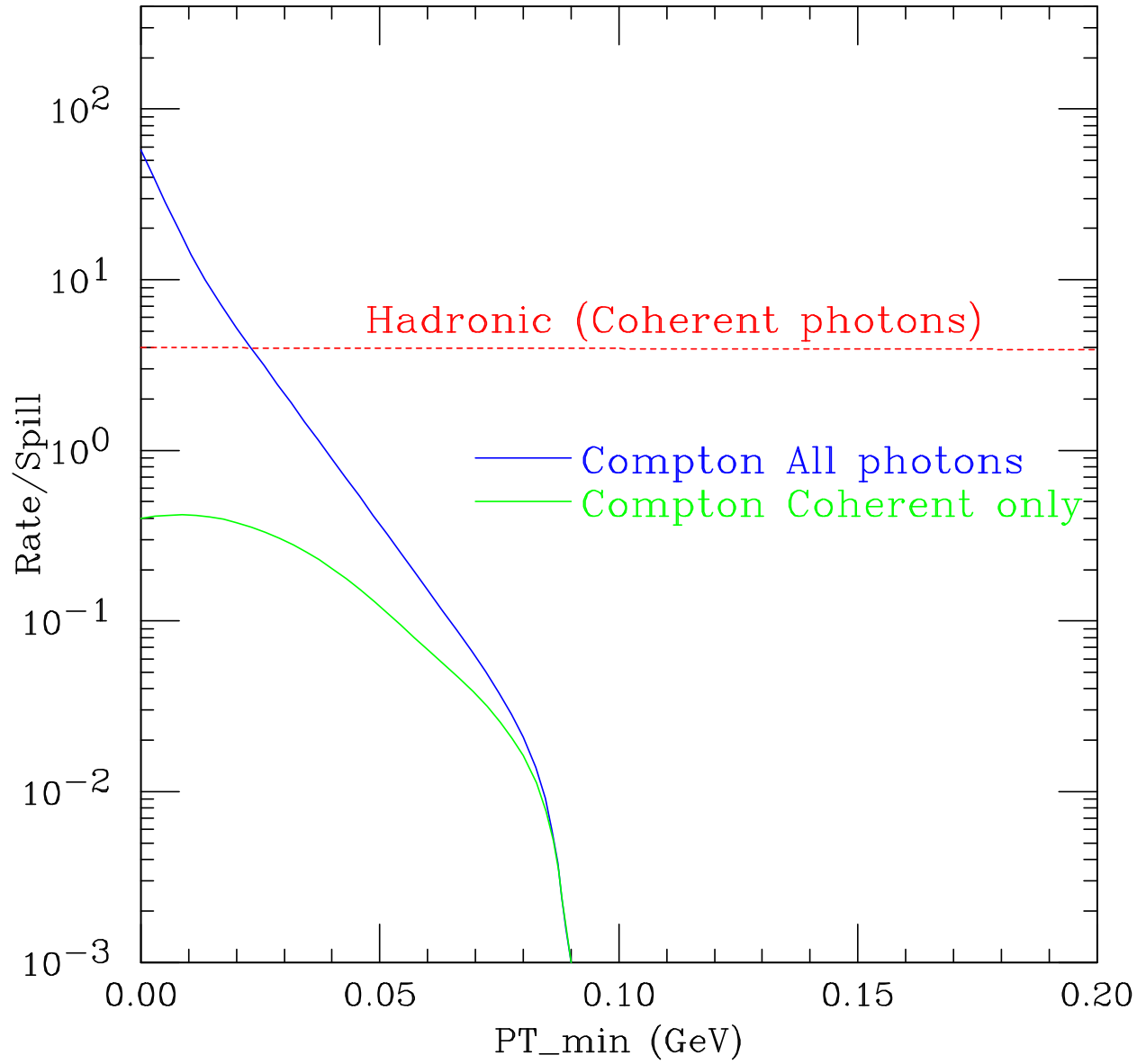
# BETHE-HEITLER RATES



# ATOMIC COMPTON BACKGROUND

- Cross section strongly peaked at low energy photons.
- Final state includes both soft photon and electron, typical energy 10 to 50 MeV.
- Asymmetry expected to be essentially zero for polarized target (electrons not polarized when microwaves are on).
- Find several 100/spill, but total energy less than Bethe-Heitler (about 10% to 20% of total hadronic energy).
- Makes 10% to 20% dilution for flux integration method A.
- Rate drops to zero for  $p_T > 0.1$  GeV (kinematic limit), so no background to counting mode.
- No contribution to flux integration method B [no energy in HAD calorimeter].

# ATOMIC COMPTON RATES





## EXPECTED RESULTS

- More conservative (larger error) analysis method assumes **subtraction** of results with/without coherent bremsstrahlung peaks.
- Error on  $A_1(k) = \Delta\sigma^{\gamma N}(k)/2\sigma^{\gamma N}(k)$  given by

$$\delta A_1(k) = \frac{1}{P_\gamma P_t f \sqrt{N_c}} \frac{\sqrt{2-r}}{\sqrt{r}}$$

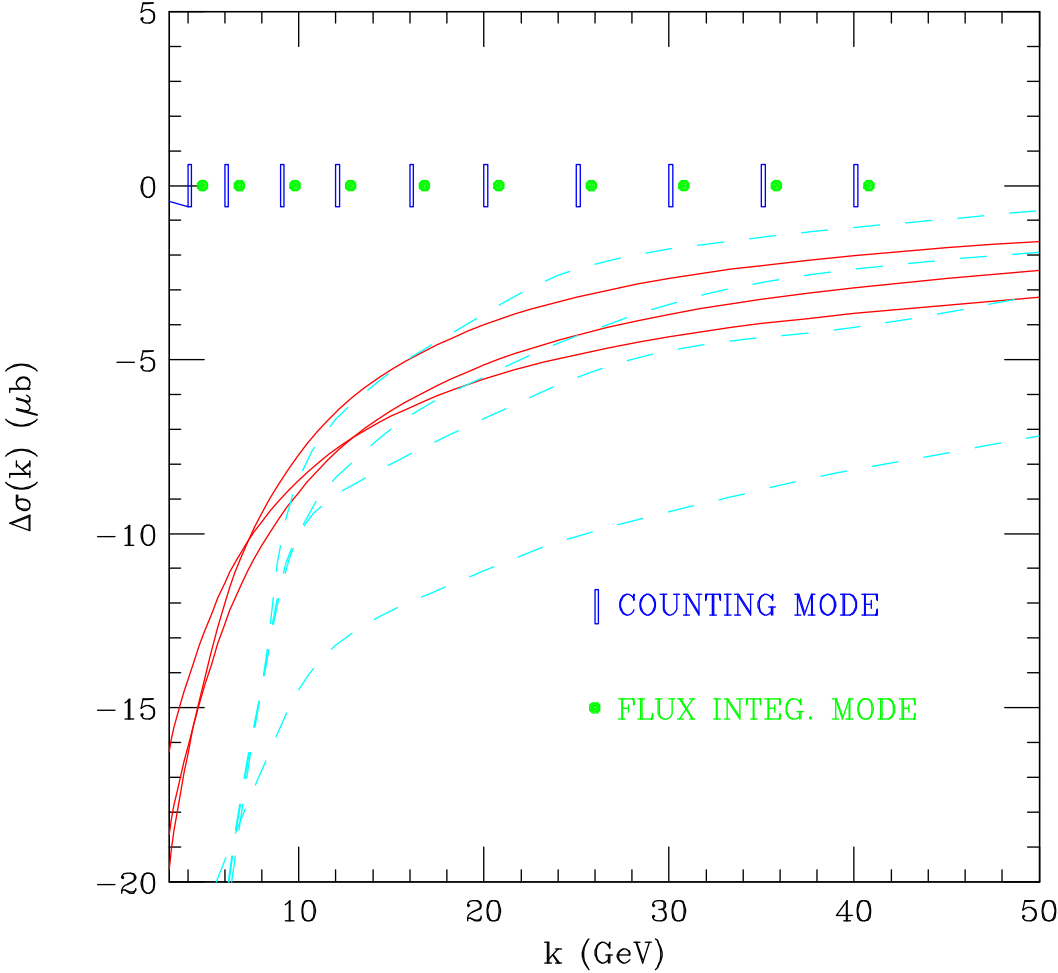
where  $r$  is **fraction** of counts from coherent peaks, and  $0.3 < r < 0.8$ , depending on setting.

- In **counting mode**, rate of coherent counts  $N_c \approx 4 \times 10^7/\text{day}$ . In **flux integration mode**,  $N_c \approx 10^9/\text{day}$ .
- Error on  $\Delta\sigma$  obtained by scaling by  $2\sigma \approx 250 \mu\text{b}$ .

- Analysis using **simultaneous fit** to all data (includes highly polarized incoherent photons near endpoint) estimated to reduce statistical errors by factor of two.
- Most **systematic errors** in counting mode scale with size of  $A_1$ : estimate **6% to 8%** relative error from combined beam and target parameters and modeling uncertainties. Expect to be smaller than counting mode statistical errors.
- **Run plan** will be optimized depending on preliminary results: if asymmetries large, more time will be spent on counting mode.
- Final results on both **proton** and **neutron** will be small enough to clearly determine **magnitude** and **energy dependence** of  $\Delta\sigma$  for  $4 < k < 40$  GeV.

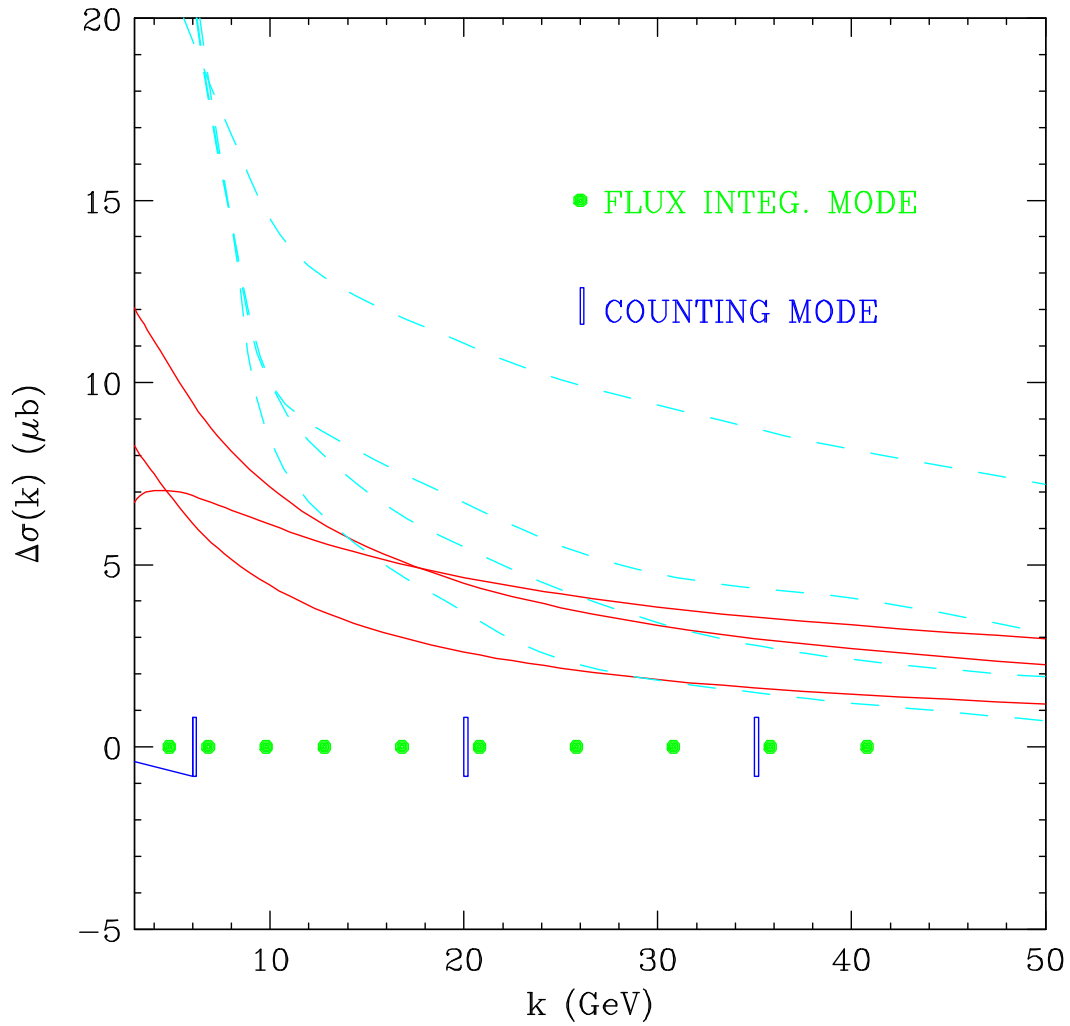
# EXPECTED ERRORS FOR PROTON

Systematic errors (not shown) expected to be 6% to 8% (relative).



# EXPECTED ERRORS FOR NEUTRON

Systematic errors (not shown) expected to be 6% to 8% (relative).



## ERROR ON GDH INTEGRALS

- To estimate **systematic** error and provide **scale** of expected results, will arbitrary assume results follow Bianchi and Thomas Fit II.
- Total errors are small compared to expected values and total integrals.
- Can readily determine **sign and magnitude** of controversial **isovector** contribution (limit of Bjorken Sum Rule at  $Q^2 = 0$ ).

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| target            | $2\pi^2\alpha\kappa^2/M^2$ | $4 < k < 40$ GeV                  |
|-------------------|----------------------------|-----------------------------------|
| proton            | $204 \mu\text{b}$          | $-14 \pm 0.5 \pm 1.0 \mu\text{b}$ |
| neutron           | $232 \mu\text{b}$          | $14 \pm 0.8 \pm 1.0 \mu\text{b}$  |
| isoscalar (p+n)/2 | $219 \mu\text{b}$          | $0 \pm 0.4 \pm 0.7 \mu\text{b}$   |
| isovector (p-n)/2 | $-15 \mu\text{b}$          | $-28 \pm 0.4 \pm 0.7 \mu\text{b}$ |

# REQUEST

- **Two weeks** checkout (plus one week for photon beam).
- **Two months** data taking at nominal 120 Hz, assuming 50% efficiency due to PEP-II.
- **Resources** for photon beam, polarimeter, detectors, and some target equipment.
- **Collaboration** will provide much target equipment, some diamonds, and assembly of detectors.

## SUMMARY

- A solid, **fundamental experiment**, providing **baseline** for studies of spin structure of nucleon.
- Test **convergence** of isovector and isoscalar GDH Sum Rule.
- Connections to  **$g_1$**  at low  $x$ , Bjorken Sum Rule.
- **No** existing data: **surprises possible!**
- Study QCD in non-perturbative regime with one of simplest possible interactions.
- **SLAC** is only place experiment can be done  **$5 < k < 40$  GeV**.
- Energy range extends **factor 8** beyond Jefferson Lab.
- **Strong collaboration** with experience and resources needed to do experiment.