

LHC AND THE ORIGIN OF NEUTRINO MASS

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ICTP

B. Bajc, G. S., 06

B.Bajc, M. Nemevšek, G. S., 07

*In progress with A. Arhrib, B. Bajc, D. Ghosh, T. Han, G.-Y.
Huang, I. Puljak,*

With the degrees of freedom of the SM

ν masses parametrized by

Weinberg $d = 5$ effective operator

$$\mathcal{L} = Y_{ij} \frac{L_i H H L_j}{M}$$

$$\frac{v^2}{M} Y = U_{PMNS} \ m_\nu^{diag} \ U_{PMNS}^T$$

neutrino mass - Majorana

M signals the appearance of new physics

Violation of lepton number: $\Delta L = 2$

- neutrino-less double beta decay $\nu 0\beta\beta$
a text-book fact
- same sign charged lepton pairs in colliders

Keung, G.S., 83

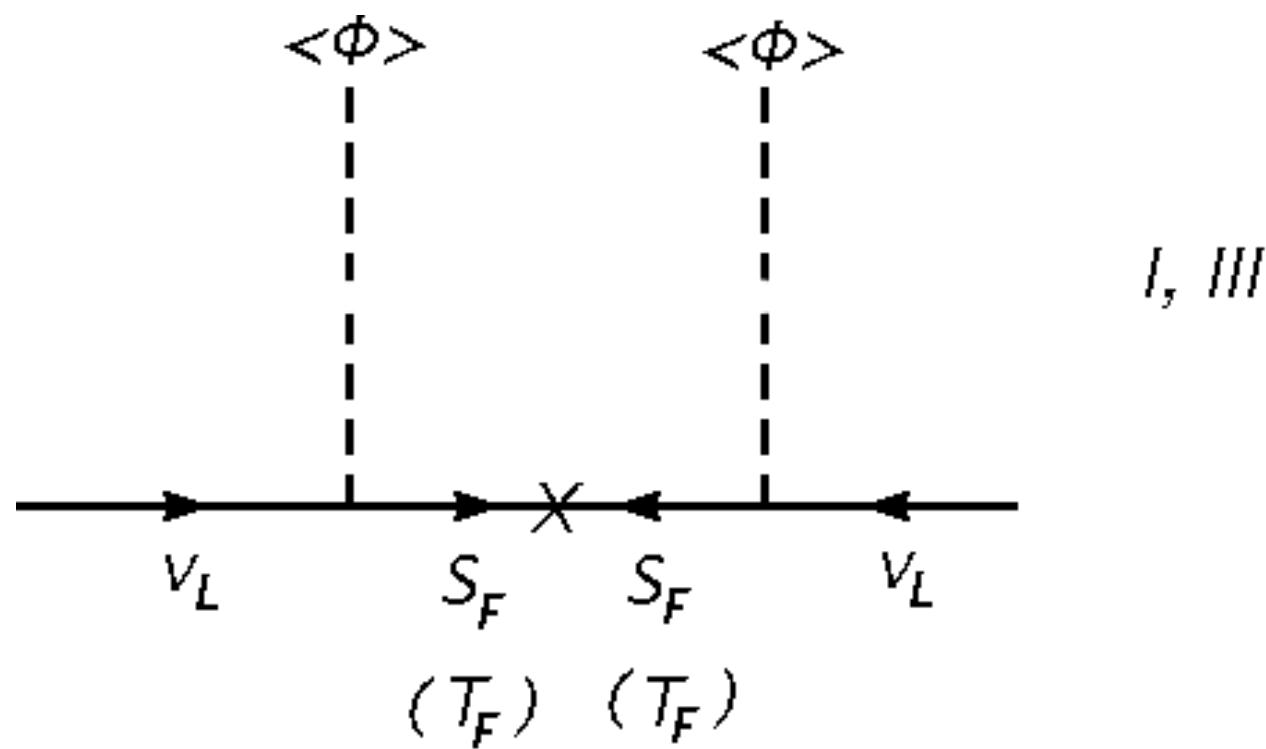
- If M is huge, no hope of direct observation of new physics
- $M = 10^{13}GeV - 10^{14}GeV$ corresponds to Y of order one
- However, small Yukawas are natural in a sense of being protected by symmetries.
- Keep M free and look for theoretical predictions (grand unification)

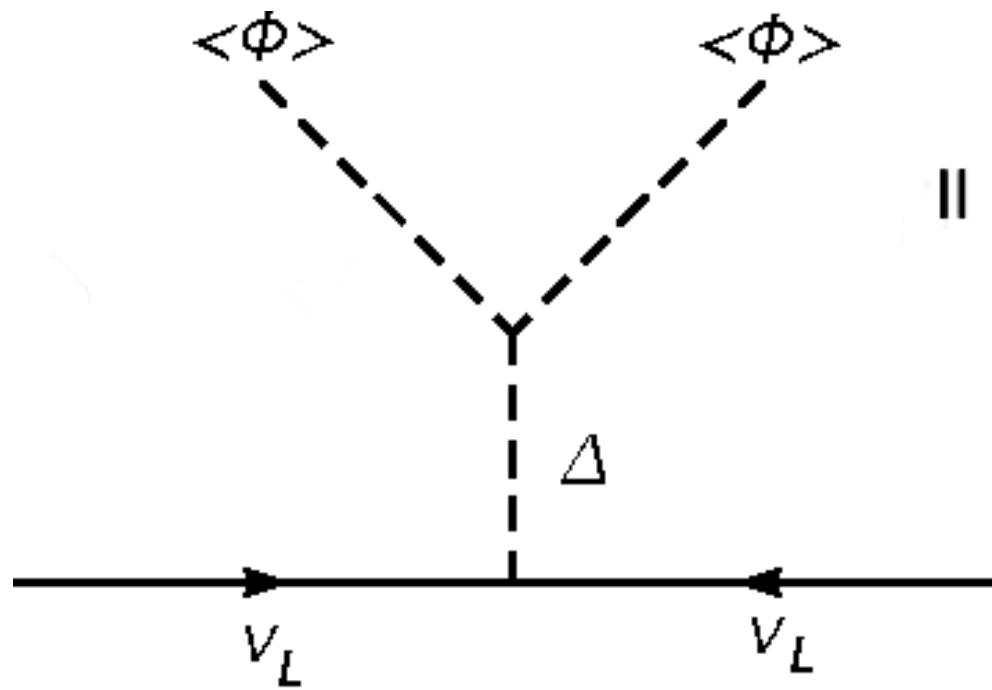
Only 3 ways of producing the Weinberg operator

By exchange of heavy

- fermion singlet ($1_C, 1_W, Y = 0$) TYPE I SEESAW
Minkowski, 77
 - boson weak triplet ($1_C, 3_W, Y = 2$) TYPE II SEESAW
Lazarides et al, 80
Mohapatra, Senjanović, 80
 - fermion weak triplet ($1_C, 3_W, Y = 0$) TYPE III SEESAW
Foot et al, 86

I and II very well studied, III almost ignored in the past





All this by itself not more useful than just Weinberg operator
unless

- we can reach the scale M , interesting only for low M
- we have a theory of these singlets, triplets (GUT for example)

This reminiscent of the Fermi theory of low energy weak interactions:

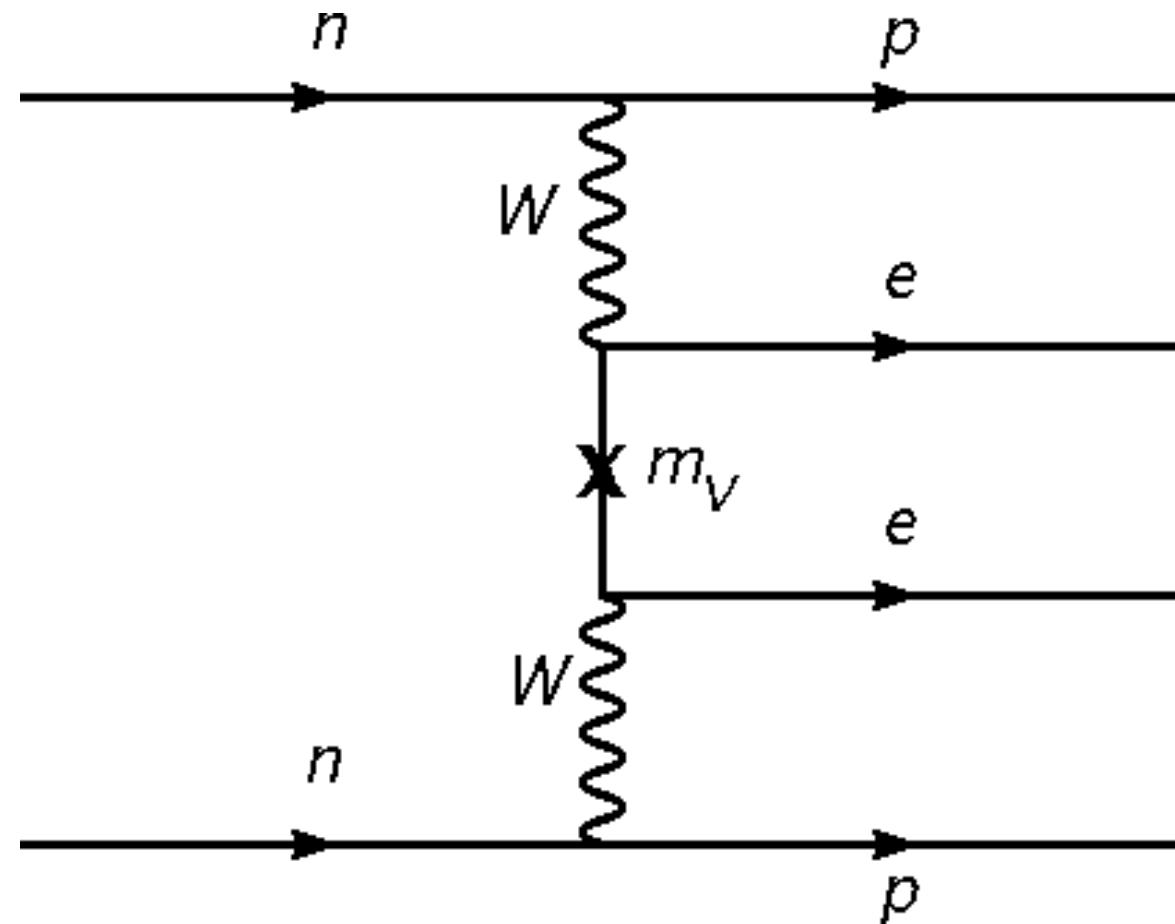
saying that the four fermion interactions can be described by the exchange of a new particle (W boson) not useful except

- when you can reach the new scale (M_W)
- you have a theory of this new particle: $SU(2)_L \times U(1)$ Standard Model gauge theory

that correlates different processes at low energies $E \ll M_W$

ν mass window to new physics - if Majorana

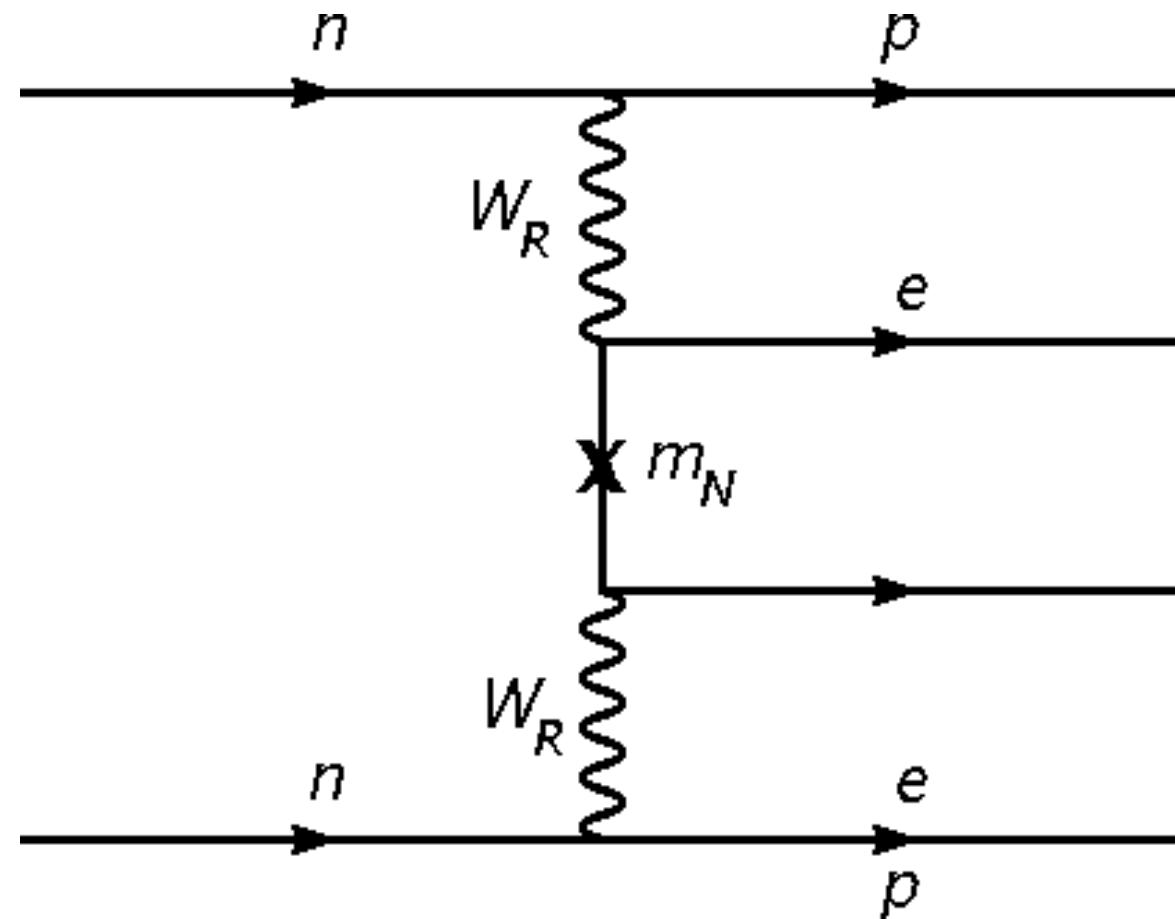
- Dirac case complete - new physics not necessary
- SM with Majorana neutrino not complete
- Majorana case connects m_ν to different new phenomena like $\nu 0\beta\beta$ decay



in general m_ν , not directly connected to $\nu 0\beta\beta$ decay: depends on
the completion

Example:

LR symmetry with low W_R , ν_R masses has a nonzero $\nu 0\beta\beta$ decay
even with $y_D, m_\nu \rightarrow 0$

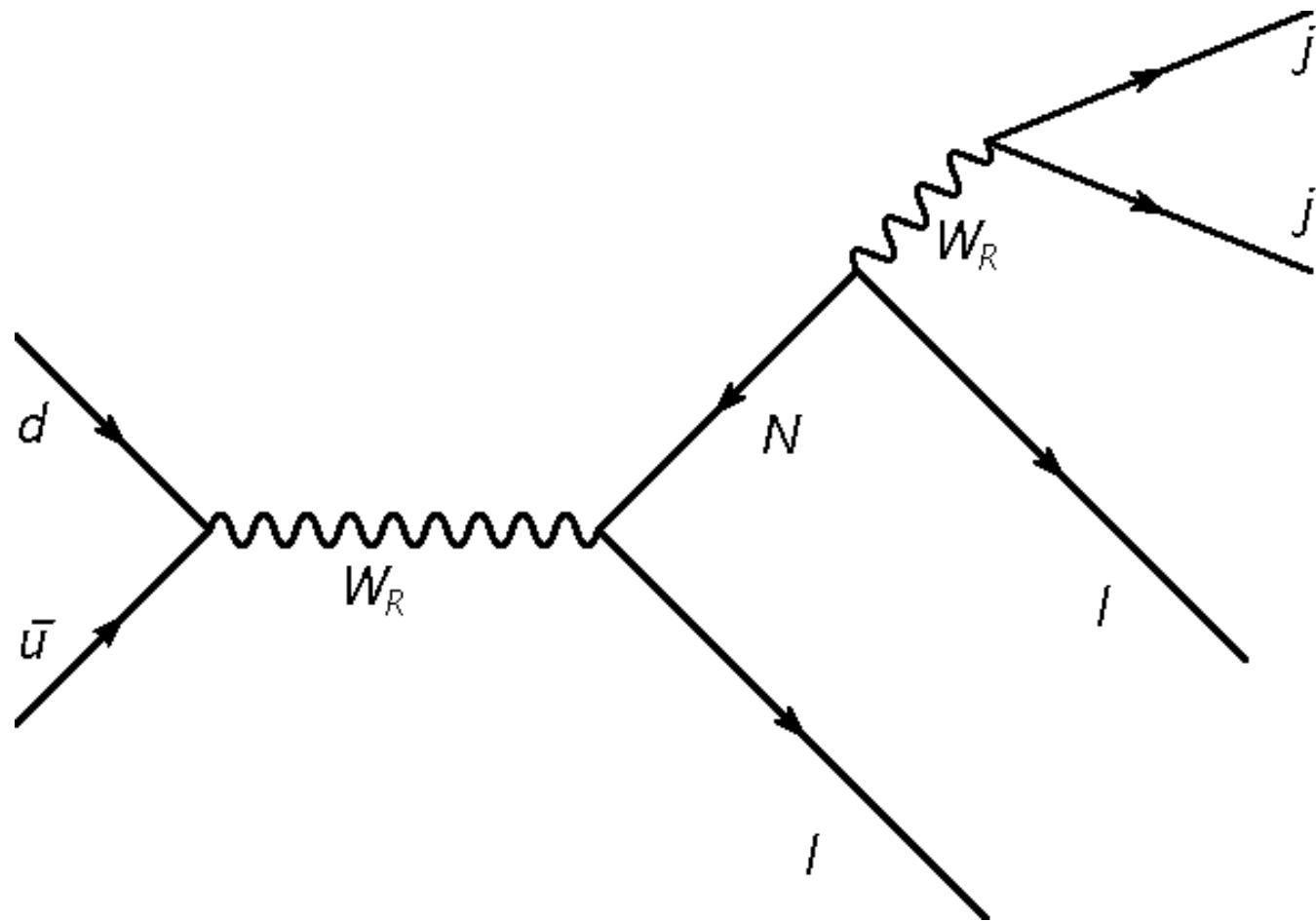


This is why it is important for the see-saw to be traced in colliders:
measure $\Delta L = 2$ operators not only in $\nu 0\beta\beta$ decays, but also in
colliders

Keung, Senjanović, 83

L-R symmetric theories: $SU(2_L) \times SU(2_R) \times U(1)$ gauge theory

- ν_L implies ν_R
- Type I seesaw: connects neutrino mass to scale of parity restoration
- colliders: produce W_R through Drell-Yan



- direct test of parity restoration
- direct test of lepton number violation
- determination of W_R and N masses

Ferrari et al, 99

Gninenko et al, 07

LHC easily probes W_R up to 3-4 TeV and ν_R in 100 - 1000 GeV

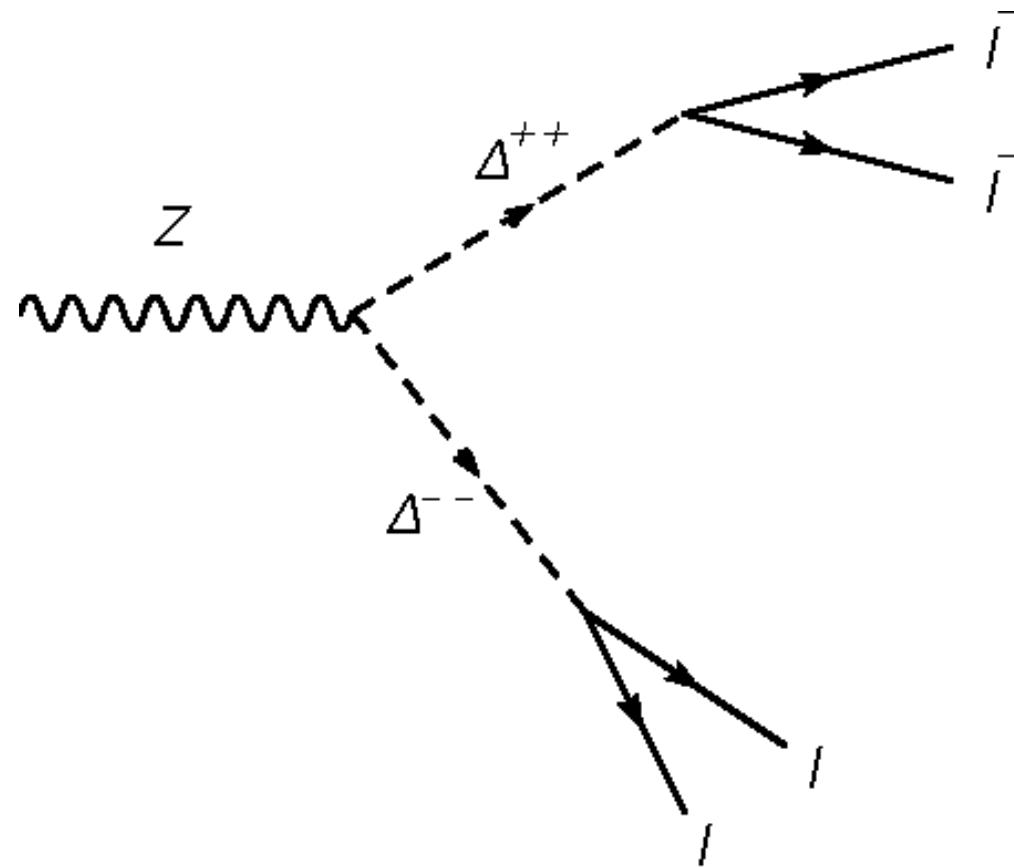
L-R theory: also type II

Type II: pair production of doubly charged Higgses, which decay into same sign lepton (anti lepton) pairs

$$M_\nu = Y_\Delta v_\Delta$$

probe directly M_ν if no type I

Kadastik, Raidal, Rebane, 07 and references therein



Datta, Guchait, Pilaftsis, 93

Datta, Guchait, Roy, 93

Ferrari et al, 99

Han, Zhang, 06

Gninenko et al, 07

del Aguila, Aguilar-Saveedra, Pittau, 07

del Aguila, Aguilar-Saveedra, 07

Han et al, 07

Akeroyd, Aoki, Sugiyama, 07

Fileviez Perez et al, 07

Kadastik, Raidal, Rebane, 07

Kersten and Smirnov, 07

Chao et al, 08

Franceschini, Hambye, Strumia, 08

Fileviez Perez et al, 08

many more in type I and also type II

Interesting theories:

$$m_{Dirac} \ll M_{\nu_R} \quad (\text{see-saw})$$

$$M_{\nu_R}, M_{W_R} \sim \mathcal{O}(1 - 10) \text{ TeV}$$

Handle on a see-saw scale form grand unification : SO(10) theory

- SO(10) unifies a family of fermions and postulates right-handed neutrinos
- has L-R symmetry in a form of charge conjugation of Dirac
- naturally both type I and II seesaw

- usually no low scale from running
- typically $Y_{Dirac} \sim Y_{top}$: fits with $M_R \sim 10^{14} GeV$

Such theories have a natural see-saw mechanism

(m_ν and $\nu 0\beta\beta$ well described)

but no low see-saw scale

(no $\Delta L = 2$ in colliders)

Take for example the SO(10) model with Yukawas

$$\mathcal{L}_Y = 16_F^i \left(Y_{10}^{ij} 10_H + Y_{126}^{ij} 126_H \right) 16_F^j$$

Lazarides, Shafi, Wetterich, 81

Babu, Mohapatra, 92

Bajc, Senjanović, Vissani, 02

Only two 3×3 symmetric Yukawa matrices

Y_{10} and Y_{126}

to describe all light fermions (m_d, m_u, m_e, m_ν)

Full theory with such Yukawas for example in the minimal renormalizable supersymmetric $\text{SO}(10)$:

- three copies of 16_F
- $210_H, 126_H, \overline{126}_H, 10_H$

Clark, Kuo, Nakagawa, 83

Aulakh, Mohapatra, 83

Aulakh, Bajc, Melfo, Senjanović, Vissani, 04

The theory over constrained and quite predictive

Some evidence that constraints from Higgs sector and Yukawa sector are in contradiction

Aulakh, 05, 06

Bajc, Melfo, Senjanović, Vissani, 05

Bertolini, Malinsky, Schwetz, 06

Although some new hope for consistent fit comes from recent (yet unpublished) results

Doršner, Nemevšek, to appear

possibility: relate proton decay branching ratios to neutrino masses and mixings.

Even with new physics - only indirect

Simple predictive GUT candidate with measurable seesaw?

MINIMAL SU(5)

The minimal Georgi-Glashow model ruled out because

$$\text{Minimal: } 24_H + 5_H + 3(10_F + \bar{5}_F)$$

1. **gauge couplings do not unify**
 - 2 and 3 meet at 10^{16} GeV (as in susy),
 - but 1 meets 2 too early at $\approx 10^{13}$ GeV
2. **neutrinos massless** (as in the SM)

Add just one extra fermionic 24_F

New Yukawa terms (higher dimensional operators a must as in the minimal model)

$$\mathcal{L}_{Y\nu} = y_0^i \bar{5}_F^i 24_F 5_H + \frac{1}{\Lambda} \bar{5}_F^i (y_1^i 24_F 24_H + \dots) 5_H + h.c.$$

Under $SU(3)_C \times SU(2)_W \times U(1)_Y$ decomposition

$$24_F = (1, 1)_0 + (1, 3)_0 + (8, 1)_0 + (3, 2)_{5/6} + (\bar{3}, 2)_{-5/6}$$

singlet $S = (1, 1)_0$

triplet $T = (1, 3)_0$

$$\mathcal{L}_{Y\nu} = L_i \left(y_T^i T + y_S^i S \right) H + h.c.$$

Mixed Type I and Type III seesaw:

$$(M_\nu)^{ij} = v^2 \left(\frac{y_T^i y_T^j}{m_T} + \frac{y_S^i y_S^j}{m_S} \right)$$

→ one massless neutrino

The only possible pattern:

$$m_3 \ll m_8 \ll m_{(3,2)} \ll M_{GUT}$$

A solution

$$m_3 = 10^2 \text{GeV}$$

$$m_8 = 10^7 \text{GeV}$$

$$m_{(3,2)} = 10^{14} \text{GeV}$$

$$M_{GUT} = 10^{16} \text{GeV}$$

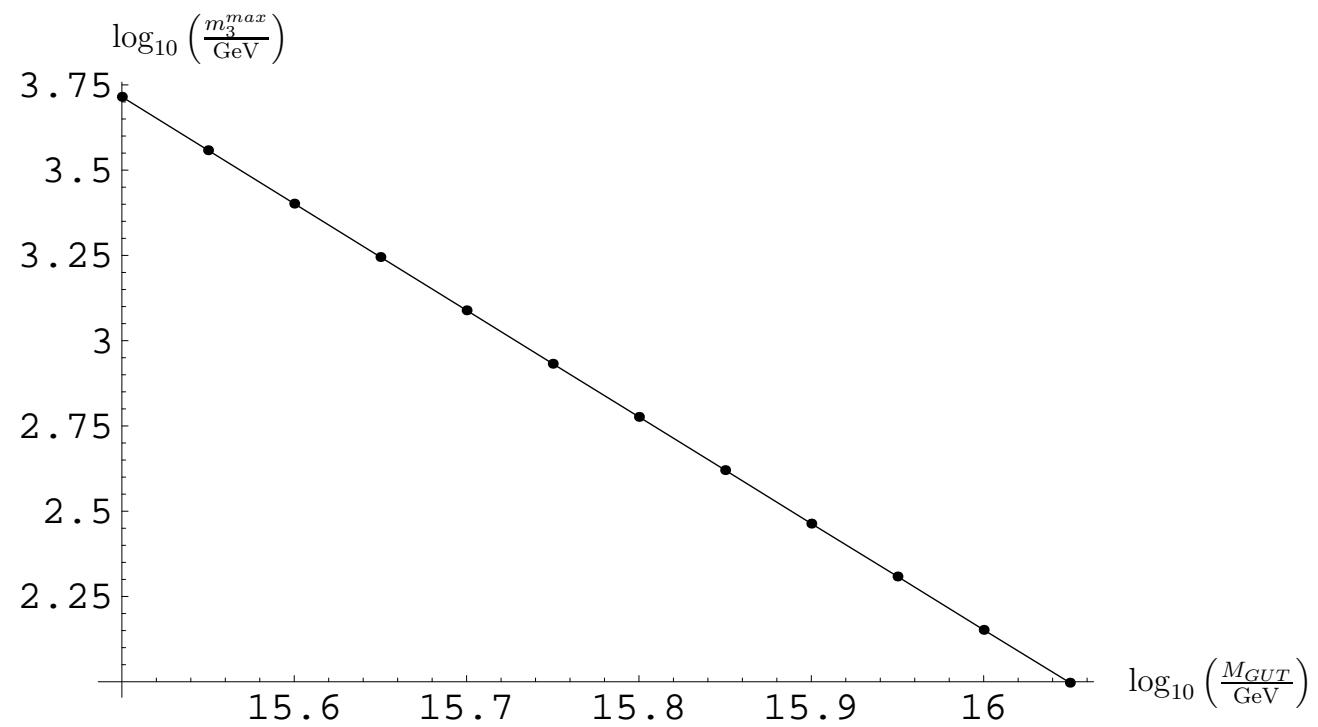
1-loop result:

For $M_{GUT} \gtrsim 10^{15.5}$ GeV (p decay)

$\rightarrow m_3 \lesssim 1\text{TeV}$

Prediction of the model

$m_3^{max} - M_{GUT}$ at two loops



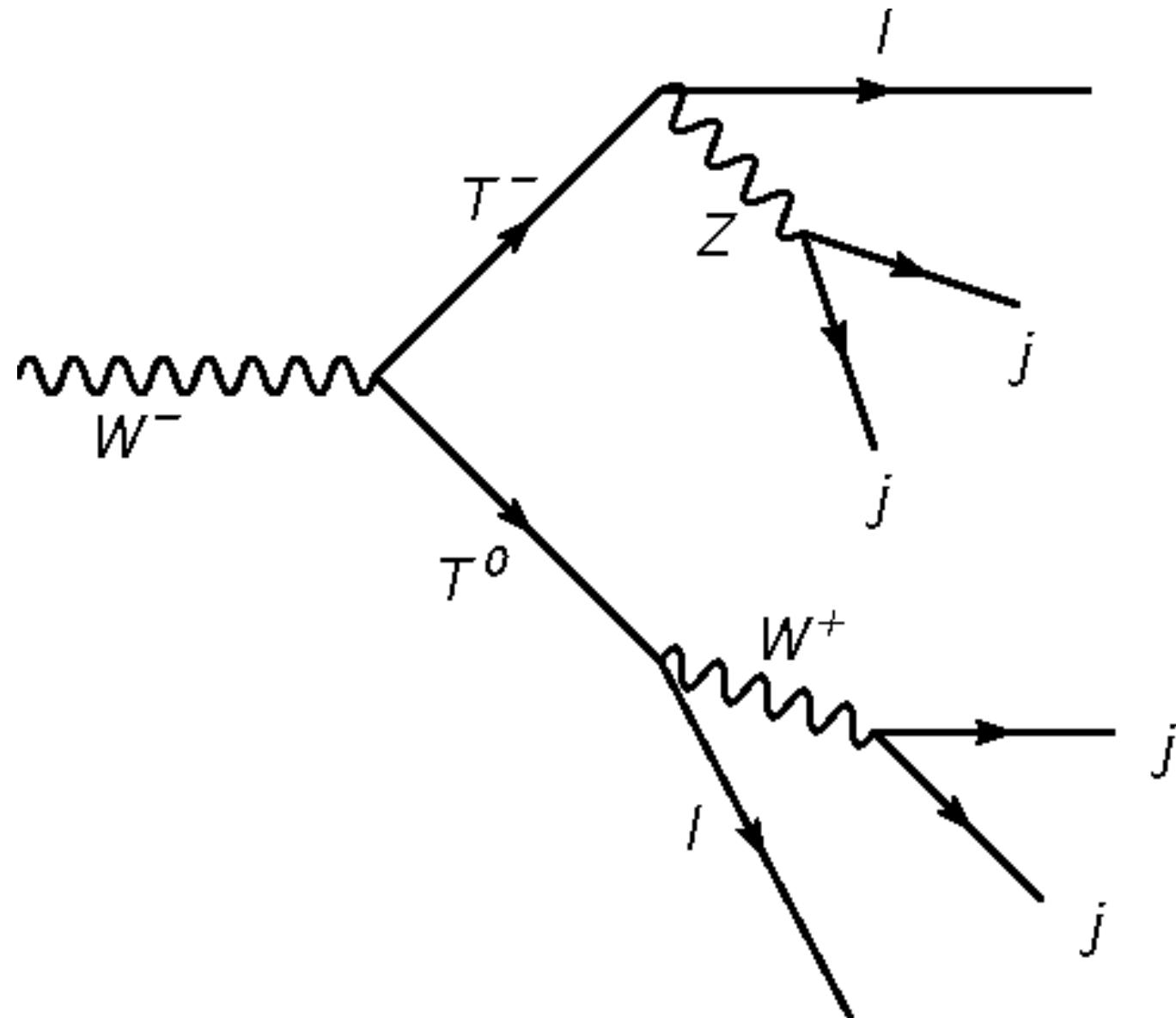
T at LHC ?

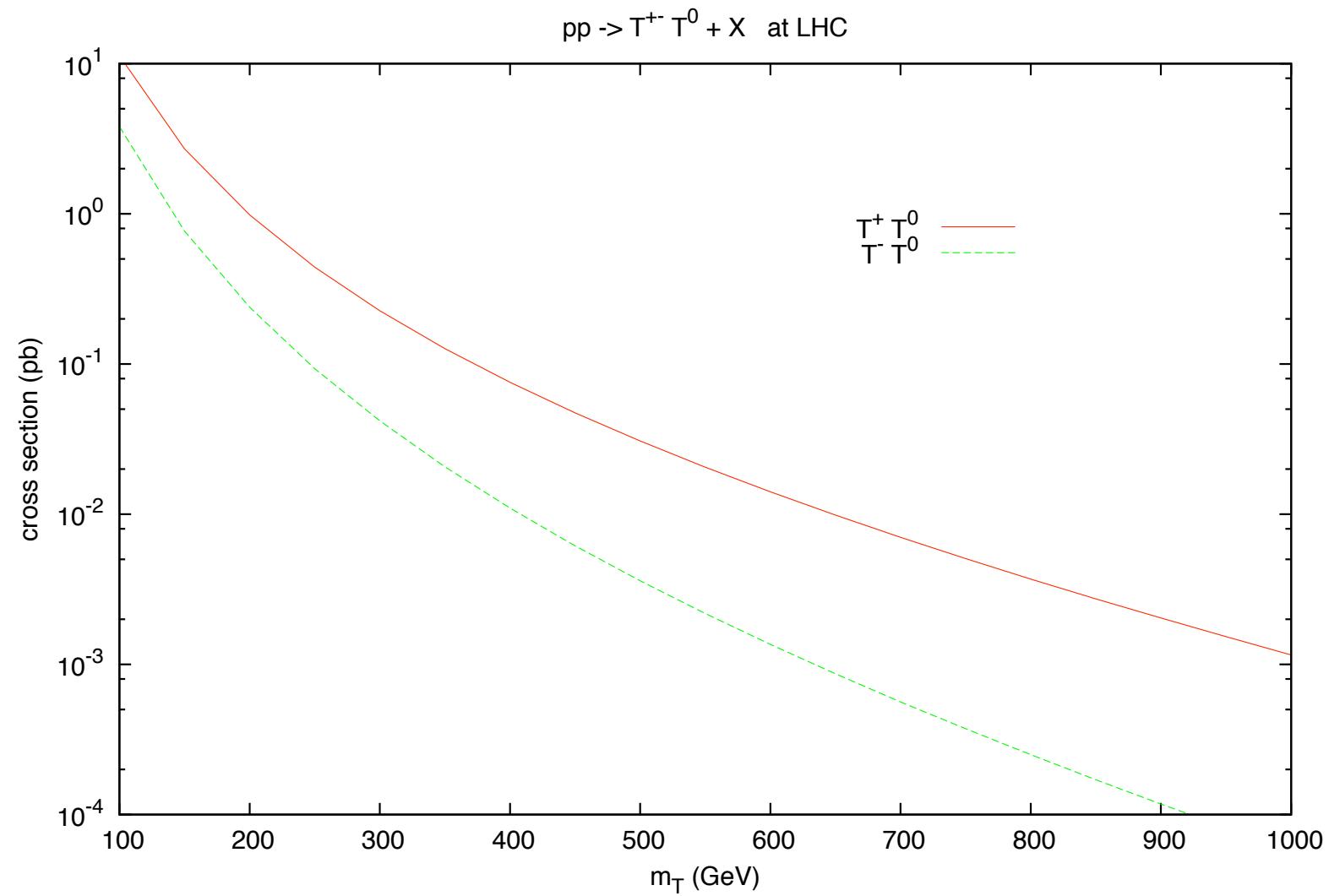
$T^{0,\pm}$ weak triplet

→ produced through gauge interactions
(Drell-Yan)

$$pp \rightarrow W^\pm + X \rightarrow T^\pm T^0 + X$$

$$pp \rightarrow (Z \text{ or } \gamma) + X \rightarrow T^+ T^- + X$$





$$\Gamma_T \approx m_T |y_T|^2$$

The best channel is like-sign dileptons + jets

$$BR(T^\pm T^0 \rightarrow l_i^\pm l_j^\pm + 4 \text{ jets}) \approx \frac{1}{20} \times \frac{|y_T^i|^2 |y_T^j|^2}{(\sum_k |y_T^k|^2)^2}$$

Same couplings y_T^i contribute to

- ν mass matrix and
- T decays

Normal hierarchy:

$$\frac{vy_T^{i*}}{\sqrt{2}} = i\sqrt{m_T} \left(U_{i2}\sqrt{m_2^\nu} \cos z \pm U_{i3}\sqrt{m_3^\nu} \sin z \right)$$

Inverse hierarchy:

$$\frac{vy_T^{i*}}{\sqrt{2}} = i\sqrt{m_T} \left(U_{i1}\sqrt{m_1^\nu} \cos z \pm U_{i2}\sqrt{m_2^\nu} \sin z \right)$$

U = PMNS matrix, z = arbitrary complex number

Ibarra, Ross, 03

Measuring T decays \rightarrow constraints on z (θ_{13} , phases)

exp. limit: $m_T \gtrsim m_Z$

Total decay width of T^\pm , T^0

$$\Gamma_T = \frac{m_T}{32\pi} \left(\sum_k |y_T^k|^2 \right) \left[2f_1 \left(\frac{m_W}{m_T} \right) + f_1 \left(\frac{m_Z}{m_T} \right) + f_0 \left(\frac{m_H}{m_T} \right) \right]$$

$$f_n(x) = (1 - x^2)^2(1 + 2nx)$$

From the general parametrization above

$$\sum_k |y_T^k|^2 \geq \frac{m_T}{v^2} \sqrt{\Delta m_S^2} \quad (\text{normal hierarchy})$$

$$\sum_k |y_T^k|^2 \geq \frac{m_T}{v^2} \sqrt{\Delta m_A^2} \quad (\text{inverse hierarchy})$$

Upper limit on total triplet lifetime

$$\tau_T \lesssim 2 \left(\frac{100 \text{ GeV}}{m_T} \right)^2 \text{ mm} \quad (\text{normal hierarchy})$$

(and $\sqrt{\Delta m_A^2 / \Delta m_S^2} \approx 5$ times smaller for inverse hierarchy)

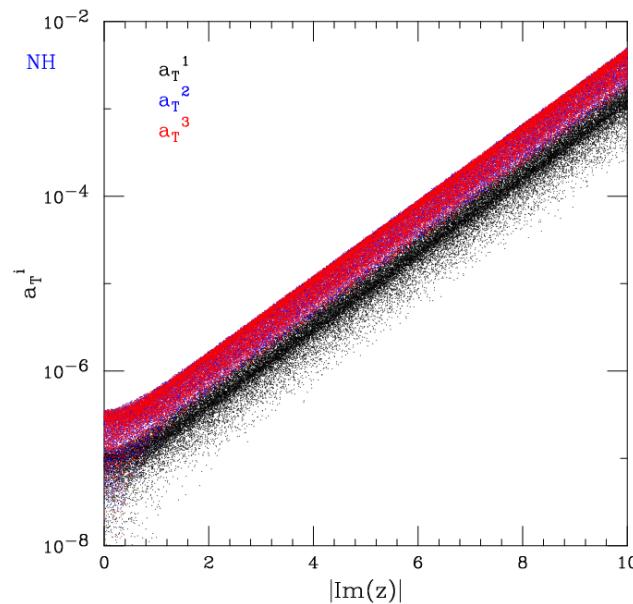
Measure lifetime?

But should be easier to measure

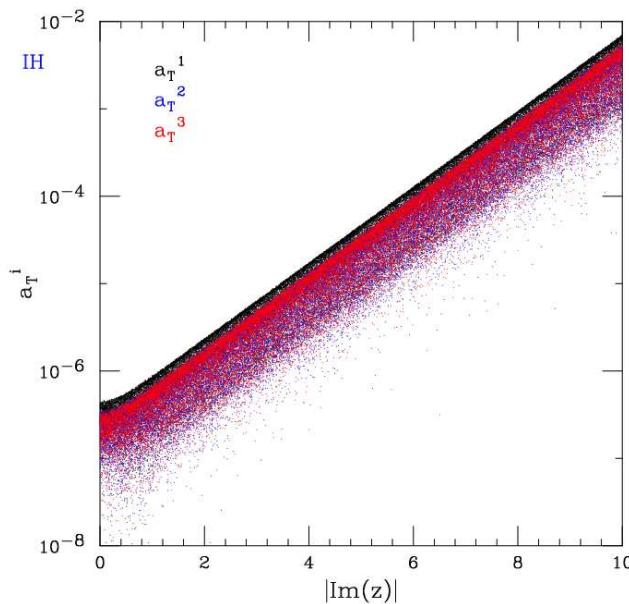
- slower decay modes
- branching ratios

$|y_T^k|$ from $\tau(T \rightarrow l_k jj)$ are partially correlated (connected by unknown complex z and not yet measured θ_{13} and phases δ, Φ in U_{PMNS})

Scanning over whole parameter space

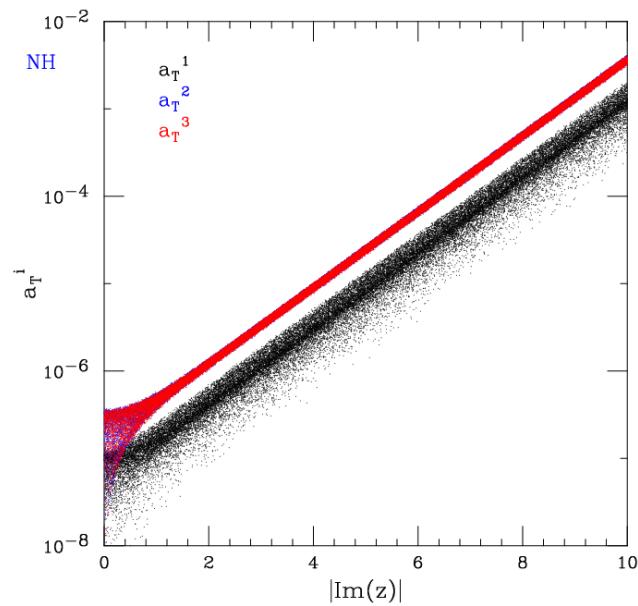


normal hierarchy

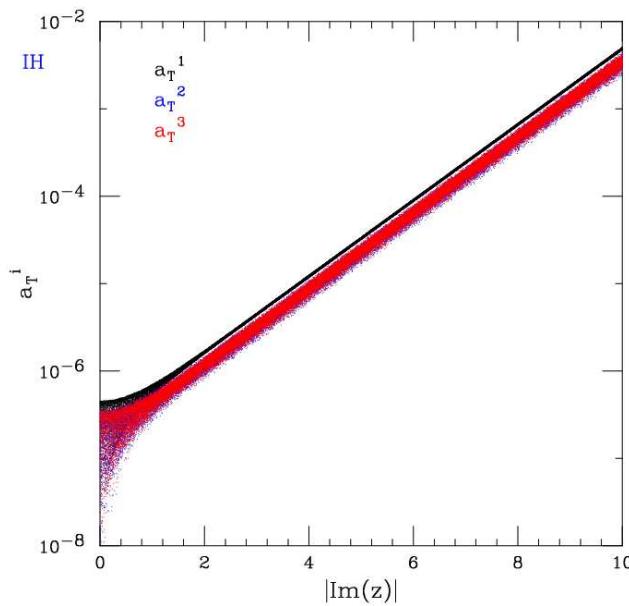


inverse hierarchy

Assuming Majorana phase $\Phi = 0$



normal hierarchy



inverse hierarchy

SM background:

in ideal detectors is 0 (no $\Delta L = 2$ in SM)

But real life not ideal

Background mainly from

- $t\bar{t}nj:$

$$\begin{aligned} t &\rightarrow W^+ b \\ \bar{t} &\rightarrow W^- (\bar{b} \rightarrow W^+ \bar{q}) \end{aligned}$$

- $b\bar{b}nj:$

$$\begin{aligned} b &\rightarrow W^- (q \rightarrow W^+ q') \\ \bar{b} &\rightarrow W^+ \bar{q}'' \end{aligned}$$

$W^+ \rightarrow l^+ \nu$ produce final states $\rightarrow l^+ l^+ 4j +$ missing energy

Cross sections huge (QCD), but phase space fortunately small

- neutrinos must carry small transverse energy
- a lepton and two jets near a hypothetical m_T

Other important non-QCD modes

- $W^+ W^+ n_j$
- $W^+ Z n_j$

$$Z \rightarrow q(\bar{q} \rightarrow W^+ \bar{q}')$$

Some estimates:

with just very loose cuts: $\sigma_{background} \approx \mathcal{O}(10 - 100)$ fb

Different for different final states (e^+ , μ^+ or τ^+)

Del Aguila, Aguilar-Saavedra, 07

Seems under control ($\sigma_{background} \lesssim 1$ fb) with better cuts

Franceschini, Hambye, Strumia, 08

Cuts in general influence the signal as well

Incremental increase of cuts on the signal ($m_T = 400$ GeV):

$$\sigma_{signal} = 34.37 \text{ fb without any cuts}$$

Cuts ↓	$\sigma_{\text{sig.}}(\text{fb})$
$p_T(\ell) > 30(\text{GeV})$	33.50
$p_T(jets) > 20 \text{ (GeV)}$	21.96
$ \eta(\ell) < 2.5$	19.68
$ \eta(jets) < 3$	18.57
$\Delta R_{\ell\ell} > 0.3$	18.42
$\Delta R_{\ell j} > 0.4$	17.20
$\Delta R_{jj} > 0.7$	7.33

Arhrib, Bajc, Ghosh, Han, Huang, Puljak, Senjanović, to appear

Conclusions

- experimental probe of (Majorana) neutrino mass origin: lepton number violation at LHC (same sign dileptons), a high energy analogue of neutrino-less double beta decay
- an explicit example of predictive GUT theory: ordinary minimal SU(5) with extra fermionic adjoint
- weak fermionic triplet predicted in the TeV range (type III)
- its decay connected with neutrino mass
- good chances to find it at LHC
- possible even to get information on unmeasured neutrino parameters

R measures separations

$$R = [(\Delta\phi)^2 + (\Delta\eta)^2]^{1/2}$$

where $\Delta\phi$ and $\Delta\eta$ are the azimuthal angular separation and (pseudo) rapidity difference between two particles