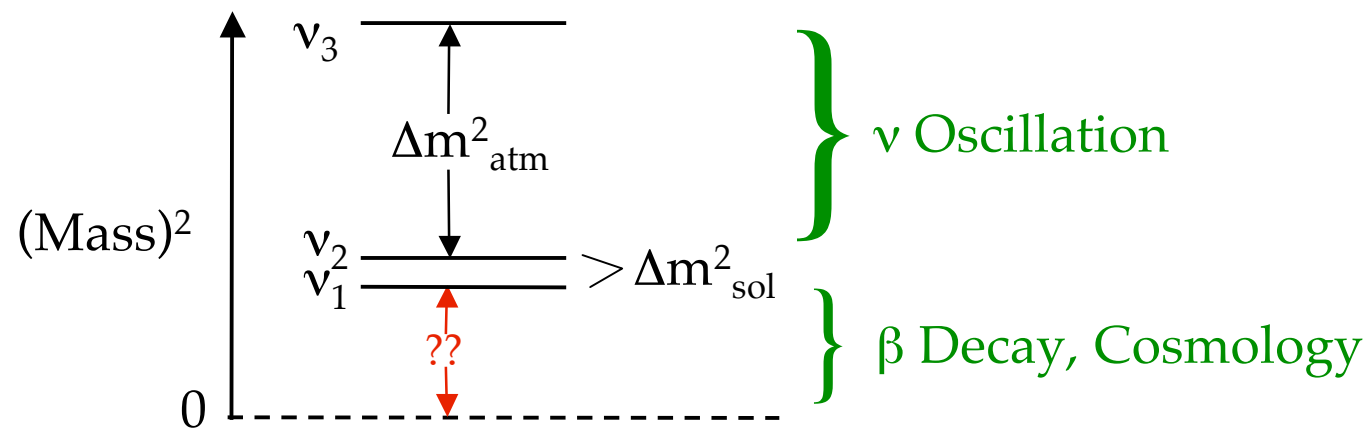




Neutrino Properties

Boris Kayser
Neutrino 2008
May 28, 2008

What Is the Absolute Scale of Neutrino Mass?



How far above zero
is the whole pattern?

Oscillation Data

➡ $\text{Mass}[\text{Heaviest } \nu_i] > \sqrt{\Delta m^2_{\text{atm}}} \cong 0.05 \text{ eV}$

A Cosmic Connection

Cosmological Data + Cosmological Assumptions \longrightarrow

$$\Sigma m_i < (0.17 - 1.0) \text{ eV} .$$

Mass(ν_i) \uparrow (Seljak, Slosar, McDonald)
Pastor

If there are only 3 neutrinos,

$$0.05 \text{ eV} \lesssim \text{Mass}[\text{Heaviest } \nu_i] < (0.07 - 0.4) \text{ eV}$$

\uparrow $\sqrt{\Delta m^2_{\text{atm}}}$

Cosmology \uparrow

The *cosmological assumptions* seem reasonable, but are not guaranteed. A *laboratory determination* of the absolute ν mass scale will be essential.

Does $\bar{v} = v$?

What Is the Question?

For each *mass eigenstate* ν_i , and *given helicity* h ,
does —

- $\overline{\nu}_i(h) = \nu_i(h)$ (Majorana neutrinos)

or

- $\overline{\nu}_i(h) \neq \nu_i(h)$ (Dirac neutrinos) ?

Equivalently, do neutrinos have *Majorana masses*? If they do, then the mass eigenstates are *Majorana neutrinos*.

Majorana Masses

Out of, say, a left-handed neutrino field, ν_L , and its charge-conjugate, ν_L^c , we can build a Left-Handed Majorana mass term —

$$m_L \overline{\nu_L} \nu_L^c$$


Majorana masses do not conserve the Lepton Number L defined by —

$$L(\nu) = L(\ell^-) = -L(\bar{\nu}) = -L(\ell^+) = 1.$$

A Majorana mass for any fermion f causes $f \leftrightarrow \bar{f}$.

Quark and *charged-lepton* Majorana masses are forbidden by electric charge conservation.

Neutrino Majorana masses would make the neutrinos *very* distinctive.

Majorana ν masses cannot come from $H_{SM} \bar{\nu}_R \nu_L$, the analogue of the q and ℓ mass terms.

Possible Majorana mass terms:

$$\underbrace{H_{SM} H_{SM} \overline{\nu_L^c} \nu_L}_{\text{Not renormalizable}}, \quad \underbrace{H_{I_W=1} \overline{\nu_L^c} \nu_L}_{\left\{ \begin{array}{l} \text{This Higgs} \\ \text{not in SM} \end{array} \right\}}, \quad \underbrace{m_R \overline{\nu_R^c} \nu_R}_{\text{No Higgs}}$$

Majorana neutrino masses must have a different origin than the masses of quarks and charged leptons.

Why Majorana Masses \longrightarrow Majorana Neutrinos

The objects ν_L and ν_L^c in $m_L \overline{\nu_L} \nu_L^c$ are not the mass eigenstates, but just the neutrinos in terms of which the model is constructed.

$m_L \overline{\nu_L} \nu_L^c$ induces $\nu_L \longleftrightarrow \nu_L^c$ mixing.

As a result of $K^0 \longleftrightarrow \overline{K}^0$ mixing, the neutral K mass eigenstates are —

$$K_{S,L} \cong (K^0 \pm \overline{K}^0)/\sqrt{2} . \quad \overline{K_{S,L}} = K_{S,L} .$$

As a result of $\nu_L \longleftrightarrow \nu_L^c$ mixing, the neutrino mass eigenstate is —

$$\nu_i = \nu_L + \nu_L^c = “\nu + \overline{\nu}” . \quad \overline{\nu_i} = \nu_i .$$

Why Most Theorists Expect Majorana Masses

The Standard Model (SM) is defined by the fields it contains, its **symmetries** (notably weak isospin invariance), and its renormalizability.

Leaving neutrino masses aside, anything allowed by the SM symmetries occurs in nature.

Since $I_W(\nu_R) = 0$, *Right-Handed Majorana mass terms* $m_R \overline{\nu_R^c} \nu_R$ are allowed by the SM symmetries.

Then quite likely *Majorana masses* occur in nature too.

To Determine
Whether
Majorana Masses
Occur in Nature

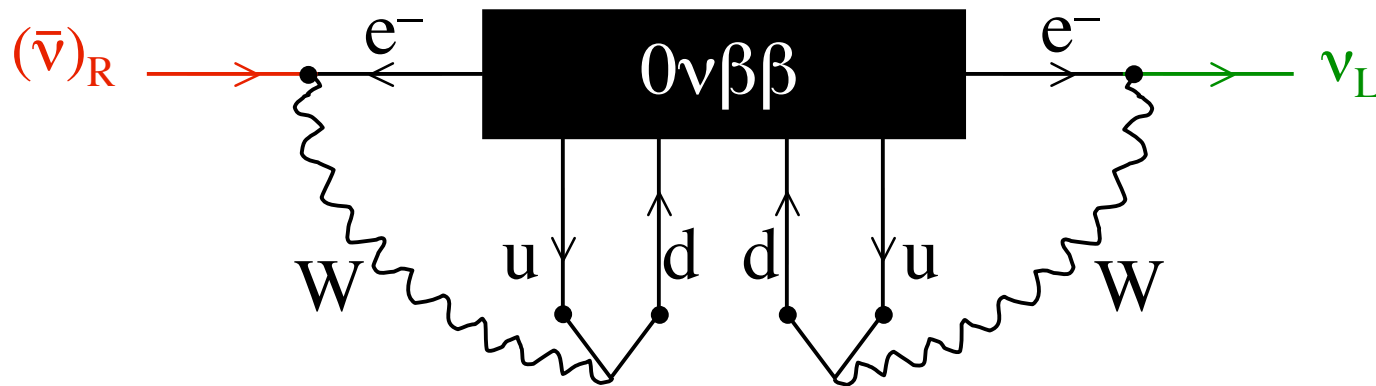
The Promising Approach — Seek Neutrinoless Double Beta Decay $[0\nu\beta\beta]$



We are looking for a *small* Majorana neutrino mass. Thus, we will need *a lot* of parent nuclei (say, one ton of them).

Whatever diagrams cause $0\nu\beta\beta$, its observation would imply the existence of a Majorana mass term:

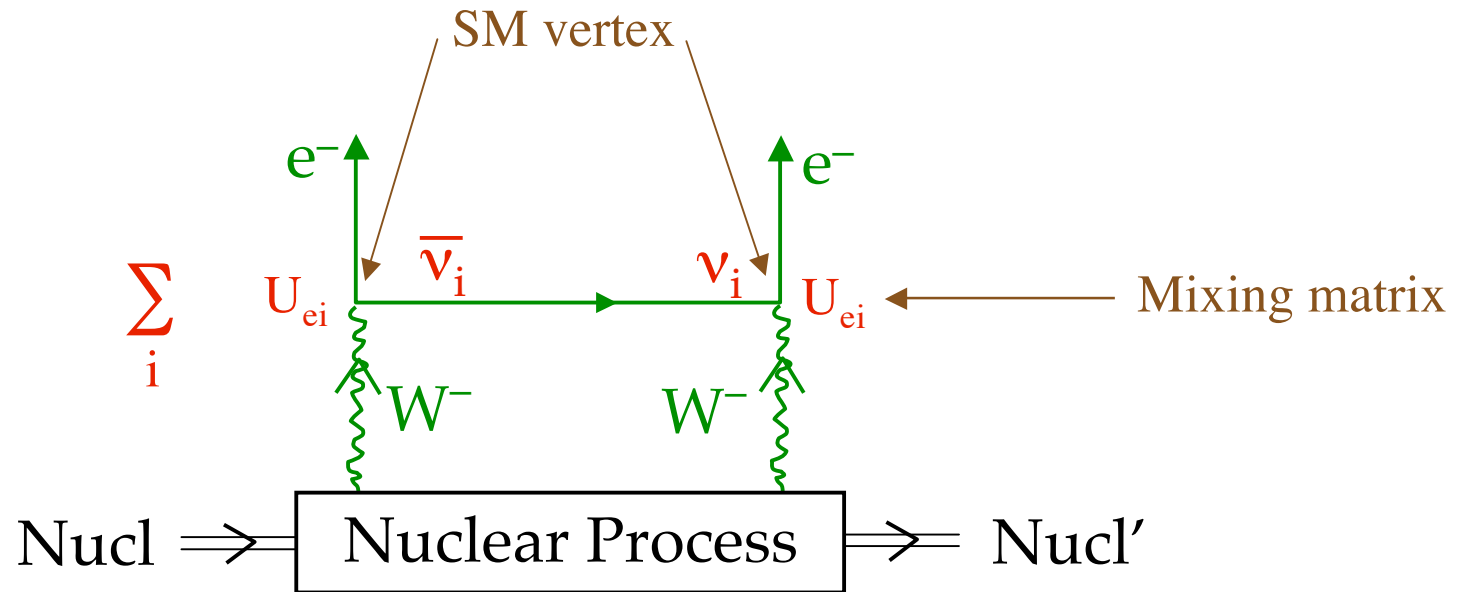
(Schechter and Valle)



$(\bar{\nu})_R \rightarrow \nu_L$: A (tiny) Majorana mass term

$\therefore 0\nu\beta\beta \rightarrow \bar{\nu}_i = \nu_i$

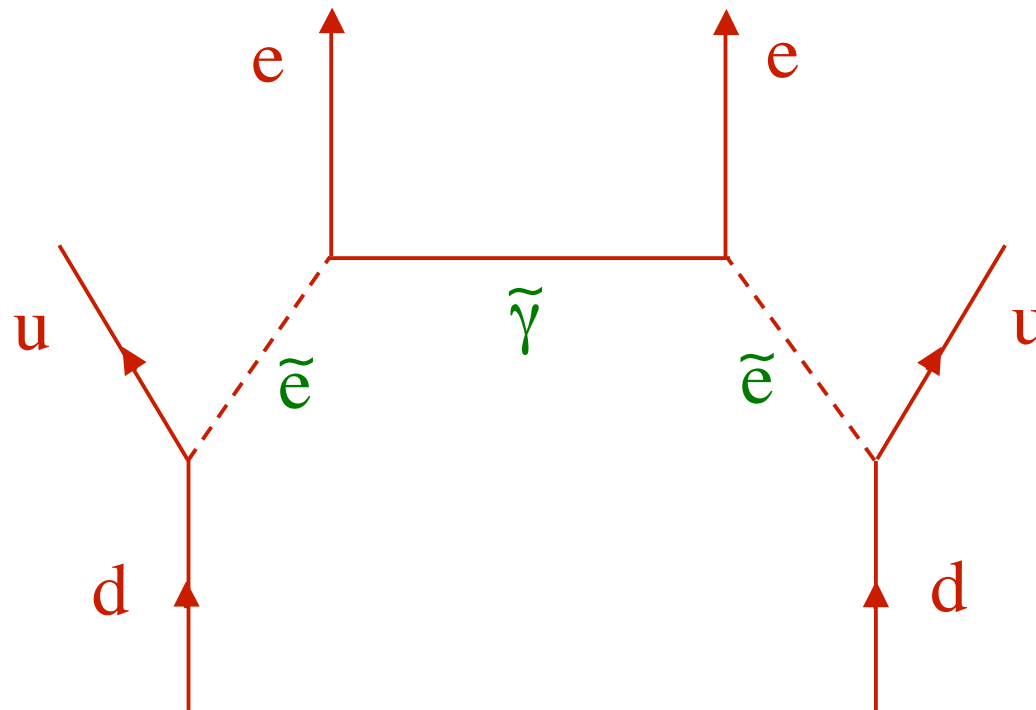
We anticipate that $0\nu\beta\beta$ is dominated by a diagram with Standard Model vertices:



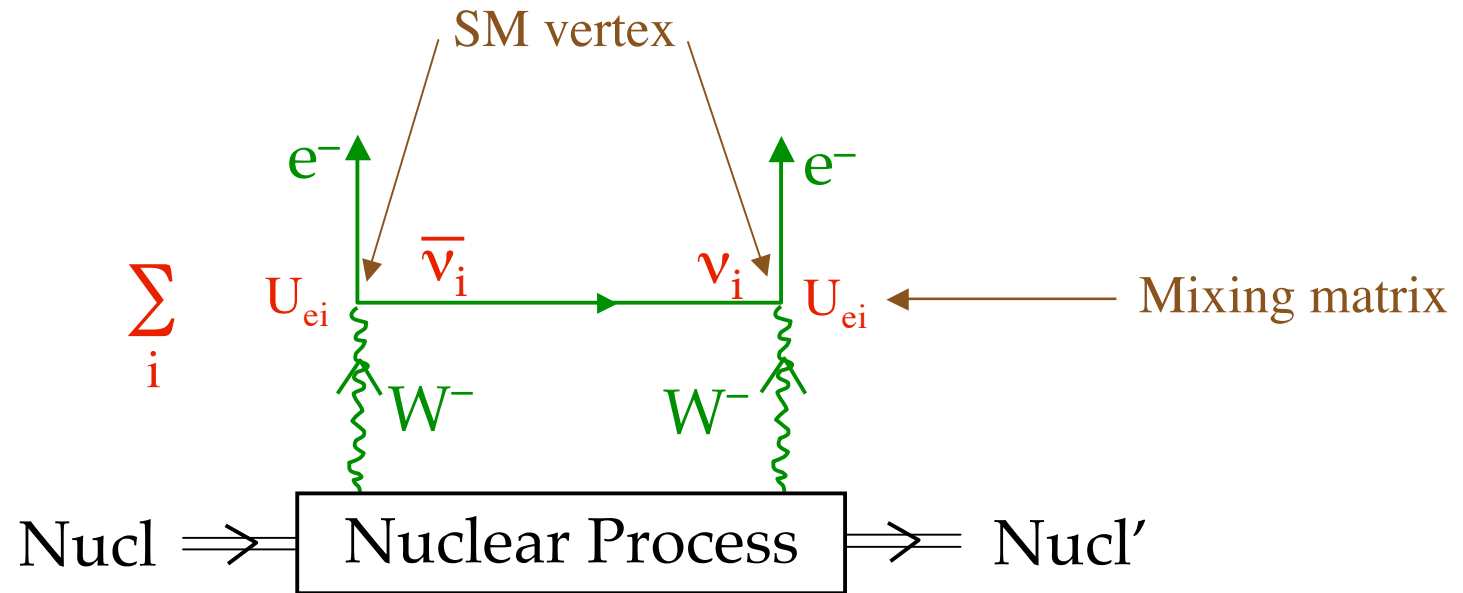
But there could be other contributions to $0\nu\beta\beta$,
which at the quark level is the process

$$dd \rightarrow uuee.$$

An example from Supersymmetry:



If the dominant mechanism is —



then —

$$\text{Amp}[0\nu\beta\beta] \propto \left| \sum_i m_i U_{ei}^2 \right| \equiv m_{\beta\beta}$$

Mass (ν_i)

Why $\text{Amp}[0\nu\beta\beta]$ Is \propto Neutrino Mass

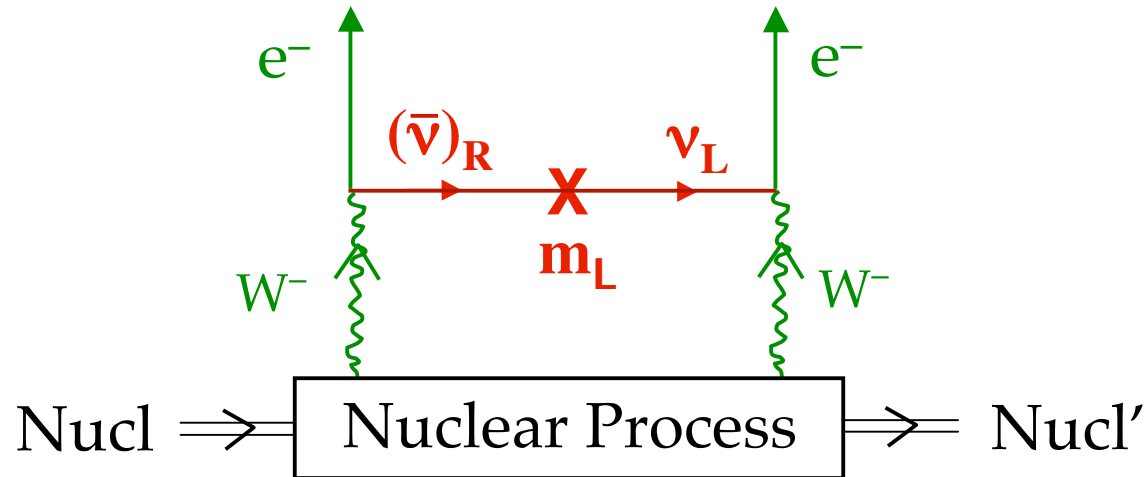


— manifestly does not conserve L.

But the Standard Model (SM) weak interactions *do* conserve L. Absent any non-SM L-violating interactions, the $\Delta L = 2$ of $0\nu\beta\beta$ can only come from *Majorana neutrino masses*, such as —

$$m_L (\overline{\nu}_L^c \nu_L + \overline{\nu}_L \nu_L^c) \quad \begin{array}{c} (\bar{\nu})_R \xrightarrow{\quad} \text{X} \xrightarrow{\quad} \nu_L \\ m_L \end{array}$$

Treating the neutrino masses perturbatively,
we have —



A Left-Handed Majorana mass term is just what
is needed to —

- 1) Violate L
- 2) Flip handedness

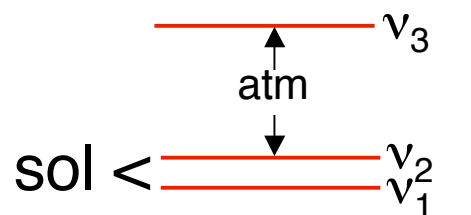
— and allow the decay to occur.

How Large is $m_{\beta\beta}$?

How sensitive need an experiment be?

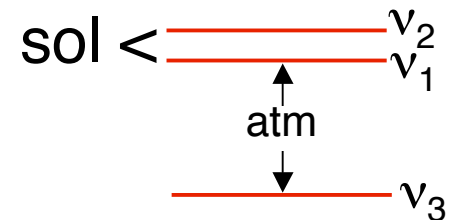
Suppose there are only 3 neutrino mass eigenstates. (More might help.)

Then the spectrum looks like —



Normal hierarchy

or

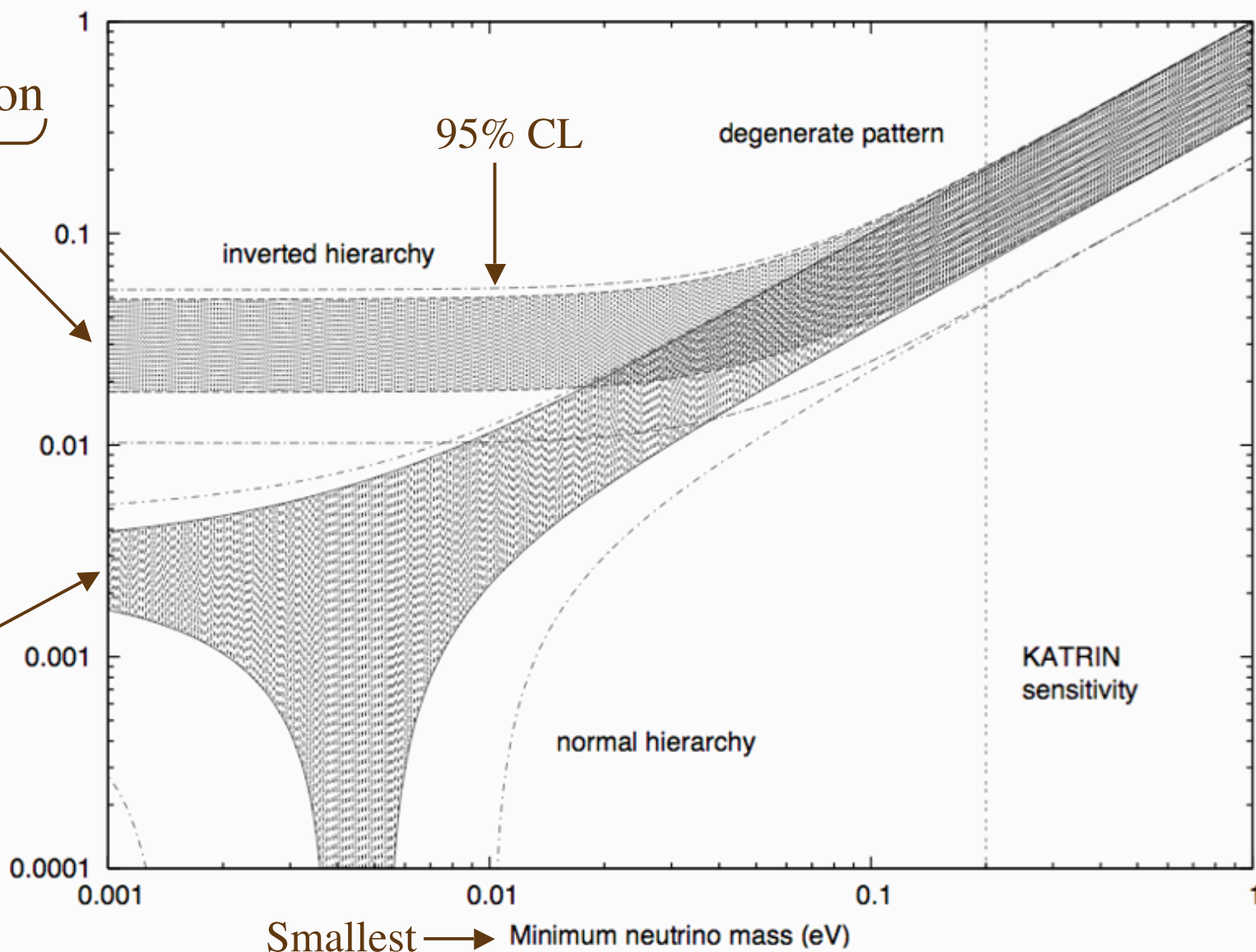


Inverted hierarchy

Takes 1 ton

$m_{\beta\beta}$

Effective Majorana mass (eV)



Takes
100 tons

$m_{\beta\beta}$ For Each Hierarchy

There is no clear theoretical preference
for either hierarchy.

If the hierarchy is **inverted**—
then $0\nu\beta\beta$ searches with sensitivity
to $m_{\beta\beta} = 0.01$ eV have
a very good chance to see a signal.

*Sensitivity in this range is a good target
for the next generation of experiments.*

Determining $m_{\beta\beta}$

The most important goal of $0\nu\beta\beta$ searches
is to observe the process.

Observation at any non-zero level
would establish that —

- Neutrinos have Majorana masses
- Neutrinos are Majorana particles
- Lepton number is not conserved

What We Would Learn From Information On $m_{\beta\beta}$

Suppose accelerator experiments have determined the hierarchy to be **inverted**.

Suppose $0\nu\beta\beta$ searches are negative, but establish convincingly that $m_{\beta\beta} < 0.01$ eV. Then, barring unlikely cancellations from exotic mechanisms, we can say that **neutrinos are Dirac particles**: $\bar{\nu} \neq \nu$.

Suppose accelerator experiments have **not** determined the hierarchy, but $0\nu\beta\beta$ searches have found a convincing signal with $m_{\beta\beta} < 0.01$ eV. Then, barring exotic mechanisms, the hierarchy must be **normal**.

Bahcall, Murayama, Pena-Garay; de Gouvêa, Jenkins

According to the Standard Model, the leptonic mixing matrix U is unitary.

Then, if m_{Heaviest} is the mass of the heaviest neutrino mass eigenstate,

$$m_{\beta\beta} \equiv \left| \sum_i m_i U_{ei}^2 \right| \leq m_{\text{Heaviest}} \sum_i |U_{ei}|^2 = m_{\text{Heaviest}}$$

A measured value of $m_{\beta\beta}$ would be a lower bound on the mass of the heaviest neutrino.

Majorana CP-Violating Phases

Although the Cabibbo-Kobayashi-Maskawa **quark** mixing matrix can have only **one** ~~CP~~ phase, the Pontecorvo-Maki-Nakagawa-Sakata **leptonic** mixing matrix U can have **three**:

$$U = \begin{bmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{bmatrix} \times \begin{bmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{bmatrix} \times \begin{bmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} e^{i\alpha_1/2} & 0 & 0 \\ 0 & e^{i\alpha_2/2} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$c_{ij} \equiv \cos \theta_{ij}$
 $s_{ij} \equiv \sin \theta_{ij}$

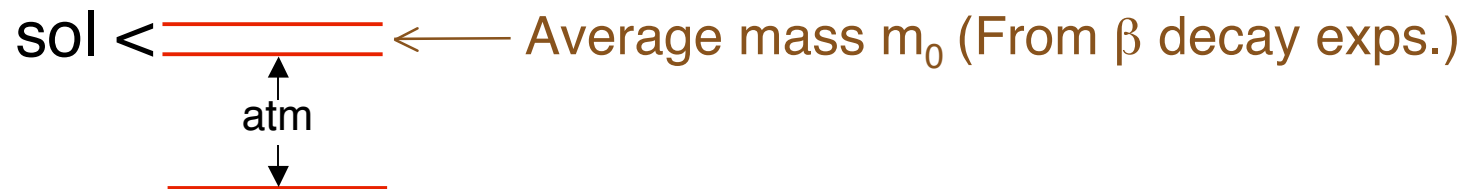
Analogue of the quark ~~CP~~ phase

Majorana ~~CP~~ phases

The **Majorana \mathcal{CP} phases** are physical only if neutrinos are Majorana particles.

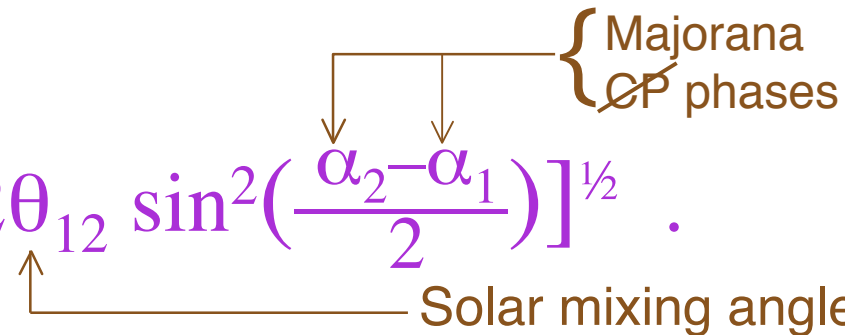
They only affect processes involving violation of lepton number L , such as **$0\nu\beta\beta$** .

Consider **$0\nu\beta\beta$** when the neutrino mass spectrum is **inverted**:




For an inverted spectrum,

$$m_{\beta\beta} \cong m_0 \left[1 - \sin^2 2\theta_{12} \sin^2 \left(\frac{\alpha_2 - \alpha_1}{2} \right) \right]^{1/2} .$$


 Majorana
~~CP~~ phases
 Solar mixing angle

$$m_0 \cos 2\theta_{12} \leq m_{\beta\beta} \leq m_0$$

$$0.4 m_0 \leq m_{\beta\beta} \leq m_0$$

From SNO 

CP is violated if $\alpha_2 - \alpha_1 \neq 0, \pi$.

*To establish CP, we must determine
 $m_{\beta\beta}$ to within a factor of ~ 2 .*

Pascoli, Petcov, Rodejohann; Barger, Glashow, Langacker, Marfatia

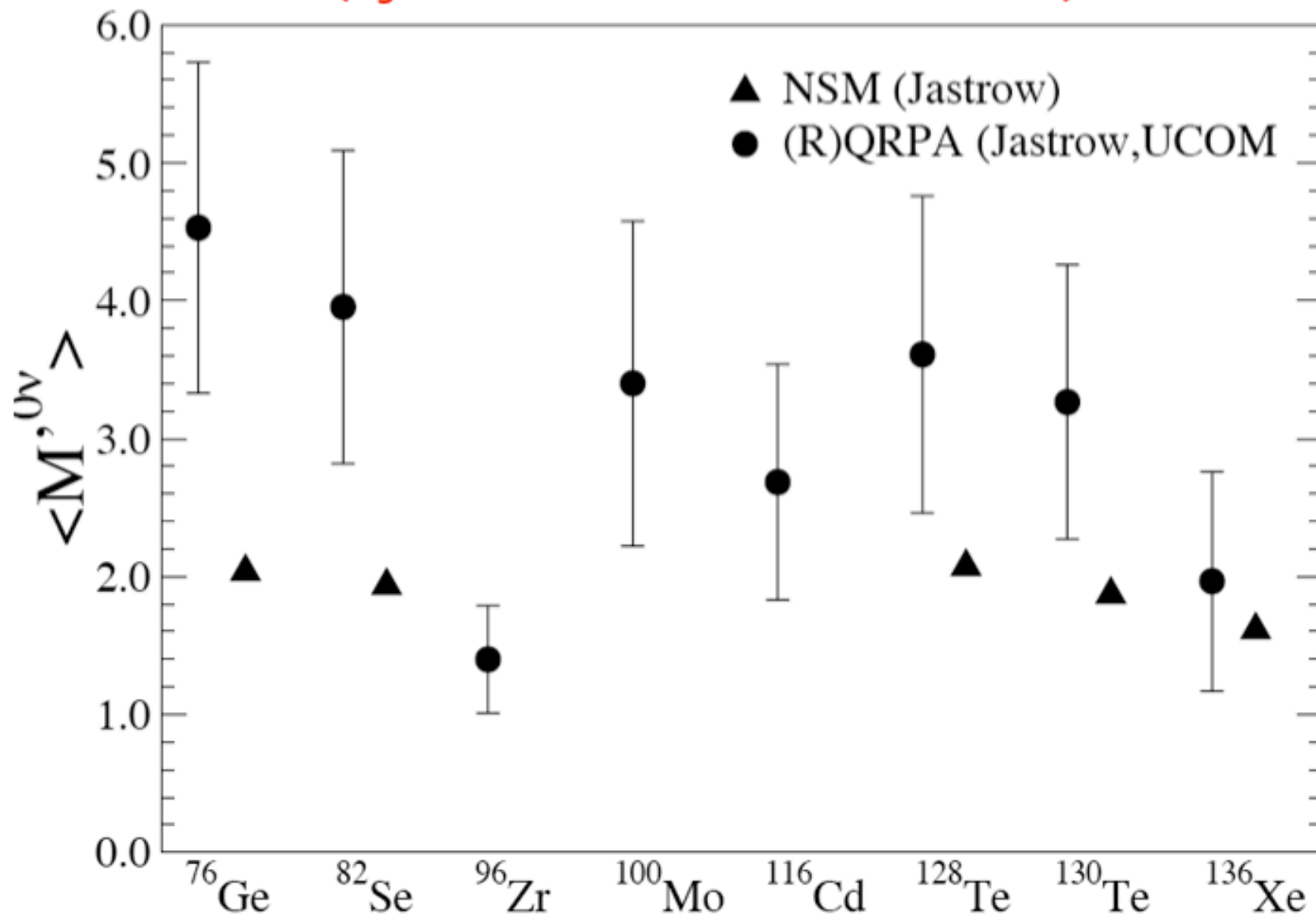
Nuclear Matrix Elements for $0\nu\beta\beta$

If $0\nu\beta\beta$ is dominated by light neutrino exchange, then —

$$\Gamma(0\nu\beta\beta) = (m_{\beta\beta})^2 \times (\text{Nuclear m. e.})^2 \times (\text{Phase space})$$

The **nuclear m. e.** $\mathcal{M}^{0\nu}$ is calculated by the Quasi Particle Random Phase Approximation (QRPA) or the Nuclear Shell Model (NSM).

Full estimated range of $M^{0\nu}$ within QRPA framework and comparison with NSM
(higher order currents now included in NSM)



Vogel

Sources of Uncertainty in the QRPA Calculations

$0\nu\beta\beta$ is $nn \rightarrow pp + ee$. If the two neutrons are separated by $> 2 - 3$ fm, there is *near cancellation* between the $J(nn) = 0$ and the $J(nn) \neq 0$ contributions.

As a result, there is great sensitivity to short-distance features, such as which separation distances dominate, nucleon structure, and short-range repulsion.

There is also sensitivity to the strength g_{pp} of the particle-particle neutron-proton interaction. This parameter is fixed by reference to $2\nu\beta\beta$ decay.

The Bottom Line

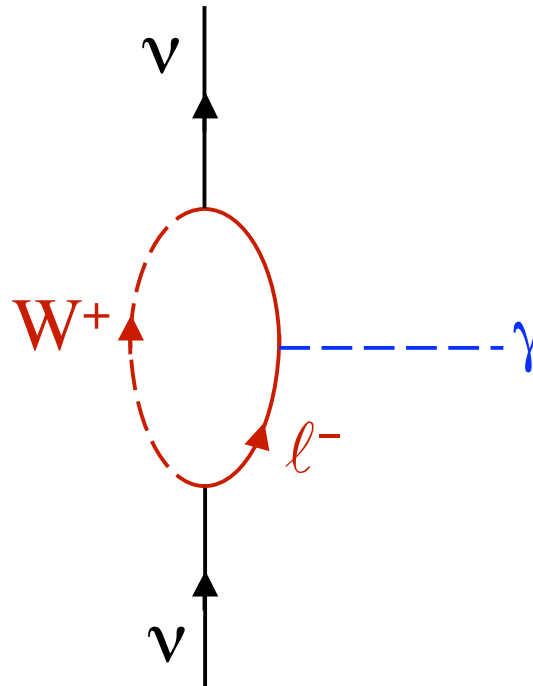
*For the commonly-considered $0\nu\beta\beta$ candidates, such as ^{76}Ge , the nuclear *m. e.* is uncertain by a factor of 2, and perhaps a factor of 3.*

Hopefully, this will improve, to permit cleaner interpretation of $0\nu\beta\beta$ results.

Special thanks to Petr Vogel
for nuclear-physics wisdom.

What Are the Neutrino Dipole Moments?

In the Standard Model, loop diagrams like —



produce, for a *Dirac* neutrino of mass m_ν ,
a magnetic dipole moment —

$$\mu_\nu = 3 \times 10^{-19} (m_\nu/1\text{eV}) \mu_B$$

(Marciano, Sanda; Lee, Shrock; Fujikawa, Shrock)

A *Majorana* neutrino cannot have a magnetic or electric dipole moment:

$$\vec{\mu} \left[\begin{array}{c} \uparrow \\ e^+ \end{array} \right] = - \vec{\mu} \left[\begin{array}{c} \uparrow \\ e^- \end{array} \right]$$

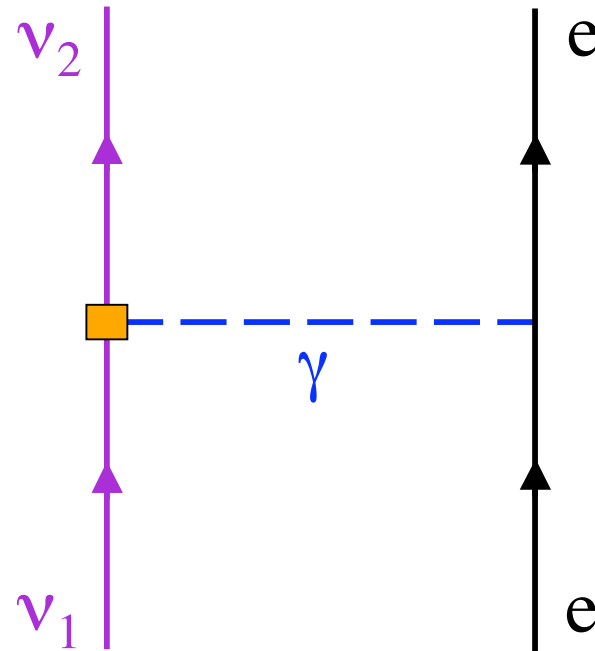
But for a Majorana neutrino,

$$\overline{\nu}_i = \nu_i$$

Therefore,

$$\vec{\mu} [\overline{\nu}_i] = \vec{\mu} [\nu_i] = 0$$

Both *Dirac* and *Majorana* neutrinos can have *transition* dipole moments, leading to —



One can look for the dipole moments this way.

To be visible, they would have to *vastly* exceed
Standard Model predictions.

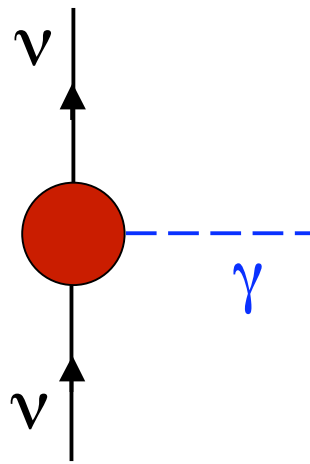
Present Bounds On Dipole Moments

$$\text{Upper bound} = \left\{ \begin{array}{ll} 7 \times 10^{-11} \mu_B & ; \text{Wong et al. (Reactor)} \\ 5.4 \times 10^{-11} \mu_B & ; \text{Borexino (Solar)} \\ 3 \times 10^{-12} \mu_B & ; \text{Raffelt (Stellar E loss)} \end{array} \right.$$

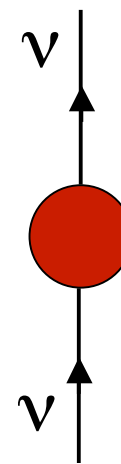
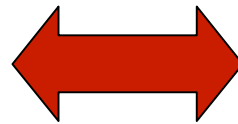
New Physics can produce larger dipole moments than the $\sim 10^{-20} \mu_B$ SM ones.

But the dipole moments cannot be arbitrarily large.

The Dipole Moment – Mass Connection




Dipole Moment



Mass Term

$$\mu_\nu \sim \frac{eX}{\Lambda} \leftarrow \begin{cases} \text{Scale of} \\ \text{New Physics} \end{cases}$$

$$m_\nu \sim X\Lambda$$


$$m_\nu \sim \frac{\Lambda^2}{2m_e} \frac{\mu_\nu}{\mu_B} \sim \left(\frac{\mu_\nu}{10^{-18} \mu_B} \right) \left(\frac{\Lambda}{1 \text{ TeV}} \right)^2 \text{ eV} \quad (\text{Bell } et \text{ al.})$$

Any dipole moment leads to a contribution to the neutrino mass that grows with the scale Λ of the new physics behind the dipole moment.

The dipole moment must not be so large as to lead to a violation of the upper bound on neutrino masses.

The constraint —

$$m_\nu \sim \frac{\Lambda^2}{2m_e} \frac{\mu_\nu}{\mu_B} \sim \left(\frac{\mu_\nu}{10^{-18} \mu_B} \right) \left(\frac{\Lambda}{1 \text{ TeV}} \right)^2 \text{ eV}$$

can be evaded by some new physics.

But the evasion can only go so far.

In the *Majorana* case, a *symmetry* suppresses the contribution of the dipole moment to the neutrino mass. So a bigger dipole moment is permissible. One finds —

For *Dirac* neutrinos, $\mu < 10^{-15} \mu_B$ for $\Lambda > 1$ TeV

For *Majorana* neutrinos, $\mu < \text{Present Bound}$

(Bell, Cirigliano, Davidson, Gorbahn, Gorchtein,
Ramsey-Musolf, Santamaria, Vogel, Wise, Wang)

*An observed μ below the present bound
but well above $10^{-15} \mu_B$ would imply
that neutrinos are *Majorana* particles.*

A dipole moment that large requires
L-violating new physics $\lesssim 1000$ TeV.

Neutrinoless double beta decay at the planned level
of sensitivity only requires this new physics
at $\sim 10^{15}$ GeV, near the Grand Unification scale.

*Searching for $0\nu\beta\beta$ is the more conservative way
to probe whether $\bar{\nu} = \nu$.*

Conclusion

Some very highly motivated experiments lie ahead.

We look forward to the results.