Recoilless Resonant Emission and Detection of Electron Antineutrinos

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Abstract. Recoilless resonant capture of monoenergetic electron antineutrinos (Mössbauer antineutrinos) emitted in bound-state β -decay in the system ³H - ³He is discussed. The recoilfree fraction including a possible phonon excitation due to local lattice expansion and contraction at the time of the nuclear transition, homogeneous and inhomogeneous line broadening, and the relativistic second-order Doppler effect are considered. It is demonstrated that homogeneous line broadening is essential due to stochastic magnetic relaxation processes in a metallic lattice. Inhomogeneous line broadening plays an equally important role. An essential issue which has been overlooked up to now, is an energy shift of the resonance line due to the direct influence of the binding energies of the ³H and ³He atoms in the lattice on the energy of the electron antineutrinos. This energy shift as well as the second-order Doppler shift exhibit variations in a non-perfect (inhomogeneous) lattice and may seriously jeopardize the observation of Mössbauer antineutrinos. If successful in spite of these enormous difficulties, Mössbauer antineutrino experiments could be used to gain new and deep insights into the nature of neutrino oscillations, determine the neutrino mass hierarchy as well as up to now unknown oscillation parameters, search for sterile neutrinos, and measure the gravitational redshift of electron antineutrinos in the field of the Earth.

1. Introduction

After the discovery of the Mössbauer effect with γ -transitions in nuclei [1], the possibility of observing recoilless resonant emission and detection of antineutrinos (Mössbauer antineutrinos) was discussed in several publications [2],[3]. In Ref. [3] an extensive list (including a figure of merit) of possibly suitable nuclear transitions has been provided. More recently, the question concerning Mössbauer neutrinos has been revived for the tritium (³H) - helium (³He) system [4],[5]. The main idea is to use 18.6 keV electron antineutrinos that are emitted without recoil in the bound-state β -decay of ³H to ³He and are resonantly absorbed - again without recoil - in the reverse bound-state process in which ³He is transformed to ³H. Recoilless emission and absorption are intended to be achieved by embedding ³H and ³He into metallic lattices.

In the present paper, we want to discuss the basic conditions which have to be fulfilled to enable the observation of the Mössbauer effect with antineutrinos in the ${}^{3}\text{H} - {}^{3}\text{He}$ system. In particular, we will consider lattice expansion and contraction processes which have been neglected up to now but might considerably reduce the recoilfree fraction. We will critically review magnetic relaxation phenomena in metallic systems and show that the induced homogeneous line broadening, as mentioned earlier [5], can not be avoided, in contradiction to a very optimistic recent suggestion [6]. Concerning inhomogeneous broadening we will describe the direct influence of the binding energies of the ${}^{3}\text{H}$ and ${}^{3}\text{H}$ atoms in the metal matrix on the energy of the antineutrinos - a problem which is discussed here for the first time and which may prevent the observation of Mössbauer antineutrinos. We will describe relativistic effects

and their connection to second-order Doppler shifts, which again can not be discarded since they also give rise to inhomogeneous line broadening. Both homogeneous and inhomogeneous line broadening effects are estimated to be many orders of magnitude larger than the natural width (minimal width) $\Gamma = \hbar/\tau = 1.17 \times 10^{-24}$ eV as calculated on the basis of the lifetime $\tau = 17.81$ y of ³H. The observation of Mössbauer neutrinos will be a very difficult experiment and may turn out to be unsuccessful with the techniques and ideas available at present.

2. Bound-state β -decay and its resonant character

The usual continuum-state β -decay (C β) where a neutron in a nucleus transforms into a proton is a three-body process where the emitted electron (e⁻) and the electron antineutrino (\bar{v}_e) occupy states in the continuum leading to broad energy spectra for the e⁻ as well as for the \bar{v}_e . In the bound-state β -decay (B β), however, the e⁻ is directly emitted into a bound-state atomic orbit [7]. Since this is a two-body process, the emitted \bar{v}_e has a fixed energy $E_{\bar{v}_e} = Q + B_z - E_R$. The \bar{v}_e -energy is determined by the Q value, the binding energy B_z of the atomic orbit the electron is emitted into, and by the recoil energy E_R of the atom formed after the decay. This process occurs, e.g., in the bound-state tritium decay.

The reverse process is also important: a \bar{v}_e and an e⁻ in an atomic orbit are absorbed by the nucleus and a proton is transformed into a neutron. Also this is a two-body process. The required energy of the antineutrino is given by $E'_{\bar{v}_e} = Q + B_z + E'_R$, where E'_R is the recoil energy of the atom after the transformation of a proton into a neutron. This process occurs, e.g., in the bound-state EC-decay of ³He when irradiated by electron antineutrinos.

Since both $E_{\bar{v}_e}$ and $E'_{\bar{v}_e}$ are well defined, B β has a resonant character which, however, is partially destroyed by the recoil occurring after emission and absorption of the \bar{v}_e . The resonance cross section is given by [8] $\sigma = 4.18 \cdot 10^{-41} \cdot g_0^2 \cdot \rho(E_{\bar{v}_e}^{res})/ft_{1/2}$ (in units of cm²) where $g_0 = 4\pi(\hbar/mc)^3|\psi|^2 \approx 4(Z/137)^3$ for low-Z, hydrogen-like wavefunctions ψ ; *m* is the electron mass, and $\rho(E_{\bar{v}_e}^{res})$ is the resonant spectral density, i.e., the number of antineutrinos in an energy interval of 1 MeV around $E_{\bar{v}_e}^{res}$. For a super-allowed transition, $ft_{1/2} \approx 1000$ s. For the ³H - ³He system, the resonance energy is 18.60 keV, $ft_{1/2} = 1000$ s, and $B\beta/C\beta = 6.9 \cdot 10^{-3}$ with 80% and 20% of the B β events proceeding via the atomic ground state and excited atomic states, respectively [7]. If gases of ³H and ³He are used at room temperature the profiles of the emission and absorption probabilities are Doppler broadened and both emission as well as absorption of the electron antineutrinos will occur with recoil. Thus the expected resonance cross-section $\sigma \approx 1 \cdot 10^{-42}$ cm². Clearly, an observation would require very strong sources of ³H and large target (³He) masses [4] and thus make such an experiment virtually impossible. However, making use of the Mössbauer effect of antineutrinos, i.e., using recoilfree resonant antineutrino emission and absorption, would increase the resonance cross-section by many orders of magnitude, typically to $\sigma_R \approx 1 \cdot 10^{-33}$ cm² [4],[5].

3. Mössbauer antineutrinos: Recoilfree resonant antineutrino emission and absorption

3.1. Recoilfree fraction

3.1.1. Lattice excitations due to momentum transfer In analogy to usual Mössbauer spectroscopy with photons [1],[9], recoilfree emission and absorption can be realized by embedding the atoms of the source (in the present example, ³H) and the target (³He) into solid-state lattices, e.g., into metallic matrices. Recoilfree processes require that the lattice excitations (e.g. phonons) will remain unchanged by the emission and the absorption of the antineutrino. Considering the momentum transfer only, the recoilfree fraction is given by $f = exp \left\{ -(\frac{E}{\hbar c})^2 \cdot \langle x^2 \rangle \right\}$, where *E* is the transition energy (18.6 keV for the ³H - ³He system) and $\langle x^2 \rangle$ is the mean-square atomic displacement. The recoilfree fraction is biggest at low temperatures. However, even at very low temperatures, f < 1, because of the zero-point motion, which itself is a consequence of the Heisenberg uncertainty principle. In the Debye approximation and in the limit of very low temperatures T, $f(T \to 0) = exp \left\{ -\frac{E^2}{2Mc^2} \cdot \frac{3}{2k_B\theta} \right\}$, where θ is the effective Debye

temperature, k_B is the Boltzmann constant, and $\frac{E^2}{2Mc^2}$ is the recoil energy which would be transmitted to a free atom of mass M. For ³H and ³He in a metal matrix, e.g. Nb, effective Debye temperatures up to $\theta \approx 800$ K have been estimated [4],[6]. Thus $f(0) \approx 0.27$ and the probability for recoilfree emission and consecutive recoilfree capture of electron antineutrinos is given by $f^2 \approx 0.07$ (for $T \to 0$).

3.1.2. Lattice excitations by lattice expansion and contraction Concerning the recoilfree fraction, the anology with usual (photon) Mössbauer spectroscopy is insufficient: For electron antineutrinos one has to consider an additional process, which is not important for photon Mössbauer spectroscopy with excited nuclear states. In this latter case, a radioactive parent nucleus decays and populates a nuclear level (the Mössbauer state) of the daughter nucleus. Deexcitation from this Mössbauer state to the groundstate can then proceed via the recoilfree emission of a Mössbauer photon. Due to the relatively long lifetime of the Mössbauer state, most rearrangement processes of the electron shell caused by the preceeding nuclear decay and occurring on a timescale of $< 10^{-12}$ s (much shorter than the lifetime of the Mössbauer state) have settled.¹ Thus, the emitted Mössbauer photon from the source is not directly involved in the nuclear decay and, therefore, is likely to exhibit the right energy that is required to excite the same Mössbauer level in the absorber (target). The situation is different for antineutrino emission and capture. These processes occur at the same time when the nuclear transformation to the different element takes place; in fact the antineutrinos take part in the nuclear transformation processes. Considering the ³H - ³He system as the particular example, ³H is more strongly bound in the metallic lattice than ³He, and ³H and ³He use different amounts of space. As a consequence, the lattice-deformation energies for ³H and ³He, e.g. in the Nb lattice, are $E_L^{^{3}H} = 0.099$ eV and $E_L^{^{3}He} = 0.551$ eV, respectively [11]. Assuming again an effective Debye temperature of $\theta \approx 800$ K one can estimate - in analogy to the situation with momentum transfer - that the probability that this lattice deformation will not cause lattice excitations is smaller than $exp\left\{-\frac{E_L^{^{3}He}-E_L^{^{3}H}}{k_B\theta}\right\}\approx 1\cdot 10^{-3}$. This factor appears in the emission as well as in the capture process of the antineutrinos. Thus, in addition to the factor $f^2 \approx 0.07$ (for $T \to 0$), which reflects the momentum transfer in the emission and capture processes of the \bar{v}_e , lattice deformation results in a further reduction factor of at least $1 \cdot 10^{-6}$.

Therefore the total probability for recoilfree emission and consecutive recoilfree capture of \bar{v}_e is smaller than $\approx 7 \cdot 10^{-8}$. This estimate has to be confirmed by more detailed theoretical calculations; however, it emphasizes the importance of a thorough understanding of \bar{v}_e recoilfree emission and capture.

3.2. Linewidth

For the ³H decay with a lifetime $\tau = 17.81$ y, the natural linewidth Γ , i.e., the minimal width, $\Gamma = \hbar/\tau = 1.17 \times 10^{-24}$ eV. In two recent contributions [6] it has been argued that such a narrow line can indeed be achieved experimentally. We strongly disagree with these claims and want to stress that basically two types of line broadening are important [12],[13],[14],[5].

3.2.1. Homogeneous broadening Homogeneous broadening is caused by electromagnetic relaxation. For example, spin-spin interactions between nuclear spins of ³H and ³He and with the spins of the nuclei of the metallic lattice lead to fluctuating magnetic fields. Contrary to the notion in [6], magnetic relaxations are stochastic processes and can not be described by a periodic energy modulation of an excited hyperfine state. The simplest magnetic relaxation model consists of a three-level system: the groundstate and two excited hyperfine-split states (energy separation $\hbar\Omega_0$) between which transitions (so-called relaxation processes) take place with an average frequency Ω . With stochastic processes, three frequency regimes can be distinguished [15]:

 $^{^{1}}$ An exception are so-called after effects in non-metallic lattices where some rearrangement processes in the electron shell involve rather long-lived (several ns) electronic configurations, e.g., different oxydation states, which can be detected in Mössbauer spectroscopy by their different hyperfine interactions [10].

a) $\Omega \ll \Omega_0$. For the simple three-level system, two lines separated by $\hbar\Omega_0$ will be observed. The lines will be broadened to an effective experimental linewidth $\Gamma_{exp} \approx \hbar\Omega$ as suggested by the time-energy uncertainty principle. Only in the limit of very small Ω values, the lines exhibit natural width. With increasing Ω the lines broaden.

b) $\Omega \approx \Omega_0$. The lines are severely broadened. In fact, the intensity is distributed over a broad pattern which extends roughly over a range given by the total hyperfine splitting $\hbar\Omega_0$, as suggested by the time-energy uncertainty principle.

c) $\Omega \gg \Omega_0$. This is the frequency regime of motional narrowing. The system stays only for a short time (typically $1/\Omega$) in one of the levels and then stochastically jumps into the other one. Thus an averaging process over the energies of both levels takes place, resulting in one line at the center of the hyperfine-splitting pattern. In this high-frequency limit the linewidth is practically natural.

For typical hyperfine splittings due to nuclear spin-spin interaction in metallic lattices, $\Omega_0 \approx 10^5 \text{ s}^{-1}$. Typical relaxation times for ³H and ³He in a Pd lattice are $T_2 \approx 2$ ms, and for NbH, $T_2 \approx 79 \ \mu \text{s}$ [16],[4]. The latter gives a linewidth Γ_{exp} due to homogeneous broadening, $\Gamma_{exp} = 9 \times 10^{-12} \text{ eV} \approx 7 \times 10^{12} \Gamma$. Due to stochastic relaxation processes, homogeneous broadening by ≈ 12 orders of magnitude has to be expected in the ³H - ³He system because the stochastic relaxation frequences are far below the motionalnarrowing regime. As a consequence, also the resonance cross-section σ_R will be reduced by ≈ 12 orders of magnitude. To compensate for this effect one would have to increase the number of ³He atoms in the target by the same factor!

3.2.2. Inhomogeneous broadening In imperfect lattices, inhomogeneous broadening is caused by stationary effects, in particular by impurities, lattice defects, variations in the lattice constant, and other effects which destroy the periodicity of the lattice. This is a critical issue also for \bar{v}_e since - as will be described in section 4 - the source contains a large amount of ³H but very little ³He whereas the target contains a lot of ³He but practically no ³H [4],[5]. Clearly, the ³H and ³He distributions on the interstitial sites will be random and will destroy lattice periodicity. An additional process due to variations of the zero-point energy will be discussed in section 3.3. In general, for photon Mössbauer spectroscopy, in the best single crystals, inhomogeneous broadening is of the order of 10^{-13} eV to 10^{-12} eV [13].

A feature which is different between usual Mössbauer spectroscopy with photons and Mössbauer antineutrinos is connected to the variation of the binding energies of ³H and ³He in an inhomogeneous metallic lattice. The binding energies directly affect the energy of the \bar{v}_e : In a perfect lattice, the difference in binding energies in the lattice between ³He and ³H [11], which is given to the \bar{v}_e when ³H decays into ³He, exactly compensates the binding-energy difference needed for the reverse process, when the \bar{v}_e is captured and ³He transforms into ³H. However, in the source and target intended to be used in a real experiment (see section 4) such a compensation even within an experimental linewidth of $\Gamma_{exp} = 9 \times 10^{-12}$ eV will be extremely unlikely considering the fact that the binding energies per atom are in the eV range [11]. Inhomogeneities in real lattices as mentioned above and, in particular, the vastly different amounts of ³H and ³He in the source and target than Γ_{exp} and thus destroy the resonance condition.

In usual Mössbauer spectroscopy with photons, different binding strengths due to inhomogeneities in source and absorber (target) affect the photon energy only via the *change* in the mean-square nuclear charge radius between the groundstate and the excited state of the nucleus. This leads to the *isomer shift*, i.e., a shift of the photon energy in the range typical for *hyperfine interactions* (in the $10^{-7} - 10^{-9}$ eV range) [17]. Thus variations of isomer shifts due to an inhomogeneous lattice lead to a line broadening which is also in the neV range. For \bar{v}_e of the ³H - ³He system, a neV shift would already correspond to $\sim 100\Gamma_{exp} \approx 10^{15}\Gamma$. However, since the \bar{v}_e energy is *directly* affected, one has to expect a variation of the \bar{v}_e energy several orders of magnitude larger than the neV range, i.e., much larger than $10^{15}\Gamma$.

3.3. Relativistic effects

An atom vibrating around its equilibrium position in a lattice does not only exhibit a mean-square displacement $\langle x^2 \rangle$ but also a mean-square velocity $\langle v^2 \rangle$. According to Special Relativity Theory this causes a time-dilatation effect which results in a reduction of frequency (energy): $\Delta \omega = \omega - \omega' = -v^2 \omega/(2c^2)$. Since this reduction is proportional to $(v/c)^2$ it is often called second-order Doppler shift (SOD).

Within the Debye model, the energy shift between source (s) at temperature T_s and target (t) at temperature T_t is given by

$$(\Delta E/E) = \frac{9k_B}{16Mc^2}(\theta_s - \theta_t) + \frac{3k_B}{2Mc^2}[T_s \cdot f(T_s/\theta_s) - T_t \cdot f(T_t/\theta_t)]$$

where $f(T/\theta) = 3(\frac{T}{\theta})^3 \cdot \int_0^{\theta/T} \frac{x^3}{exp(x) - 1} dx.$

At low temperatures, the temperature-dependent term can be neglected if source and target are at about the same temperature (e.g., in a liquid-He bath at 4.2 K) [5]. However, even in the low-temperature limit, the first term which is caused by the zero-point energy can not be neglected. As discussed in detail in [5], it is *not* required that the chemical bonds (i.e. the Debye temperatures) of ³H and ³He have to be the same in the metal matrix. However, the chemical bond for ³H has to be the same in source and target, and the same condition has to be fulfilled for ³He. As a consequence, the surroundings of ³H (and those for ³He) including nearest and higher-order nearest neighbors in source and target should be as similar as possible. This is critical, since, as already mentioned in section 3.2, source and target contain vastly different amounts of ³H and ³He [4],[5].

Another critical issue is a possible variation of the effective Debye temperature due to inhomogeneities within the lattice of the source (or the target) itself. If the effective Debye temperature varies by 1 K, the relative change due to a variation of the zero-point energy would be $(\Delta E/E) \approx 2 \times 10^{-14}$ which corresponds to a lineshift of 3×10^{14} times the natural width Γ . Even after taking homogeneous broadening into account, i.e., considering the above-mentioned linewidth $\Gamma_{exp} = 9 \times 10^{-12}$ eV, the variation of the zero-point energy would still be $\sim 43\Gamma_{exp}$. Thus, also the variation of the zero-point energy within the source and the target will significantly contribute to inhomogeneous broadening.

4. Feasibility of Mössbauer antineutrino experiments

4.1. The ${}^{3}H - {}^{3}He$ system

As discussed in detail in [3],[4],[5], the most promising system for the observation of Mössbauer antineutrinos is ³H as source and ³He as target. The key idea is to use Nb as metal matrix [4]. The source can be produced by chemically loading ³H into metallic Nb, where ³H occupies the tetrahedral interstitial sites. The ³He target can be prepared by using the 'tritium trick': First load ³H into the Nb matrix, wait until enough ³H has decayed into ³He, and then remove all the remaining ³H from the Nb matrix. After this procedure, also the ³He should occupy the tetrahedral interstitial sites.

For a base line of 10 m, typical source strengths of 1 MCi of ³H and absorber masses of \sim 1 g of ³He have been considered resulting in a typical β -activity of \sim 10 counts per day after an activation time of 65 days [4].

4.2. Enormous experimental difficulties

The most difficult experimental problems to observe recoilfree resonant emission and absorption of \bar{v}_e are the following:

(i) *How large is the recoilfree fraction?* The recoilfree fraction due to the momentum transfer of the \bar{v}_e is reasonable: $f^2 \approx 0.07$ (for $T \rightarrow 0$). However, the critical issue is the lattice expansion and contraction of the metallic lattice due to the different elements before and after the decay (see section 3.1.2): An additional reduction factor of at least six orders of magnitude has been estimated. This problem has been overlooked until now, because it does not play a role in the Mössbauer effect with photons.

- (ii) How small an experimental linewidth can be achieved? In contrast to the claims presented in [6], the natural linewidth $\Gamma = 1.17 \times 10^{-24}$ eV will not be observed, mainly because of two reasons: a) Homogeneous line broadening will be caused by stochastic magnetic relaxation. The effect of other processes connected with lattice vibrations are unimportant.² Homogeneous broadening is estimated to cause an experimental linewidth $\Gamma_{exp} = 9 \times 10^{-12}$ eV $\approx 7 \times 10^{12}\Gamma$ [5]. b) Inhomogeneous broadening can not be avoided in such imperfect lattice systems as ³H in Nb and ³He in Nb: The random distributions of ³H and ³He in source and target destroy the lattice periodicity, and different contents of these elements will cause further problems. Thus, in addition to second-order Doppler shifts (see section 3.3) of the resonance lines due to (small) changes in the zero-point energy, much larger shifts are expected because of the variation of binding energies (strengths) of ³H and ³He in the imperfect Nb metal matrix (see section 3.2.2). These different binding energies directly influence the energy of the \bar{v}_e . Also this shift has been overlooked until now, because it is only a tiny (hyperfine interaction) effect leading to the isomer shift in Mössbauer spectroscopy with photons. With Mössbauer antineutrinos, this direct influence on the \bar{v}_e energy will cause a broadening much larger than $10^{15}\Gamma$ (and thus σ_R will be reduced by the same factor, see section 3.2) and can turn out to be the main killer of such an experiment.
- (iii) Can ³H be removed from the Nb metal matrix to low enough concentrations? The 'tritium trick' is a very clever method to make sure that both ³H and ³He occupy the tetrahedral interstitial sites in the Nb metal matrix [4]. However, any ³H remaining in the target will act as unwanted background.
- (iv) *The application of low temperatures (liquid He)* will be necessary to achieve temperature stability and to make sure that source and target are at the same temperature. Otherwise second-order Doppler shifts due to different temperatures will be present. Another requirement is an efficient and homogeneous (across the source matrix) dissipation of the heat generated by non-resonant $C\beta$ decay events in the source.

5. Interesting experiments

If Mössbauer antineutrinos could be observed successfully, several interesting experiments could be performed. Here is a short selection:

- (i) A Mössbauer antineutrino experiment could provide a unique possibility for a better understanding of the true nature of neutrino oscillations [18],[19],[20],[21]. Because of the extremely sharp energy distribution, oscillations of Mössbauer antineutrinos would indicate a stationary phenomenon where the evolution of the neutrino state occurs in space rather than in time.
- (ii) Due to the low \bar{v}_e energy of 18.6 keV, Mössbauer-antineutrino oscillations would allow us to use ultra-short base lines to determine oscillation parameters and the mass hierarchy. For example, for the determination of the mixing angle Θ_{13} , a base line of only ~ 10 m (instead of 1500 m) would be sufficient. In addition, very small uncertainties for Θ_{13} , accurate measurements of Δm_{12}^2 and Δm_{31}^2 [22], and a determination of the neutrino mass hierarchy [23] could be achieved.
- (iii) In a disappearance experiment with 18.6 keV Mössbauer \bar{v}_e a search for the conversion $\bar{v}_e \rightarrow v_{sterile}$ [24] could be performed. If $\Delta m^2 \approx 1$ eV, the oscillation length would only be ~ 5 cm. This would require ultra-short base lines, which would be difficult to realize otherwise.
- (iv) Gravitational redshift \bar{v}_e measurements within a distance of ~ 4 m in the gravitational field of the Earth could be carried out. In contrast to photons, \bar{v}_e are particles with a (small) rest mass and, in principle, could behave differently from photons in a gravitational field. For the determination of the redshift an accuracy of ~ $0.01 \times \Gamma_{exp}$ could be reached.

 $^{^2}$ In the frequency modulation picture, lattice vibrations cause sidebands, the amplitudes of which are tiny, because the modulation index is small due to the high frequencies of the lattice vibrations. Thus, essentially only the carrier frequency remains. In cases where the modulation index is big and sidebands with appreciable amplitudes are expected, the recoilfree fraction vanishes, since the mean-square atomic displacement is large, i.e., there is no Mössbauer effect [9].

6. Conclusions

The system ³H (source) and ³He (target) has been considered for a possible observation of recoilfree resonant (Mössbauer) emission and absorption of electron antineutrinos. Mössbauer antineutrinos would allow us to perfom interesting new measurements. However, the experiment is very challenging as emphasized in sections 3 and 4. In particular, we have argued that - contrary to the claims of Ref. [6] - the natural linewidth ($\Gamma = 1.17 \times 10^{-24} \text{ eV}$) will not be observed because homogeneous broadening alone would result in an experimental linewidth of $\Gamma_{exp} = 9 \times 10^{-12} \text{ eV} \approx 7 \times 10^{12}\Gamma$. Even if an experimental linewidth of $\Gamma_{exp} = 9 \times 10^{-12} \text{ eV} \approx 7 \times 10^{12}\Gamma$. Even if an experimental linewidth of $\Gamma_{exp} = 9 \times 10^{-12} \text{ eV} \approx 7 \times 10^{12}\Gamma$. Even if an experimental linewidth of $\Gamma_{exp} = 9 \times 10^{-12} \text{ eV} \approx 7 \times 10^{12}\Gamma$. Even if an experimental linewidth of $\Gamma_{exp} = 9 \times 10^{-12} \text{ eV} \approx 7 \times 10^{12}\Gamma$. Even if an experimental linewidth of $\Gamma_{exp} = 9 \times 10^{-12} \text{ eV} \approx 7 \times 10^{12}\Gamma$. Even if an experimental linewidth of $\Gamma_{exp} = 9 \times 10^{-12} \text{ eV} \approx 7 \times 10^{12}\Gamma$. Even if an experimental linewidth of $\Gamma_{exp} = 9 \times 10^{-12} \text{ eV} \approx 7 \times 10^{12}\Gamma$. Even if an experimental linewidth of $\Gamma_{exp} = 9 \times 10^{-12} \text{ eV} \approx 7 \times 10^{12}\Gamma$. Even if an experimental linewidth of $\Gamma_{exp} = 9 \times 10^{-12} \text{ eV} \approx 7 \times 10^{12}\Gamma$. Even if an experimental linewidth of $\Gamma_{exp} = 9 \times 10^{-12} \text{ eV}$ could be reached (which would still be highly fascinating for many \bar{v}_e experiments), the chances for the observation of Mössbauer antineutrinos are drastically reduced because of two newly discussed effects. They have been overlooked up to now because they play no significant role with photon Mössbauer spectroscopy: a) an additional suppression of the recoilfree fraction because of *lattice expansion and contraction at the time of the nuclear transition*, and b) the *direct influence of the binding energies* of ³H and ³He atoms in the metal matrix on the energy of the electron antin

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