



Optimizing the Greenfield Beta-Beam

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The Unanswered Questions

- What is the magnitude of θ_{13} ?
 - Main channels to determine θ_{13}
 - $\nu_e \rightarrow \nu_e$ or $\bar{\nu}_e \rightarrow \bar{\nu}_e$: P_{ee} or $P_{\bar{e}\bar{e}}$; Disappearance Expts
 - $\nu_\mu \rightarrow \nu_e$ or $\nu_e \rightarrow \nu_\mu$: $P_{\mu e}$ or $P_{e\mu}$; Appearance Expts
- What is the sign of Δm_{31}^2 ?
 - Main channels to determine $sign(\Delta m_{31}^2)$
 - $\nu_\mu \rightarrow \nu_e$ or $\nu_e \rightarrow \nu_\mu$: $P_{\mu e}$ or $P_{e\mu}$; Appearance Expts
 - “binned” $\nu_\mu \rightarrow \nu_\mu$ $P_{\mu\mu}$; Disappearance Expts
 - $\nu_e \rightarrow \nu_e$ P_{ee} ; Disappearance Expts
- Is there CP violation in the lepton sector?
 - Main channel to see δ_{CP}
 - $\nu_\mu \rightarrow \nu_e$ or $\nu_e \rightarrow \nu_\mu$: $P_{\mu e}$ or $P_{e\mu}$; Appearance Expts
 - Also in principle possible using $\nu_\mu \rightarrow \nu_\mu$

Plausible Strategy to Answer the Questions

• THE WISHLIST

- Measurement of θ_{13}
- Measurement of $\text{sgn}(\Delta m_{31}^2)$
- Measurement of δ_{CP}

• THE TOOLS

- The Oscillation Channel: $P_{e\mu}$
- The Beam: Beta-Beam
- The Detector: 50 kton iron

• THE OPTIMIZATION

- Baseline: L
- Lorentz Boost: γ
- Luminosity: N_β
- Source Ions: ${}^8\text{B}$ and ${}^8\text{Li}$ OR ${}^{18}\text{Ne}$ and ${}^6\text{He}$

Optimizing the Source Ions

For a given source ion:

- Flux in forward direction increases as γ^2
- Peak energy of the beam is roughly $\gamma(E_0 - m_e) \approx \gamma E_0$
- Cross-section increases as $E \propto \gamma$
- Probability roughly goes as $1/E^2 \propto 1/\gamma^2$

• Events (N_μ) \propto flux * cross-section * probability

- Sensitivity $\propto N_\mu \propto \gamma$
- Until the flux at the “most interesting” energy saturates

• Sensitivity $\propto N_\mu \propto N_\beta$
($N_\beta \equiv$ Luminosity)

Optimizing the Source Ions

● Demand that shape of the event spectrum at a given L is same for both ${}^8\text{B}$ and ${}^8\text{Li}$ and ${}^{18}\text{Ne}$ and ${}^6\text{He}$

● Peak energy of the beam is roughly γE_0

● Total flux is proportional to $N_\beta \gamma^2$

● Spectrum with same peak energy and same total flux:

$$\frac{N_\beta^{(1)}}{N_\beta^{(2)}} = \left(\frac{E_0^{(1)}}{E_0^{(2)}} \right)^2, \quad \frac{\gamma^{(1)}}{\gamma^{(2)}} = \frac{E_0^{(2)}}{E_0^{(1)}}$$

● $E_0^{(\text{B})}/E_0^{(\text{Ne})} \simeq 3.5 \Rightarrow \gamma^{(\text{Ne})}/\gamma^{(\text{B})} \simeq 3.5$ [Accelerator]

● $E_0^{(\text{B})}/E_0^{(\text{Ne})} \simeq 3.5 \Rightarrow N_\beta^{(\text{B})}/N_\beta^{(\text{Ne})} \simeq (3.5)^2 \simeq 12$ [Source]

Conclusions

● Beta-beams offer a pure, intense and well known neutrino flux with very low systematic uncertainties and very low backgrounds – ideal for precision experiments

● L , γ , N_β and ion sources have to be chosen optimally

● $\sin^2 2\theta_{13}$ discovery: Either ${}^{18}\text{Ne}$ and ${}^6\text{He}$ at $\sim 700 - 900$ km or ${}^8\text{B}$ and ${}^8\text{Li}$ at the magic baseline are optimal

● Mass Hierarchy: Take ${}^8\text{B}$ and ${}^8\text{Li}$ at the magic baseline

● CP Violation: Use ${}^{18}\text{Ne}$ and ${}^6\text{He}$ at the short baseline

● Optimally use ${}^8\text{B}$ and ${}^8\text{Li}$ at the magic baseline + ${}^{18}\text{Ne}$ and ${}^6\text{He}$ at ~ 750 km two-baseline set-up for all three