

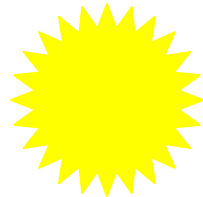
# Large Scale Structure (Galaxy Correlations)

*Bob Nichol (ICG, Portsmouth)*

QuickTime™ and a  
TIFF (Uncompressed) decompressor  
are needed to see this picture.

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# Overview



- **Redshift Surveys**
- **Theoretical expectations**
- **Statistical measurements of LSS**
- **Observations of galaxy clustering**
- **Baryon Acoustic Oscillations (BAO)**
- **ISW effect**

I will borrow heavily from two recent reviews:

1. [Percival et al. 2006, astro-ph/0601538](#)
2. [Nichol et al. 2007 \(see my webpage\)](#)

# Redshift Surveys

*Rich history from Hubble, through CfA, to SDSS*



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Random galaxy

**Z=0.182**

$$z = \frac{\lambda_{obs}}{\lambda_{emitted}} - 1$$

$$cz \approx H_0 d$$

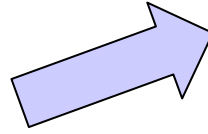
(locally)

# Redshift Surveys II

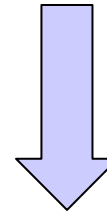
*Now on an industrial scale*



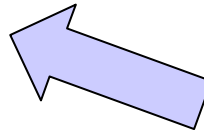
**SDSS (DR6 ~800k galaxies)**



QuickTime™ and a  
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are needed to see this picture.



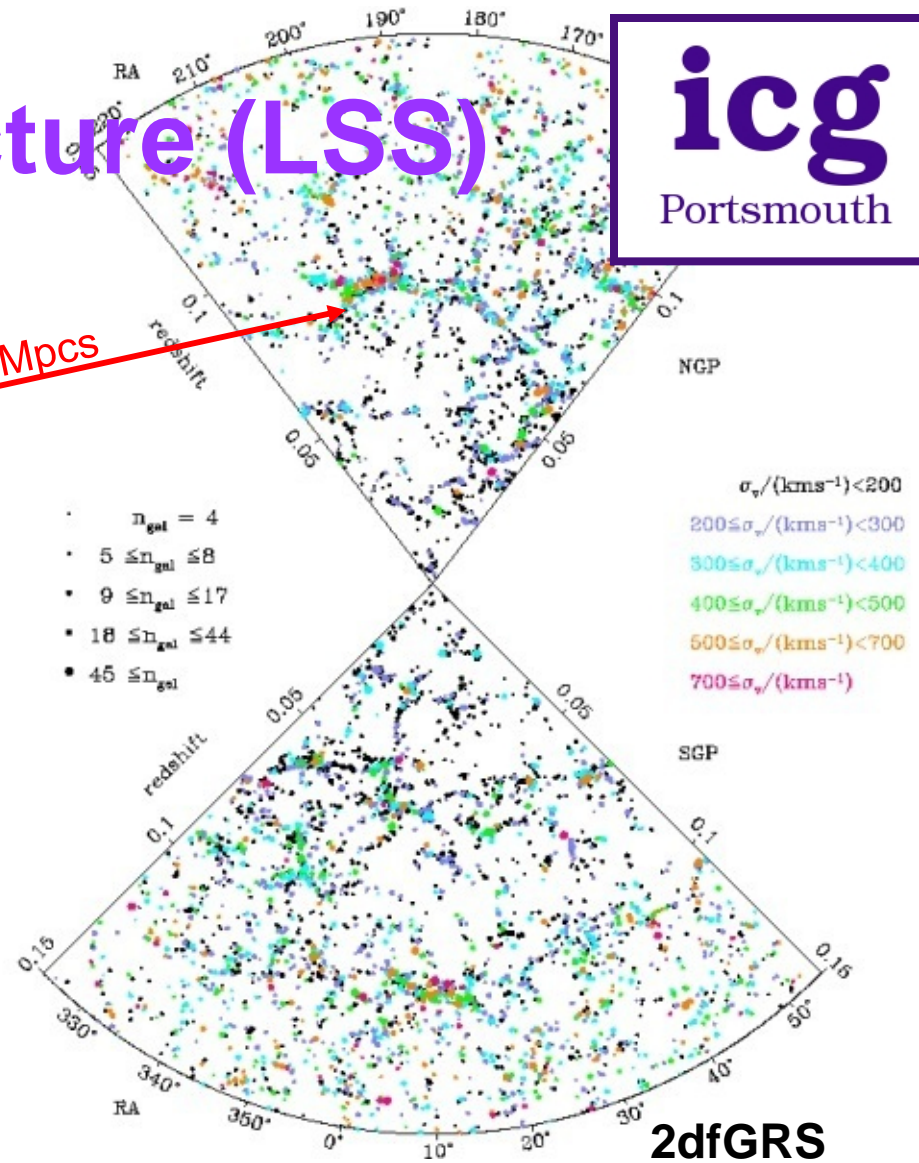
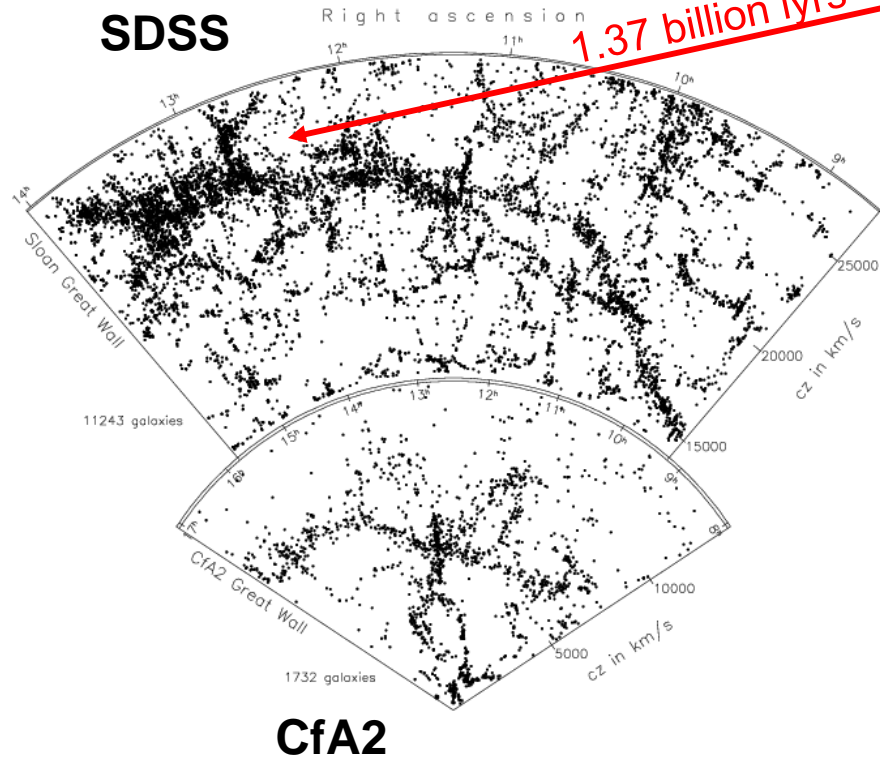
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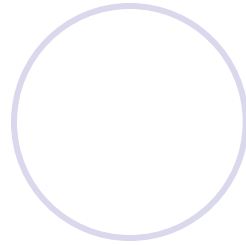
# Large Scale Structure (LSS)

*Observational Definition*

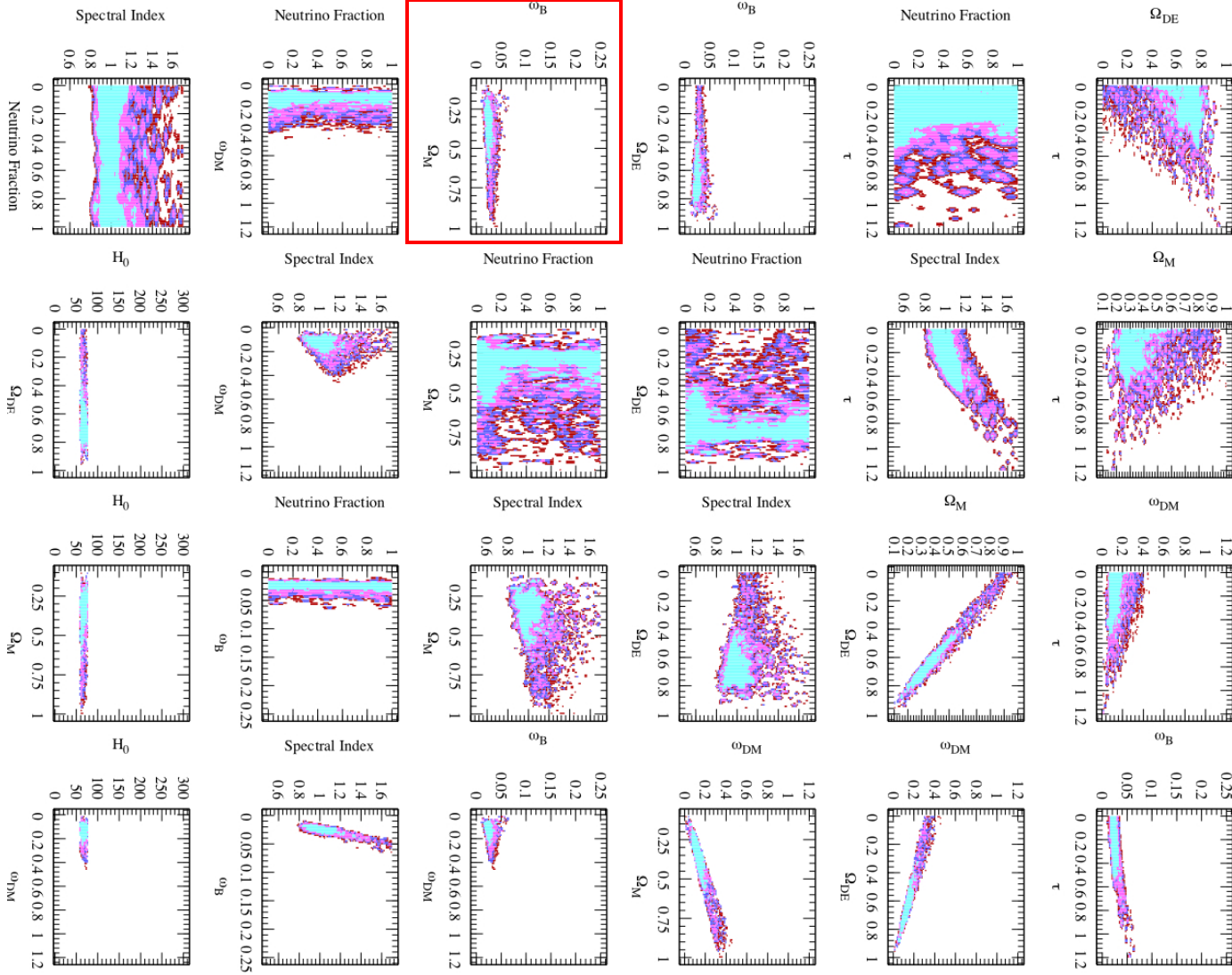


Structures larger than clusters, typically  $> 10Mpc$   
 (larger than a galaxy could have moved in a Hubble time)

# CMB



Only gain insight from the combination of LSS & CMB



0.6 < h < 0.8

# Definitions

We define a dimensionless overdensity as

$$\delta(x) = \frac{\rho(x) - \bar{\rho}}{\bar{\rho}}$$

where  $\delta \ll 1$  on large scales. Then, the autocorrelation function is

$$\xi(x_1, x_2) = \langle \delta(x_1) \delta(x_2) \rangle$$

where  $\langle \rangle$  denote the average over an ensemble of points or densities. Assuming homogeneity and isotropy, then

$$\xi(x_1, x_2) = \xi(|x_1 - x_2|) = \xi(r)$$

In practical terms, the correlation function is given by

$$P_{12} = n^2 (1 + \xi(r)) dV^2$$

# Definitions II

The equivalent in Fourier space is the **power spectrum**

$$P(k) = \frac{1}{(2\pi)^3} \langle \delta(k_1) \delta(k_2) \rangle = \delta_{dirac}(k_1 - k_2) P(k)$$

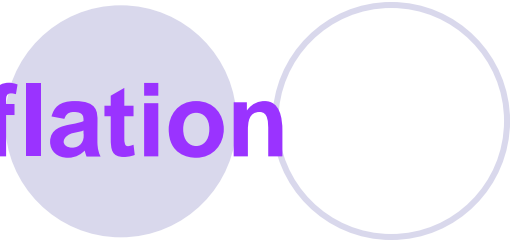
we have suppressed the volume term on the  $P(k)$  and therefore it has **units of  $\text{Mpc}^3$**

The correlation function and power spectrum are related

$$P(k) = \int \xi(r) e^{ik \cdot r} d^3 r$$



# Inflation



We do not consider inflation here. We just assume an **adiabatic scale-invariant power spectrum** of fluctuation created by **quantum processes** deep in the Inflationary era,

$$P(k) = k^n \quad (n \approx 1)$$

# Jeans Length

After inflation, the evolution of density fluctuations in the matter depend on scale and the composition of that matter (CDM, baryons, neutrinos, etc.)

An important scale is the **Jeans Length** which is the scale of fluctuation where pressure support equals gravitational collapse,

$$\lambda_J = \frac{c_s}{\sqrt{G\rho}}$$

where  $c_s$  is the sound speed of the matter, and  $\rho$  is the density of matter.

# Transfer Function

The ratio of the time-integrated growth on a particular scale compared to scales much larger than the Jeans Length is known as the **Transfer Function**:

$$T(k) \equiv \frac{\delta(k, z = 0)}{\delta(k, z = \infty)} \frac{\delta(0, z = \infty)}{\delta(0, z = 0)}, \quad (1)$$

where  $\delta(k, z)$  are density perturbations at  $k$  and  $z$ . By definition,  **$T(k)$  goes to 1** on large scales. Therefore,

$$P(k) \approx \left\langle \left| \delta(k) \right|^2 \right\rangle \approx T(k)^2$$

*Eisenstein & Hu, 1998, 496, 605*

*Eisenstein & Hu, 1999, 511, 5*

# Matter-radiation equality

For  $\lambda > \lambda_J$ , the *fluctuations grow at the same rate independent of scale* and therefore, the primordial power spectrum is maintained

For  $\lambda < \lambda_J$ , the *fluctuations can not grow in the radiation era* because of pressure support (or velocities for collisionless particles). In *matter dominated era*, *pressure disappears* and thus all scales can grow.

**Therefore, in a Universe with CDM and radiation the Jeans length of the system grows to the particle horizon at matter-radiation equality and then falls to zero. Critical scale of  $\lambda_{eq}$  or  $k_{eq}$**

# Matter-radiation equality II



The **redshift of equality** is

$$z_{eq} \approx 25000\Omega_m h$$

The **particle horizon** therefore is

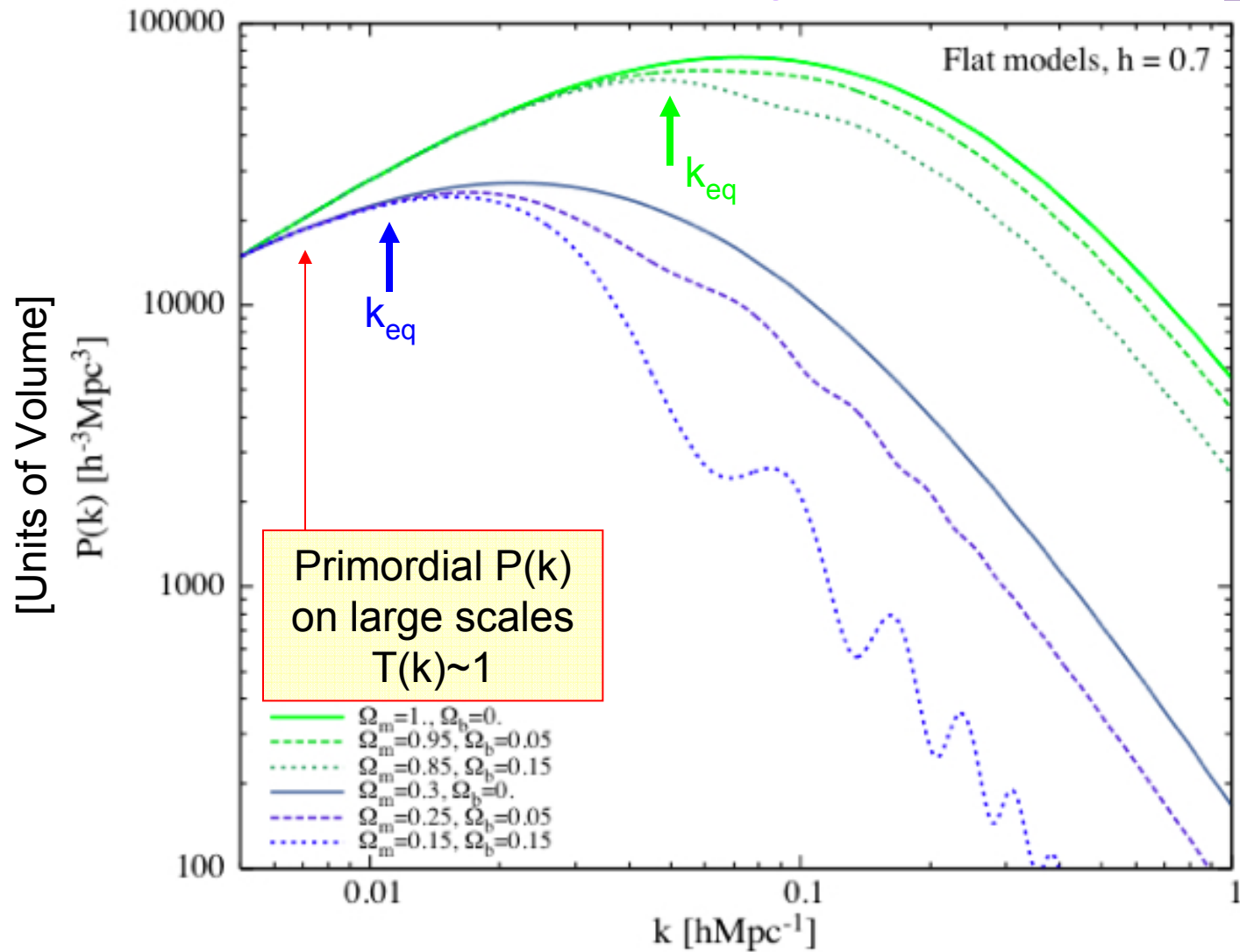
$$k_{eq} \approx 0.075\Omega_m h^2$$

which is imprinted on the power spectrum as fluctuations **smaller than this scale are suppressed** in the radiation era compared to scales on larger scales

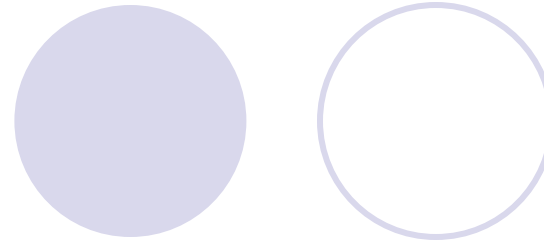
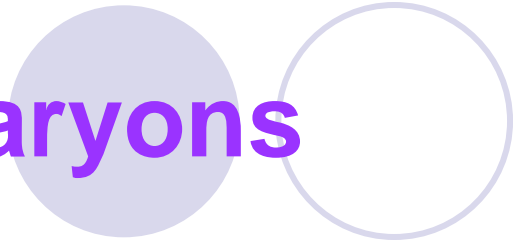
The existence of dark energy and curvature today is insignificant.  $\Omega_m$  is the **density of CDM and baryons**

# P(k) models

Full boltzmann codes now exist or fitting formulae



# Baryons



Although they make-up a small fraction of the density (which is dominated by CDM), they dominate the pressure term. Baryons have two effects on the  $T(k)$ :

1. **Suppression of the growth rates** on scales smaller than the Jeans length
2. **Baryon Acoustic Oscillations (BAO)**, which are sound waves in the primordial plasma

# Baryon Acoustic Oscillations



baryons

photons

QuickTime™ and a  
TIFF (Uncompressed) decompressor  
are needed to see this picture.

Initial fluctuation in DM. Sound wave driven out  
by intense pressure at  $0.57c$ .

**Courtesy of Martin White**



# Baryon Acoustic Oscillations



baryons

photons

QuickTime™ and a  
TIFF (Uncompressed) decompressor  
are needed to see this picture.

After  $10^5$  years, we reach recombination and  
photons stream away leaving the baryons behind

# Baryon Acoustic Oscillations



baryons

photons

QuickTime™ and a  
TIFF (Uncompressed) decompressor  
are needed to see this picture.

Photons free stream, while baryons remain still as  
pressure is gone

**Courtesy of Martin White**

# Baryon Acoustic Oscillations



baryons

photons

QuickTime™ and a  
TIFF (Uncompressed) decompressor  
are needed to see this picture.

Photons almost fully uniform, baryons are attracted  
back by the central DM fluctuation

**Courtesy of Martin White**

# Baryon Acoustic Oscillations



baryons

photons

*Fourier transform  
gives sinusoidal  
function*

QuickTime™ and a  
TIFF (Uncompressed) decompressor  
are needed to see this picture.

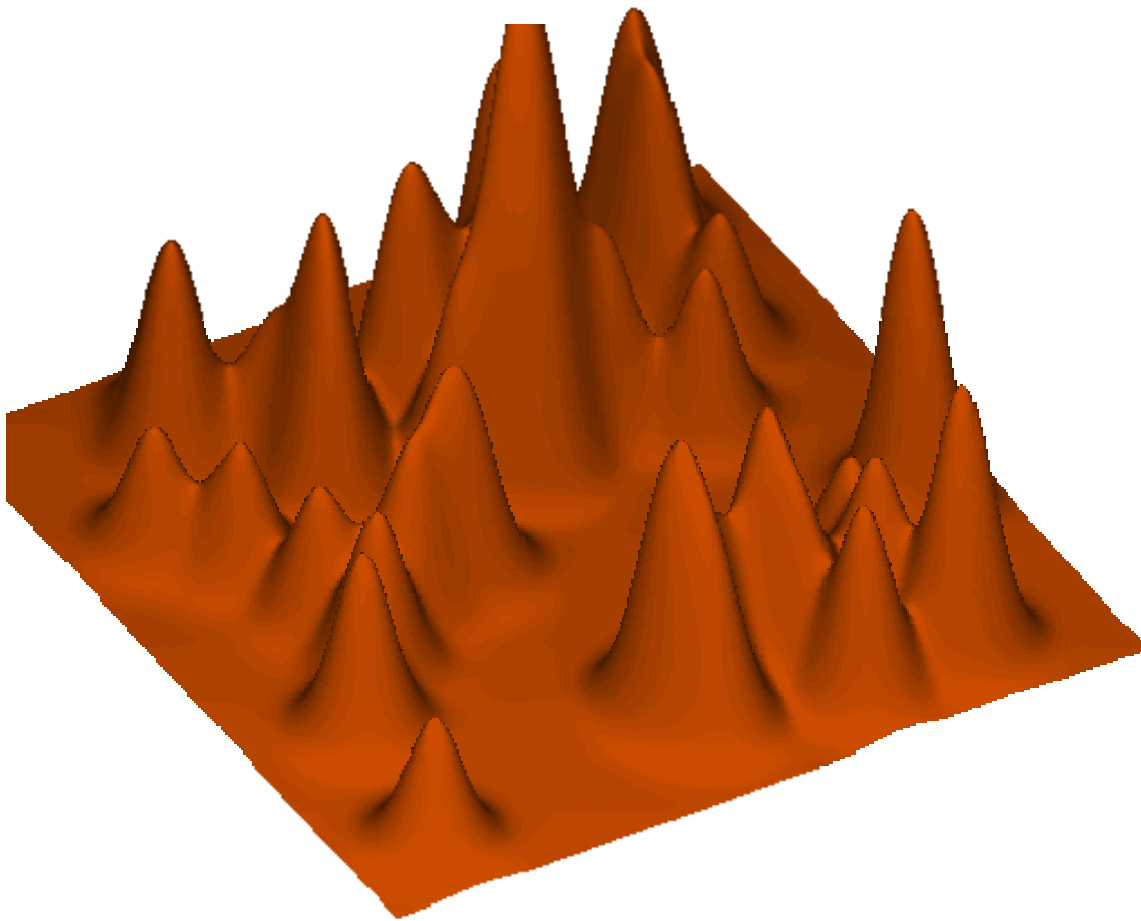
Today. Baryons and DM in equilibrium. The final configuration is the original peak at the center and an echo (the sound horizon) ~150Mpc in radius

**Courtesy of Martin White**

# Baryon Acoustic Oscillations

*Many superimposed waves. See them statistically*

**icg**  
Portsmouth

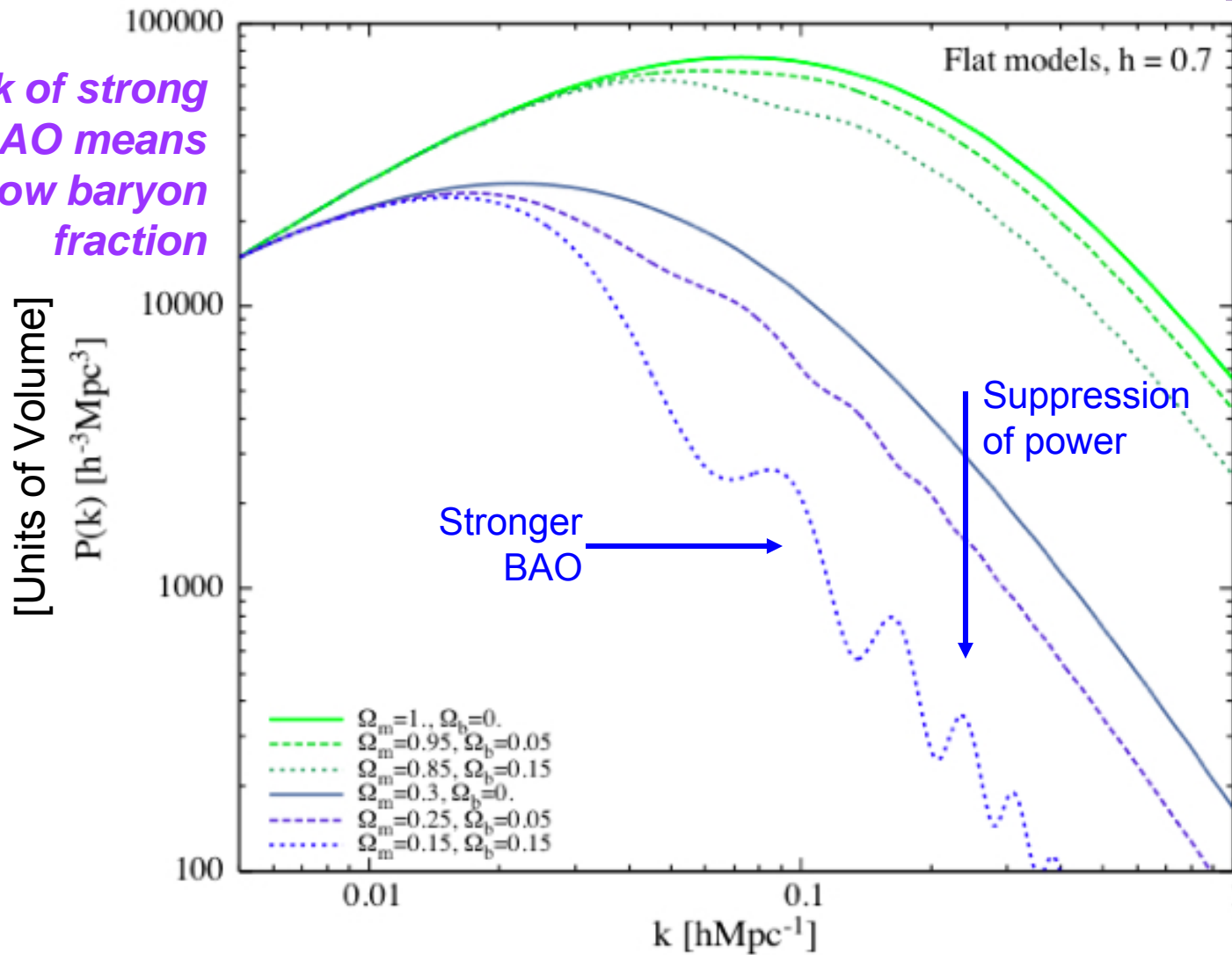


Sound horizon can be predicted once (physical) matter and baryon density known

$$\approx \Omega_m h^2$$

# P(k) models II

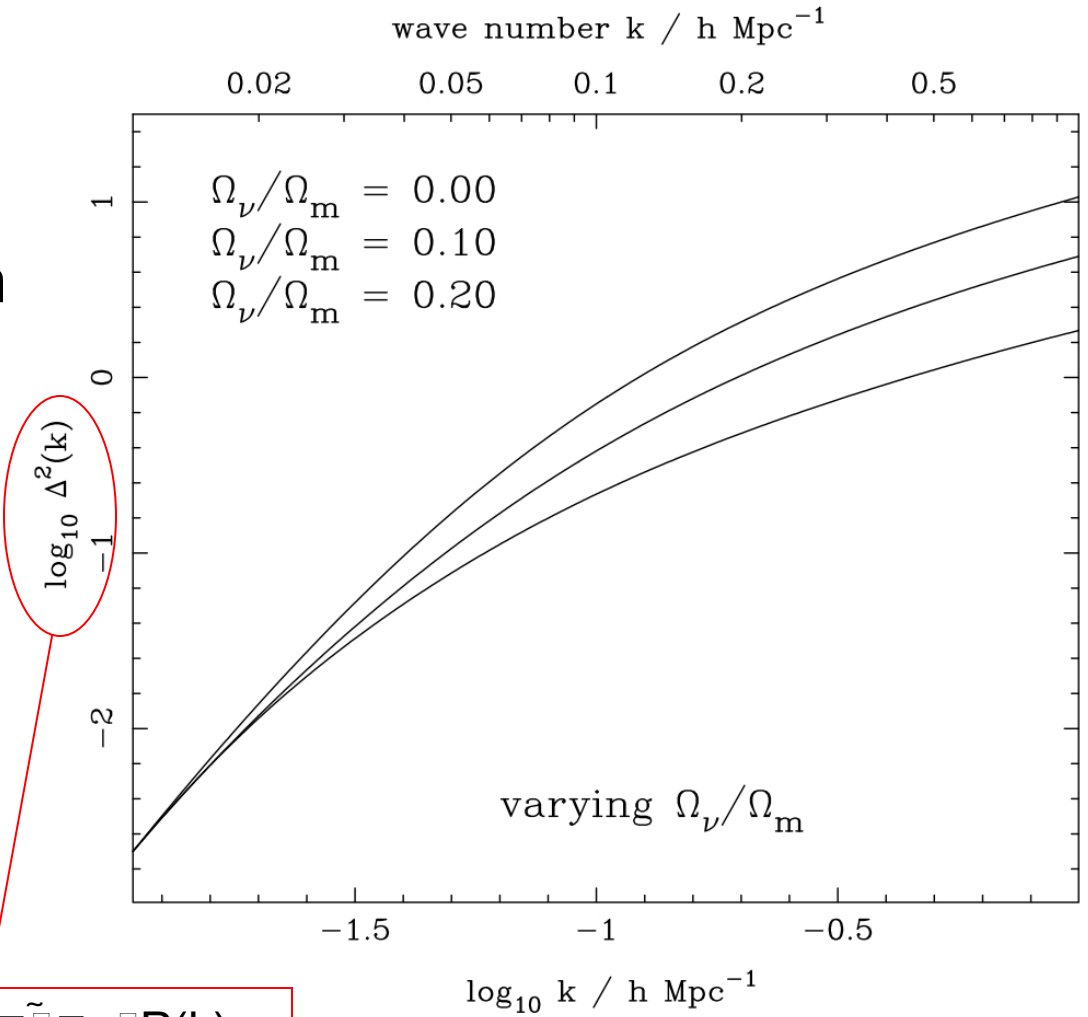
*Lack of strong  
BAO means  
low baryon  
fraction*



# Neutrinos



The existence of massive neutrinos can also introduce a suppression of  $T(k)$  on small scales relative to their Jeans length. Degenerate with the suppression caused by baryons



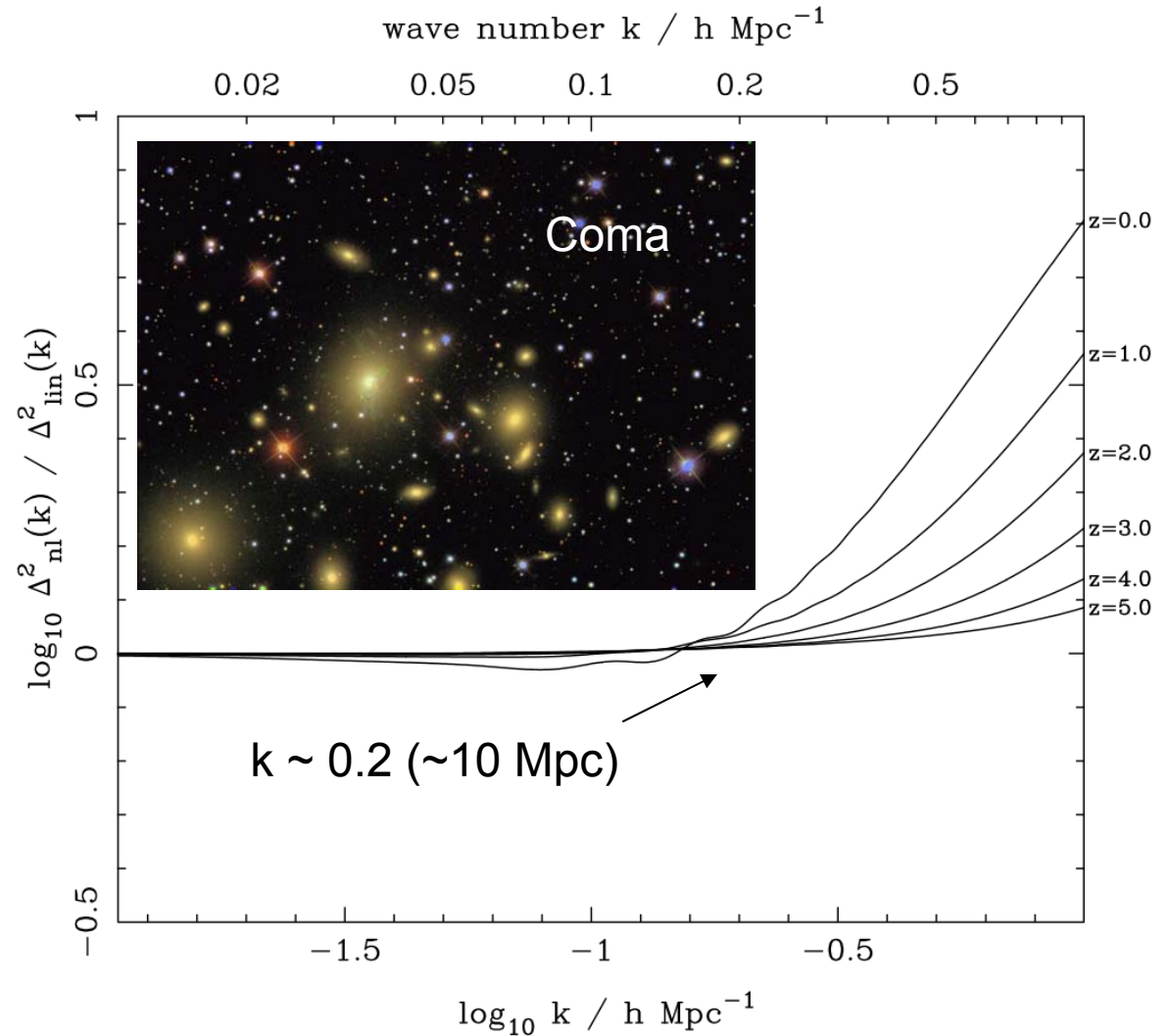
$$\Delta^2(k) \approx \frac{2\pi^2}{k^3} P(k)$$

# Non-linear scales



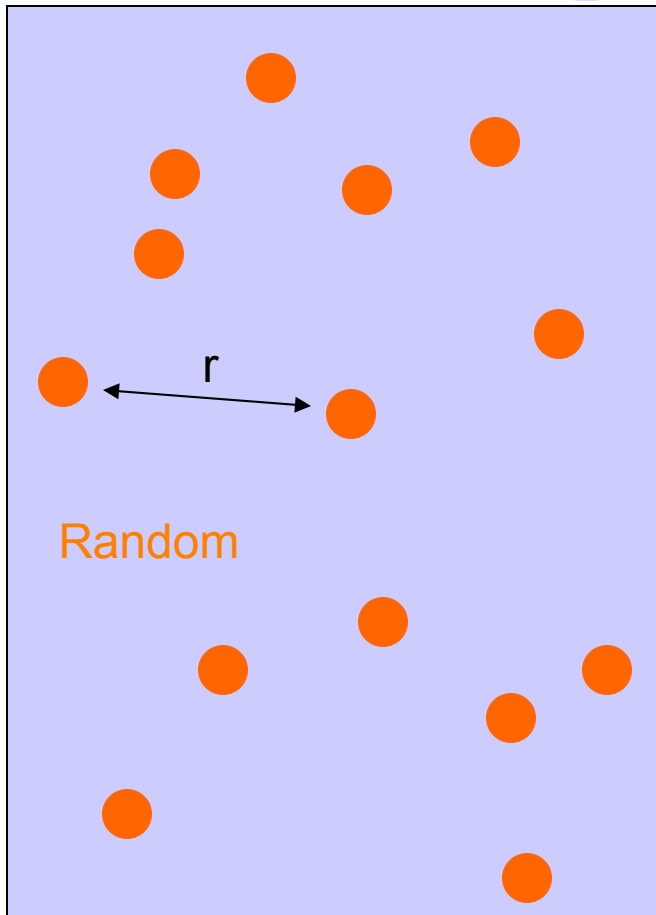
We have discussed linear perturbations but on small scales we must consider **non-linear effects**.

These can be modeled or numerically solved using **N-body simulations** etc.





# Measuring $\xi(r)$ or $P(k)$

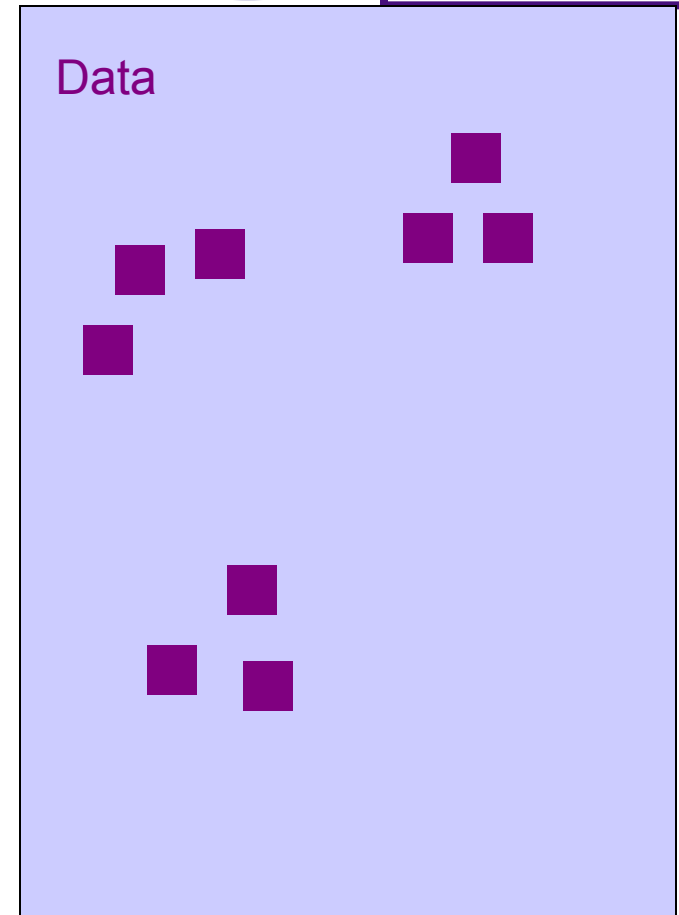


Simple estimator:  
 $\xi(r) = DD(r)/RR(r) - 1$

Advanced estimator:  
 $\xi(r) = (DD-RR)^2/RR-1$

*The latter does a better job with edge effects, which cause a bias to the mean density of points*

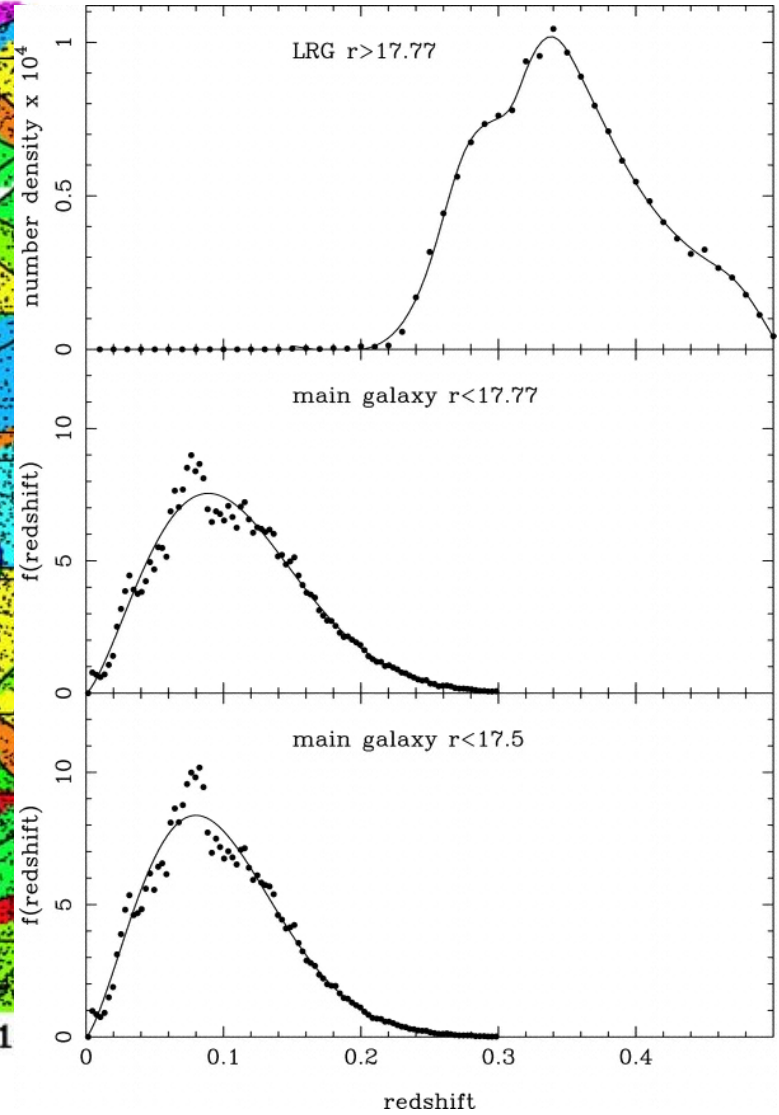
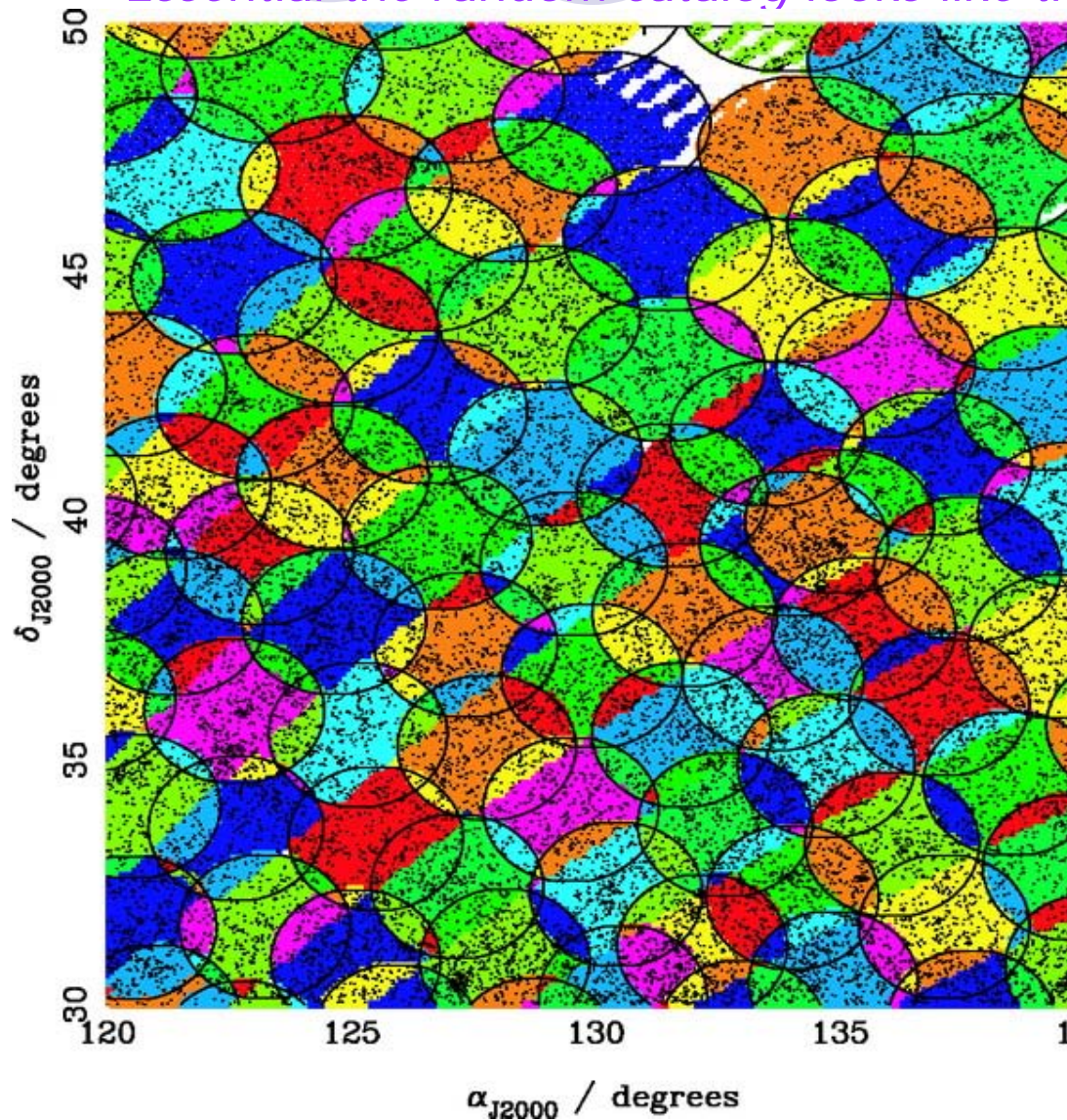
*Usually 10x as many random points over SAME area / volume*



Same techniques for  $P(k)$  - take Fourier transform of density field relative to a random catalog over same volume. Several techniques for this - see Tegmark et al. and Pope et al. Also “weighted” and mark correlations

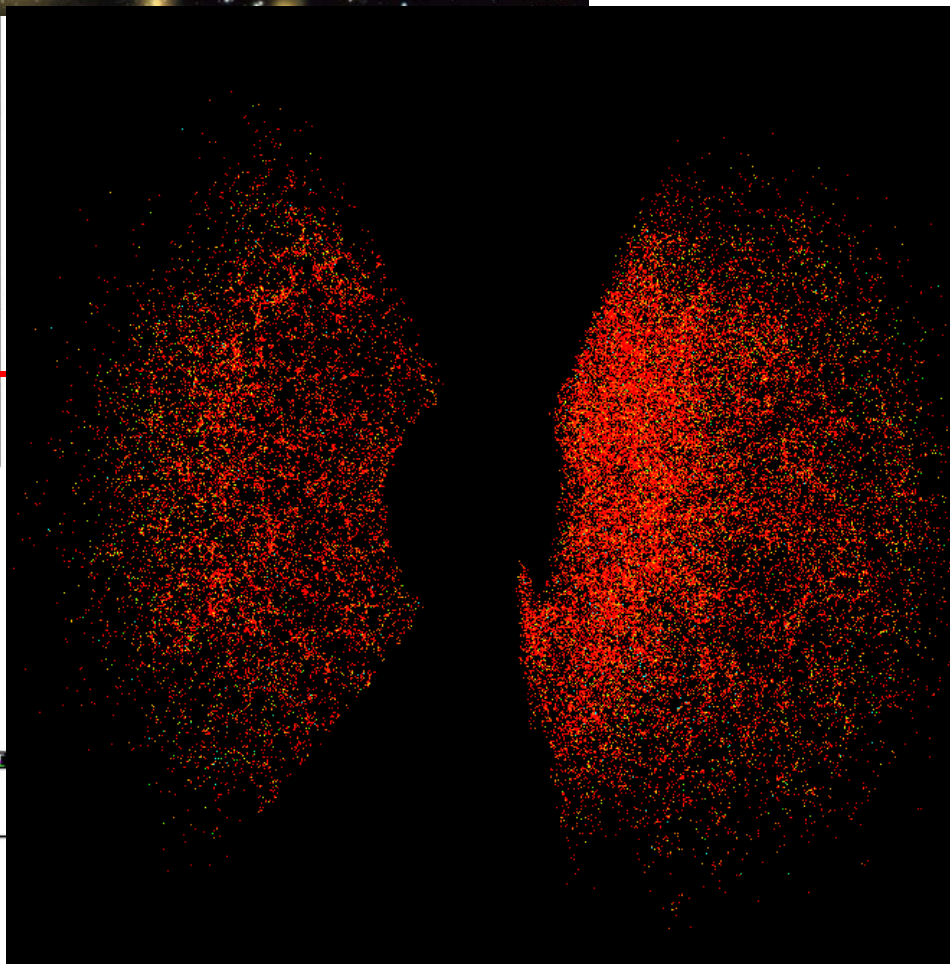
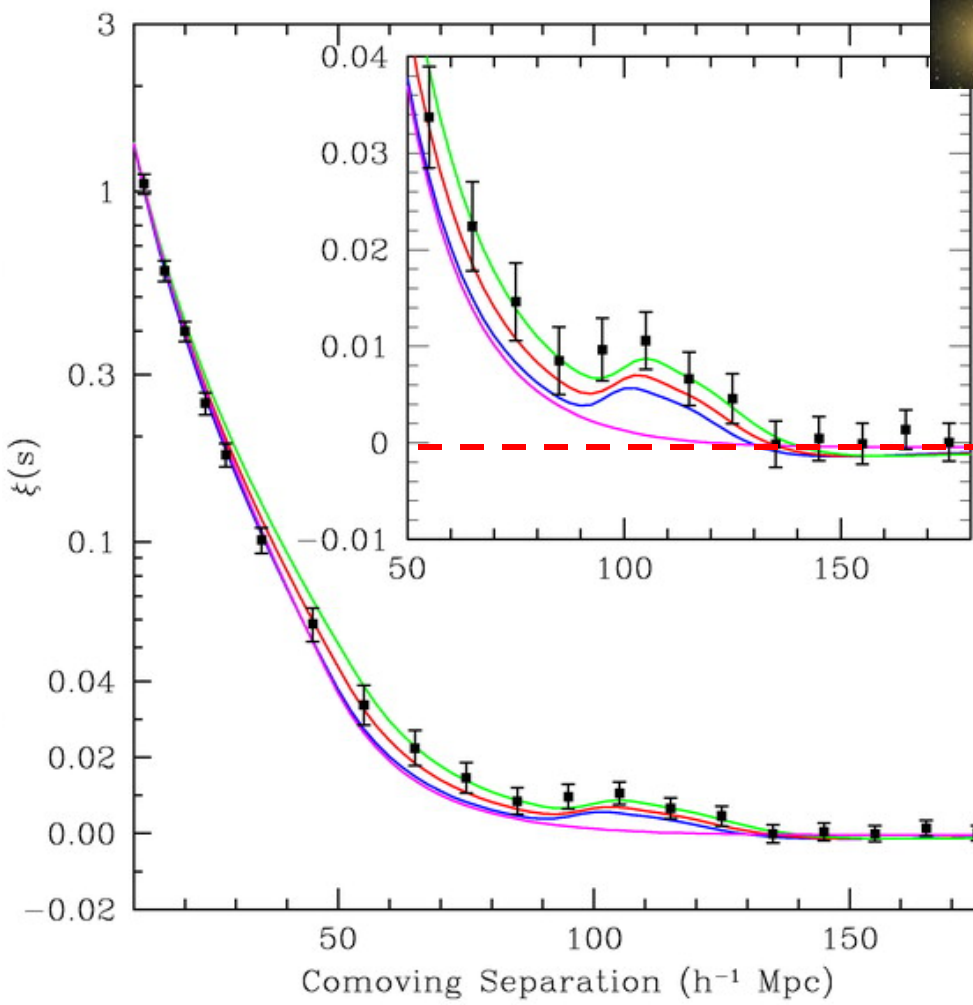
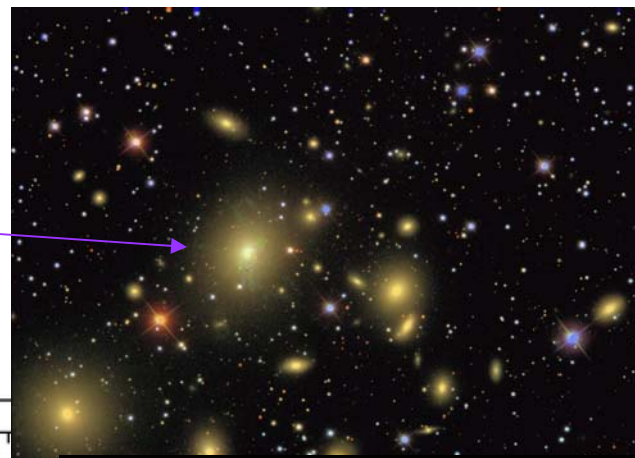
# Measuring $\xi(r)$ II

*Essential the random catalog looks like the real data!*



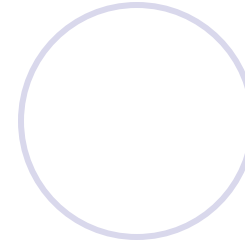
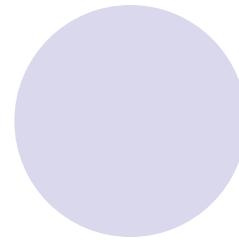


# $\xi(r)$ for LRGs



# Errors on $\xi(r)$

*Hardest part of estimating these statistics*



On small scales, the errors are Poisson

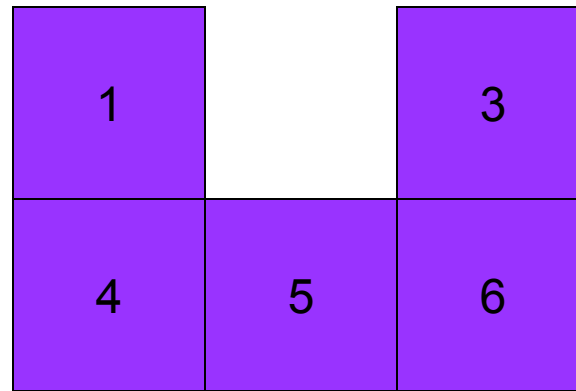
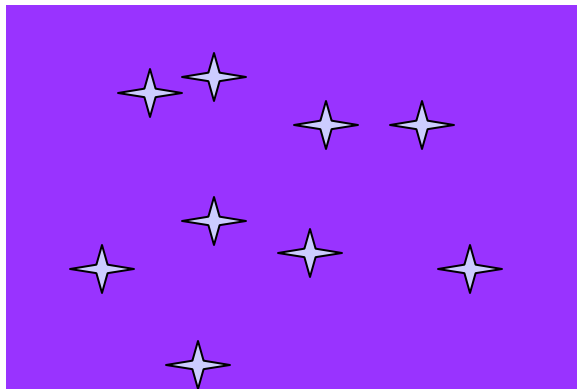
On large scales, errors correlated and typically larger than Poisson

- *Use mocks catalogs*
  - PROS: True measure of cosmic variance
  - CONS: Hard to include all observational effects and model clustering
- *Use jack-knives (JK)*
  - PROS: Uses the data directly
  - CONS: Noisy and unstable matrices

# Jack-knife Errors

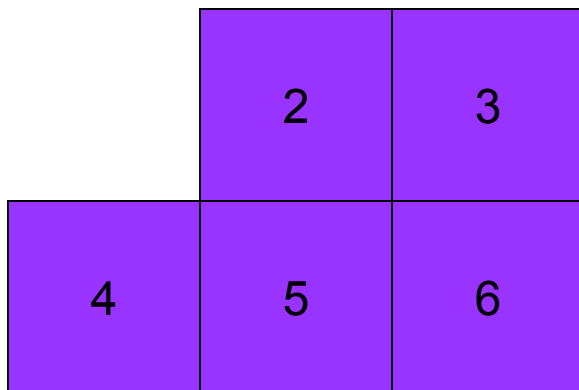


Real Data



N=6

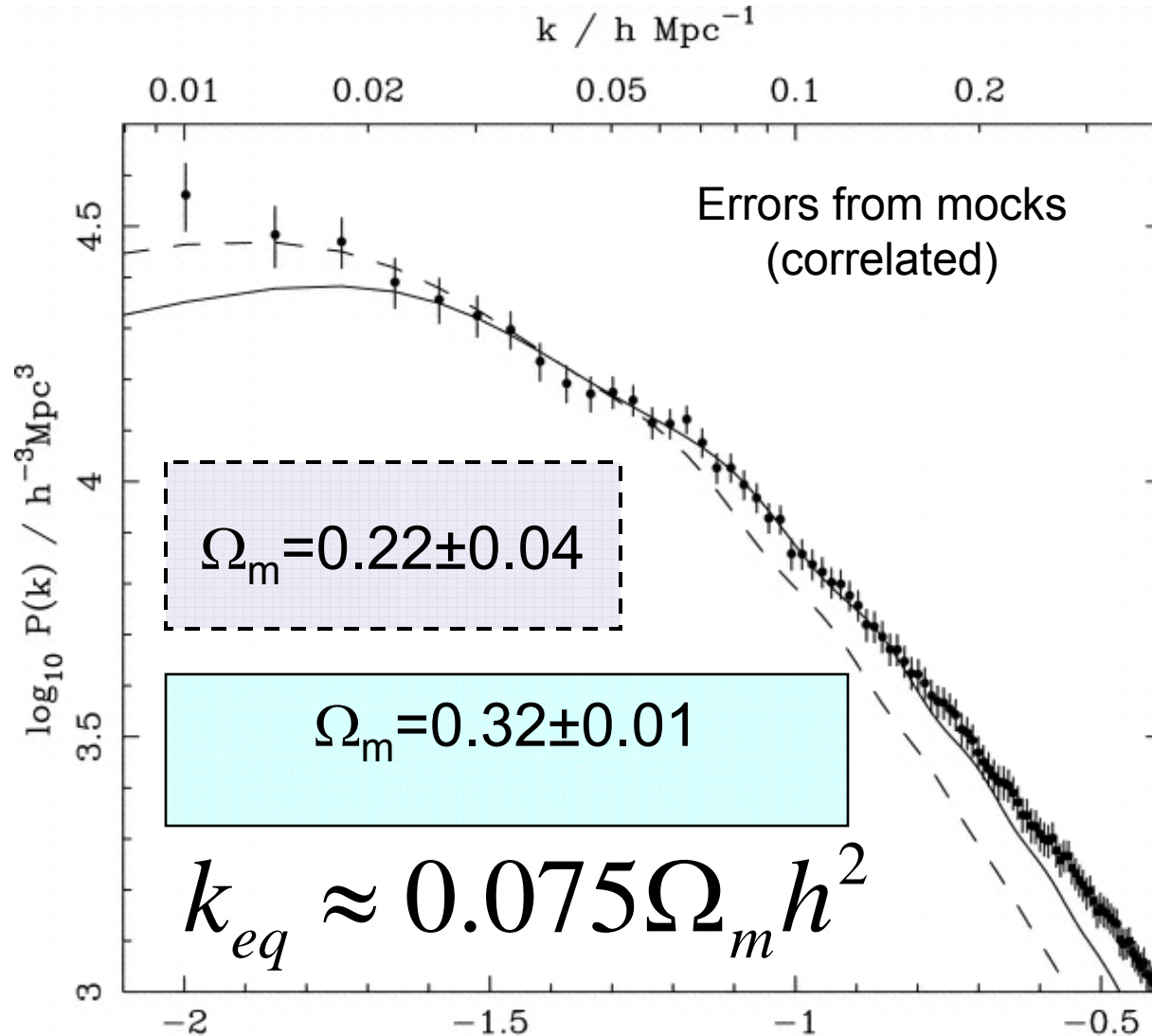
- Split data into N equal subregions
- Remove each subregion in turn and compute  $\xi(r)$
- Measure variance between regions as function of scale



$$\sigma^2 = \frac{(N-1)}{N} \sum_{i=1}^N (\xi_i - \bar{\xi})^2$$

Note the (N-1) factor because there are N-1 estimates of mean

# Latest P(k) from SDSS



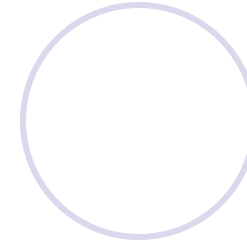
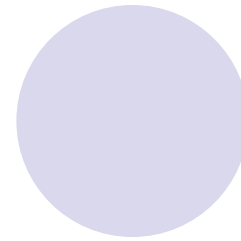
No turn-over yet seen in data!

$2\sigma$  difference

Depart from “linear” predictions at much lower  $k$  than expected

**Strongest evidence yet for  $\Omega_m \ll 1$  and therefore, DE**

# Hindrances

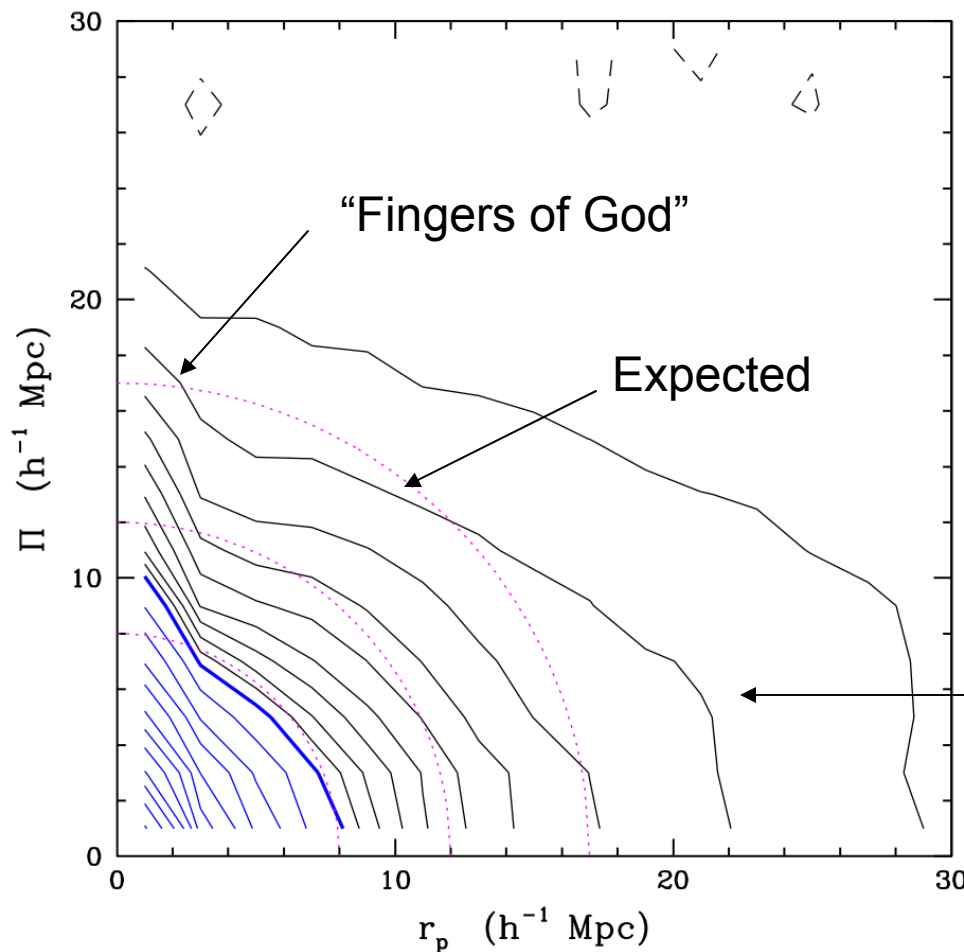


There are **two** “hindrances” to the full interpretation of the  $P(k)$  or  $\xi(r)$

- *Redshift distortions*
- *Galaxy biasing*

# Redshift distortions

We only measure redshifts not distances

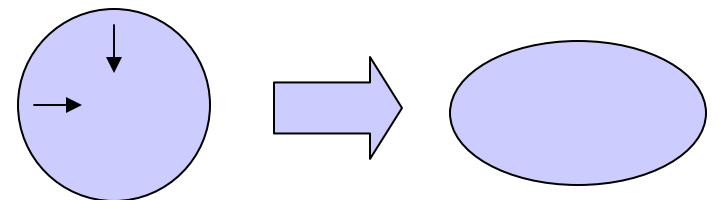


Therefore we usually quote  $\xi(s)$  as the “redshift-space” correlation function, and  $\xi(r)$  as the “real-space” correlation function.

We can compute the 2D correlation function  $\xi(\pi, r_p)$ , then

$$w(r_p) = 2 \int_0^{\pi_{\max}} \xi(r_p, \pi) d\pi$$

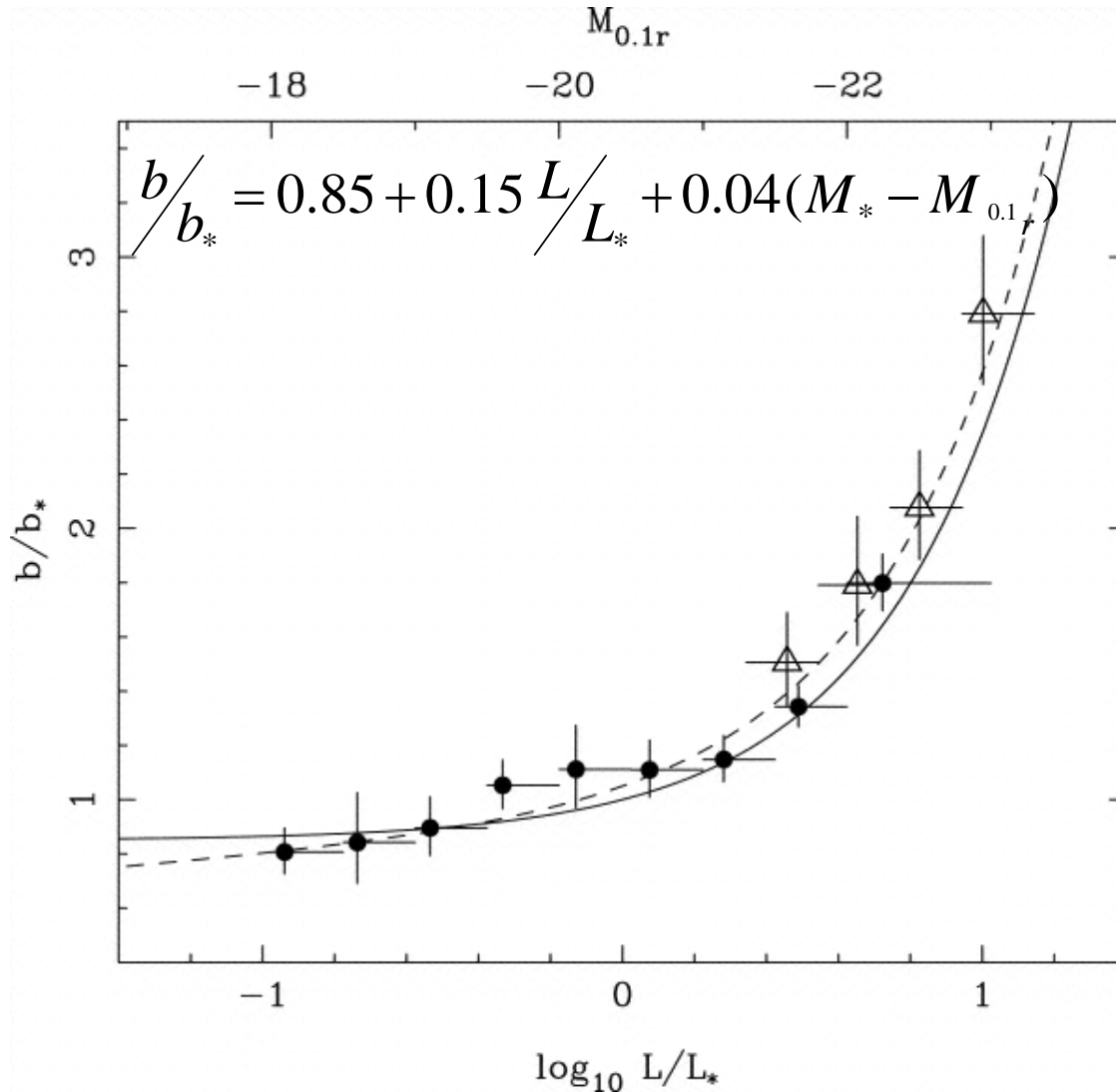
Infall around clusters





# Biassing

We see galaxies not dark matter



Maximal ignorance

$$\delta_{gal} = b \delta_{dm}$$

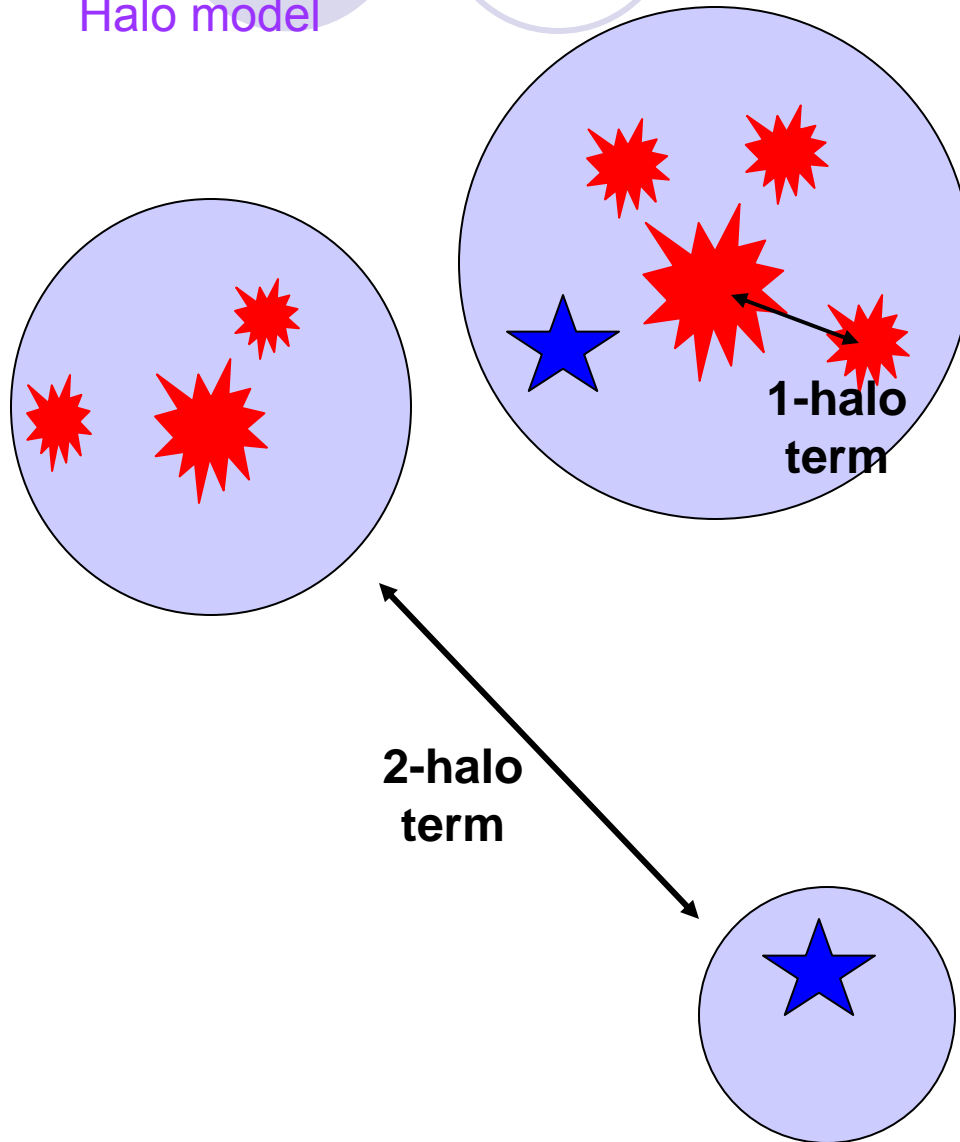
$$P(k)_{gal} = b^2 P(k)_{dm}$$

However, we know it depends on color & L

*Is there also a scale dependence?*

# Biasing II

Halo model

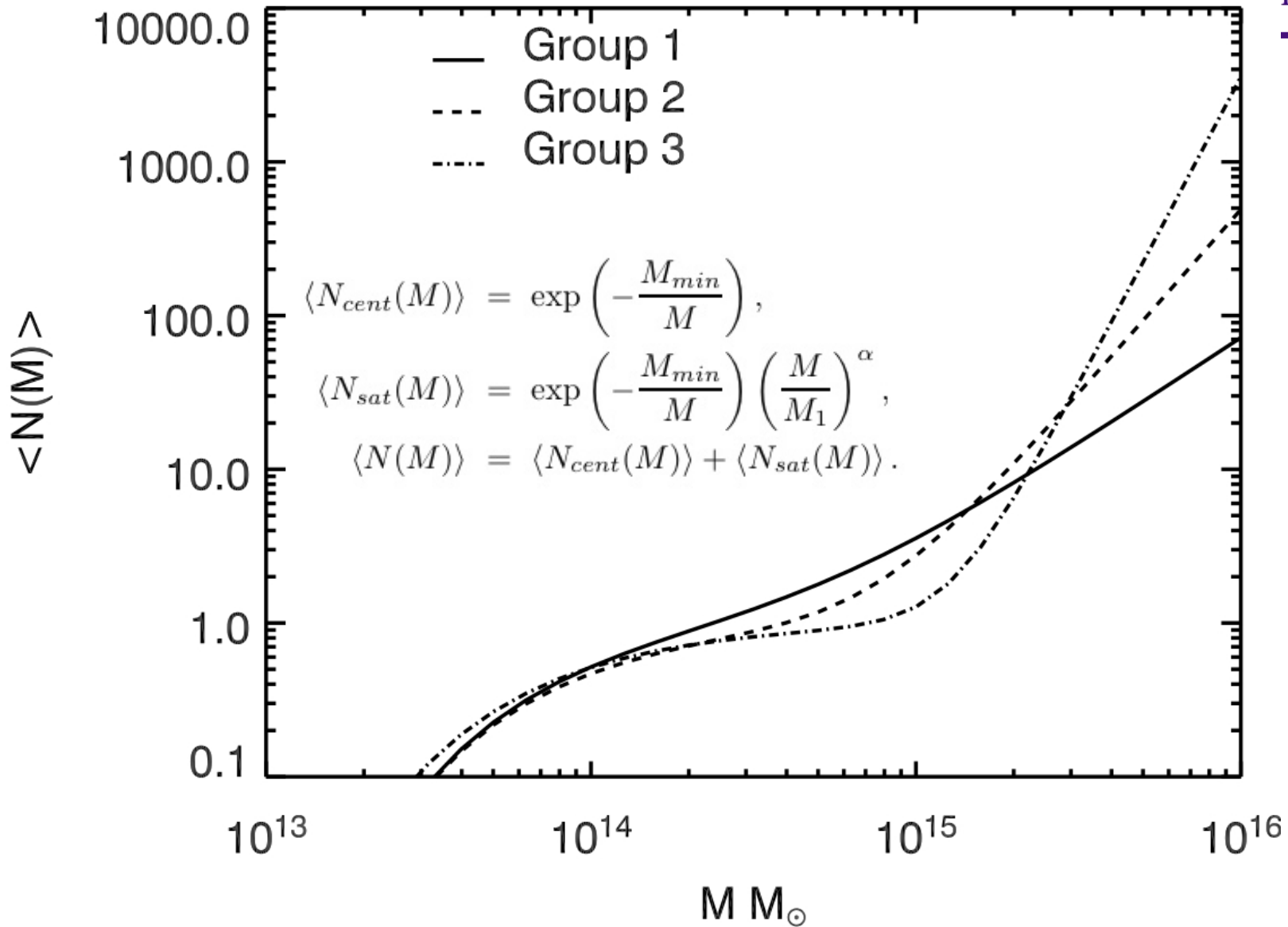


All galaxies reside in a DM halo

Elegant model to decompose **intra-halo** physics (biasing) from **inter-halo** physics (DM clustering)

$$P(k) = P_{1-halo} + P_{2-halo}$$

# Biasing III



# Hindrances (cont.)

There are two “hindrances” to the full interpretation of the  $P(k)$  or  $\xi(r)$

- *Redshift distortions*
- *Galaxy biasing*

How will we solve these problems?

*Higher-order statistics can help greatly*