

# Theoretical Aspects of SUSY Studies at ILC

S.Y. Choi (Chonbuk, Korea)

Why SUSY ?

What did we do here?

How to probe SUSY?

Future Tasks

Outlook

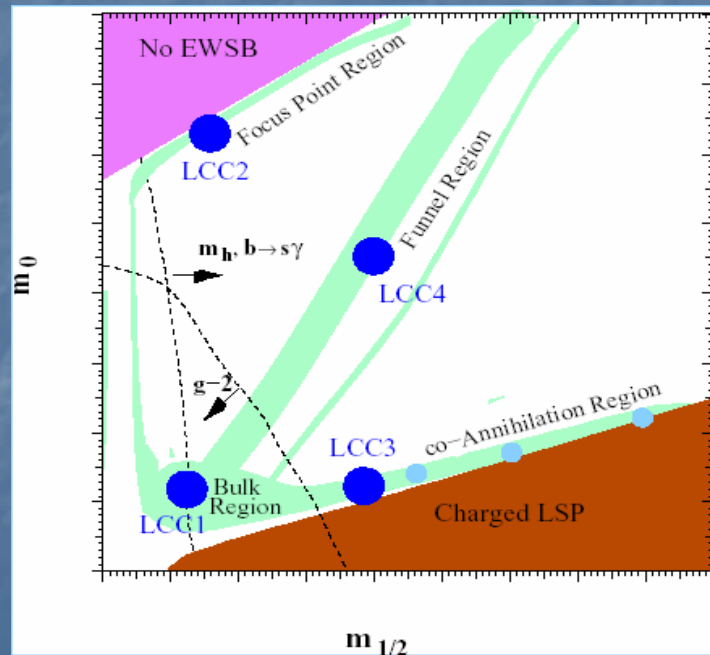
# Why SUSY?

Natural extension of 4-dimensional space-time by fermionic coordinates, linking bosons to fermions and vice versa

SUSY breaking unknown but expected to be discovered at the Tera-scale

Resolve a lot of physics issues such as gauge hierarchy, grand unification and cold dark matter

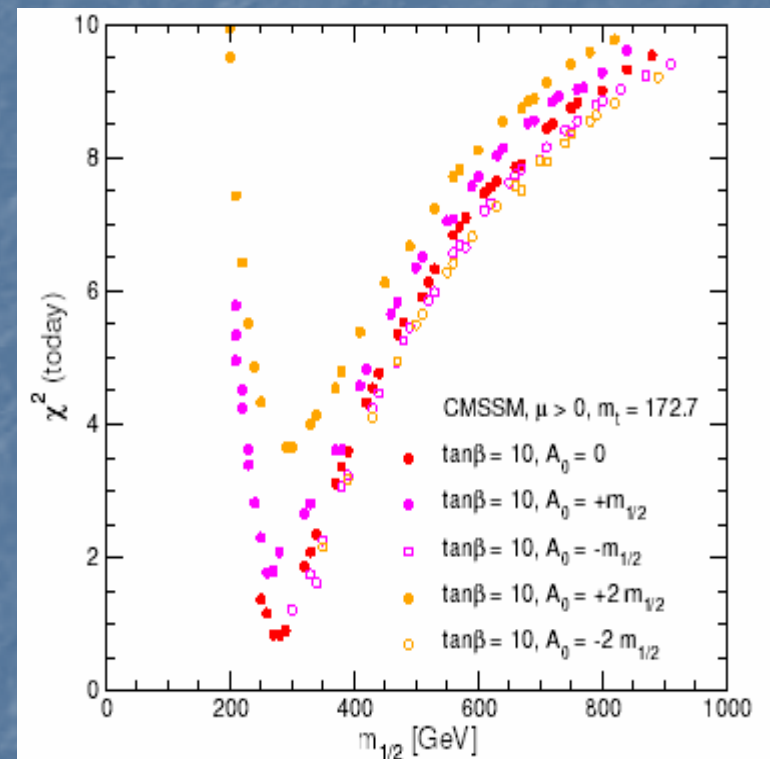
High precision measurements and cosmological observations prefer (slightly) low-scale SUSY



[M. Battaglia]

# Why SUSY?

$m_h > 114.4 \text{ GeV}$  for SM-like  $h$   
 $m_{\chi_1^\pm} > 103.5 \text{ GeV}$   
 $m_{\tilde{e}} > 99 \text{ GeV}$  for  $m_{\tilde{e}} - m_{\chi_1^0} > 10 \text{ GeV}$   
 $B(b \rightarrow s\gamma) = (3.25 \pm 0.54) \times 10^{-4}$   
 $B(B_s \rightarrow \mu^+\mu^-) < 1.5 \times 10^{-7}$   
 $\Delta a_\mu = (27.1 \pm 9.4) \times 10^{-10}$   
 $m_t = 172.7 \pm 2.9 \text{ GeV}$   
 $m_W = 80.425 \pm 0.034 \text{ GeV}$   
 $\sin^2 \theta_{\text{eff}} = 0.23150 \pm 0.00016$   
 $\eta_B = (6.1 \pm 0.4) \times 10^{-10}$   
 $0.094 < \Omega_{\text{CDM}} h^2 < 0.129$



[G.Weiglein]



# What did we do here?

A. Belyaev

SUSY at ILC

G. Weiglein

Indirect Sensitivities on the Scale of SUSY

J. Kalinowski

SPA Studies

C. Milstene

Analysis of Stop Quark with Small Stop-Neutralino Mass Difference at a Linear Collider

A. Freitas

Studying Light Sneutrinos at the ILC and Physical Implications

J. Proulx

Update on Slepton and Gaugino Mass Resolution Studies

S. Gopalakrishna

B-physics and Linear Collider Signatures of Light Stop and Sbottom

Y.G. Kim

Probing the Majorana Nature and CP Properties of Neutralinos

W. Porod

Correlations between Neutrino Physics and Collider Physics in the Bilinear Model

M. Battaglia

Detector and Simulation Issues of SUSY Searches at ILC

S. Hillert

Physics Potential of Vertex Detector as Function of Beam Pipe Radius

S. Heinemeyer

FeynHiggs

C. Balazs

Electroweak Baryogenesis in the MSSM

J.A.R. Cembranos

Collider Signatures of SuperWIMP Warm Dark Matter"

T. Krupovnickas

The Challenges of Focus Point at the LHC and LC

A. Belyaev

Implications of Non-universal SUGRA Models at ILC

H. Baer

Scenarios for SUSY CDM and the ILC

W. de Boer

Why the EGRET Excess of Diffuse Galactic Gamma Rays Points Towards Heavy Scalars

S. Hesselbach

CP-odd and T-odd Asymmetries in Chargino and Neutralino Production and Decay

G. Moortgat-Pick

The Physics Case for the Polarization of Both Beams at the ILC

G. Moortgat-Pick

Impact of Forward-Backward Asymmetries for Constraining Heavy Virtual Particles

Z. Zhang

Analysis of Two Challenging SUSY DM Scenarios at ILC

A. de Roeck

Non-universal Scalar Masses/Gravitino DM Benchmarks

**DISCUSSION ON SUSY BENCHMARK POINTS AT ILC**

# What did we do here?

|               |                                                                                     |
|---------------|-------------------------------------------------------------------------------------|
| A. de Roeck   | SUSY and BSM                                                                        |
| G. Weiglein   | LHC-ILC Interplay                                                                   |
| S. Hesselbach | Identifying the NMSSM by Combined LHC-ILC Analyses                                  |
| D. Zerwas     | SUSY Parameter Determination                                                        |
| W. de Boer    | Dark Matter Not So Dark Anymore?"                                                   |
| C. Balazs     | Supersymmetric Origin of Matter"                                                    |
| A. Freitas    | Analyzing the Stop Co-annihilation Region                                           |
| M. Peskin     | LHC and ILC Cosmology Predictions from Scans of the MSSM Parameters"                |
| F. Richard    | Dark Matter with Heavy Scalars at the ILC                                           |
| M. Perelstein | Dark Matter at Colliders: a Model-Independent Approach?                             |
| J. Alexander  | Dark Matter and Precision Measurements in the Focus Point Region                    |
| J. Gunion     | Dark Matter from Light Neutralinos and CP-odd Higgs Bosons in the NMSSM and the ILC |
| J. Reuter     | Multi-particle Event Generators for the MSSM                                        |
| P. Bechtle    | SUSY Parameter Measurements with Fittino                                            |
| W. Porod      | Progress Report on SPheno                                                           |
| H. Baer       | Progress Report on ISAJET                                                           |
| A. Belyaev    | Progress Report on IsaTools                                                         |
| G. Belanger   | Progress Report on MicrOmegas                                                       |
| H. Baer       | Constraints on SUSY Parameters from Present Data                                    |
| D. Cline      | Direct Dark Matter Detection                                                        |
| M. Battaglia  | Can the Relic Density Be Determined at Colliders?                                   |
| J. Kalinowski | SUSY Benchmarks                                                                     |
| A. Belyaev    | SUSY at ILC: SUGRA Scenarios and Connections                                        |
| W. Porod      | Flavor, CP, RPV, Neutrino Physics at ILC                                            |
| A. Safonov    | SUSY Tools                                                                          |
| K. Kawagoe    | Detector and Simulation Issues                                                      |

# What did we do here?

5 conveners: A. Belyaev, S.Y. Choi, K. Kawagoe, J. Kalinowski, A. Safonov  
3 mini-plenary, 5 parallel, 2 joint and 1 discussion sessions  
More than 50 talks in SUSY, ILC/LHC, ILC/Cos, and Loopfest

Impossible to give justice to all

More than half of the talks are related to CDM  
Most studies are based on mSUGRA  
New benchmark points are discussed and proposed  
A few new realistic simulations

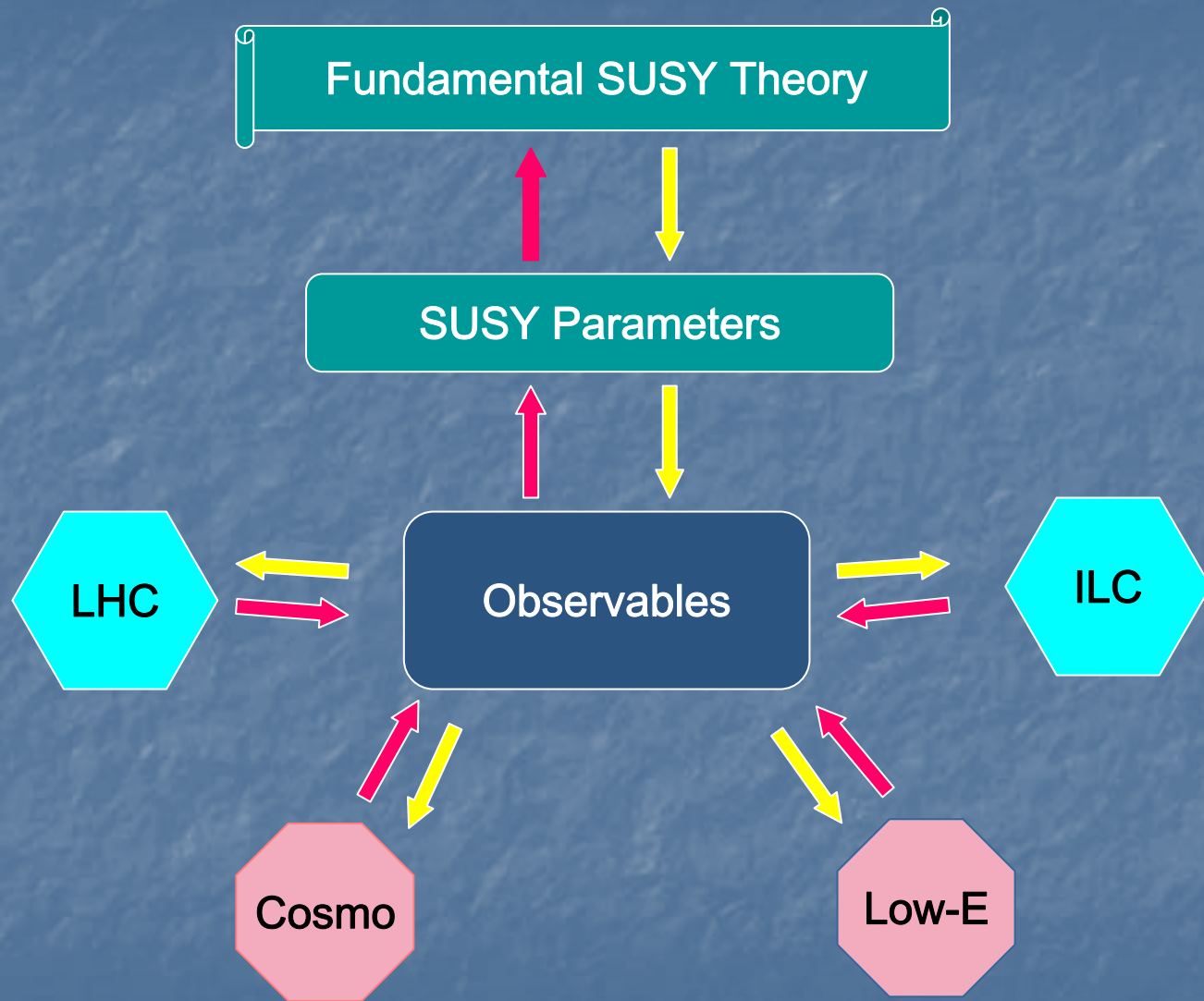
-----

Here: theoretical aspects of SUSY  
SUSY tools and experiments covered by Alexi Safonov



# How to Probe SUSY?

# Grand SUSY Path





# Requirements

## Precise and efficient theoretical predictions [A. Belyaev, A. Safonov]

- => Higher-order corrections and automatic calculation tools
- => Consistent RGE programs

## Excellent accelerator and detector performance is a must

- => Physics/detector-oriented benchmarks [LCCs by Phy. Bench. Panel]
- => Detector performance evaluations [K. Kawagoe]

## Overall (model-independent) combined analyses are urgent?!

- => New benchmarks for Cos/LHC/ILC [J. Kalinowski ] under discussion!
- => Perform full simulations for the LHC/ILC/Cos points within three years. Remember that LHC will start running in 2007. [M. Nojiri]

## R-parity, CP and flavor violating phenomena [W. Porod]

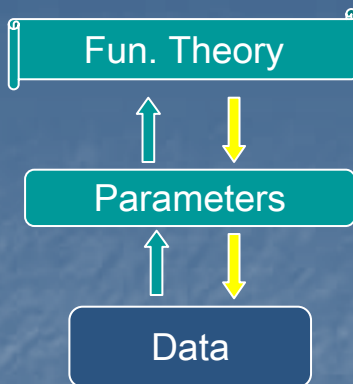
- => Neutrino and LE flavor physics
- => EW baryogenesis [C. Balazs]
- => Direct CP violation
- => ...

In addition: NMSSM, GDM and other SUSY breaking scenarios

# Synergy

Constructive Interference/Cooperation  $\Leftrightarrow$  Quantum Jump in Quality

ILC  $\Leftrightarrow$  LHC  $\Leftrightarrow$  Cosmology  
Discovery  $\Leftrightarrow$  Precision  
Theory  $\Leftrightarrow$  Tool  $\Leftrightarrow$  Experiment



# The SPA Project

## SPA Convention

**renorm. schemes / LE parameters / observables**

## Program repository

**th. /exp. analyses / LHC+ILC tools / SLHA**

## Theoretical and experimental tasks

**short- and long-term sub-projects**

## Reference point SPS1a'

**derivative of SPS1a, consistent with all data**

## Current and future developments

**CP-MSSM, NMSSM, RpV, String effective th. etc**

Visit <http://spa.desy.de/spa> and join the project as an author



# Recent Progress: A Few Examples

Recent, interesting and provocative

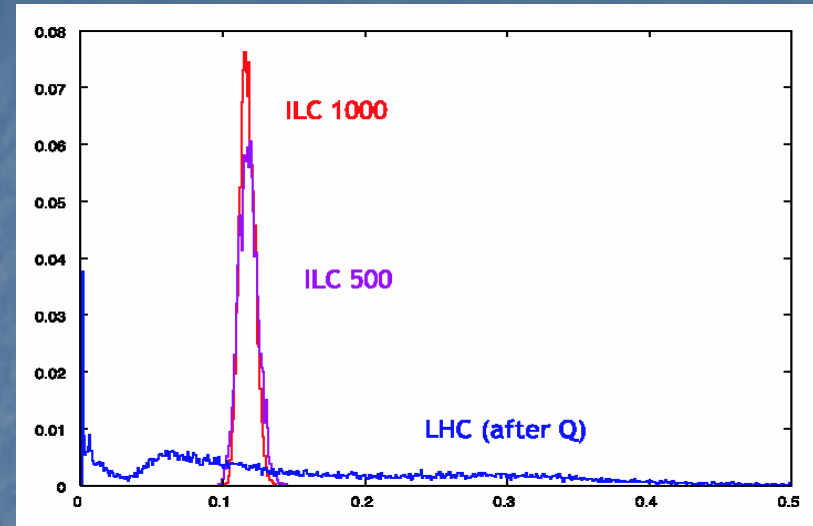
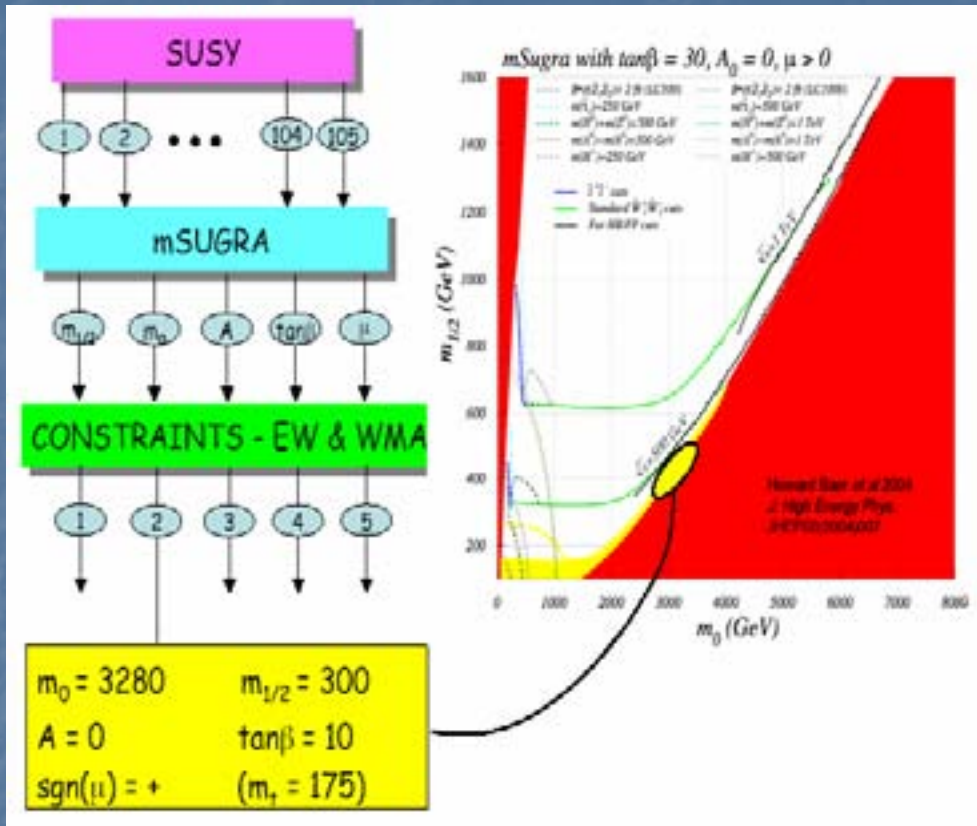
With emphasis on

Significant improvements of ILC on LHC measurements

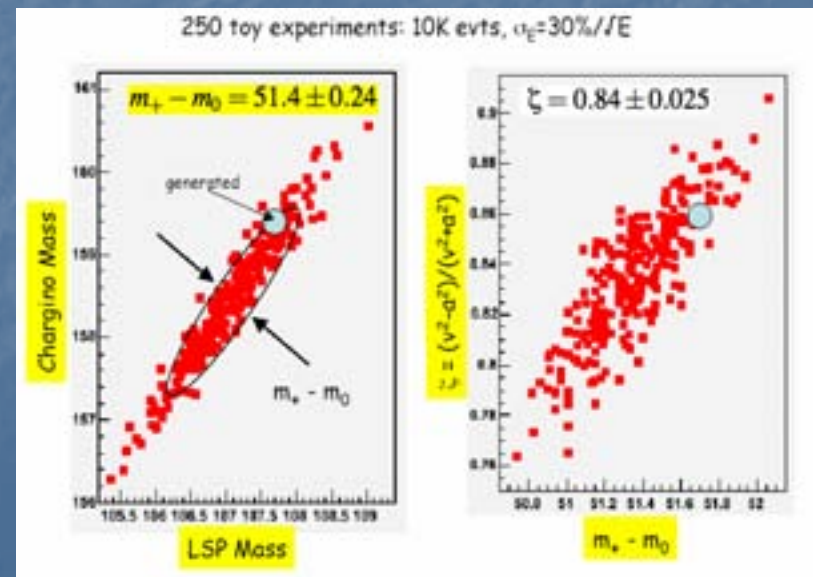
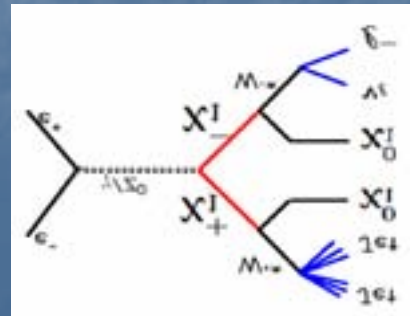
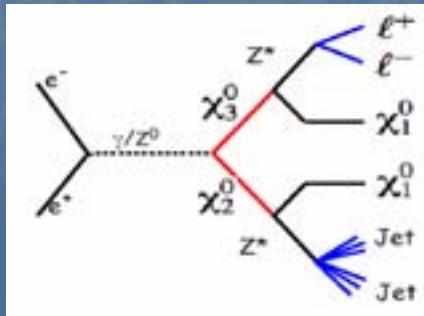
Matching the current and future CDM relic density measurements

# Focus on Focus Points (LCC2)

[J. Alexander, M. Peskin, F. Richard, ...]



[Markov Chain Scan]

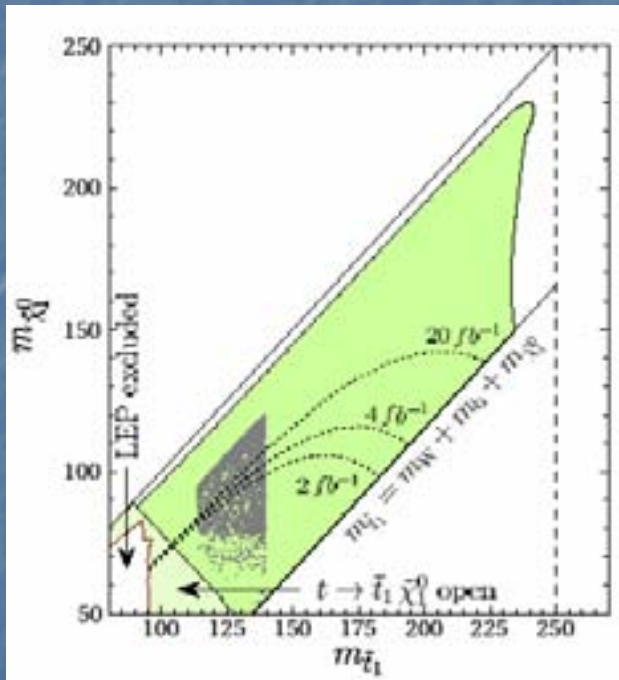


# EW Baryogenesis in MSSM

[C. Milestene, C. Balazs, A. Freitas]

Light R-handed stop for 1<sup>st</sup> order phase transition  
New CP phases from  $\mu$  and tri-linear parameter A

Small stop-LSP mass difference  $\Leftrightarrow$  Stop co-annihilation

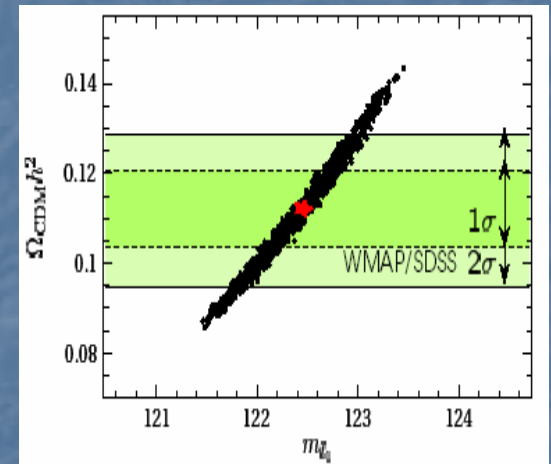


$$\begin{aligned} e^+e^- &\rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^- \\ e^+e^- &\rightarrow \tilde{\chi}_1^0 \tilde{\chi}_2^0 \\ e^+e^- &\rightarrow \tilde{\chi}_2^0 \tilde{\chi}_2^0 \end{aligned}$$

$$\begin{aligned} M_1 &= 112.6 \pm 0.2 \text{ GeV} \\ M_2 &= 225.0 \pm 0.7 \text{ GeV} \\ |\mu| &= 320.0 \pm 3.3 \text{ GeV} \end{aligned}$$

$$\begin{aligned} |\phi_\mu| &< 1.0 \\ \tan \beta &= 5^{+0.5}_{-2.6} \end{aligned}$$

$$e^+e^- \rightarrow \tilde{t}_1 \tilde{t}_1^* \rightarrow c \bar{c} \tilde{\chi}_1^0 \tilde{\chi}_1^0$$





## Indirect Searches: Galactic Gamma Spectrum in EGRET

Excess over conventionally expected yield

Candidate:  $\chi\chi \rightarrow b\bar{b} \rightarrow \pi^0 \rightarrow \gamma \Rightarrow m_\chi \sim 50 \text{ to } 100 \text{ GeV} | M_{\text{scal}} \sim 1 \text{ TeV}$

Higgs limit requires then: squarks and sleptons above  $\approx \text{TeV}$

EWSB (and g-2) require: squarks and sleptons  $\leq 2$  TeV

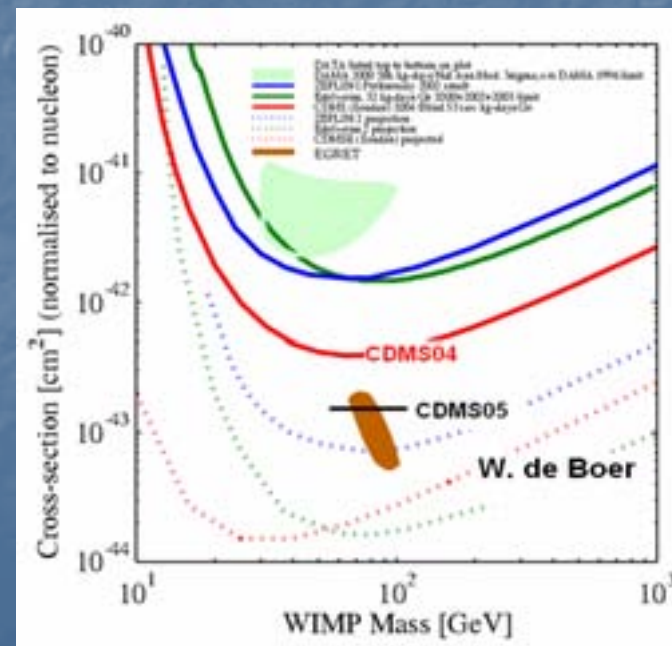
$\tan\beta \approx 50-55$  preferred

## Conclusion dep crucially on conventional bkgd: under sufficient control?

## Direct searches

CDMS05 is already sensitive to the proposed parameter range.

[F. Richard, D. Cline]

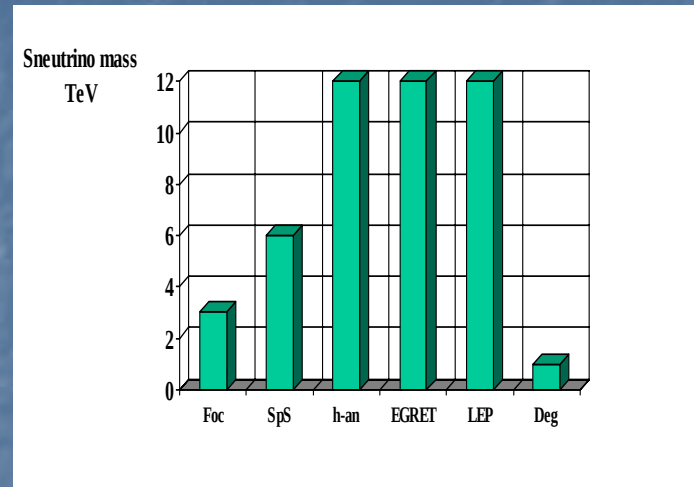




# High Precision: Exploiting Virtual Effects of High-mass Particles

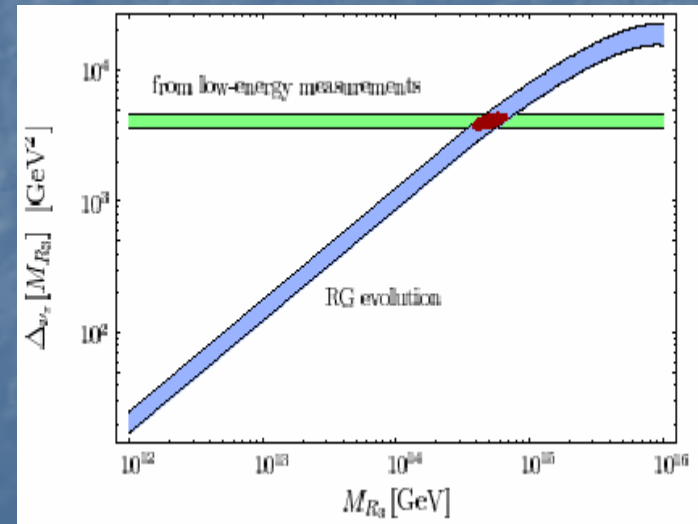
[F. Richard, G. Moortgat-Pick, Z. Zhang]

Chargino production affected by sneutrino t-channel exchanges  
Sneutrion mass large in focus-point theories  
Indirect sensitivities up to 12 TeV



[A. Freitas]

High precision in slepton/sneutrino sector sensitive to R-handed neutrino scale around  $10^{14}$  GeV



# What if

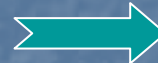
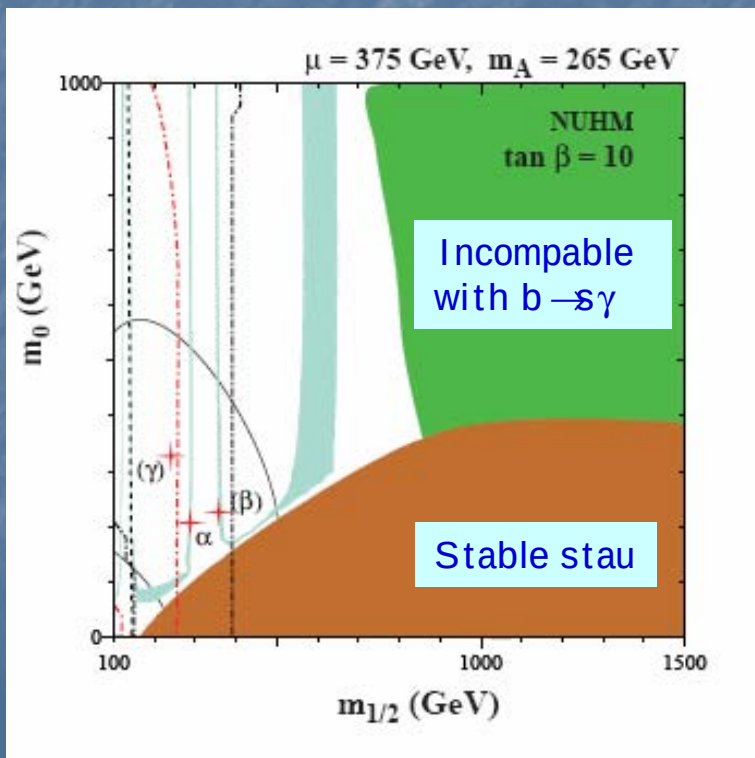
## Non-Universal Higgs Masses

[A. de Roeck, A. Belyaev, H. Baer]

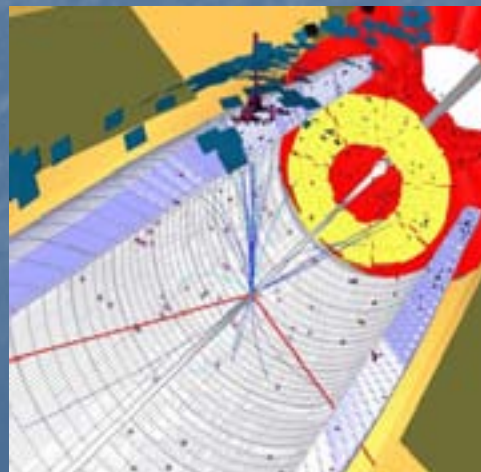
$$m_{H_{u,d}}^2 = (1 + \delta_{u,d})m_0^2$$



EW vacuum conditions no longer fix  $\mu$  and  $m_A$   
Can use this freedom to get new signatures



$\alpha \Rightarrow \chi_2 \rightarrow \chi Z$   
 $\beta \Rightarrow \chi_2 \rightarrow \chi h$   
 $\gamma \Rightarrow \chi_2 \rightarrow \chi Z^*$



Simulated SUSY  
event in the CMS  
detector for  $\alpha$

# What if

## CP-violated MSSM

[S. Hesselbach]

CP-odd asymmetries in  
gaugino/higgsino

Beam polarization important  
[G. Moortgat-Pick]

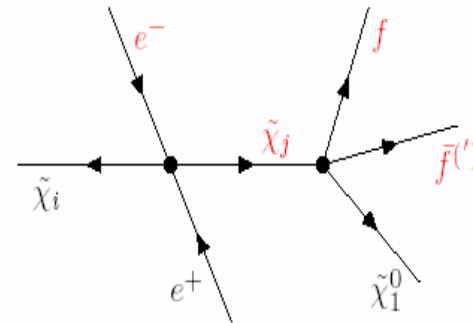
[Y.G. Kim]

$$\tilde{\chi}_i^0(\vec{p}) \rightarrow \tilde{\chi}_j^0 + f^-$$

in the neutralino rest frame

Majorana nature can be confirmed by  
lepton energy/angular distribution  
lepton invariant mass/opening angle

Triple products:  $T = \vec{p}_{e^-} \cdot (\vec{p}_f \times \vec{p}_{\tilde{f}'})$  or  $T = \vec{p}_{e^-} \cdot (\vec{p}_{\tilde{\chi}_j} \times \vec{p}_f)$



→ T-odd asymmetry:

$$A_T = \frac{\sigma(T > 0) - \sigma(T < 0)}{\sigma(T > 0) + \sigma(T < 0)} = \frac{\int \text{sign}(T) |T|^2 d\text{Lips}}{\int |T|^2 d\text{Lips}}$$

→ CP-odd, if final state interactions and finite-widths effects can be neglected

# What if

## R-parity Violation

[W. Porod]

$$\text{MSSM} + \epsilon_i \tilde{L}_i \hat{H}_u + B_i \epsilon_i \tilde{L}_i H_u$$

$$m_{\nu, \text{eff}} = \frac{M_1 g^2 + M_2 g'^2}{4 \det(\mathcal{M}_{\chi^0})} \begin{pmatrix} \Lambda_1^2 & \Lambda_1 \Lambda_2 & \Lambda_1 \Lambda_3 \\ \Lambda_1 \Lambda_2 & \Lambda_2^2 & \Lambda_2 \Lambda_3 \\ \Lambda_1 \Lambda_3 & \Lambda_2 \Lambda_3 & \Lambda_3^2 \end{pmatrix}$$

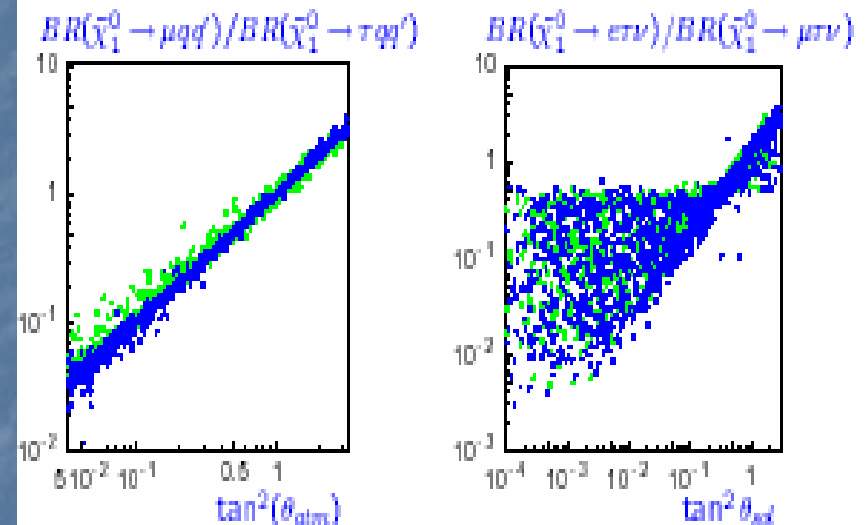
$$\Lambda_i = \mu v_i + v_d \epsilon_i$$

$$\tan^2 \theta_{\text{atm}} = \left( \frac{\Lambda_2}{\Lambda_3} \right)^2, U_{e3}^2 = \frac{\Lambda_1^2}{\Lambda_2^2 + \Lambda_3^2}, \tan^2 \theta_{\text{sol}} = \left( \frac{\bar{\epsilon}_1}{\bar{\epsilon}_2} \right)^2$$

$$\Gamma(\tilde{\chi}_1^0 \rightarrow W^\pm l_i^\mp) \propto \frac{\Lambda_i^2}{\det \mathcal{M}_{\tilde{\chi}^0}}$$

$$\Gamma(\tilde{\chi}_1^0 \rightarrow \sum_i Z \nu_i)$$

$$\Gamma(\tilde{\chi}_1^0 \rightarrow \nu \tau + l_i^-) \propto \frac{\epsilon_i^2}{\mu^2}$$



Gravitino could be a warm DM even in this model



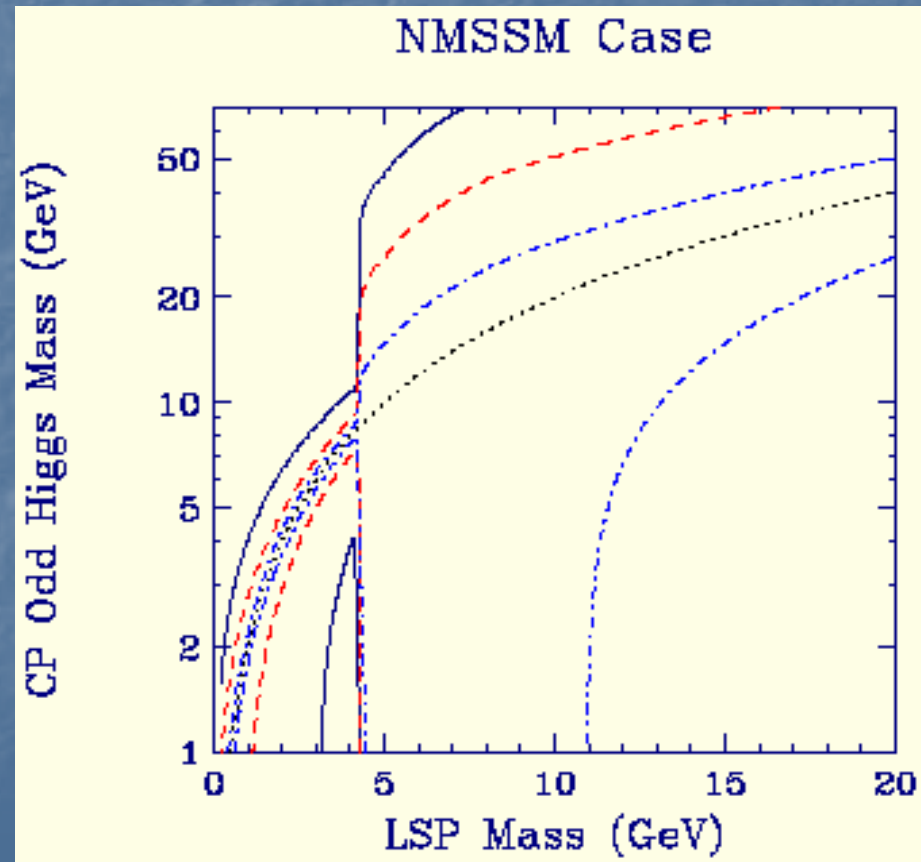
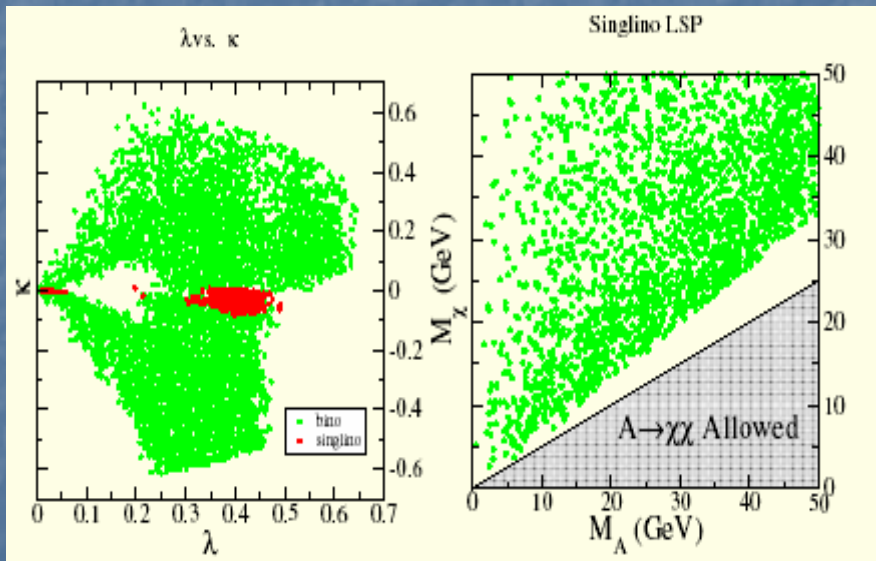
# What if

## NMSSM

[J. Gunion, S. Hesselbach]

$$\lambda \widehat{S} \widehat{H}_u \widehat{H}_d + \frac{\kappa}{3} \widehat{S}^3$$

$$\tan \beta = \langle H_u \rangle / \langle H_d \rangle, \quad \mu_{\text{eff}} = \lambda \langle S \rangle \equiv \lambda x$$



# Future Tasks for SUSY enthusiasts

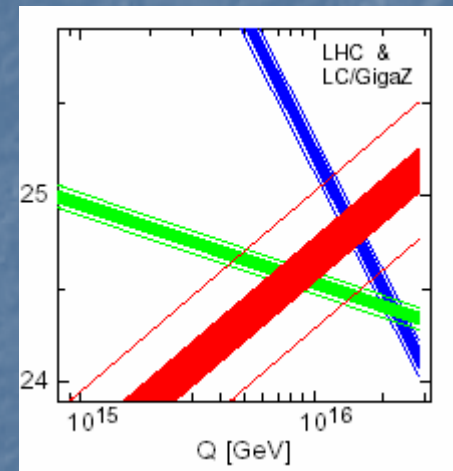
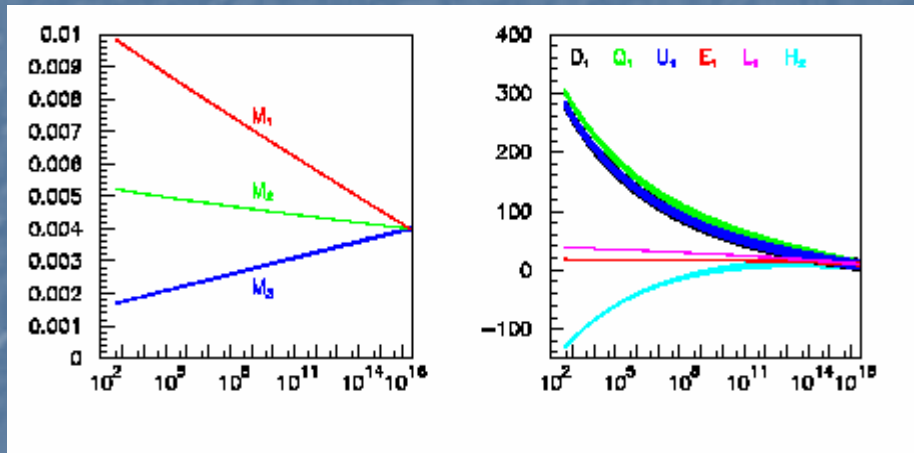
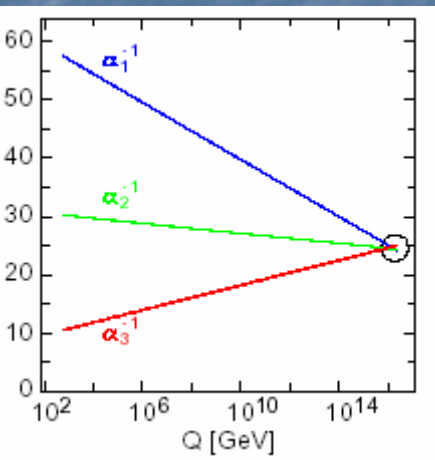
Perform more precise theoretical calculations to match expected experimental precision: factor 10 ~ one more loop

Develop several indep. tools: connection of fund. parameters to observables  
: predictions for relic density etc

Experimental simulations for many more scenarios and reference points

# Outlook

## High Precision SUSY Analyses at LHC + ILC + Cos + LE



Telescope to GUT / Planck Scale Physics