

Little Higgs

@

Snowmass

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Outline

1. motivation

- "naturalness problem"

2. little Higgs construction

- "collective breaking"

3. little Higgs and experiments

T -parity

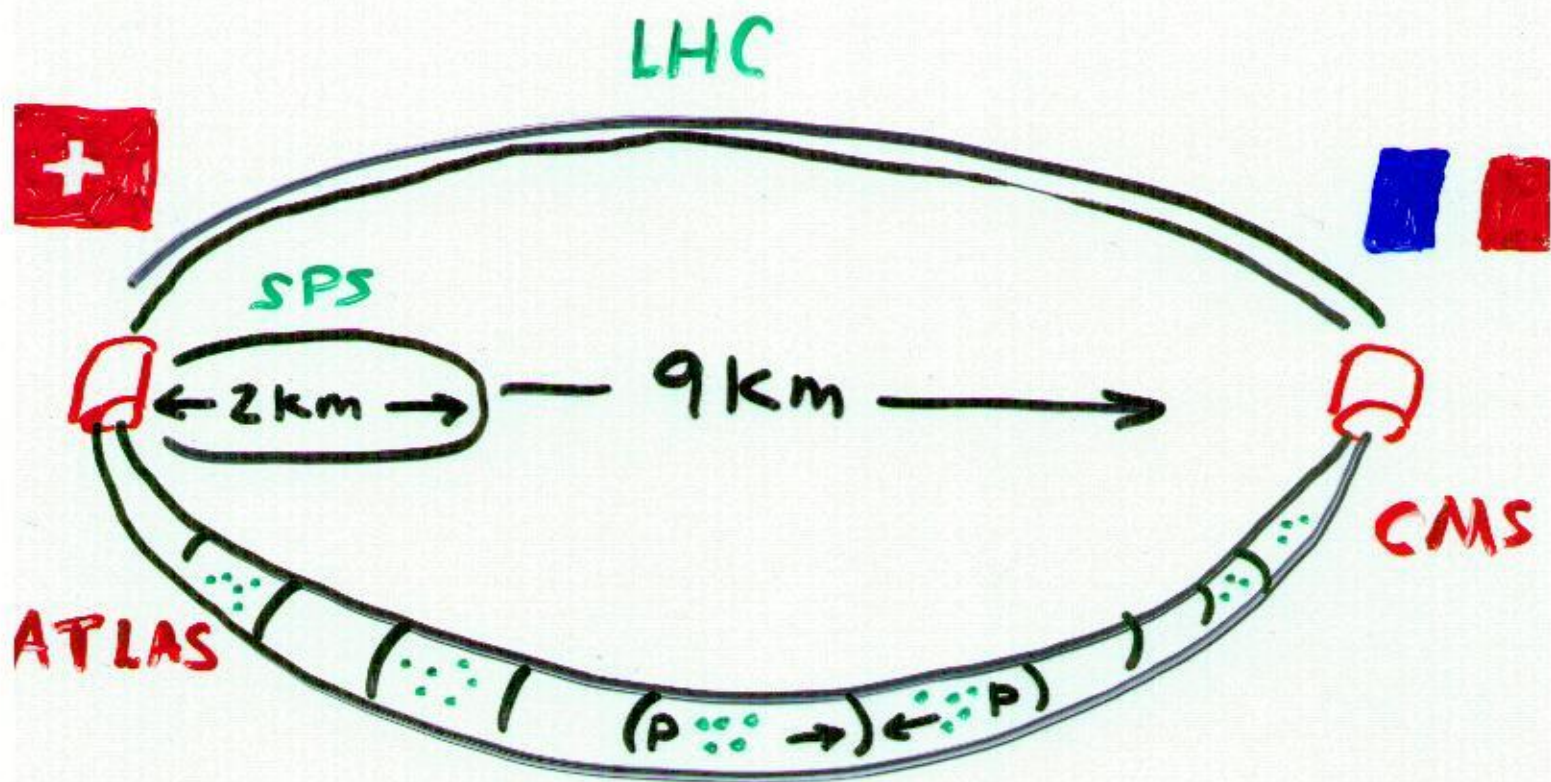
- precision electroweak $\leftrightarrow$ fine tuning
- phenomenology @ LHC

What do we
expect to see
@ the

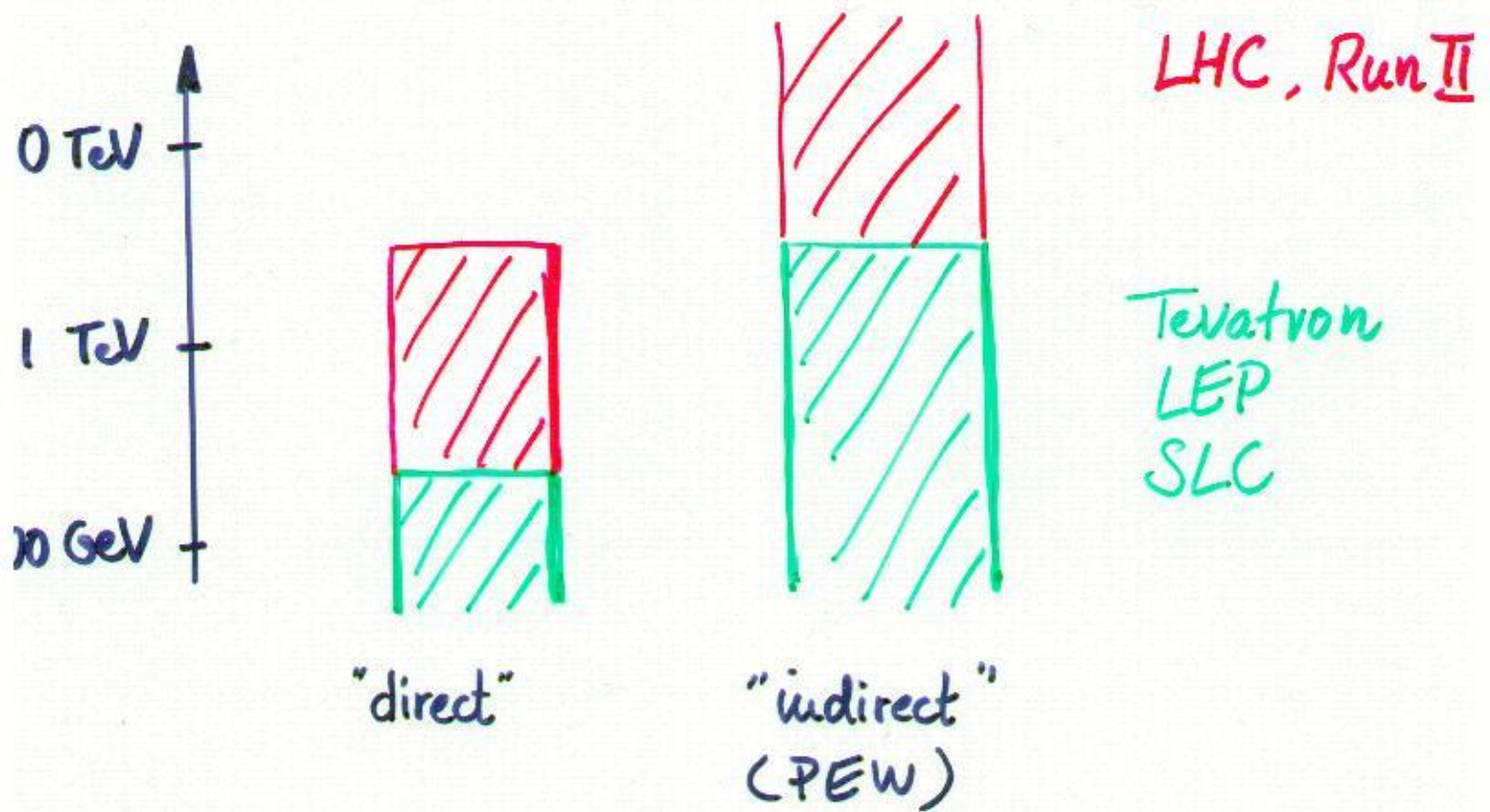
LHC

?

Theorists view of the LHC



Experimental tests of the Standard Model



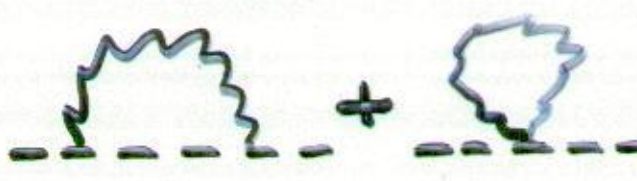
- Standard Model only @ multi-TeV
- cleverly hidden (weakly coupled) extension beyond the Standard Model

a. ~~Naturalness~~ ~~Hierarchy~~ Problem

Assume that the SM (with a Higgs of mass ≈ 200 GeV) is valid up to $\Lambda \approx 10$ TeV

⇒ Problem: quadratic divergences at 1-loop

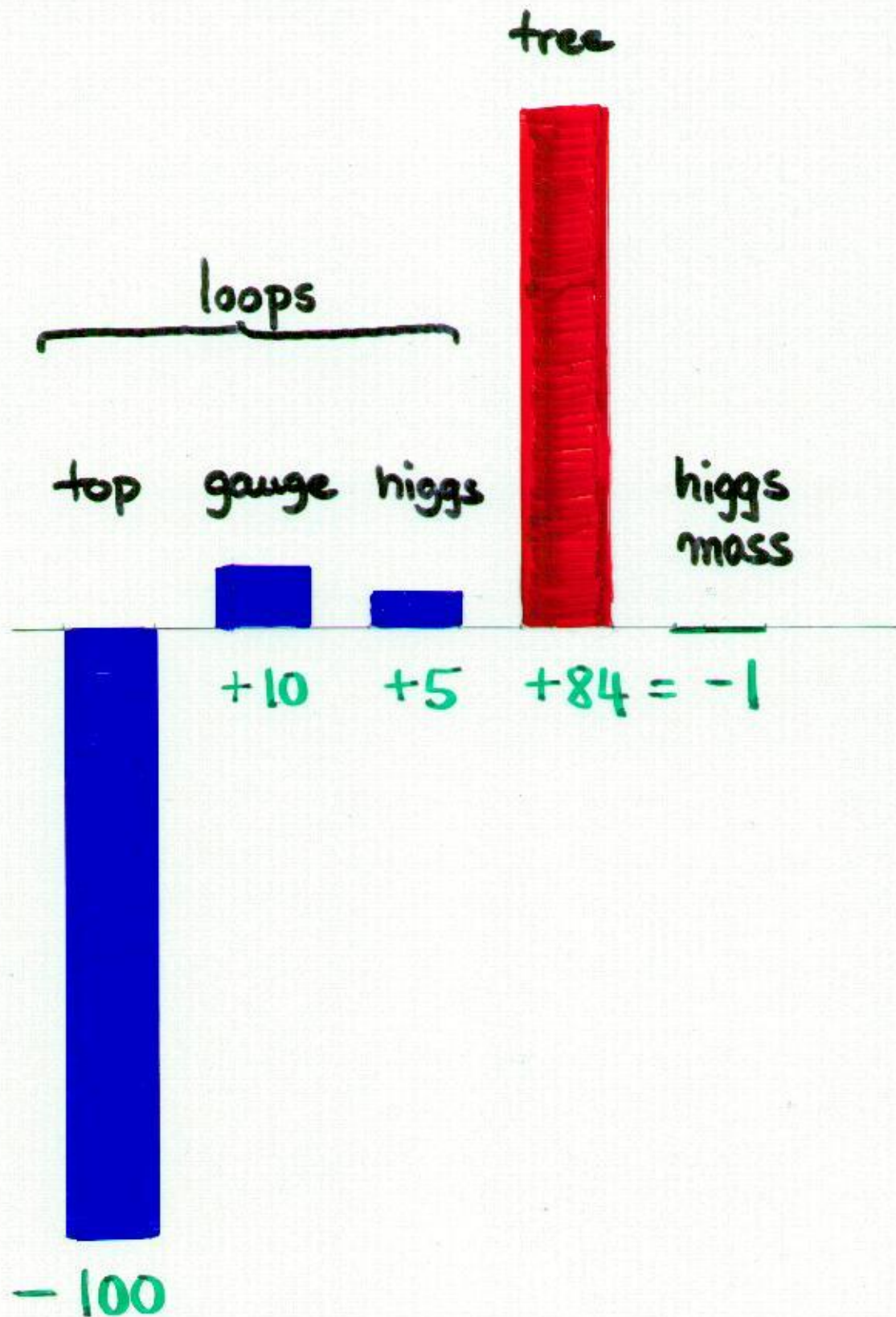
top:  $\sim \frac{-\lambda_t^2}{16\pi^2} \Lambda^2 \approx -(2 \text{ TeV})^2$

$SU(2) \times U(1)$ gauge:  $\approx (700 \text{ GeV})^2$

Higgs:  $\approx (500 \text{ GeV})^2$

Corrections are 100 times bigger than the expected mass !

fine tuning with $\Lambda = 10 \text{ TeV}$

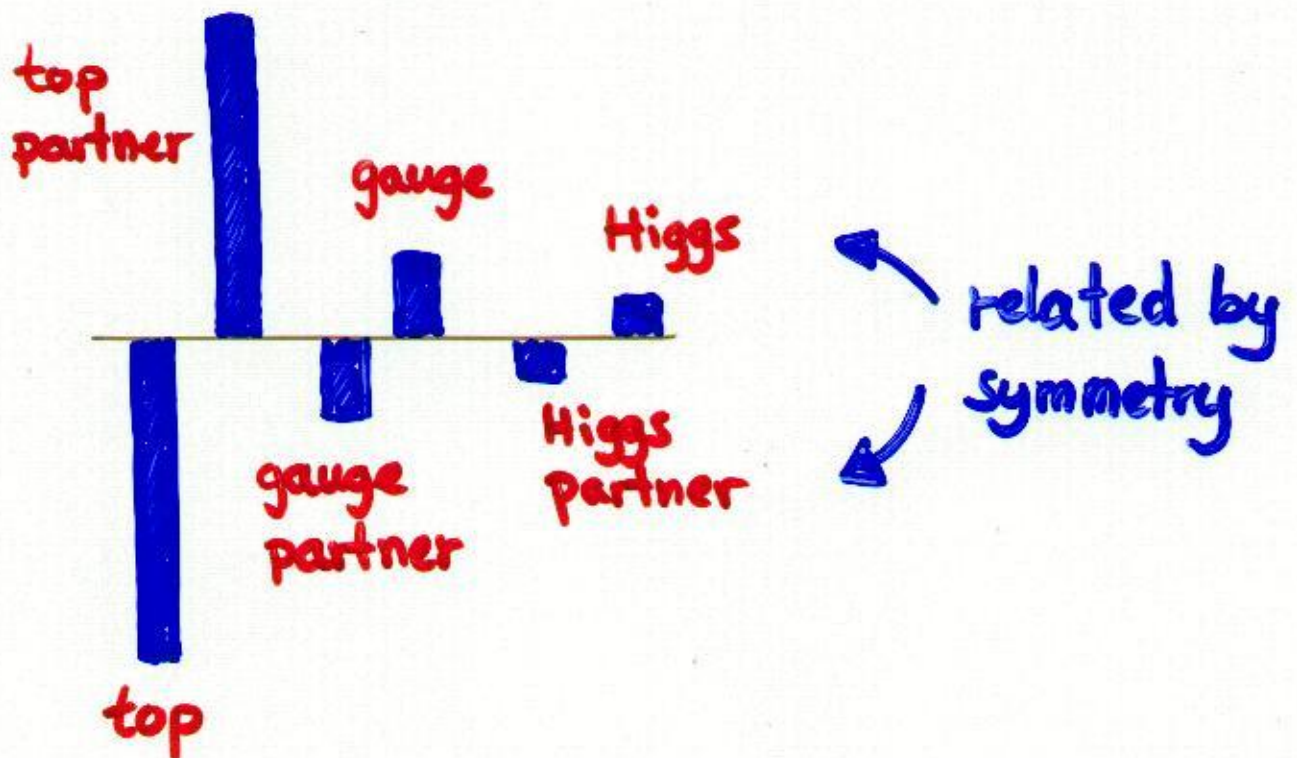


b. (weakly coupled extension)

What to do?

Cancel the divergences with new
particles running in the loop

+ a symmetry



Example: SUSY



couplings related
by SUSY

$$\delta m_H^2 \approx - \frac{\lambda_t^2}{16\pi^2} \Lambda^2 + \frac{\lambda_t^2}{16\pi^2} \Lambda^2$$

fermion canceled by boson

Summarize ...

Precision EW data

+

Higgs naturalness problem

predict

New (weakly coupled) particles
related to ...

top

2 TeV

W, Z

at or below

5 TeV

higgs

10 TeV

(assumed $\leq 10\%$ tuning)

The MSSM is
fine-tuned,

are there
alternatives?

5

2. Little Higgs

'84 Composite
Higgs



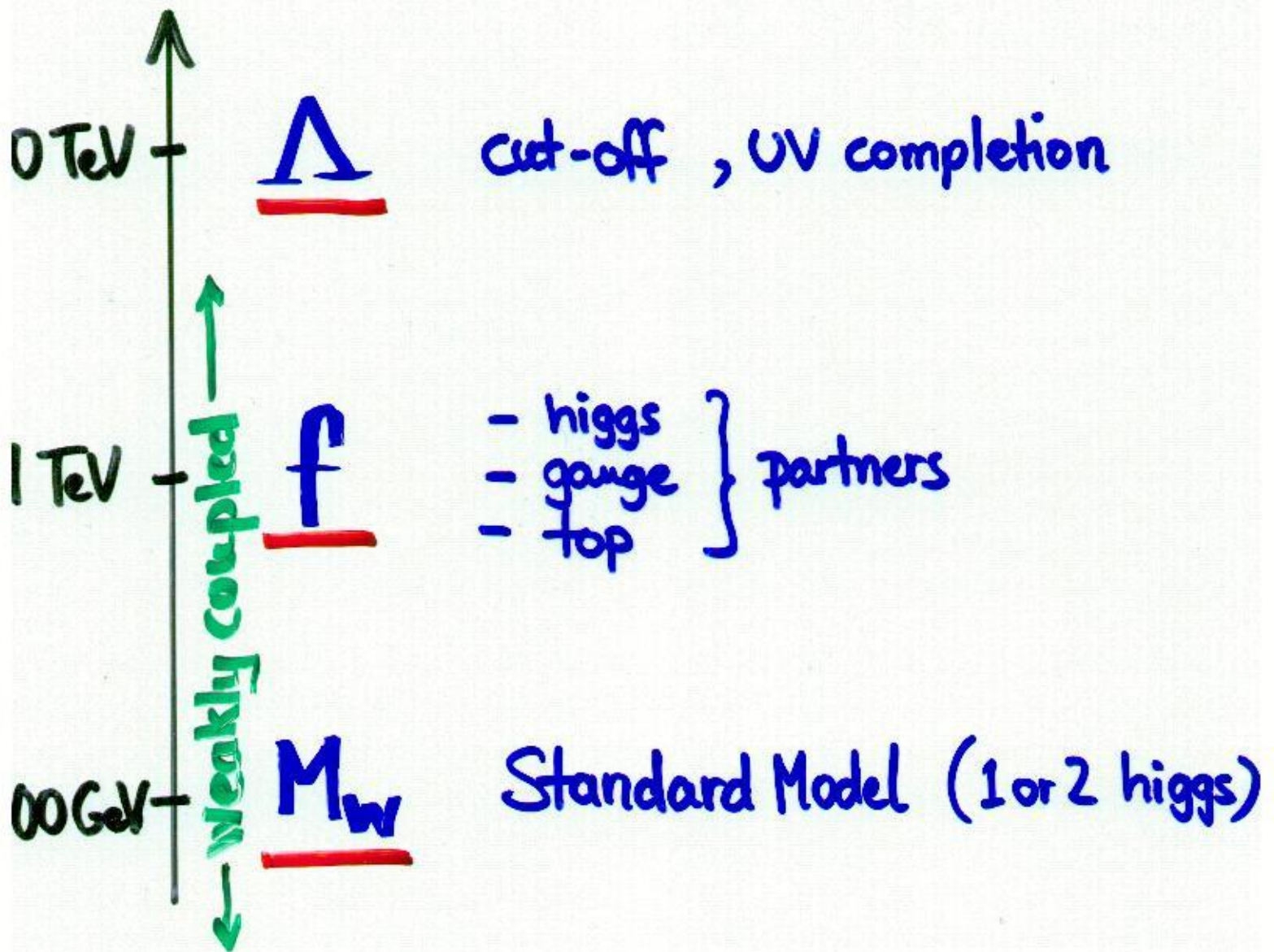
'19 Extra
Dimensions



'01

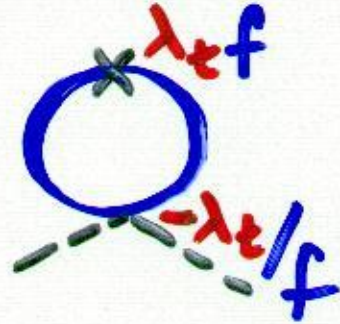


little higgs spectrum



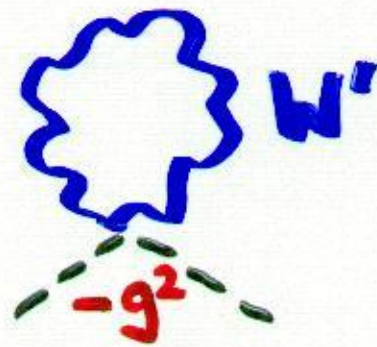
Little Higgs loop cancellations

- new colored fermion χ , mass $\sim \text{TeV}$



fermion cancels fermion

- new gauge bosons W', Z' , mass $\sim \text{TeV}$



boson cancels boson

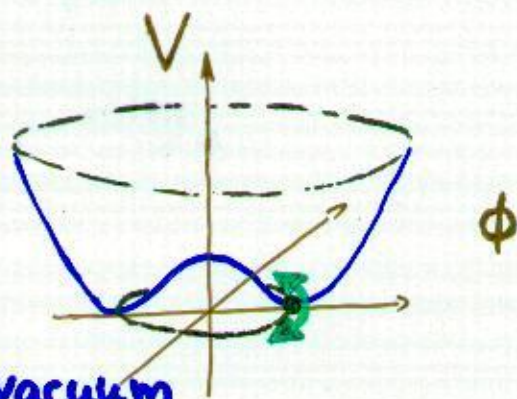
What symmetry relates
the coupling constants?

the little higgs is a
"pseudo-Nambu-Goldstone-
boson"

Higgs as a Nambu-Goldstone boson

Complex ϕ

Symmetry $\phi \rightarrow e^{i\alpha} \phi$



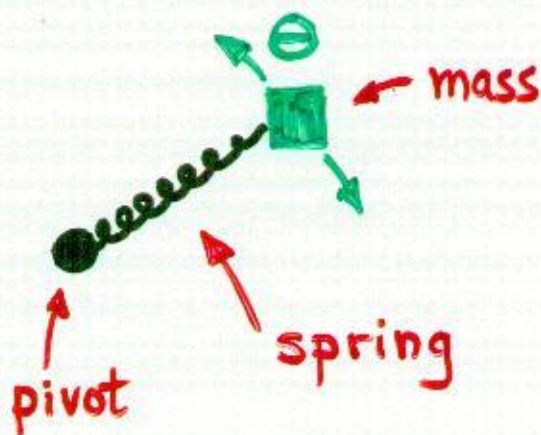
⇒ degenerate ground state - vacuum

⇒ massless excitations: "Nambu-Goldstone" fields

$$\phi(x) = r(x) e^{i\Theta(x)}$$

$\Theta(x)$ massless, but also

- no potential
- no couplings to top gauge field



Higgs as a NGB

* Spontaneously broken
global symmetry *

e.g. "simplest": $SU(3)/SU(2)$
Kaplan, Schmaltz

5 NGBs

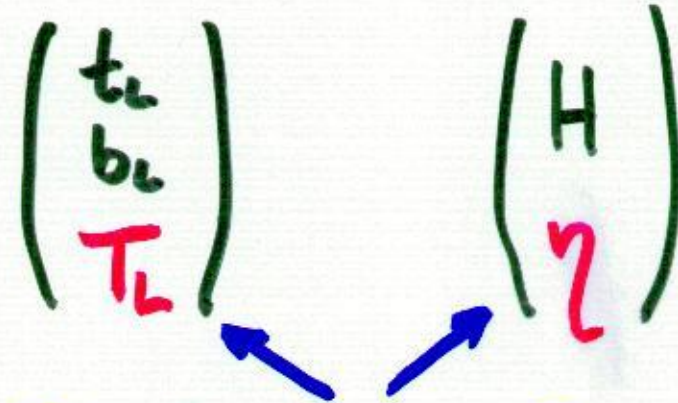
= H complex doublet
+ η real scalar

top Yukawa (1)

larger symmetry ($SU(2) \rightarrow SU(3)$)

$\Rightarrow$ larger representations

e.g. $\begin{pmatrix} t_L \\ b_L \\ T_L \end{pmatrix} \quad \begin{pmatrix} H \\ \eta \end{pmatrix}$



"L.H. partners"

TeV scale masses

top Yukawa (2)

* collective symmetry breaking 

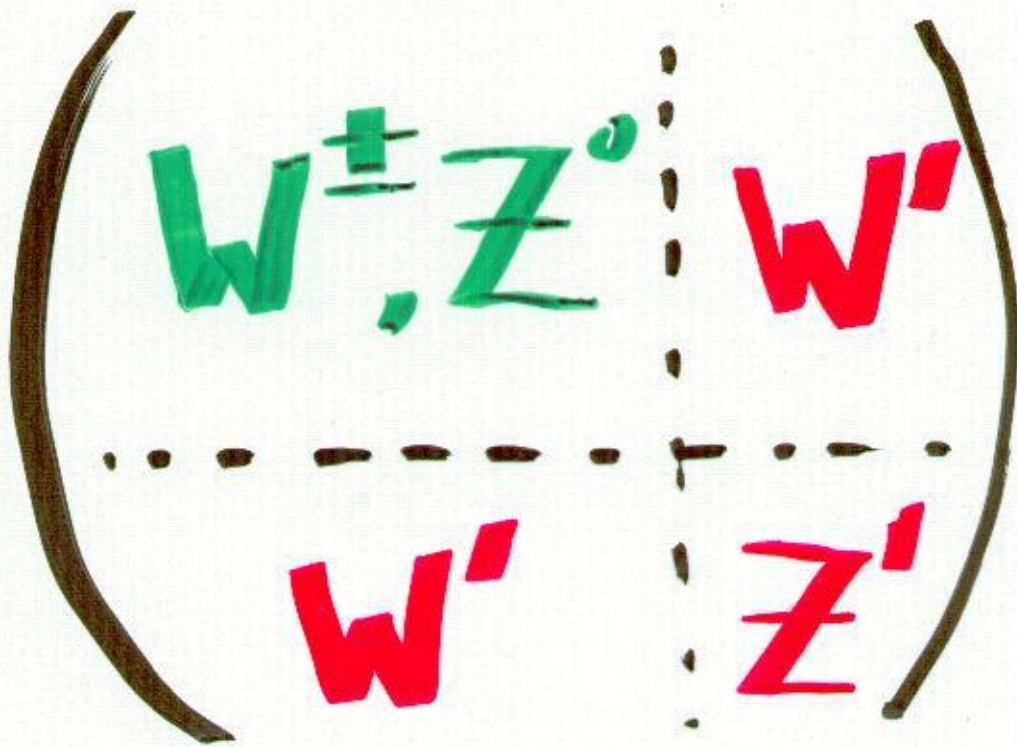
$$\lambda_t \begin{pmatrix} t_L \\ b_L \end{pmatrix} t_R H$$



$$\lambda_1 \begin{pmatrix} t_L \\ b_L \\ T_L \end{pmatrix} t_R^1 \begin{pmatrix} H \\ \gamma \end{pmatrix} + \lambda_2 \begin{pmatrix} t_L \\ b_L \\ T_L \end{pmatrix} t_R^2 \begin{pmatrix} -H \\ -\gamma \end{pmatrix}$$

note: $SU(3)$ symmetry relates t, T
couplings

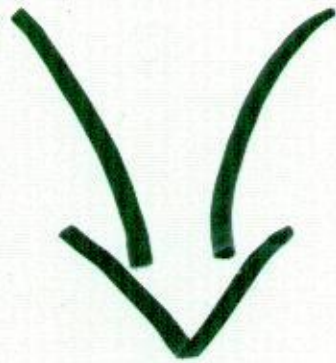
SU(2) gauge sector



W, Z "partners" with
TeV scale masses

General L.H. features

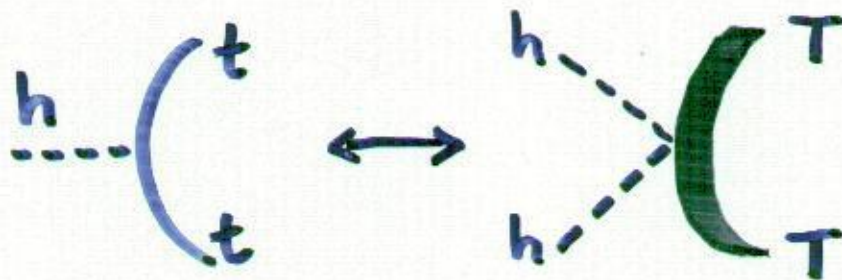
* new bosonic symmetry



1. "L.H. partners"

$T', W', Z', \eta \dots$

2. coupling relations



New predicted particles

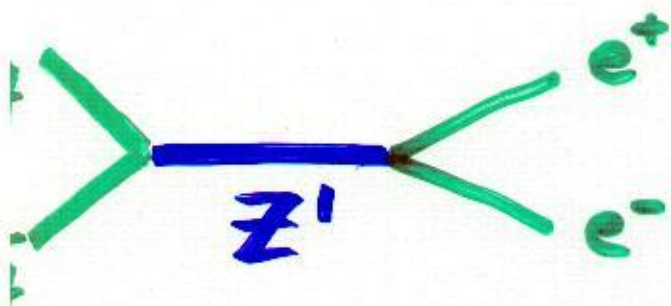
* top partner : T $m_T \sim 1-2 \text{ TeV}$

* gauge boson : W', Z' $m_{Z'} \sim 3-5 \text{ TeV}$
partners

* scalars : $\phi ?$ $m_\phi \sim ??$

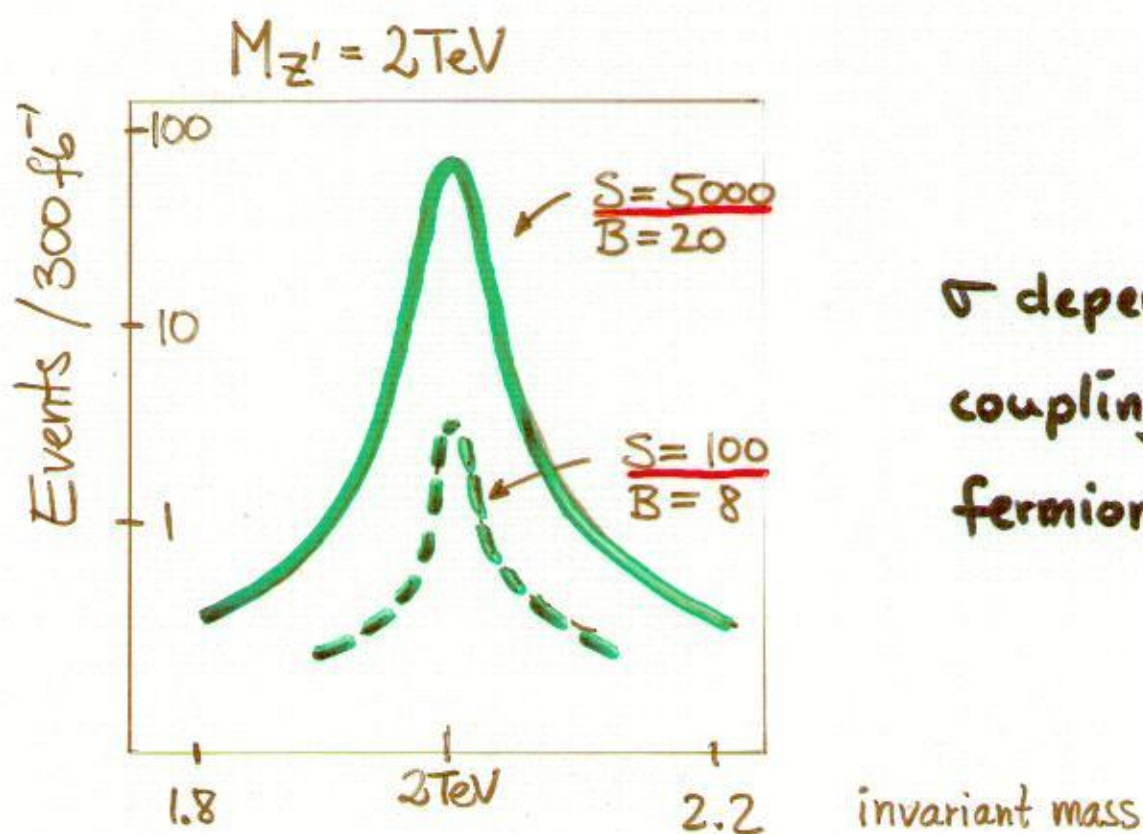
(lower bounds on masses from precision EW ,
upper bounds from Higgs naturalness)

Z' at the LHC (ATLAS)



2 isolated electrons

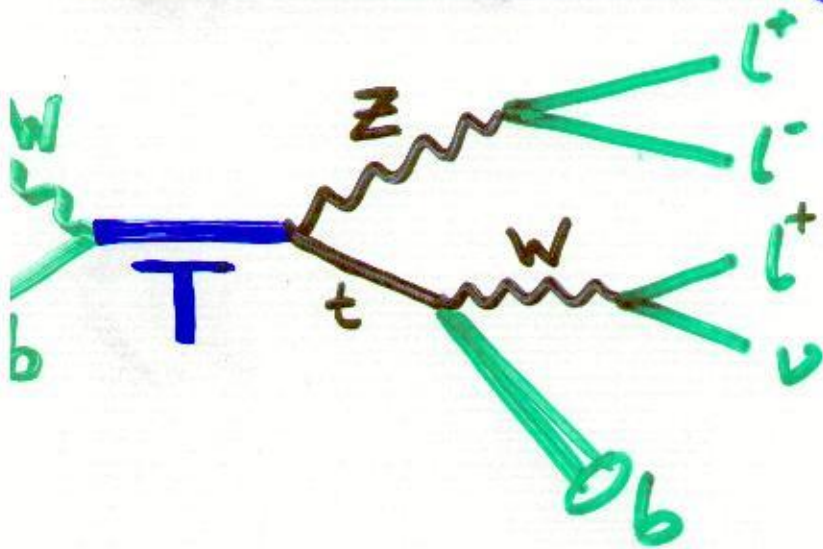
invariant mass > 800 GeV



σ depends on Z'
coupling to light
fermions

background: Drell-Yan $Z/\gamma \rightarrow e^+e^-$

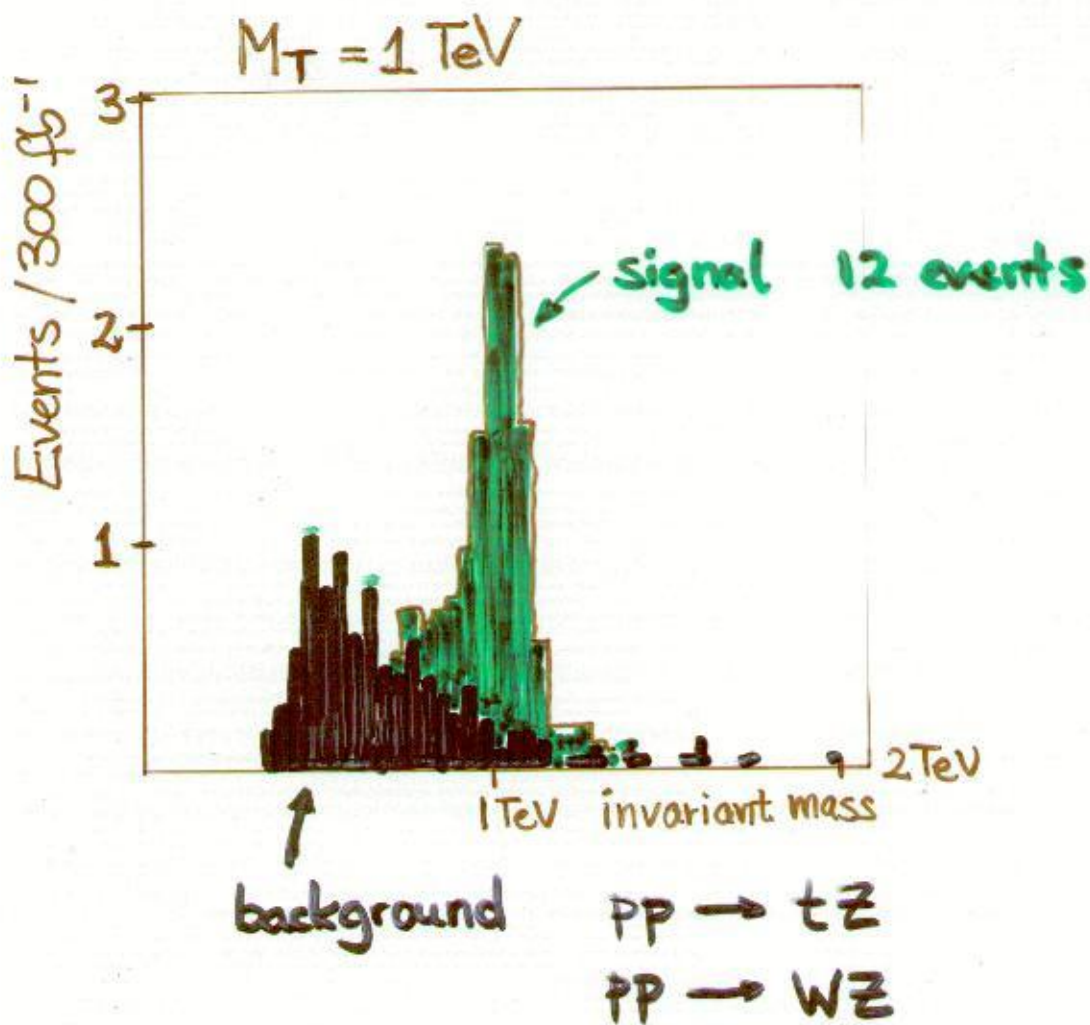
T at the LHC (ATLAS study)



3 isolated leptons

$E_T^{\text{miss}} (> 100 \text{ GeV})$

1 b jet



Precision EW constraints

Kribs et.al. - Gregoire et.al. - Marandella et.al.
Han-Skiba

• $Z-Z'$ mixing

$$g^2 \begin{pmatrix} f^2 & v^2 \\ v^2 & v^2 \end{pmatrix} \Rightarrow \delta m_Z^2 \approx \frac{v^4}{f^2}$$

(Note: Red arrows in the original image point from $m_{Z'}^2$ to the top-left and top-right elements of the matrix, and from m_Z^2 to the bottom-right element.)

• Z coupling modification

$$g \begin{array}{c} \nearrow Z' \\ \searrow Z \end{array} \Rightarrow \delta g \approx \frac{v^2}{f^2}$$

• four fermion operators

$$\begin{array}{c} \nearrow Z' \\ \searrow Z \end{array} \approx \frac{E^2}{f^2}$$

$$f \gtrsim \text{few TeV}$$

a conundrum ---

in Little Higgs

$$m_{\text{LH}} \gtrsim \text{few TeV}$$

in SUSY

$$m_{\text{SUSY}} \gtrsim \text{few 100 GeV}$$

--- from Precision EW

R-parity

all superpartners odd

LSP dark matter!

⇒ pair production

⇒ no tree level precision EW

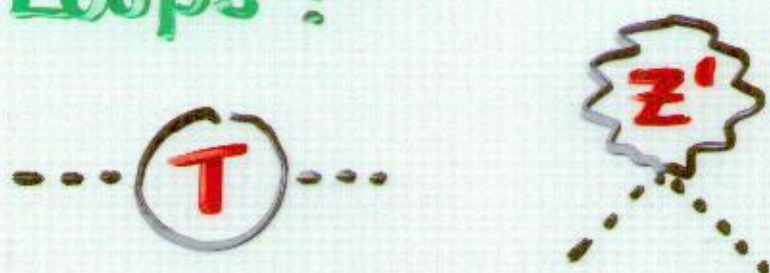


$$\Delta_{\text{PEW}} \sim \frac{1}{16\pi^2} \frac{m_Z^2}{m_{\text{SUSY}}^2}$$

T-parity

H.-C. Cheng, I. Low

Naturalness requires new states
in Loops!



Precision EW problems arise from
Trees!



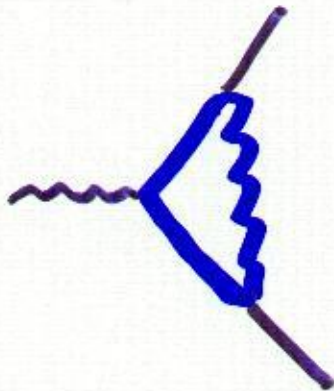
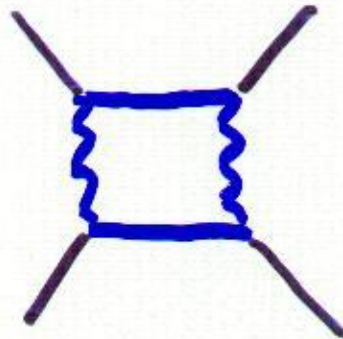
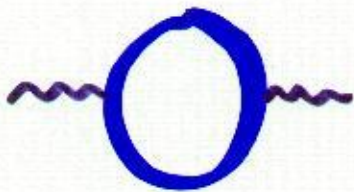
all new heavy states carry new
 Z_2 charge : T-parity

T parity precision EW

Hubisz, Meade, Noble, Perelstein
in "Littlest Higgs"

Cheng, Low

$$m_{hh} \gtrsim 500 \text{ GeV}$$



T parity pheno —

(Hubisz, Meade)
Littlest Higgs

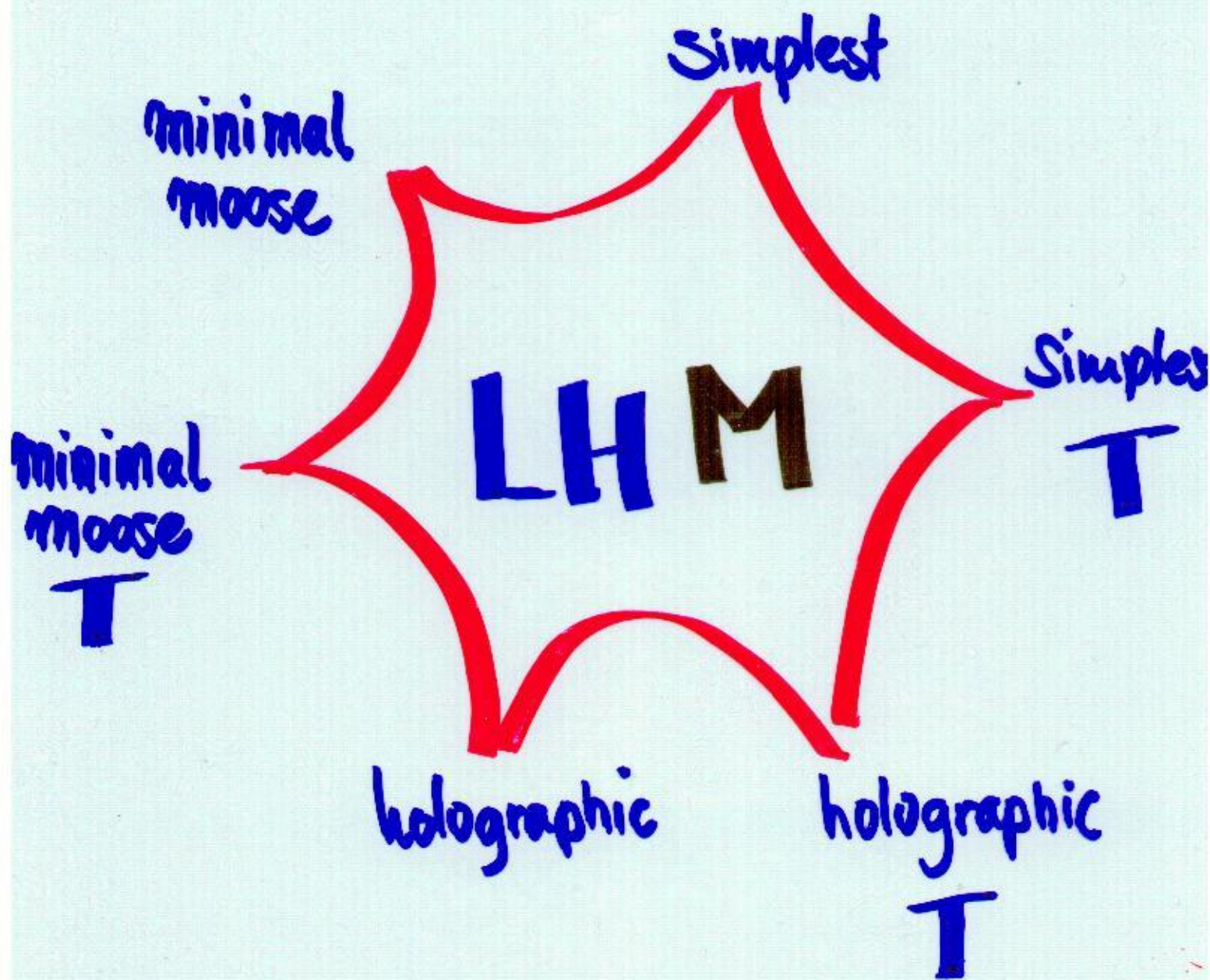
- pair produce new particles
(exception: T partner)
- cascade decays
- missing energy signals

Similar to SUSY !

» Can we measure spin of
"partners" at the LHC ?

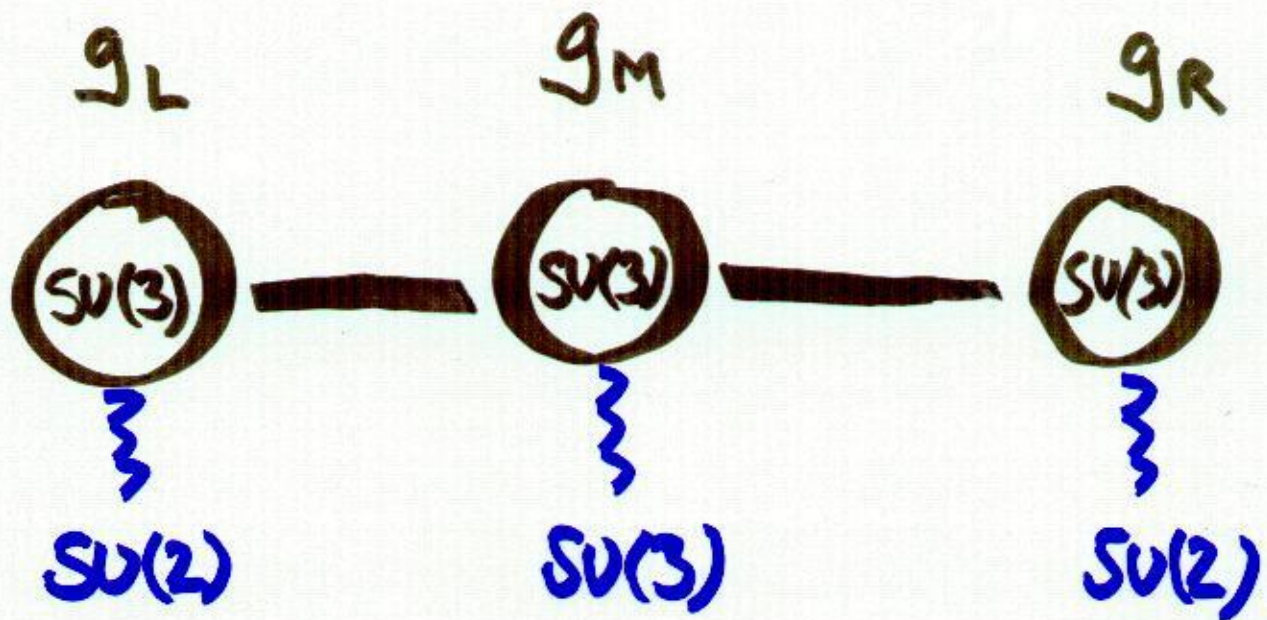
- LTP dark matter

Little Higgs - M-theory



LHM

- Thaler
- Cheng, Thaler, Wang



- $g_L = g_R \Rightarrow T$ parity
- $g_L, g_R \gg g_M \Rightarrow$ simplest
- $\ll \Rightarrow$ minimal moose

LHM

Cheng, Thaler, Wang
to appear

one Lagrangian

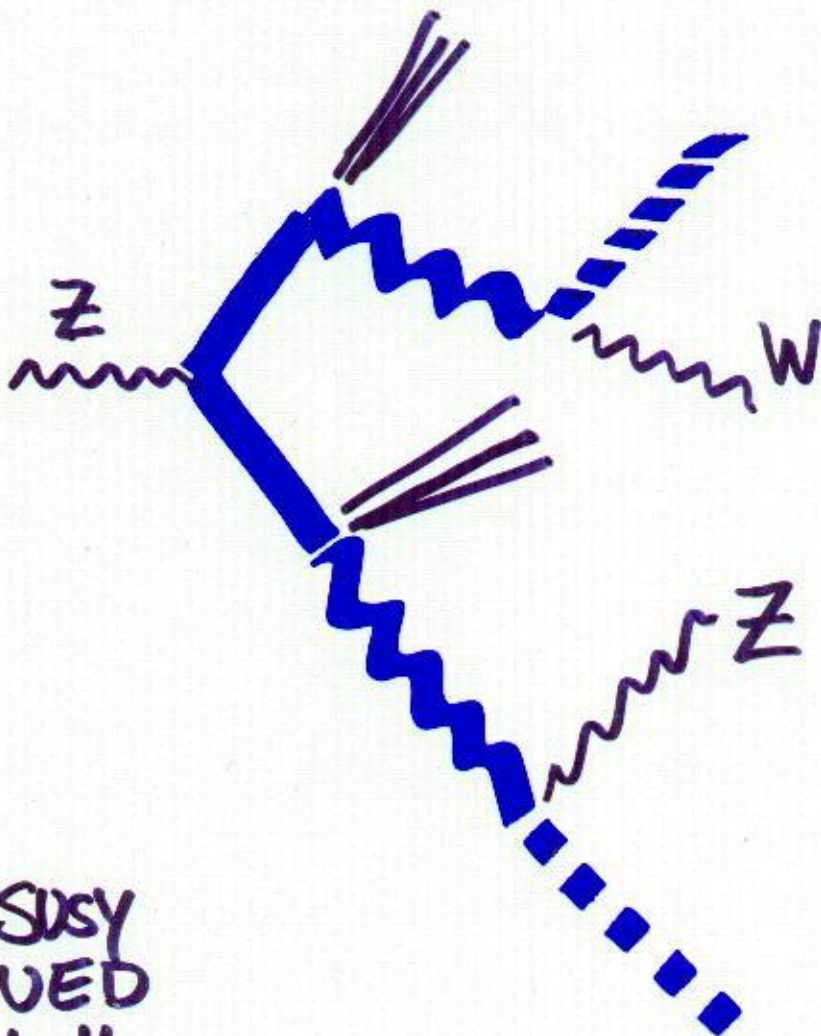
$\Leftrightarrow$ many little higgs model

great for unified L.H. study !

(like MSSM)

General lesson ?

- precision EW
 - weak scale dark matter
- } New particle
Parity



- pair product
- ~~E~~_t
- cascades

- SUSY
- UED
- L.H.
- ???

Summary

★ the SM works with a cut-off @ 1 TeV
but fine tuned for $\Lambda \gtrsim 2 \text{ TeV}$

$\Rightarrow$ predict

colored field $\lesssim 2 \text{ TeV}$

gauge partners $\lesssim 5 \text{ TeV}$

★ little Higgs = perturbative theory
with naturally canceling Λ^2
divergences, "collective"

★ precision EW implies $f \gtrsim \text{few TeV}$

or

T-parity

★ didn't talk about

... flavor

... UV completions

... other models