

# Measuring Mass and Cross Section Parameters at a Focus Point Region



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LCWS 2005



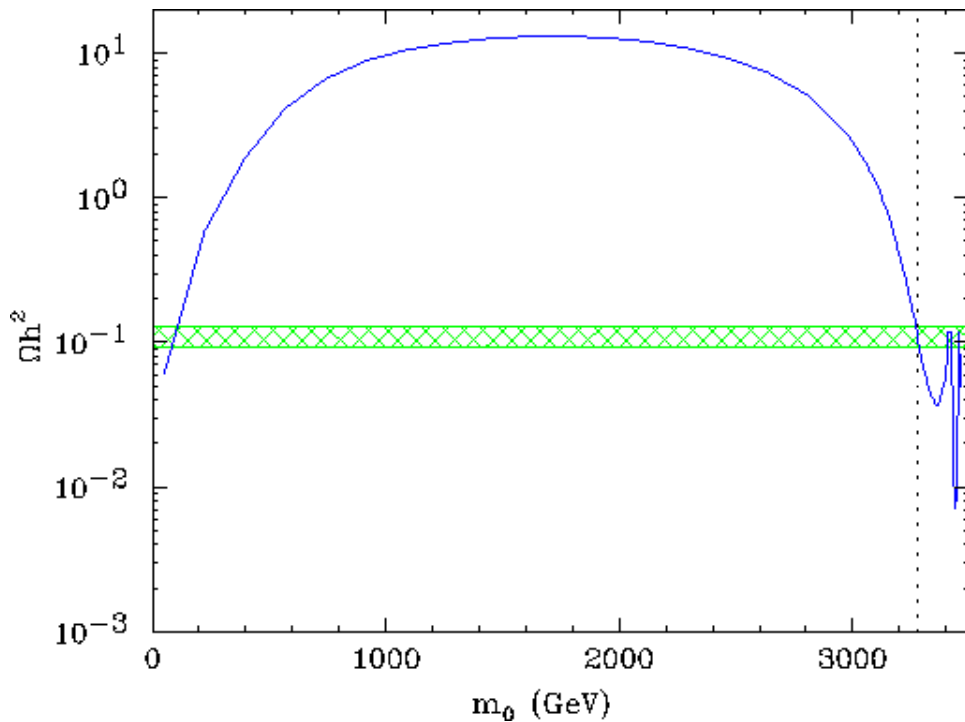
# Cornell LC Cosmology Group

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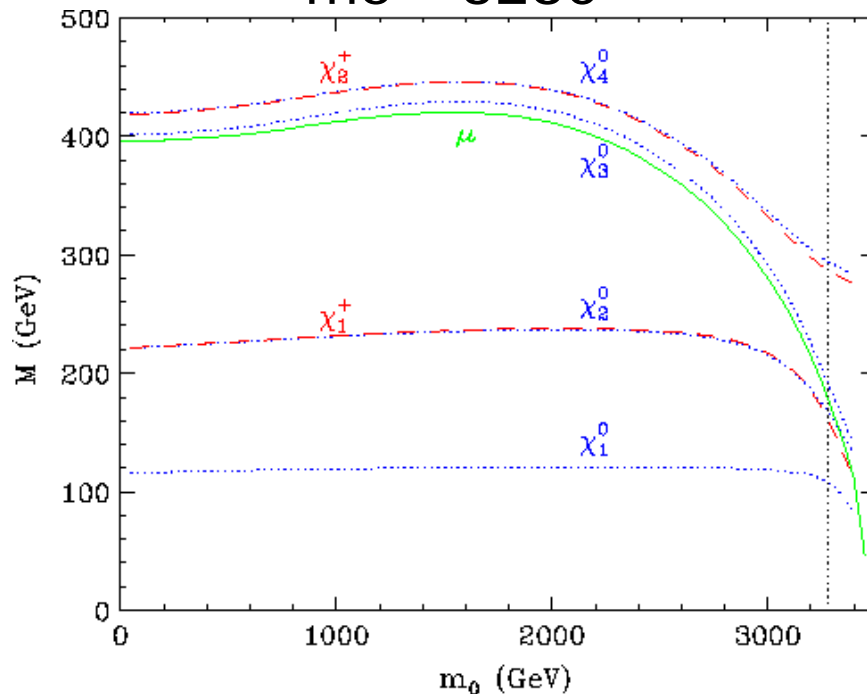
# Introduction



- SUSY models have good dark matter candidates.
- But WMAP  $\Omega_{\text{h}} h^2$  limits relic densities
- We will study an MSUGRA focus point that is consistent with WMAP

# Focus Point "LCC2"

$M_{1/2} = 300$ ,  $A_0 = 0$ ,  $\tan\beta = 10$ ,  
 $\mu > 0$ ,  $m_t = 175\text{GeV}$ ,  
 $m_0 = 3280$

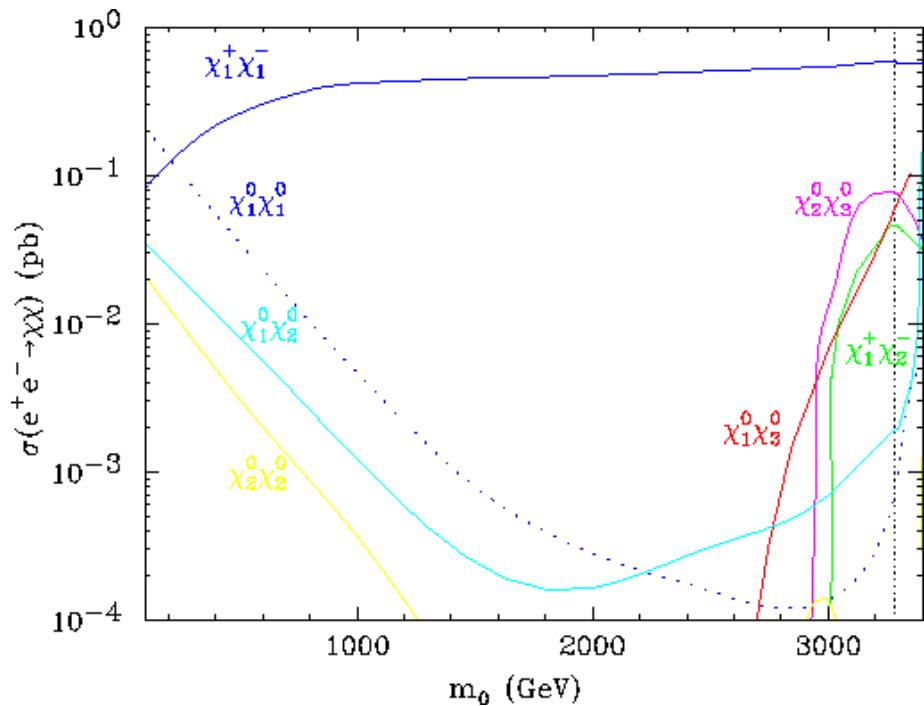


- Scalars are very heavy
- 2 Charginos ( $\chi_i^+$ )  
3 neutralinos ( $\chi_j^0$ )  
will be accessible at  $s^{1/2} = 500\text{GeV}$
- $\chi_1^0$  is the LSP and the Dark Matter Candidate

# Pair Production Cross Sections

We expect Signals from the following Neutralino/Chargino Pairs.

- $\chi_1^+ \chi_1^-$
- $\chi_1^+ \chi_2^-$
- $\chi_1^0 \chi_3^0$
- $\chi_2^0 \chi_3^0$





# Cross Sections and Masses

## Neutralino Mass Parameters (GeV)

- $\chi_1^0$  : -107.7
- $\chi_2^0$  : -166.3
- $\chi_3^0$  : +190.0
- $\chi_1^+$  : -159.4
- $\chi_2^-$  : -286.6

Pair	$\sigma_L$ (fb)	$\sigma_R$ (fb)
$\chi_1^+ \chi_1^-$	940	119
$\chi_1^+ \chi_2^-$	48.9	40.3
$\chi_1^0 \chi_3^0$	56.8	44.1
$\chi_2^0 \chi_3^0$	92.4	70.9



# SUSY Decay Signatures

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- $\chi_1^+ \chi_1^-$  :  $4J + E_{\text{miss}}, 2J + 1L + E_{\text{miss}}$
- $\chi_1^+ \chi_2^-$  :  $6J + E_{\text{miss}}, 4J + 2L + E_{\text{miss}}$
- $\chi_1^0 \chi_3^0$  :  $2J + E_{\text{miss}}, 2L + E_{\text{miss}}$
- $\chi_2^0 \chi_3^0$  :  $4J + E_{\text{miss}}, 4L + E_{\text{miss}}, 2L + 2J + E_{\text{miss}}$

Note that the number of jets could be increased by radiated gluons



# Analysis Goals

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- Determine expected uncertainties in cross section measurements.
- Determine uncertainties in measuring mass differences with di-lepton or di-jet invariant mass distributions
- Measure relative sign (phase) of mass parameters
- Determine mass of LSP using di-lepton or di-jet energy distributions





# Monte Carlo Samples

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## SUSY

- Generated at Cornell by Karl Ecklund
- Isajet 7.69
- Includes :  $\chi_1^+ \chi_1^-$ ,  $\chi_1^+ \chi_2^-$ ,  $\chi_1^0 \chi_3^0$ ,  $\chi_2^0 \chi_3^0$

## SM Backgrounds

- Generated at SLAC by Tim Barklow
- WHiZaRD 1.22
- Includes daughters from:  $e^+e^-$ ,  $e^-\gamma$ ,  $\gamma e^+$ ,  $\gamma\gamma$ ; such as  $t\bar{t}$ ,  $W^+W^-$ , Zpair

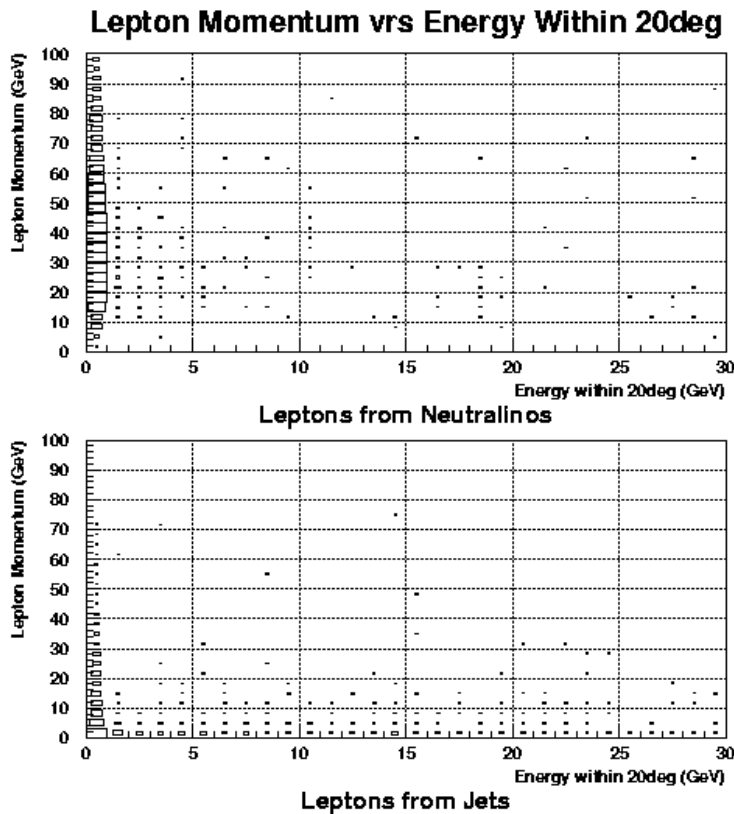


# Monte Carlo (cont)

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- Both SUSY and SM include Brems/Beamstrahlung (SUSY uses Isajet, SM uses CIRCE v1)
- Polarization: electron  $\pm 95\%$ , positron 0%
- Detector simulation done by LCD Root Fast MC, SD Mar01 (root based SLAC software)

# Analysis: Signal Lepton Selection for SUSY Signature



- We want Leptons that are isolated from jets.
- Lepton ID uses MC truth
  - $P_{\text{lepton}} > 10\text{GeV}$
  - $E_{20} < 2\text{ GeV}$ ; Total energy of other tracks and showers within  $20^\circ$  of lepton should be less than  $2\text{GeV}$



# Analysis: Jet Identification

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- $y_{\text{cut}}=0.004$
- $y_{ij}=2(\min(E_i, E_j))^2(1-\cos(\theta_{ij}))/E_{\text{cm}}^2$
- $y_{ij} < y_{\text{cut}}$  then jet-like
- Jet finding is done using the Durham Algorithm on all tracks, and unmatched showers, except for leptons identified as signal leptons

# MC Truth Jet Matching (Used in B-Tagging)

- Best match given by greatest  $Q_{ij}$
- $Q_{ij} = (2E_{iaj} - E_{inj} - E_{jni}) / (E_i + E_j)$
- $E_i$  = Energy in list I
- $E_{iaj}$  = Energy in list I and j
- $E_{inj}$  = Energy in list I but not J
- $Q_{ij} = 1$  Perfect match
- $Q_{ij} = -1$  completely different
- Not able to do honest B-tag with simulation, so jets found by Durham Algorithm are given best match with MC Truth table, then use expected b-tag efficiency (~50%).



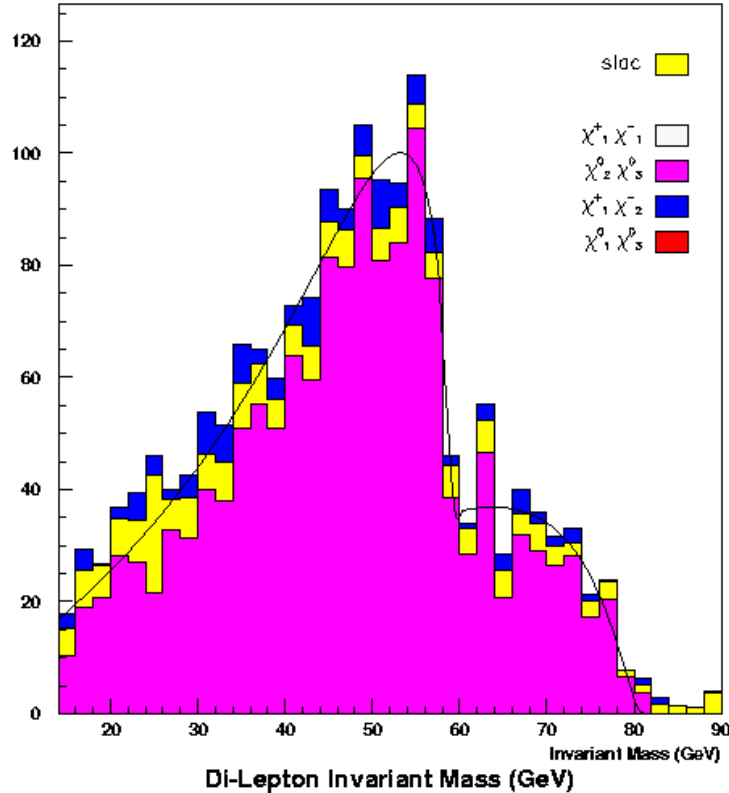
# Event Selection: $\chi_2^0\chi_3^0 \rightarrow 2J2L\chi_1^0$

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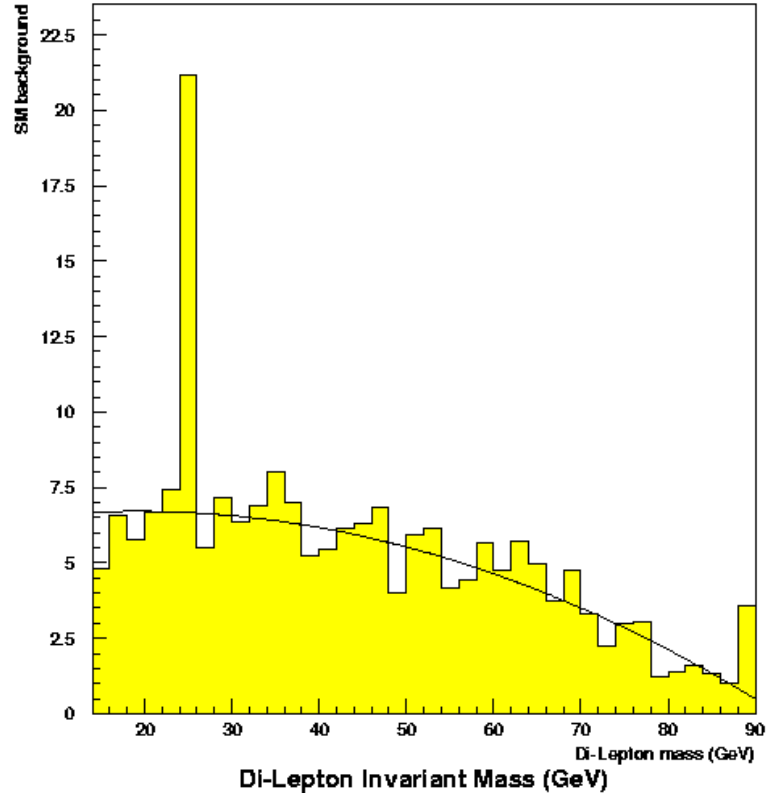
- 2 Isolated Leptons, opposite charge, same flavor
- 2 or 3 jets found. (allows for a gluon jet)
- $E_{\text{miss}} > 275 \text{ GeV}$
- $P_T > 10 \text{ GeV}$
- $|\cos(\theta)| < 0.95$  (all jets and leptons)
- $E(j \text{ or } L) < 110\text{GeV}$
- Anti-Btag to remove  $t\bar{t}$  backgrounds.

# 2or3J2L Di-Lepton Invariant Mass Distribution

2J2L, Di-Lepton Invariant Mass, With Cuts, 500fb<sup>-1</sup>



2J2L, Di-Lepton Mass, SM Backgrounds, 500fb<sup>-1</sup>





# Analysis of Mass Distribution

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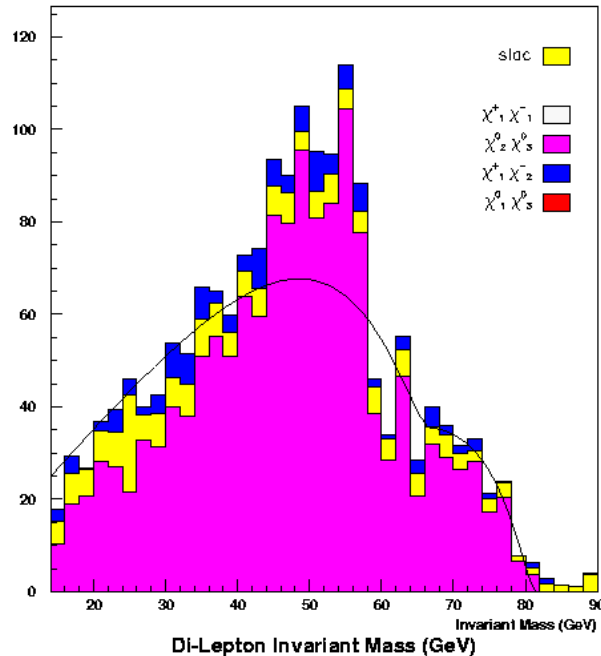
- Small Background
- Mass edges expected at 58.6GeV and 82.3GeV. Visible!
- We have a functional form for the distribution (A. Birkedal)
- The distribution is insensitive to LSP mass
- Expected Cross section uncertainty on  $\sigma_L$  and  $\sigma_R$  are each  $\sim \pm 2.6\text{fb}$  (2.8%, 3.6%)
- Log Likelihood Fit to edges yields:  
 $\Delta m_{21} = 58.7\text{GeV} +0.2\text{GeV} -0.1\text{GeV}$   
 $\Delta m_{31} = 82.0\text{GeV} +0.4\text{GeV} -0.1\text{GeV}$
- We can also determine relative sign of mass parameters for  $\chi_1^0$   $\chi_2^0$   $\chi_3^0$



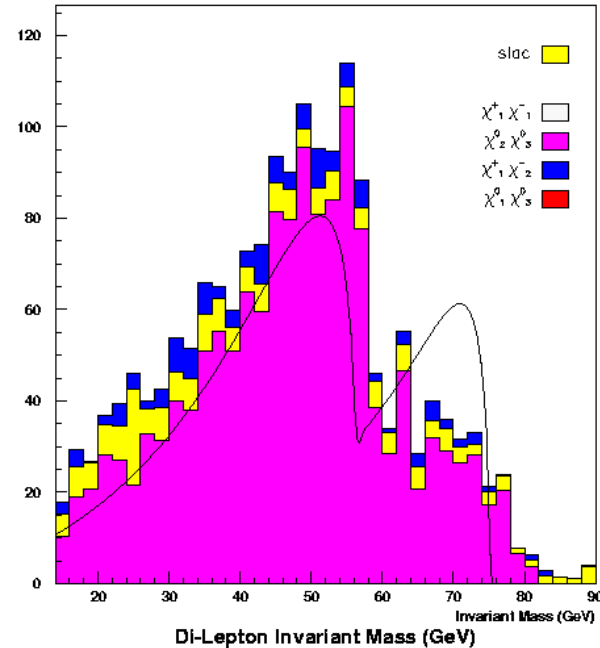
# Determine Relative Sign of

$$m_{\chi_{10}}, m_{\chi_{20}}, m_{\chi_{30}}$$

2J2L, Both Opposite Sign



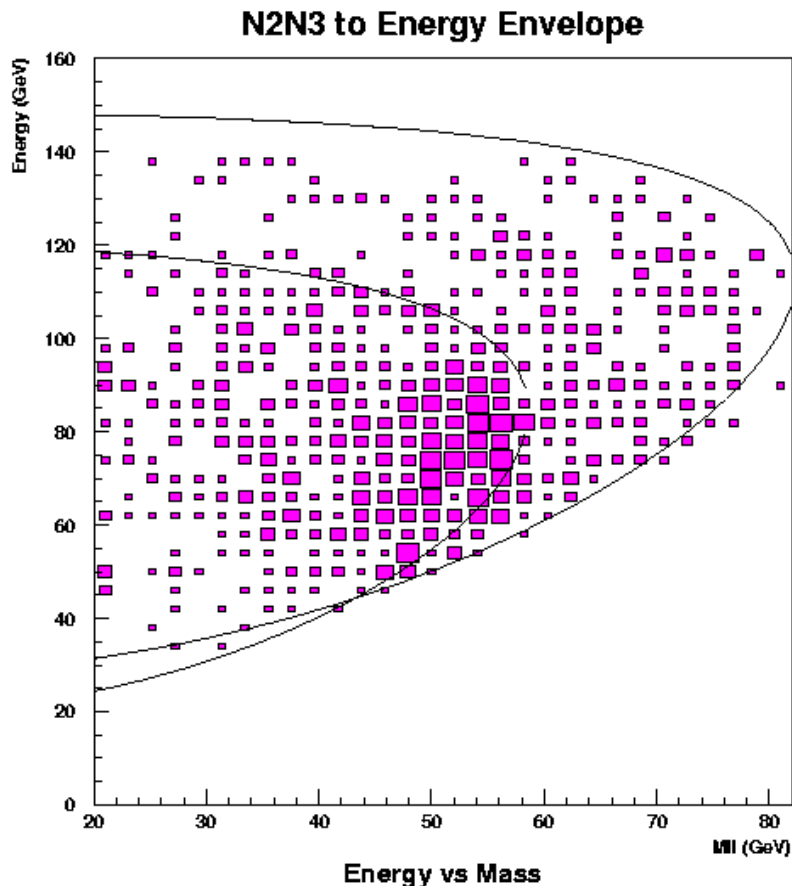
2J2L, Both Same Sign



$$\log[\text{like}(+m_{20}, -m_{30})] - \log[\text{like}(-m_{20}, -m_{30})] = 228 \quad \text{equivalent to } 21\sigma$$

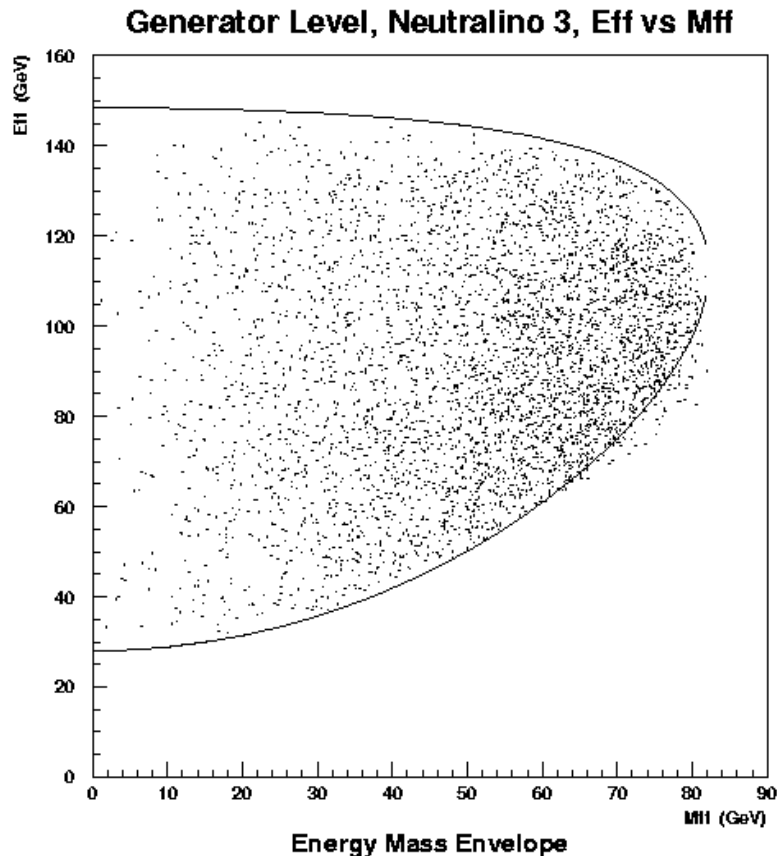
$$\log[\text{like}(+m_{20}, -m_{30})] - \log[\text{like}(+m_{20}, +m_{30})] = 84.7 \quad \text{equivalent to } 13\sigma$$

# LSP Mass from E(LL) Distribution

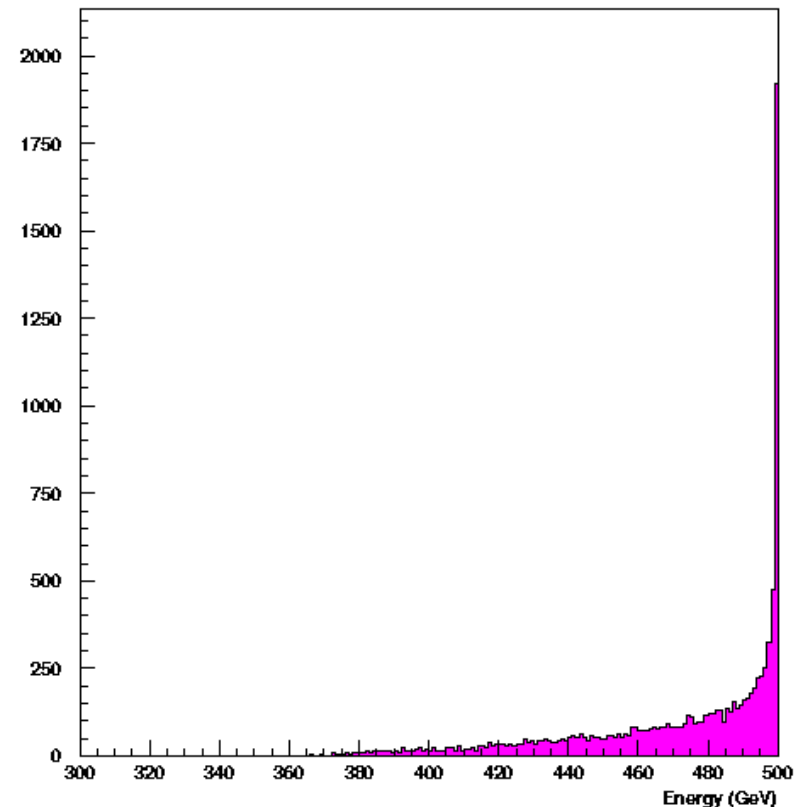


- LSP mass sets boundaries in dilepton energy vs. mass.
- Because of low stats near boundary, will fit to 1-D energy histogram.

# Beam/Breamstrahlung distorts Energy Envelope

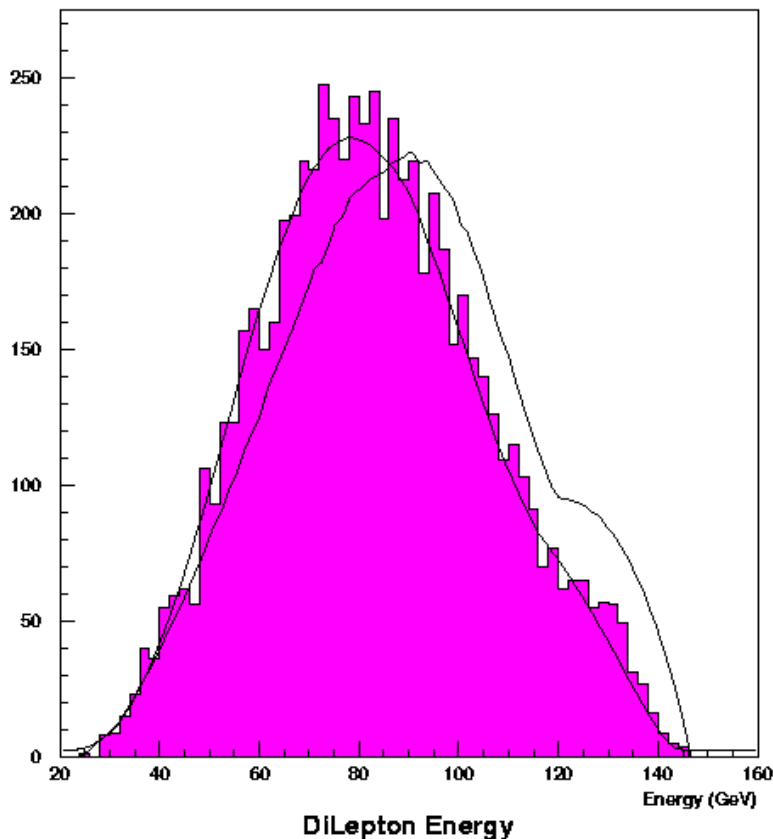


**Total CM Beam Energy Distribution After ISR**



# Energy Distribution Numerically Calculated

Generator Level DiLepton Energy Distribution

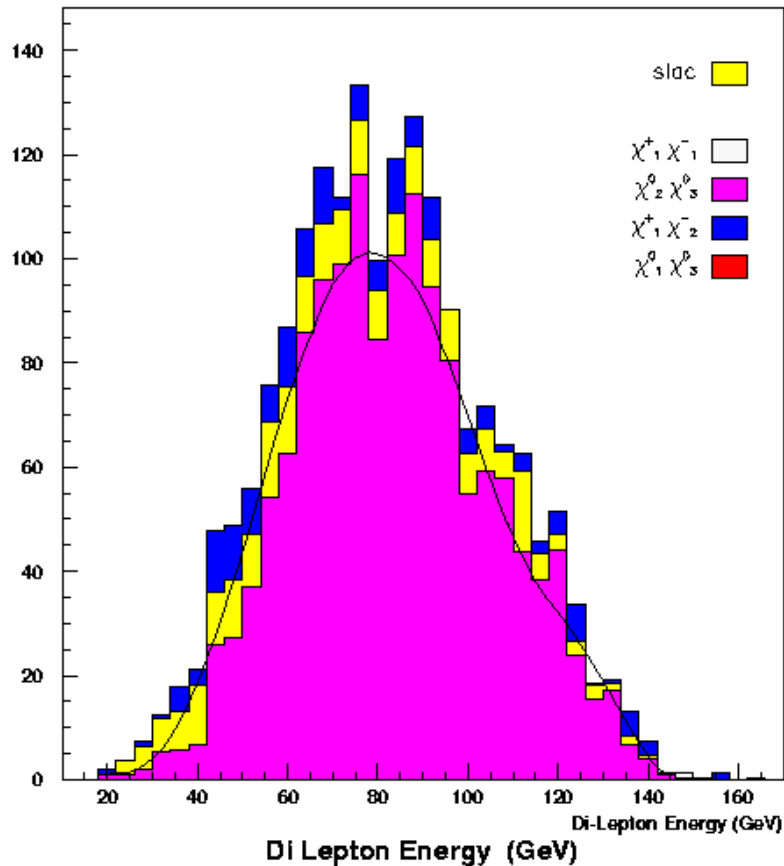


Numerically Integrate

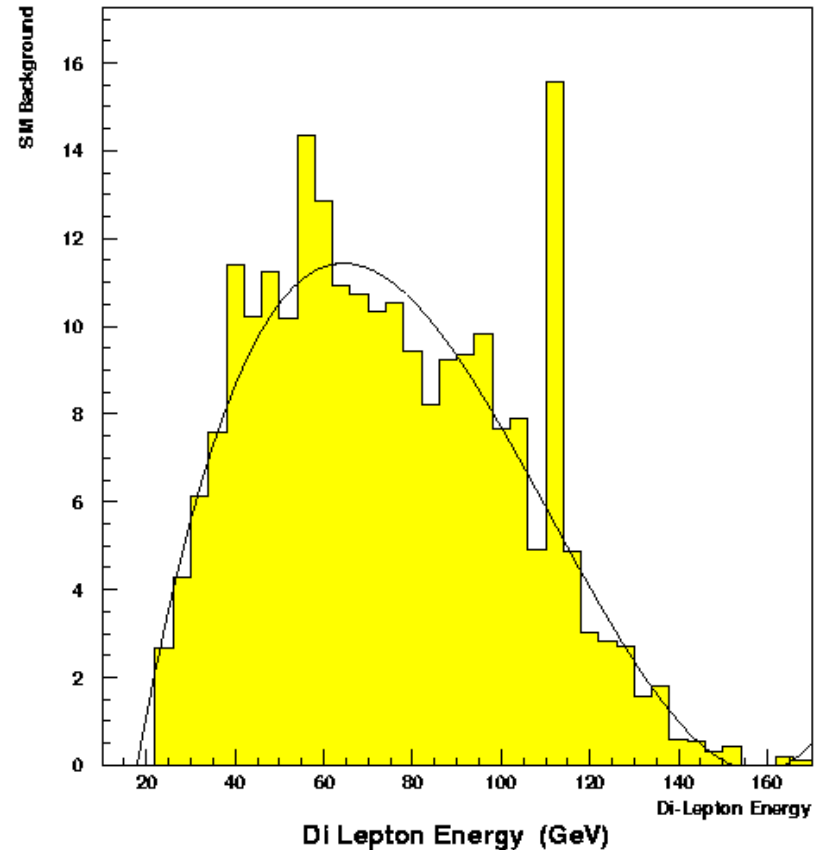
- Isajet ISR spectrum,
- Invariant mass distribution
- Isajet angular distribution (phase space)

# E(LL) Distribution

2J2L, Di-Lepton Energy, After cuts, 500fb<sup>-1</sup>



2J2L, Di-Lepton Energy, Backgrounds, 500fb<sup>-1</sup>





# Log Likelihood Fit to E(LL)

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- Using edges determined in mass analysis, results of Log Likelihood fit give:

107.5GeV +0.5GeV -1.1 GeV

(true answer 107.7GeV)

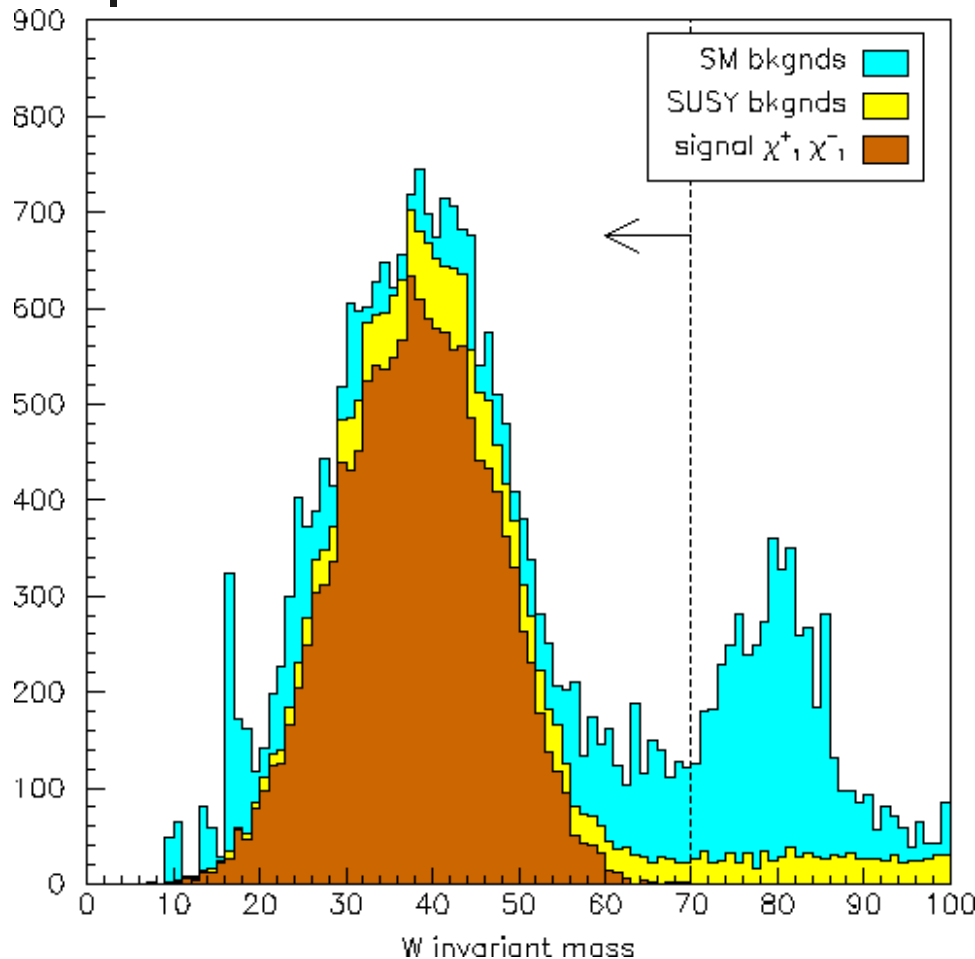


# Other Modes at Cornell

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- $e^+e^- \rightarrow \chi_1^+\chi_1^- \rightarrow jjl + E_{\text{miss}}$  by Jim Pivarski
- $e^+e^- \rightarrow \chi_1^0\chi_3^0; \chi_2^0\chi_3^0 \rightarrow jj + E_{\text{miss}}$  by Laura Fields
- $e^+e^- \rightarrow \chi_1^+\chi_2^- \rightarrow 6j + E_{\text{miss}}; 4j + 2L + E_{\text{miss}}$  by Dan Hertz

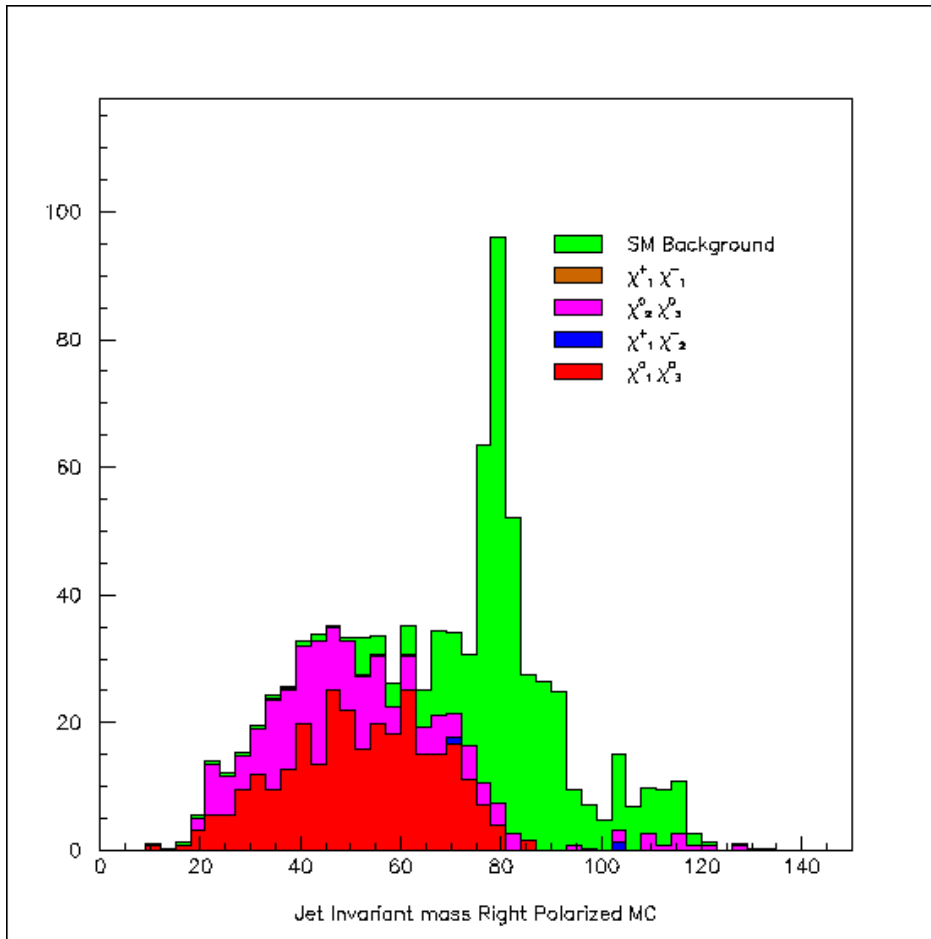
$$e^+e^- \rightarrow \chi_1^+ \chi_1^- \rightarrow jjl + E_{\text{miss}}$$



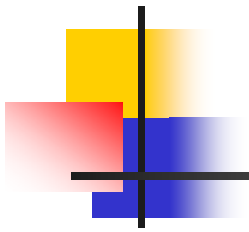
- Study by Jim Pivarski
- will determine cross section uncertainty.
- Mass difference measurement should be possible
- Should give a second measure of  $M_{\text{LSP}}$



$$e^+e^- \rightarrow \chi_1^0 \chi_3^0; \chi_2^0 \chi_3^0 \rightarrow jj + E_{\text{miss}}$$



- By Laura Fields
- W peak near edge, so no mass measurement
- Cross section of  $\chi_1^0 \chi_3^0$  depends on  $\chi_2^0 \chi_3^0$ .
- $\chi_1^0 \chi_3^0$  :  $\delta\sigma_L \sim 5\text{fb}^{-1}$   
 $\delta\sigma_R \sim 4\text{fb}^{-1}$  , or 9%


$$e^+e^- \rightarrow \chi_1^+ \chi_2^- \rightarrow 6j + E_{\text{miss}};$$
$$4j + 2L + E_{\text{miss}}$$

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- By Dan Hertz
- Very Preliminary
- Mode has on shell W and Z emitted during chargino decay.
- There will be too few events for mass edges to be determined. But backgrounds should be small.
- Work to determine uncertainty in cross section measurement in progress.



# Conclusions

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- Mass differences of  $\chi_2^0$  and  $\chi_3^0$  with LSP mass can be measured with uncertainties  $<0.5\text{GeV}$ .
- Mass of LSP can be determined with 2J2L, E(LL) distribution with uncertainty  $\sim 1\text{GeV}$ .
- Cross sections of  $\chi_2^0\chi_3^0$  can be determined with uncertainty  $\sim 2.6\text{fb}$  ( $\sigma_L$  2.8%, and  $\sigma_R$  to 3.6% )
- Cross sections of  $\chi_1^0\chi_3^0$  can be determined with  $\sim 9\%$  uncertainty (L. Fields).



# Current and Future Tasks

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- Complete  $\chi_1^+\chi_1^-$  analysis for cross section,  $\chi_1^+$  mass difference, and second LSP mass measure (J. Pivarski)
- Complete  $\chi_1^+\chi_2^-$  analysis for cross section (D. Hertz)
- Convert these uncertainties into uncertainties in MSUGRA parameters ( $M_1, M_2, \mu, \tan\beta$ ), and ultimately  $\Omega_{\text{DM}}h^2$  (A. Birkedal, K. Matchev)



# Special Thanks

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- T. Barklow for generating our SM backgrounds.