## Study of the Higgs-Bosons parity at the ILC

## Content:

- CP-sensitive observable
- Detector simulation
- Selection from SM background
- Status of the study
- Conclusion / outlook


## Higgs-parity JPC $=0$ ??

- CP-even SM-like Higgs or CP-odd like e.g. $\mathrm{A}^{0}$ in 2HDM?
- $\mathrm{h} \tau \tau$ - coupling transmits Higgs-parity into spin-polarisation of the $\tau$ 's

- For $\tau$-decays into 2 or 3 pions via $\rho$ - or $a_{1}$ - resonances


$$
\frac{\left.\Gamma_{\left(\tau^{+}\right.} \xrightarrow[\longrightarrow]{\rho} \pi^{+} \pi^{0} v\right)}{\Gamma_{\text {total }}} \approx 25 \%
$$

$$
\frac{\left.\Gamma_{\left(\tau^{+} \xrightarrow{a}\right.} \pi^{+} \pi^{+} \pi^{-} v\right)}{\Gamma_{\text {total }}} \approx 10 \%
$$

- Reconstruction of the $\tau$-polarisation from the final-states
- Reconstruction of the correlation of the transverse spin-components $\tau$ decays simulated with Tauola/Photos


## The observable

- Planes spanned by the 4-momenta of the pions

- Correlation sensitive to Higgs-parity :


## the acoplanarity $\Phi$.

- Use energies to distinguish between $\Phi$ and $\Phi$ ' by the sign of $\mathrm{y}_{1} \cdot \mathrm{y}_{2}$

$$
y_{1}=\frac{E_{\pi^{+}}-E_{\pi^{0}}}{E_{\pi^{+}}+E_{\pi^{0}}} \quad y_{2}=\frac{E_{\pi^{-}}-E_{\pi^{0}}}{E_{\pi^{-}}+E_{\pi^{0}}}
$$

$\rightarrow$ only direct accessible information from reconstructed momenta used.
THUS: precise reconstruction of the 4-momenta both for neutral (e.g. the photons from the $\pi^{0}$ ) and charged objects is essential.
$\rightarrow$ Challenge to the performance of a high precision detector, especially to the calorimeter.

## Theoretical distributions



Thus:

- $\mathrm{N}_{\text {signal }}$ according to expected $\sigma_{\mathrm{i}}$ and $\Gamma_{\mathrm{i}}$
- SM-background: $\mathrm{O}\left(10^{8}\right)$ evt / $1 \mathrm{ab}^{-1}$
- include detector-effects like expected precisions on 4-momenta reconstruction
$\rightarrow$ usage of the fast/ parameterized detector simulation SIMDET (based on the TESLA-design)


## But:

- generator-level / no detector effects
- pure signal / no backgrounds
- scaled from very high statistics


## Quality of the fast simulation (especially calorimeter)

- Precision of the position- and energy-reconstruction for photons
- Resolvability of objects close to each other
- Problem: calorimeter description too much simplified for very specific tasks


Comparison with the GEANT3-based full simulation BRAHMS shows large differences:

- artefacts in the position-resolution
- too high separability for close-by photons
$\rightarrow$ for such exclusive reconstructions: modifications for the fast simulation are necessary.


## GEANT 3 studies

Main question: detector response for $\mathrm{E}_{\text {neutral }}$ in the ECAL (e.g. $\gamma$ from $\pi^{0}$ ):

- precision of the reconstruction of
- the particle energy
- the position and thus the direction of the momentum
- separability of energy-depositions close to each other
- neutral close to an other neutral
- neutral close to a charged energy-deposition
$\rightarrow$ Study of this parameters with GEANT 3 for a signal channel to build a post processing routine: $\mathrm{HZ} \rightarrow \tau^{+} \tau^{-} \nu \nu$ with $\tau^{ \pm} \rightarrow \rho^{ \pm} \nu \rightarrow \pi^{ \pm} \pi^{0} \nu$

Resulting parameterizations:
a) energy resolution for the ECAL: $\sigma=\frac{12 \%}{\sqrt{E}}$

## b) Position resolution

Distance at the calorimeter surface (generator-level to closest reconstructed)

## Fit function:

$f(x)=a \cdot x \cdot \exp \left(-b \cdot x^{2}\right), b=\frac{1}{2 \cdot \sigma^{2}}$
(1D projection of 2D-Gaussian)




Resulting resolutions:

$$
\begin{aligned}
& \sigma=5.5 \mathrm{~mm} \text { for } E \leq 0.25 \mathrm{GeV} \\
& \sigma=0.8 \mathrm{~mm} \text { for } E \geq 25 \mathrm{GeV}
\end{aligned}
$$

## c) Resolvability of 2 photons

Distribution fitted and then scaled to:
$\mathrm{P}_{\text {resolve }}=0$ for $\Delta<2 \mathrm{~cm}$
$(\sim 2 \cdot$ Moliere radius $)$
$P_{\text {resolve }}=1 \mathrm{for} \Delta>14.5 \mathrm{~cm}$ (photons treated as isolated)


## d) Resolvability $\gamma \leftrightarrow \pi^{ \pm}$

Plateau at $\Delta=11.5 \mathrm{~cm}$ reached
$\rightarrow$ Fit scaled to:


## Comparison of old and new detector-output




## Back to the main task

Find and reconstruct the useful $\mathrm{H} \rightarrow \tau \tau$ events.


Example: Higgsstrahlung-process at $\sqrt{s}=350 \mathrm{GeV}$ and $m_{H}=120 \mathrm{GeV}$

$$
\begin{aligned}
& \sigma\left(e^{+} e^{-} \rightarrow Z^{0} H^{0}\right)=0.148 p b \quad \frac{\Gamma_{\left(H^{0} \rightarrow \tau^{+} \tau^{-}\right)}}{\Gamma_{\text {total }}}=9.2 \% \\
& \frac{\Gamma\left(\tau^{+} \xrightarrow{\rho} \pi^{+} \pi^{0} v\right)}{\Gamma_{\text {total }}} \approx 25 \% \quad \frac{\left.\Gamma_{\left(\tau^{+}\right.} \xrightarrow{a} \pi^{+} \pi^{+} \pi^{-} v\right)}{\Gamma_{\text {total }}} \approx 10 \%
\end{aligned}
$$

Expected number of events per $1 \mathrm{ab}^{-1}: 1616$

|  | $\mathbf{Z} \rightarrow \mathbf{X}$ | $\rightarrow \nu \nu$ | $\rightarrow \mathbf{e}^{+} \mathbf{e}^{-} / \mu^{+} \mu^{-}$ | $\rightarrow \mathbf{q q}$ |
| :---: | :---: | :---: | :---: | :---: |
| $\rho \rho$ | 832 | 166 | 56 | 582 |
| $\mathrm{a}_{1} \rho$ | 655 | 131 | 44 | 458 |
| $\mathrm{a}_{1} \mathrm{a}_{1}$ | 129 | 26 | 9 | 90 |
| SUM | 1616 | 323 | 109 | 1130 |

## Simulated signal-topology



## SM-background considered

| $\mathbf{e}^{+} \mathbf{e}^{-} \rightarrow$ | final-state | $\sigma$ (ab) |
| :---: | :---: | :---: |
| $\begin{gathered} Z^{0} Z^{0} \\ \left(\gamma^{*}\left\|Z^{0} \gamma^{*}\right\| Z^{0}\right) \end{gathered}$ | 41 | 0.7 *105 |
|  | 4 q | 4.8 *105 |
|  | 1 qq | 4.4 *105 |
| $\mathbf{W}^{+} \mathbf{W}$ | Iv lv | 1.4 * $10^{6}$ |
|  | qq lv | 5.9 * $10^{6}$ |
|  | 4 q | 6.1 * $10^{6}$ |
| $\gamma / Z^{0}$ | all visible | 35.0 * $10^{6}$ |
| $\mathbf{e}_{\mathbf{i}} \gamma \rightarrow \mathbf{e i}_{\mathbf{i}} \gamma^{*} / \mathbb{Z}^{0}$ | qq | 13.3 * $10^{6}$ |
|  | II (visible) | 5.7 * $10^{6}$ |
| $\mathbf{e}_{\mathbf{i}} \gamma \rightarrow \mathbf{f}_{\mathbf{j}} \mathbf{W}^{ \pm}$ | qq | 2.5 * $10^{6}$ |
|  | 1 v | 1.2 * $10^{6}$ |
| HZ $\rightarrow$ X | non-signal | $1.4 * 10^{5}$ |

## All together:

~ 7.4 * $10^{7}$ events

+ 2 photon background

Spin correlation for SMbackground not taken into account. Assumption: well understood (specially for ZZ)

Event generation with PYTHIA (no full 4-f generator used)

Full interference $\gamma^{*} / Z^{0}$ taken into account

All $\tau$ decayed via
Tauola/Photos

## $\tau$-identification

Typically low multiplicity, isolated jets

Thus: Cone-based lepton identification
(based on algorithm by B. Sobloher)

- 1 or 3 tracks
- cone half-angle: $9.5^{\circ}$
- $\mathrm{E}_{\text {seed, min }}>0.7 \mathrm{GeV}$
- $\mathrm{E}_{\text {sum, } \mathrm{cone}, \min }>5 \mathrm{GeV}$
- $\cos \theta_{\text {beam axis }}>9.5^{\circ}$
- isolation to other tracks with half-angle: $12.5^{\circ}$


## Preselection

- $21 \mathrm{GeV}<\mathrm{m}_{\text {visible }}<355 \mathrm{GeV}$
- event multiplicity: $\leq 80$ reconstructed eflow-objects
- $\cos \theta_{\text {event momentum }} \mid \leq 0.995$
- $\geq 1$ pair of hadronic $\tau$-candidates from the lepton ID, with
- angle between the candidates: $75^{\circ}<\alpha<175^{\circ}$
- $21 \mathrm{GeV}<\mathrm{m}_{\tau \tau}<120 \mathrm{GeV}\left(\mathrm{m}_{\mathrm{H}}=120 \mathrm{GeV}\right)$
$\rightarrow$ Effective reduction of backgrounds with very different topology:

$$
\begin{aligned}
\mathrm{e}^{\mathrm{i}} \gamma \rightarrow \mathrm{e}_{\mathrm{i}} \gamma^{*} / \mathrm{Z}^{0} & \rightarrow \mathrm{e}_{\mathrm{i}} \text { qq from } 13.3^{* 1} 0^{6} \text { to } 5218(\sim 0.04 \%) \\
& \rightarrow \mathrm{e}_{\mathrm{i}} \text { II from } 5.7^{* 1} 10^{6} \text { to } 21659(\sim 0.38 \%) \\
\mathrm{e}^{+} \mathrm{e}^{-} \rightarrow \mathrm{Z}^{0} \mathrm{Z}^{0} \rightarrow & \rightarrow \tau \text { qq to } 15006(\sim 25 \%)
\end{aligned}
$$

Keeping the signal-efficiency above 84.5 \% in all signal-channels.

## Selection for $\tau \tau$ qq final states

## Consists of 4 main steps:

1. event shape
2. $\tau$ candidates
3. hadronic Z-decay
4. kinematical fit to the HZ system


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LCWS 2005



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## Kinematic Fit

- $Z \rightarrow q q$ system forced into 2 jets
- soft cut on $\mathrm{y}_{12}$
- Input into the fit:
- 4-momenta of the hadronic jets
- 3-momenta of the $\tau$-candidates, used only as directions
- Constraints:
- invariant mass of the $Z^{0}$ system $=M_{Z}=91.19 \mathrm{GeV}$
- momentum conservation $\Sigma p_{x}=\Sigma p_{y}=\Sigma p_{z}=0$
- energy conservation $\Sigma \mathrm{E}=350 \mathrm{GeV}$
- Only fits with $\chi^{2}<25$ (with 7 d.o.f) are accepted


## Results of the fit




Rejecting (almost) all backgrounds beside $\mathrm{ZZ} \rightarrow \tau \tau$ qq and HZ-backgrounds

## Recoil-mass w.r.t. the 2 jets





## Cut-flow for $\tau \tau$ qq search (most relevant)

|  | Signal | other HZ | $\mathrm{ZZ} \rightarrow \tau \tau \mathrm{qq}$ | $\mathrm{ZZ} \rightarrow 4 \mathrm{q}$ | $\mathrm{WW} \rightarrow \mathrm{qq} \mathrm{\tau v}$ | $\mathrm{WW} \rightarrow 4 \mathrm{q}$ |
| :--- | :---: | ---: | :---: | ---: | ---: | ---: |
| $\mathrm{N}_{\text {evt }} / 1 \mathrm{ab}^{-1}$ | 1040 | $\sim 140000$ | 65270 | 477000 | 1952000 | 6081000 |
| preselection | 881 | 4940 | 14293 | 8554 | 198021 | 142905 |
| evt shape | 810 | 2928 | 7961 | 4374 | 52493 | 57456 |
| $\tau$-cand. | 604 | 481 | 2190 | 7 | 1980 | 130 |
| $Z \rightarrow q q$ side | 594 | 467 | 1942 | 1 | 901 | 30 |
| kin. fit | 410 | 187 | 97 | $/$ | 6 | $/$ |
| $\rho \rho$ and $\mathrm{a}_{1} \rho$ | 401 | 126 | 97 | $/$ | 4 | $/$ |

Resulting in $\rho \rho$-case: $\varepsilon \sim 38 \%$ at S / B $\sim 3.05$

$$
\mathrm{a}_{1} \rho \text {-case: } \varepsilon \sim 39 \% \text { at } S / B \sim 1.15
$$

## Reconstructed acoplanarities

from high statistics and scaled to $N_{\text {exp }} / 1 a b^{-1}$

$A_{H}=\quad 0.116 \pm 0.058$
$A_{A}=\quad-0.132 \pm 0.058$
$\rightarrow \Delta A=A_{H}-A_{A}=0.248$


$$
\begin{array}{lr}
A_{H}= & 0.051 \pm 0.054 \\
A_{A}= & -0.040 \pm 0.054 \\
\rightarrow \Delta A=0.091
\end{array}
$$

## Selection for $Z \rightarrow I I, I=e, \mu$

- event-shape like $\cos \theta_{\text {event-momenta }}$
- 1 pair of hadronic $\tau$-candidates
- invariant mass
- angle between the candidates
- $1 \mathrm{e}^{+} \mathrm{e}^{-}$or $\mu^{+} \mu^{-}$pair
- invariant mass
- recoil mass
$\rightarrow$ With only HZ- and ZZ-backgrounds left:

$\rho \rho$-case: signal efficiency $\varepsilon \sim 47.5 \%$, S / B $\sim 1.55$

$$
\begin{aligned}
& A_{H}=0.041 \pm 0.133 \\
& A_{A}=-0.077 \pm 0.124
\end{aligned}
$$

$$
\rightarrow \Delta \mathrm{A}=0.118
$$

$\mathrm{a}_{1} \rho$-case: signal efficiency $\varepsilon \sim 46.5 \%$, S / B $\sim 0.6$

$$
\begin{aligned}
& A_{H}=0.034 \pm 0.112 \\
& A_{A}=-0.027 \pm 0.116
\end{aligned}
$$

$$
\rightarrow \Delta \mathrm{A}=0.061
$$

## Summary / Conclusion

- $\tau$ identification and reconstruction possible at high efficiency with anticipated detector
- Realistic measurement for CP in $\mathrm{H} \rightarrow \tau \tau$ performed
- Including
- detector effects
- full SM-background statistics
- 2-photon backgrounds
- full effects of ISR and FSR
- Significance to distinguish a CP-even from a CP-odd HiggsBoson of $4.7 \sigma$ for $1 \mathrm{ab}^{-1}$ can be expected
- Techniques like likelihoods, NN could enhance significances

