Experimental Study of RF Pulsed Heating on Oxygen Free Electronic Copper

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Experimental Study of RF Pulsed Heating on Oxygen Free Electronic Copper

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Abstract

When the thermal stresses induced by RF pulsed heating are larger than the elastic limit, microcracks and surface roughening will occur due to cyclic fatigue. Therefore, pulsed heating limits the maximum surface magnetic field and through it the maximum achievable accelerating gradient. An experiment using circularly cylindrical cavities operating in the TE$_{011}$ mode at a resonant frequency of 11.424 GHz was designed to study pulsed heating on Oxygen Free Electronic (OFE) copper. An X-band klystron delivered up to 10 MW to the cavities in 1.5 $\mu$s pulses at 60 Hz repetition rate. One run was executed at a temperature rise of 120 K for $56 \times 10^6$ pulses. Cracks at grain boundaries, slip bands and cracks associated with these slip bands were observed. The second run consisted of $86 \times 10^6$ pulses with a temperature rise of 82 K, and cracks at grain boundaries and slip bands were seen. Additional information can be derived from the power-coupling iris, and we conclude that a pulsed temperature rise of 250 K for several million pulses leads to destruction of copper. These results can be applied to any mode of any OFE copper cavity.

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I. INTRODUCTION

RF pulsed heating is a process by which metals are heated by the eddy currents created by a pulsed high-power RF source. Stress is induced on the metal surface when the heating occurs faster than the material has time to expand, which is governed by the speed of sound in the material. Such material will be prone to cyclic fatigue in which damage in the form of surface roughening and microcracks will occur over time if the induced stress is greater than the yield strength of the material.

A. Relevance to Accelerator Physics

Accelerating gradients in room temperature linear accelerators are limited by RF breakdown, dark current trapping, and pulsed heating. As one example, P. Wilson has taken the geometry of the Next Linear Collider traveling wave structure [1] and developed parameterizations for these limits with wavelength ($\lambda$). They are

\[
G_{\text{break}} = \frac{1.1 \text{ GeV/m}}{[\lambda(\text{cm})]^{7/8}}, \quad (1a)
\]

\[
G_{\text{trap}} = \frac{1.6 \text{ MeV}}{\lambda}, \quad (1b)
\]

\[
G_{\text{pulse}} = (28 \text{ MeV/m}) \frac{\Delta T^{1/2}}{[\lambda(\text{mm})]^{1/8}}, \quad (1c)
\]

A plot of these limits (Fig. 1) shows that pulsed heating could become the most restrictive phenomenon at short wavelength. Recent experiments have shown that breakdown is a multifaceted phenomenon [2, 3], and gradient limits are not as simple as implied by Eqs. (1). Underlying physical phenomenon are complex, material properties are important, and details of the structure geometry can matter because local regions of high field or high pulsed heating may determine the overall behavior.

The experiment reported in this paper was designed to study the effects of pulsed heating on OFE copper, the material most commonly used in normal conducting accelerator structures. (OFE copper is Oxygen Free Electronic copper. It is C10100 in the Copper Unified Numbering System.) The experiment has been performed with a cavity geometry and mode where pulsed heating was the dominant effect. The results are observation of pulsed heating effects and an upper limit on the maximum tolerable temperature rise. The
FIG. 1: Gradient limits due to RF breakdown, dark current trapping and pulsed heating. The data points represent gradient achieved with reasonable dark current [4]. The gradient limit for pulsed heating assumes a damage threshold of $\Delta T = 40$ K and is scaled from parameters of the Next Linear Collider assuming the filling time scales as $T_p \sim \lambda^{3/2}$.

limit can be applied to any cavity and any mode by calculating the electromagnetic fields and pulsed temperature rise throughout. If the temperature rise in part of the structure exceeds the maximum tolerable amount, the structure will have a limited gradient and/or, as the experiment shows, a limited lifetime.

B. Thermal Fatigue

Copper was studied in this experiment because of the preponderance of use in RF cavities. For copper, the boundary between elastic and plastic deformation is reached gradually with changes in stress or strain. In the region of elastic deformation, no permanent deformation will occur when stress is removed and no damage occurs. Under plastic deformation, when the applied stress or strain is beyond the yield point, permanent changes will be left in
the material. Microscopically, atoms at different planes in the crystal lattice will slip past each other causing vacancies and different configurations. If the metal is constantly stressed in the plastic region, these microscopic changes will accumulate as damage. This damage, known as cyclic fatigue, usually occurs at the surface because of the discontinuity of the crystal lattice. It evolves in the form of slip planes and microcracks on the surface.

The stress or strain necessary to cause damage by cyclic fatigue is much less than that required to break the material under static deformation. However, damage from cyclic fatigue occurs after many cycles of stress or strain. It generally occurs in three stages. The first stage is cyclic hardening of the material, in which the metal becomes stronger. The stress necessary to cause a certain amount of strain increases. This stage occurs within a few percent of the cycles to failure.

The second stage is the crack nucleation stage. In this stage, slip and cracks begin to initiate in the metal. They usually occur on the free surface of the metal and are most likely due to localized concentrations of plastic strain or imperfections in the crystal lattice.

The third stage is crack propagation. In this stage, fracture mechanics is used to describe the propagation of the cracks on the surface. Normally, the total lifetime of a metal is defined by the number of cycles it takes for cracks to nucleate plus the number of cycles it takes cracks to reach a particular length. Crack propagation is usually responsible for mechanical failure.

In the study of RF pulsed heating, we are more interested in the changes of electrical performance, so the nucleation of cracks is more relevant. Cracks on the surface will increase the surface resistivity of copper and degrade the cavity Q.

Thermal fatigue is cyclic fatigue caused by repetitive heating and cooling. Eddy currents that are developed from tangential magnetic fields on the surface will heat the surface. A simple example is shown in Fig. 2 where a fast high-power source heats the surface [5]. The heating happens quickly enough that the bulk of the metal is inertially confined and cannot expand transversely. Inertial confinement is the mechanical constraint that causes stress to occur on the surface. Using static linear elasticity with the assumptions that the transverse strain and normal stress are zero, the temperature rise at which the stress on the surface exceeds the yield stress $\sigma_y$ is [5]

$$\Delta T_y = \frac{(1 - \nu)\sigma_y}{E\alpha},$$

where $\nu$ is Poisson’s ratio, $E$ is the elastic modulus and $\alpha$ is the coefficient of linear thermal
FIG. 2: Metal surface being heated with a fast high-power source [5]. The surface itself expands normally into the vacuum.

### TABLE I: Parameters of fully annealed OFE copper at room temperature.

<table>
<thead>
<tr>
<th>Property</th>
<th>Value</th>
<th>Source</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\rho$ (Density)</td>
<td>$8.95 \times 10^3$ kg/m$^3$</td>
<td>[6]</td>
</tr>
<tr>
<td>$c_\varepsilon$ (Specific heat at constant strain)</td>
<td>385 J/kg-K</td>
<td>[6]</td>
</tr>
<tr>
<td>$k$ (Thermal conductivity)</td>
<td>390 W/m-K</td>
<td>[6]</td>
</tr>
<tr>
<td>$\alpha$ (Coefficient of linear thermal expansion)</td>
<td>$1.65 \times 10^{-5}$ K$^{-1}$</td>
<td>[6]</td>
</tr>
<tr>
<td>$\rho_{\text{res}}$ (Electrical resistivity)</td>
<td>$1.7 \times 10^{-8}$ $\Omega$-m</td>
<td>[6]</td>
</tr>
<tr>
<td>$E$ (Elastic modulus)</td>
<td>123 GPa</td>
<td>[7]</td>
</tr>
<tr>
<td>$\nu$ (Poisson’s ratio)</td>
<td>0.345</td>
<td>[7]</td>
</tr>
<tr>
<td>$\sigma_y$ (Yield stress)</td>
<td>62 MPa</td>
<td>[5]</td>
</tr>
</tbody>
</table>

expansion.

For temperature rises above $\Delta T_y$, plastic deformation and damage will occur. However, due to hysteresis, the stress must exceed the yield stress in both tension and compression in order for damage to continuously occur. Hence, the threshold temperature for damage due to pulsed heating occurs above $2\Delta T_y$ [5]. Using the numbers given in Tab. I for fully annealed OFE copper, the threshold temperature rise is 40 K. Uncertainties associated with the mechanical properties of fully annealed OFE copper give significant uncertainty
in this temperature threshold. Different surface preparations will affect the lifetime of the material [8]. Also, other sources have identified a safe threshold of 110 K temperature rise for pulsed heating from electron flux [9, 10]. However, the preparation of the surface in [9, 10] was not specified and could be much different than that used in the experiments described in this paper.

II. EXPERIMENTAL SETUP

We used a TE$_{011}$ mode in a circular cylindrical cavity with the length and radius chosen to maximize the temperature rise on the endcaps of the cylinders for two reasons. First, the purely azimuthal electric field in the cavity will minimize the chance of RF field breakdown on any surface in the cavity. This will isolate the effects of pulsed heating damage to the cavity surface. Second, the TE$_{011}$ mode does not require physical contact between the endcaps and the cylindrical sidewall. This simplifies removal and analysis of the damaged endcap surfaces. It would also allow re-use of the main body of the cavity with endcaps with different materials or surface preparations, but this was not done. Not only are the endcaps easily removable, they allow for simple tuning of the cavity by adjusting its axial length.

The TE$_{011}$ mode is excited by high-power RF pulses from the available 50 MW, 1.5 µs pulse, 11.424 GHz (X-band) klystrons at SLAC. Due to the high Q of the cavity, long pulse lengths are desired, so no pulse compression systems are used. At a repetition rate of 60 Hz, the surface heats up on every RF pulse then cools back down to the ambient temperature by the time the next RF pulse begins.

During the experiment, it would be ideal to measure the pulsed temperature rise on the cavity surface as well as the RF properties of the cavity. Since we are most interested in the effects of pulsed heating on these RF properties, we performed some measurements by parasitically exciting a low-power steady-state TE$_{012}$ mode. As the surface heats up, the Q will decrease due to the increase of the surface resistivity with temperature. The coupling to the TE$_{012}$ mode will dynamically change with the RF pulse. By measuring the change in reflected power from the coupling to the TE$_{012}$ mode, the temperature rise of the surface of the cavity can be extracted.
A. Cavity Design

The dimensions of the cavity were optimized such that the maximum heating occurs on the cavity endcaps. It is also desirable to minimize the heating on the cylindrical sidewall. Since the lifetime of copper varies as a power law with the applied stress [8, 11], the cavity may be re-used several times with different endcaps before it becomes too damaged.

On the endcaps, the tangential magnetic field is purely radial and varies as $J_1(p_{11}r/R)$ where $R$ is the radius of the endcap and $p_{11}$ is the first zero of $J_1(x)$. The local power dissipated on the surface varies as the square of the magnetic field, hence the temperature rise on the surface of the endcaps will appear as zones similar to tree rings. The maximum, which occurs at 48% of the cavity radius, will be referred to as the maximum temperature rise. Fig. 3 shows the maximum normalized temperature rise of the cavity endcaps and sidewall for a fixed resonant frequency of 11.424 GHz with various cavity lengths. The maximum temperature rise on the sidewall occurs in the center ($d/2$). The most appropriate cavity length is $d = 1.90$ cm.

At this length, the optimum coupling to the TE$_{011}$ mode is $\beta = 1.28$. The maximum temperature rise slowly varies with $\beta$ about this optimum value which increases the tolerances for machining and simulation.

The input power is coupled to the cavity through the magnetic field developed in a TE$_{10}$ mode inside a waveguide mounted on the cylindrical sidewall centered along the cavity’s axial length. The input coupler is a standard WR-90 waveguide with a circular aperture cut into the middle of its cross-section. The coupling coefficient $\beta$ determines the aperture size used to couple from the input waveguide to the cavity. The correct aperture size was determined through computer simulation using the finite-difference codes MAFIA [12] and GdfidL [13]. Due to a non-perfect surface finish from machining, we assumed a 10% degradation in the unloaded Q of the cavity to determine the aperture size. The design parameters for the TE$_{011}$ mode are given in Tab. II.

The parameters for the TE$_{012}$ mode, except for the coupling, are fixed from the cavity dimensions. This mode is also excited through a waveguide that is centered along the cylindrical sidewall at $1/4$ the cavity’s axial length, a position where the magnetic field of the TE$_{012}$ mode is at its maximum. The width of the input coupler is that of a WR-42 waveguide (0.42 inches) so that its cutoff frequency is above 11.424 GHz. The width was
FIG. 3: Maximum temperature rises on cavity endcaps and sidewall normalized to input power as a function of cavity length $d$ at a fixed resonant frequency of 11.424 GHz. This plot does not include consideration of temperature rise at the coupling iris.

**TABLE II: Cavity design parameters for the TE_{011} mode.**

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$f_{res}$ (Resonant frequency)</td>
<td>11.424 GHz</td>
</tr>
<tr>
<td>$d$ (Axial length)</td>
<td>1.90 cm</td>
</tr>
<tr>
<td>$R$ (Radius)</td>
<td>2.2075 cm</td>
</tr>
<tr>
<td>$Q_0$ (Unloaded Q)</td>
<td>21900</td>
</tr>
<tr>
<td>Estimated $Q_0$ (Unloaded Q with estimated degradation)</td>
<td>19710</td>
</tr>
<tr>
<td>$Q_{ext}$ (External Q)</td>
<td>15400</td>
</tr>
<tr>
<td>$Q_L$ (Loaded Q)</td>
<td>8650</td>
</tr>
<tr>
<td>$\beta$ (Coupling coefficient)</td>
<td>1.28</td>
</tr>
<tr>
<td>$R_a$ (Radius of coupling aperture)</td>
<td>3.75 mm</td>
</tr>
<tr>
<td>$d_a$ (Thickness of coupling aperture)</td>
<td>1.88 mm</td>
</tr>
</tbody>
</table>
TABLE III: Cavity design parameters for the TE$_{012}$ mode.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$f_{res}$ (Resonant frequency)</td>
<td>17.820 GHz</td>
</tr>
<tr>
<td>$Q_0$ (Unloaded Q)</td>
<td>21960</td>
</tr>
<tr>
<td>Estimated $Q_0$ (Unloaded Q with estimated degradation)</td>
<td>19760</td>
</tr>
<tr>
<td>$Q_{ext}$ (External Q)</td>
<td>19760</td>
</tr>
<tr>
<td>$Q_L$ (Loaded Q)</td>
<td>9880</td>
</tr>
<tr>
<td>$\beta$ (Coupling coefficient)</td>
<td>1.0</td>
</tr>
<tr>
<td>$R_a$ (Radius of coupling aperture)</td>
<td>2.85 mm</td>
</tr>
<tr>
<td>$d_a$ (Thickness of coupling aperture)</td>
<td>1.034 mm</td>
</tr>
</tbody>
</table>

FIG. 4: A picture of the cavity body with one endcap shown on the outside. The water-cooling pipes can be seen on the bottom of the cavity body.

tapered to 0.622 inches after a length of 10.4 cm to make use of available WR-62 vacuum windows. The length was chosen such that the power at 11.424 GHz would be attenuated by over 150 dB to avoid damaging the measurement electronics. The input coupler is designed to critically couple into the TE$_{012}$ mode so that the steady-state reflected power is nominally zero when there is no temperature rise in the cavity. The design parameters for the TE$_{012}$ mode are shown in Tab. III. A 10% degradation in $Q_0$ was similarly assumed.

A picture of the test cavity with one endcap placed outside is shown in Fig. 4. An
<table>
<thead>
<tr>
<th>STEP</th>
<th>DESCRIPTION</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Cooling channel and grooves machined on copper endcap</td>
</tr>
<tr>
<td>2</td>
<td>Surface of copper endcap machined to class-16 finish</td>
</tr>
<tr>
<td>3</td>
<td>Copper endcap brazed to stainless-steel ring</td>
</tr>
<tr>
<td>4</td>
<td>Stainless-steel ring assembly machined to correct dimensions</td>
</tr>
<tr>
<td>5</td>
<td>Surface of copper endcap diamond fly-cut to mirror finish</td>
</tr>
<tr>
<td>6</td>
<td>Surface of copper endcap chemically-etched for 5 seconds for vacuum cleaning</td>
</tr>
<tr>
<td>7</td>
<td>Stainless-steel ring assembly welded to stainless-steel piston</td>
</tr>
<tr>
<td>8</td>
<td>RF spring gaskets placed in RF groove around circumference of copper endcap</td>
</tr>
<tr>
<td>9</td>
<td>Piston assemblies inserted into cavities and placed under vacuum</td>
</tr>
</tbody>
</table>

**TABLE IV:** Piston assembly and copper endcap surface preparation.

A spiral channel is cut into the back of each endcap for water-cooling to remove the average heat that is dissipated. This prevents the cavity’s resonant frequency from drifting due to thermal expansion. Water-cooling pipes were also added around the circumference of the cavity on both sides of the input coupler as shown in Figs. 4 and 5.

Two grooves are cut along the outer radius of the endcaps as shown in Fig. 7. One groove is used to remove the degeneracy between the $TE_{011}$ mode and the $TM_{111}$ mode as well as the degeneracy between the $TE_{012}$ mode and the $TM_{112}$ mode. The TM modes require current to cross from the endcap to the cylindrical sidewall, hence their resonant frequencies...
FIG. 5: Assembly schematic of cavity with endcaps. The sideview of the cavity is shown on the right. All dimensions are in inches.
are shifted by creating a gap. The gap between this groove and the sidewall is 1.1 mm. The depth of the groove was initially set to 1.0 mm. However, at this depth, there were interference of other modes with the TE_{012} mode that prevented the temperature diagnostic from being used during the first high-power test. Using a cavity mock-up, the correct depth of the groove was empirically determined to be 2.5 mm to isolate the TE_{012} mode and this was used for the second high-power test.

The second groove houses a gold-plated stainless-steel spring gasket that becomes an RF short when compressed. The RF short prevents coaxial modes from being excited in the gap along the length of the piston and prevents RF breakdown from occurring in this gap.

Cold-test results demonstrated some errors in the meshing of the input coupler during simulation. The measured coupling coefficient to the TE_{011} mode was approximately 1.7
STEP | DESCRIPTION
--- | ---
1 | Vapor degrease in 1,1,1 trichloroethane [14] for 5 minutes
2 | Alkaline soak clean using Enbond Q527 [15] for 5 minutes at 180°F
3 | Cold tap water rinse for two minutes
4 | Immerse in 50% hydrochloric acid at room temperature for 1 minute
5 | Cold tap water rinse for 1 minute
6 | Immerse in the following solution for 5 seconds at room temperature:
   Phosphoric Acid, 75% 21 gallons
   Nitric Acid, 42° Baumé 7 gallons
   Acetic Acid, Glacial 2 gallons
   Hydrochloric Acid 19.2 fluid ounces
7 | Cold tap water rinse for minimum of 2 minutes
8 | Immerse in solution of Oxyban 60 [16] (1% by volume) for 2–5 minutes
9 | Cold tap water rinse for 1 minute
10 | Cold deionized water rinse for 1 minute
11 | Hot deionized water rinse for 30 seconds
12 | Immerse in analytical grade isopropyl alcohol at 115°F for 30 seconds
13 | Blow dry with dry nitrogen blast
14 | Dry in air oven at 150°F

TABLE V: Procedure for vacuum cleaning of endcap surface.

which reduced the temperature rise per watt by approximately 4% from the optimum value. As indicated earlier, the TE\textsubscript{012} mode suffered from interference with other modes which was fixed for the second high-power test. The cold-test results also demonstrated leakage of power from the TE\textsubscript{012} mode into the input coupler for the TE\textsubscript{011} mode. Hence the cavity has to be treated as a two-port cavity for the TE\textsubscript{012} mode during data analysis. The comparison of the RF parameters of each mode before and after the high-power tests will be given in Sec. IV. See [17, pp. 65–78] for a complete discussion of the cold-test results.
B. **Klystron setup**

Two different setups were used to conduct high-power tests with X-band klystrons. They are shown in Fig. 8. Each setup is required to protect the klystron by limiting the reflected power to a maximum of 5 MW. Fifty-five-dB directional couplers were placed in front of each cavity to measure the forward and reflected power. The power measurements allow us to determine the coupling and Q of each cavity.

In the setup for the first high-power test, two similar cavities were used simultaneously. By using an asymmetric magic-tee, the reflected power from each cavity would go to the load. The advantage of this setup is that each cavity would receive the maximum input power possible since no high-power circulators exist. Also, four endcaps can be tested simultaneously. The disadvantage is that the cavities have to be tuned to each other while the klystron is on. The differential screws did not offer a fine enough adjustment, and the cavities have to be tuned by adjusting water flow to the endcaps. Also, the measurement of the loaded Q of each cavity suffered from systematics that will be explained later.

From the experiences gained with the first high-power test, we changed to the second setup. This setup has the advantage of relaxing the necessity of fine-tuning the cavity. Normally, the only disadvantage is the amount of power that must be thrown away in order to protect the klystron. However, due to RF breakdown that was known to occur at the aperture at approximately 8.5 MW from the first test, this was not a hindrance.

It is not possible to reach the desired power level in the cavity immediately due to
absorbed gases in copper. Normally at SLAC high-power components are first placed under vacuum then baked out at high temperature (at least 400 °C) for a few days to remove gas. However, the RF spring gaskets used to prevent the excitation of coaxial modes along the pistons cannot be baked at such a high temperature. They may lose their elastic properties causing their effectiveness as RF shorts to deteriorate. Thus, the cavity body and the magic-tee were baked out separately at high temperature because they were new and were not handled in a clean environment. However, the endcaps did not go through a high-temperature bake-out. Afterwards, the components were assembled and attached to the klystron. After being placed under vacuum, the components were baked using heater tapes at 150 °C for 3 days. This procedure removes some absorbed gas on the surface.

The klystron power level must be increased slowly as the high-power fields in the cavity and other waveguide components pull more gas out of the surface. This is known as power conditioning. There are interlocks to shutdown the klystron when there is too much gas in the system. If this is not done, damage may result to the components due to RF breakdown. Over time, the gas is slowly removed and the power may be increased. As will be discussed later, RF breakdown at the high-power coupling aperture limited the amount of power that could be put into the cavity. At this point, gas is released violently and the cavity cannot be conditioned any further in a reasonable amount of time.

C. Diagnostic Setup

The forward and reflected X-band powers are measured with crystal detectors attached to 55-dB directional couplers. Additional attenuation is added to give appropriate power levels for the crystals, which had sensitivities between 500 to 700 mV/mW. The forward power signal is digitized, binned by power level and counted to measure the number of high-power pulses accrued when temperature rise and Q’s of the TE₀₁₁ and TE₀₁₂ modes are measured.

The diagnostic setup that measures the pulsed temperature rise and Q of the TE₀₁₂ mode is shown in Fig. 9. A CW low-power RF source excites the diagnostic mode. The source frequency is roughly 17.8 GHz and is adjusted to minimize reflected power. A waveguide low-pass filter protects the electronics from high-power klystron harmonics that are coupled out and are not cutoff by the WR-42 hybrid waveguide. A circulator, with approximately 32 dB isolation at 18 GHz, isolates the reflected signal from the input signal, and directional
couplers with crystal detectors are placed on either side of the circulator to measure forward and reflected powers. The steady-state reflection from the cavity with a coupling coefficient $\beta = 0.7$ is 16 dB below the input power. There is 2 dB insertion loss in the circulator and directional coupler, so the reflected signal is 14 dB above the input power that leaks through the circulator. The reflected power increases during the pulsed heating, and the reflected signal can be measured without significant error caused by imperfect isolation. The amplitude and phase of the reflected CW signal will change when the cavity is heated from a high-power, X-band pulse. Those changes are measured with the quadrature mixer. The RF switch can be opened between high-power pulses when the temperature has returned to ambient, and the energy in the $TE_{012}$ mode will drain from the cavity. The decay time and steady-state reflected power can be combined to give the coupling coefficient and unloaded $Q$. Changes in $Q_0$ indicate surface deterioration.
III. THEORY

The temperature rise on the surface of the cavity can be determined using the familiar heat conduction equation with knowledge of the electromagnetic fields in the cavity and the input power. In reality, the heat conduction equation is coupled to the elasticity equations because of the small amount of heat dissipation that occurs due to mechanical strain of the material. This coupling term is quite small in our case [17, pp. 88–91] and may be ignored.

A. Heat Conduction

It is simplest to reduce the heat conduction equation to an integral using Green’s functions. The surface heating is from the power dissipation that occurs from the eddy currents created from surface magnetic fields. Since the power dissipated per unit area on the surface is proportional to the square of the magnetic field, the heat generated per unit volume is

\[ \dot{g}(z,t) = \frac{dP(z,t)}{dA dz} = \frac{dP(t)}{dA} \left( \frac{2}{\delta} e^{-2z/\delta} \right) \quad z \geq 0, \]  

where \( \delta \) is the skin-depth. For a one-dimensional infinite slab the temperature rise on the surface \( z = 0 \) is

\[ \Delta T(z = 0, t) = \frac{2}{\rho c_e} \int_0^t dt' \frac{dP(t')}{dA} \frac{1}{\delta} \exp \left[ \frac{4\alpha_d (t - t')}{\delta^2} \right] \text{erfc} \left[ \frac{2}{\delta} \sqrt{\alpha_d (t - t')} \right], \]  

where \( \alpha_d = k/\rho c_e \) is the thermal diffusivity.

For a square RF pulse of length \( t_p \), the diffusion depth \( D = \sqrt{\alpha_d t_p} \) characterizes the length into the surface of which the effect of the heat source decays on the order of \( 1/e \) at time \( t_p \). If the diffusion depth in a material is much longer than its skin-depth, then the decay of the magnetic field into the material can be ignored. In this regime, the effect of the penetration of the magnetic field into the material on the heating is small. For copper, a 1 \( \mu \)s pulse creates a diffusion depth \( D = 10.8 \mu \)m as compared to \( \delta = 0.6 \mu \)m at f=11.424 GHz.

Letting \( \delta \to 0 \), Eq. 4 becomes

\[ \Delta T(z = 0, t) \big|_{\delta \to 0} = \frac{1}{\rho c_e \sqrt{\pi \alpha_d}} \int_0^t \frac{dt'}{\sqrt{t - t'}} \frac{dP(t')}{dA}. \]  

This is the same result if we had considered a prescribed surface heat flux \( dP(t)/dA \) with no volume energy generation. For a 1 \( \mu \)s pulse, Fig. 10 shows the temperature rise on the
FIG. 10: The temperature rise at various times in the conductor normalized to the surface temperature at $t = 1.0 \, \mu s$, for a pulse length of $t_p = 1.0 \, \mu s$.

surface normalized to the temperature rise at $1 \, \mu s$. The error from ignoring the skin-depth on temperature rise is less than 3%.

Eq. 4 assumes the surface is semi-infinite; however, the cavity surface is two-dimensional. When a full analysis is done [17, pp. 101–109], the error in using Eq. 4 to predict the temperature rise on every part of the cavity surface is small for short times. Fig. 11 depicts this comparison for the cavity endcaps. For times of a $1000 \, \mu s$ or less, the one-dimensional approximation is good.

**B. Pulsed Heating of Test Cavity**

The calculations shown previously assumed that all the thermal parameters were constant. For temperature rises of 300 K, the specific heat increases by about 5% and the thermal conductivity decreases by about 5%. The error for not including this temperature dependence in the calculation becomes 1% [17, p. 100]. Hence, Eq. 4 is valid by taking $\alpha_d$
FIG. 11: 1-D and 2-D temperature rises of the cavity endcaps for various pulse lengths normalized to the maximum temperature rise for 1-D.

The electrical resistivity is an important parameter for the surface temperature rise. Its (linear) dependence on temperature causes the unloaded Q of the cavity to decrease over the length of a pulse. Since a temperature rise of 100 K will cause the resistivity to increase by 40%, the temperature dependence must be taken into account when calculating the pulsed temperature rise. Its influence can be seen from the local power dissipation

\[
\frac{dP(t)}{dA} = \frac{1}{2} R_s |H(t)|^2,
\]

where \( R_s = \sqrt{\pi \mu_0 \rho_{res}} \).

The calculation is also complicated by the magnetic field’s dependence on Q. The cavity behaves as a damped, driven oscillator, so the amplitude of the fields are affected by the
FIG. 12: Comparison of variable $\rho_{\text{res}}$ with constant $\rho_{\text{res}}$ on the temperature rise of the cavity endcaps for a 10 MW, 1 $\mu$s pulse.

The details of this calculation are fully explained in [17, Chapter 3, Appendix A]. Using the cavity parameters given in Tab. II, Fig. 12 shows the effect of including the temperature dependence of $\rho_{\text{res}}$ for a 10 MW, 1 $\mu$s pulse on the cavity endcaps. The inclusion of this effect increased the temperature rise by 10%.

Notice after a time longer than 3 pulse-lengths, the temperature rise on the surface decays to within 30% of its maximum value. Since there is approximately 17 ms between pulses, the temperature rise decays close to zero by this time. There will be some average temperature rise due to the combined effect of many pulses; however, water-cooling stabilizes this temperature rise to about 10 K above room temperature [17, pp. 63–64].

The degradation in the unloaded Q for each mode is calculated from [17, p. 218]

$$
\frac{1}{Q_0(T)} = \frac{1}{\sqrt{4\pi\mu f}} \int_{S_w} dS \sqrt{\rho_{\text{res}}(T(\vec{r}))} |\vec{H}(\vec{r})|^2,
$$

where $S_w$ is the entire cavity surface and $\vec{r}$ is a point on the surface. For the above example, the Q change for both modes is shown in Fig. 13.
FIG. 13: Change in $Q_0$ for both TE$_{011}$ and TE$_{012}$ modes for a 10 MW, 1 µs pulse.

The amplitude and phase of the reflected power from the TE$_{012}$ mode will change as its unloaded $Q$ degrades over the time of a high-power pulse. The amplitude change is due to a change in the coupling to the mode. The phase shift is due to the change in the resonance frequency which depends on two effects. The first and major effect is the dependence of the cavity’s resonant frequency on $Q$. This effect can be intuitively grasped by realizing that the unloaded $Q$ depends on geometry. A finite skin-depth means the effective volume that contains electromagnetic fields is bigger than the volume in vacuum. As the $Q$ changes, so will the skin-depth and this effective volume. Hence the frequency changes accordingly. The second effect is due to any deformation that might occur after the pulse turns off.

A calculation of the expected signal looking through the diagnostic port from the TE$_{012}$ mode is shown in Fig. 14 for a 10 MW, 1 µs pulse. In this case, we’ve assumed coupling through the diagnostic port of $\beta = 1$, and, in addition, leakage out the high-power port with coupling $\beta = 0.22$. It is to be noticed that the extrema of these curves occur some time after the pulse shuts off. This lag time is on order of the cavity fill-time.
FIG. 14: Magnitude and phase of the reflected signal with respect to the input signal due to the change in $Q_0$ of the TE$_{012}$ mode.

The change in the unloaded Q and resonant frequency of the TE$_{012}$ mode is extracted from measurements of the amplitude and phase of the reflected power [17, p. 126]. The maximum temperature rise on the endcaps can be extracted from Eq. 7 with two assumptions. The first assumption is knowledge of the field pattern of the mode. This is well known on the endcaps and the majority of the cylindrical sidewall. The only places where it is not known analytically is near the coupling apertures. The apertures modify the fields locally. The second assumption is the ratio between the maximum temperature rise on the cavity endcaps to the maximum temperature rise on the sidewall which is approximately 2 for
the dimensions used. Since changes in unloaded Q of the TE\textsubscript{012} mode is eight times more sensitive to resistivity changes on the endcaps as compared to the sidewall, the overall error due to this assumption is less than 1%. See [17, pp. 126–132] for more details.

IV. EXPERIMENTAL RESULTS

Results are presented from two different high-power tests. The first test used the two-cavity setup depicted in Fig. 8 which provided four endcaps to analyze afterwards. The second test used the one-cavity setup which only provided two endcaps but made the experiment easier to run.

A. First Test

In this particular run, we used an XL-3 50 MW klystron that was limited to 1.25 \( \mu \)s pulses at a repetition rate of 60 Hz. The vacuum in the cavities was approximately \( 10^{-9} \) Torr. Due to interference of other modes with the TE\textsubscript{012} mode, the diagnostic to measure the pulsed temperature rise was not used in this run.

1. Run-Up Procedure

The entire experimental run occurred over a two-month period in which it took approximately two weeks to reach 8.5 MW of input power to each cavity due to outgassing from the copper surface and RF breakdown. We did not go above 8.5 MW due to the extensive RF breakdown at the high-power coupling aperture.

During the experiment, the cavities were tuned to each other in a way that their resonant frequencies would match after thermal expansion due to average heating. At this input level, the temperature rise due to average heating on the endcap is calculated to be 10 K and causes a 4 MHz decrease in resonant frequency.

2. RF High-Power Results

With the forward and reflected power measurements at X-band, the coupling coefficient \( \beta \) and the loaded Q, \( Q_L \), can be determined [17, pp. 140–150]. The input power to each
TABLE VI: Cavity Q measurements of cavity 1 and 2 using a HP8510C network analyzer before and after the first high-power test. The change in $Q_{\text{ext}}$ is due to the increase in size of the high-power coupling apertures.

<table>
<thead>
<tr>
<th>Cavity</th>
<th>Initial $Q_0$</th>
<th>Final $Q_0$</th>
<th>Initial $QL$</th>
<th>Final $QL$</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>20350 ± 520</td>
<td>14360 ± 300</td>
<td>7670 ± 110</td>
<td>5010 ± 50</td>
</tr>
<tr>
<td>2</td>
<td>20610 ± 530</td>
<td>16810 ± 260</td>
<td>7670 ± 110</td>
<td>5010 ± 50</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Cavity</th>
<th>Initial $\beta$</th>
<th>Final $\beta$</th>
<th>Initial $Q_{\text{ext}}$</th>
<th>Final $Q_{\text{ext}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>1.65 ± .06</td>
<td>1.87 ± .05</td>
<td>12320 ± 520</td>
<td>7690 ± 260</td>
</tr>
<tr>
<td>2</td>
<td>1.69 ± .06</td>
<td>2.36 ± .07</td>
<td>12220 ± 530</td>
<td>7140 ± 250</td>
</tr>
</tbody>
</table>

cavity was measured to be 8.5 MW ± 0.6 MW. This corresponds to a calculated temperature rise of 120 K ± 10 K. The uncertainties are due to systematic errors in the calibration of the directional couplers and random errors caused by the fluctuation of the crystal detector voltage from noise. The experiment was run at this temperature rise for $5.6 \times 10^7$ pulses.

An HP8510C vector network analyzer was used to determine the RF parameters of each cavity before and after the high-power test. The results, given in Tab. VI, show a 20% to 30% degradation in unloaded Q. The damage that resulted on the surface will be shown later. The degradation in external Q is from the increase of the size of the coupling aperture due to damage from pulsed heating. This will also be shown later.

The coupling coefficient, $\beta = Q_0/Q_{\text{ext}}$, is determined by measuring the forward and reflected power to and from the cavity. The reflected power is measured near its steady-state value before the RF pulse shuts off. This measurement over the course of the experimental run is shown in Fig. 15 for both cavities. The time-domain measurement of $\beta$ at the end of the run is consistent with the frequency-domain measurement. A few general points can be made about the changing trend in the value of $\beta$ for both cavities. In the first 20 million pulses, $\beta$ increases for both cavities. This must be due to a degradation in $Q_{\text{ext}}$ because $Q_0$ can only decrease due to damage. After 20 million pulses, $\beta$ decreases for cavity 1 and increases more slowly for cavity 2. This demonstrates that the degradation of $Q_0$ from surface damage has become dominant. The overall decreasing trend for cavity 1 as compared to the increasing trend demonstrated for cavity 2 is supported by the data given in Tab. VI. Cavity 1 suffered a smaller change in $Q_{\text{ext}}$ than cavity 2 but suffered a greater change in $Q_0$. 24
The variation shown in \( \beta \) for cavity 2 after 50 million pulses is due to systematic errors.

In principle, \( Q_L \) can be measured through the exponential decay of the reflected power when the RF pulse turns off and \( Q_0 \) can be determined by combining \( \beta \) and \( Q_L \) measurements. However, that was not possible for a combination of reasons. Pulsed heating affects RF properties and measurements, so the input power had to be lowered to below 2 MW before measurements could be made. The cavities, which were tuned to each other under full power, become mismatched to each other and, in addition, mismatched to the klystron output cavity. This problem became worse over time as \( \beta \) for cavity 2 increased. These mismatches mixed together the characteristic decays, and the variations of \( Q_L \) and \( Q_0 \) during the experimental run could not be determined [17, pp. 144–150]. However, the trend in Fig. 15 with the data in Tab. VI shows a clear degradation of \( Q_0 \) for each cavity.

3. Visual Inspection of Copper Surface

At the end of the experimental run, the endcaps were removed from the cavities and inspected. One such endcap is shown in Fig. 16. Each endcap is made from polycrystalline OFE copper; therefore, the structure on the surface is made from crystal grains whose lattices are oriented in a generally random direction with respect to each other. Fig. 16 shows an obvious visual change in the crystal grains in the region where the temperature
FIG. 16: Picture of one endcap from the first high-power test. A change in the crystal grains is visible even in the region where the temperature rise was lower by 10%. The region of the endcap nearest the high-power coupler is on the lower left in the right-hand picture. Tarnish from the sputtering of copper is on the lower part of the endcap.

rise is maximum, which is approximately half-way between the center and outer radius of the endcap. In this area in which there is high-amplitude cyclic straining, steps may form in crystal grain boundaries with height differences on the order of microns [18, p. 126]. This would change the direction of light specularly reflected from the surface, which will cause a contrast between the grains in the fatigued area as compared to the rest of the surface.

Also visible on the surface are black patches that appear on the half of the endcap that is closest to the high-power coupling aperture. These patches are most likely due to multipacting as they appear to occur in pairs. Electrons would orbit around the radial magnetic field lines along the endcap. According to GdfidL simulations, the maximum magnetic field on the endcap at the azimuth of the high-power coupling aperture is 5% higher than the point diametrically opposite of it. Since the energy of multipacting electrons is restricted, this could explain why the patches only occur on half of the endcap surface nearest the high-power coupling aperture.

There is also a tarnish visible on the surface. The tarnish is thicker at the outer radius and at the azimuth closest to the high-power coupling aperture. As will be shown in the next
FIG. 17: An internal cross-section of one endcap in the region of maximum temperature rise on the surface. The endcap surface is the boundary between the white and black regions of the pictures. The crack on the left propagated 25 µm into the surface before reaching an internal grain boundary. The crack on the right propagated 15 µm into the surface.

section, scanning-electron microscope studies show this tarnish to be copper globules that were sputtered onto the surface. Because these globules may add to the surface roughness of the cavity, they may contribute to the degradation in $Q_0$ shown in Tab. VI.

4. Internal Cross-Section

Cracks nucleated at the surface may propagate into the interior of the metal. One endcap was cut internally along a diameter and polished to view its cross-section. Cracks were only found near the area of maximum temperature rise. Less than 10 cracks were visible at a microscope magnification of 1000 and only 2 cracks are longer than 10 µm. These cracks are shown in Fig. 17. These cracks were first created at the surface and then propagated internally, because higher stresses and strains occur at the surface than in the interior of the metal [19, p. 66]. Only a few cracks will propagate internally as compared to the amount of cracks that are nucleated at the surface.

Slip will occur when the shear stress along a slip plane is above a critical value [11, Sec.
FIG. 18: Comparison snapshot of a region of maximum temperature rise on the left and a region of zero temperature rise on the right for one endcap. The length scale is 100.7 µm.

6.2.3]. Since the normal stress axis occurs parallel to the endcap surface, the maximum shear stress occurs along a plane inclined at 45° to the surface. Since the endcap is made from polycrystalline copper, only grains that have slip planes oriented close to this angle will show slip if the stress is large enough. The cracks in Fig. 17 begin propagating at roughly 45° to the surface within the first few microns into the surface, which is known as Stage I crack propagation. Also seen to occur is Stage II crack propagation in which cracks propagate perpendicular to the surface and perpendicular to the stress axis [18, p. 60].

5. Scanning Electron Microscope Inspection of Copper Endcap Surface

Each endcap was inspected with a scanning electron microscope using secondary scattering with a 5 kV beam. First, scans were taken along a random diameter of each endcap. Cracks are only visible in the region where the maximum heating occurred at a radius of 10.6 mm. The thickness of this region is approximately 4 to 5 mm for each endcap. No other damage is visible on the surface.

Second, scans were taken around the region of maximum heating at different magnifications. One such region is shown on the left of Fig. 18. Numerous cracks are visible on the surface. The bumps that occur on the surface are due to the copper globules that sputtered onto the endcaps from the high-power coupling aperture. For comparison, the center of
FIG. 19: Fatigue slip bands on a particular crystal grain in the area of maximum temperature rise. The picture on the right is a close-up of these slip bands in which some microcracks are evident at the base of the slip bands. The scale is 100.7 µm on the left and 10.1 µm on the right.

the endcap is shown on the right of Fig. 18. No cracks are visible in the center where the temperature rise is close to zero. The copper globules sputtered on the surface are most dense near the outer radius where no cracks are visible. This suggests that pulsed heating and not the copper globules are responsible for the nucleation of cracks on the surface.

As mentioned earlier, some crystal grains will show signs of slip if they have the proper orientation. Fig. 19 shows an example of these slip bands as striations on the surface. Slip bands are created from stress relaxation of the surface due to plastic deformation, which results in surface intrusions and extrusions. Surface intrusions create a notch effect for possible nucleation of microcracks as demonstrated on the right of Fig. 19 [18, p. 60]. In general, crack propagation along the surface is perpendicular to fatigue striations [19, p. 95].

Grain boundaries are another common site for crack nucleations [19, p. 67]. Fig. 20 is an example of cracks along grain boundaries. In the picture on the left, the transition between the two different textures on the surface is shown by the red arrows. The texture on the right-hand side of the picture is due to slip bands. A close-up of the grain-boundary crack is in the right-hand picture. Notice that the striations of the slip bands end at the crack. Grain boundaries act as natural barriers for slip bands, because the neighboring grains usually have incompatible orientations that prevent slip bands propagating across
FIG. 20: Grain-boundary cracks in the area of maximum temperature rise. The grain boundary is the transition between the two different textures on the surface shown by the red arrows. The texture on the right-hand side of the picture on the left is due to slip bands. A close-up of one crack is in the right-hand picture where the grain boundary is clear. The length scales are 100.7 µm and 10.1 µm respectively.

The enhanced stress from this incompatibility may lead to crack nucleation at the grain boundary. See [17, Appendix B] for more pictures of cracks and slip bands.

Scans were completed along random diameters of each endcap at the same magnification of 100. Each snapshot corresponded to an area approximately 0.9 mm by 0.9 mm. Fig. 21 shows the results of these scans.

In general, the scans indicate that surface roughening from fatigue is a precursor for crack nucleation, because most of the regions containing cracks are within the regions of surface roughness. Also, the bands generally surround the expected area of maximum temperature rise at the radius of 10.6 mm. The widths of these regions are listed in Tab. VII. The variation in the widths of damage reported in Tab. VII among each endcap is due to the location of the scanned diameter with respect to the azimuth of the high-power coupling aperture. The widths are generally larger when the scanned diameter is closer to the aperture. This feature is largely explained by the higher temperature rise in this area due to the higher surface magnetic field as explained in Sec. IV A 3.

Numerous pictures were taken in areas that showed many cracks. Tab. VIII shows the
FIG. 21: Random scans along diameters of each endcap. The solid line corresponds to regions of surface roughening and the dotted line is for regions that contain cracks on the surface. The centers of the endcaps are at position 0 mm.
TABLE VII: Widths of regions of surface roughening and cracks for each endcap from the first high-power test.

<table>
<thead>
<tr>
<th>Region</th>
<th>1 (mm)</th>
<th>2 (mm)</th>
<th>3 (mm)</th>
<th>4 (mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Roughness</td>
<td>6.4</td>
<td>4.5</td>
<td>3.8</td>
<td>3.2</td>
</tr>
<tr>
<td>Cracks</td>
<td>5.1</td>
<td>3.8</td>
<td>0.7</td>
<td>5.8</td>
</tr>
</tbody>
</table>

TABLE VIII: Average radius and standard deviation of crack positions for each endcap.

<table>
<thead>
<tr>
<th>Endcap</th>
<th>Average Radius (mm)</th>
<th>Standard Deviation (mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>10.4</td>
<td>1.3</td>
</tr>
<tr>
<td>2</td>
<td>11.3</td>
<td>0.9</td>
</tr>
<tr>
<td>3</td>
<td>10.5</td>
<td>1.4</td>
</tr>
<tr>
<td>4</td>
<td>11.1</td>
<td>1.1</td>
</tr>
</tbody>
</table>

average radius and standard deviation of the positions at which the highest density cracks were found. The maximum temperature rise is expected to occur at approximately 10.6 mm.

6. Damage to High-Power Coupling Aperture

There was damage to the high-power coupling apertures that provided unexpected information about temperature limitations from pulsed heating. Fig. 22 shows that significant damage has occurred to the high-power coupling aperture of cavity 1. Simulations using HFSS [20] show that the strength of the magnetic field on the aperture will cause a temperature rise of 250 K. The magnetic field wraps around the edge of the aperture and is enhanced. The damage on the aperture occurs at this spot. The electric field is generally azimuthal except near the aperture in which it is curved towards the surface. The electric field at the aperture is approximately 85 MV/m, which is sufficient to cause RF breakdown. Pitting has occurred at this spot.

Since the damage on the aperture appears to occur in the direction of the surface magnetic
FIG. 22: A picture of the high-power coupling aperture of cavity 1 after the first high-power test. The aperture has been rounded in the direction of the magnetic field. The electric field has caused pitting to occur on either side of the aperture at right angles to the rounding.

field, a likely explanation for the damage is fatigue due to pulsed heating. As cracks develop in the aperture region, the heating will increase due to the larger electrical resistivity. The increased heating will cause more cracks to develop and increase the size of cracks that already exist. Eventually local melting will result. Metal will evaporate and spray from these cracks [9, Ch. 7]. This result indicates that extensive damage will occur at a temperature rise of 250 K for 50 million pulses. This is an important limit.

B. Second Test

The second high-power test was conducted with cavity 1 from the previous high-power test using new OFE copper endcaps after the cavity was cleaned for vacuum. Since most of the cavity was processed with high power previously, it took only one week to reach full power. The vacuum in the cavity throughout the run is $10^{-9}$ Torr.

The same klystron was used but in a different test area. In this area, the diagnostic measurement setup was closer to the modulator which added more noise to the crystal detector voltages. Since the forward power was measured with a peak-power analyzer, this did not affect that measurement. However, it increased the error in the determination of the coupling coefficient and the loaded Q in the time-domain.
1. **High-Power Results**

The cavity was excited with 7.3 MW ± 0.3 MW, 1.5 µs pulses at 60 Hz for $8.6 \times 10^7$ pulses. This corresponds to a calculated maximum temperature rise on the endcaps of $82 \pm 3$ K. Tab. IX gives the RF parameters of the TE$_{011}$ mode before and after the test. The table shows a $Q_0$ degradation of 5% and a $Q_{ext}$ degradation of 10%. The RF parameters for the TE$_{012}$ mode are given in Tab. X. For the TE$_{012}$ mode, port 1 corresponds to the low-power diagnostic port and port 2 corresponds to the high-power port. As Tab. X demonstrates, there is some leakage of the TE$_{012}$ mode out the high-power port due to a non-zero coupling. Further tests indicate that it leaks as a TE$_{10}$ mode in the waveguide, which means the leakage is caused by asymmetry about the large high-power coupling aperture. This leakage must be taken into account when determining the RF parameters in the time-domain.

Since the endcaps are cut to a mirror-finish and the cavity sidewall has had damage from the previous high-power test, we expect the resistivities on the endcaps and the sidewall to be different. Assuming the resistivities are constant along each surface, the measured value

<table>
<thead>
<tr>
<th>Initial $Q_0$</th>
<th>Final $Q_0$</th>
<th>Initial $Q_{ext}$</th>
<th>Final $Q_{ext}$</th>
<th>Initial $Q_L$</th>
<th>Final $Q_L$</th>
<th>Initial $\beta$</th>
<th>Final $\beta$</th>
</tr>
</thead>
<tbody>
<tr>
<td>17750 ± 360</td>
<td>16870 ± 310</td>
<td>6850 ± 220</td>
<td>6200 ± 180</td>
<td>4940 ± 40</td>
<td>4530 ± 40</td>
<td>2.59 ± .07</td>
<td>2.72 ± .06</td>
</tr>
</tbody>
</table>

**TABLE IX:** Cavity Q measurements of TE$_{011}$ mode of cavity 1 using a HP8510C network analyzer before and after the second high-power test. The resonant frequency is 11.425 GHz. The errors are due to errors from fits to the data.

<table>
<thead>
<tr>
<th>Initial $Q_0$</th>
<th>Final $Q_0$</th>
<th>Initial $Q_L$</th>
<th>Final $Q_L$</th>
</tr>
</thead>
<tbody>
<tr>
<td>20380 ± 360</td>
<td>18570 ± 320</td>
<td>10940 ± 140</td>
<td>10140 ± 120</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Initial $Q_{1,ext}$</th>
<th>Final $Q_{1,ext}$</th>
<th>Initial $Q_{2,ext}$</th>
<th>Final $Q_{2,ext}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>28180 ± 850</td>
<td>26920 ± 910</td>
<td>144500 ± 5400</td>
<td>130800 ± 5100</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Initial $\beta_1$</th>
<th>Final $\beta_1$</th>
<th>Initial $\beta_2$</th>
<th>Final $\beta_2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.72 ± .02</td>
<td>0.69 ± .02</td>
<td>0.14 ± .005</td>
<td>0.14 ± .005</td>
</tr>
</tbody>
</table>

**TABLE X:** Cavity Q measurements of TE$_{012}$ mode of cavity 1 using a HP8510C network analyzer before and after the second high-power test. The resonant frequency is 17.850 GHz.
of $Q_0$ for each mode determines these resistivities. The results are given in Tab. XI. The theoretical resistivity at room temperature for pure copper is $1.7 \times 10^{-8} \Omega\cdot m$, which is close to the initial value measured for the endcaps. If the resistivity is constant along the endcap surface, then the resistivity increased by approximately 25%.

Constant resistivity is a good approximation before the high-power test; however, the damage to the endcaps shown later indicates that the resistivity will be different within a band around the area of maximum temperature rise. The visible band of damage has a width of 7 - 8 mm, corresponding to temperature rises from 65 - 82 K. The resistivity within this band can be found using the $Q_0$ measurements and taking $\rho = 1.73 \times 10^{-8} \Omega\cdot m$ outside the band. The result, given in Tab. XI, is 60% increase in resistivity. This is one bound to the resistivity change due to pulsed heating, and the constant resistivity approximation gives a lower bound of 25% change. See [17, Tab. 4.10, p. 173] for a more detailed table.

Since the temperature rise is proportional to the square-root of electrical resistivity, the temperature is expected to increase over time as the copper surface becomes degraded from fatigue damage. With these resistivity increases, the maximum temperature rise on the endcaps increased between 10% to 25% to between 90 K and 105 K. Over time, the resistivity is expected to increase due to further damage from an increased temperature rise, which leads to thermal run-away.

The measurements of $Q_0$ in the frequency-domain for the TE\textsubscript{011} mode do indicate a degradation due to an increase in the surface electrical resistivity. The time-domain measurements were harmed by noise and systematics. Some of this error is due to a mismatch of the test
FIG. 23: Measurement of $\beta_1$ during the high-power test for the TE$_{012}$ mode.

cavity with the klystron output cavity as well standing-waves that exist in the coupling arm of the 55-dB directional coupler. See [17, pp. 174–178] for more details. The degradation in $Q_{ext}$ is due to damage to the high-power coupling aperture; however, it is not as extensive as compared to the first test.

Since the measurement of the RF parameters of the TE$_{012}$ mode in the time-domain occurs between klystron pulses, they do not suffer from modulator noise. However, there is a large scatter in the data partly due to vibrations of the endcaps from the flow of cooling water seen as fluctuations in the steady-state value of the reflected power from the diagnostic port. Despite this scatter, Fig. 23 shows a general decreasing trend in $\beta_1$ over time. This is expected from the $Q_0$ degradation due to fatigue damage on the surface of the endcaps. Although there is some degradation of $Q_{ext,1}$ from damage to the diagnostic coupling aperture, there is more degradation of $Q_0$ resulting in an overall decrease in $\beta_1$.

The measurement of $Q_L$ for the TE$_{012}$ in the time-domain was made difficult due to the vibration of the endcaps as well as mode leakage out the high-power port. The leakage may have caused reflections from the magic-tees and the klystron output cavity that could influence the measurement. Hence, an accurate isolated determination of $Q_0$ over time was not possible.
FIG. 24: Measured and theoretical prediction of maximum temperature rise on the endcaps during a high-power pulse. Changes in amplitude and phase of the reflected TE$_{012}$ power are assumed to be caused by temperature rise alone in this measurement. There is discussion of this assumption in the text. The theoretical prediction is based on a 7.3 MW power input. The RF pulse is initiated at time 0 µs.

Using the experimental setup described in Sec. II C, the maximum pulsed temperature rise on the surface of the endcaps may be inferred from the measurement of the change in $Q_0$ of the TE$_{012}$ mode. The outputs from the quadrature mixer determine the amplitude and phase of the reflected power. From this the change in resonant frequency and $Q$ is determined. From our measurements the change in resonant frequency is mostly due to changes in $Q$ with only small effects due to a change in cavity volume from pulsed thermal expansions. The measurement is made difficult by vibrations of the endcaps and modulator noise. The measured signals are low-pass filtered with an FFT to reduce the noise. See [17, pp. 182–186] for details of this measurement.

Fig. 24 shows the measured maximum temperature rise on the endcap along with the theoretical prediction based on an input power of 7.3 MW. The maximum temperature rise is 72 K. This measurement has random and systematic errors. The random errors are associated with residual noise on the waveforms. The systematic errors arise from the error in the resistivity of the endcaps reported in Tab. XI, and the difference between the shapes of the measured and theoretical temperature rises in Fig. 24. Those differences are:

1. The rapid rise and fall times when the X-band power is turned on and off. They are comparable to the cavity fill-time.
2. The apparent temperature rise after the high-power RF has been turned off.

The actual measurements are changes in amplitude and phase of the reflected TE$_{012}$ power, and the measured results in Fig. 24 interpret those changes as being caused by temperature rise alone. In fact, other phenomena also contribute to the amplitude and phase changes. The long-term behavior is the initial manifestation of an acoustic effect that is important but does not affect measurement of the maximum temperature rise. Stress waves are launched on the endcap surfaces that cause the endcap positions in the cavity to vibrate. This is seen by a large ramp and a 4 kHz oscillation in the signal that occurs after the RF pulse turns off [17, p. 188]. The rapid rise and fall of the signal with X-band power is not understood. These features were present throughout the data taking indicating that they are not due to changes in surface properties caused by RF pulsed heating. Given the limits of our understanding, the best measurement of the maximum temperature rise is 82 K based on the input power measurement.

2. Visual Inspection of Copper Endcap Surface

As with the first high-power test, an obvious visual change in the grains of both endcaps is shown in Fig. 25. The width of these regions is between 7 and 8 mm. There is also tarnish
on the surfaces as before; however, the amount of copper sputtered from the high-power coupling aperture is much less than the first high-power test because of the lower input power. Therefore, it is reasonable to conclude that most of the resistivity change reported earlier is due to fatigue damage. There is also no visible evidence of multipacting on the surface. This is reasonable, since the surface magnetic field is 15% less than the first test. In the first test, multipacting only occurred on a half-circle (see Fig. 16) in which a 5% decrease in the magnetic field is enough to prevent multipacting on the other half-circle.

3. Scanning Electron Microscope Inspection of Copper Endcap Surface

As before, the endcaps were examined with a scanning electron microscope using secondary-scattering with a 5 kV electron beam. The amount of cracks on the surface is smaller than in the first test, which is attributed to a lower pulsed temperature rise. As a point of comparison, the picture on the left of Fig. 26 shows a region in the area of maximum temperature rise with a multitude of fatigue slip bands including grains with multiple slip. Multiple slips can occur when the crystal axes of the grain are such that the applied shear stress is greater than a critical value on more than one slip system [21, p. 29]. On the right is a region near the center of the endcap in which the pulsed temperature rise...
FIG. 27: Grain-boundary cracks in the area of maximum temperature rise. The grain boundary is the transition where the whitening due to slip bands stop. A close-up of one crack is on the right where the grain boundary is clear. The length scales are 100.7 µm and 25.0 µm respectively.

rise is close to zero. A grain boundary is evident from a change in contrast in the picture; however, no fatigue slip bands or cracks occur in this area.

The results from this experimental run indicate that cracks only occur along grain boundaries. Grain boundaries are clearly seen between areas that contain fatigue slip bands and areas that do not have them. Figure 27 shows such a case in which a crack clearly occurs along a grain boundary in the area of maximum temperature rise. Cracks tend to nucleate at grain boundaries due to incompatibility of slip from one grain to the next. Incompatible slip will increase the local stress at a grain boundary. See [17, Appendix B] for more pictures of fatigue slip bands and cracks.

As before, a scan along a random diameter of each endcap at constant magnification of 100 was completed. Each snapshot covered an area approximately 0.9 mm by 0.9 mm in size. Arbitrary values were assigned to regions that had cracks or slip bands as with the first test. Figure 28 shows the results of these scans.

The plots show that surface roughening and slip bands occur around the area of maximum temperature rise at the radius 10.6 mm. The offset that occurs in the plot for endcap 1 is due to an offset of 2 mm of the scanned diameter from the center of the endcap. The center of the endcap was approximated at the time the diameters were scanned and determined more precisely afterwards. The small amount of cracks that were found do support the
FIG. 28: Random scans along diameters of each endcap. The solid line corresponds to regions of surface roughening and the dotted line is for regions that contain cracks on the surface. The centers of the endcaps are at position 0 mm.

<table>
<thead>
<tr>
<th>Region</th>
<th>1 (mm)</th>
<th>2 (mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Roughness</td>
<td>4.8</td>
<td>8.8</td>
</tr>
<tr>
<td>Cracks</td>
<td>0.0</td>
<td>0.0</td>
</tr>
</tbody>
</table>

TABLE XII: Widths of regions of surface roughening and cracks for endcaps 1 and 2.

conclusion that surface roughening and slip bands are precursors to crack nucleation which corroborates the findings from the first high-power test. The widths of the regions of surface roughening and cracks are given in Tab. XII.

V. CONCLUSION

We have demonstrated that the cyclic stress induced by pulsed heating beyond the yield stress of fully-annealed OFE copper results in damage to the surface in the form of surface
roughening and cracks. The two experiments have shown such damage to occur at 56 million pulses at a calculated $120 \pm 10$ K temperature rise on the surface and at 86 million pulses at a calculated temperature rise of $82 \pm 3$ K on the surface. The measurements of pulsed temperature rise are in reasonable agreement with the calculations for the second high-power test. From the destruction of the high-power coupling aperture, we also know that 56 million pulses at a temperature rise of approximately 250 K will create enough cracks to cause local melting of the surface. Cracks cause the electrical resistivity of the surface to increase; consequently, the temperature rise increases for the same applied power density.

Since the cavity Q depends on the electrical resistivity of the surface, surface roughening and cracks that ensue will degrade the RF properties of a device long before catastrophic damage like melting and copper sputtering occur. The numbers given above are not thresholds for damage to occur, rather they are observations of damage for the parameters and under the conditions of these experiments. The number of pulses would correspond to only one or two months of accelerator operation, and, therefore, because of thermal run-away they are pulsed temperature rises that cannot be exceeded when accelerator lifetime is an issue.

These results are for a particular cavity and a particular mode, but they can be applied to OFE copper cavities operating in any standing or traveling wave mode. The cavity geometry can be entered into a field calculating computer program, such as MAFIA and GdfidL, and the ratio of accelerating gradient to pulsed temperature rise calculated. Our results then give the maximum accelerating gradient if pulsed heating is the limiting phenomenon. It has been observed in recent tests of NLC structures that reducing the pulsed temperature rise in the input power coupler increased the achievable gradient [22].

Preparation of the cavities and, in particular, the endcap surfaces followed standard SLAC procedures for copper to be used in high-power RF applications. It is known that cyclic fatigue is dependent on surface preparations [8], and the light chemical etch performed on the surface for vacuum preparation may have reduced the lifetime. Grain boundaries are primary sights for crack nucleation, and the etching of material within the grain boundaries can increase the stress concentration in that area. There are open questions about whether the gradient limitation from RF pulsed heating can be reduced by different surface preparations, or, alternatively, through the use of dispersion strengthened materials such as GlidCop® [23], operating at lower ambient temperature or diamond coating [24]. For exam-
ple, it has been shown [3] that the addition of tungsten can increase achievable accelerator gradients by increasing the threshold for damage from RF breakdown.

This experiment shows that pulsed heating is a serious issue with the potential of limiting gradients in future accelerators.

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The authors would like to acknowledge Prof. S. Schultz for his suggestion of using a second mode to measure the pulsed temperature rise in the cavity. We would like to thank G. Bowden for his assistance in the mechanical design of the test cavity. We would also especially like to thank G. Caryotakis, A. Vlieks and A. Menegat for their assistance in the running of these experiments. We also appreciate contributions from D. Yu and T. Lee to an earlier experiment.


[14] 1,1,1 Trichloroethane is a product of Dow Chemical Co.


[16] Oxyban 60 is a product of Thiokol/Dynachem Corp., Tustin, CA.


[22] D. Burke, private communication.

[23] GlidCop is a registered trademark of OM Group, Inc., Cleveland, Ohio.
