HADRONIC PRODUCTION WITH A DRELL-YAN TRIGGER*

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ABSTRACT

We predict a dramatic change in the ratio of cross sections for producing fast \( \pi^+ \)'s and \( \pi^- \)'s in association with a massive dilepton pair as a function of the mass of the pair. For small dilepton mass the \( \pi^+/\pi^- \) ratio should equal that measured in the absence of a dilepton pair. As the mass of the pair rises, the \( \pi^+/\pi^- \) ratio should fall by a factor of 1.7 in the reactions \( p\bar{p} \to \pi(\mu^+\mu^-)X \) and \( p\bar{\pi}^- \to \pi(\mu^+\mu^-)X \), rise by a factor of 2.6 in \( p\pi^+ \to \pi(\mu^+\mu^-)X \), and fall by a factor of about 25\% in \( pp \to \pi(\mu^+\mu^-)X \). At FNAL and CERN SPS energies, triggering at dilepton pairs of masses \( m_{\mu\mu} = 2 - 3 \) GeV should be enough to produce a clearly observable effect.

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The production of massive dilepton pairs by the Drell-Yan mechanism has long been a useful testing ground for parton model ideas. In this note we wish to propose a new example in which the Drell-Yan mechanism may be useful for probing the quark dynamics underlying ordinary small-$p_t$ hadronic fragmentation processes.

The parton model asserts that hadrons may be regarded in the infinite momentum frame as collections of colinearly moving, non-interacting pointlike constituents. Partons may be divided into two classes: valence partons, which carry a sizable fraction (roughly half) of the momentum, as well as the net quantum numbers, of the hadron, and sea partons, whose probability distributions vary as $1/x$ at small $x$ and vanish with some large power of $(1-x)$ at large $x$.

Purely hadronic interactions are mediated by the interactions between the very slow ("wee") partons of the colliding hadrons. For the purposes of this discussion, sea partons may be taken as quarks, antiquarks, or gluons interchangeably.

Now it has recently been observed that the $x$-distributions of fast mesons produced in proton-proton collisions closely resemble the $x$-distributions of the valence partons known from deep inelastic electron-nucleon and neutrino-nucleon scattering. If these mesons were produced from the fast partons by fragmentation, just as hadrons are produced from quarks in $e^+e^-$ annihilation, the meson spectra would fall much more steeply in $x$ than is observed (since one would have to convolute a fragmentation function for mesons out of quarks over a probability function for finding the quark in the initial hadron). This observation has led Das and Hwa to propose that fast mesons are produced in hadronic reactions by the fusion of valence and sea partons, at $x_v$ and $x_s$, respectively, into mesons at $x = x_v + x_s$. Fragmentation processes $A + B \rightarrow M + X$, where the meson $M$ is in the fragmentation region of the hadron $A$, measure then the combined probability
for finding two quarks at once in the wave-function of the hadron $A$, $F_{VS}^A(x_v, x_s)$:

$$\frac{1}{\sigma} E \frac{d\sigma}{d^3p} (A + B \rightarrow M + X) = \int k_{VS}^A(x_v, x_s) \psi^M(x_v, x_s) \, dx_v \, dx_s$$

(1)

where $\sigma$ is the nondiffractive cross section of $A$ on $B$. Here $\psi^M(x_v, x_s)$ is a quark-antiquark recombination function for the meson $M$. We can write it as a two-body piece plus a many-body piece

$$\psi^M(x_v, x_s) = \psi_2(x_v, x_s) \delta \left( 1 - \frac{x_v}{x} - \frac{x_s}{x} \right) + R(x_v, x_s)$$

Due to the difficulty of many-body recombination, the many-body component $R$ becomes competitive only at $x$ very near 1, where it gives rise to Regge behavior.* The two quarks of the two-body component $\psi_2$ carry the valence quantum numbers of the meson $M$.

Now we turn to the production of a fast meson with a Drell-Yan trigger. One parton in the hadron $A$, with momentum fraction $x_a$, annihilates against a parton in the hadron $B$, with momentum fraction $x_b$, to produce a massive dilepton pair with mass $m_{\mu\mu} \left( m_{\mu\mu}^2 / s \equiv \tau = x_a x_b \right)$. This is illustrated in Fig. 1. Then two partons from the hadron $A$ fuse to form the fast meson $M$. Thus, this reaction measures the combined probability for finding three partons in the wave-function of the hadron $A$ simultaneously. The doubly differential cross section, normalized to the Drell-Yan cross section, is

*Phenomenological analyses of inclusive spectra indicate that Regge behavior sets in in most fragmentation processes only at $x \gtrsim 0.85$. The data of pp $\rightarrow \pi^\pm + X$ show no evidence for Regge behavior (i.e., for an $M^2/s$ vs $t$ correlation) for $x$ values up to $x = 0.9$. 


where $Q_i$ is the charge of the $i$th parton and $a, b$ run over all allowed valence and sea partons. In the above formula we have required that one of the partons which fuses into the meson $M$ be a valence parton in hadron $A$, an approximation which is good for fast ($x \gtrsim 0.2$) mesons. In the actual numerical calculations described below the contribution from sea-sea recombinations is included for all values of $x$.

Consider next the process $p \bar{p} \rightarrow \pi^+ (\mu^+ \mu^-) + X$. If the dilepton mass is small, dilepton production will be dominated by sea parton annihilation. The ratio of $\pi^+$ to $\pi^-$ differential cross sections should be the same as is seen in ordinary hadronic reactions: about two, since the proton has two valence up quarks, which preferentially form $\pi^+$, and only one valence down quark, which forms a $\pi^-$. However, as soon as the mass of the dilepton pair becomes large ($\tau \gtrsim 0.3$), valence-valence annihilation dominates over valence-sea and sea-sea annihilations. Since (i) the coupling of the quark to the virtual photon is proportional to the charge of the quark, (ii) the quark and anti-quark that annihilate must have the same flavor, and (iii) the proton (anti-proton) has two up (anti-up) and one down (anti-down) valence quarks, the annihilating quark is eight times
more likely to be an up than a down quark. Since partons that annihilate to form Drell-Yan pairs cannot emerge to produce mesons, the strong preference of the Drell-Yan process to proceed through $u\bar{u}$ annihilation compared to $d\bar{d}$ annihilation completely dilutes the excess of fast up quarks emerging from the collision and, as a result, the ratio of fast $\pi^+$'s over $\pi^-$'s collapses.\(^5\)

To obtain a simple-minded estimate of the effect, we write the proton wave function as

$$\begin{align*}
\nu U D u \bar{u} d \bar{d} s \bar{s}
\end{align*}$$

and assume an SU(3) symmetric sea. We then have

$$\begin{align*}
\sum_{a,b} R_{ab}^Q (\pi^+) &= \frac{16}{9} R_{UU}^U + \frac{2}{9} R_{DD}^U + \frac{8}{9} R_{Uu}^U \\
&\quad + \frac{2}{9} R_{Dd}^U + \frac{16}{9} R_{uU}^U \\
&\quad + \frac{2}{9} R_{Ud}^U + \frac{8}{3} R_{qq}^U \\
\sum_{a,b} R_{ab}^Q (\pi^-) &= \frac{16}{9} R_{uu}^D + \frac{4}{9} R_{UU}^D + \frac{8}{9} R_{uU}^D + \frac{1}{9} R_{dD}^D + \frac{4}{3} R_{qq}^D.
\end{align*}$$

In the above equations, the upper index labels the (valence) quark that goes to form the meson, and the lower indices ($U, D$ for valence quarks, $u, d, s$ (or $q, \bar{q}$, generically) for sea quarks) label the quarks that annihilate into the lepton pair. From Eq. (3) we see that, all $R_{ij}^U/R_{ij}^D$ being equal, $R(\pi^+/\pi^-) = 2$ when sea-sea annihilation dominates, but only $9/8$ when valence-valence annihilation dominates the Drell-Yan process.

We now present our predictions in the context of a specific model. In order to determine without extraneous free parameters the relative magnitudes of the
various terms in Eq. (3), we have written down an improved version of the well-
known Kuti-Weisskopf model.\textsuperscript{6} We write down a valence-plus-n-parton proba-
bility density
\begin{equation}
dP_n(x_i^i, i=1,2,3; x_1, \ldots, x_n) = \prod_{i=1}^{n} \frac{1}{n!} \prod_{j=1}^{n} f_q(x_j) dx_j \delta\left(1 - \sum_i x_i - \sum_j x_j\right)
\end{equation}
and then calculate the multi-parton distributions by summing on n and integrating
over all the unseen partons—all but one, for instance, in the case of F(x). Thus
we automatically satisfy the normalization constraints relating F_Q(x), F_q(x),
F_{Qq}(x_v, x_s), and the three-body probabilities of Eq. (2). The f(x)'s are input
matrix elements for the various partons: we take
\begin{equation}
f_U(x) \sim x^{-\alpha_0},
\end{equation}
where \(\alpha_0 = 1/2\) is the Regge intercept of the non-leading meson trajectories,
\begin{equation}
f_D(x) \sim x^{-\alpha_0} (1-x),
\end{equation}
where the extra power of (1-x) is included to ensure that
\begin{equation}
\lim_{x \to 1} \nu W_2^{en}(x) / \nu W_2^{ep}(x) \approx 1/4
\end{equation}
in agreement with observation and
\begin{equation}
f_q(x) = g^2 x^{-1} (1-x)^k.
\end{equation}
The structure functions are then calculated using techniques similar to those
employed by Kuti and Weisskopf. We have fitted the resulting expressions for
the structure functions into data on deep inelastic electron-nucleon\textsuperscript{7} and
neutrino-nucleon\textsuperscript{8} scattering, varying \(g^2\) and \(R\) as free parameters. With values
\(g^2 = 3.8\) and \(k = 2.7\), the fits are excellent. Our sea distribution vanishes
like \( (1 - x)^7 \), * and our up quark distribution vanishes like \( (1 - x)^{3.8} \). The calculation is similar in the case of pions, where we require that our valence distribution vanish like \( (1 - x)^2 \). Details of the calculation will be presented elsewhere. 11

In Fig. 2 we show our prediction for the ratio of the charged pion spectra vs \( x \).

\[
R(\pi^+ / \pi^-) = \frac{\frac{E}{d^3 p} \frac{d\sigma}{dp} (p + B \rightarrow \pi^+ + x)}{\frac{E}{d^3 p} \frac{d\sigma}{dp} (p + B \rightarrow \pi^- + x) \quad B = \pi^\pm, p, \bar{p}}, \tag{5}
\]

for the no-trigger case and for a Drell-Yan trigger with \( \tau = 0.2 \). Figure 3 shows the above ratios at fixed \( x = 0.5 \) as a function of \( \sqrt{\tau} \). The data are for the reactions \( pp \rightarrow \pi^\pm X \) and are from Ref. 12. The \( pp \) and \( p\pi^- \) ratios fall quickly as valence-valence annihilation takes over from sea-sea and valence-sea annihilation. In \( pp \) Drell-Yan scattering, the \( \pi^+ / \pi^- \) ratio falls much more gradually since there are no valence antiquarks in protons and valence-sea annihilation dominates over sea-sea annihilation only at relatively large \( \sqrt{\tau} \). The \( \pi^+ / \pi^- \) ratio in \( p\pi^+ \) scattering actually rises since a fast \( \pi^+ \) can be produced in association with \( p\pi^+ \) valence annihilation, but if a fast \( \pi^- \) is to be produced from the proton, valence-valence (\( dd \)) annihilation is forbidden. So the \( \pi^- \) cross section

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*The deep inelastic lepton scattering data does not determine the shape of the sea distribution well. We have determined the behavior \( (1 - x)^7 \) from a Drell-Yan model fit to the new high-mass dilepton data. 9 A detailed analysis of meson spectra in proton-proton collisions within the framework of the Das-Hwa model yields also a power which is close to seven. 10*
falls much more rapidly than does the \( \pi^+ \).

That the particle ratios change so quickly as the mass of the lepton pair increases is not an artifact of our model. Rather, it reflects the fact that the densities of valence and sea quarks cross over at quite low \( x \) (\( x \approx 0.05 \))—a fact which is already known from earlier fits to structure functions. That the effect happens at such a low \( \tau \) is obviously a great advantage to experimentalists looking for it, since the Drell-Yan cross section falls steeply as a function of the dilepton mass, and good statistics can be collected only for \( \tau \lesssim 0.3 \), especially with meson beams.

The formalism presented in this note can be easily applied to the analysis of other hadronic fragmentation processes initiated by hard collisions, such as deep inelastic electron-nucleon and neutrino-nucleon scattering and—more speculatively—large \( p_t \) hadron-hadron collisions. An analysis of the influence of a large \( p_t \) trigger to the leading baryon spectra was recently carried out by J. Ranft. 13 A detailed report with many applications is in preparation. 11

In conclusion, we believe that it would be worthwhile to put a considerable experimental effort into testing the above predictions. The observation of an effect of the predicted magnitude and quantum number systematics would provide an important confirmation to the parton model ideas of how hadronic reactions are initiated and how the final state structure of a hadron's constituents governs the spectrum and multiplicity of particles produced in hadronic reactions.

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5. That the properties of jets in hadronic reactions are altered by the presence or absence of a Drell-Yan trigger has also been pointed out by S. J. Brodsky and N. Weiss, SLAC-PUB-1926 (Phys. Rev. D, in press).


10. D. W. Duke and F. E. Taylor, "A Determination of the Sea Quark Distributions in the Proton Single Particle Inclusive Production," in preparation. We thank Drs. Duke and Taylor for informing us about their results prior to publication.


12. Fermilab data from the FNAL–Northern Illinois collaboration, to be published. We thank Dr. F. E. Taylor for providing us with the data. CERN ISR data from the CHLM collaboration, to be published. We thank Prof. J. C. Sens for providing us with the data.

FIGURE CAPTIONS

1. Production of a fast meson M out of hadron A with an associated Drell-Yan trigger. Partons from A with momentum fractions $x_v$ and $x_s$ fuse to form the meson; the dilepton has $M^2 = x_v x_s s$.

2. $R(\pi^+/\pi^-)$ defined in Eq. (5) vs $x^* = x_\pi$ for $pp \rightarrow \pi^\pm X$ (dashed line and data from Ref. 11) and vs $x^* = x_\pi/(1 - \tau^{1/2})$ for $pB \rightarrow \pi^\pm (\mu^+ \mu^-)X$ at $\tau = 0.2$ (continuous lines), with $B = p, \bar{p}, \pi^+, \pi^-$.

3. $R(\pi^+/\pi^-)$ defined in Eq. (5) at $x_\pi = 0.5$ vs $\tau^{1/2} = M^2_{\mu^+ \mu^-}/s$, for the reaction $pB \rightarrow \pi^\pm (\mu^+ \mu^-)X$ with $B = p, \bar{p}, \pi^+, \pi^-$. 
Fig. 1
Fig. 2
Fig. 3