Search for $B$-Meson Decays to Two-body Final States with $a_0(980)$ Mesons


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We present a search for $B$ decays to charmless final states involving charged or neutral $a_0$ mesons. The data sample corresponds to 89 million $B\bar{B}$ pairs collected with the BABAR detector operating at the PEP-II asymmetric-energy $B$ Factory at SLAC. We find no significant signals and determine the following 90% C.L. upper limits: $\mathcal{B}(B^0 \to a_0 \pi^+) < 5.1 \times 10^{-6}$, $\mathcal{B}(B^0 \to a_0 K^+) < 2.1 \times 10^{-6}$, $\mathcal{B}(B^- \to a_0 K^0) < 3.9 \times 10^{-6}$, $\mathcal{B}(B^+ \to a_0^0 \pi^+) < 5.8 \times 10^{-6}$, $\mathcal{B}(B^+ \to a_0^0 K^+) < 2.5 \times 10^{-6}$, and $\mathcal{B}(B^0 \to a_0^0 K^0) < 7.8 \times 10^{-6}$, where in all cases $B$ indicates the product of branching fractions for $B \to a_0 X$ and $a_0 \to \eta \pi$, where $X$ indicates $K$ or $\pi$.

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We report results on measurements of $B$-meson decays to charmless final states with $a_0$ mesons $[1,2]$. Both experimentally and theoretically, most work in charmless two-body $B$ decays has involved states with only pseudoscalar and vector mesons. The only charmless $B$ decay involving scalar mesons that has been observed is $B \to f_0(980)K$ $[2]$. There have been no previously published searches for $B$ decays to final states with $a_0$ mesons. In this paper we search for the decays $B \to a_0 \pi$, $B \to a_0 K$, and $B \to a_0 K^0$ for both charged and neutral $a_0$ mesons. These measurements should provide information both for $B$ decays to scalar mesons and the nature of those mesons.

Some specific predictions can be made for the decays $B \to a_0 \pi^\pm$ if factorization is assumed and if the decay is a “tree” process, that is, one in which a virtual $W$ decays rather than being reabsorbed, as it is in a penguin (loop) process. The dominant such process is shown in Fig. 1(a). The companion tree process, shown in Fig. 1(b), is expected to be greatly suppressed, since the virtual $W$ cannot produce an $a_0$ meson $[4]$. This is a firm prediction of the Standard Model because the weak current has a $G$-parity even vector part and a $G$-parity odd axial-vector part. The latter can produce an axial-vector or pseudoscalar particle while the former produces a vector particle, but neither can produce a $G$-parity odd scalar meson. Penguin processes such as shown in Fig. 1(c) are allowed, but are suppressed relative to the tree processes. Thus the decay $B \to a_0 \pi^\pm$ is expected to be “self-tagging” (the charge of the pion identifies the $B$ flavor). The decays with a kaon in the final state should be dominated by penguin processes (Fig. 1(d)); however, there is a cancellation for these decays $[4]$, so they also should have rather small branching fractions. The diagrams for neutral $B$ decays involving $a_0^0$ mesons are similar to those shown in Fig. 1.

The nature of the $a_0$ is still not well understood. It is thought to be a $q\bar{q}$ state with a possible admixture of a $KK$ bound-state component due to the proximity to the $KK$ threshold $[8,9]$. The $a_0$ mass is known to be about 985 MeV and the dominant decay mode is $a_0 \to \eta \pi$, which is the mode used in the present analysis. A recent analysis $[8]$ that uses this $\eta \pi$ decay channel finds a Breit-Wigner width of $(71 \pm 7)$ MeV, with no better fit obtained when the more correct Flatté shape $[10]$ is used. Also since the branching fraction for $a_0 \to \eta \pi$ is not well known, we report the product branching fraction $\mathcal{B}(B \to a_0 X) \times \mathcal{B}(a_0 \to \eta \pi)$, where $X$ indicates $K$ or $\pi$.

The results presented here are based on data collected with the BABAR detector $[11]$ at the PEP-II asymmetric $e^+e^-$ collider located at the Stanford Linear Accelerator Center. An integrated luminosity of 81.9 $fb^{-1}$, corresponding to 88.9 $\pm$ 1.0 million $B\bar{B}$ pairs, was recorded at the $\Upsilon(4S)$ resonance (center-of-mass energy $\sqrt{s} = 10.58$ GeV).

The track parameters of charged particles are measured by a combination of a silicon vertex tracker, with five layers of double-sided silicon sensors, and a 40-layer central drift chamber, both operating in the 1.5-T magnetic field of a superconducting solenoid. We identify photons and electrons using a CsI(Tl) electromagnetic calorimeter (EMC). Further charged particle identification (PID) is provided by the average energy loss ($dE/dx$) in the tracking devices and by an internally-reflecting, ring-imaging Cherenkov detector (DIRC) covering the central region.

We select $a_0$ candidates from the decay channel $a_0 \to \eta \pi$ with the decays $\eta \to \gamma \gamma \ (\eta \eta)$ and $\eta \to \pi^+ \pi^- \pi^0 \ (\eta_{3\pi})$. We apply the following requirements on the in-
variant masses (in MeV) relevant here: $500 < \eta_\gamma < 585$
for $\eta_\gamma\gamma$, $553 < m_{\pi\pi} < 560$ for $\eta_\pi\pi$, $120 < m_\gamma < 150$
for $\pi^0$, and $775 < m_{\eta\eta} < 1175$ for $a_0 \to \eta\eta$. These
requirements are typically quite loose compared with
typical resolutions in order to achieve high efficiency
and retain sufficient sidebands to characterize the back-
ground for subsequent fitting. We reconstruct $K^0$ can-
didates through the $K^0 \to \pi^+\pi^-$ decay; to obtain a
low-background, well-understood $K^0_S$ sample, we require
$488 < m_{\pi\pi} < 508$ MeV, the three-dimensional flight dis-
tance from the event primary vertex to be greater than
$2 \text{ mm}$, and the angle between flight and momentum vec-
tors, in the plane perpendicular to the beam direction,
to be less than 40 mrad.

We make several PID requirements to ensure the iden-
tity of the pions and kaons. Secondary tracks in $\eta_\pi\pi$ can-
didates must have measured DRC, $dE/dx$, and EMC outputs consistent with pions. For the decays $B \to a_0 h^+$,
where $h^+$ indicates a charged pion or kaon, the par-
ticle $h^+$ must have an associated DRC signal with a
Cherenkov angle within $3.5$ standard deviations of the
expected value for either a $\pi^\pm$ or $K^\pm$ hypothesis (we
describe below the separation between the two hypotheses).

A $B$-meson candidate is characterized kinemati-
cally by the energy-substituted mass $m_{\text{ES}} = [(s + p_B) + p_B]^2 - E_{B}\,^2$, and energy difference $\Delta E = E_B - \frac{1}{2}\sqrt{s}$, where $(E_B, p_B)$ and $(E_0, p_0)$ are the four vectors of the $B$-candidate and the initial
electron-positron system, respectively. The asterisk denotes the $\Upsilon$(4S) frame, and $s$ is the square of the invariant mass of the electron-positron system. The
$\Delta E$ ($m_{\text{ES}}$) resolution is about 40 MeV (3.0 MeV). We require $|\Delta E| \leq 0.2 \text{ GeV}$ and $5.2 \leq m_{\text{ES}} \leq 5.29 \text{ GeV}$.

Backgrounds arise primarily from random combina-
tions in continuum $e^+e^- \to q\bar{q}$ ($q = u, d, s, c$) events. We reduce these by using the angle $\theta_T$ between the thrust
axis of the $B$ candidate in the $\Upsilon$(4S) frame and that
of the rest of the charged tracks and neutral clusters in the
event. The distribution of $|\cos \theta_T|$ is sharply peaked
near 0.9 for combinations drawn from jet-like $q\bar{q}$ pairs,
and nearly uniform for $B$-meson decays. We require $|\cos \theta_T| < 0.9$ for the $a_0 K^0$ decay modes, tightening for
higher-background $a_0 h$ channels: 0.8 for $a_0 (\eta_\pi\pi) h^+$, 0.7
for $a_0 (\eta_\gamma\gamma) h^+$ and $a_0 (\eta_\pi\pi) h^+$, and 0.6 for $a_0 (\eta_\gamma\gamma) h^+$. We also use, in the fit described below, a Fisher discriminant $F$ that combines the angles with respect to the beam axis of the $B$ momentum and $B$ thrust axis (in the $\Upsilon$(4S) frame), and moments describing the energy flow about the $B$ thrust axis $S_{\Upsilon}$.

For the $\eta \to \gamma\gamma$ modes we use additional event-
selection criteria to reduce backgrounds from several
charmless $B$ decay modes. We require $|\cos \theta^\eta_{\text{dec}}| \leq 0.86$, where $\theta^\eta_{\text{dec}}$ is the $\eta$ decay angle, the angle of the photons in the $\eta$ rest frame with respect to the boost direction from the $B$ to that frame. We also require $\cos \theta^a_0_{\text{dec}} \leq 0.8$, where $\theta^a_0_{\text{dec}}$ is the $a_0$ decay angle, defined similarly to $\theta^\eta_{\text{dec}}$,
with sign such that high-momentum $\eta$ mesons populate
the region near +1. From Monte Carlo (MC) simulation
we estimate that the residual charmless $B\bar{B}$
background is less than one event for all decays except
$a_0 (\eta_\gamma\gamma) K^0$ (the notation indicates the decay mode of the
$\eta$ used in reconstructing the $a_0$) and $a_0 (\eta_\gamma\gamma) h^+$, where
we include in the fit a $B\bar{B}$ component, that we find to be
less than 0.5% of the total sample in both cases.

We obtain yields and branching fractions from ex-
tended unbinned maximum-likelihood fits, with input ob-
serverables $\Delta E, m_{\text{ES}}, F, S_{\eta\eta}$ and for charged modes the
PID variables $S_{\pi}$ and $S_{K}$; the last quantities are the
number of standard deviations between the measured
Cherenkov angle and the expectation for pions and kaons.

For each event $i$, hypothesis $j$ (signal, continuum back-
ground, $B\bar{B}$ background), and, for the $a_0h^+$ decays, fla-
vor $k$, we define the probability density function (PDF)

$$P_{jk}^i = P_j(m_{\text{ES}}^i) \mathcal{P}_j(\Delta E_k^i, [S_{\pi}^i]) \mathcal{P}_j(F^i) \mathcal{P}_j(m_{\eta\eta}^i).$$  \hspace{1cm} (1)

The term in brackets for $S$ pertains to the $a_0h^+$ modes.
The absence of correlations among observables (except
between $\Delta E$ and $S$, which both depend on the momen-
tum of the particle $h^+$) in the background $P^i_k$, is con-
ﬁrmed in the (background-dominated) data samples en-
tering the fit. For the signal component, we correct for
effects due to the neglect of small correlations (more de-
tails are provided in the systematics discussion below).

The likelihood function is

$$\mathcal{L} = \exp \left(-\sum_{j,k} Y_{jk} \prod_i \left[ \sum_{j,k} Y_{jk} P_{jk}^i \right] \right),$$  \hspace{1cm} (2)

where $Y_{jk}$ is the yield of events of hypothesis $j$ and flavor
$k$ that we ﬁnd by maximizing $\mathcal{L}$, and $N$ is the number of
events in the sample.

We determine the PDF parameters from simulation for the signal and $B\bar{B}$ background components, and
initial values of the continuum background parameters
from $(m_{\text{ES}}, \Delta E)$ sideband data. We parameterize each of
the functions $\mathcal{P}_{\text{sig}}(m_{\text{ES}}), \mathcal{P}_{\text{sig}}(\Delta E_k), \mathcal{P}_j(F), \mathcal{P}_j(S_{\pi})$ and
the peaking component of $\mathcal{P}_j(m_{\eta\eta})$ with either a 
Gaussian function, the sum of two Gaussian functions
or an asymmetric Gaussian function, as required to de-
scribe the distribution. Slowly varying distributions $(a_0$ candidate mass and $\Delta E$ for combinatoric background)
are represented by second order Chebyshev polynomials.
The $q\bar{q}$ combinatoric background in $m_{\text{ES}}$ is described by
the function $f(x) = x^{1 - x^2}$, with $x \equiv 2m_{\text{ES}}/\sqrt{s}$ and free parameter $\xi$; for $B\bar{B}$ background, we
add a Gaussian function to the quantity $f(x)$. Large
control samples of $B \to D\pi$ decays of topology similar
to the signal are used to verify the simulated resolutions
in $\Delta E$ and $m_{\text{ES}}$. Where the control data samples reveal
differences from MC, we shift or scale the resolution used
in the likelihood fits. Examples of many of these PDF shapes from a very similar analysis are shown in Ref. 11. Additionally, the Breit-Wigner signal parameters for the $a_0$ mass and width are determined from an inclusive dataset that is much larger than the sample used for this analysis. The widths are consistent with expectations from the natural-width values of Ref. 8.

In Table 4 we show for each decay mode the measured product branching fraction, together with the quantities entering into its determination. The free parameters in the fit include the signal and background yields and six parameters describing the background PDFs: slopes for the polynomial shape for the $\Delta$ and $a_0$ mass distributions, the parameter $\xi$ used in the $m_{ES}$ description, and three parameters describing the asymmetric Gaussian function for $F$. For calculation of branching fractions, we assume that the decay rates of the $T(4S)$ to $B^+B^-$ and $B^0\bar{B}^0$ are equal [13]. We combine branching fraction results from the two $\eta$ decay channels by adding the values of $-2\ln L$, adjusted for a small fit bias (see below) and taking proper account of the correlated and uncorrelated systematic errors. In Figs. 2 and 3 we show projections onto $m_{ES}$ and $\Delta E$ of subsamples enriched with a mode-dependent threshold requirement on the signal likelihood (computed ignoring the PDF associated with the variable plotted).

The statistical error on the signal yield is taken as the change in the central value when the quantity $-2\ln L$ increases by one unit from its minimum value. The significance is taken as the square root of the difference between the value of $-2\ln L$ (with systematic uncertainties included) for zero signal and the value at the minimum, with other parameters free in both cases. The 90% confidence level (C.L.) upper limit is taken to be the branching fraction below which lies 90% of the total of the likelihood integral in the positive branching fraction region. Most of the yield uncertainties arising from lack of knowledge of the PDFs have been included in the statistical error since most background parameters are free in the fit. Varying the signal PDF parameters within their estimated uncertainties, we determine the uncertainties in the signal PDFs to be 1–5 events, depending on the final state. The contribution to this uncertainty from the parameterization of the $a_0$ signal shape is small. We verify that the value of the likelihood of each fit is consistent with the expectation found from an ensemble of simulated experiments.

Uncertainties in our knowledge of the efficiency, found from auxiliary studies, include 0.8% $N_t$, 2.5% $N_s$, and 4% for a $K_s^0$ decay, where $N_t$ and $N_s$ are the number of signal tracks and photons, respectively. Our estimate of the number of produced $B\bar{B}$ events is uncertain by 1.1%. The neglect of correlations among observables in the fit can cause a systematic bias; the correction for this bias (between $-3$ and $+3$ events) and assignment of the resulting systematic uncertainty (0.5–2 events) is determined from simulated samples with varying background populations. Published data 8 provide the uncertainties in the $B$-daughter product branching fractions (1–2%). Selection efficiency uncertainties are 0.5–3.5% for $\cos \theta_T$ and 0.5% for PID (for the $a_0h^+$ modes).

In conclusion, we do not find significant signals for these $B$-meson decays to states with $a_0$ mesons. The measured branching fractions and 90% C.L. upper limits

FIG. 2: Projections of the $B$-candidate $m_{ES}$ and $\Delta E$ for (a, b) $a_0h^+$, and (c, d) $a_0h^+$. Points with errors represent data, solid curves the full fit functions, dashed curves the background functions (the peaking $BB$ background component is negligible), and the dotted curve shows the kaon portion of the signal. These plots are made with a minimum requirement on the likelihood and thus do not show all events in the data samples.

FIG. 3: Projections of the $B$-candidate $m_{ES}$ and $\Delta E$ for (a, b) $a_0K^0_S$, and (c, d) $a_0K^0_S$. Points with errors represent data, solid curves the full fit functions, and dashed curves the background functions. These plots are made with a minimum requirement on the likelihood and thus do not show all events in the data samples.
TABLE I: Signal yield, detection efficiency $\epsilon$, daughter branching fraction product ($\prod B_j$), significance (including systematic uncertainties, taken to be zero if corrected yield is negative), measured product branching fraction (see text), and the 90% C.L. upper limit on this branching fraction.

| Mode | Yield $\beta$(%) | $\prod B_j$(%) | Signif. | $B(10^{-6})$ | UL$(10^{-6})$
|------|-----------------|----------------|---------|--------------|-----------
| $a_0 (\pi \pi^- \gamma)$ $\pi^+$ | $18^{+11}_{-10}$ | 18.8 | 39.4 | 1.3 | $2.3^{+1.5}_{-1.0}$ ± 0.9 |
| $a_0 (\pi \pi^- \gamma)$ $\pi^-$ | $15^{+9}_{-8}$ | 15.5 | 22.6 | 1.6 | $3.9^{+2.3}_{-1.5}$ ± 1.0 |
| $a_0 \pi^+$ | | | | | 2.0 $2.8^{+1.6}_{-1.3} + 0.7$ < 5.1 |
| $a_0 (\pi \pi^- \gamma) K^+$ | $2^{+6}_{-4}$ | 17.9 | 39.4 | 0.1 | $0.0^{+0.6}_{-0.3}$ ± 0.3 |
| $a_0 (\pi \pi^- \gamma) K^-$ | $13^{+8}_{-6}$ | 14.9 | 22.6 | 1.1 | $3.1^{+2.7}_{-1.3}$ ± 1.9 |
| $a_0 K^+$ | | | | | 0.4 $0.4^{+1.0}_{-0.8} ± 0.2$ < 2.1 |
| $a_0 (\pi \pi^- \gamma) K^0$ | $-12^{+8}_{-12}$ | 21.4 | 13.5 | 0.0 | $-3.7^{+2.9}_{-2.3} ± 0.9$ |
| $a_0 (\eta \pi) K^0$ | $0^{+7}_{-5}$ | 15.8 | 7.9 | 0.5 | $2.7^{+6.4}_{-4.3} ± 1.9$ |
| $a_0 K^0$ | | | | | $0.6^{+1.5}_{-1.4} ± 0.8$ < 3.9 |
| $a_0 (\pi \pi^- \gamma) K^0$ | $17^{+11}_{-9}$ | 12.8 | 39.4 | 1.4 | $3.1^{+2.4}_{-1.9} ± 1.2$ |
| $a_0 (\pi \pi^- \gamma) K^0$ | $1^{+8}_{-6}$ | 9.5 | 22.6 | 0.3 | $1.2^{+3.9}_{-2.0} ± 1.7$ |
| $a_0 \pi^+$ | | | | | | 1.4 $2.6^{+1.7}_{-1.4} ± 1.0$ < 5.8 |
| $a_0 (\pi \pi^- \gamma) K^+$ | $0^{+5}_{-3}$ | 12.4 | 39.4 | 0.3 | $0.3^{+1.1}_{-0.6} ± 0.4$ |
| $a_0 (\eta \pi) K^+$ | $6^{+3}_{-5}$ | 9.1 | 22.6 | 0.5 | $1.9^{+2.1}_{-1.4} ± 2.5$ |
| $a_0 K^+$ | | | | | 0.4 $0.4^{+1.0}_{-0.8} ± 0.3$ < 2.5 |
| $a_0 (\eta \pi) K^0$ | $0^{+3}_{-2}$ | 15.0 | 13.3 | 0.5 | $1.4^{+3.7}_{-2.3} ± 1.2$ |
| $a_0 (\eta \pi) K^0$ | $4^{+3}_{-2}$ | 9.7 | 7.8 | 1.2 | $6.6^{+2.4}_{-2.8} ± 2.8$ |
| $a_0 K^0$ | | | | | 1.0 $2.8^{+3.4}_{-2.4} ± 1.1$ < 7.8 |

are given in Table I. Assuming $\eta \pi$ to be the dominant $a_0$ decay mode, we rule out the predictions for the decay $B^- \rightarrow a_0 K^0$ derived in Ref. [13].

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[1] Throughout this note, when we refer to $a_0$, we mean specifically $a_0(980)$.