Measurement of the $B^0 \rightarrow D^{**}+\ell^-\bar{\nu}_\ell$ Decay Rate and $|V_{cb}|$

(The BABAR Collaboration)

1 Laboratoire de Physique des Particules, F-74941 Annecy-le-Vieux, France
2 Università di Bari, Dipartimento di Fisica e INFN, I-70126 Bari, Italy
3 Institute of High Energy Physics, Beijing 100039, China
4 University of Bergen, Inst. of Phys., N-5007 Bergen, Norway
5 Lawrence Berkeley National Laboratory and University of California, Berkeley, CA 94720, USA
6 University of Birmingham, Birmingham, B15 2TT, United Kingdom
7 Ruhr Universität Bochum, Institut für Experimentalphysik 1, D-44780 Bochum, Germany
8 University of Bristol, Bristol BS8 1TL, United Kingdom
9 University of British Columbia, Vancouver, BC, Canada V6T 1Z1
10 Brunel University, Uxbridge, Middlesex UB8 3PH, United Kingdom
11 Budker Institute of Nuclear Physics, Novosibirsk 630090, Russia
12 University of California at Irvine, Irvine, CA 92617, USA
13 University of California at Los Angeles, Los Angeles, CA 90024, USA
14 University of California at Riverside, Riverside, CA 92521, USA
15 University of California at Santa Barbara, Santa Barbara, CA 93106, USA
16 University of California at Santa Cruz, Institute for Particle Physics, Santa Cruz, CA 95064, USA
17 California Institute of Technology, Pasadena, CA 91125, USA
University of Cincinnati, Cincinnati, OH 45221, USA
University of Colorado, Boulder, CO 80309, USA
Colorado State University, Fort Collins, CO 80523, USA
Technische Universität Dresden, Institut für Kern- und Teilchenphysik, D-01062 Dresden, Germany
Ecole Polytechnique, LLR, F-91128 Palaiseau, France
University of Edinburgh, Edinburgh EH9 3JZ, United Kingdom
Università di Ferrara, Dipartimento di Fisica and INFN, I-44100 Ferrara, Italy
Florida A&M University, Tallahassee, FL 32307, USA
Laboratori Nazionali di Frascati dell’INFN, I-00044 Frascati, Italy
Università di Genova, Dipartimento di Fisica and INFN, I-16146 Genova, Italy
Harvard University, Cambridge, MA 02138, USA
Universität Heidelberg, Physikalisches Institut, Philosophenweg 12, D-69120 Heidelberg, Germany
Imperial College London, London, SW7 2AZ, United Kingdom
University of Iowa, Iowa City, IA 52242, USA
Iowa State University, Ames, IA 50011-3160, USA
Université de l’Acelerateur Linéaire, F-91898 Orsay, France
Queen Mary, University of London, E1 4NS, United Kingdom
University of London, Royal Holloway and Bedford New College, Egham, Surrey TW20 0EX, United Kingdom
University of Louisville, Louisville, KY 40292, USA
University of Manchester, Manchester M13 9PL, United Kingdom
University of Maryand, College Park, MD 20742, USA
University of Massachusetts, Amherst, MA 01003, USA
Massachusetts Institute of Technology, Laboratory for Nuclear Science, Cambridge, MA 02139, USA
McGill University, Montréal, QC, Canada H3A 2T8
Università di Milano, Dipartimento di Fisica and INFN, I-20133 Milano, Italy
University of Mississippi, University, MS 38677, USA
Université de Montréal, Laboratoire René J. A. Lévesque, Montréal, QC, Canada H3C 3J7
Mount Holyoke College, South Hadley, MA 01075, USA
Università di Napoli Federico II, Dipartimento di Scienze Fisiche and INFN, I-80126, Napoli, Italy
NIKHEF, National Institute for Nuclear Physics and High Energy Physics, NL-1009 DB Amsterdam, The Netherlands
University of Notre Dame, Notre Dame, IN 46556, USA
Oak Ridge National Laboratory, Oak Ridge, TN 37831, USA
Ohio State University, Columbus, OH 43210, USA
University of Oregon, Eugene, OR 97403, USA
University di Padova, Dipartimento di Fisica and INFN, I-35131 Padova, Italy
Université Paris VI et VII, Laboratoire de Physique Nucléaire et de Hautes Energies, F-75252 Paris, France
Università di Pavia, Dipartimento di Elettronica and INFN, I-27100 Pavia, Italy
University of Pennsylvania, Philadelphia, PA 19104, USA
Università di Perugia, Dipartimento di Fisica and INFN, I-06100 Perugia, Italy
Università di Pisa, Dipartimento di Fisica, Scuola Normale Superiore and INFN, I-56127 Pisa, Italy
Prairie View A&M University, Prairie View, TX 77446, USA
Princeton University, Princeton, NJ 08544, USA
Università di Roma La Sapienza, Dipartimento di Fisica and INFN, I-00185 Roma, Italy
Universität Rostock, D-18051 Rostock, Germany
Rutherford Appleton Laboratory, Chilton, Didcot, Oxon, OX11 0QX, United Kingdom
DSM/Dapnia, CEA/Saclay, F-91191 Gif-sur-Yvette, France
University of South Carolina, Columbia, SC 29208, USA
Stanford Linear Accelerator Center, Stanford, CA 94309, USA
Stanford University, Stanford, CA 94305-4060, USA
State Univ. of New York, Albany, NY 12222, USA
University of Tennessee, Knoxville, TN 37996, USA
University of Texas at Austin, Austin, TX 78712, USA
University of Texas at Dallas, Richardson, TX 75083, USA
Università di Torino, Dipartimento di Fisica Sperimentale and INFN, I-10125 Torino, Italy
Università di Trieste, Dipartimento di Fisica and INFN, I-34127 Trieste, Italy
Vanderbilt University, Nashville, TN 37235, USA
University of Victoria, Victoria, BC, Canada V8W 3P6
University of Wisconsin, Madison, WI 53706, USA
Yale University, New Haven, CT 06511, USA
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This work is dedicated to the memory of Paolo Poropat.
We present a measurement of the Cabibbo-Kobayashi-Maskawa matrix element $|V_{cb}|$ based on a sample of about 53,700 $B^0 \to D^{*+} \ell^- \bar{\nu}_\ell$ decays observed by the BABAR detector. We obtain the branching fraction averaged over $\ell = e, \mu$, $\mathcal{B}(B^0 \to D^{*+} \ell^- \bar{\nu}_\ell) = (4.90 \pm 0.07{(\text{stat.})}^{+1.00}_{-0.31{(\text{syst.})})} \%$.

We measure the differential decay rate as a function of $w$, the relativistic boost $\gamma$ of the $D^{*+}$ in the $B^0$ rest frame. By extrapolating $d\Gamma/dw$ to the kinematic limit $w \to 1$, we extract the product of $|V_{cb}|$ and the axial form factor $A_1(w = 1)$. We combine this measurement with a lattice QCD calculation of $A_1(\gamma = 1)$ to determine $|V_{cb}| = (38.7 \pm 0.3{(\text{stat.})} \pm 1.7{(\text{syst.})}^{+1.5}_{-1.3}{(\text{theory})}) \times 10^{-3}$.

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In the Standard Model of electroweak interactions, the Cabibbo-Kobayashi-Maskawa (CKM) matrix describes the flavor mixing among quarks and determines the strength of CP violation by a single non-trivial weak phase. The CKM matrix element $V_{cb}$ measures the weak coupling of the $b$ to the $c$ quark. In this Letter, we present measurements of the branching fraction $\mathcal{B}(B^0 \to D^{*+} \ell^- \bar{\nu}_\ell)$ [1] and $|V_{cb}|$. The rate for this weak decay is proportional to $|V_{cb}|^2$ and is influenced by strong interactions through form factors, which are not known a priori. In the limit of infinite $b$-quark and $c$-quark masses, these form factors are determined by a single Isgur-Wise function [2]. The value of this function when the $D^{*+}$ is at rest relative to the $B^0$ has been computed for finite $c$- and $b$-quark masses using lattice QCD [3].

In this analysis, we measure the differential decay rate $d\Gamma/dw$, where $w$ is the product of the four-velocities of the $B^0$ and $D^{*+}$, and corresponds to the relativistic boost $\gamma$ of the $D^{*+}$ in the $B^0$ rest frame. We extrapolate the rate to the zero-recoil limit $w = 1$, and use the theoretical result for the form factor there [3] to extract $|V_{cb}|$.

The analysis is based on a data sample of 79 fb$^{-1}$ recorded on the $\Upsilon(4S)$ resonance and 9.6 fb$^{-1}$ recorded 40 MeV below it, with the BABAR detector [4] at the PEP-II asymmetric-energy $e^+e^-$ collider. We use samples of GEANT Monte Carlo (MC) simulated events that correspond to about three times the data sample size.

The momenta of charged particles are measured by a tracking system consisting of a five-layer silicon vertex tracker (SVT) and a 40-layer drift chamber (DCH), operating in a 1.5-T solenoidal magnetic field. Charged particles of different masses are distinguished by their energy loss in the tracking devices and by a ring-imaging Cherenkov detector. Electromagnetic showers from electrons and photons are measured in a CsI(Tl) calorimeter. Muons are identified in a set of resistive plate chambers inserted in the iron flux-return yoke of the magnet.

We select events that contain a $D^{*+}$ candidate and an oppositely charged electron or muon with momentum $1.2 < p_\ell < 2.4$ GeV/c. (Unless explicitly stated otherwise, momenta are measured in the $\Upsilon(4S)$ rest frame, which does not coincide with the laboratory frame, due to the boost of the PEP-II beams.) In this momentum range, the electron (muon) efficiency is about 90% (60%) and the hadron misidentification rate is typically 0.2% (2.0%). We select $D^{*+}$ candidates in the momentum range $0.5 < p_{D^{*+}} < 2.5$ GeV/c in the channel $D^{*+} \to D^0 \pi^+_\ell$, with the $D^0$ decaying to $K^-\pi^+$, $K^-\pi^+\pi^-\pi^+$, or $K^-\pi^+\pi^0$. The charged hadrons of the $D^0$ candidate are fit to a common vertex and the candidate is rejected if the fit probability is less than 0.1%. We require the invariant mass of the hadrons to be within 17 MeV/c$^2$ of the $D^0$ mass for the decays to only charged particles, and 34 MeV/c$^2$ for $K^-\pi^+\pi^0$ decays. For $D^0 \to K^-\pi^+$, we accept only candidates from portions of the Dalitz plot where the square of the decay amplitude, as determined by Ref. [5], is at least 10% of the maximum it attains anywhere in the plot. For the pion from $D^{*+}$ decay, $\pi^+_\ell$, the momentum in the laboratory frame must be less than 450 MeV/c, and the transverse momentum greater than 50 MeV/c.

In semileptonic decays, the presence of an undetected neutrino complicates the separation of the signal from background. We compute a kinematic variable with considerable power to reject background by determining, for each $B$-decay candidate, the cosine of the angle between the momentum of the $B^0$ and of the $D^{*+}\ell^-$ pair, under the assumption that only a massless neutrino is missing:

$$
\cos\theta_{B^0,D^{*+}\ell^-} = \frac{2E_{\not\not P_e}E_{D^{*+}\ell^-} - M_{B^0}^2 - M_{D^{*+}\ell^-}^2}{2p_{D^{*+}\ell^-}}.
$$

This quantity constrains the direction of the $B^0$ to lie along a cone whose axis is the direction of the $D^{*+}\ell^-$ pair, but with an undetermined azimuthal angle about the cone’s axis. The value of $w$ varies with this azimuthal angle; we take the average of the minimum and maximum values as our estimator $\bar{w}$ for $w$. This results in a resolution of 0.04 on $w$. We divide the sample into 10 bins in $\bar{w}$ from 1.0 to 1.5, with the last bin extending to the kinematic limit of 1.504.

The selected events are divided into six subsamples, corresponding to the two leptons and the three $D^0$ decay modes. In addition to signal events, each subsample contains backgrounds from six different sources: combinatoric (events from $B\bar{B}$ and continuum in which at least one of the hadrons assigned to the $D^{*+}$ does not originate from $D^{*+}$ decay); continuum ($D^{*+}\ell^-\pi^+$ combinations from $e^+e^- \rightarrow c\bar{c}$); fake leptons (combined with a true $D^{*+}$); uncorrelated background ($\ell$ and $D^{*+}$ produced in the decay of two different $B$ mesons); events.
from $B \to D^{*+} \pi^- \nu \ell$ decays; and correlated background events due to the processes $\bar{B}^0 \to D^{*+} \pi^- \ell^\tau$, $\tau^- \to \ell^- X$ and $\bar{B}^0 \to D^{*+} X_c$, $X_c \to \ell^- Y$. We estimate correlated background (which amounts to less than 0.5% of the selected candidates) from Monte Carlo simulation based on measured branching fractions [6], while we determine all the others from the data. Except for the combinatoric background, all other background sources exhibit a peak in the $\Delta M = M_{D^{*+}} - M_{D^0}$ distribution, where $M_{D^{*+}}$ and $M_{D^0}$ are the measured $D^{*+}$ and $D^0$ candidate masses.

We determine the composition of the subsamples in each $\bar{w}$ bin in two steps. First we estimate the amount of combinatoric, continuum, and fake-lepton background by fitting the $\Delta M$ distributions in the range $0.139 < \Delta M < 0.165$ GeV/$c^2$ simultaneously to three sets of events: data recorded on resonance, data taken below the $T(4S)$ (thus containing only continuum background), and data in which tracks that fail very loose lepton-selection criteria are taken as surrogates for fake leptons. The distributions are fit with the sum of two Gaussian functions with a common mean and different widths to describe $D^{*+} \to D^0 \pi^+_\ell$ decays and empirical functions, based on the simulation, for the combinatoric background. The four parameters of the Gaussian functions are common, while the fraction of peaking events and the parameters describing the combinatoric background differ for the signal, off-peak, and fake-lepton samples.

Since the $\Delta M$ resolution depends on whether or not the $\pi^+_\ell$ track is reconstructed only in the SVT or in the SVT and DCH, the fits are performed separately for these two classes of events. We rescale the number of continuum and fake-lepton events in the mass range $0.143 < \Delta M < 0.148$ GeV/$c^2$, based on the relative on- and off-resonance luminosity and measured hadron misidentification probabilities. In the subsequent analysis we fix the fraction of combinatoric, fake-lepton, and continuum events in each $\bar{w}$ bin to the values so obtained. Figure 1 shows the $\Delta M$ fit results for the on-resonance data.

In a second step, we fit the $\cos \theta_{B^0,D^{*\ell}}$ distributions in the range $-1 < \cos \theta_{B^0,D^{*\ell}} < 5$ and determine the signal contribution and the normalization of the uncorrelated and $B \to D^{*+} \pi^- \nu \ell$ backgrounds. Neglecting resolution effects, signal events meet the obvious constraint $|\cos \theta_{B^0,D^{*\ell}}| < 1$, while $B \to D^{*+} \pi^- \nu \ell$ events extend below $-1$, and uncorrelated background events are spread over the entire range considered.

We perform the fit separately for each $\bar{w}$ bin, with the individual shapes for the signal and for each of the six background sources taken from MC simulation, specific for each of the six subsamples. Signal events are generated with the form-factor parameterization of Ref. [7], tuned to the results from CLEO [8]. Radiative decays ($\bar{B}^0 \to D^{*+} \ell^- \nu \ell$) are modeled by PHOTOS [9] and treated as signal. $B \to D^{*+} \ell^- \nu \ell$ decays involving orbitally excited charm mesons are generated according to the ISGW2 model [10], and decays with nonresonant charm states are generated following the prescription in Ref. [11]. To reduce the sensitivity to statistical fluctuations we require that the ratio of all three $D^{*0}$ decay modes and for the electron and muon samples. Fit results are shown in Fig. 2. In total, there are 70,822 events in the range $|\cos \theta_{B^0,D^{*\ell}}| < 1.2$. The average fraction of these events that are signal is $(75.9 \pm 0.3)\%$, where the error is only statistical.

To extract $|V_{cb}|$, we compare the signal yields to the expected differential decay rate

$$d\Gamma/dw = \frac{G_F^2}{48\pi^3} M_{D^{*+}}^2 (M_{B^0} - M_{D^{*+}})^2 G(w) F(w)^2 |V_{cb}|^2,$$

where

$$G(w) = \sqrt{w^2 - 1(w + 1)} \left( 1 + 4 \frac{w}{w + 1} \frac{1 - 2wr + r^2}{(1 - r)^2} \right)$$

is a phase-space factor, $r = M_{D^{*+}}/M_{B^0}$. We parameterize the form factor $F(w)$ with a Taylor expansion:

$$F(w) \approx F(1) (1 - \rho_F^2(w - 1) + c(w - 1)^2),$$

FIG. 1: Yields of on-resonance data (points) and the results of the fit (line) to the $\Delta M$ distribution, with contributions from continuum, fake-lepton, and combinatoric-$D^{*+}$ backgrounds summed over all $\bar{w}$ bins.

FIG. 2: Yields of on-resonance data (points) and the results of the fit (histograms) to the $\cos \theta_{B^0,D^{*\ell}}$ distribution, summed over all $\bar{w}$ bins.
where we neglect terms of order greater than two in \((w - 1)\). We fit the data to determine \(\mathcal{F}(1)|V_{cb}|, \rho_F\) and \(c\).

Dispersion relations inspired by QCD can be used to constrain the shape of the form factor and reduce the number of parameters to be determined [7, 12]. Therefore we consider also the parameterization proposed in Ref. [7], which relates \(\mathcal{F}(w)\) to the axial-vector form factor \(A_1(w)\) according to the following expression:

\[
\mathcal{F}(w)^2G(w) = A_1(w)^2\sqrt{w-1}(w+1)^2 \left\{ 2 \frac{1-2wr+r^2}{(1-r)^2} \right\} \times \left( 1 + R_1(w) \frac{w-1}{w+1} \right) + \left[ 1 + (1-R_2(w)) \frac{w-1}{1-r} \right]^2,
\]

where \(R_1(w) \approx R_1(1) - 0.12(w-1) + 0.05(w-1)^2, R_2(w) \approx R_2(1) + 0.11(w-1) - 0.06(w-1)^2\), and we use the values \(R_1(1) = 1.18 \pm 0.32\) and \(R_2(1) = 0.71 \pm 0.21\) measured by CLEO [8]. Using dispersion relations we express the ratio \(A_1(w)/A_1(1)\) as a function of a single unknown parameter \(\rho_A^2\):

\[
\frac{A_1(w)}{A_1(1)} \approx 1 - 8\rho_A^2 (z + (53\rho_A^2 - 15)z^2 - (231\rho_A^2 - 91)z^3),
\]

where \(z = (\sqrt{w+1} - \sqrt{2})/(\sqrt{w+1} + \sqrt{2})\). It must be noted that, for \(w \to 1\), \(A_1(w) \to \mathcal{F}(1)\), so we expect \(A_1(1) \approx \mathcal{F}(1)\).

We perform a least-squares fit of the sum of the observed signal plus background yields to the expected yield in the ten bins in \(\bar{w}\). We define for each of the six data subsamples

\[
\chi^2 = \sum_{i=1}^{10} \frac{(N^i_{\text{data}} - N^i_{\text{MC}} - \sum_{j=1}^{N_{\text{MC}}} W_j^i)^2}{\sigma_{\text{MC}}^2 + \sum_{j=1}^{N_{\text{MC}}} W_j^i^2},
\]

where \(N^i_{\text{data}}\) is the number of observed events in the \(i\)th bin; \(N^i_{\text{MC}}\) and \(\sigma_{\text{MC}}^2\) are the number of estimated background events and its error. The backgrounds are fixed to the estimated rates. The expected signal yield is calculated at each step of the minimization from the reweighted sum of \(N_{\text{MC}}\) simulated events. Each weight is the product of four weights, \(W_j^i = W^C W_j^{e,i} W^S W_j^{f,j,i}\). The factors \(W^C\), \(W_j^{f,j,i}\) do not vary during the minimization, while the terms \(W^S\), \(W_j^{f,j}\) depend on parameters which are determined by the fit, and vary at each step of the minimization.

The first factor \(W^C\) accounts for relative normalization of the data and MC samples, and is common to all subsamples. \(W^C\) depends on the total number of \(B\bar{B}\) events, \(N_{\text{MC}}^B = (85.9 \pm 0.9) \times 10^6\), on the fraction of \(B^0\) events, \(f_{\text{MC}} = 0.489 \pm 0.012\) [6], on the branching fraction \(B(D^{+}\to D^0\pi^+) = 0.677 \pm 0.005\) [6], and on the \(B^0\) lifetime \(\tau_{B^0} = 1.536 \pm 0.014\) ps [6]. \(W_j^{f,j,i}\) accounts for differences in reconstruction and particle-identification efficiencies predicted by the Monte Carlo simulation and measured with data, as a function of particle momentum. Only the \(\pi^+_j\) tracking efficiency varies significantly with \(\bar{w}\).

The weight \(W^S\) accounts for potential small differences in efficiencies for the six data subsamples and allows for adjustments of the \(D^0\) branching fractions, properly dealing with the correlated systematic uncertainties. It is the product of several scale factors that are floating parameters in the fit, each constrained to an expected value with a corresponding experimental error. For instance, to account for the uncertainty in the multiplicity-dependent tracking efficiency, we introduce a factor \(W_{trk}^{S} = 1 + N_{trk}\delta_{trk}\), where \(N_{trk}\) is the number of charged tracks in the \(D^{+}\to D^{0}\pi^{0}\) candidates in each sample and \(\delta_{trk}\) is constrained to zero within the estimated uncertainty in the single-track efficiency: \(\pm 0.8\%\). Similarly, correction factors are introduced to adjust lepton, kaon, and \(\pi^0\) efficiencies, and \(D^0\) branching fractions, taking into account correlations.

The fourth factor, \(W_{f,j,i}^{f,j}\), adjusts the fitted decay distribution relative to the one used in the generation of the MC events. This term depends on \(|V_{cb}|\) and on the shape parameters. It is a function of \(w\) and is determined for each simulated event at each step of the fit.

Figure 3 (top) compares the observed signal and background yields, summed over all six subsamples, with the result of the fit. Figure 3 (bottom) illustrates the extrapolation to \(w = 1\) for the two form-factor parameterizations. The numerical values obtained for the two different form-factor parameterizations are listed in Table I. For both fits, the \(\chi^2\) per degree of freedom is satisfactory, and the scale factors introduced to allow adjustments of the efficiencies and branching fractions deviate from their default values by less than one standard deviation.

| Table I: Results of the fits to \(d\Gamma/d\bar{w}\) for the two parameterizations of the form factor. The errors stated include statistical error of the data and MC as well as uncertainties due to tracking, particle identification, and \(D^0\) branching fractions that are directly assessed in the fit procedure.

| \(A_1(1)|V_{cb}|\times 10^4\) | \(\rho^2\) | \(c\) | \(\chi^2/\text{ndf}\) |
|----------------------|-------|-----|----------------|
| \(\mathcal{F}\)         | 35.0 ± 0.9 | 0.95 ± 0.09 | 0.54 ± 0.17 | 67/57 |
| \(A_1\)                | 35.5 ± 0.8 | 1.29 ± 0.03 | -         | 69/58 |

In Table II we present a summary of the statistical and systematic uncertainties. From the fit to the \(\bar{w}\) distribution we obtain errors that combine the statistical error with systematic errors introduced by the uncertainties in scale factors. We separate the various contributions in the following way: first, we extract the statistical errors by fixing all scale factors to their fitted values. The systematic errors due to the uncertainties in a given scale factor is extracted from a separate fit in which this scale factor is fixed. We take the square root of reduction in
vertex reconstruction is common to all samples and independent of are independent of a vector meson to two pseudoscalar mesons. We define the efficiency for the low-momentum pion from the samples with and without cuts on the vertex probability. Decays selected from generic hadronic events. For fixed from the angular distribution of the frame. We use a large set of \( D^{\ast+} \rightarrow D^0 \pi^+ \), \( D^0 \rightarrow K^- \pi^+ \) decays selected from generic hadronic events. For fixed values of the \( D^\ast+ \) momentum, we compare the observed angular distribution to the one expected for the decay of a vector meson to two pseudoscalar mesons. We define the relative efficiency as the ratio of the observed to the expected distribution and parameterize its dependence on the laboratory momentum of the \( \pi^\ast_+ \). The study is performed in several bins of the polar angle of the detector. We perform the measurement in the data and in the simulation, and we find that the functions parameterizing the efficiency are consistent within the statistical errors. To assess the systematic uncertainty on \( |V_{cb}| \), we vary the parameters of the efficiency function by their uncertainty, including correlations. We add in quadrature the uncertainty in the absolute scale, as determined using high-momentum tracks reconstructed in both the SVT and the DCH. We obtain a systematic error of \( \pm 1.1\% \) on \( |V_{cb}| \).

**TABLE II:** Summary of uncertainties.

| Source of Uncertainty | \( \delta(A_1(|V_{cb}|)) \) (%) | \( \delta P_{A_1} \) | \( \delta B \) (%) |
|-----------------------|-------------------------------|----------------|-------|
| Data and MC statistics | 0.7 | 0.03 | 1.4 |
| \( B(D^0 \rightarrow K^- \pi^+) \) | 1.1 | - | 2.2 |
| \( B(D^0 \rightarrow K^- \pi^+ \pi^- \pi^0) \) | 0.4 | - | 0.8 |
| \( B(D^0 \rightarrow K^- \pi^+ \pi^0) \) | 0.5 | - | 1.0 |
| Particles identification | 1.1 | - | 2.2 |
| Tracking \& \( K^0 \) reconstr. | 1.3 | - | 2.6 |
| Partial Sum | 2.2 | 0.03 | 4.5 |
| \( B^+ \) lifetime | 0.5 | - | - |
| Number of \( B\overline{B} \) | 0.6 | - | 1.2 |
| \( B(D^{\ast+} \rightarrow D^0 \pi^+) \) | 0.4 | - | 0.7 |
| \( B(T(4S) \rightarrow B^0 \overline{B}^0) \) | 1.2 | - | 2.5 |
| \( D^{\ast+} \ell^- \) vertex efficiency | 0.5 | - | 1.0 |
| \( \pi_s \) efficiency | 1.1 | 0.01 | 1.9 |
| \( D^{\ast+} \pi \ell \nu \) sample composition | 1.8 | 0.06 | 2.0 |
| \( B \) momentum | 0.3 | - | 0.7 |
| Radiative corrections | 0.2 | 0.01 | 0.4 |
| \( \cos \theta_{B^0, D^{\ast+}} \) & \( \tilde{w} \) fit method | 0.8 | 0.02 | 1.6 |
| \( R_0(1) \) and \( R_0(1) \) | \( 0.6 \) | \( 0.26 \) | \( 0.39 \) |
| Total Error | \( +4.4 \) | \( 0.27 \) | \( +4.3 \) |

The largest error in the background subtraction is due to the uncertainty in the composition and form factors of the \( D^{\ast+} \pi \ell^- \nu_\ell \) decays. We consider twelve different \( D^{\ast+} \pi \) states, narrow and wide, as well as nonresonant \( D^{\ast+} \pi \). To assess the impact of these decays on the fit we repeat the analysis assuming that only one mode at a time populates the whole sample, and then take as the systematic error half the difference between the maximum and minimum fitted parameters.

We assess the effect of the uncertainty in the average \( B^0 \) momentum, as determined from a sample of fully reconstructed hadronic \( B \) decays on the fit results. We take into account an uncertainty of \( \pm 30\% \) in the emission rate of the radiative photons predicted by PHOTOS [9].

We also assess the impact of changes in the bin size on the fits to the \( \cos \theta_{B^0, D^{\ast+}} \) and \( \tilde{w} \) distributions.

There are several uncertainties related to the form factors and their parameterization. The form factor ratios

![Graph](image-url)
$R_1$ and $R_2$ affect the lepton momentum spectrum and thus the differential decay rate as a function of $w$, as well as the fraction of events satisfying the lepton momentum requirements. We assess these effects by varying $R_1$ and $R_2$ within the measurement errors [8], taking into account their correlation. As a consistency check, we compare the measured momentum spectra of the $D^{*+}$ and leptons with the spectra expected from the fit results. We find very good agreement for the $D^{*+}$, but the lepton spectrum favors a larger value for $R_1$, though one consistent with the available measurement.

If we fit separately $c$ and $\mu$ samples, we find exactly the same value for $\rho^2_{A_1}$. The values of $A_1|V_{cb}|$, $(35.8 \pm 0.5) \times 10^{-3}$ and $(35.0 \pm 0.5) \times 10^{-3}$ respectively, differ by 1.2 standard deviation.

The value of $c$, given in Table I, shows that the data disfavor a purely linear dependence of $F$ on $w$, by almost three standard deviations. The fits for the two different parameterizations of the $w$ dependence of the form factors are consistent at $w = 1$. We choose $A_1(1)|V_{cb}| = (35.5 \pm 0.3 \pm 1.6) \times 10^{-3}$, and $\rho^2_{A_1} = 1.29 \pm 0.03 \pm 0.27$, where the errors listed refer to the statistical, and the systematic uncertainties. The correlation between $A_1(1)|V_{cb}|$ and $\rho^2_{A_1}$ is 0.56, taking into account statistical and systematic errors. A recent lattice calculation [3] (including a QED correction of 0.7%) gives $A_1(1) = F(1) = 0.919^{+0.030}_{-0.035}$, with which we obtain

$$|V_{cb}| = (38.7 \pm 0.3 \pm 1.7 \pm 1.5_{-1.3}) \times 10^{-3},$$

where the first error is statistical, the second is systematic, and the third reflects the uncertainty in $A_1(1)$. Integrating over the fitted $\bar{w}$ distribution these parameters result in the branching fraction $B(B^0 \rightarrow D^{*+} \ell^- \bar{\nu}_\ell) = (4.90 \pm 0.07^{+0.36}_{-0.35})\%$, where the errors are the statistical and systematic uncertainties.

In summary, we have measured the CKM parameter $|V_{cb}|$ and the exclusive branching fraction for $B^0 \rightarrow D^{*+} \ell^- \bar{\nu}_\ell$ with high precision. The result for $|V_{cb}|$ is consistent with another BABAR measurement based on lepton and hadron spectra from inclusive semileptonic B-meson decays [13], $|V_{cb}| = (41.4 \pm 0.4\,(\text{stat.}) \pm 0.4\,(\text{exp.}) \pm 0.6\,(\text{theory})) \times 10^{-3}$. The results for $|V_{cb}|$ and the branching fraction are also consistent with earlier measurements [14] based on the technique employed here, except for those from the CLEO experiment [15].

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\begin{itemize}
  \item \textsuperscript{*} Now at Department of Physics, University of Warwick, Coventry, United Kingdom
  \item Also with Università della Basilicata, Potenza, Italy
  \item Also with IFIC, Instituto de Física Corpuscular, CSIC-Universidad de Valencia, Valencia, Spain
  \item Deceased
\end{itemize}

\[1]\] Charge conjugate decay modes are implicitly included, $\ell = e, \mu$.


