

CKM Fits: Standard Model and New Physics

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<http://ckmfitter.in2p3.fr>

The CKM Matrix: The Four Parameters

$$V_{\text{CKM}} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

Consider the Wolfenstein parametrization as in [EPJ C41:1-131,2005](#) : unitarity-exact and phase convention independent.

$$\lambda^2 = \frac{|V_{us}|^2}{|V_{ud}|^2 + |V_{us}|^2}, \quad A^2 \lambda^4 = \frac{|V_{cb}|^2}{|V_{ud}|^2 + |V_{us}|^2} \quad \text{and} \quad \bar{\rho} + i\bar{\eta} = -\frac{V_{ud} V_{ub}^*}{V_{cd} V_{cb}^*}$$

- ✓ λ is measured from $|V_{ud}|$ and $|V_{us}|$ in nuclear decays and semileptonic kaon decays, resp.
- ✓ A is determined from $|V_{cb}|$ and λ .
- ✓ The last two parameters are to be determined from angles and sides measurements of the CKM unitarity triangle.

The CKM Matrix: The Four Parameters

STANDARD MODEL FIT

Inputs:

$$\left| \frac{V_{ub}}{V_{cb}} \right|$$

$$\Delta m_d$$

$$\Delta m_s$$

$$B \rightarrow \tau \nu$$

$$|\varepsilon_K|$$

$$\sin 2\beta$$

$$\alpha$$

$$\gamma$$

CP-conserving Observables

CP-violating Observables

For a complete review of the inputs used in these analyses, please refer to Lacker @ FPCP07

NP IN $\Delta F=2$ FIT

Assumptions:

1. NP only in short distance part of the mixing
2. CKM matrix still unitary
3. Decays b in $q_1 q_2 q_3$ are SM (V_{ub} , γ , α (knowing β))

$$\frac{\langle B_q^0 | H_{eff}^{\text{SM} + \text{NP}} | \overline{B}_q^0 \rangle}{\langle B_q^0 | H_{eff}^{\text{SM}} | \overline{B}_q^0 \rangle} = r_q^2 e^{i2\theta_q} = 1 + h_q e^{i2\sigma_q}$$

The theory for all processes w/ mixing is modified accordingly, e.g. $\sin(2\beta)$ becomes $\sin(2\beta + 2\theta_d)$.

In addition to the inputs on the left, consider $a_{SL}(d)$ and $a_{SL}(s)$ plus $\Delta\Gamma(s)$.

CKM Global Fit Inputs (selection of) : $|V_{ub}|$

$|V_{ub}|$ is one of the basic (hence critical) ingredients of all the CKM fits (SM and NP). Its measurement results from the average of exclusive and inclusive measurements in semileptonic decays of b hadrons.

$$|V_{ub}| [10^{-3}] = 3.50 \pm 0.10_{\text{exp}} \pm 0.47_{\text{theo}} \text{ (exclusive, includes revised HPQCD)}$$

$$|V_{ub}| [10^{-3}] = 4.52 \pm 0.09_{\text{exp}} \pm 0.44_{\text{theo}} \text{ (inclusive, using HFAG06)}$$

Our average :

$$|V_{ub}| [10^{-3}] = 4.03 \pm 0.09_{\text{exp}} \pm 0.44_{\text{theo}}$$

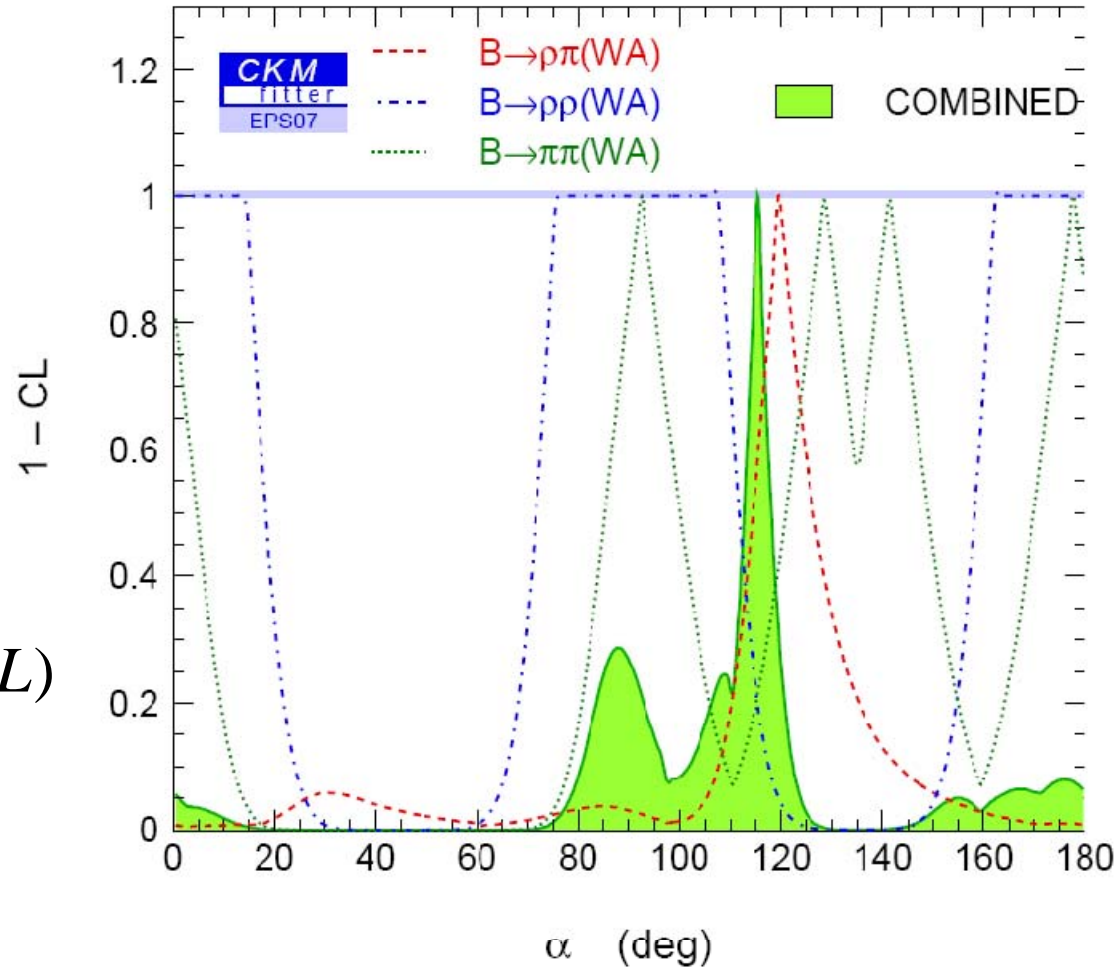
The high value of the inclusive determination is in slight disagreement with the indirect measurement/prediction in SM from $\sin 2\beta$. Note : the uncertainty on m_b might be underestimated (cf Matthias Neubert's talk @ FPCP07) which would result in improving the agreement between both determinations. So does the global fit ...

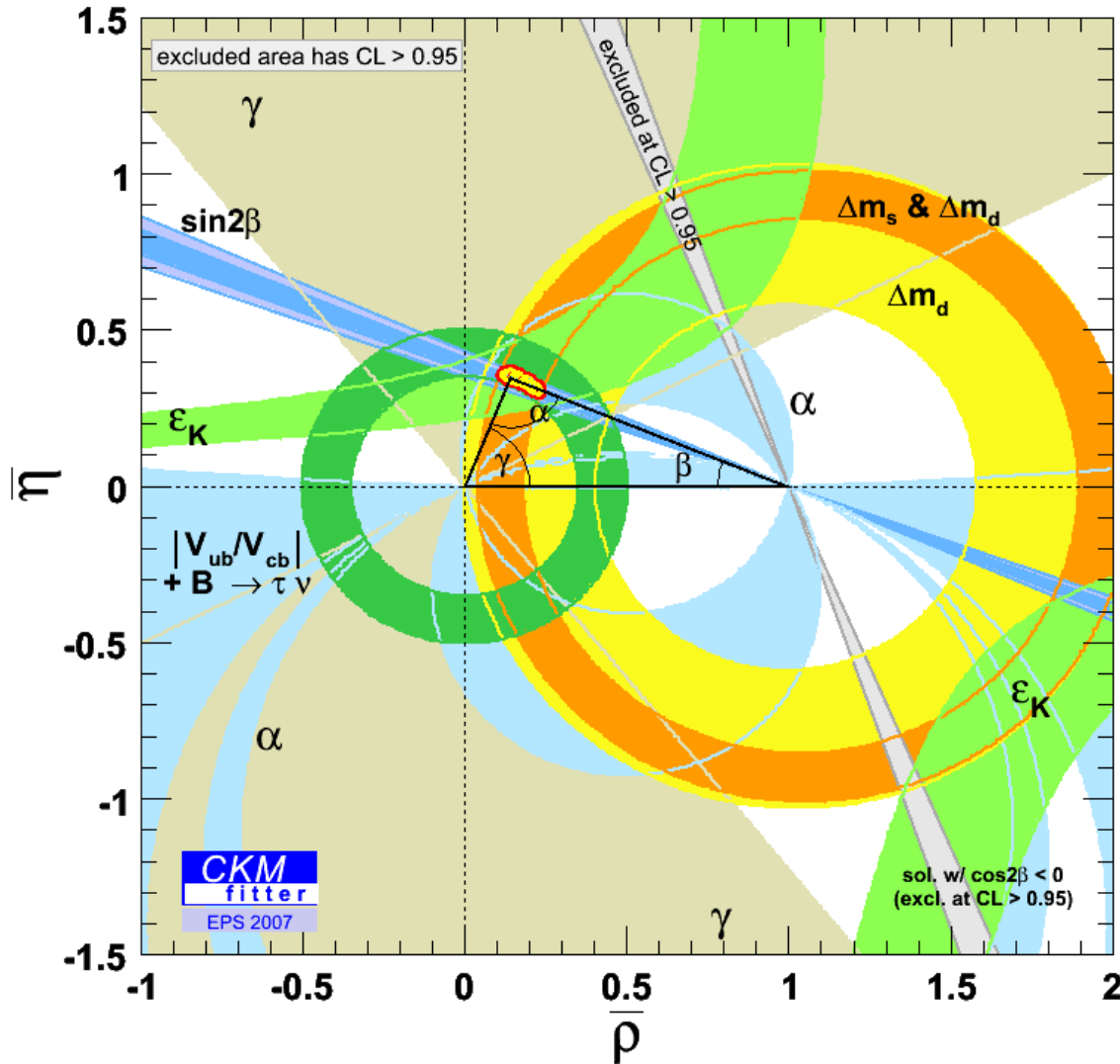
Today, exclusive determination contributes at the same level as inclusive in the average. Wait for new HFAG averages.

CKM Global Fit Inputs (selection of) : α

Combination of Belle and Babar measurements in charmless B decays $\pi\pi, \rho\rho$ and $\rho\pi$.

$$\alpha = 115.5^{+8.6}_{-37.5} \text{ deg (95\% CL)}$$

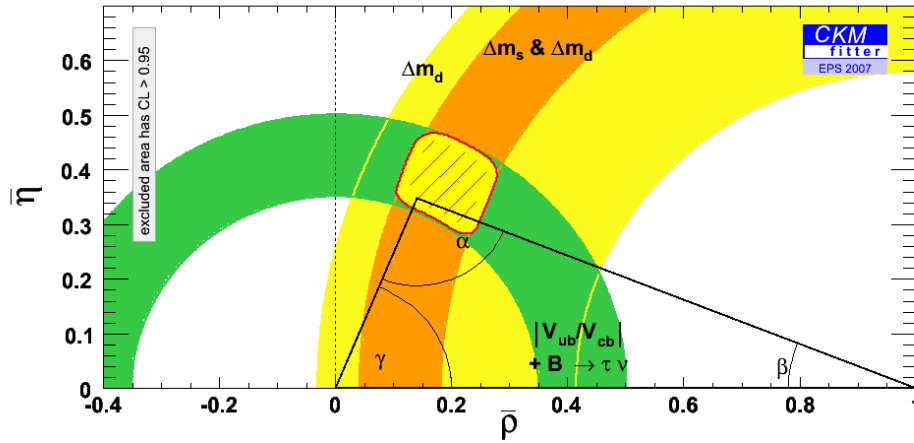




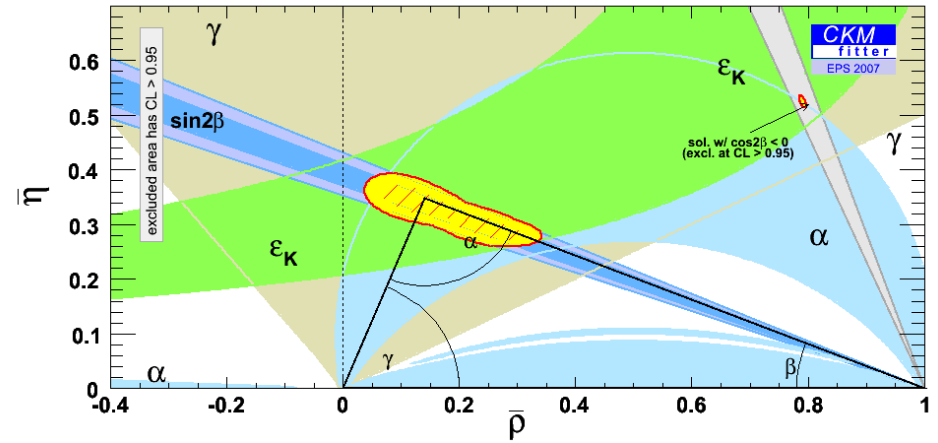
Inputs:

- $\left| \frac{V_{ub}}{V_{cb}} \right|$
- $\left| \frac{V_{ub}}{V_{cb}} \right| + B \rightarrow \tau \nu$
- Δm_d
- Δm_s
- $B \rightarrow \tau \nu$
- $|\epsilon_K|$
- $\sin 2\beta$
- α
- γ

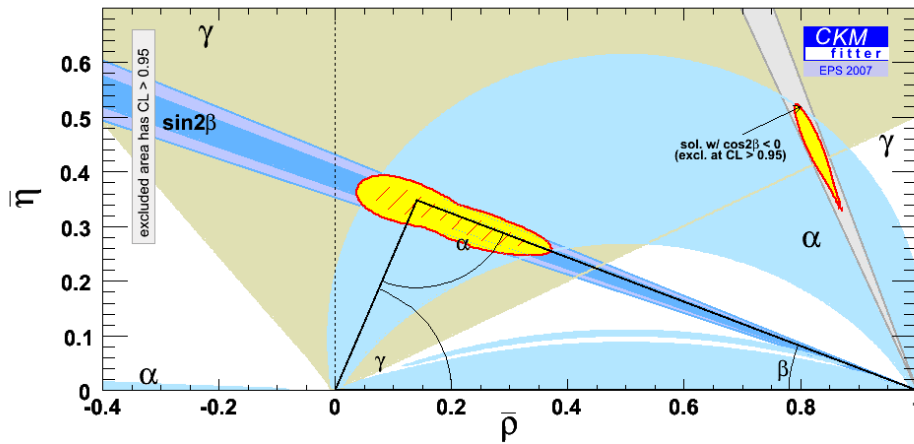
The global CKM fit: Testing the CKM Paradigm



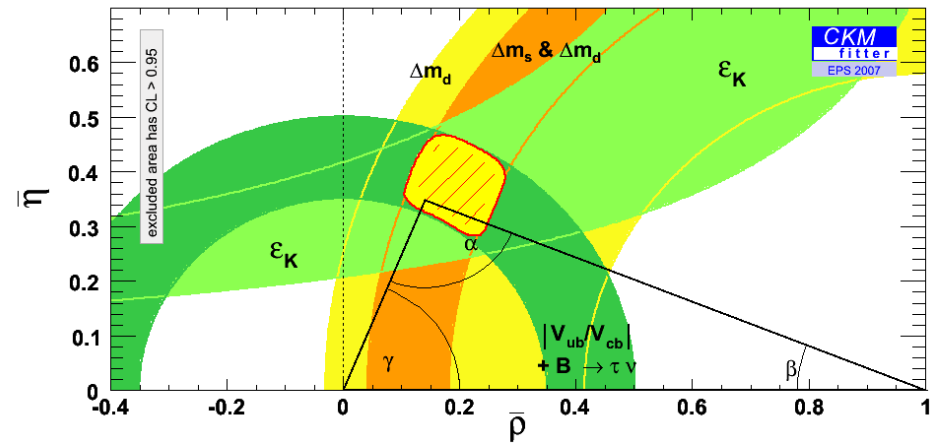
CP-Conserving observables imply CP violation.



CP-Violating observables stresses the same feature

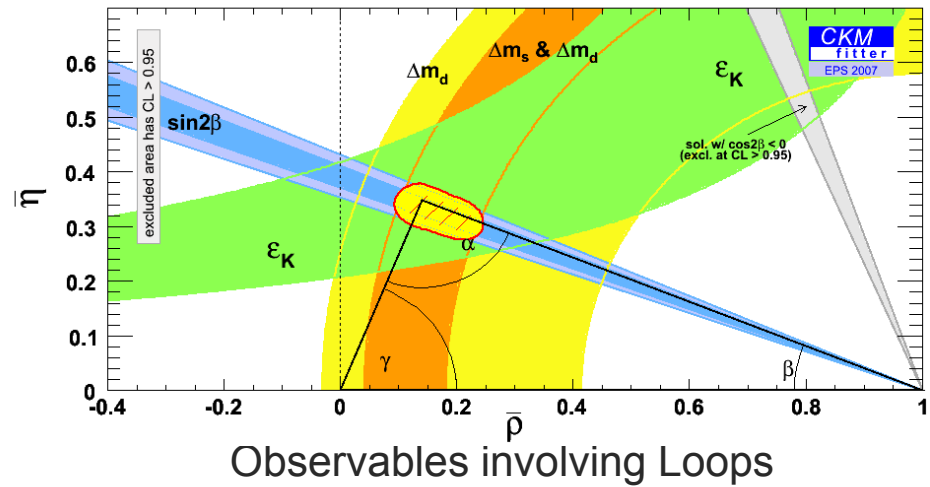
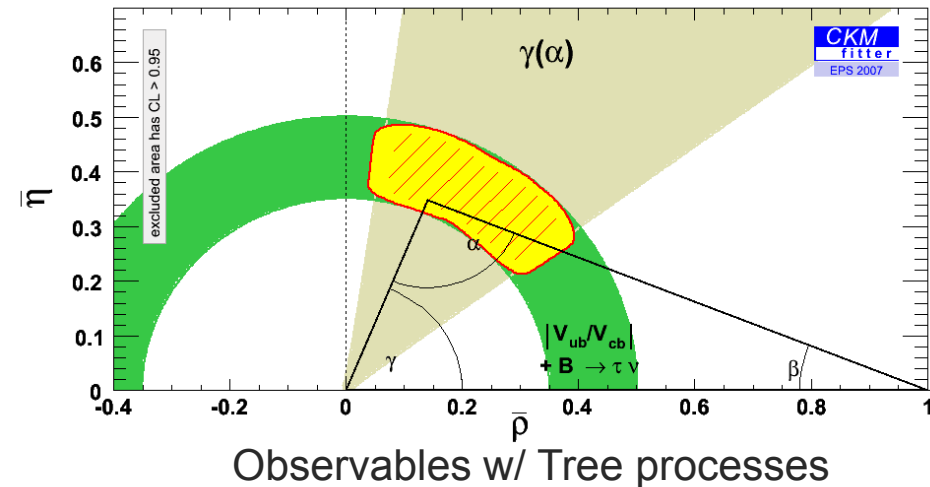


Angles (small theoretical uncertainties)



No angles (large theoretical uncertainties)

The global CKM fit: Testing the CKM Paradigm (cont.)



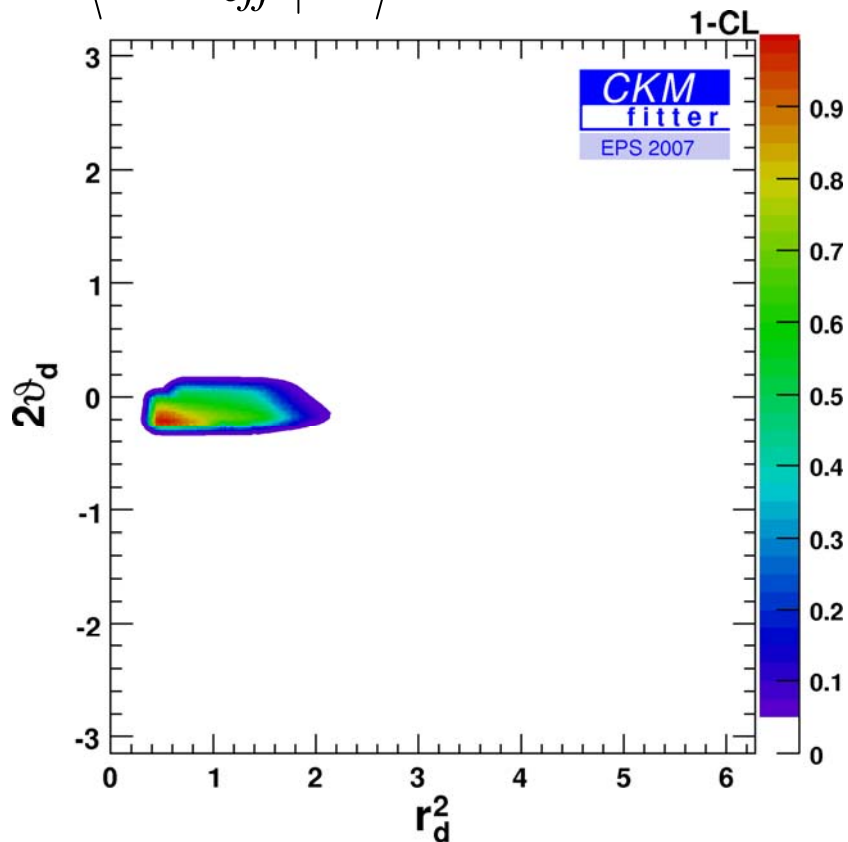
Assuming there is no NP in $\Delta I=3/2$ $b \rightarrow d$ EW penguin amplitude. Use α with β (charmonium) to produce a new γ Tree.

Even if we are not entered a precision era, the CKM mechanism IS the dominant source of CP violation, enough to accommodate within the Standard Model the whole set of Observables.

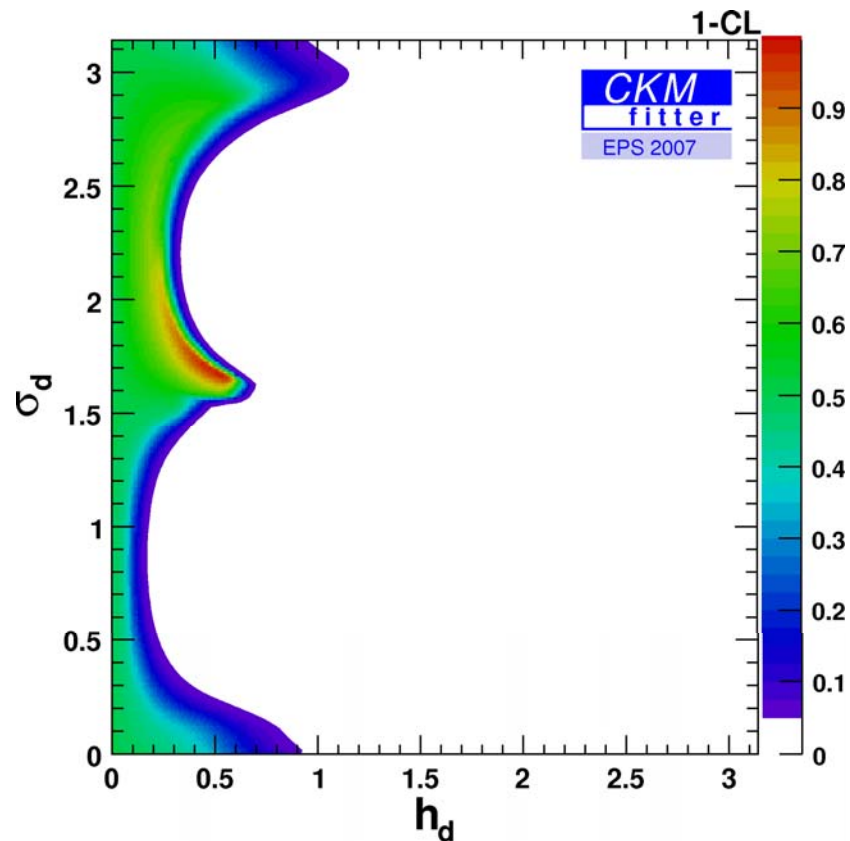
As a consequence, the space left to NP in B_d system IS strongly constrained.

NP in B_d System

$$\frac{\langle B_q^0 | H_{eff}^{SM+NP} | \overline{B}_q^0 \rangle}{\langle B_q^0 | H_{eff}^{SM} | \overline{B}_q^0 \rangle} = r_q^2 e^{i2\theta_q} = 1 + h_q e^{i2\sigma_q}$$



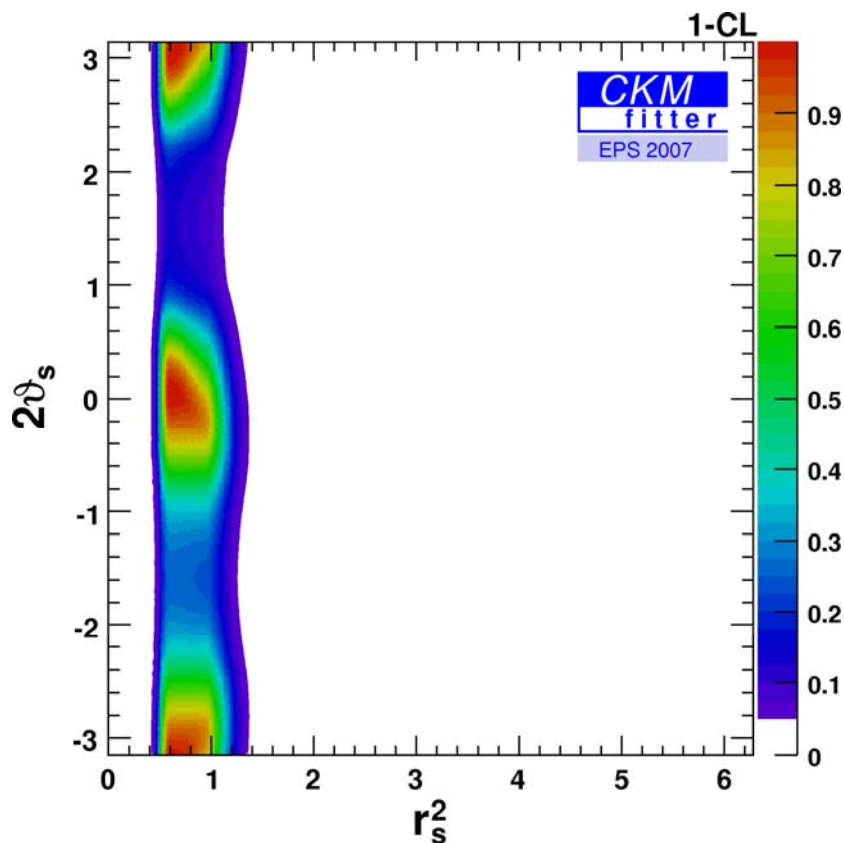
Not much room left for NP in $\Delta F|_d=2$.



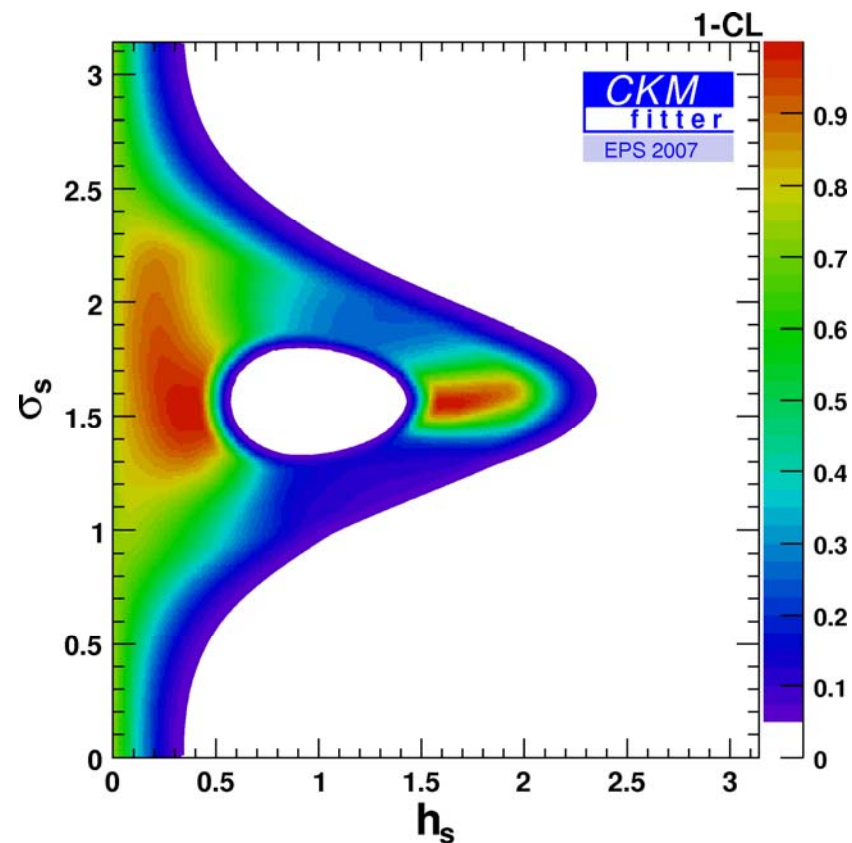
The preferred regions of parameter space (maximum 1-CL) are displaced w.r.t the SM one. Reflects the V_{ub} vs $\sin(2\beta)$ tension.

NP in B_s System

Δm_s , $\Delta \Gamma_s$ and A_{SL}^s



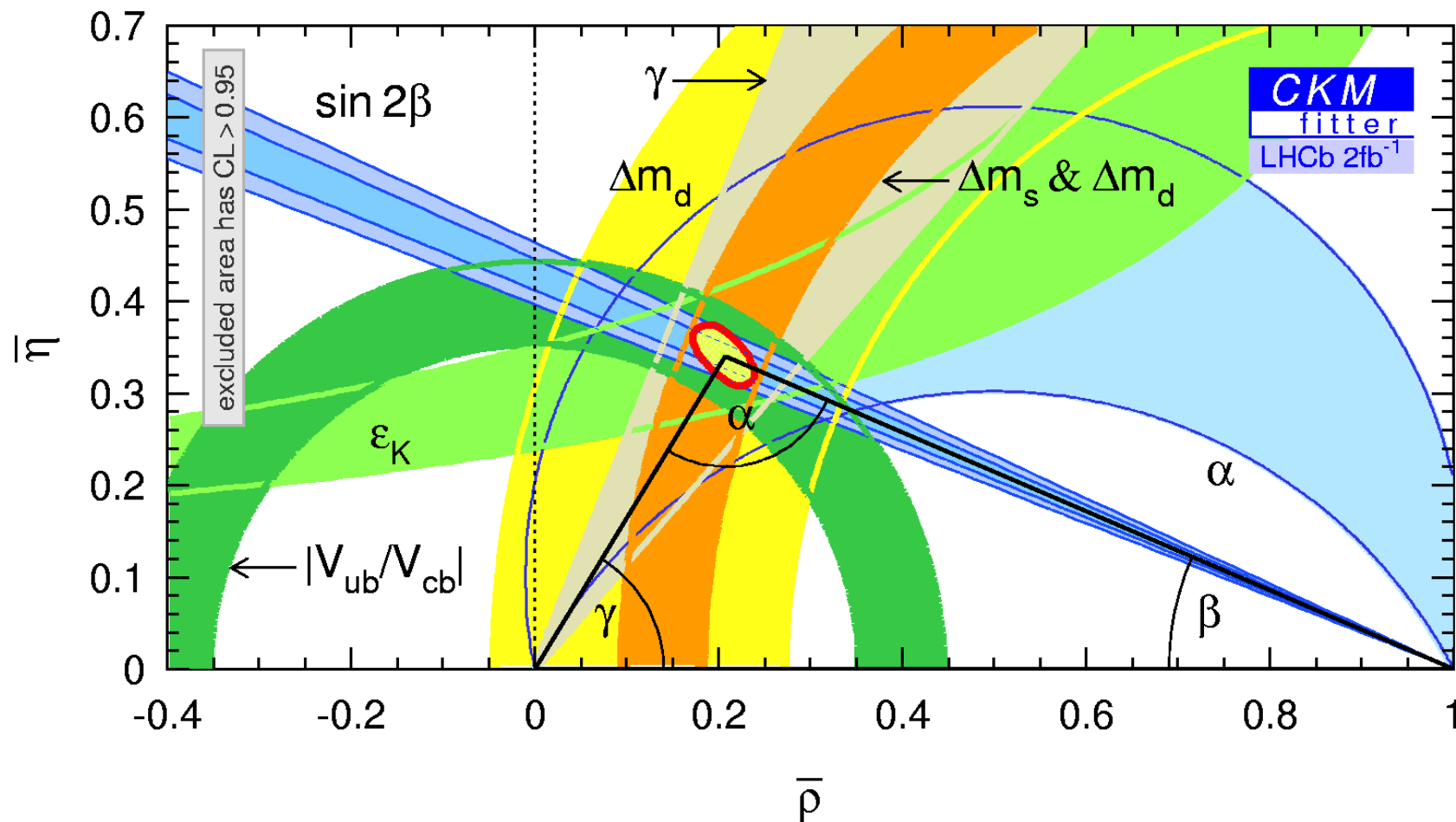
First constraint for NP in the B_s sector come from the Tevatron. Still plenty of room for NP.



$h_s \leq 3$ while $h_d \leq 1$

Large theoretical uncertainties: LQCD

Towards the precision era : LHCb 2 fb⁻¹ EPS 2009 ?



Assumptions:
LHCb TDR

$$\sigma(\Delta m_s) = 0.01$$

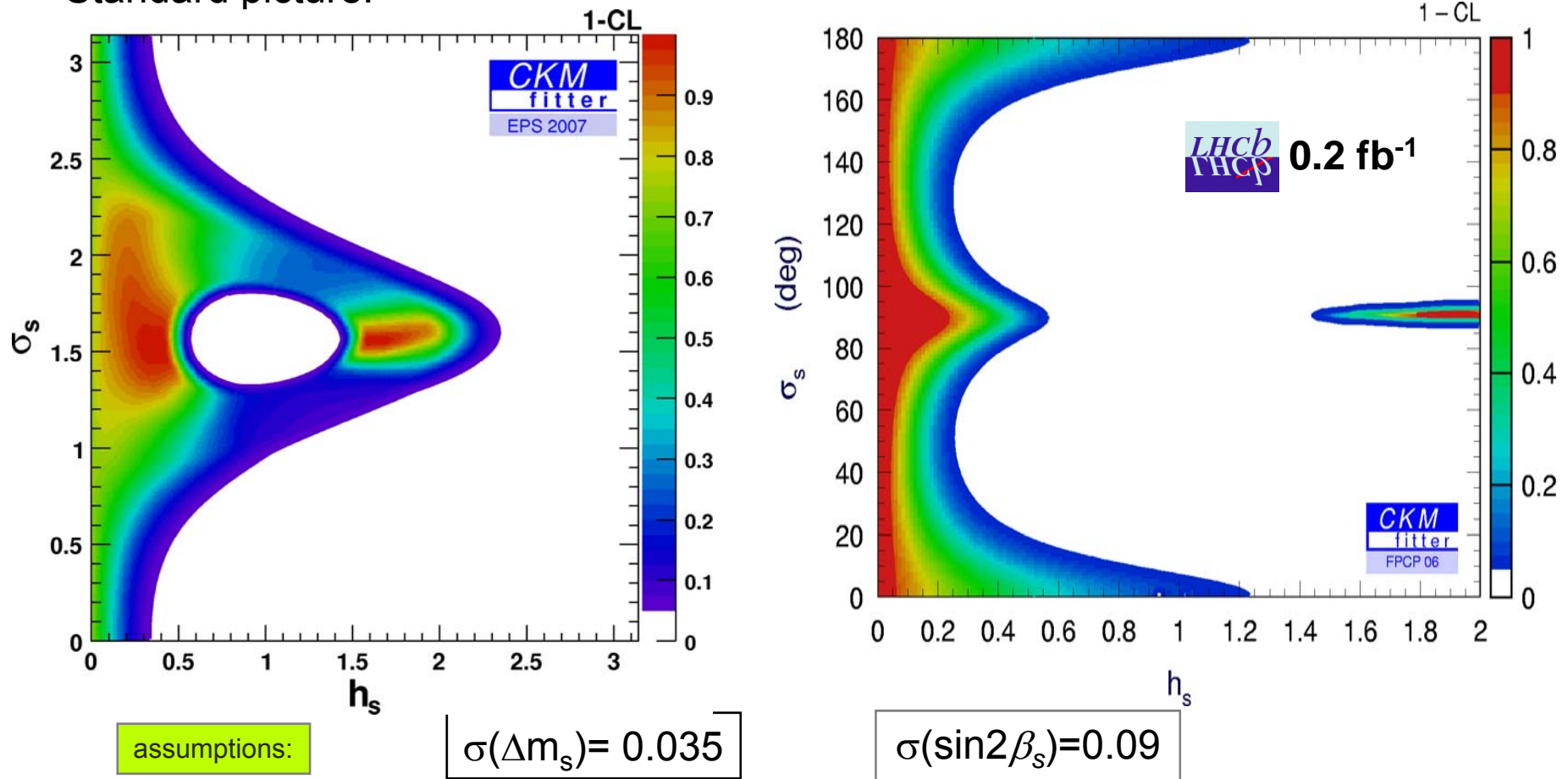
$$\sigma(\sin 2\beta) = 0.02$$

$$\sigma(\alpha) = 10^\circ$$

$$\sigma(\gamma) = 5^\circ$$

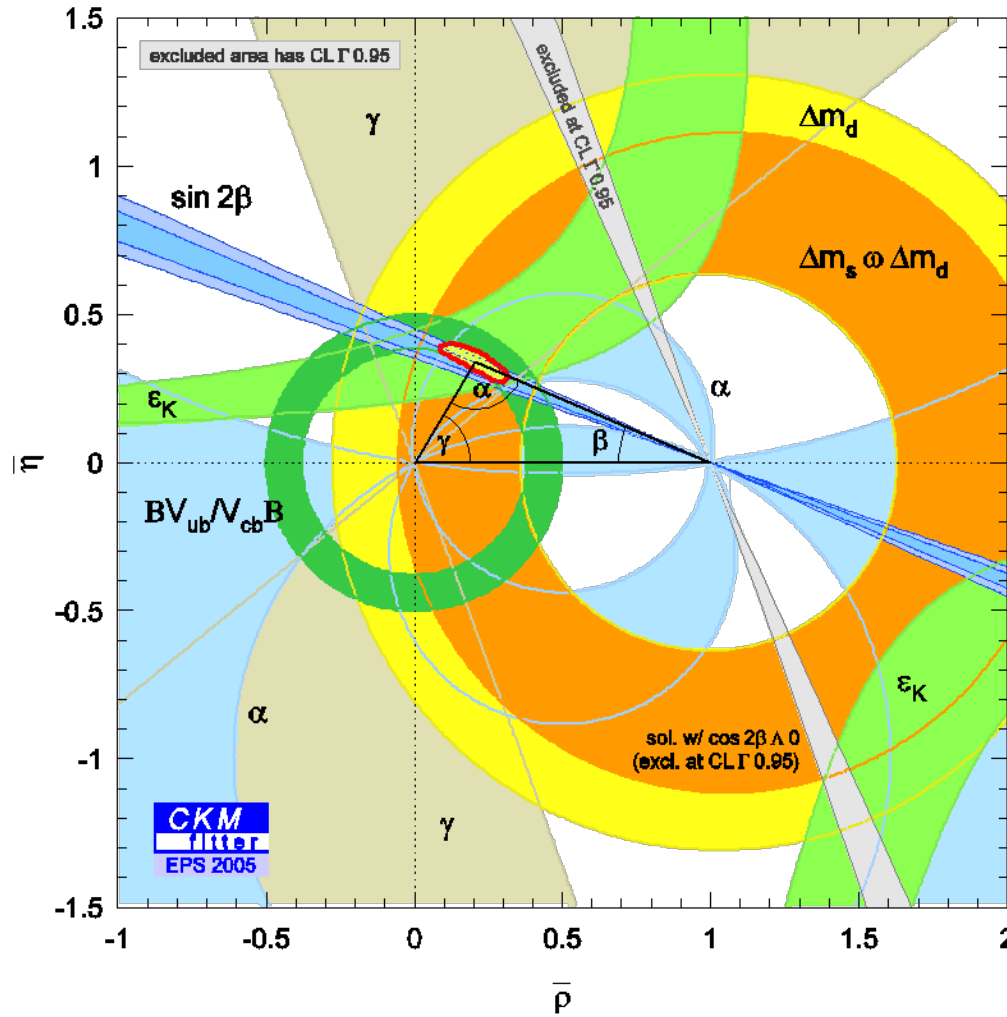
Towards the precision era : LHCb 0.2 fb⁻¹ EPS2009

β_s is precisely predicted in the Standard Model. LHCb can rapidly constrain NP parameters thanks to Bs decays in $J/\psi \Phi$ for instance. Hopefully it won't be that Standard picture.



Conclusions

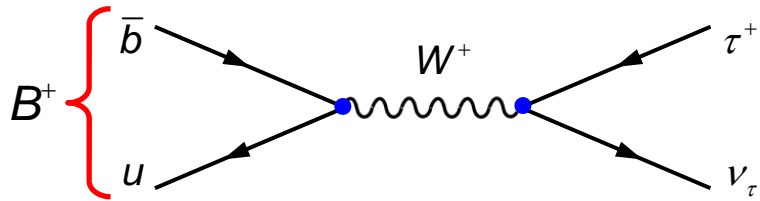
1. The CKM mechanism faced a great success in describing flavor dynamics of many constraints from vastly different scales. It's the dominant source of CP violation in B system. The BaBar and Belle experiments provided fantastic measurements in that respect.
2. Stringent constraints on NP, established in a model-independent manner in $\Delta F=2$ transitions, are already existing in the B_d system. The Tevatron measurements in the B_s sector start to constraint NP in the Bs sector.
3. We are not entered the precision era yet. A precise/ $O(5\%)$ γ measurement is around thanks to the LHCb experiment. The step forward for improving α measurement is more delicate.
4. The B_s system is a basically new territory to explore. B_s transitions might be powerful probes for NP.



Inputs:

- $\left| \frac{V_{ub}}{V_{cb}} \right|$
- Δm_d
- Δm_s
- $B \rightarrow \tau \nu$
- $|\epsilon_K|$
- $\sin 2\beta$
- α
- γ

3. NP : $B^+ \rightarrow \tau^+ \nu_\tau$

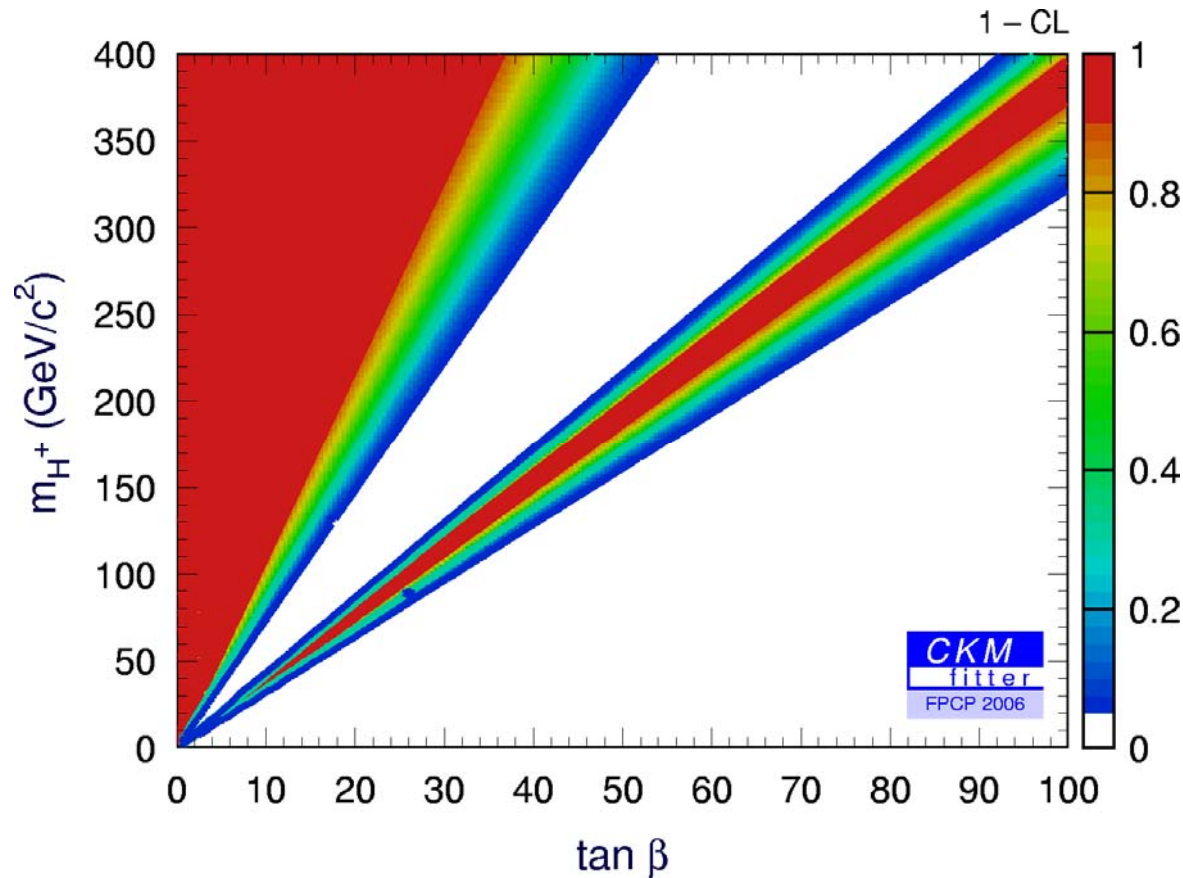


In addition, decay mediated by a charged Higgs.

$$BF(B^+ \rightarrow \tau^+ \nu_\tau) =$$

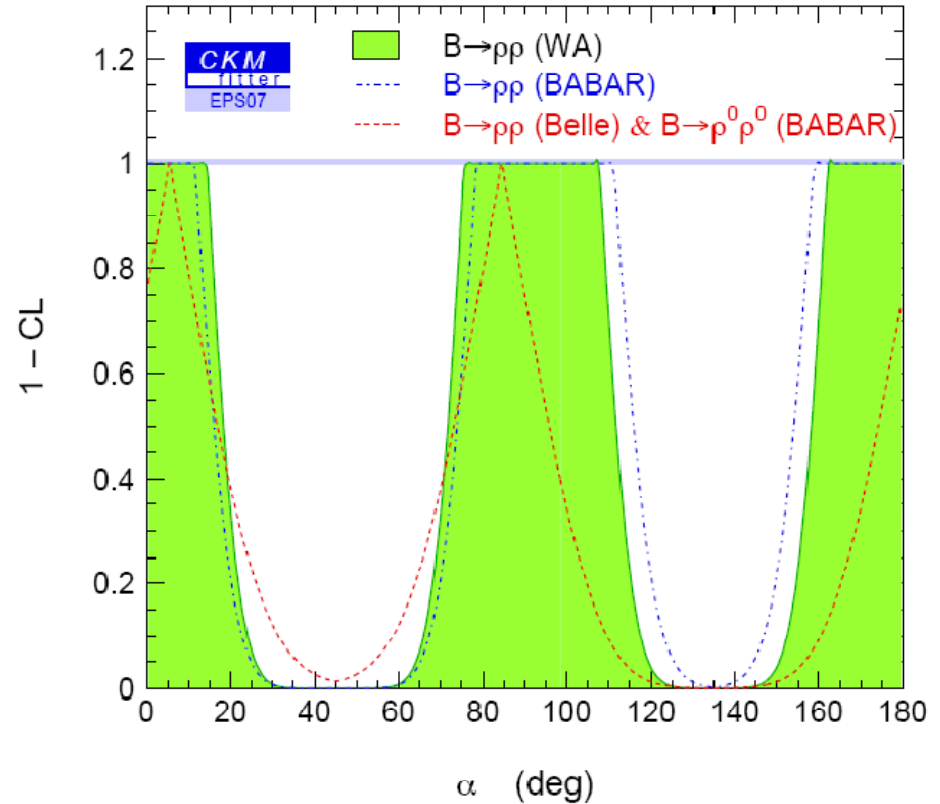
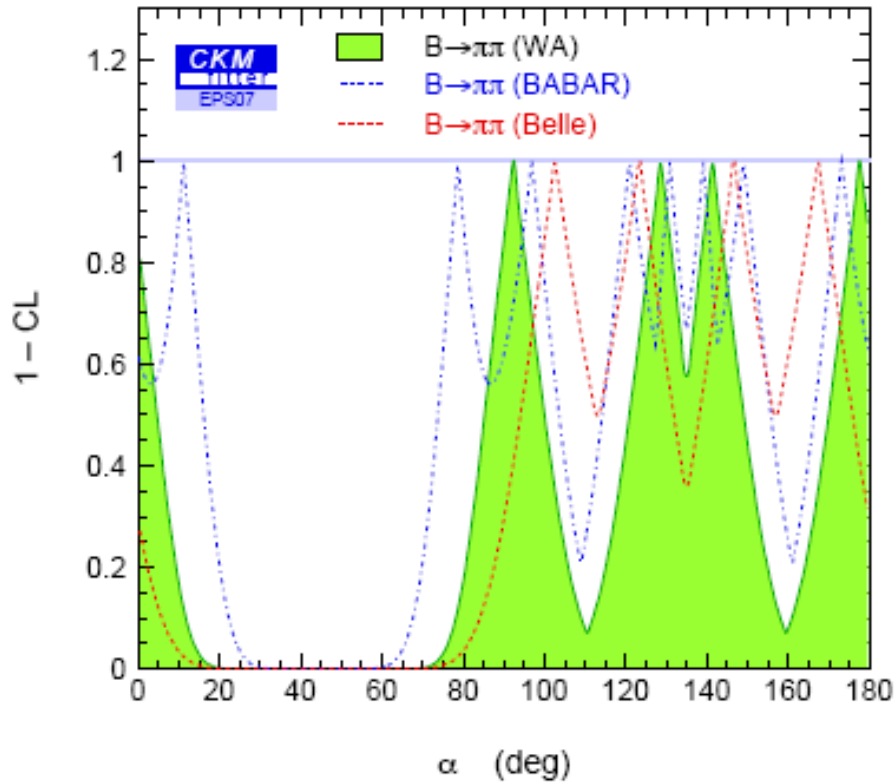
$$BF(B^+ \rightarrow \tau^+ \nu_\tau)_{SM} \times C_H$$

$$C_H = \left(1 - \frac{m_B^2}{m_H^2}\right) \tan^2 \beta$$



CKM Global Fit Inputs (selection of) : α

Combination of Belle and Babar measurements in charmless B decays $\pi\pi, \rho\rho$ and $\rho\pi$.

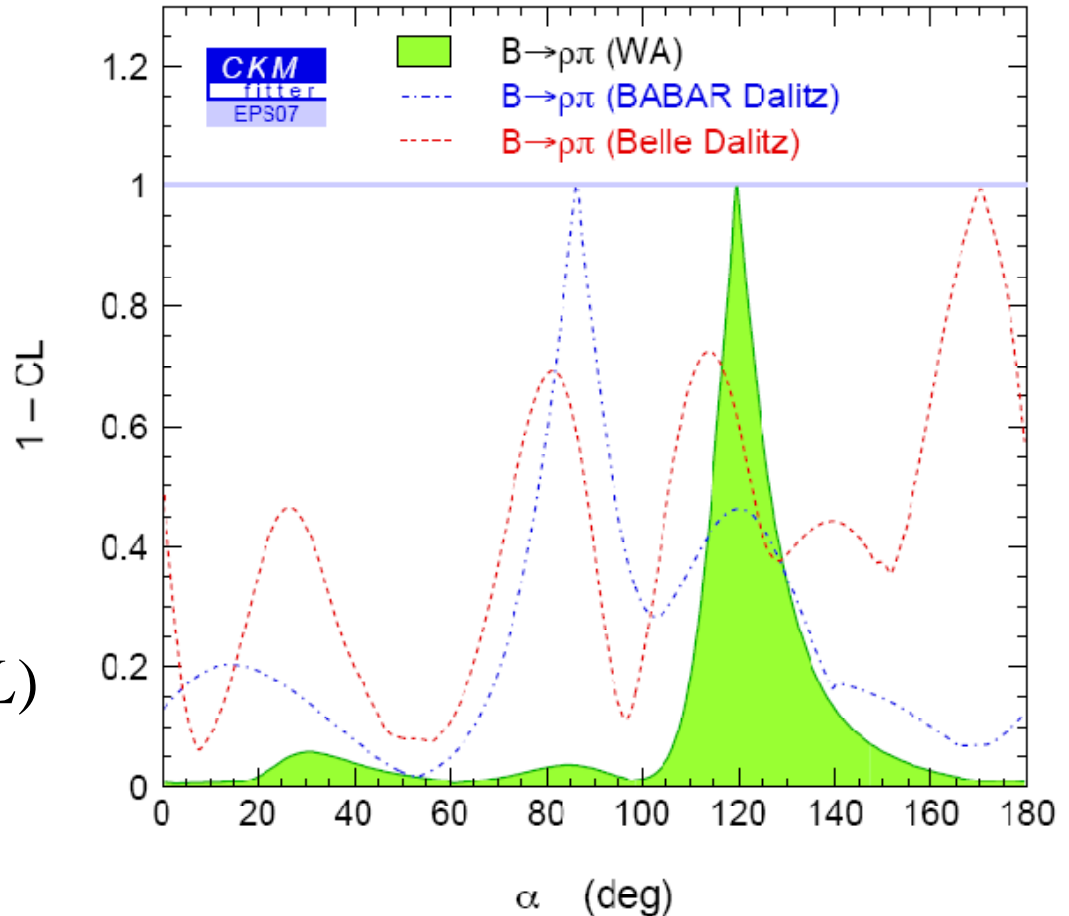


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CKM Global Fit Inputs (selection of) : α

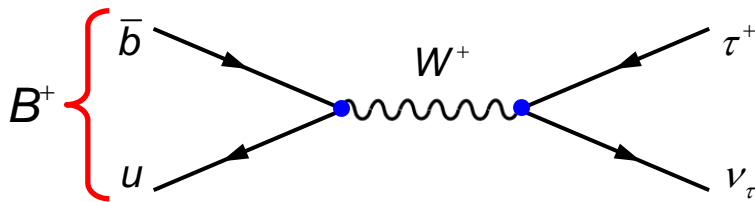
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$$B^+ \rightarrow \tau^+ \nu_\tau$$

- ☀ helicity-suppressed annihilation decay sensitive to $f_B \times |V_{ub}|$
- ☀ Powerful together with Δm_d : **removes f_B (Lattice QCD) dependence**
- ☀ Sensitive to charged Higgs replacing the W propagator



$$\text{BR}(B^+ \rightarrow \tau^+ \nu) = \frac{G_F^2 m_B \tau_B}{8\pi} m_\tau^2 \left(1 - \frac{m_\tau^2}{m_B^2}\right)^2 f_B^2 |V_{ub}|^2$$

