

# **A Search for B Meson Decay to a Muon, a Neutrino, and a Photon**

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**A Search for B Meson Decay to a Muon, a  
Neutrino, and a Photon**

A Dissertation

Presented to the Faculty of the Graduate School

of

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by

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## Abstract

### A Search for B Meson Decay to a Muon, a Neutrino, and a Photon

Michael G. Greene

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This thesis describes a search for the rare decay  $B^+ \rightarrow \mu^+ \nu_\mu \gamma$ , performed at the Stanford Linear Accelerator Center. The BABAR detector is used to analyze  $81.65 \text{ fb}^{-1}$  of data, with  $(88.6 \pm 0.6) \times 10^6$  charged  $B$  meson decays, from the PEP-II  $e^+e^-$  collider running at the  $\Upsilon(4S)$  resonance. The background estimate for the analysis is three events, and three signal candidates are observed. An upper limit on the branching fraction is set at  $\mathcal{B}(B^+ \rightarrow \mu^+ \nu_\mu \gamma) < 1.8 \times 10^{-5}$ , at the 90% confidence level.

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