#### Monte Carlo Study of Tau-Charm Factory

#### Xiaoling Fan

#### August 16, 1994

Monte Carlo study of Tau-Charm Factory has been seriously done by  $\tau cF$  team working at CERN and Spain. In order to prepare a specific proposal for a Tau-Charm Factory construction in Beijing, a Monte Carlo group in IHEP was set up in May 1994 to study the physics goals of Tau-Charm -Factory.

In our Monte Carlo simulation, a simple MC frame was constructed. We did not consider the detailed structure of detector, events are generated by MC generators, then the track parameters are smeared according to the detector performances which are completely based on the talk presented at the Third Workshop on the Tau-Charm Factory by Professor Jasper Kirkby<sup>[\*]</sup>.

<sup>[\*]</sup>Jasper Kirkby, presented at the Third Workshop on the Tau-Charm Factory, Marbella, Spain, 1–6 June, 1993. Following espects are covered in this talk:

1.  $m_{\tau}$  measurement at  $\tau cF$ .

2.  $m_{\nu_{\tau}}$  measurement at  $\tau cF$ .

3. Measurement of Michel Parameter at  $\tau cF$ 

4. D purely leptonic decay at  $\tau cF$ .

5.  $D\bar{D}$  mixing at  $\tau cF$ .

6.  $D_s$  purely leptonic decay at  $\tau cF$ .

# 1. $\tau$ Mass Measurement at $\tau$ -Charm Factory

### BES

- Scanning near the thresthold of  $\tau^+\tau^-$  pair production, data-driven maximum likelihood searching strategy.
- 12 energy points.

•  $\int Ldt \sim 5000 nb^{-1}$ .

Based on the  $e\mu$  channel:

 $m_{ au} = 1776.9 \pm {}^{0.4}_{0.5} \pm 0.2 \; {
m MeV}$ 

:

Synthesizing all 6 decay modes  $(e\mu, e\pi, ee, \mu\pi, \mu\mu, \pi\pi)$  to decrease the statistical error,  $m_{\tau}$  has been got:

 $m_{ au} = 1776.87 \pm^{0.23}_{0.24} \pm^{0.20}_{0.17} \; {
m MeV}$ 

### $\tau$ -Charm Factory

~ •

the set of

• Same method as BES.

• 20 energy points.

•  $\int Ldt \sim 20 \times 1000 nb^{-1} = 20 pb^{-1}$ .

 $L_{\tau c} \sim 100 L_{BEPC}, \sim 2$  days.

•  $\varepsilon_{e\mu} = 45\%$  (conservative).

•  $\Delta = 0.5$  MeV, 1.0 MeV.

BES: 1.4 MeV.

 $\tau$ cF: 1.0 MeV (standard mode).  $\tau$ cF: 0.1 MeV (monochromator mode).

•  $m_{\tau}^{input} = 1777.00$  MeV.

•  $\sigma_B \sim 1\%\sigma$ .



Flow Chart of one time Monte Carlo Simulation for tou Mass Tau Charm Factory Monte Carlo Simulation



Moutput - Minput (MeV)



ţ

Error of tau Mass (+MeV)



Error of tau Mass (-MeV)

# Tau Charm Factory Monte Carlo Simulation



#### $\tau$ Mass

Based on  $e\mu$  channel,  $m_{\tau}$  is expected to be obtained as (only statistical error):

$$m_{ au} \pm \substack{0.10 \\ 0.16}$$
 ( $\Delta = 0.5 \text{ MeV}$ )  
 $m_{ au} \pm \substack{0.17 \\ 0.24}$  ( $\Delta = 1.0 \text{ MeV}$ )

Synthesizing all 6 decay modes  $(e\mu, e\pi, ee, \mu\pi, \mu\mu, \pi\pi)$  to decrease the statistical error,  $m_{\tau}$  is expected to be obtained as (only statistical error):

 $m_{ au} \pm_{0.08}^{0.05}$  ( $\Delta = 0.5 \text{ MeV}$ )  $m_{ au} \pm_{0.12}^{0.09}$  ( $\Delta = 1.0 \text{ MeV}$ )

The statistical error on  $\tau$  mass is expected to be 0.1 MeV/ $c^2$  or less at  $\tau cF$ . It is important to precise test of lepton unversality!

## Systematic Error

- Unstability of beam energy.
- Uncertainty of beam energy spread.
- Uncertainty in detector acceptance.
- Errors in luminosity measurement.
- Background events for each decay channel.
- Bias deduced from the energy step during the scanning.

BES: ~ 0.20 MeV/ $c^2$ .

 $\tau cF: < 0.10 \text{ MeV}/c^2$  is expected !

# 2. $\tau$ Neutrino Mass Measurement at $\tau CF$

• •

÷ -

. .

# 1. Operating Energy Points

· · · · ·

$\sqrt{S}$ (GeV)	$\sigma_{\tau\tau}$ (nb)	$N_{\tau\tau}/\mathrm{Year}$
3.555 <sup>1)</sup>	0.22	$3.4  imes 10^6$
4.25 <sup>2)</sup>	3.56	$5.5 \times 10^{7}$
10 <sup>3)</sup>	0.86	$4.0 \times 10^{7}$

•  $\tau$ -C:  $L \sim 10^{33} cm^{-2} s^{-1}$ 

- B:  $L \sim 3 \times 10^{33} cm^{-2} s^{-1}$ 
  - 1)  $\tau$  is produced almost at rest.
  - 2) With maximum  $\sigma_{\tau\tau}$ .
  - 3) With back-to-back topology.





#### 2. Channel Selection

Mode	$ au \to KK\pi\nu_{ au}$	$\tau \to 5\pi \nu_{\tau}$
Br	$(2.2\pm^{1.7}_{1.1}) imes10^{-3}$	$(5.6 \pm 1.6) \times 10^{-4}$
$Q=m_{ au}-m_{h}$	$\sim 0.65 \text{ GeV}$	$\sim 1.08 \text{ GeV}$
$\bar{p}(\sqrt{S} = 10 GeV)$	$\sim 1.25 \text{ GeV}$	~ 0.83 GeV
$\bar{p}(\sqrt{S} = 4GeV)$	$\sim 0.5 \text{ GeV}$	~ 0.33 GeV
$\sigma_m(\sqrt{S} = 10 GeV)$	6.0 MeV	
$\sigma_m(\sqrt{S}=4GeV)$	3.5 MeV	

•  $\tau cF$ : TOF + dE/dX.

Only  $\tau \to KK\pi\nu_{\tau}$  process has been analysed so far due to the time limitation. The analyses of  $\tau \to 5\pi\nu_{\tau}$  is in progress.

2) For same upper limit of  $m_{\nu_{\tau}}$ ,  $\sigma_{m_{\nu_{\tau}}} \propto \sigma_m/\sqrt{N}$ ,

 $\sigma_m(BF) \sim 1.6 \times \sigma_m \ (\tau cF)$ 

 $N_{KK\pi}(BF) \sim 2N_{KK\pi} \ (\tau cF)$ 







Mode	DATA	$\tau^+\tau^-$	qq	DD*	D*D*	$D_s^+ D_s^-$
4 Prong, $N_{\gamma}=0$	3.4 %	5.9 %	4.5 %	1.4 %	0.5 %	0.9 %
$P_{miss} > 200 MeV$	2.7 %	5.8 %	3.1 %	1.4 %	0.5 %	0.9 %
e/μ tag	0.3 %	1.7 %	0.2 %	0.4 %	0.2 %	0.3 %

Particle Decay to All Known Channels

•  $\tau^+\tau^-$ : KORALB

• qq: LUND 6.2

3. The Upper Limit of  $m_{\nu_{\tau}}$ 1)  $\tau \to \rho''(1750)\nu_{\tau} \to KK\pi\nu_{\tau}$ 

Tag:  $\tau \to e\nu_e\nu_\tau, \mu\nu_\mu\nu_\tau$ .

÷ .

2) Global selection efficiency.

 $\tau\text{-C: } \varepsilon_{lKK\pi}(\sqrt{S} \sim 4GeV) \sim 15\%$ B:  $\varepsilon_{lKK\pi}(\sqrt{S} \sim 10GeV) \sim 25\%$ BES:  $\varepsilon_{lKK\pi} \sim 10\%$ ARGUS:  $\varepsilon_{l3\pi} \sim 25\%$ 

3) The fraction of event with  $m_{KK\pi} > 1.75 GeV$ ,

 $f_{end} \sim 1.5\%$ 

4) Tagged Events

 $N_{tagged} \sim 2N_{\tau\tau} \times (B_e + B_\mu) \times Br(KK\pi) \times f_{end} \times \varepsilon_{lKK\pi}$ 

~ 8 events/year  $\sqrt{S} = 3.555 \text{ GeV}$ ~ 130 events/year  $\sqrt{S} = 4.25 \text{ GeV}$ ~ 150 events/year  $\sqrt{S} = 10 \text{ GeV}$ 



5) Estimation of  $m_{\nu_{\tau}}$  limit.

$$L_i(m_{\nu_\tau}) = \int_{2m_K + m_\pi}^{m_\tau} \frac{d\Gamma(m, m_{\nu_\tau})/dm}{\Gamma_{tot}} R(m, m') dm$$
$$L(m_{\nu_\tau}) = \prod_{i=1}^N L_i(m_{\nu_\tau})$$
$$C.L. = \int_0^{m_{\nu_\tau}} L_i(m_{\nu_\tau}) dm_{\nu_\tau}$$

The statistical upper limit (95% C.L.) on the  $\nu_{\tau}$ mass is ~ 5 MeV/ $c^2$  from  $\tau^{\pm} \rightarrow K^- K^+ \pi^{\pm} \nu_{\tau}$  events, it is almost the same as that given by Jasper Kirkby (4.7 MeV/ $c^2$ ). He also showed that the statistical upper limit (95% C.L.) on the  $\nu_{\tau}$  mass is 3.5 MeV/ $c^2$  from  $\tau^{\pm} \rightarrow 5\pi^{\pm}\nu_{\tau}$  events. Combining both decays gives an upper limit (95% C.L.) of 2.9 MeV/ $c^2$ .

In order to realize this accuracy, very careful control of backgrounds and systematic errors will be required.



#### 3. Michel Parameter Measurement at $\tau cF$

For tau leptonic decay,

 $au 
ightarrow e^- + ar{
u_e} + 
u_{ au}$ 

In tau rest frame,

$$\frac{dN}{dx} \sim x^2 [12(1-x) - \frac{8}{3}\rho(3-4x) + r(x)]$$

 $\begin{array}{l} \mathbf{x} = \mathbf{E}_e / \mathbf{E}_{max}.\\ \rho \ = \ \frac{3}{4} \frac{(g_V - g_A)^2}{(g_V - g_A)^2 + (g_V - g_A)^2}.\\ \mathbf{r}(\mathbf{x}): \text{ radiative corrections.} \end{array}$ 

• Possible  $\rho$  value

- V-A type: $\rho = \frac{3}{4}$ Pure V type: $\rho = \frac{3}{8}$ Pure A type: $\rho = \frac{3}{8}$ V+A type: $\rho = 0$
- In standard model  $\rho = \frac{3}{4}$ .
- Present experimental result:  $\rho_{\tau} = 0.727 \pm 0.033 \ (\sqrt{s} \sim 10 \text{ GeV}).$

If Tau-Charm Factroy operates at tau rest frame, tag channels,

$$\tau \rightarrow \pi \nu_{\tau}, \ K \nu_{\tau}$$

Monochromatic Pion and Kaon momentum can ensure clean data sample!

In our Monte Carlo simulation,

•  $\sqrt{s}=3.555$  GeV,  $\rho$  is sensitive in whole x region.

- $\sqrt{s}=4.25$  GeV,  $\rho$  is not sensitive in whole x region.
- $\sqrt{s}=10$  GeV,  $\rho$  is fairly not sensitive in whole x region.

We expect  $\rho$  accuracy to be 0.5 % at  $\tau$ cF.



04/08/94 23.42

# 4. Pure Leptonic Decay of D at $\tau cF$

## 1) Importance

- Foundamental decay constant (upper limit  $f_D < 290 \text{MeV}$ ).
- $f_B$  can be extrapolated reliably by  $f_D$ .
- Test to theoretical models (Lattice QCD, Potential, Bag, ...).
- 2) Advantages over B-Factory
  - Large data sample (for one year running).

Particle	MKIII $(9.3pb^{-1})$	B-F $(2fb^{-1})$	$\tau cF (10 f b^{-1})$
$D^0$ (single)	$5.4 imes 10^4(\psi^{''})$	$1.5 \times 10^7 (10 \text{GeV})$	$5.8 imes 10^7(\psi^{''})$
$D^+$ (single)	$3.9 imes10^4(\psi^{''})$	$0.7 \times 10^7 (10 {\rm GeV})$	$4.2 \times 10^{7} (\psi^{''})$

- Pure  $D\bar{D}$  final states near threshold.
- Backgrounds can be directly measured above or below threshold.
- Tagging technique can be used to tag D signal.
- Particle seperation is easier than that at high energy region  $(\sqrt{S} \sim 10 \text{ GeV}).$

3) Expected Pure Leptonic Events

$$B_r(D^+ \to \mu^+ \nu) = \frac{G_F^2}{8\pi} f_D^2 \tau_D m_D m_\mu^2 |V_{cd}|^2 (1 - \frac{m_\mu^2}{m_D^2})^2$$
$$f_D = 175 \text{ MeV} \Rightarrow B_r = 2.7 \times 10^{-4}$$
$$f_D = 250 \text{ MeV} \Rightarrow B_r = 5.5 \times 10^{-4}$$

 $N_{tag} = 2N_{D\bar{D}}Br(D \to K\pi\pi)Br(D \to \mu\nu)\varepsilon_{K\pi\pi}\varepsilon_{\mu\nu}$ 

- In our Monte Carlo,  $N_{D\bar{D}} = 2.1 \times 10^7$ .
- Only  $D \to K\pi\pi$  is used as the tagged channel.

$$\begin{array}{ll} Br(D \to K\pi\pi) = 8\% & \varepsilon(D \to K\pi\pi) \sim 60\% \\ Br(D \to \mu\nu) = 2.7 \times 10^{-4} & \varepsilon(D \to \mu\nu) \sim 80\% \end{array}$$

- From MKIII's experimence, a factor of 1.5 should be introduced to  $N_{tag}$ . In  $\tau$ cF, more channels available for tagging, at least a factor of 2 should be applied to  $N_{tag}$ .
- Conservative estimation on  $N_{tag}$ .

$$N_{tag}(D \to \mu \nu) \approx 1100$$





· •• ;

4) Backgrounds

 $D^+ \to \bar{K^0}\pi^+, \bar{K^0}\mu^+\nu, \pi^0\pi^+, \dots$ 

 $\nu$  square missing masses from the backgrounds lie in high mass band, well seperated from signal.

5) Statistical Error

From 1100 detected events, 3% statistical error for  $Br(D \rightarrow \mu\nu)$  is expected, since  $Br \propto f_D^2$ ,  $1 \sim 2\%$  statistical error for  $f_D$  is expected.

6) Systematic Error

Systematic errors arise from:

- uncertainties in detector efficiency.
- contribution from background events.
- uncertainties in particle identification, fake photons, mis-tracked particles etc..

It is expected that the systematic error for  $f_D$  will be the same level as its statistical error.



# 5. $D^0 \overline{D^0}$ Mixing at $\tau cF$

1) Current Status

• Standard Model predicts,

$$r_D \equiv \frac{Br(\bar{D^0} \to D^0 \to f)}{Br(D^0 \to f)} \le 10^{-5} - 10^{-4}$$

• Present upper limit:  $r_D < 10^{-3}$  at 90% C.L.

2) Signature of Mixing

$$egin{aligned} \psi'' &
ightarrow D^0 ar{D^0} (\sim D^0) 
ightarrow (K^- \pi^+) (K^- \pi^+) \ \psi'' &
ightarrow D^0 ar{D^0} (\sim D^0) 
ightarrow (K^- e^+ 
u) (K^- e^+ 
u) . \end{aligned}$$

Double Cabbibo Suppressed Decay (DCSD), same final state as  $D^0 \overline{D^0}$  mixing,

I.I. *Bigi*<sup>[\*]</sup> proved: DCSD is impossible in the above processes due to the quantum statistics violation!

[\*] Proc. Tau-Charm Factory Workshop, SLAC, California, USA, 23-27 May 1989, ed. L.V. Beers, SLAC-Report-343(1989).

3) Backgrounds Simulation

$$\begin{split} \psi'' &\to D^0 \bar{D^0} \to (K^- \pi^+) (K^+ \pi^-). & \text{dominant} \\ \psi'' &\to D^0 \bar{D^0} \to (K^- \pi^+) (K^+ K^-) \\ \psi'' &\to D^0 \bar{D^0} \to (K^- \pi^+) (\pi^+ \pi^-) . \end{split}$$

Strong ability of particle identification at  $\tau CF$  is essential for background rejection.

In our Monte Carlo, a small sample of background  $(K^-\pi^+)(K^+\pi^-)$ events (5000) was produced, no contamination  $(K^-\pi^+)(K^-\pi^+)$ found. ENCOURAGING! More background events need to be produced to carefully study the misidentification of particles (MKIII had 3 like-sign kaon events, unable to see if they came from backgrounds at  $\sigma_{TOF} = 200$  ps).

AIM: To keep the background to the level of one event or less!

4) Optimistic estimation on mixing events

Suppose:  $r_D = 10^{-4}$ ,  $\varepsilon_1 = \varepsilon_2 = 80\%$ ,

$$N_m = 2N_{D^0\bar{D^0}}Br(D^0 \to K^-\pi^+)Br(\bar{D^0} \to K^-\pi^+)\varepsilon_1\varepsilon_2$$
  
= 2 × 2.9 × 10<sup>7</sup> × (3.65 × 10<sup>-2</sup>)<sup>2</sup> × 10<sup>-4</sup> × (0.80)<sup>2</sup>  
~ 5

A few mixing events expected under  $r_D = 10^{-4}$ .

6. Pure Leptonic Decay of  $D_s$  at  $\tau cF$ 

The width of pure leptonic decays of  $D_s$  is,

$$\Gamma(D_s \to l\nu) = \frac{G_F^2}{8\pi} f_{D_s}^2 m_{D_s} m_l^2 |V_{cs}|^2 (1 - \frac{m_l}{m_{D_s}})^2$$

which can be determined from the branching ratio and lifetime,

$$Br(D_s \to l\nu) = \frac{\Gamma(D_s \to l\nu)}{\Gamma_{total}} = \tau_{D_s} \cdot \Gamma(D_s \to l\nu)$$

so the weak decay constant  $f_{D_s}$  can be experimentally determined.

1)  $\tau$ -Charm Factory

- $\sqrt{S} = 4.03$  GeV,  $\sigma \sim 400$ pb.
- $\int Ldt \sim 10 f b^{-1}$  in one year.
- $N_{D_s^+ D_s^-} \sim 400 pb \times 10 fb^{-1} \sim 4 \times 10^6$ .

• 
$$e^+e^- \rightarrow D_S^+ D_S^-$$
,  $D_S^+ \rightarrow \eta'\rho^+$ ,  $D_S^- \rightarrow \nu\nu$   
 $\rho^+ \rightarrow \pi^+ \pi^0$ ,  $\pi^0 \rightarrow \gamma\gamma$  9.5% × 30.0% × 98.798% = 2.82%  
•  $e^+e^- \rightarrow D_S^+ D_S^-$ ,  $D_S^+ \rightarrow \eta'\rho^+$ ,  $D_S^- \rightarrow \nu\nu$   
 $\rho^+ \rightarrow \pi^+ \pi^0$ ,  $\eta \rightarrow \eta^+ \pi^- \tau^\eta$   
 $\pi^0 \rightarrow \gamma\gamma$ ,  $\eta \rightarrow \gamma\gamma$  9.5% × 44.1% × 98.798% × 38.9% = 1.61%  
•  $e^+e^- \rightarrow D_S^+ D_S^-$ ,  $D_S^+ \rightarrow \eta\rho^+$ ,  $D_S^- \rightarrow \nu\nu$   
 $\rho^+ \rightarrow \pi^+ \pi^0$ ,  $\eta \rightarrow \gamma\gamma$   
 $\pi^0 \rightarrow \gamma\gamma$  7.9% × 38.9% × 98.798% = 3.04%  
•  $e^+e^- \rightarrow D_S^+ D_S^-$ ,  $D_S^+ \rightarrow \eta\rho^+$ ,  $D_S^- \rightarrow \nu\nu$   
 $\rho^+ \rightarrow \pi^+ \pi^0$ ,  $\eta \rightarrow \pi^+ \pi^- \pi^0$   
 $\pi^0 \rightarrow \gamma\gamma$ ,  $\pi^0 \rightarrow \gamma\gamma$  7.9% × 23.6% × 98.798% × 98.798% = 1.82%  
•  $e^+e^- \rightarrow D_S^+ D_S^-$ ,  $D_S^+ \rightarrow K^{*0}K^+$ ,  $D_S^- \rightarrow \nu\nu$   
 $K^{*0} \rightarrow K^\pm \pi^\mp$  2.6%  
•  $e^+e^- \rightarrow D_S^+ D_S^-$ ,  $D_S^+ \rightarrow K^{*0}K^+$ ,  $D_S^- \rightarrow \nu\nu$   
 $K^{*0} \rightarrow K^\pm \pi^\mp$ ,  $K^{*+} \rightarrow K^+ \pi^0$   
 $\pi^0 \rightarrow \gamma\gamma$  5.0%  
•  $e^+e^- \rightarrow D_S^+ D_S^-$ ,  $D_S^+ \rightarrow \phi \eta^+$ ,  $D_S^- \rightarrow \nu\nu$   
 $\phi \rightarrow K^+K^-$  2.8% × 49.1% = 1.37%  
•  $e^+e^- \rightarrow D_S^+ D_S^-$ ,  $D_S^+ \rightarrow \phi \rho^+$ ,  $D_S^- \rightarrow \nu\nu$   
 $\eta^+ \rightarrow \gamma^0 \sigma^+$ ,  $\phi \rightarrow K^+ K^-$   
 $\pi^0 \rightarrow \gamma\gamma$  5.2% × 49.1% × 98.798% = 2.52%

- -

- 2) Advantages Over B-Factory
  - Measuring backgrounds experimentally by lowering the beam energy below the threshold.
  - Lower backgrounds.
  - Operating near threshold, single-tagging technique can be used.
  - Particle identification is easier than that at high energy region ( $\sqrt{S} \sim 10$  GeV).
- 3) Monte Carlo Simulation
  - $C_s I(Tl)$  calorimeter enables us to tag some neutral decay channels with large branching ratios.
  - at least ~ 25% branching fraction of total  $D_s$  decay modes can be used to tag  $D_s$  signal.
  - single-tagging efficiency  $\epsilon_s \sim 60\%$
  - resolution of  $D_s$  invariant mass  $\sigma_m^{inv} \sim 10$  MeV.
  - resolution of  $D_s$  beam constrained mass  $\sigma_m^{bc} \sim 1.2$  MeV.

A more detailed Monte Carlo study shows that the backgrounds from  $D\bar{D}, DD^*, D^*D^*$  contribute less in the  $D_s$  signal region, the signal can be clearly distinguished.



 $e^+e^- \rightarrow D_s^+ D_s^-, D_s^+ \rightarrow \phi \pi^+, D_s^- \rightarrow \mu^- V_{\mu}$ 





## 4) Estimation of $f_{D_s}$

Assuming the branching ratio of  $D_s \to \mu\nu$  is  $5 \times 10^{-3}$ . According to our Monte Carlo simulation, the detector acceptance for this process is ~ 75%, 4000 - 5000  $D_s \to \mu\nu$  events will be expected in one year's running. The statistical error for  $f_{D_s}$  can be reached  $1 \sim 2\%$ .

Systematic errors arise from:

- uncertainties in detector efficiency.
- contribution from background events.
- uncertainties in particle identification, fake photons, mis-tracked particles etc..

It is expected that the systematic error for  $f_{D_s}$  will be the same level as its statistical error.





#### Summary

At Tau-Charm Factory:

$\sigma_{m_{\tau}}$ (MeV)	< 0.1  MeV
Upper Limit of $m_{\nu_{\tau}}$ (MeV)	$\sim 3~{ m MeV}$
$\sigma_{ ho}$ (%)	O(0.5%)
$D-\bar{D}$ Mixing	$r_D \sim 10^{-4}$
$\sigma_{f_D}$ (%)	O(2%)
$\sigma_{f_{D_s}}$ (%)	O(2%)

Based on full advantages of the large increase in statistics expected at Tau-Charm Factory, and a highresolution detector,  $\tau cF$  will provide a super experimental tool to fundamental measurement with unprecedented precision in a wide range involving  $\tau$ , charm and charmonium decays. The threshold region can offer the best control of systematic errors.

 $\tau$ cF and B-factory are complementary rather than replaceable each other.