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TRANSPORT

A COMPUTER PROGRAM FOR DESIGNING CHARGED PARTICLE BEAM TRANSPORT SYSTEMS*

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 K_2 fringing-field integral

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REFERENCES

INTRODUCTION

TRANSPORT is a first- and second-order matrix multiplication computer program intended for the design of static-magnetic beam transport systems. It has been in existence in various evolutionary versions since 1963. The present version, described in this manual, includes both first- and second-order fitting capabilities.

Many people from various laboratories around the world have contributed either directly or indirectly to the development of TRANSPORT. The first-order matrix methods were developed by the AGS machine theorists¹ followed by a paper by Penner.² The extension of the first-order matrix methods to include second and higher orders was conceived and developed by Brown, Belbeoch and Bounin³ in Orsay, France, in 1958-59. The original first-order TRANSPORT computer program was written in BALGOL by C.H. Moore at SLAC in collaboration with H.S. Butler and S.K. Howry in 1963. The second-order portion of the program was developed and debugged by Howry and Brown,⁴ also in BALGOL. The resulting BALGOL version was translated into FORTRAN by S. Kowalski at MIT and later debugged and improved by Kear. Howry and Brown at SLAC.⁵ In 1971-72, D. Carey at FNAL completely rewrote the program and developed an efficient second-order fitting routine using the coupling coefficients (partial derivatives) of multipole components to the optics as derived by Brown.⁶ This version was implemented at SLAC by F. Rothacker in the early spring of 1972 and subsequently carried to CERN in April, 1972, by K.L. Brown. C. Iselin of CERN made further contributions to the program structure and improved the convergence capabilities of the first-order fitting routines.

A standard version of the resulting program has now been adopted at SLAC, FNAL, and CERN. This manual describes the use of this standard version and is not necessarily applicable to other versions of TRANSPORT. Copies of this manual may also be obtained from

- 1. The Reports Office, CERN, 23 Geneva, Switzerland (Ref. CERN 73-16).
- 2. The Reports Office, Fermi National Accelerator Laboratory, P. O. Box 500, Batavia, IL 60510 (Ref. NAL-91).

A standard version of TRANSPORT has been implemented on the IBM 360, using the FORTRAN H compiler. It requires approximately 270,000 bytes of memory for operation. It is normally distributed on 9 track magnetic tape at 800 BPI having a standard IBM label. This program may be obtained from:

Frank Rothacker TRANSPORT Program Librarian Mail Bin 88 Stanford Linear Accelerator Center P. O. Box 4349 Stanford, California 94305

European users are encouraged to obtain the program from:

Ch. Iselin CH-1211 CERN 23 Geneva, Switzerland

PDP 10, IBM and CDC users may also obtain the program from:

D. C. Carey Fermi National Accelerator Laboratory P. O. Box 500 Batavia, IL 60510

Using the Program at SLAC

All input data must be in the form of 80 byte records. Columns 1-72 are processed by the program, and columns 73-80 are treated as comments. Usually columns 73-80 are used as the line number identification field. The job control language deck setup for operating the program at SLAC is as follows:

// job card information //STEP1 EXEC PGM = TRANS, REGION = 280 K //STEPLIB DD DSN = WYL.CG.FXR.L, DISP = SHR //FT04F001 DD SYSOUT = B //FT06F001 DD SYSOUT = A //FT05F001 DD * transport data deck goes here. The present authors assume responsibility for the contents of this manual, but in no way imply that they are solely responsible for the entire evolution of the program.

MATHEMATICAL FORMULATION OF "TRANSPORT"

General Conventions

A beam line is comprised of a set of magnetic elements placed sequentially at intervals along an assumed reference trajectory. The reference trajectory is here taken to be a path of a charged particle passing through idealized magnets (no fringing fields) and having the central design momentum of the beam line.

In TRANSPORT,^{*} a beam line is described as a sequence of elements. Such elements may consist not only of magnets and the intervals between them, but also of specifications of the input beam, calculations to be done, or special configurations of the magnets. A certain relation, described below, of the magnets and their fields to the assumed reference trajectory is considered normal. Alternative configurations can be described by means of elements provided for such purposes.

The two coordinates transverse to the initial reference trajectory are labeled as horizontal and vertical. A bending magnet will normally bend in the horizontal plane. to allow for other possibilities a coordinate rotation element is provided. Because of such other possibilities, when describing bending magnets we shall often speak of the bend and nonbend planes. The transverse coordinates will also often be labeled x and y, while the longitudinal coordinate will be labeled z.

All magnets are normally considered "aligned" on the central trajectory. A particle following the central trajectory through a magnet experiences a uniform field which begins and ends abruptly at the entrance and exit faces of the idealized magnet. Therefore, through a bending magnet the reference trajectory is the arc of a circle, while through all other magnetic elements it is a straight line. To accomodate a more gradual variation of field at the ends of a bending magnet a fringing field element is provided. In order to represent an orientation with respect to the reference trajectory other than normal of a magnet or section of a beam line, a misalignment element also exists.

The magnetic field of any magnet, except a solenoid, is assumed to have midplane symmetry. This means that the scalar potential expanded in transverse coordinates

^{*}For a more complete description of the mathematical basis of TRANSPORT, refer to SLAC-75,⁴ and to other references listed at the end of this manual.

about the reference trajectory is taken to be an odd function of the vertical coordinate. If a coordinate rotation is included, then the potential is odd in the coordinate to which the vertical has been rotated. For a bending magnet this will always be in the nonbend plane.

The program TRANSPORT will step through the beam line, element by element, calculating the properties of the beam or other quantities, described below, where requested. Therefore one of the first elements is a specification of the phase space region occupied by the beam entering the system. Magnets and intervening spaces and other elements then follow in the sequence in which they occur in the beam line. Specifications of calculations to be done or of configurations other than normal are placed in the same sequence, at the point where their effect is to be made.

The Transfer Matrix R

The following of a charged particle through a system of magnetic lenses may be reduced to a process of matrix multiplication. At any specified position in the system an arbitrary charged particle is represented by a vector (single column matrix) X, whose components are the positions, angles, and momentum of the particle with respect to the reference trajectory, i.e.

$$X = \begin{bmatrix} x \\ \theta \\ y \\ \phi \\ \ell \\ \delta \end{bmatrix}$$

Definitions:

- x = the horizontal displacement of the arbitrary ray with respect to the assumed central trajectory.
- θ = the angle this ray makes in the horizontal plane with respect to the assumed central trajectory.
- y = the vertical displacement of the ray with respect to the assumed central trajectory.

- ϕ = the vertical angle of the ray with respect to the assumed central trajectory.
- ℓ = the path length difference between the arbitrary ray and the central trajectory.
- $\delta = \Delta p = p$ is the fractional momentum deviation of the ray from the assumed central trajectory.

This vector, for a given particle, will henceforth be referred to as a ray. The magnetic lens is represented to first order by a square matrix R, which describes the action of the magnet on the particle coordinates. Thus the passage of a charged particle through the system may be represented by the equation

$$X(1) = RX(0) \quad , \tag{1}$$

where X(0) is the initial coordinate vector and X(1) is the final coordinate vector of the particle under consideration. The same transformation matrix R is used for all such particles traversing a given magnet [one particle differing from another only by its initial coordinate vector X(0)].

The traversing of several magnets and interspersing drift spaces is described by the same basic equation, but with R now being replaced by the product matrix $R(t) = R(n) \dots R(3)R(2)R(1)$ of the individual matrices of the system elements. This cumulative transfer matrix is automatically calculated by the program and is called TRANSFORM 1. It may be printed where desired, as described in later sections.

This formalism may be extended to second order by the addition of another term.⁴ The components of the final coordinate vector, in terms of the original, are now given as

$$X_i(1) = \sum_j R_{ij} X_j(0) + \sum_{jk} T_{ijk} X_j(0) X_k(0) ,$$

where T is the second-order transfer matrix. It too is accumulated by the program as one traverses a series of elements. At each point the series is again truncated to second order. Normally the program will calculate only the first-order terms and their effect. If it is desired to include second-order effects in a beam line, an element is provided which specifies that a second-order calculation is to be done. For more information on the T matrix, see the references at the end of the manual. The following of a charged particle via TRANSPORT through a system of magnets is thus analogous to tracing rays through a system of optical lenses. The difference is that TRANSPORT is a matrix calculation which truncates the problem to either firstor second-order in a Taylor's expansion about a central trajectory. For studying beam optics to greater precision than a second-order TRANSPORT calculation permits, raytracing programs which directly integrate the basic differential equation of motion are recommended.⁷

<u>The Beam Matrix σ </u>

In accelerator and beam transport systems, the behavior of an individual particle is often of less concern than is the behavior of a bundle of particles (the beam), of which an individual particle is a member. An extension of the matrix algebra of Eq. (1) provides a convenient means for defining and manipulating this beam. TRANSPORT assumes that the beam may be correctly represented in phase space by an ellipsoid in the six-dimensional coordinate system described above. Particles in a beam are assumed to occupy the volume enclosed by the ellipsoid, each point representing a possible ray. The sum total of all phase points, the phase space volume, is commonly referred to as the "phase space" occupied by the beam.

The validity and interpretation of this phase ellipse formalism must be ascertained for each system being designed. However, in general, for charged particle beams in, or emanating from accelerators, the first-order phase ellipse formalism of TRANSPORT is a reasonable representation of physical reality. For other applications, such as charged particle spectrometers, caution is in order in its use and interpretation.

The equation of an n-dimensional ellipsoid may be written in matrix form as follows:

$$X(0)^T \sigma(0)^{-1} X(0) = 1 \quad , \tag{2}$$

where $X(0)^T$ is the transpose of the coordinate vector X(0), and $\sigma(0)$ is a real, positive definite, symmetric matrix.

The volume of the n-dimensional ellipsoid defined by sigma is $[\pi^{m/2}/\Gamma(n/2+1)]$ (det σ)^{1/2}. The area of the projection in one plane is $A = \pi(\det \sigma_1)^{1/2}$, where σ_1 is the submatrix corresponding to the given plane. This is the "phase space" occupied by the beam.

As a particle passes through a system of magnets, it undergoes the matrix transformation of Eq. (1). Combining this transformation with the equation of the initial ellipsoid, and using the identity $RR^{-1} = I$ (the unity matrix), it follows that

$$X(0)^T (R^T R^{T^{-1}}) \sigma(0)^{-1} (R^{-1} R) X(0) = 1$$

from which we derive

$$[RX(0)]^T [R\sigma(0) R^T]^{-1} [RX(0)] = 1 .$$
(3)

The equation of the new ellipsoid after the transformation becomes

$$X(1)^T \sigma(1)^{-1} X(1) = 1 \quad , \tag{4}$$

where

$$\sigma(1) = R\sigma(0) R^T \quad . \tag{5}$$

It can readily be shown that the square roots of the diagonal terms of the sigma matrix are a measure of the "beam size" in each coordinate. The off-diagonal terms determine the orientation of the ellipsoid in n-dimensional space (for TRANSPORT n = 6).* Thus, we may specify the beam at any point in the system via Eq. (5), given the initial "phase space" represented by the matrix elements of $\sigma(0)$.

The initial beam is specified by the user as one of the first elements of the beam line. Normally it is taken to be an upright ellipse centered on the reference trajectory; that is, there are no correlations between coordinates. Both correlations and centroid displacements may be introduced via additional elements.

The phase ellipse may be printed wherever desired. For an interpretation of the parameters printed see the section under Type Code 1.0.

^{*} See the Appendix of this report (to be published under a separate cover), or the Appendix of Ref. 5, for a derivation of these statements.

When a second-order calculation is specified, the second-order matrix elements are included in the beam matrix.

Fitting

Several types of physical elements have been incorporated in the program to facilitate the design of very general beam transport systems. Included are an arbitrary drift distance, bending magnets, quadrupoles, sextupoles, solenoids, and an accelerator section (to first-order only). Provision is made in the program to vary some of the physical parameters of the elements comprising the system and to impose various constraints on the beam design. In a first-order run one may fit either the TRANSFORM (R) matrix representing the transformation of an arbitrary ray through the system and/or the phase ellipse (sigma) matrix representing a bundle of rays by the system as transformed. In a second-order run one may fit either the second-order TRANSFORM (T) matrix or minimize the net contribution of second-order terms to the beam (sigma) matrix.

The program will normally make a run through the beam line using values for the physical parameters as specified by the user and printing the results. If constraints and parameters to be varied are indicated, it will attempt to fit. To do this it will make an additional series of runs through the beam line. Each time it will calculate corrections to be made from the previous step to the varied parameters to try to satisfy the indicated constraints. When the constraints are satisfied (or the fitting procedure has failed) the program will make a final run through the beam line again printing the results. In this final run the values of the physical parameters used are those which are the result of the fitting procedure.

Thus, in principle, the program is capable of searching for and finding the firstor second-order solution to any physically realizable problem. In practice, life is not quite so simple. The user will find that an adequate knowledge of geometric magnetic optics principles is a necessary prerequisite to the successful use of TRANSPORT. He (or she) should possess a thorough understanding of the first-order matrix algebra of beam transport optics and of the physical interpretation of the various matrix elements. In other words, the program is superb at doing the numerical calculations for the problem but not the physics. The user must provide a reasonable physical input if he (or she) expects complete satisfaction from the program. For this reason a list of pertinent reprints and references is included at the end of this manual. They should provide assistance to the inexperienced as well as the experienced user.

INPUT FORMAT FOR TRANSPORT

By the TRANSPORT input DATA SET is meant the totality of data read by the program in a single job. A DATA SET may consist of one or more problems placed sequentially. A problem specifies a calculation or set of calculations to be done on a given beam line.

A problem, in turn, may consist of one or more problem steps. The data in the first step of a problem specify the beam line and the calculations to be made. The data in succeeding steps of the same problem specify only changes to the data given in the first step.

A common example of a problem with several steps is sequential fitting. In the first step one may specify that certain parameters are to be varied to satisfy certain constraints. Once the desired fit has been achieved the program will then proceed to the next step. The data in this step now need specify only which new parameters to vary, or old ones no longer to vary, or which constraints to add or delete. The values of the varied parameters that are passed from one step to the next one are those that are the result of the fitting procedure.

A problem step contains three kinds of DATA cards: the TITLE card, the INDI-CATOR card, and the ELEMENT cards.

The TITLE card contains a string of characters and blanks enclosed by single quotes. Whatever is between the quotes will be used as a heading in the output of a TRANSPORT run.

The second card of the input is the INDICATOR card. If the data which follow describe a new problem, a zero (0) is punched in any column on the card. If the data which follow describe changes to be made in the previous problem step, a one (1) or two (2) is punched in any column on the card. For further explanation read the Indicaator Card section of this manual.

The remaining cards in the deck for a given problem step contain the DATA describing the beam line and the calculations to be done. The DATA consist of a sequence of elements whose order is the same as encountered as one proceeds down the beam line. Each element specifies a magnet or portion thereof or other piece of equipment, a drift space, the initial beam phase space, a calculation to be done, or a

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print instruction. Calculation specifications, such as misalignments and constraints, are placed in sequence with the other beam line elements where their effect is to take place. The input format of the cards is "free-field," which is described below. The data for a given problem step are terminated by the word SENTINEL, which need not be punched on a separate card.

Each element, in turn, is given by a sequence of items (mostly numbers), separated by spaces and terminated by a semicolon. The items, in order, are a type code number, a very field, the physical parameters, and an optional label.

The type code number identifies the element, indicating what sort of entity (such as a magnet, drift space, constraint, etc.) is represented. It is an integer (number) followed by a decimal point. The interpretation of the physical parameters which follow is therefore dependent on the type code number. The type code numbers and their meanings are summarized in Table I. If the type code number is negative, the element will be ignored in the given problem step. However, storage for that element will be allocated by the program, so that the element may be introduced in a later step of the same problem. Storage space for any element in any problem step must be allocated in the first step of the problem.

The vary field indicates which physical parameters of the element are to be adjusted if there is to be any fitting. It is punched immediately (no intervening blanks) to the right of the decimal point of the type code number. See the section under type code 10.0 for an explanation of the use of vary codes.

The physical parameters are the quantities which describe the physical element represented. Such parameters may be lengths, magnetic fields, apertures, rotation angles, beam dimensions, or other quantities, depending on the type code number. The meanings for the physical parameters for each type code are described thoroughly in the section for that type code. A summary, indicating the order in which the physical parameters should be punched, is given in Table I. For any element the first physical parameter is the second entry in Table I or the second parameter in the section describing a given element. In some cases the parameters of an element do not really refer to physical quantities, but will nevertheless be referred to as such in this manual. The label, if present, contains one to four characters and is enclosed by single quotes, slashes, or equal signs. During the calculation the elements will be printed in sequence and the label for a given element will be printed with that element. Labels are useful in problems with many elements and/or when sequential fitting is used. They must be used to identify any element to be changed in succeeding steps of a given problem.

Provision has been made in the program to allow the user to introduce comments before any type code entry in the data deck. This is accomplished by enclosing the comments made on each card within single parentheses.

Each element must be terminated by a semicolon (;). Optionally a semicolon may be replaced by an asterisk (*) or a dollar sign (\$). Spaces before and after the semicolon are allowed but not required. If the program encounters a semicolon, dollar sign, or asterisk before the expected number of parameters has been read in and if the indicator card was a zero (0), the remaining parameters are set to zero. If the indicator card was a one (1) or two (2), then the numbers indicated on the card are substituted for the numbers remaining from the previous solution; all other numbers are unchanged.

The "free-field" input format of the data cards makes it considerably easier to prepare input than the standard fixed-field formats of FORTRAN. Numbers may be punched anywhere on the card and must simply be in the proper order. They must be separated by one or more blanks. Several elements may be included on the same card and a single element may continue from one card to the next. A single number must be all on one card; it may not continue from one card to the next. The program storage is limited to a total of 2,000 locations (including type codes and those parameters not punched but implied equal to zero) and 500 elements.

A decimal number (e.g., 2.47) may be represented in any of the following ways:

2.47 .00247+3 .0247E+02 247E-2 247000-5

The sample problem below contains two problem steps, each beginning with title

and indicator cards and terminating with a SENTINEL. The first step causes TRANS-PORT to do a first-order calculation with fitting. The second initiates a second-order calculation with the data that is a result of that fitting. Corresponding elements between the two steps are identified by having the same label.

The type ten element which specifies the fitting condition is labeled FIT1. It is active for the first-order calculation, but is turned off for the second-order calculation. The vary codes for elements DR1 are set to zero for the second-order problem. The second-order element, SEC1, is ineffective during the fitting, but causes the program to compute the second-order matrices in the second calculation.



SENTINEL Second sentinel signifies end of run.

As many problems and problem steps as one wishes may be stacked in one job.

Note that in previous versions of TRANSPORT a decimal point was required with every numerical entry except the indicator card (which must not have a decimal point in any version of TRANSPORT).

The Use of Labels

The use of labels is available for identification of individual elements. When inserted for the user's convenience, the association of a label with a given element is optional. If the parameters of an element are to be changed between steps of a given problem, a label is required. The label identifies the element in the earlier step to which the changes specified in the latter step are to apply.

The label may be placed anywhere among the parameters of a given element. It should be enclosed in quotes, slashes, or equal signs. Blanks within a label are ignored. The maximum length of a label is four non-blank characters.

As an example, the following all denote the same drift space:

'DRF' 3. 1.5 ; 3/DRF/15-1* 3. .15E1 = D R F = \$

On a 15.0 type code element the label may not be the third item. This is to avoid ambiguities with the unit name. Thus the following are not equivalent:

> This entry is used as the units symbol. This entry is used as a label. 15. 1. 'FT' 'CM' ; 15. 1. 'CM' 'FT' ;

If the parameters describing an element are to differ in succeeding steps of a given problem the element must be included in both steps, having the same label each time. All elements which appear in a problem must be included in the first step (indicator card 0) of that problem. Only those to be changed in later steps need to be labeled. In later steps (indicated card 1) of a problem only those elements to be changed are specified. The elements to be changed are identified by their labels.

If the type code number of an element is negative in a given step of a problem, that element will be ignored when the calculation is performed. However, storage space in the computer will be allocated for the element for possible activation in later steps of the problem. In the later step, only those parameters to be changed need to be specified. The storage space allocated for the parameters of a given element is determined only by the type code. The sole exceptions are the continuation codes for type codes 1.0 and 14.0.

For example, if a fitting constraint is to be ignored in the first step of a problem, but activated in a latter step, it should be indicated in both steps. In the first step such an element might appear as

-10. 'FIT';

In the later step one would then insert

10. 1. 2. 0.0 .001 'FIT' ;

causing a waist constraint to be imposed on the beam. Alternatively one can specify the physical parameters in the first step and then, in the later step, merely indicate that the element is now to be activated. The above procedure is therefore equivalent to placing the element:

-10. 1. 2. 0.0 .001 'FIT' ;

in the first problem step, and the element

10. 'FIT';

in the later step.

Vary codes may also be inserted or removed in passing from one problem step to the next. For instance, one might wish to vary the field of a quadrupole in one step of a problem and then use the fitted value as data in the following step. The first step might then contain the element:

5.01 5.0 10.0 5.0 'QUAD';

and the following step would contain the element

5. 'QUAD';

Since, in the second step, the first item on the card contains no vary code the vary code is deleted. All other parameters, not being respecified, are left unchanged.

Several elements may have the same label. If, as in the above example, one wished to vary the field of several quadrupoles in one step, then pass the final values to the next step, one could give all such elements the same label. There might be four quadrupoles, all labeled 'QUAD', being varied simultaneously. If the data for the next step contain the single element

5. 'QUAD';

the vary code on all elements labeled 'QUAD' will be deleted.

The physical parameters of an element may be changed between steps of a problem. In the first step a bending magnet may be given a length of 5 meters.

4. 5.0 10.0 0.0 'BEND' ;

In a succeeding step, its length could be increased to 10 meters by inserting the element 4. 10.0 'BEND' ;

All parameters, up to and including the one to be changed, must be specified. the remaining, if deleted, will be left unchanged from the previous step.

Table 1: Summary of TRANSPORT Type Codes

	PHYSICAL ELEMENT	TYPE CODE	2nd ENTRY	3rd ENTRY	4th ENTRY	Sth ENTRY	6th ENTRY	7th ENTRY	8th ENTRY	9th ENTRY
- 1	BEAM	1.000000	x(cna)	θ(mar)	y(cm)	¢(mr)	l (cm)	δ(percent)	P.	
	r.m.s. ADDITION TO	1.0000000	Δx(cm)	Δθ(mr)	Δy(can)	∆¢(mr)	Δ£ (Cm)	Δδ(percent)	ΔP	0
	BEAM ENVELOPE	2 11	ANGLE JOF						(Gev/C)	
	POLE FACE ADIATION	2	ROTATION (degrees)							
	DRIFT	3.v	LENGTH (metres)		FIELD GRADIENT					
	BENDING MAGNET	4.vvv	LENGTH (metres)	FIELD (kG)	(n-value)					
	QUADRUPOLE	5.vv0	LENGTH (metres)	FIELD (kG)	HALF-APERTURE (cm)					
	TRANSFORM 1 UPDATE	6.0	0.0	1.0						
	TRANSFORM 2 UPDATE	6.0	0.0	2.0						
	BEAM CENTROID SHIFT	7. vvvvv	SHIFT (x)(can)	SHIFT (0) (mr)	SHIFT (y)(cm)	SHIFT (¢)(mr)	SHIFT (1)(cm)	SHIFT (& percent)		
•	ALIGNMENT TOLERANCE	8.000000	DISPLACEMENT (x) (cm)	ROTATION (0)(mr)	DISPLACEMENT (y)(cm)	ROTATION (¢)(mr)	DISPLACEMENT (z)(cm)	ROTATION (a)(mr)	CODE NUMBER	
	REPEAT CONTROL	9.0	NUMBER OF REPEATS							
	FITTING CONSTRAINTS	10.0	±I	J	DESIRED VALUE OF (I,J) MATRIX ELEMENTS	ACCURACY OF FIT				
t	Note: +I is used f	or fitting	a beam (σ) matrix elem	mentI is used	for fitting an R1 mat	rix element.	I	•		L
ļ	- (I + 20) i	s used for	fitting an R2 matrix	element.		·····				
	ACCELERATOR	11.0	LENGTH (metres)	E (energy gain) (GeV)	<pre>\$ (phase lag) (degrees)</pre>	(WAVELENGTH) (cm)				
	BEAM (Rotated Ellipse)	12.0	THE FIFTEEN CORRELAT	IONS AMONG THE SIX EL	EMENTS (This entry mu	st be preceded by	a type code 1.0 entry	.)		
	INPUT/OUTPUT ' OPTIONS	13.0	CONTROL CODE NUMBER							
	ARBITRARY R MATRIX	14.000000	R(J,1)	R(J,2)	R(J,3)	R(J,4)	R(J,5)	R(J,6)	J	
	UNITS CONTROL (Transport Dimensions)	15.0	CODE	UNIT SYMBOL	SCALE FACTOR (if required)					
	QUADRATIC TERM OF BENDING FIELD	16.0v	1.0	$\varepsilon(1) = \beta(\frac{1}{\rho_0})^2$	p, in units of transv	erse length (cm)				
	MASS OF PARTICLES IN BEAM	16.0	3.0	M/m (dimensionless)	m = mass of electron					
	HALF-APERTURE OF BENDING MAGNET IN x-PLANE	16.0	4.0	w/2 (cm)						
	HALF-APERTURE OF BENDING MAGNET IN y-PLANE (gap)	16.0	5.0	g/2 (cm)						
	LENGTH OF SYSTEM	16.0	6.0	L (metres)						
ĺ	FRINGE FIELD COR- RECTION COEFFICIENT	16.0	7.0	K ₁ (dimensionless)						
	FRINGE FIELD COR- RECTION COEFFICIENT	16.0	8.0	K ₂ (dimensionless)						
	CURVATURE OF ENTRANCE FACE OF BENDING MAGNET	16.0v	12.0	(1/R ₁) (1/metres)						
	CURVATURE OF EXIT FACE OF BENDING MAGNET	16.0v	13.0	(1/R ₂) (1/metres)						
	FOCAL PLANE ROTATION	16.0	15.0	Angle of focal plane See type code 16.0 f	e rotation (degrees). For details.					
	INITIAL BEAM LINE x-COORDINATE	16.0V	16.0	Xe						
	INITIAL BEAM LINE y-COORDINATE	16.0V	17.0	Уa						
	INITIAL BEAM LINE z-COORDINATE	16.0V	18.0	20						
	HORIZONTAL ANGLE	16.0V	19.0	θ.						
	INITIAL BEAM LINE VERTICAL ANGLE	16.0V	20.0	\$ 0						
	SECOND-ORDER CALCULATIONS	17.0								
	SEXTUPOLE	18.0v	LENGTH (metres)	FIELD (kG)	HALF-APERTURE (cm)					
	SOLENOID	19.vv	LENGTH (metres)	FIELD (kG)						
	BEAM ROTATION	20.v	ROTATION (degrees)							
	STRAY FIELD	21.0	See later section of	report.						
	Note: The v's foll Vary Codes	lowing the t	ype codes indicate th are standard TRANSPOR	e parameters which ma T units (as shown) un	ny be varied. See sec less changed via type	tion under type co code 15.0 entries	de 10.0 for a detaile	d explanation of		

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OUTPUT FORMAT

General Appearance

Here we give a brief description of the general appearance of the output and its meaning. The user may refer to the sample output shown on pages 22 through 27. It is the printed output resulting from the sample data shown in the section on input format. In a simple example it is not possible to show each of the different type codes. Several of the type codes produce output which is not characteristic of all other type codes. We therefore refer the user to the sections on the various type codes for an explanation of any features peculiar to a given type code.

The output for each step of a given problem is printed separately. The printing for one step is completed before that for the next step is begun. Therefore we will describe the output for a single problem step. The output shown below is from a problem with two steps.

Initial Listing

For each problem step, the program begins by printing out the user's input records.

Listing During the Calculation

The program now begins the calculation. If there is no fitting, one listing of the beam line will be made. If there is fitting there will normally be two listings. The first will represent the beam line before any fitting has occurred. The second will be based on the new values of the physical parameters which were altered by the fitting process. If sequential fitting is employed and an indicator card of two (2) is used the first run will be omitted. The user should read the section describing the indicator card for further explanation.

In any listing the elements are printed in order with their labels and physical parameters. Elements with negative type code numbers are ignored. Each listed element is preceded by the name of that type of element, enclosed in asterisks. All physical elements are listed in this way. Some of the other elements are not explicitly listed but produce their effect in either the calculated quantities or the listing of the beam line. For descriptions of individual cases, the reader should consult the sections on the type codes.

Calculated quantities appear in the listing as requested in the input data. Important cases will be described in greater detail below. The physical parameters for each element are printed with the appropriate units. For some elements a calculated quantity, not in the input data, will appear, enclosed in parenthesis. Such quantities are explained in the sections under the individual type codes.

Calculated Quantities

The important cases of calculated quantities which appear in the output are the transfer matrices, the beam matrix, the layout coordinates, and the results of the fitting procedure. The transfer and beam matrices and layout coordinates appear as requested in the listing of the beam line. The results of the fitting procedure appear between the two listings. All these quantities are explained in greater detail below.

The transfer and beam matrices appear only where requested. A request for printing of layout coordinates should be made at the beginning of the beam line. The coordinates will then be printed after each physical element. In all cases the quantities printed are the values of the interface between two elements. They are evaluated at a point after the element listed above them and before the element listed below. For further explanation of calculated quantities the user should read the section on the mathematical formulation of TRANSPORT and the sections on the appropriate type codes. For the transfer matrix the appropriate type code is thirteen; for the beam matrix it is one, and for the coordinate layout it is again thirteen.

Quantities relevant to the fitting appear between the two listings of the beam line. At each iteration of the fitting procedure a line is printed containing the value of the relaxation factor used, the value of chi-squared before the iteration was made, and the corrections made to each of the varied parameters. Once the fitting is complete the final chi-squared and the covariance matrix are printed. For further details the user should read the section on type code 10.0.

TRANSPORT UPDATED JULY 1974

NEW MISALIGNMENT FEATURES MAY BE ACTIVATED BY MEANS OF CODE ON MISALIGNMENT CARD A 1 IN THE TENS POSITION CAUSES THE RESULTS OF THE MISALIGNMENT TO BE PLACED IN A MISALIGNMENT TABLE, UHICH IS PRINTED WHEREVER AN 13. B. CARD IS INSERTED A 4 IN THE ONES POSITION MISALIGNS ALL SUBSEQUENT BEND MAGNETS, UP TO TEN A 5 IN THE ONES POSITION MISALIGNS ALL SUBSEQUENT QUADRUPOLES, UP TO TEN A 3 IN THE ONES POSITION MISALIGNS ALL SUBSEQUENT BENDS OR QUADS, UP TO TEN THE UNITS FOR BEND ANGLE, POLE FACE ROTATION ANGLE, AND LAYOUT ANGLE MAY BE CHANGED VIA A 15. 7. ENTRY THE ANGLES OF THE REFERENCE TRAJECTORY NOW APPEAR IN THE COORDINATE LAYOUT THE PRINTING OF PHYSICAL PARAMETERS FOR ELEMENTS MAY BE SUPPRESSED BY A 13. 17. CARD

ONLY VARIED ELEMENTS OR CONSTRAINTS WILL BE PRINTED IF A 13. 18. CARD IS INSERTED THE TRANSPER AND BEAM MATRICES WILL OCCUPY A SINGLE LINE IF A 13. 19. CARD IS INSERTED THE INITIAL LISTING OF THE DECK WILL BE DELETED IF 10 IS ADDED TO THE IMDICATOR THE BEAM MATRIX IS PRINTED AFTER EACH ELEMENT ONLY IF ACTIVATED VIA A 13. 3. CARD THE TRANSPER MATRIX MAY BE PRINTED AFTER EACH ELEMENT BY USING A 13. 6. CARD

THE BEAH CENTROID MAY BE VARIED

"FORTRAN H CHEC	K ON BETA FIT					17		
0								
1.000000		0.50000	1.00000	0.50000	1.00000	0.50000	1.00000	1.00000;
-17.	"SEC1" ;							
13.		3.00000;						
3.3	"DR1 "	2.74500;						
2.0		0.0 ;						
4.000		9.87900	10.00000	0.50000;				
2.0		0.0 ;						
3.3	"DR1 "	2.74500;						
- 13.		4.00000;						
10.0	"FIT "	-1.00000	2.00000	0.0	0.00010;			
SENTINEL								

PORTRAN H CHE	CK ON BI	ETA PIT												
BEAN	1.		1.00000	CEV										
0.0 M				+			0.0	0.500	CM					
							0.0	1.000	MR	0.0				
							0.0	0.500	CH	0.0	0.0			
							0.0	1.000	HR	0.0	0.0	0.0		
							0.0	0.500	CM	0.0	0.0	0.0	0.0	
	_	.					0.0	1.000	PC	0.0	0.0	0.0	0.0	0.0
DRIFT	3.	"DR1 "	2.74500	n										
VARY CODE	- 3													
2.745 n							0.0	0.570	Cn					
							0.0	1.000	CH CH	0.401				
							0.0	0.370	10	0.0	0.0			
							0.0	0.500	CM	0.0	0.0	0.401		
							0.0	1 000	80	0.0	0.0	0.0	0.0	
	,		0.0	DEC			0.0	1,000	FU	0.0	0.0	0.0	0.0	0.0
2.745 H			0.0	044			0.0	0.570	СН					
							0.0	1.000	HR	0.481				
							0.0	0.570	СН	0.0	0.0			
							0.0	1.000	HR	0.0	0.0	0.481		
							0.0	0.500	CH	0.0	0.0	0.0	0.0	
							0.0	1.000	PC	0.0	0.0	0.0	0.0	0.0
BEND	4.		9.87900	n	10.00000	KG	0.50000	(3.	336 11 .	169.690	DEG)		
12.624 1							0.0	10.013	CM	•				
							0.0	12.324	MR	0.993				
							0.0	0.369	CM	0.0	0.0			
							0.0	1.360	MR	0.0	0.0	-0.086		
							0.0	11.690	CM	-0.992	-0.972	0.0	0.0	
							0.0	1.000	PC	0.999	0.994	0.0	0.0	-0.991
ROTAT	2.		0.0	DEC										
12.624 M							0.0	10.013	CH					
							0.0	12.324	НR	0.993				
							0.0	0.369	CH	0.0	0.0			
							0.0	1.360	ĦR	0.0	0.0	-0.086		
							0.0	11.690	СН	-0.992	-0.972	0.0	0.0	·
	-						0.0	1.000	PC	0.999	0.994	0.0	0.0	-0.991
DRIFT	3.	"DRI "	2.74500	M										
VART COPE	- ,								~ ~					
12.309 M							0.0	13.3//	GR	0 004				
							0.0	12.324	CH	0.770				
			•				0.0	1 340	UR MB	0.0	0.0	0 681		
							0.0	11 690	CH CH	-0.988	-0.972	0.001	0 0	
							0.0	1 000	BC	-0.900	0.972	0.0	Å. Å	-0 991
							0.0	1.000	10	0.,,,,	0.,,,	0.0	0.0	-0.991
"IKANSPOKIT I"	1.00383	-0.00418	0.0	0.0	0.0	13.36808								
_	1.83605	-1.00383	0.0	0.0	0.0	12.24879								
	0.0	0.0	-1.00383	-0.00418	0.0	0.0								
	0.0	0.0	-1.83605	-1.00383	0.0	0.0								
-	1.22488	-1.33681	0.0	0.0	1.00000	-11.58649								
	0.0	0.0	0.0	0.0	0.0	1.00000								
FIT	10.0	"FIT "	-1. 2.	0.0	/0.	00010	(-0.	00418)						
LENGTH	15.1	36899 H												
CORRECTIONS														
0.10000E+01	(0.1747	/6E+04) -	0.0208											
0.10000E+01	(0.6324	7E-02) -	0.0000											
*COVARIANCE	(FIT 0.3	39529%-05)												
0.000														

FORTRAS & CHECK OF BETA FIT

BEA:1	1.		1.00000	GEV										
0.0	1						0.0	0.500	CH					
							0.0	1.000	NR	0.0				
							0.0	0.500	CM	10.0	0.0			
							0.0	1.000	HR .	0.0	0.0	0.0		
							0.0	0 500	CH	0.0	0.0	0.0	0 0	
							0.0	1 000	PC	0.0	0.0	0.0	0.0	
****	2	"ne1 "	2 72616	*1			0.0	1.000	rç	0.0	0.0	0.0	0.0	0.0
UKIF1	J.	176.1	2.72414											
VARI CO	UF. = 3								~ ~					
2.724	1						0.0	0.309	Un					
							0.0	1.000	nĸ	0.4/8				
							0.0	0.569	Cn	0.0	0.0			
							0.0	1.000	nR	0.0	0.0	0.4/8		
							0.0	0.500	CH	0.0	0.0	0.0	0.0	
							0.0	1.000	PC	0.0	0.0	0.0	0.0	0.0
ROTAT	2.		0.0	DEG										
2.724	1						0.0	0.569	CH					
							0.0	1.000	MR	0.478				
							0.0	0.569	CH	0.0	0.0			
							0.0	1.000	MR	0.0	0.0	0.478		
							0.0	0.500	CM	0.0	0.0	0.0	0.0	
							0.0	1.000	PC	0.0	0.0	0.0	0.0	0.0
BEND	4.		9.87900	н	10.00000	KG	0.50000	(3.3	36 11 ,	169.690	DEC)		
12.603	4						0.0	10.013	CH					
							0.0	12.324	HR	0.993				
							0.0	0.370	CM	0.0	0.0			
							0.0	1.357	tiR	0.0	0.0	-0.086		
	•						0.0	11.690	CH	-0.992	-0.972	0.0	0.0	
							0.0	1.000	PC	0.999	0.994	0.0	0.0	-0.991
	2		0.0	DEC							••••		•••	
12 603	4		0.0	020			0.0	10.013	CH					
12.005	1						0.0	12.324	HR	0.993				
							0.0	0 370	CM	0.0	0 0			
							0.0	1 357	MP	0.0	0.0	-0 086		
							0.0	11 600	CH CH	-0.001	-0.072	-0.000		
							0.0	11.070	50	-0.772	-0.972	0.0	0.0	-0.001
	•						0.0	1.000	PC	0.999	0.994	0.0	0.0	-0.991
DRIFT	3.	"DKI "	2./2414	n										
VARY CO	DE = 3								5					
15.327	M						0.0	13.352	CH					
							0.0	12.324	nĸ	0.990				
							0.0	0.500	CM	0.0	0.0			
							0.0	1.357	MR	0.0	0.0	0.676		
							0.0	11.690	CH	-0.989	-0.972	0.0	0.0	
							0.0	1.000	PC	0.999	0.994	0.0	0.0	-0.991
TRANSFORM	1													
	-1.00000	-0.00000	0.0	0.0	0.0	13.34253								
• ·	-1.83605	-1.00000	0.0	0.0	0.0	12.24879								
	0.0	0.0	-1.00000	0.00000	0.0	0.0								
	0.0	0.0	-1.83605	-1.00000	0.0	0.0								
	-1.22488	-1.33425	0.0	0.0	1.00000	-11.58649								
	0.0	0.0	0.0	0.0	0.0	1.00000								
4T17#	10.0	"FIT "	-1, 2.	0.0	D /O.	00010	(-0.	00000)						
LENGTH	15.3	2727 11												

36. I

"SECOND ORD	ER										
1.00000	0		0.50000	1.00000	0.50000	1.00000	0.50000	1.00000	1.00000;		
* 17.		SEC1" ;	3.00000;								
* 3.0	"	DRI "	2.72414;								
2.0			9.87900	10.00000	0.50000+						
2.0			0.0 :		0150000,						
* 3.0	"'	DRI "	2.72414; 4.00000;								
• -10.	"1	FIT "	-1.00000	2.00000	0.0	0.00010;					
SENTINEL SECOND ORDE	R										
BEAH	۱.		1.0000	B GEV							
0.0	11					0.0	0.500 (m			
						0.0	1.000	1R 0.0			
						0.0	1.000	111 0.0	0.0 0.0		
						0.0	0.500	:H 0.0	0.0 0.0	0.0	
						0.0	1.000	C 0.0	0.0 0.0	0.0	0.0
#2ND ORDER#	17.	"SECI"	GA	USSIAN DIS	TRIBUTION						
DRIFT	3.	"DR1 "	2.7241	s n			0 560 /	- M			
2.724	п					0.0	1.000 1	IR 0.478			
						0.0	0.569	CH 0.0	0.0		
						0.0	1.000 1	IR 0.0	0.0 0.478		
						-0.00	0 0.500 0	CM 0.0	0.0 0.0	0.0	
	•					0.0	1.000	PC 0.0	0.0 0.0	0.0	0.0
ROTAT	и 2.		0.0	PEG		0.00	0 0 569 0	. 11			
4.744						0.00	1.000 1	1R D.478			
						0.0	0.569	CH 0.0	0.0		
						0.0	1.000	IR 0.0	0.0 0.478		
						-0.00	0 0.500	CH -0.000	0.0 0.0	0.0	
						0.0	1.000	PC 0.0	0.0 0.0	0.0	0.0
BEND	. 4.		9.8790	DM	10.00000 KG	0.0000		3.336 11 ,	169.690 DEG)		
12.003	А					0.00	12.324	18 0.993			
						0.0	0.370	n 0.0	0.0		
						0.0	1.358 1	1R 0.0	0.0 -0.086		
						-0.00	2 11.690	CH -0.992	-0.972 0.0	0.0	
						0.0	1.000	PC 0.999	0.994 0.0	0.0	-0.991
ROTAT	, ² .		0.0	DEG		0.06					
12.003	n					0.00	7 12.324	18 0.993			
						0.0	0.370	0.0	0.0		
						0.0	1.358 1	IR 0.0	0.0 -0.086		
						-0.00	2 11.690	CM -0.992	-0.972 0.0	0.0	
						0.0	1.000	PC 0.999	0.994 0.0	0.0	-0.991
DRIFT	. 3.	"DR1 "	2.7241	• 11		0.07	R 13.352	. M			
15.347	71					0.07	7 12.324	18 0.996			
						0.0	0.500	CH 0.0	0.0		
						0.0	1,358	1R 0.0	0.0 0.676		
						-0.02	11.690	CH -0.988	-0.972 0.0	0.0	
						0.0	1.000	rc 0.999	0.994 0.0	0.0	-0.991
*TRANSFORM	17	-0.0000			0 0 11	14251					
	-1.83605	-1.0000	0 0.0	0.0	0.0 12	24879					
	0.0	0.0	-1.00000	0.00000	0.0 0.	0					
	0.0	0.0	-1.83605	-1.00000	0.0 0.	.0					
	-1.22488	-1.3342	5 0.0	0.0	1.00000 -11	. 58649					
	0.0	0.0	0.0	0.0	0.0 1.	.00000					

24

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* 2 N I	D O	RDER TRANSI	orn*														
1	11	1.124E-03	3														
1	12	1.225E-03	3 1	22	6.673E-04												
1	13	0.0	1	23	0.0	1	33	-4.871E-03									
1	14	0.0	1	24	0.0 _	1	34	-2.042E-03	1	44	-1.112E-03						
ī	15	0.0	1	25	0.0	1	35	0.0	ī	45	0.0	1	55	0.0			
1	16	2.065E-02	2 1	26	3.066E-02	1	36	0.0	1	46	0.0	1	56	0.0	1	66	7.908E-02
2	11	6.046E-07	,														
2	12	1.316E-06	5 2	22	6.126E-04												
2	13	0.0	2	23	0.0	2	33	-5.504E-03									
2	14	0.0	2	24	0.0	2	34	-2.999E-03	2	44	-1.021E-03						
2	15	0.0	2	25	0.0	2	35	0.0	2	45	0.0	2	55	0.0			
2	16	3.097E-02	2 2	26	3.564E-02	2	36	0.0	2	46	0.0	2	56	0.0	2	66	3.835E-02
3	11	0.0									÷						
3	12	0.0	3	22	0.0												
3	13	-7.500E-04	• 3	23	-2.042E-03	3	33	0.0									
3	14	-2.042E-03	3	24	-2.224E-03	3	34	0.0	3	44	0.0						
3	15	0.0	3	25	0.0	3	35	0.0	3	45	0.0	3	55	0.0			
3	16	0.0	3	26	0.0	3	36	-1.064E-02	3	46	-3.414E-03	3	56	0.0	3	66	0.0
4	11	0.0															
4	12	0.0	4	22	0.0												
4	13	5.503E-03	34	23	5.994E-03	4	33	0.0									
4	14	-2.999E-03	3 4	24	-2.042E-03	- 4	34	0.0	4	44	0.0						
4	15	0.0	- 4	25	0.0	- 4	35	0.0	4	45	0.0	4	55	0.0			
4	16	0.0	4	26	0.0	4	36	5.756E-03	4	46	4.367E-03	4	56	0.0	4	66	0.0
LEI	NGT	H	15.3	272	7 11												

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TITLE CARD

The title card is the first card in every problem step of a TRANSPORT data set. The title card is always required and must be followed by the indicator card (see next section) to indicate whether the data to follow is new (0 card) or a continuation of a previous data set (a 1 card or a 2 card).

The title must be enclosed within either quotation marks ('), slashes (/), or equal signs (=) on a single card. The string may begin and end in any column (free field format), for example

'SLAC 20 GeV/c SPECTROMETER'

or

/SLAC 20 GeV SPECTROMETER/

Note that whichever character is used to enclose the title *must not be used* again within the title itself.

Example of a DATA SET for a Single Problem Step



INDICATOR CARD (0, 1, or 2)

The second card of the input for each step of a problem is the indicator card. If the data which follow describe a new problem, a zero (0) is punched in any column on the card. If the data which follow describe changes to be made in the previous step of a given problem, a one (1) or two (2) is punched in any column on the card.

If a given problem step involves fitting, the program will normally list the beam line twice, printing each time the sequence of elements along with transfer or beam matrices where specified. The first listing uses the parameters of each element before any fitting has taken place. The second shows the results of the fitting. If a problem involving fitting has several steps, the second run of a given step often differs little from the first run of the following step.

If the second or subsequent step of a problem involves fitting and one wishes to print both runs through the beam line, a one (1) is punched on the indicator card. If the first listing is to be suppressed a two (2) is punched. If no fitting is involved, the program will ignore the 2 and will do one single run through the system.

If the initial listing is to be deleted, 10 is added to the indicator to give 10, 11 or 12. In order to be consistent with earlier versions of TRANSPORT, an indicator of minus one (-1) is interpreted as a two (2), but nine (9) is not interpreted as twelve (12).

The sample problem input shown on page 14 causes TRANSPORT to do a firstorder calculation with fitting (0 indicator card) and then to do a second-order calculation (1 indicator card) with the data that is the result of the fitting.

COMMENT CARDS

Comment cards may be introduced anywhere in the deck where an element would be allowed by enclosing the comments made on each card within single parentheses. No parentheses are allowed within the parentheses of any comment card. The comments are not stored, but appear only in the initial listing of the given problem step.

Example of the Use of Comment Cards in a Data Set

'Title Card' 0 (THIS IS A TEST PROBLEM TO ILLUSTRATE THE) (USE OF COMMENT CARDS) elements (COMMENTS MAY ALSO BE MADE BETWEEN) (TYPE CODE ENTRIES) elements SENTINEL

LISTING OF AVAILABLE TRANSPORT TYPE CODE ENTRIES

INPUT BEAM : Type Code 1.0

The phase space and the average momentum of the input beam for a TRANSPORT calculation are specified by this element. The input is given in terms of the semi-axes of a six-dimenational erect \bullet beam ellipsoid representing the phase space variables x, θ, y, ϕ, ℓ , and δ . Each of these six parameters is entered as a positive quantity, but should be thought of as $\pm x, \pm \theta$, etc.; hence, the total beam width is 2x, the total horizontal beam divergence is 2θ and so forth.

Usually the BEAM card is the third card in the deck. If other than standard TRANSPORT units are to be used, the units specification cards (Type Code 15.0) should precede the BEAM card. Standard TRANSPORT units for x, θ , y, ϕ , ℓ , and δ are cm, mr, cm, mr, cm and percent. The standard unit for the momentum p(0) is GeV/c. Also if a beam line coordiante layout is desired, the card specifying that a layout is to be made (a 13.0 12.0 element), and any initial coordinates (see Type Code 16.0) all precede the BEAM card.

There are eight entries (all positive) to be made on the BEAM card.

- 1 The Type Code 1.0 (specifies a BEAM entry follows).
- 2 One-half the horizontal beam extent (x) (cm in standard units).
- 3 One-half the horizontal beam divergence (θ) (mr).
- 4 One-half the vertical beam extent (y) (cm).
- 5 One-half the vertical beam divergence (ϕ) (mr).
- 6 One-half the longitudinal beam extent (ℓ) (cm).
- 7 One-half the momentum spread (δ) (in units of percent $\Delta p/p$).
- 8 The momentum of the central trajectory [p(0)] (GeV/c).

All eight entries <u>must</u> be made even if they are zero (0). As for all other type codes, the last entry <u>must</u> be followed by a semicolon, dollar sign, or asterisk. Thus a typical BEAM entry might be

^{*}For a rotated (non-erect) phase ellipsoid input, see Type Code 12.0.
meaning, $x = \pm 0.5$ cm, $\theta = \pm 2.0$ mr, $y = \pm 1.3$ cm, $\phi = \pm 2.5$ mr, $\ell = \pm 0.0$ cm, $\delta = \pm 1.5$ percent $\Delta p/p$, and the central momentum p(0) = 10.0 GeV/c.

The units of the tabulated matrix elements in either the first-order R or sigma matrix or second order T matrix of a TRANSPORT print-out will correspond to the units chosen for the BEAM card. For the above example, the $R(12) = (x/\theta)$ matrix element will have the dimensions of cm/mr; and the $T(236) = (\theta/y\delta)$ matrix element will have the dimensions mr/(cm \cdot percent) and so forth.

The longitudinal extent ℓ is useful for pulsed beams. It indicates the spread in length of particles in a pulse. It does not interact with any other component and may be set to zero if the pulse length is not important.

The phase ellipse (sigma matrix) beam parameters may be printed as output after every physical element if activated by a (13. 3. ;) element. Alternatively, individual printouts may be activated by a (13. 1. ;) element. The projection of the semi-axes of the ellipsoid upon each of its six coordinates axes is printed in a vertical array, and the correlations among these components indicating the phase ellipse orientations are printed in a triangular array (see the following pages).

The phase ellipse beam matrix

1.

The beam matrix carried in the computer has the following construction:

	x	θ	y	ø	l	δ
x	σ(11)					
θ	σ(21)	$\sigma(22)$				
y	σ(31)	$\sigma(32)$	σ(33)			
θ	σ(41)	$\sigma(42)$	σ(43)	σ(44)		
l	σ(51)	$\sigma(52)$	σ(53)	σ(54)	σ(55)	
δ	σ(61)	$\sigma(62)$	$\sigma(63)$	$\sigma(64)$	$\sigma(65)$	$\sigma(66)$

The matrix is symmetric so that only a triangle of elements is needed.

In the printed out this matrix has a somewhat different format for ease of interpretation:

			x	θ	y	ø	l
x	$\sqrt{\sigma}(11)$	CM					
θ	$\sqrt{\sigma}$ (22)	MR	r (22)				
y	$\sqrt{\sigma}$ (33)	СМ	r(31)	r (32)			
ϕ	$\sqrt{\sigma}(44)$	MR	r(41)	r(42)	r(43)		
l	$\sqrt{\sigma}$ (55)	CM	r(51)	r(52)	r (53)	r(54)	
δ	$\sqrt{\sigma}$ (66)	PC	r(61)	r (62)	r(63)	r(64)	r (65)

where

$$r(ij) = \frac{\sigma(ij)}{[\sigma(ii) \ \sigma(jj)]^{1/2}}$$

As a result of the fact that the σ matrix is positive definite, the r(ij) satisfy the relation

$$|r(ij)| \leq 1$$

The full significance of the $\sigma(ij)$ and the r(ij) are discussed in detail in the Appendix ("Description of Beam Matrix"). The units are always printed with the matrix.

In brief, the meaning of the $\sqrt{\sigma}(ii)$ is as follows:

 $\sqrt{\sigma}(11) = x_{max} =$ the maximum (half)-width of the beam envelope in the x(bend)-plane at the point of the print-out. $\sqrt{\sigma}(22) = \theta_{max} =$ the maximum (half)-angular divergence of the beam envelope in the x(bend)-plane. $\sqrt{\sigma}(33) = y_{max} =$ the maximum (half)-height of the beam envelope. $\sqrt{\sigma}(44) = \phi_{max} =$ the maximum (half)-angular divergence of the beam envelope in the y(non-bend)-plane. $\sqrt{\sigma}(55) = \ell_{max} =$ one-half the longitudinal extent of the bunch of particles. $\sqrt{\sigma}(66) = \delta =$ the half-width $(\frac{1}{2}\Delta p/p)$ of the momentum interval being transmitted by the system. The units appearing next to the $\sqrt{\sigma}(ii)$ in the TRANSPORT print-out are the units chosen for coordinates x, θ , y, ϕ , ℓ and $\delta = \Delta p/p$, respectively.

To the immediate left of the listing of the beam envelope size in a TRANSPORT print-out, there appears a column of numbers whose values will normally be zero. These numbers are the coordinates of the centroid of the beam phase ellipse (with respect to the initially assumed central trajectory of the system). They may become nonzero under one of three circumstances:

- 1. when the misalignment (Type Code 8.0) is used,
- 2. when a beam centroid shift (Type Code 7.0) is used, or
- 3. when a second-order claculation (Type Code 17.0) is used.

To aid in the interpretation of the phase ellipse parameters listed above, an example of an (x, θ) plane ellipse is illustrated below. For further details the reader should refer to the Appendix of this report.



A TWO-DIMENSIONAL BEAM PHASE ELLIPSE

The area of the ellipse is given by:

$$A = \pi (\det \sigma)^{1/2} = \pi x_{max} \ \theta_{int} = \pi x_{int} \ \theta_{max} = \pi \epsilon \ .$$

The equation of the ellipse is:

$$\gamma x^2 + 2\alpha x\theta + \beta\theta^2 = \epsilon$$

where

$$\sigma = \begin{bmatrix} \sigma_{11} & \sigma_{21} \\ \sigma_{21} & \sigma_{22} \end{bmatrix} = \epsilon \begin{bmatrix} \beta & -\alpha \\ -\alpha & \gamma \end{bmatrix}$$

and

$$\beta\gamma - \alpha^2 = 1$$
 , $r_{21} = r_{12} = -\frac{\alpha}{\sqrt{1 + \alpha^2}} = -\frac{\alpha}{\sqrt{\beta\gamma}}$

r.m.s. addition to the BEAM

To allow for physical phenomena such as multiple scattering, provision has been made in the program to permit an r.m.s. addition to the beam envelope. There are nine entries to be included:

- 1 Type Code 1.0 (specifying a BEAM entry follows).
- 2 The r.m.s. addition to the horizontal beam extent (Δx) (cm).
- 3 The r.m.s. addition to the horizontal beam divergence $(\Delta \theta)$ (mr).
- 4 The r.m.s. addition to the vertical beam extent (Δy) (cm).
- 5 The r.m.s. addition to the vertical beam divergence $(\Delta \phi)$ (mr).
- 6 The r.m.s. longitudinal beam extent $(\Delta \ell)$ (cm).
- 7 The r.m.s. momentum spread $(\Delta \delta)$ (in percent $\Delta p/p$).
- 8 The momentum change in the central trajectory $[\Delta p(0)]$ in (GeV/c).
- 9 The code digit 0. indicating an r.m.s. addition to the BEAM is being made.

The units for the r.m.s. addition are the same as those selected for a regular BEAM Type Code 1.0 entry. Thus a typical r.m.s. addition to the BEAM would appear as follows:

1. .1 .2 .15 .3 0. .13 -0.1 0. ;

where the last entry (0.) preceding the semicolon signifies an r.m.s. addition to the BEAM is being made and the next to the last entry indicates a central momentum change of -0.1 GeV/c.

FRINGING FIELDS AND POLE-FACE ROTRATIONS FOR BENDING MAGNETS: Type Code 2.0

To provide for fringing fields and/or pole-face rotations on bending magnets, the Type Code 2.0 element is used.

There are two parameters:

- 1 Type Code 2.0.
- 2 Angle of pole-face rotation (degrees).

The Type Code 2.0 element must either <u>immediately</u> precede a bending magnet (Type Code 4.0) element (in which case it indicates an entrance fringing field and pole-face rotation) or <u>immediately</u> follow a Type Code 4.0 element (exit fringing field and pole-face rotation) with no other data entries between.* A positive sign of the angle on either entrance or exit pole-faces corresponds to a non-bend plane focusing action and bend plane defocusing action.

For example, a symmetrically oriented rectangular bending magnet whose total bend is 10 degrees would be represented by the three entries

2. 5. ; 4. --- ; 2. 5. ;

The angle of rotation may be varied. For example, the element 2.1 5. ; would allow the angle to vary from an initial guess of 5 degrees to a final value which would, say, satisfy a vertical focus constraint imposed upon the system. See the Type Code 10.0 section for a complete discussion of vary codes.

Even if the pole-face rotation angle is zero, 2. 0. ; entries must be included in the data set before and after a Type Code 4.0 entry if fringing-field effects are to be calculated.

A single Type Code 2.0 entry that follows one bending magnet and precedes another will be associated with the <u>latter</u>.

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^{*} It is extremely important that no data entries be made between a Type Code 2.0 and a Type Code 4.0 entry. If this occurs, it may result in an incorrect matrix multiplication in the program and hence an incorrect physical answer. If this rule is violated, an error message will be printed.

Should it be desired to misalign such a magnet, an update element must be inserted immediately before the first type 2.0 code entry and the convention appropriate to misalignment of a <u>set</u> of elements applied, since, indeed, three separate transformations are involved. See section under Type Code 8.0 for a discussion of misalignment calculations and the section under Type Code 6.0 for a discussion of updates.

The type code signifying a rotated pole-face is 2.0. The input format is:

The units for β are degrees.

Pole – Face Rotation Matrix

The first-order R matrix for a pole-face rotation used in a TRANSPORT calculation is as follows:

$$R = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ \frac{tan\beta}{\rho_0} & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & -\frac{tan(\beta-\psi)}{\rho_0} & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix}$$

Definitions:

- β = Angle of rotation of pole-face (see figure on following page for sign convention of β).
- ρ_0 = Bending radius of central trajectory.

g =Total gap of magnet.

 ψ = Correction term resulting from spatial extent of fringing fields.*

* See SLAC-75⁴ (page 74) for a discussion of ψ .

where

$$\psi = K_1 \left(\frac{g}{\rho_0}\right) \left(\frac{1 + \sin^2\beta}{\cos\beta}\right) \left[1 - K_1 K_2 \left(\frac{g}{\rho_0}\right) \tan\beta\right] \,^{\bullet}$$



FIELD BOUNDARIES FOR BENDING MAGNETS

The TRANSPORT sign conventions for x, β , R and h are all positive as shown in the figure. The positive y direction is out of the paper. Positive β 's imply transverse focusing. Positive R's (convex curvatures) represent negative sextupole components of strength S = (-h/2R) sec³ β . (See SLAC-75, page 71.)

* See Type Code 16.0 for input formats for g, K_1 , K_2 TRANSPORT entries.

DRIFT: Type Code 3.0

A drift space is a field-free region through which the beam passes. There are two parameters:

- 1 Type Code 3.0 (specifying a drift length).
- 2 (Effective) drift length (meters). The length of a drift space may be varied in either first- or second-order fitting.

Typical input format for a DRIFT:



DRIFT Space Matrix

The first-order R matrix for a drift space is as follows:

1	L	0	0	0	0]
0	1	0	0	0	0	
0	0	1	L	0	0	
0	0	0	1	0	0	
0	0	0	0	1	0	
Lo	0	0	0	0	1	

where

L = the length of the drift space.

The dimensions of L. are those chosen for longitudinal length via a



15. 8. ''; type code entry (if used) preceding the BEAM (Type Code 1.0) card. If no 15. 8. entry is made, the units of L. will automatically be in meters (standard TRANSPORT units).

WEDGE BENDING MAGNET: Type Code 4.0

A wedge bending magnet implies that the central trajectory of the beam enters and exists perpendicularly to the pole-face boundaries (to include fringing-field effects and non-perpendicular entrance or exit boundaries – see Type Codes 2.0 and 16.0).

There are four first-order parameter to be specified for the wedge magnet via Type Code 4.0:

- 1 Type Code 4.0 (specifying a wedge bending magnet).
- 2 The (effective) length L of the central trajectory in meters.
- 3 The central field strength B(0) in kG,

$$B(0) = 33.356 \ (p/\rho_0)$$

where p is the momentum in GeV/c and ρ_0 is the bending radius of the central trajectory in meters.

4 - The field gradient (n-value, dimensionless); where n is defined by the equation

$$B_y(x, 0, t) = B_y(0, 0, t)(1 - nhx + \ldots) ,$$

where

$$h = 1/\rho_0$$
. See SLAC-75 (page 31).⁴

The quantities L, B(0), and n may be varied for first-order fitting (see Type Code 10.0 for a discussion of vary codes).

The bend radius in meters and the bend angle in degrees are printed in the output.

A typical first-order TRANSPORT input for a wedge magnet is

If fringing field effects are to be included, a Type Code 2.0 entry must immediately precede and follow the pertinent Type Code 4.0 entry (even if there are no pole-face rotations). Thus a typical TRANSPORT input for a bending magnet including fringing fields might be: Labels (not to exceed four spaces) if desired 2. 0. ' ' ; 4. L. B(0). n. ' ' ; 2. 0. ' ' ;

For non-zero pole-face rotations a typical data input might be

2. 10. ; 4. L. B(0). n. ; 2. 20. ;

Note that the use of labels is optional and that all data entries may be made on one line if desired.

The sign conventions for bending magnet entries are illustrated in the following figure. For TRANSPORT a positive bend is to the right looking in the direction of particle travel. To represent a bend in another sense, the coordinate rotation matrix (Type Code 20.0) should be used as follows:

A <u>bend up</u> is represented by rotation the (x,y) coordinates by -90.0 degrees about the (z) beam axis as follows:

- Labels (not to exceed four spaces) if desired Г 20. -90. '';، ، ; 2. β(1). **4**. L. B. n. ''; β(2). 2. • ' ; · ' ; (returns coordinates to their initial orientation) 20. +90. A <u>bend</u> down is accomplished via:

20. +90. ''; 2. 4. 2. 20. -90. ''; A bend to the left (looking in the direction of beam travel) is accomplished by rotating the x,y coordinates by 180 degrees, e.g.

20. +180. ''; 2. 4. 2. 20. -180. '';



FIELD BOUNDARIES FOR BENDING MAGNETS

The TRANSPORT sign conventions for x, β , R and h are all positive as shown in the figure. The positive y direction is out of the paper. Positive β 's imply transverse focusing. Positive R's (convex curvatures) represent negative sextupole components of strength $S = (-h/2R) \sec^2\beta$. (See SLAC-75, page 71.)

First – Order Wedge Bending Magnet Matrix

Definitions:
$$h = 1/\rho_0$$
, $k_x^2 = (1-n)h^2$, $k_y^2 = nh^2$.
 $\alpha = hL$ = the angle of bend.
 L = path length of the central trajectory

The field expansion for the midplane of a bending magnet is taken from Eq. (18) page of 31 of SLAC-75, thereby defining the dimensionless quantities n and β as follows:

$$B_{y}(x,0,t) = B_{y}(0,0,t) \left[1 - nhx + \beta h^{2}x^{2} + \gamma h^{3}x^{3} + \ldots\right]$$

The type code signifying a BEND is 4.0. The input format for a TRANSPORT calculation is:

Label (not to exceed four spaces) 4. L. B. n. '';

If n is not included in the data entry, the program assumes it to be zero. A β entry for a second-order calculation is made via the 16.0 1.0 element. (Do not confuse this β with a pole-face rotation.)

The standard units for L and B are meters and kG. If desired, these units may be changed by 15.0 8.0 and 15.0 9.0 type code entries preceding the BEAM Card.



Illustration of the mangetic midplane (x axis) for dipole, quadrupole and sextupole elements. The magnet polarities indicate multipole elements that are positive with respect to each other.

QUADRUPOLE: Type Code 5.0

A quadrupole provides focusing in one transverse plane and defocusing in the other.

There are four parameters to be specified for a TRANSPORT calculation:

- 1 Type Code 5.0 (specifying a quadrupole).
- 2 (Effective) magnet length L (in meters).
- Field at pole tip B (in kG). A positive field implies horizontal focusing; a negative field, vertical focusing.
- 4 Half-aperture a (in cm). Radius of the circle tangent to the pole tips.

The length and field of a quadrupole may be varied in first-order fitting. The aperture may not be.

The strength of the quadrupole is computed from its field, aperture and length. The horizontal focal length is printed in parentheses as output. A positive focal length indicates horizontal focusing and a negative focal length indicates horizontal defocusing. The quantity actually printed is the reciprocal of the (θ/x) transfer matrix element $(1/R_{21})$ for the quadrupoles. Thus two identical quadrupoles of opposite polarity will have different horizontal focal lengths due to the difference between the sine and the hyperbolic sine.

The type code for a QUAD is 5.0. The input format for a typical data set is:



The standard TRANSPORT units for L, B and a are meters, kG and cm, respectively. If other units are desired they must be chosen via the appropriate 15.0 Type Code entries preceding the BEAM (Type Code 1.0) card.

$\cos k_q L$	$\frac{1}{k_q}\sin k_q L$	0	0	0	0]
$-k_q \sin k_q L$	$\cos k_q L$	0	0	0	0
0	0	$\cos h k_q L$	$\frac{1}{k_q} \sin h k_q L$	0	0
0	0	$k_q \sin h k_q L$	$\cos h k_q L$	0	0
0	0	0	0	1	0
0	0	0	0	0	1 J

These elements are for a quadrupole which focuses in the horizontal (x) plane (B positive). A vertically (y-plane) focusing quadrupole (B negative) has the first two diagonal submatrices interchanges.

<u>Definitions</u>: L = the effective length of the quadrupole. a = the radius of the aperture. B_0 = the field at the radius a. k_q^2 = $(B_0/a)(1/B_0\rho_0)$, where $(B\rho_0)$ = the magnetic rigidity (momentum) of the central trajectory.



Illustration of the magnetic midplane (x axis) for dipole, quadrupole and sextupole elements. The magnet polarities indicate multipole elements that are positive with respect to each other.

TRANSFORM 1 UPDATE*: Type Code 6.0.1.

To re-initialize the matrix TRANSFORM 1 (the product of the R matrices, R1) use Type Code 6.0. A (6. 0. 1. ;) card effects an update of the R1 matrix and initiates the accumulation of a new product matrix at the point of the update. This facility is often useful for misaligning a set of magnets or fitting only a portion of a system.

The matrix R1 is updated by no other element. It is not used in the calculation of the beam matrix. The beam matrix is claculated from the auxiliary transfer matrix R2 described on the next page.

A TRANSFORM 1 matrix will be printed at any position in the data set where a (13. 4. ;) entry is inserted.

See the following section for the introduction of an auxiliary transformation matrix R2 (TRANSFORM 2) to avoid the need for TRANSFORM 1 updates.

The (6. 0. 1. ;) card also causes an update of the R2 matrix.

^{*} By "updating" we mean initiating a new starting point for the accumulation (multiplication) of the R matrix. At the point of update the previos accumulation is discontinued. When the next element possessing a transfer matrix is encountered, the accumulated transfer matrix R1 is set equal to the individual transfer matrix R for that element. Accumulation is resumed thereafter.

AUXILIARY TRANSFORMATION MATRIX (R2): Type Code 6.0.2.

The R1 matrix represents the accumulated transfer matrix from either the beginning of the beam line or the last explicit R1 update (6. 0. 1. ;). However several elements in TRANSPORT which affect the beam matrix cannot be represented in any transfer matrix. To avoid update complications with R1 an auxiliary transfer matrix R2 exists. To avoid update complications with R1 an auxiliary transfer matrix R2 exists. The beam matrix is then calculated from the R2 matrix and the beam matrix at the last R2 update.

Both the R1 and R2 matrices are normally available for printing. However there is no redundancy in computer use, since, internally to the program, only R2 is calculated at each element. The matrix R1 is calculated from R2 only as needed.

The R2 matrix is updated explicitly via a (6. 0. 2. ;) entry. It may be printed by a (13. 24. ;) entry. Constraints on R2 are imposed similarly to those on R1. For details see the section describing Type Code 10.0.

The complete list of elements which update TRNASFORM 2 is:

- 1. A beam Type Code 1.0 entry.
- 2. The (6. 0. 1. ;) entry.
- 3. The (6. 0. 2. ;) entry.
- 4. A centroid shift Type Code 7.0 entry.
- 5. A misalignment Type Code 8.0 entry.
- 6. A stray field Type Code 21.0 entry.

Please note that automatic updates of TRANSFORM 2 occur when an align element (Type Code 8.0) is inserted specifying the misalignment of all subsequent bending magnets. These TRANSFORM 2 updates take place immediately before and immediately after any bending magnet which has either the entrance or exit fringe fields specified via a Type Code 2 entry.

SHIFT IN THE BEAM CENTROID: Type Code 7.0

Sometimes it is convenient to redefine the beam centroid * such that it does not coincide with the TRANSPORT reference trajectory. Provision has been made for this possibility via Type Code 7.0. Seven parameters are required:

1 - Type Code 7.0.

(2 to 7) - The coordinates x, θ, φ, ℓ, and δ defining the shift in the location of the beam centroid with respect to its previous position. The units for x, φ, y, φ, ℓ, δ are the same as those chosen for the BEAM (Type Code 1.0 entry), normally cm, mr, cm, mr, cm, and percent.

Any or all of the six beam centroid shift parameters may be varied in first-order fitting. The centroid position may then be constrained at any later point in the beam line by this procedure.

The transformation matrix R2 is updated by this element.

In order for this code to function properly, the initial BEAM entry (Type Code 1.0) must have a nonzero phase space volume, for example a

1. 0. 0. 0. 0. 0. 0. p(0).;

BEAM entry is not permissible when calculating a shift in the beam centroid, whereas a

1. 1. 1. 1. 1. 1. 1. p(0).;

entry (nonzero phase volume) is acceptable.

*By "beam centroid" we mean the center of the beam ellipsoid.

MAGNET ALIGNMENT TOLERANCES: Type Code 8.0

The first-order effects of the misalignment of a magnet or group of magnets are a shift in the centroid of the beam and a change in the beam focusing characteristics. Two varieties of misalignment are commonly encountered: (1) the magnet is displaced and/or rotated by a known amount; or (2) the actual position of the magnet is uncertain within a given tolerance. TRANSPORT has the capability of simulating the misalignment of either single magnets or entire sections of a beam line. Any combination of the above alternatives may be simulated through the use of the "align" element. The results may be displayed in either the printed output of the beam (sigma) matrix or tabulated in a special misalignment table (described below).

There are eight parameters to be specified:

- 1 Type Code 8.0 (specifying a misalignment).
- 2 The magnet displacement in the horizontal direction (cm).
- 3 A rotation about the horizontal axis (mr).
- 4 A displacement in the vertical direction (cm).
- 5 A rotation about the vertical axis (mr).
- 6 A displacement in the beam direction (cm).
- 7 A rotation about the beam direction (mr).
- 8 A three-digit code number (defined below) specifying the type of misalignment.

The three displacements and three rotations comprise the six degrees of freedom of a rigid body and are used as the six misalignment coordinates. The coordinate system employed is that to which the beam is referred at the point it enters the magnet. For example, a rotation of a bending magnet about the beam direction (parameter 7 above) is referred to the direction of the beam where it enters the magnet. The units employed are the standard TRANSPORT units shown above, unless redefined by Type Code 15.0 entries. If the units are changed, the units of the misalignment displacements are those determined by the 15. 1. type code entry; the units for the misalignment rotations are those determined by the 15. 2. type code entry.

The misalignment of any physical element or section of a beam line may be simulated. Misaligned sections of a beam line may be nested. A beam line rotation (Type Code 20.0) may be included in a misaligned section. Thus, for example, one can simulate the misalignment of magnets that bend vertically. The arbitrary matrix (Type Code 14.0) may not be included in a misaligned section. A misalignment must never be included in a second-order run (Type code 17.0).

A misalignment element may indicate that a single magnet or section of the beam line is to be misaligned, or it may indicate that all subsequent magnets of a given type (quadrupoles and/or bending magnets) are to be misaligned. The type of misalignment is specified in the three-digit code number, and the location of the Type Code 8.0 align element depends on the type of misalignment.

If a misalignment pertains to a single magnet or a single section of the beam line, then the misalignment element (Type Code 8.0) must directly follow that magnet or section of the beam line. If a misalignment element indicates that all subsequent magnets of a given type are to be misaligned, it must precede the first of such magnets. Further description of the available types of misalignment is given in the table below.

The results of the misalignment may be displayed in either the beam (sigma) matrix or in a misalignment table. If the results are displayed in the beam (sigma) matrix, then that matrix is altered by the effects of the misalignment. The effects of additional misalignments cause further alterations, so that at any point along the beam line, the beam (sigma) matrix will contain the combined effects of all previous misalignments.

The misalignment table can be used to show independently the effect on the beam matrix of a misalignment in each degree of freedom of each misaligned magnet. Each new misalignment to be entered in the table creates a new set of six duplicates of the beam matrix. Printed for each duplicate beam matrix are the centroid displacement and the beam half width in each of the six beam coordinates. Each of the six matrices shows the combined result of the undisturbed beam matrix and the effect of the misalignment in a single coordinate of a single magnet or section of the beam line. In a single TRANSPORT run the results of misaligning up to ten magnets or sections of the beam line may be included in the misalignment table. Further requests for entry in the misalignment table will be ignored. Examples of such a table and the input which generated it are shown below.

When the user specifies that the actual position of the magnet(s) is uncertain within a given tolerance, the printout will show a change in the beam (sigma) matrix resulting from the effects of the misalignment(s). Thus, if one wishes to determine the uncertainty in the beam centroid resulting from uncertainties in the positioning of the magnets, the initial beam dimensions should be set to zero, i.e., the beam card entry at the beginning of the system should appear as follows:

1. 0. 0. 0. 0. 0. 0. p(0).

If it is desired to know the effect of an uncertainty in position on the beam focusing characteristics, then a nonzero initial phase space must be specified. The printout will then show the envelope of all possible rays, including both the original beam and the effects of the misalignment.

If the misalignment is a known amount, it may affect the beam centroid as well as the beam dimensions. Therefore one should place on the BEAM card the actual dimensions of the beam entering the system. For a known misalignement, the program requires that the initial beam specified by Type Code 1.0 <u>must</u> be given a <u>nonzero</u> phase volume, to insure a correct printout.

An align element pertaining to a single magnet or section of the beam line updates the BEAM (sigma) matrix and the R2 matrix, but not the R1 matrix. A misalignment element which indicates misalignment of all subsequent magnets of a given type will update the BEAM (sigma) matrix and the R2 matrix before each bending magnet with fringe fields and after each misaligned magnet of any type.

The tolerances may be varied. Thus, type-vary code 8.111111 permits any of the six parameters (2 through 7 above) to be adjusted to satisfy whatever BEAM constraints may follow. For fitting, a misalignment must pertain to a single magnet or single section of the beam line, and the results must be displayed in the beam (sigma) matrix. (See the section under Type Code 10.0 for a discussion of the use of vary codes.)

The meaning of the options for each digit of the three-digit code number is given in the following table. A. The units position specifies the magnet(s) or section of the beam line to be misaligned.

Code Number	Interpretation
XX0	The single magnet (type code element) immediately preceding
	the align card is to be misaligned. A bending magnet with
	fringe fields should be misaligned using one of the options
	described below.
XX1	The last R1 matrix update (the start of the beam line or a
	6. 0. 1. ; type code entry) marks the beginning of the
	section to be misaligned. The misalignment element itself
	marks the end. The section is treated as a unit and mis-
	aligned as a whole. The misalignments of quadrupole triplets
	and other combinations involving more than two quadrupoles
	may be studied using this code digit.
XX2	The last R2 matrix update (see Type Code 6.0 for a list of
	elements which update R2) marks the beginning of the
	misaligned section. The misalignedment element marks
	the end. This options makes use of the fact that R2 matrix
	updates do not affect the R1 matrix.
·	A bending magnet with fringing fields or pole face rotations
	(Type Code 2.0) should be misaligned using this option. See
	examples 1 and 2 below for an illustration of this. An array
	of quadrupoles provides another example of the use of this
	option. By successive application of align elements, the
	elements of a quadrupole triplet could be misaligned
	relative to each other, and then the triplet as a whole
	could be misaligned. See example 3 below for an illustration
	of this.

Code Number	Interpretation
	An array of quadrupoles provides another example of the use of this option. By successive application of align elements, the elements of a quadrupole triplet could be misaligned relative to each other, and then the triplet as a whole could be misaligned. See example 3 below for an illustration of this.
XX3	All subsequent bending magnets and quadrupoles are independently misaligned by the amount specified. This option is useful in conjunction with the tabular display of the misalignment results (see below). A bending magent, with fringing fields included, is treated as a single unit and misaligned accordingly.
XX4	All subsequent bending magnets, including fringing fields, are independently misaligned by the amount specified. See XX3 above for further comments.
XX5	All subsequent quadrupoles are independently misaligned by the amount specified. See example 4 below for an illustration of this. See XX3 above for further comments.

Code Number	Interpretation
X0X	The beam matrix contains the results of the misalignment.
	The beam matrix is printed wherever a 13. 1. ; card
	is encountered. The beam matrix will then contain
	contributions from all previous misalignments.
X1X	A table is used to store the results of misalignments.
	The effect of up to ten independently misaligned magnets
	may be shown in the table in a single run. The table is
	printed via a 13. 8. ; card, and may be compared with
	the undisturbed beam matrix (printed by a 13. 1. ; card)
	at any point. An example of such a table is shown below.

B. The tens position defines the mode of display of the results of the misalignment.

C. The hundreds position distinguishes between an uncertainty in position (0XX) or a known displacement (1XX).

Any combination of digits may be used to define the exact circumstances intended. Thus, code 111. indicates the deliberate displacement of a set of magnets (referred to the point where the beam enters the set), with the results to be stored in a table. Example No. 1: A Bending Magnet with a Known Misalignment

A bending magnet (including fringe fields) misaligned by a known amount might be represented as follows:

3. L(1). ; 6. 0. 2. ; ; 2. 0. 4. 1. B. n. 2. 0. ; ; 0. 0. 0. 0. 2. 102. 8. 0. ; 3. L(2). ;

This represents a known rotation of the bending magnet about the incoming beam direction (z axis) by 2.0 mr. The result of this misalignment will be a definite shift in the beam centroid, and a mixing of the horizontal and vertical coordinates. The use of the 6. 0. 2. ; transform two update and the misalignment code number XX2 is necessary because the magnetic array (bending magnet + fringing fields) consists of three type code elements instead of one.

Example No. 2: A Bending Magnet with an Uncertain Position

A bending magnet having an uncertainty of 2 mrad in its angular positioning about the incoming beam (z axis) would be represented as follows:

3. L(1). ; 6. 0. 2. ; 2. ; 4. L. B. n. 0. 2. 0. ; ; 0. 0. 0. 0. 2.0 002. 8. 0. ; 3. L(2). ;

To observe the uncertainty in the location of the outcoming beam centroid, the input BEAM card should have zero phase space dimensions as follows:

1. 0. 0. 0. 0. 0. p(0). ;

If the beam dimensions on the input BEAM card are nonzero, the resultant beam (sigma) matrix will show the envelope of possible rays, including both the input beam and the effect of the misalignment.

Example No. 3: A Misaligned Quadrupole Triplet

One typical use of both the R1 and R2 matrices is to permit the misalignment of a triplet. For example, an uncertainty in the positions within the following triplet:

5. 1. -8. 10. ; 4. 2. 7. 10. ; 5. 1. -8. 10. ;

may be induced by appropriate 8. element as noted:

6.	0.	1.	;				
5.	1.	-8.	10.	;			
6.	0.	2.	;				
5.	2.	7.	10.	;			
5.	1.	-8.	10.	;			
8.					 	000.	;
8.					 	002.	;
8.					 	001.	;

The first 8. card in the list refers to the misalignment of the third magnet only. The second 8. card refers to the misalignment of the second and third magnets as a single unit via the R2 matrix update (the 6. 0. 2. ; entry). The last 8. card refers to the misalignment of the whole triplet as a single unit via the R1 matrix update (the 6. 0. 1. ; entry).

The comments about the BEAM card (Type Code 1.0 entry) in Example 2 above are applicable here also.

Example No. 4: Misaligned Quadrupoles in a Triplet

Individual uncertainties in the positions of the quadrupoles in the triplet in Example 3 above may be induced by a single misalignment as follows:

8. **--- 015**.; - - -_ _ _ - -- - -- - -5. 1. -8. 10. ; 5. 2. 7. 10. ; 5. 1. -8. 10. ;

The effect of each misalignment coordinate on each quadrupole will be stored separately in a table. This table is printed wherever a 13. 8. ; type code is inserted.

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"RECOMBINED MODE HIGH RESOLUTION BEAM"

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		1.00000 15.00000; misalignment	0.0 200.00000; element																																Shown is the input for a misslignment run of The misslignment element specifies that all e given an uncertain misslignment by the amount	to ten quadrupoles) are to be entered in a table. ed by the indicated print instruction is shown in	
		0.10000	0.0																upoles to	saligned															ignment Table. a beam line. 7 upoles are to b	results (for up e output produc	
		0.10000	0.86/00					Г			Т								quadr	be mi									T		1				ut for a Misal early part of sequent quadr	ectified and the e portion of the	DOM INGRE
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	0.304	0.020	0.050	0.0		0.0		2.540			2.540					0.0				0.0	•				0.0				2.540		\$C.2		tion for table				
		000001.0	00295.0	9.18192		9.18192		-4.00060			3.45510					18.66998				18.66998					18.66998				3.51760				print instruct missionment			f desired	
	7.00000 8.00000	0.02000	80.74998; 80.74998;	10.25000	~180.00000; 1.75000; 180.00000;	10.25000	-180.00000; 27.68999;	10.00000	1.00000;	3.60000;	10.0000	1.00000	4.00000	1.200000	8.53000;	20.00000	8.53000; -180.0000;	1.50000:	180.00000;	20.00000	8.53000;	-180.00000;	180.0000;	8.53000:	20.00000	8.53000; -180.00000;	1.00000;	4.00000;	10.00000	2.00000;	10.00000	1.000001	8.00000; 4.00000;		upoles and	rint instructions i	
				E		z	:	F			2		:			=				=					5				E		:		=		e e quadr	table p	
		0		1 9		" 32	;	10"		17.1	"Q2		"C21			- B3				" B4					5 8				"Q3		4 h		"C3	3	more beam lin including more	misalignment	NEL .
•	15. 15.	00000 8	3.0	4.000	20.0 3.0 20.0	4.000	3.0	5.00	13.	3.0	5.00	13.	13.		2.0	4.000	2.0	3.0	20.0	2.0	2.0	20.0	0.0	2.0	4.000	20.0	13.	13.	5.00	3.0	0.0	13.	13.		rr ^u	r	TLUTS

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REPETITION: Type Code 9.0

Many systems include a set of elements that are repeated several times. To minimize the chore of input preparation, a 'repeat' facility is provided.

There are two parameters:

- 1 Type Code 9.0
- 2 Code digit. If nonzero, it states the number of repeitions desired from the point if appears. If zero it marks the end of a repeating unit.

For example, a total bend of 12 degrees composed of four 3-degree bending magnets each separated by 0.5 metres could be represented by 9. 4. ; 4. ---; 3. .5; 9. 0. ; Those elements (in this case a bend and drift) between the 9. 4. ; and 9. 0. ; would be employed four times.

There is no indication of the 9.0 cards in the printed TRANSPORT output when calculating except for the repeated listing of the elements they control.

Vary codes may be used within a repeating unit in the usual fashion. However <u>all</u> repetitions of a given varied element will be coupled.

Repeat cards may be nested four deep. By "nesting" we mean a repeat within a repeat. An example is given below.

Example of Nesting

.



The total length of this sequence is:

 $2^*(10. + 3^*(20 + 4^* 50) + 1.5) = 1343$.

VARY CODE AND FITTING CONSTRAINTS: Type Code 10.0

Some (not all) of the physical parameters of the elements comprising a beam line may be varied in order to fit selected matrix elements. In a first-order calculation one might fit elements of the R1 or R2 transformation matrices or the beam (sigma) matrix. In second order one might constrain an element of the second-order matrix T1 or minimize the net contribution of aberrations to a given beam coordinate. Special constraints are also available.

One may not mix orders in fitting. First order vary codes and constraints must be inserted only in a first-order calculation, and similarly for second order.

The physical parameters to be varied are selected via 'Vary Codes' attached to the type codes of the elements comprising the system. The fitting constraints on matrix elements are selected via Type Code 10.0 entries placed in the system where the constraint is to be imposed.

Vary Codes

Associated with each physical element in a system is a vary code which specifies which physical parameters of the element may be varied. This code occupies the fraction portion of the type code specifying the element. It has one digit for each parameter, the digits having the same order in the code as the physical parameters have on the card. A '0' indicates the parameter may not be varied; a '1' that it may be. For instance, 3.0 is the combined type (3) and vary code (0) for a drift length which is to remain fixed; 3.1 indicates a drift length that may be varied (by the virtue of the .1). The Type Code 4.010 indicates a bending magnet with a variable magnetic field. In punching the code 3.0, the zero need not be punched. In punching the 4.010 code, the first zero must be punched but the second zero need not be.
First - Order Vary Codes

In a first-order run the following parameters marked v may be varied, those marked 0 may not be varied.

BEAM	1.vvvvvv0 – All components of the input beam
	may be varied, except the momentum.
R.M.S. ADDITION	1.vvvvv00 - All components of an r.m.s. addition
	may be varied except the momentum change Δp .
ROTAT	2.v - The pole face angle of a bending manget
	may be varied.
DRIFT	3.v – The drift length may be varied.
BEND	4.vvv – The length, the field, and/or the n-value
	may be varied.
QUAD	5.vv0 - The length may be varied; the field may be,
	the aperture may <u>not</u> be.
AXIS SHIFT	7.vvvvvv - Any of the axis shift parameters
	may be varied.
ALIGN	8.vvvvvv0 – Any of the alignment parameters
	may be varied.
INITIAL COORDINATES	16.0v – Any of the three initial position floor
	coordinates or two angle coordinates may be varied.
MATRIX	14.vvvvvv0 - Any of the first order matrix elements
	may be varied.
SOLENOID	19.vv – The length and/or field may be varied.
BEAM ROTATION	20.v – The angle of rotation may be varied.

The use of the permissive 'may' rather than the imperative 'will' in discussing variables is meaningful. The program will choose the parameters it will vary from among those that it may vary. In general it chooses to vary those parameters that have the greatest influence upon the conditions to be fit.

Second - Order Vary Codes

In a second-order run the following parameters may be varied:

DRIFT	3.v – The drift length may be varied. Variation of a drift length
	should be done with <u>caution</u> as it may affect the first-order
	properties of the beam line. But inversely coupled drift spaces
	straddling a sextupole will, for example, show only second-order
	effects.
$\epsilon(1)\ldots$	16.0v 1. – The normalized quadratic term (sextupole component)
	in the midplane expansion for the field of a bending magnet
	may be varied.
1/R1	16.0v 12 The pole face curvature of a bending magnet entrance
	may be varied.
1/R2	16.0v 13 The pole face curvature of a bending magnet exit
•	may be varied.
SEXTUPOLE	18.0v – The field strength may be varied.

The special parameter cards (Type Code 16.0) once introduced apply to all subsequent magnets in a beam line until another Type Code 16.0 specifying the same parameter is encountered. Thus if such a parameter is varied, the variation will apply <u>simultaneously</u> to all subsequent magnets to which it pertains. The variation will persist until the parameter or vary code attached to the parameter is changed by the introduction of another Type Code 16.0 card specifying the same parameter.

Coupled Vary Codes

It is possible to apply the same correction to each of several variables. This may be done by replacing the digit 1 in the vary code with one of the digits 2 through 9, or a letter A through Z. All such variables whose vary digits are the same, regardless of position will receive the same correction. For example, the three type-vary codes (5.0A, 5.01, 5.0A) might represent a symmetric triplet. The same correction will be made to the first and third quadrupoles, guaranteeing that the triplet will remain symmetric. If a vary digit is immediately preceded by a minus sign, the computed correction will be subtracted from, rather than added to, this variable. Thus parameters with the same vary digit, one of them being preceded by a minum sign, will be inversely coupled. For example the type-vary code sequence (3.B, 5.01, 3.-B) will allow the quadrupole to move without altering the total system length.

Vary digits may also be immediately preceded by a plus sign without changing their meaning. Thus 5.0A is the same as 5.0+A. For historical reasons, the vary digits (9 and 4), (8 and 3), and (7 and 2) are also inversely coupled. Inverse coupling may not be used with type codes 1.0 or 8.0.

The total number of independent variables in a first-order run is limited to 20 by reasons of the mathematical method of fitting and to 10 for a second-order run. So far as this limit is concerned, variables that are tied together count as one. Variables within repeat elements (Type Code 9.0) also count only one.

Possible Fitting Constraints

A variety of possible constraints is available. Fitting may be done in either firstor second-order, but not in both simultaneously. The order of the constraint must be appropriate to the order of the run. A list of constraints available is given below. They are explained more fully on later pages.

First - order constraints

- 1. An element of the first-order transfer matrix R1.
- 2. An element of the auxiliary first-order matrix R2.
- 3. A σ (BEAM) matrix element.
- 4. The correlations r in the beam coordinates.
- 5. The first moments of the beam.
- 6. The total system length.
- 7. An AGS machine constraint.
- 8. The reference trajectory floor coordinates.

Second – order constraints

- 1. An element of the second-order transfer matrix T1.
- 2. An element of the second-order auxiliary transfer matrix T2.
- 3. The net contributions of aberrations to a given corrdinate of the beam matrix σ .
- 4. The strength of sextupoles used in the system.

The second-order matrices are actually computed using the auxiliary matrix T2. Therefore, when activating second-order fitting, one <u>must not</u> include any element which causes an update of the R2 matrix. For a complete list of such elements see Type Code 6.0.

The present value of the constrained quantity, as well as the desired value, is printed in the output. In the case of transfer matrix elements this value may be checked by printing the transfer matrix itself. Certain other constrained quantities may be checked similarly. Exceptions are noted in the explanations following.

R1 matrix fitting cosntraints

There are five parameters to be specified when imposing a constraint upon the (i,j) element of an R1 matrix.

- 1 Type Code 10.n (specifying that a fitting constraint follows).
- 2 Code digit (-i).
- 3 Code digit (j).
- 4 Desired value of the (i,j) matrix element.
- 5 Desired accuracy of fit (standard deviation).

Note that any fitting constraint on an R1 matrix element is from the preceding update of the R1 matrix. An R1 matrix is updated only by a (6. 0. 1. ;) entry.

The symbol (n) is normally zero or blank. If n = 1, then entry 4 is taken to be a lower limit on the matrix element. If n = 2, entry 4 is taken to be an upper limit.

Desired Optional Condition	Typical Fitting Constraint				
Point to point imaging:					
Horizontal plane $R(12) = 0$	101. 2. 00001 'F1' ;				
Vertical plane $R(34) = 0$	103. 4. 00001 'F2' ;				
Parallel to point focus:					
Horizontal plane $R(11) = 0$	101. 1. 00001 'F3' ;				
Vertical plane $R(33) = 0$	103. 3. 00001 'F4' ;				
Point to parallel transformation:					
Horizontal plane $R(22) = 0$	102. 2. 00001 'F5' ;				
Vertical plane $R(44) = 0$	104. 4. 00001 'F6' ;				
Achromatic beam:					
Horizontal plane	101. 6. 00001 'F7' ;				
R(16) = R(26) = 0	102. 6. 00001 'F8' ;				
Zero dispersion beam:					
Horizontal plane $R(16) = 0$	101. 6. 00001 'F9' ;				
Simultaneous point to point and					
waist to waist imaging:					
Horizontal plane	101. 2. 00001 'F10' ;				
R(12) = R(21) = 0	102. 1. 00001 'F11' ;				
Vertical plane	103. 4. 00001 'F12' ;				
R(34) = R(43) = 0	104. 3. 00001 'F13' ;				
Simultaneous parallel to point and					
waist to waist transformation:					
Horizontal plane	101. 1. 00001 'F14' ;				
R(11) = R(22) = 0	102. 2. 00001 'F15' ;				
Vertical plane	103. 3. 00001 'F16' ;				
R(33) = R(44) = 0	104. 4. 00001 'F17' ;				

Some typical R1 matrix constraints are as follows:

R2 matrix fitting constraints

There are five parameters to be specified when imposing a constraint upon the (i,j) element of an R2 matrix.

- 1 Type Code 10.n
- 2 Code digit -(20 + i).
- 3 Code digit (j).
- 4 Desired value of the (i,j) matrix element.
- 5 Desired accuracy of fit (standard deviation).

Some typical R2 matrix constraints are as follows:

The symbol (n) is normally zero or blank. If n = 1, then entry 4 is taken to be a lower limit on the matrix element. If n = 2, entry 4 is taken to be an upper limit.

		and the second se						
Desired Optional Condition			pical	Fitt	ing	Const	traint	
Point to point imagin	g :							
Horizontal plane	R(12) = 0	10.	-21.	2.	0.	.001	'F1'	;
Vertical plane	R(34) = 0	10.	-23.	4.	0.	.001	'F2'	;
Parallel to point focus								
Horizontal plane	R(11) = 0	10.	-21.	1.	0.	.001	'F1'	;
Vertical plane	R(33) = 0	10.	-23.	3.	0.	.001	'F2'	;
Achromatic beam:								
Horizontal plane		10.	-21.	6.	0.	.001	'F3'	;
R(16) = R(26) = 0			-22.	6.	0.	.001	'F4'	;

See Type Code 6.0 for a complete list of elements which update the R2 matrix.

σ (BEAM) matrix fitting constraints

There are five parameters to be specified when imposing a constraint upon the (i,j) element of a $\sigma(\text{BEAM})$ matrix.

- 1 Type Code 10.n
- 2 Code digit (i). $(i \leq j)$
- 3 Code digit (j).
- 4 Desired value of the (i,j) matrix element.
- 5 Desired accuracy of fit (standard deviation).

The symbol (n) is normally zero or blank. If n = 1, then entry 4 is taken to be a lower limit on the matrix element. If n = 2, entry 4 is taken to be an upper limit. If i = j, then the value inserted in entry 4 is the desired beam size $[\sigma(ii)]^{1/2}$ e.g. $x(max) = [\sigma(11)]^{1/2}$ etc.

Some typical σ matrix constraints are as follows:

Desired Optional Condition			Турі	cal	Fit	ting	Cons	strain	t
Horizontal waist $\sigma(21)$	=	0	10.	2.	1.	0.	.001	'F1'	;
Vertical Waist $\sigma(43)$	_	0	10.	4.	3.	0.	.001	'F2'	;
Fit beam size to x(max)	==	1 cm	10.	1.	1.	1.	.001	'F3'	;
Fit beam size to y(max)	=	2 cm	10.	3.	3.	2 .	.001	'F4'	;
Limit max beam size to x		2 cm	10.2	1.	1.	2.	.01	'F5'	;
Limit min beam size to y	==	1 cm	10.1	3.	3.	1.	.01	' F 6'	;

In general, it will be found that achieving a satisfactory 'beam' fit with TRANS-PORT is more difficult than achieving an R matrix fit. When difficulties are encountered, it is suggested that the user 'help' the program by employing sequential (step by step) fitting procedures when setting up the data for his problem. More often than not a "failure to fit" is caused by the user requesting the program to find a physically unrealizable solution. An often encountered example is a violation of Liouville's theorem. Beam correlation matrix (r) fitting constraints

Five parameters are needed for a constraint on the (i,j) element of the beam correlation matrix.

- **1** Type Code **10**.n
- 2 Code digit (10 + i).
- 3 Code digit (j).
- 4 Desired value of the (i,j) matrix element.
- 5 Desired accuracy of fit (standard deviation).

TRANSPORT does not print the beam (σ) matrix directly. Instead it prints the beam half widths and represents the off-diagonal elements by the correlation matrix. If one wishes to fit an element of this matrix to a nonzero value it is convenient to be able to constrain the matrix element directly.

Some typical r matrix constraints are as follows:

Desired Optical Condition	Typical Fitting Constraint						
Horizontal waist $r(21) = 0$	10. 12. 1. 0001 'F1';						
yy' correlation = $r(34) = 0.2$	10. 13. 4. 0.2 .001 'F2';						

First moment constraint

In first order, known misalignments and centroid shifts cause the centre (centroid) of the phase ellipsoid to be shifted from the reference trajectory, i.e., they cause the beam to have a nonzero first moment. The first moments appear in a vertical array to the left of the vertical array giving the $\sqrt{\sigma(ii)}$. The units of the corresponding quantities are the same.

It is perhaps helpful to emphasize that the origin always lies on the reference trajectory. First moments refer to this origin. However, the ellipsoid is defined with respect to its centre, so the covariance matrix, as <u>printed</u>, defines the second moment about the mean.

First moments may be fitted. The code digits are i = 0 and j, where j is the index of the quantity being fit. Thus 10. 0. 1. .1 .01 ; constraints the horizontal (1.) displacement of the ellipsoid to be 0.1 ± 0.01 cm.

This constraint is useful in deriving the alignment tolerances of a system or in warning the system designer to offset the element in order to accommodate a centroid shift.

System length constraint

A running total of the lengths of the various elements encountered is kept by the program and may be fit. The code digits are i = 0., j = 0.

Thus the element (10. 0. 0. 150. 5. ;) would make the length of the system prior to this element equal to 150 ± 5 metres. Presumably there would be a variable drift length somewhere in the system. By redefining the cumulative length via the (16. 6. L. ;) element, partial system lengths may be accumulated and fit.

AGS machine constraint*

Provision has been made in the program for fitting the betatron phase shift angle μ , associated with the usual AGS treatment of magnet systems.

In the horizontal plane: use code digits i = -11., j = 2., and specify:

$$\Delta = \frac{1}{2\pi} \cos^{-1} [0.5 (R_{11} + R_{22})] = \frac{\mu}{2\pi} \text{ (horiz)}$$

= freq./(No. of periods)

In the vertical plane: i = -13., j = 4., and

$$\Delta = \frac{1}{2\pi} \cos^{-1} \left[0.5 \left(R_{33} + R_{44} \right) \right] = \frac{\mu}{2\pi} \text{ (vert)}$$

For example, if there are 16 identical sectors to a proposed AGS machine and the betatron frequencies per revolution are to be 3.04 and 2.14 for the horizontal and vertical planes respectively, then the last element of the sector should be followed by the constraints:

^{*} See Courant and Snyder.¹ Also note that this constraint is valid only when the unit cell structure and the corresponding beta functions are both periodic.

10.-11.2..190.001;10.-13.4..134.001;

i.e. $\frac{3.04}{16} = 0.190$ and $\frac{2.14}{16} = 0.134$.

For example: A typical data listing might be:

```
5.01 - - - ;

3. - - - ;

5.01 - - - ;

3. - - - ;

10. -11. 2. 0.190 .001 ;

10. -13. 4. 0.134 .001 ;
```

Floor coordinate fitting constraint

Five parameters are needed to specify a floor coordinate constraint:

- **1** Type Code **10.0**
- 2 Code digit 8.
- 3 Code digit (j).
- 4 Desired value of floor coordinate.
- 5 Desired accuracy of fit (standard deviation).

The code digit (j) indicates the floor coordinate to be constrained. Its possible values are 1 to 6 indicating the floor x, y, z, theta, phi, and psi, respectively. Theta is the angle which the floor projection of the reference trajectory makes with the floor z axis. Phi is the vertical pitch. Psi is a rotation about the reference trajectory. This is also the order in which coordinates are printed in the floor layout activated by the 13. 12. ; element. Initial coordinates are given on Type Codes 16. 16. ; through 16. 20. ; and Type Code 20.

The floor coordinates are actually zero-th rather than first order properties of a beam line. However, in TRANSPORT, they may be constrained in a first-order fitting run, and therefore are included here.

T1 matrix fitting constraints

Five parameters are needed for a constraint on the (i,j,k) element of the secondorder transfer matrix T1.

- 1 Type Code 10.0
- 2 Code digit (-i).
- 3 Code digit (10j + k).
- 4 Desired value of the (i,j,k) matrix element.
- 5 Desired accuracy of fit (standard deviation).

Note that upper and lower limit constraints are not available for second order fitting.

Some typical T1 matrix constraints are as follows:

Desired Optical Condition	Typical Fitting Constraint
Geometric aberration $T_{122} = 0$	101. 220 .001 'F1' ;
Chromatic aberration $T_{346} = .5$	103. 465 .001 'F2';

There must be <u>no</u> updates of the R2 matrix when constraining an element of the T1 matrix. There is no limit on the number of constraints which may be imposed.

If no drift lengths are varied the problem will be linear and the absolute size of the tolerances will be unimportant. Only their relative magnitude will be significant. Sometimes only a subset of the elements of the matrix T_{ijk} which give significant contributions to beam dimensions need be eliminated. In such cases one may wish to minimize the effect of this subset, by weighing each matrix element according to its importance. One does this by including a constraint for each such matrix element, and setting its tolerance equal to the inverse of the phase space factor which the matrix element multiplies. For a matrix element T_{ijk} acting on an uncorrelated initial phase space, the tolerance factor would be $1/(x_{0j}x_{0k})$, where x_{0j} and x_{0k} are the initial beam half widths specified by the Type Code 1.0 card.

T2 matrix fitting constraints

Five parameters are needed for a constraint on the (i,j,k) element of the second order auxiliary transfer matrix T2.

- 1 Type Code 10.0
- 2 Code digit -(20 + i).
- 3 Code digit (10j + k).
- 4 Desired value of the (i,j,k) matrix element.
- 5 Desired accuracy of fit (standard deviation).

Note that upper and lower limit constraints are not available for second-order fitting.

Some typical T2 matrix constraints are as follows:

Desired Optical Condition	Typical Fitting Constraint	
Geometric aberration $T_{122} = 0$	1021. 220 .001 'F1';	
Chromatic aberration $T_{346} = .5$	1023. 465 .001 'F2';	

By using a T2 constraint the user may fit an element of the second-order transfer matrix which pertains to any section of the beam. One causes an R2 update at the beginning of the section with a 6. 0. 2. ; element. One then places the T2 constraint at the end of the section. Any number of such constraints may be imposed. This is the only second-order constraint that may be used in conjunction with an R2 update.

If a printing of the T1 matrix is requested via a 13. 4. ; element it will be the second-order transfer matrix from the last R1 update. The comments about phase space weighting, made in connection with the T1 constraint, are equally valid for the T2 constraint, provided the phase space factors are obtained from the beam matrix at the position of the R2 update.

Second – order σ (BEAM) matrix fitting constraint

Five parameters must be specified for a constraint on the second-order contributions to a beam matrix diagonal element σ_{ii} .

- 1 Type Code 10.0
- 2 Code digit (i).
- 3 Code digit (i).
- 4 The number 0.
- 5 Desired accuracy of fit (standard deviation).

If, for example, one wished to minimize the net contributions of second-order aberrations to the horizontal divergence, one would insert the following card:

10. 2. 2. .0 .01 ;

The quantity that is minimized is the net increase due to second-order terms in the second moment of the beam about the origin. This quantity is treated as the chi-squared of the problem, so the <u>only</u> meaningful desired value for the fit is zero. The square root of this quantity is printed in the output. It is computed using the R_2 matrix. Therefore, once again, one must <u>not</u> include any element which updates the R_2 matrix. Centroid shifts must not be inserted when doing second-order fitting, even immediately following the beam card.

The second-order image of the initial beam centroid at some later point in the beam is not necessarily the beam centroid at the later point. The parameters printed by TRANSPORT are the new centroid position and the beam matrix about the new centroid. One must therefore look at both of these to observe the effects of the fitting procedure. It may even happen that an improvement in one parameter will be accompanied by a slight deterioration in the other.

The beam profile at any point is a function of the initial beam parameters. One may therefore impose weights on the effect of the various aberrations by the choice of parameters on the BEAM card. One might, for example, adjust the strength of the correction of the chromatic aberrations by the choice of the $\Delta p/p$ parameter. In particular, when using a BEAM constraint, one should not attempt to minimize or eliminate chromatic aberrations if $\Delta p/p$ is set equal to zero on the beam card (Type Code 1.0).

Correlations (the 12.0 card) may also be included in the initial beam specification.

Sextupole strength constraints

Five parameters must be specified for a constraint on sextupole strength.

- 1 Type Code 10.0
- 2 Code digit 18.
- 3 Code digit 0.
- 4 The number 0.
- 5 Desired maximum sextupole field strength.

A single sextupole constraint card applies to all sextupoles which follow. The maximum field strength is treated as a standard deviation an may be exceeded on an optimal fit.

One can employ this constraint to find the optimal locations for sextupoles. By placing inversely coupled drift lengths before and after the sextupole its longitudinal position may be varied. By constraining the field strength the sextupole can be slid to a position where the coupling coefficients to the aberrations will be largest. One will need to experiment with adjusting the maximum field strength to achieve the best configuration.

Internal constraints

A set of upper and lower bounds on the value of each type of parameter is in the memory of the program. If a correction is computed for a parameter which would take its value outside this range, it is reset to the limit of the range. The current limit are:

Type Code	Limits					
1.0	0	< input beam				
2.0	-60	< pole-face rotation < 60 (deg)				
3.0	0	< drift				
4.0	0	< magnet length				
5.0	0	< quad length				
20.0	-360	< beam rotation < 360 (deg)				

These limits apply <u>only</u> when a parameter is being varied. <u>Fixed</u> values that exceed this range may be used as desired.

These constraints were included to avoid physically meaningless solutions.

<u>Corrections and covariance matrix</u>

When the program is fitting, it makes a series of runs through the beam line. From each run it calculates the chi-squared and the corrections to be made to the varied parameters. For each iteration a single line is printed containing these quantities.

The program calculates the corrections to be made using a matrix inversion procedure. However, because some problems are difficult, it proceeds with caution. The corrections actually made are sometimes a fixed fraction of those calculated. This fraction, used as a scaling factor, is the first item appearing on the line of printed output. The second factor is the chi-squared before the calculated corrections are made. Following are the corrections to be made to the varied parameters. They are in the order in which they appear in the beam line. If several parameters are coupled, they are considered as one and their position is determined by the first to appear.

When covnergence has occured, the final value of the chi-squared and the covariance matrix are printed. The covariance matrix is symmetric, so only a triangular matrix is shown. The diagonal elements give the change in each varied parameter needed to produce a unit increase in the chi-squared. The off-diagonal elements give the correlations between the varied parameters.

The appearance of the chi-squared and covariance matrix is:



For more details on the mathematics of the fitting, the user should consult the Appendix. For an example of the output of the program he (or she) should refer to the section on output format.

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ACCELERATION: Type Code 11.0

An energy gain is reflected in both the divergence and the width of the beam. This element provides a simulation of a travelling wave linear accelerator energy gain over a field free drift length (i.e. no externally applied magnetic field).

There are five parameters:

- **1** Type Code **11.0**
- 2 Accelerator length (metres).
- 3 Energy gain (GeV).
- 4 ϕ (phase lag in degrees).
- 5 λ (wavelength in cm).

The new beam energy is printed as output.

The energy of the reference trajectory is assumed to increase linearly over the entire accelerator length. If this is not the case, an appropriate model may be constructed by combining separate 11.0 elements. An 11.0 element with a zero energy gain is identical to a drift length.

None of the parameters may be varied.

Second-order matrix elements have not been incorporated in the program for the accelerator section.

The units of parameters 2, 3 and 5 are changed by 15. 8., 15. 11., and 15. 5. type code entries respectively.



<u>Definitions</u>: L = effective length of accelerator sector.

 E_0 = particle energy at start of sector.

 ΔE = energy gain over sector length.

 ϕ = phase lag of the reference particle <u>behind</u> the crest of the accelerating wave, i.e. if ϕ is positive then for some $\ell > 0$ the particles having this value are riding the crest of the wave; the units of ϕ are degrees.

 λ = wavelength of accelerating wave; the units of λ are those of ℓ (normally cm).

This matrix element assumes that $E_0 \gg m_0 c^2$ (fully relativistic).

BEAM (ROTATED ELLIPSE): Type Code 12.0

To allow the output beam from some point in a system to become the input beam of some succeeding system, provision has been made for re-entering the correlation matrix which appears as a triangular matrix in the beam output. (See section under Type Code 1.0 for definitions.)

There are 16 parameters:

1 - Type Code **12.0**

2 to 16 - The 15 correlations [r(ij)] among the 6 beam components – in the order printed (by rows).

Several cards may be used to insert the 15 correlations, if necessary.

Since this element is solely an extension of the beam input, a 12.0 element must immediately be preceded by a 1.0 (BEAM) element entry.

The effect of this element in the printed output is shown only in the beam matrix. If the beam matrix is printed automatically, it is not printed directly after the BEAM element but only after the correlation matrix has been inserted.

OUTPUT PRINT CONTROL INSTRUCTIONS: Type Code 13.0

A number of control codes which transmit output print instructions to the program have been consolidated into a single type code.

There are two parameters:

- **1** Type Code **13.0**
- 2 Code number.

The effects of the various code numbers will be described below (not in numerical order).

Several codes are available to control various aspects of the printed output. Most type codes produce a line of output that advertises their existence. Those that do not, usually have an obvious effect upon the remainder of the output and thus make their presence clear.

Beam Matrix Print Controls 1., 2., 3.

(13. 1. ;): The current beam (σ) matrix is printed by this code.

(13. 3. ;): The beam (σ) matrix will be printed after every physical element which follows this code.

(13. 2. ;): The effect of a previous (13. 3. ;) code is cancelled and the beam (σ) matrix is printed only when a (13. 1. ;) code is encountered or when another (13. 3. ;) code is inserted. The suppression of the beam matrix is the normal default.

Transformation Matrix Print Controls 4., 5., 6., 24.

(13. 4. ;): The current transformation matrix R1 (TRANSFORM 1) is printed by this code. If the program is computing a second-order matrix, this second-order transformation matrix will be included in the print-out. This matrix is cumulative from the last R1 (TRANSFORM 1) update. The units of the elements of the printed matrix are consistent with the input units associated with the Type Code 1.0 (BEAM) entry. (13. 6. ;): The transformation matrix R1 will be printed after every physical element which follows this code. The second order matrix will be printed automatically only if the one-line form (code 13. 19. ;) of the transformation is selected. The second order matrix will, however, be printed at each location of a (13. 4. ;) element. The first-order matrix will not be repeated.

(13. 5. ;): The automatic printing of R1 will be suppressed and R1 will be printed only when subsequently requested.

(13. 24. ;): The TRANSFORM 2 matrix, R2, will be printed by this code. The format and units of R2 are identical with those of R1, which is printed by the (13. 4. ;) code. For a list of elements which update the R2 matrix, see Type Code 6.0.

The units of the tabulated matrix elements in either the first-order R or sigma matrix or second-order T matrix of a TRANSPORT print-out will correspond to the units chosen for the BEAM card. For example, the $R(12) = (x/\theta)$ matrix element will normally have the dimensions of cm/mr; and the $T(236) = (\theta/y\delta)$ matrix element will have the dimensions mr/(cm-percent $\Delta p/p$) and so forth.

Misalignment Table Print Control 8.

The misalignment summary table is printed wherever a (13. 8. ;) element is inserted. Its contents are the effects of all previously specified misalignments whose results were to be stored in a table. A full description of the table and its contents is to be found in the section on the align element (Type Code 8.0).

Coordinate Layout Control 12.

One can produce a layout of a beam line in any Cartesian coordinate system one chooses. The coordinates printed represent the x, y and z position, and the angles theta, phi and psi, respectively, of the reference trajectory at the interface between two elements. Theta is the angle which the floor projection of the reference trajectory makes with the floor z axis. Phi is the vertical pitch. Psi is a rotation about the reference trajectory. In the printed output the values given are those at the exit of the element listed above and at the entrance of the element listed immediately below. A request for a layout is specified by placing a (13. 12. ;) card before the beam card. If no additional cards are inserted the reference trajectory of the beam line will be assumed to start at the origin and proceed along the positive z-axis. The y-axis will point up and the x-axis to the left. One can also specify other starting coordinates and orientations by placing certain other cards before the beam card. For a description of such cards see Type Code 16.0 (special parameters).

The calculation of the coordinates is done from the parameters of the physical elements as given in the data. Therefore, if effective lengths are given for magnetic elements, the coordinates printed will be those at the effective field boundary. The effects of fringing fields in bending magnets are not taken into account.

General Output Format Controls 17. 18. 19.

(13. 17. ;): The subsequent printing of the physical parameters of all physical elements will be suppressed. Only the type code and the label will remain. This element is useful in conjunction with the (13. 19. ;) element which restricts the beam (σ) matrix and the transformation (R1) matrix each to a single row. The elements of these matrices then appear in uninterrupted columns in the output, similar to the TRAMP computer code used at the Rutherford Laboratory, CERN, and elsewhere.

(13. 18. ;): Only varied elements and constraints will be printed. This element, in conjunction with the various options on the indicator card, can produce a very abbreviated output. The entire output of a multistep problem can now easily be printed on a teletype or other terminal.

(13. 19. ;): The beam (σ) and transformation (R1 or R2) matrices, when printed, will occupy a single line. Only those elements are printed which will be nonzero if horizontal midplane symmetry is maintained. The second-order transformation matrix will obviously occupy several lines. This element, in conjunction with the 13. 17. ; element and either the 13. 3. ; element or the 13. 6. ; element, will produce output in which the printed matrix elements will occupy single uninterrupted columns. For visual appearances it is recommended that, if both beam (σ) and transformation matrices are desired, they be printed in separate steps of a given problem.

Punched Output Controls 29., 30., 31., 32., 33., 34., 35., 36.

If the control is equal to 29, all of the terms in the first-order matrix and the x and y terms of the second-order matrix are punched.

If the control is equal to 30, all of the terms of the first-order matrix and all second-order matrix elements are punched out.

If the control, n, is greater than 30, all of the first-order terms are punched and the second-order matrix elements which correspond to (n-30.), i.e., if n = 32, the second-order theta matrix elements are punched out. If n = 31, the second-order x matrix elements are punched, and so forth.

ARBITRARY TRANSFORMATION INPUT: Type Code 14.0

To allow for the use of empirically determined fringing fields and other specific (perhaps nonphase-space-conserving) transformations, provision has been made for reading in an arbitrary transformation matrix. The first-order 6×6 matrix is read in row by row.

There are eight parameters for each row of a first-order matrix entry:

- 1 Type Code 14.0
- 2 to 7 The six numbers comprising the row. The units must be those used to print the transfer matrix; in other words, consistent with the BEAM input/output.
 - 8 Row number (1. to 6.)

A complete matrix must be read and applied one row at a time. Rows that do not differ from the unit transformation need not be read.

For example, $(14. -.1 .9 \ 0. 0. 0. 0. 2. ;)$ introduces a transformation matrix whose second row is given but which is otherwise a unit matrix. Note that this transformation does not conserve phase space because R(22) = 0.9, i.e. the determinant of $R \neq 1$.

Any of the components of a row may be varied; however, there are several restrictions.

Type Code 14.0 elements that immediately follow one another will all be used to form a single transformation matrix. If distinct matrices are desired, another element must be inserted to separate the Type Code 14.0 cards. Several do-nothing elements are available; for example, a zero length drift (3. 0. ;) is a convenient one.

When the last of a sequence of Type Code 14.0 cards is read, the assembled transformation matrix will be printed in the output. Note that

$$\begin{pmatrix} 1 & 0 \\ a_{21} & a_{22} \end{pmatrix} \begin{pmatrix} a_{11} & a_{12} \\ 0 & 1 \end{pmatrix} \neq \begin{pmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{pmatrix}$$

Hence, a matrix formed by successive 14. (3. 0. ;), 14. – elements is not always equal to the one formed by leaving out the (3. 0. ;) element.

If components of a 14.0 card are to be varied it must be the last 14.0 card in its matrix. This will force a matrix to be split into factors if more than one row has variable components.

If it is desired to read in the second-order matrix coefficients for the i^{th} row, then the following 22 additional numbers may be read in.

9 - continuation code 0.

10 to 30 - The 21 coefficients:

T(i11) T(i12) T(i13) T(i14) T(i15) T(i16) T(i22) T(i23) T(i24) T(i25) T(i26) T(i33) T(i34) T(i35) T(i36) T(i44) T(i45) T(i46) T(i55) T(i56) T(i66) in that order, where i is the row number. It is necessary to read in the first-order matrix row which corresponds to the second-order matrix row being read in.

As in the first-order case, full rows not different from the identity matrix [i.e., R(ii) = 1, all other R(ij) = 0, and all T(ijk) = 0] need not be read in.

INPUT-OUTPUT UNITS: Type Code 15.0

TRANSPORT is designed with a standard set of units that have been used throughout this manual. However, to accommodate other units conveniently, provision has been made for redefining the units to be employed. This is accomplished by insertion of one or more of the following elements.

There are four parameters to be specified:

- 1 Type Code 15.0
- 2 Code digit.
- 3 The abbreviation of the unit (see examples below). This will be printed on the output listing. It must be enclosed in single quotes and is a maximum of three characters long (four for energy). The format for insertion is the same as for labels.

4 - The scale factor (if needed).

The scale factor is the size of the new unit relative to the standard TRANSPORT unit. For example, if the new unit is inches and the standard TRANSPORT unit cm, the scale factor is (2.54). The various units that may be changed are:

Code Digit	Quantity	Standard TRANSPORT Unit	Symbols used in SLAC-75
1.0	horizontal and vertical transverse dimensions, magnet apertures, and misalignment displacements	cm	x,y
2.0	horizontal and vertical angles and misalignment rotation angles	mr	$ heta,\phi$
3.0	vertical beam extent (only)* and bending magnet gap height	cm	У
4.0	vertical beam divergence (only)*	mr	${oldsymbol{\phi}}$
5.0	pulsed beam length and wave length in accelerator	cm	l
6.0	momentum spread	percent (PC)	δ
7.0	bend, pole face rotation, and coordinate layout angles	degrees (DEG)	
8.0	length (longitudinal) of elements, layout coordinates, and bending magnet pole face curvatures	metres (M)	t
9.0	magnetic fields	kG	В
10.0	mass	electron mass	m
11.0	momentum and energy gain in accelerator section	GeV/c GeV	р(0) ДЕ

* These codes should not be used if the coordinate rotation (20.0) type code is used anywhere in the system.

 Units are normally restored at the end of a problem step. Once changed, they remain the same for all succeeding problem steps in an input deck until a 0 indicator card is encounter, at which time they are reset to standard TRANSPORT units. The units may be reset to standard units by inserting a (15.0) Type Code entry.

The 15.0 elements are the first cards in a deck (immediately following the title card and the 0 and 1 indicator card) and should not be inserted in any other location. They produce no printed output during the calculation, their effect being visible only in the output from other elements.

<u>Example</u>: To change length to feet, width to inches, and momentum to MeV/c, add to the front of the deck the elements

15. 8. 'FT' 0.3048; 15. 1. 'IN' 2.54; 15. 11. 'MEV' 0.001;

The scale factor, 0.3048, multiplies a length expressed in the new unit, feet, to convert it to the reference unit, metres, etc.

For the conventional units listed below, it is sufficient to stop with the unit name (the conversion factor is automatically inserted by the program). If units other than those listed below are desired, then the unit name and the appropriate conversion factor must be included. If the automatic feature is used with older versions of the program, there must be no blank spaces between the quotes and the unit name.

Input-output units: Type Code 15.0

Unit					Code	Digit					
	1.	2.	3.	4.	5.	6.	7.	8.	9.	10.	11.
'CM'	1.		1.		1.			.01	• • •		
'M'	100.		100.		100.			1.			• • •
'IN'	2.54		2.54		2.54			.0254			
'FT'	30.48		30.48		30.48			.3048			
'MM'	.1		.1		.1			.001			
'R'		1000.		1000.	• • •						
'MR'		1.		1.					.		
'PC'						1.					• • •
'P/10'						.1					• • •
'N'			. _			100.					• • •
'MeV'											.001
'GeV'											1.
'KG'									1.		
'G'					• • •				.001		

(Conversion factors for dimension changes versus code digit and unit)

PC is an abbreviation for percent

P/10 means one-tenth of a percent

~ ·

N means 100 percent

SPECIAL INPUT PARAMETERS: Type Code 16.0

A number of constants are used by the program which do not appear as parameters in elements of any Type Code. A special element has been provided to allow the designer to set their values. These special parameter entries must always precede the physical element(s) to which they apply. Once introduced, they apply to all succeeding elements in the beam line unless reset to zero or to new values.

There are three parameters:

- **1** Type Code **16.0**
- 2 Code digit.
- 3 Value of the constant.

A number of such constants have been defined in this manner. All have a normal value that is initialized at the beginning of each run.

Code Digits for Special Parameters

- ϵ(1) A second-order measure of magnetic field inhomogeneity in bending magnets. If B(x) = B(0)[1 n(x/ρ_0) + β(x/ρ_0)² ···] is the field expansion in the median (y = 0) plane, then ϵ(1) is defined as ϵ(1) = β(1/ρ_0)² (where ρ₀ is measured in unit of horizontal beam width normally cm). This parameter affects second-order calculations only. Normally the value is 0. It may be varied in second-order fitting.
- (M/m) Mass of the particles comprising the beam, in units of the electron mass; normally 0. A non-zero mass introduces the dependence of pulse length on velocity, an important effect in low-energy pulsed beams.
- 4. W/2 Horizontal half-aperture of bending magnet, in the same units as horizontal beam width, normally 0 (i.e. effect of horizontal half aperture is ignored).
- 5. g/2 Vertical half-aperture of bending magnet, in the same units as vertical beam height; this parameter must be inserted if the effect of the spatial extent of the fringing fields upon transverse focusing is to be taken into account. (See Type Code 2.0 and 4.0 as a cross reference) normally 0.

- 6. L Cumulative length of system, in the same units as system length. It is set to zero initially, then increased by the length of each element, and finally printed at the end of the system. This element allows the cumulative length to be reset as desired.
- 7. K_1 An integral related to the extent of the fringing field of a bending magnet. See section under Type Code 2.0 and SLAC-75 page 74 for further explanation. If the (16. 5. g/2. ;) element has been inserted, the program inserts a default value of $K_1 = 1/2$ unless a (16. 7. K_1 . ;) element is introduced, in which case the program uses the K_1 value selected by the user. The table below shows typical values for various types of magnet designs.
- 8. K_2 A second integral related to the extent of the fringing field. Default value of $K_2 = 0$ unless specified by a (16. 8. K_2 . ;) entry.

Typical values of K_1 and K_2 are given below for four types of fringing field boundaries:

- (a) a linear drop-off of the field,
- (b) a clamped "Rogowski" fringing field,
- (c) an unclamped "Rogowski" fringing field,
- (d) a "square-edged" nonsaturating magnet.

Model	K_1	K_2^*
Linear	b/6g	3.8
Clamped Rogowski	0.4	4.4
Unclamped Rogowski	0.7	4.4
Square-edged magnet	0.45	2.8

where b is the extent of the linear fringingfield. See page 98 of Reference 8.

^{*} For most applications K_2 is unimportant. If you find it is important to your result, you should probably be making a more accurate calculation with a differential equation ray-tracing program (see Ref. 7).

- 12. 1/R₁ Where R₁ is the radius of curvature (in units of longitudinal length, noramlly metres) of the entrance face of bending magnets. (See figure on p. 106.)
- 13. $1/R_2$ Where R_2 is the radius of curvature (in units of longitudinal length, normally metres) of the exit face of bending magnets. (See figure on p. 106.)

The pole face curvatures $(1/R_1)$ and $(1/R_2)$ affect the system only in second-order, creating an effective sextupole component in the neighbourhood of the magnet. If the parameters are not specified, they are assumed to be zero, i.e. no curvature and hence no sextupole component. Either parameter (or both) may be varied in second-order fitting.



FIELD BOUNDARIES FOR BENDING MAGNETS

The TRANSPORT sign conventions for x, β , R and h are all positive as shown in the figure. The positive y direction is out of the paper. Positive β 's imply transverse focusing. Positive R's (convex curvatures) represent negative sextupole components of strength $S = (-h/2R) \sec^3\beta$. (See SLAC-75, page 71.) Tilt – to – Focal Plane (16. 15. α . ;) Element

Very often it is desired to have a listing of the second-order aberrations along the focal plane of a system rather than perpendicular to the optic axis, i.e. along the x coordinate. If the focal plane makes an angle α with respect to the x axis (measured clockwise) then provision has been made to rotate to this focal plane and print out the second-order aberrations. This is achieved by the following procedures:

Alpha is the focal-plane tilt angle (in degrees) measured from the perpendicular to the optic axis (α is normally zero).

The programming procedure for a tilt in the x(bend)-plane (rotation about y axis) is:

16. 15. α. 3. 0. (a necessary do-nothing element) 13. 4. $-\alpha$.; (rotate back to zero) 16. 15. (a necessary do-nothing element) 3. 0. ; ; (to turn off rotation element) 0. 16. 15.

The programming procedure for a tilt in the y-plane (rotation about x-axis) is:

16.	15.	α.	;	
20 .	90 .	;		
3.	0.	;		
20 .	-90 .	;		
13.	4.	;		· .
16.	15.	$-\alpha$.	;	(rotate back to zero)
20 .	90.	;		
3.	0.	;		
20 .	-90 .	;		
16.	15.	0.	;	(to turn off rotation element)

Initial Beam Line Coordinates and Direction

When requesting a beam line coordinate layout via a (13. 12. ;) element one can employ any coordinate system one desires. The position and direction of the beginning of the reference trajectory in this coordinate system are given on elements 16. 16. through 16. 20. Such cards should be placed before the beam card, but after any units changes. Their meanings are as follows:

16.	16.	x_0 , y_0 and z_0 , respectively, the coordinates of the
16.	17.	initial point of the reference trajectory in the units chosen
16.	18.	for longitudinal length.
16.	19.	θ_0 and ϕ_0 , the initial horizontal and vertical angles
16.	20 .	of the reference trajectory in degrees.

The angle ψ may be set by using Type Code 20.0.

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When specifying the initial orientation of the reference trajectory via the two angles, one must give the horizontal angle first. The meaning of the two angles is given in the following figure. Any of the above five parameters not explicitly specified will be taken to equal zero.

The initial coordinates may be varied in first-order fitting. Their values will affect only the beam line floor coordinates and not any beam or transfer matrix element.



SPECIFICATION OF INITIAL ANGLES θ_0 AND ϕ_0 FOR BEAM LINE LAYOUT.

SECOND-ORDER CALCULATION: Type Code 17.0

A second-order calculation may be obtained provided no alignments are employed. A special element instructs the program to calculate the second-order matrix elements. It must be inserted immediately following the beam (1. element).

Only one parameter should be specified:

1 - <u>Type Code 17.0</u> (signifying a second-order calculation is to be made).

To print out the second-order T1 matrix terms at a given location in the system, the (13. 4. ;) print control card is used. For T2, the (13. 24. ;) print control card is used. The update rules are the same as those for the corresponding first-order R matrix. See SLAC-75 for definitions of subscripts in the second order T(ijk) matrix elements.

The values of the BEAM (sigma) matrix components may be perturbed from their first-order value by the second-order aberrations. In a second-order TRANSPORT calculation, the initial beam is assumed to have a Gaussian distribution. For exact details the reader should consult the Appendix. For the beam matrix to be calculated correctly, there should be no elements which update the R2 matrix. If a centroid shift is present, it must immediately follow the beam (Type Code 1.0) or beam rotated ellipse (Type Code 12.0) card.

Only second-order fitting may be done in a second-order run. See the section on Type Code 10.0 for a list of quantities that may be constrained in a second-order run. If a beam constraint is to be imposed in second-order, there must be no centroid shifts present anywhere.

Second-order matrices are included in the program for quadrupoles, bending magnets (including fringing fields), the arbitrary matrix, sextupoles, and solenoids. They have not been calculated for the acceleration (Type Code 11.0) element.

SEXTUPOLE: Type Code 18.0

Sextupole (hexapole) magnets are used to modify second-order aberrations in beam transport systems. The action of a sextupole on beam particles is a second and higher order effect, so in first order runs (absence of the 17.0 card) this element will act as a drift space.

There are four parameters:

- 1 Type Code 18.0
- 2 Effective length (metres).
- 3 Field at pole tips (kG). Both positive and negative fields are possible (see figures below).
- 4 Half-aperture (cm). Radius of circle tangent to pole tips.

Other orientations of the sextupole may be obtained using the beam rotation element (Type Code 20.0).

The pole tip field may b varied in second-order fitting. It may also be constrained not to exceed a certain specified maximum field. (See the explanation of vary codes in the section on Type Code 10.0.) Such a constraint allows one to take into account the physical realities of limitations on pole tip fields.

See SLAC-75 for a tabulation of sextupole matrix elements. The TRANSPORT input format for a typical data set is:

Label is desired (not to exceed four spaces) 18. L. b. a. '';

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Illustration of the magnetic midplane (x axis) for dipole, quadrupole and sextupole elements. The magnet polarities indicate multipole elements that are positive with respect to each other.

SOLENOID: Type Code 19.0

The solenoid is most often used as a focusing element in systems passing low-energy particles. Particles in a solenoidal field travel along helical trajectories. The solenoid fringing field effects necessary to produce the focusing are included.

There are three parameters:

- **1 Type Code 19.0**
- 2 Effective length of the solenoid (meters).
- 3 The field (kG). A positive field, by convention, points in the direction of positive z for positively charged particles.

The length and the field may be varied in first-order fitting. Both first- and secondorder matrix calculations are available for the solenoid.

A typical input format is:

Label is desired (not to exceed four spaces) 19. L. B. ' ' ;

First – Order Solenoid Matrix

Solenoid R matrix

<u>Definitions</u> :	L	===	effective length of solenoid.			
	K	=	$B(0)/(2B\rho_0)$, where $B(0)$ is the field inside the			
			solenoid and $(B\rho_0)$ is the (momentum) of the			
			central trajectory.			
	С	=	cos KL			
	S	=	sin KL			

For a derivation of this transformation see report SLAC-4 by R. Helm.

Alternate forms of matrix representation of the solenoid:

$$R(\text{Solenoid}) = \begin{bmatrix} C^2 & \frac{1}{K}SC & SC & \frac{1}{K}S^2 & 0 & 0\\ -KSC & C^2 & -KS^2 & SC & 0 & 0\\ -SC & -\frac{1}{K}S^2 & C^2 & \frac{1}{K}SC & 0 & 0\\ KS^2 & -SC & -KSC & C^2 & 0 & 0\\ 0 & 0 & 0 & 0 & 1 & 0\\ 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix}$$

Rotating the transverse coordinates about the z axis by an angle = -KL decouples the x and y first-order terms, i.e.

$$R(-KL) \cdot R(\text{Solenoid}) = \begin{bmatrix} C & \frac{1}{K}S & 0 & 0 & 0 & 0 \\ -KS & C & 0 & 0 & 0 & 0 \\ 0 & 0 & C & \frac{1}{K}S & 0 & 0 \\ 0 & 0 & -KS & C & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix}$$

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COORDINATE ROTATION: Type Code 20.0

The transverse coordinates x and y may be rotated through an angle α about the z axis (the axis tangent to the central trajectory at the point in question. * Thus a rotated bending magnet, quadrupole, or sextupole may be inserted into a beam transport system by preceding and following the element with the appropriate coordinate rotation. (See examples below.) The positive sense of rotation is clockwise about the positive z axis.

There are two parameters to be specified for a coordinate rotation:

- 1 Type Code 20.0 (signifying a beam coordinate rotation).
- 2 The angle of rotation α (degrees).

The angle of rotation may be varied in a first-order fitting (see Type Code 10.0).

<u>Note</u>:

This transformation assumes that the units of (x and y) and (θ and ϕ) are the same. This is always true unless a 15.0 3.0 or a 15.0 4.0 type code has been used.

^{*} See SLAC-75,⁴ page 45 and page 12, Fig. 4, for definitions of x, y, and z coordinates.

Examples:

For a bending magnet, the beam rotation matrix may be used to specify a rotated magnet.

Example No. 1

A bend up is represented by rotating the x,y coordiantes by -90.0 degrees as follows:

-Label (not to exceed four spaces) is desired 6.7 **20**. **-90**. 2. β(1). 6 7 L. B. n. ''; 4. ، ، β(2). 2. ; (returns coordinates to their initial orientation) 20. +90. ، ، ;

A bend down is accomplished via a + 90 degree rotation.

20. +90. ''; 2. 4. 2. 20. -90. '';

A bend to the left (looking in the direction of beam travel) is accomplished by rotating the x,y coordinates by 180 degrees, e.g.

20. +180. ''; 2. 4. 2. 20. -180. '';

+

Example No. 2

A quadrupole rotated clockwise by 60 degrees about the positive z axis would be specified as follows:

20. +60. ''; 5. L. B. a. ''; 20. -60. '';

Beam rotation matrix

$$R = \begin{bmatrix} C & S & & \\ & C & S & \\ -S & C & & \\ & -S & C & \\ & & & 1 \\ & & & & 1 \end{bmatrix}$$

where

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$$C = \cos \alpha$$
,

 $S = \sin \alpha$,

 α = angle of coordinate rotation about the beam axis, blank spaces are zeros.

e.g. for $\alpha = +90$ degrees, this matrix interchanges rows 1 and 2 with 3 and 4 of the accumulated R matrix as follows:

$$\begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ -1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \end{bmatrix} \times \begin{bmatrix} R(11) & R(12) & R(13) & R(14) \\ R(21) & R(22) & R(23) & R(24) \\ R(31) & R(32) & R(33) & R(34) \\ R(41) & R(42) & R(43) & R(44) \end{bmatrix}$$
$$= \begin{bmatrix} R(31) & R(32) & R(33) & R(34) \\ R(41) & R(42) & R(43) & R(44) \\ -R(11) & -R(12) & -R(13) & -R(14) \\ -R(21) & -R(22) & -R(23) & -R(24) \end{bmatrix}$$

(The rest of the matrix is unchanged.)

STRAY MAGNETIC FIELD: Type Code 21.0

1 - Element I	No.	21.0
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2 -	Code No.	n.	n=4:	horizontal deflection
			n=2:	vertical deflection
3 -	$\langle BL \rangle$			mean value of $\int B dz$.
4 -	$\pm \langle \sigma BL \rangle$		+:	Gaussian random number generator;
				affects beam first moment.
			-:	uncertainty in $\int B dz$ – affects beam
				second moment.

Uses the misalignment element (8.) to calculate an angular deflection equal to $\int Bdz/B\rho$).

This type code is not functioning in the present version of the program.

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SENTINEL

Each step of every problem in a TRANSPORT data set must be terminated with the word SENTINEL. The word SENTINEL need not be on a separate card. For a description of the form of a TRANSPORT data set see the section on input format.

An entire run, consisting of one or several problems, is indicated by <u>an additional card</u> containing the word SENTINEL. Thus, at the end of the entire data set the word SEN-TINEL will appear twice.

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R. Helm's suggestions and criticisms at SLAC have been invaluable throughout the development of the program and the underlying theory. R. Pordes has ably assisted D. Carey at FNAL during the more recent developments of the program.

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- K. L. Brown and S. K. Howry, "TRANSPORT/360, a Computer Program for Design Charged Particle Beam Transport Systems," SLAC Report No. 91 (1970). The present manual supersedes Reference 5.
- K. L. Brown, "A Systematic Procedure for Designing High Resolving Power Beam Transport Systems or Charged Particle Spectrometers," Proc. 3rd Int. Conf. on Magnet Technology, Hamburg, Germany, May 1970, p. 348-366. (SLAC-PUB-762, June 1970).
- 7. Suggested Ray-Tracing Programs to Supplement TRANSPORT:

David C. Carey, "TURTLE (Trace Unlimited Rays Through Lumped Elements," Fermilab Report No. NAL-64 (1971). This is a computer program using TRANSPORT notation and designed to be run using the same data cards as for a previous TRANSPORT run.

K. L. Brown and Ch. Iselin, "DECAY TURTLE (Trace Unlimited Rays Through Lumped Elements)," CERN Report 74-2 (1974). This is an extension of TURTLE to include particle decay calculations.

H. Enge and S. Kowalski have developed a Ray-Tracing program using essentially the same terminology as TRANSPORT. Any experienced user of TRANSPORT should find it easy to adapt to the M.I.T. program.

8. K. G. Steffen, *High-Energy Beam Optics*, Interscience Monographs and Texts in Physics and Astronomy, Vol. 17, John Wiley and Sons, New York (1965).

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K. L. Brown et al., Nucl. Instrum. Methods 141, 393-399 (1977).

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Table 1.	Summary	of TRANSPORT	Type Codes
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PHYSICAL ELEMENT	TYPE	2nd	3rd	4th	5th EVTRY	6th -	7th EMTRY	8th	9th
	CODE	ENTRY		ENIRY	ENTRY		Ent Ki	ENIKI D	ENTRY
BEAM	1.000000	x(cm)	θ(mar)	y (cma.)	φ(mr)	* (cm)	o(percent)	ΔP	0
BEAM ENVELOPE	1.000000	ANCIE OF	οσ(mr) 	sy (cm)	cant (mi)		av (percent)	(Ge V/c)	
POLE FACE ROTATION	2.v	ROTATION (degrees)							
DRIFT	3.v	LENGTH (metres)							
BENDING MAGNET	4.vvv	LENGTH (metres)	FIELD (kG)	(n-value)					
QUADRUPOLE	5.000	LENGTH (metres)	FIELD (kG)	HALF-APERTURE (cm)					
TRANSFORM 1 UPDATE	6.0	0.0	1.0						
TRANSFORM 2 UPDATE	6.0	0.0	2.0				(
BEAM CENTROID SHIFT	7	SHIFT (x) (cm)	SHIFT (θ) (mr)	SHIFT (y) (cm)	BOTATION (A)(mr)	DISPLACEMENT (7) (cm)	BOTATION (a) (mr)	CODE	
ALIGNMENT TOLERANCE	8.000000	DISPLACEMENT (X) (CDR)	NUTATION (0)(mr)	DISPLACEMENT (y) (Cm)				NUMBER	
REPEAT CONTROL	9.0	REPEATS							
FITTING CONSTRAINTS	10.0	±I	J	DESIRED VALUE OF (I,J) MATRIX ELEMENTS	ACCURACY OF FIT				
Note: +I is used f	or fitting	a beam (o) matrix ele	mentI is used	for fitting an R1 mat	rix element.				
- (I + 20) i	s used for	11111ng an RZ matrix	E (energy soin)	é (phase leg)			1		1
ACCELERATOR	11.0	LENGTH (metres)	(GeV)	(degrees)	(WAVELENGTH) (cm)				
BEAM (Rotated Ellipse)	12.0	THE FIFTEEN CORRELAT	IONS AMONG THE SIX EI	 JEMENTS (This entry mu 	 ist be preceded by 	a type code 1.0 entry	' '.) 		
INPUT/OUTPUT OPTIONS	13.0	CONTROL CODE NUMBER							
ARBITRARY R MATRIX	14.000000	R(J,1)	R(J,2)	R(J,3)	R(J,4)	R(J,5)	R(J,6)	J	
UNITS CONTROL (Transport Dimensions)	15.0	CODE	UNIT SYMBOL	SCALE FACTOR (if required)					
QUADRATIC TERM OF BENDING FIELD	16.0v	1.0	$\varepsilon(1) = \beta(\frac{1}{\rho_0})^2$	ρ, in units of transv	/ verse length (cm)				
MASS OF PARTICLES	16.0	3.0	M/m (dimensionless)	m = mass of electron	1				
HALF-APERTURE OF BENDING MAQNET IN x-PLANE	16.0	4.0	w/2 (cm)						
HALF-APERTURE OF BENDING MAQNET IN y-PLANE (gap)	16.0	5.0	g/2 (cma)						-
LENGTH OF SYSTEM	16.0	6.0	L (metres)						
FRINGE FIELD COR- RECTION COEFFICIENT	16.0	7.0	K ₁ (dimensionless)						
FRINCE FIELD COR- RECTION COEFFICIENT	16.0	8.0	K ₂ (dimensionless)						
CURVATURE OF ENTRANCE FACE OF BENDING MAGNET	16.0v	12.0	(1/R ₁) (1/metres)						
CURVATURE OF EXIT FACE OF BENDING MAGNET	16.0v	13.0	(1/R ₂) (1/metres)						
FOCAL PLANE ROTATION	16.0	15.0	Angle of focal plan See type code 16.0	e rotation (degrees). for details.					
INITIAL BEAM LINE x-COORDINATE	16.0V	16.0	x.						
INITIAL BEAM LINE	16.0 v	17.0	у.						
INITIAL BEAM LINE 2-COORDINATE	16.0V	18.0	2.						
INITIAL BEAM LINE HORIZONTAL ANGLE	16.0V	19.0	θ.						
INITIAL BEAM LINE VERTICAL ANGLE	16.0V	20.0	••			1]		
SECOND-ORDER CALCULATIONS	17.0								
SEXTUPOLE	18.0v	LENGTH (metres)	FIELD (kG)	HALF-APERTURE (CB)					
SOLENOI D	19.vv	LENGTH (metres)	FIELD (kG)	1			1		1
BEAM ROTATION	20.v	ANGLE OF ROTATION (degrees)	1		1	1			
STRAY FIELD	21.0	See later section o	f report.	<u> </u>			<u> </u>		
Note: The v's following the type codes indicate the parameters which may be varied. See section under type code 10.0 for a detailed explanation of Vary Codes. The units are standard TRANSPORT units (as shown) unless changed via type code 15.0 entries.									

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