A Low-Energy Ring Lattice Design

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The PEP-N project at SLAC [1] consists of a Very Low-Energy small electron Ring (VLER) that will collide with the low-energy 3.1 GeV positron beam (LER) of PEP-II, producing center-of-mass energies between the 1.1 GeV and the $J/\psi$. The beams will collide head-on and will be separated in the detector magnetic field which is part of the Interaction Region [2]. The IP $\beta$ functions were chosen such as to optimize both luminosity and beam-beam tune shifts, while keeping the LER tune shifts small. This paper describes the lattice design of the VLER for the 'baseline' at 500 MeV.

1. INTRODUCTION

A proposal to build a new low energy electron storage ring that will collide with the existing 3.1 LER $e^+$ beam in the IR12 straight section of PEP-II was made in September 2000 [3]. The energy range of the electron ring will be 100 to 800 MeV resulting in a center-of-mass energy ranging from 1.1 to 3.1 GeV. The expected luminosity at 500 MeV is about $10^{31}$ cm$^{-2}$s$^{-1}$. PEP-N is to be operated simultaneously with the PEP-II collider and is designed to not interfere with the peak luminosity operation of PEP-II for BaBar data collection. The physics case [4] is mainly focused on the measurement of $R$, the ratio between multi-hadron and muon pairs cross sections, in an energy range where data are lacking or have large errors. These measurements will also allow to reduce the error on the calculated muon magnetic momentum $g_{\mu} - 2$. Due to the asymmetry of the beam energies, the detector will also profit of the particle boost to measure the Nucleon Form Factors in the time-like region, which are poorly measured and understood.

2. MACHINE LAYOUT

The VLER storage ring has been designed in order to meet the following requirements:

- to operate with an energy variable between 100 and 800 MeV;
- to provide the flexibility to keep the beam emittance constant while varying the energy;
- to collide with LER without perturbing the BaBar operation;
- to fit in the Hall 12 (20 m $\times$ 7 m), leaving enough space for the injection line from the Linac;
- to allow for head-on collisions with a minimum impact on the detector.

All these requirements are fulfilled by the present 500 MeV design. The ring circumference was chosen to be a multiple of the LER bunch spacing. However, for lack of space, we could not choose a VLER length that is a sub-multiple of the LER length. As a consequence the $e^-$ bunches will collide with many different $e^+$ bunches. Possible implications of this choice will be discussed later.

3. LATTICE DESIGN

The ring has a two-fold symmetry with a circumference of 45.36 m. This is 36 times the LER by 2 bunch spacing. The beams collide head-on and are brought into and out of collision by the detector magnetic field. The main lattice parameters are summarized in Table 1. A RF voltage of 100 kV was assumed. The emittance is the uncoupled one. Dipole fields and quadrupole gradients refer to the maximum energy of 800 MeV.

The ring layout is sketched in Figure 1. The plot size is the actual Hall 12 size (20 m $\times$ 7.16 m), the yellow circle is the detector field.

Figure 1: Ring layout.
Table I Lattice Parameters

<table>
<thead>
<tr>
<th>E (GeV)</th>
<th>0.1–0.8</th>
<th>C (m)</th>
<th>45.36</th>
</tr>
</thead>
<tbody>
<tr>
<td>I (mA)</td>
<td>10-140</td>
<td>L(cm$^{-2}$s$^{-1}$) $\times$ 10$^{31}$</td>
<td>2–200</td>
</tr>
<tr>
<td>B field (T)</td>
<td>1.63</td>
<td>Max B’ (T/m)</td>
<td>10.</td>
</tr>
<tr>
<td>freq (MHz)</td>
<td>6.6</td>
<td>h/Nb</td>
<td>72/36</td>
</tr>
<tr>
<td>$\beta_x^*$ (cm)</td>
<td>30.</td>
<td>$\beta_x^*$ (cm)</td>
<td>2.85</td>
</tr>
<tr>
<td>INT($v + x$)</td>
<td>3.</td>
<td>INT($v_y$)</td>
<td>3.</td>
</tr>
<tr>
<td>Max IR $\beta_x$ (m)</td>
<td>60.–80.</td>
<td>Max IR $\beta_y$ (m)</td>
<td>100.</td>
</tr>
<tr>
<td>$\eta_x^*$ (m)</td>
<td>0.</td>
<td>Max $\eta_x$ (m)</td>
<td>2.2–3.5</td>
</tr>
<tr>
<td>$\sigma_x^*$ (µ)</td>
<td>274.</td>
<td>$\sigma_x^*$ (µ)</td>
<td>84.</td>
</tr>
<tr>
<td>$\epsilon_o$(nm)</td>
<td>500.</td>
<td>$\kappa = \epsilon_y/\epsilon_x$</td>
<td>1</td>
</tr>
<tr>
<td>$\alpha_c$</td>
<td>.052</td>
<td>$\sigma_1$(cm)</td>
<td>1.2–0.7</td>
</tr>
<tr>
<td>$\sigma_E$/Ex10$^{-04}$</td>
<td>3.6</td>
<td>$U_o$(KeV/turn)</td>
<td>.02–.22.</td>
</tr>
<tr>
<td>$\tau_x$(ms)</td>
<td>$1000 - 5$</td>
<td>$\nu_x$</td>
<td>.011</td>
</tr>
</tbody>
</table>

The ring lattice consists of two straight sections and two arcs. In the Interaction Region (IR), asymmetric with respect to the IP since the detector field is centered at 25 cm from the IP, the beam will collide with the LER beam. The focusing at the IP and along the IR is provided by two QD-QF doublets. The first quadrupoles in the doublets will be of a permanent magnet type, to leave as much as solid angle to the detector. The IP arcs will be 250 cm long, and the vertical emittance was assumed 10% of the horizontal one. At all energies, the bunch length was fixed at 1 cm, the horizontal emittance was kept at the constant value of 250 nm, and the vertical emittance was assumed 10% of the horizontal one. The values of the charge per bunch at different energies were computed using MAD [6]. The lowest energy design lattice was used in the calculation, as it is the more problematic case for this effect. At all energies, the bunch length was fixed at 1 cm, the horizontal emittance was kept at the constant value of 250 nm, and the vertical emittance was assumed 10% of the horizontal one. The values of the charge per bunch at different energies were interpolated based on the design values. The growth rate turns out to be small compared to the damping rate due to the synchrotron radiation when the energy is larger than 200 MeV, and it increases rapidly once the energy drops below 200 MeV.

4. BEAM DYNAMICS

4.1. Dynamic Aperture

Due to the high natural chromaticity and the limited space available for the sextupoles the optimization of the dynamic aperture has to be carefully studied. Four families of sextupoles are foreseen: three for chromaticity correction in the arcs, where the betatron functions in the two planes are quite well separated and the dispersion is maximum, and one in the injection straight to correct the beam tune shift with the particle amplitude. Due to space issues the phase shift between sextupoles will probably not be optimized to exactly cancel chromatic and geometric aberrations. The dynamic aperture with a fast tracking program was computed [3] for a previous version of the 500 MeV lattice, with a lower emittance. Particles with initial conditions confined in a region of $(-10\sigma_x^*,+10\sigma_x^*)$ at nominal coupling, and for three fixed energy deviations, corresponding to $\Delta p/p = (-10\sigma_E/E, 0, +10\sigma_E/E)$, were tracked for $3 \times 10^5$ turns, corresponding to one transverse damping time. Magnet errors and synchrotron oscillations were not studied. The results looked promising since the stable area was larger than $\pm 10\sigma_x$.

4.2. Beam Lifetime

In an electron storage ring, the multiple Coulomb scattering of the charged electrons within a bunch leads to the growth of emittance in all three dimensions. The growth rates are proportional to the fourth power of the inverse of beam energy [5]. Hence, at the lower end of the energy range (100 MeV), this effect could become the dominant factor in determining the equilibrium beam size.

To estimate the effect of the intrabeam scattering, the growth rates of emittance in all three dimensions as a function of energy were computed using MAD [6]. The lowest energy design lattice was used in the calculation, as it is the more problematic case for this effect. At all energies, the bunch length was fixed at 1 cm, the horizontal emittance was kept at the constant value of 250 nm, and the vertical emittance was assumed 10% of the horizontal one. The values of the charge per bunch at different energies were interpolated based on the design values. The growth rate turns out to be small compared to the damping rate due to the synchrotron radiation when the energy is larger than 200 MeV, and it increases rapidly once the energy drops below 200 MeV.

This result indicates that below 200 MeV it might be an issue to maintain a reasonable beam size and beam lifetime since there is no equilibrium distribution if the growth rate is larger...
A Low-Energy Ring Lattice Design

Figure 2: Optical functions for the 500 MeV lattice ($\beta_x$ black, $\beta_y$ red, $\eta_x$ green).

the damping rate. However the larger vertical emittance (50% of the horizontal in the present design), and smaller damping times can help in decreasing the growth rate. The lifetime of the electron beam due to the Touschek effect was estimated as a function of the VLER energy using the simple formula by Le Duff [7] for flat beams. At all energies, the momentum acceptance is calculated with a fixed RF voltage of 100 kV. The result of calculation is shown in Figure 3 as a function of the number of particles per bunch.

Figure 3: Touschek Lifetime at different beam energies.

Each curve refers to an energy value, ranging from 100 MeV (the lowest) up to 800 MeV in 100 MeV steps. Given the design charge per bunch at each energy, the shortest beam lifetime is larger than 2 hours for 100 MeV. Of course a tracking of Touschek lost particles, taking into account the dynamic aperture and the real lattice for each energy will be performed. However even with a 30 minute short lifetime at the lowest operating energy, a gain in integrated luminosity will come from the possibility to inject in less than 5 minutes with the detector on, by keeping low the injection background rate.

4.3. Beam–Beam

The large asymmetry of the two rings, and the fact that each bunch in VLER collides with many LER bunches can lead to instabilities due to barycentre coherent motion (dipole) [8]. We believe that a strong transverse bunch-by-bunch feedback (as in PEP-II) can help. Very small (0.004) tune shifts in the LER and a careful choice of tunes will also help. We also know from PEP-II experience that the beam-beam force is a strong damper. A beam–beam simulation is needed to check this extreme weak–strong case.

5. OPEN ISSUES

The VLER design presents some special features that will require dedicated studies:
- the lattice design at low (100 MeV) and high (800 MeV) energies, with constant emittance;
- the chromaticity correction and the dynamic aperture;
- the Touschek lifetime can be a problem below 150 MeV. Possible solutions: longer bunch length, larger RF momentum acceptance, fast and efficient injection;
- the long damping times at lower energies. The segmented dipoles and a wiggler will help;
- the beam–beam case for asymmetric bunches.
6. CONCLUSIONS

The PEP-N project is in its design phase. A ‘proof-of-principle’ design of the small ring for 500 MeV has been given. The work on a high (800 MeV) and low (300 MeV) lattice is in progress and looks promising. A Workshop on the Physics Case was held at SLAC on April 30/May 1–2, 2001. A more detailed project will be presented for discussion at SLAC in September 2001.

REFERENCES