## Precision Measurement of the <br> Deuteron Spin Structure Function $g_{1}^{d *}$

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We report on a high-statistics measurement of the deuteron spin structure function $g_{1}^{d}$ at a beam energy of 29 GeV in the kinematic range $0.029<x<0.8$ and $1<Q^{2}<10(\mathrm{GeV} / \mathrm{c})^{2}$. The integral $\Gamma_{1}^{d}=\int_{0}^{1} g_{1}^{d} d x$ evaluated at fixed $Q^{2}=3(\mathrm{GeV} / \mathrm{c})^{2}$ gives $0.042 \pm 0.003$ (stat.) $\pm 0.004$ (syst.). Combining this result with our earlier measurement of $g_{1}^{p}$, we find $\Gamma_{1}^{p}-\Gamma_{1}^{n}=0.163 \pm 0.010$ (stat.) $\pm$ 0.016 (syst.), which agrees with the prediction of the Bjorken sum rule with $\mathrm{O}\left(\alpha_{s}^{3}\right)$ corrections, $\Gamma_{1}^{p}-\Gamma_{1}^{n}=0.171 \pm 0.008$. We find the quark contribution to the proton helicity to be $\Delta q=0.30 \pm 0.06$.

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[^0]The longitudinal and transverse spin-dependent structure functions $g_{1}\left(x, Q^{2}\right)$ and $g_{2}\left(x, Q^{2}\right)$ for polarized deepinelastic lepton-nucleon scattering provide information on the spin structure of the proton and neutron. A fundamental quantum chromodynamics (QCD) sum rule, originally derived from current algebra by Bjorken [1], predicts the difference $\Gamma_{1}^{p}-\Gamma_{1}^{n}=\frac{1}{6}\left(g_{A} / g_{V}\right)$ at infinite $Q^{2}$ where $\Gamma_{1}^{p(n)}=\int_{0}^{1} g_{1}^{p(n)}\left(x, Q^{2}\right) d x$ for the proton (neutron), and $g_{A}$ and $g_{V}$ are the axial-vector and vector coupling constants in neutron $\beta$-decay. QCD corrections up to third order in $\alpha_{s}$ have been computed [2], thus making a test of the Bjorken sum rule possible at finite $Q^{2}$. Measurements of $\Gamma_{1}^{p}$ [3] [4], $\Gamma_{1}^{n}$ from ${ }^{3} \mathrm{He}[5]$, as well as results from deuterium [6] targets, are in agreement with this prediction within experimental uncertainties. Separate sum rules for $\Gamma_{1}^{p}$ and $\Gamma_{1}^{n}$ were derived by Ellis and Jaffe [7] under the assumptions of $\mathrm{SU}(3)$ flavor symmetry and an unpolarized strange sea. Higher order QCD corrections have been calculated [8] [9].

The polarized spin structure function $g_{1}$ is related to the virtual photon asymmetries $A_{1}$ and $A_{2}$ :

$$
\begin{equation*}
g_{1}=\frac{F_{1}}{\left(1+\gamma^{2}\right)}\left(A_{1}+\gamma A_{2}\right) \tag{1}
\end{equation*}
$$

where $F_{1}$ is the unpolarized structure function, $\gamma^{2}=Q^{2} / \nu^{2}, \nu=E-E^{\prime}, E$ and $E^{\prime}$ are incident and scattered electron energies respectively, and $A_{1}$ and $A_{2}$ are virtual photon cross section asymmetries. [10] These asymmetries are related by kinematic factors to the experimentally measured electron asymmetries $A_{\|}$and $A_{\perp}$. The longitudinal asymmetry $A_{\|}$is the cross section asymmetry between negative- and positive-helicity electron beams when the target nucleon is polarized parallel to the beam direction. The transverse asymmetry $A_{\perp}$ is the asymmetry when the target nucleon is polarized transverse to the beam direction. We use the relationships $A_{1}=\left(A_{\|} / D-\eta A_{\perp} / d\right) /(1+\eta \zeta)$, and $A_{2}=\left(\zeta A_{\|} / D+A_{\perp} / d\right) /(1+\eta \zeta)$, where $\eta=\epsilon \sqrt{Q^{2} / E^{2}} /\left(1-\epsilon E^{\prime} / E\right), \zeta=\eta(1+\epsilon) / 2 \epsilon, D=\left(1-\epsilon E^{\prime} / E\right) /(1+\epsilon R)$ is the depolarization factor, $d=D \sqrt{2 \epsilon /(1+\epsilon)}, \epsilon^{-1}=1+2\left[1+\left(\nu^{2} / Q^{2}\right)\right] \tan ^{2}(\theta / 2), R=\sigma_{L} / \sigma_{T}$, and $\theta$ is the electron scattering angle. Thus, the quantity $g_{1}$ can be written as $g_{1}=\left(F_{1} / D^{\prime}\right)\left(A_{\|}+\tan (\theta / 2) A_{\perp}\right)$, where $D^{\prime}=$ $(1-\epsilon)(2-y) /[y(1+\epsilon R)]$ and $y=\nu / E$.

Experiment E143 used the SLAC polarized electron beam with energies of 9.7, 16.2, and 29.1 GeV incident on polarized proton and deuteron targets in End Station A to measure $g_{1}^{p}, g_{2}^{p}, g_{1}^{d}$, and $g_{2}^{d}$ in the range $1<Q^{2}<10$ $(\mathrm{GeV} / \mathrm{c})^{2}$ and $0.029<x<0.8$. This Letter reports on our analysis of the 29.1 GeV data, which yielded $g_{1}^{d}$ results with considerably smaller statistical uncertainties than previous measurements [6]. We adopt the convention that $g_{1}^{d}$ refers to the average structure function of the nucleon in the deuteron: $g_{1}^{d} \approx \frac{1}{2}\left(g_{1}^{p}+g_{1}^{n}\right)$.

The longitudinally polarized electron beam [11] was produced by a circularly polarized laser beam illuminating a strained gallium arsenide photocathode. Beam pulses of typically $2 \mu \mathrm{sec}$ duration were delivered at 120 Hz , and the helicity was selected randomly on a pulse-to-pulse basis to minimize instrumental asymmetries, which were found to be negligible. The beam polarization $P_{b}$ was measured daily with a Møller polarimeter, and was found to vary with the cathode quantum efficiency from 0.83 to 0.86 . An overall uncertainty on $P_{b}$ of $\pm 0.02$ was achieved. [4]

The target [12] was a 3 -cm-long 2.5 -cm-diameter cylinder filled with granules of deuterated ammonia, ${ }^{15} \mathrm{ND}_{3}$, of greater than $98 \%$ isotopic purity. It was polarized by the technique of dynamic nuclear polarization in a $4.8-\mathrm{T}$ magnetic field. An average in-beam polarization $P_{t}$ of $25 \%$ was measured with a nuclear magnetic resonance (NMR) technique, and a maximum of greater than $40 \%$ was achieved. The NMR signal was calibrated by measuring the thermal-equilibrium polarization near 1.6 K . An overall relative uncertainty of $4 \%$ on $P_{t}$ was achieved.

Scattered electrons were detected in two independent spectrometers [13] at angles of $4.5^{\circ}$ and $7^{\circ}$ with respect to the incident beam. Electrons were identified in each spectrometer by use of two threshold gas Čerenkov counters and a 200-element shower-counter array of lead glass blocks 24 radiation lengths thick. Particle momenta and scattering angles were measured with seven planes of scintillator hodoscopes.

The experimental longitudinal and transverse asymmetries $A_{\|}$and $A_{\perp}$ were determined from

$$
\begin{equation*}
A_{\|}\left(\text {or } A_{\perp}\right)=C_{1}\left(\frac{N_{L}-N_{R}}{N_{L}+N_{R}} \frac{1}{f P_{b} P_{t}}-C_{2}\right)+A_{r c} \tag{2}
\end{equation*}
$$

where $N_{L}$ and $N_{R}$ are the corrected numbers of scattered electrons per incident charge for negative and positive beam helicity, respectively. Charge-symmetric background processes were measured by reversing the spectrometer polarity and have no measurable asymmetry. These processes led to rate corrections of $10 \%$ at the lowest $x$ bin, decreasing rapidly at higher $x$. The rates were also corrected for deadtime effects.

The correction factors $C_{1}$ and $C_{2}$ account for the polarizations of ${ }^{15} \mathrm{~N}$, unsubstituted ${ }^{14} \mathrm{~N}$, and residual protons in the target. The factor $C_{2}$ ranges from 3 to $5 \%$ of the measured proton asymmetry, and $C_{1}$ is typically 1.016 . These factors were determined from measured nitrogen polarizations and a shell-model calculation to determine the contribution of the unpaired p-shell proton.

The dilution factor $f$ represents the fraction of measured events expected to originate from polarizable deuterons in the target. It was calculated from the composition of the target, which contained about $23 \%$ deuterons, $56 \%{ }^{15} \mathrm{~N}$,
$10 \%{ }^{4} \mathrm{He}, 6 \% \mathrm{Al}, 4 \% \mathrm{Cu}$, and $1 \% \mathrm{Ti}$ by weight. The dilution factor was $x$ dependent and varied from 0.22 at low $x$ to 0.25 at high $x$. The relative systematic error in $f$ was determined from uncertainties in the target composition and cross section ratios, and ranged from 2.2 to $2.6 \%$.

The radiative correction $\mathrm{A}_{r c}$ includes both internal [14] and external [15] contributions, and typically changed $A_{\|}$by $10 \%$ of its value. Systematic errors on $\mathrm{A}_{r c}$ were estimated based on uncertainties in the input models and correspond to relative errors on $A_{\|}$of typically $7 \%$ for $x>0.1$, increasing to $100 \%$ at $x=0.03$.

Data from the two spectrometers, which differ by about a factor of two in average $Q^{2}$, are consistent with $A_{1}^{d}, A_{2}^{d}$, and $g_{1}^{d} / F_{1}^{d}$ being independent of $Q^{2}$ in the overlap region $0.07<x<0.55$, and therefore have been averaged together. The values of $A_{1}^{d}$ from this experiment at $E=29.1 \mathrm{GeV}$ shown in Fig. 1 and listed in Table I are consistent with the higher $Q^{2}$ results from the Spin Muon Collaboration (SMC) [6].

Values of $g_{1}^{d}$ at the average $Q^{2}=3(\mathrm{GeV} / \mathrm{c})^{2}$ of this experiment are shown in Fig. 2a. The evaluation of $g_{1}^{d}$ at constant $Q^{2}$ is model-dependent. We made the assumption that $g_{1}^{d} / F_{1}^{d}$ is independent of $Q^{2}$. For $F_{1}^{d} /\left(1+\gamma^{2}\right)=$ $F_{2}^{d} /[2 x(1+R)]$ we used the New Muon Collaboration fit [16] to $F_{2}^{d}$ and the SLAC fit to $R$ [17]. Using the SLAC fit to $F_{2}^{d}$ [18] gives similar results. The systematic error on $F_{1}^{d}$ is typically $2.5 \%$, increasing to $5 \%$ at the lowest $x$ bin and $15 \%$ at the highest $x$ bin. The integral of $g_{1}^{d}$ at $Q^{2}=3(\mathrm{GeV} / \mathrm{c})^{2}$ and over the measured range $0.029<x<0.8$ is $\int_{0.029}^{0.8} g_{1}^{d}(x) d x=0.040 \pm 0.003 \pm 0.004$, where the errors are statistical and systematic respectively. The integral is decreased by 0.002 if we make the alternate assumption that both $A_{1}^{d}$ and $A_{2}^{d}$ are independent of $Q^{2}$.

Assuming $g_{1}^{d}$ varies as $(1-x)^{3}$ at high $x$ [19], the extrapolation for $x>0.8$ yields $\int_{0.8}^{1} g_{1}^{d}(x) d x=0.000 \pm 0.001$. To make the extrapolation to $x=0$, we make a model-dependent assumption that the data is described by the Regge-motivated form [20] $g_{1}^{d}(x)=C x^{-\alpha}$, where $\alpha$ is allowed to be in the range -0.5 to 0 . [21] A fit to the data of this experiment in the range $x<x_{\max }=0.1$ gives $\int_{0}^{0.029} g_{1}^{d}(x) d x=0.001 \pm 0.001$. The uncertainty includes a statistical component, the uncertainty in $\alpha$, and the effect of varying the fitting range from $x_{\max }=0.05$ to $x_{\max }=0.12$. Including the data of the SMC [6] in the fit does not change the results. An alternate form $[22], g_{1}^{d}(x)=C^{\prime} \log (x)$, which provides good fits to low $x$ data on $F_{2}$ from HERA, gives similar results. Thus, we obtain the total integral $\Gamma_{1}^{d}(E 143)=0.042 \pm 0.003$ (stat.) $\pm 0.004$ (sys.), to be compared with the results of SMC at $Q^{2}=4.7(G e V / c)^{2}$ : $\Gamma_{1}^{d}(S M C)=0.023 \pm 0.020$ (stat.) $\pm 0.015$ (sys.). The contributions to systematic uncertainties are given in Table II.

The Ellis-Jaffe sum rule for the deuteron is related to the sum rules for the proton and the neutron by: $\Gamma_{1}^{d}=$ $\frac{1}{2}\left(\Gamma_{1}^{p}+\Gamma_{1}^{n}\right)\left(1-1.5 \omega_{D}\right)$, where $\omega_{D}$ is the probability that the deuteron will be in a D-state. We use $\omega_{D}=0.05 \pm 0.01$ [23] given by $N-N$ potential calculations. No other nuclear contributions to $\omega_{D}$ are included. The sum rule predicts $\Gamma_{1}^{d}(E J)=0.069 \pm .004$ where we have used $F+D=g_{A} / g_{V}=1.2573 \pm 0.0028$ and $F / D=0.575 \pm 0.016$ [24], and $\alpha_{s}=0.35 \pm 0.05[25]$ for QCD corrections to $Q^{2}=3(\mathrm{GeV} / \mathrm{c})^{2}$. [8] Our measurement of $\Gamma_{1}^{d}$ provides a precise test of the Ellis Jaffe sum rule, and shows a disagreement of more than $3-\sigma$.

The spin structure function integral can be used in the quark parton model to extract the helicity contributions to the proton of each type of quark and antiquark. Measurements using the deuteron are expected to be more sensitive than those using either the proton or the neutron [26]. We find the total contribution from all quarks to be $\Delta q=0.30 \pm 0.06$, and the contribution from strange quarks and antiquarks to be $\Delta s=-0.09 \pm 0.02$. They are the most precise determinations to date and are consistent with earlier results [27].

The neutron spin structure function can be extracted using the relation $g_{1}^{n}(x)=2 g_{1}^{d}(x) /\left(1-1.5 \omega_{D}\right)-g_{1}^{p}(x)$. The results obtained using our earlier measurements [4] of $g_{1}^{p}(x)$ are compared in Fig. 2b with the results obtained by E142 [5] at $Q^{2}=2(G e V / c)^{2}$ using a ${ }^{3} \mathrm{He}$ target. We use the same extrapolation procedure as in the case of the deuteron and find $\Gamma_{1}^{n}(E 143)=-0.037 \pm 0.008$ (stat.) $\pm 0.011$ (sys.), compared with $\Gamma_{1}^{n}(E 142)=-0.022 \pm 0.007$ (stat.) $\pm 0.009$ (sys.). The correlations between proton and deuteron measurements were accounted for when determining the systematic uncertainty contributions in Table II.

The Bjorken sum rule prediction of $\Gamma_{1}^{p}-\Gamma_{1}^{n}=0.171 \pm 0.008$ at $3(G e V / c)^{2}$ can be tested by combining proton and deuteron results: $g_{1}^{p}(x)-g_{1}^{n}(x)=2 g_{1}^{p}(x)-2 g_{1}^{d}(x) /\left(1-1.5 \omega_{D}\right)$. The extrapolation to $x=0$ and $x=1$ follows the same procedure as in the case of the deuteron. Our result at $Q^{2}=3(G e V / c)^{2}, \Gamma_{1}^{p}(E 143)-\Gamma_{1}^{n}(E 143)=$ $0.163 \pm 0.010$ (stat.) $\pm 0.016$ (sys.), is consistent with the prediction. Contributions to systematic uncertainties are given in Table II. This result is also consistent with that obtained by combining the $\Gamma_{1}^{p}$ result from this experiment [4] and the $\Gamma_{1}^{n}$ result from E142 [5]: $\Gamma_{1}^{p}(E 143)-\Gamma_{1}^{n}(E 142)=0.149 \pm 0.014$.

In conclusion, we have performed a high-statistics measurement of the deuteron spin structure function $g_{1}^{d}$, and find the Ellis-Jaffe sum rule violated by more than $3-\sigma$. When combined with our earlier results on $g_{1}^{p}$, we find the difference $\Gamma_{1}^{p}-\Gamma_{1}^{n}$ is in agreement with the fundamental Bjorken sum rule.

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FIG. 1. The virtual photon asymmetry $A_{1}^{d}$ from this experiment. The systematic errors are indicated by the shaded band. The average $Q^{2}$ varies from $1.3(\mathrm{GeV} / \mathrm{c})^{2}$ at low $x$ to $9(\mathrm{GeV} / \mathrm{c})^{2}$ at high $x$. Data from the SMC collaboration [6] are also shown.


FIG. 2. Values of $x g_{1}$ from this experiment (E143) as a function of $x$ for (a) the deuteron and (b) the neutron. The errors are statistical only. Systematic errors are indicated by the shaded bands. Also shown are the neutron results from SLAC E142. [5]

TABLE I. Average values $A_{1}^{d}$ from the $E=29.1 \mathrm{GeV}$ data of this experiment at the indicated average values of $Q^{2}$. Also shown are values of $g_{1}^{d}$ at fixed $Q^{2}=3(\mathrm{GeV} / \mathrm{c})^{2}$, evaluated assuming $g_{1}^{d} / F_{1}^{d}$ is independent of $Q^{2}$.

|  | $<Q^{2}>$ | $A_{1}^{d}$ | $g_{1}$ at $Q^{2}=3(\mathrm{GeV})^{2}$ |
| :---: | :---: | :---: | :---: |
| $x$ | $(\mathrm{GeV} / \mathrm{c})^{2}$ | $\pm$ stat $\pm$ syst | $\pm$ stat $\pm$ syst |
|  |  |  |  |
|  |  |  |  |
|  | 1.27 | $0.007 \pm 0.037 \pm 0.007$ | $0.009 \pm 0.166 \pm 0.030$ |
| 0.031 | 1.39 | $-0.001 \pm 0.028 \pm 0.006$ | $0.026 \pm 0.111 \pm 0.029$ |
| 0.035 | 1.52 | $0.040 \pm 0.025 \pm 0.006$ | $0.144 \pm 0.089 \pm 0.024$ |
| 0.039 | 1.65 | $-0.015 \pm 0.024 \pm 0.006$ | $-0.032 \pm 0.073 \pm 0.017$ |
| 0.044 | 1.78 | $0.037 \pm 0.023 \pm 0.005$ | $-0.033 \pm 0.062 \pm 0.014$ |
| 0.049 | 1.92 | $0.009 \pm 0.022 \pm 0.004$ | $0.075 \pm 0.053 \pm 0.013$ |
| 0.056 | 2.07 | $0.023 \pm 0.022 \pm 0.004$ | $0.006 \pm 0.046 \pm 0.008$ |
| 0.063 | 2.22 | $0.054 \pm 0.022 \pm 0.004$ | $0.043 \pm 0.041 \pm 0.008$ |
| 0.071 | 2.48 | $0.053 \pm 0.022 \pm 0.004$ | $0.070 \pm 0.037 \pm 0.008$ |
| 0.079 | 2.78 | $0.106 \pm 0.023 \pm 0.005$ | $0.093 \pm 0.033 \pm 0.008$ |
| 0.090 | 3.11 | $0.156 \pm 0.025 \pm 0.009$ | $0.066 \pm 0.029 \pm 0.006$ |
| 0.101 | 3.43 | $0.133 \pm 0.019 \pm 0.010$ | $0.076 \pm 0.027 \pm 0.006$ |
| 0.113 | 3.74 | $0.129 \pm 0.023 \pm 0.010$ | $0.106 \pm 0.024 \pm 0.008$ |
| 0.128 | 4.06 | $0.143 \pm 0.030 \pm 0.012$ | $0.136 \pm 0.023 \pm 0.008$ |
| 0.144 | 4.59 | $0.294 \pm 0.041 \pm 0.021$ | $0.101 \pm 0.014 \pm 0.007$ |
| 0.172 | 5.27 | $0.288 \pm 0.061 \pm 0.022$ | $0.067 \pm 0.013 \pm 0.006$ |
| 0.218 | 5.93 | $0.316 \pm 0.108 \pm 0.028$ | $0.069 \pm 0.012 \pm 0.006$ |
| 0.276 | 6.61 | $0.311 \pm 0.255 \pm 0.029$ | $0.086 \pm 0.011 \pm 0.005$ |
| 0.350 | 7.26 |  | $0.050 \pm 0.011 \pm 0.004$ |
| 0.443 | 8.23 |  | $0.048 \pm 0.011 \pm 0.003$ |
| 0.555 | 9.11 |  | $0.005 \pm 0.012 \pm 0.002$ |
| 0.707 |  |  |  |
|  |  |  |  |

TABLE II. Contributions to the systematic uncertainties of $\Gamma_{1}^{d}, \Gamma_{1}^{n}$ and $\Gamma_{1}^{p}-\Gamma_{1}^{n}$.

| uncertainty | $\delta \Gamma_{1}^{d}$ | $\delta \Gamma_{1}^{n}$ | $\delta\left(\Gamma_{1}^{p}-\Gamma_{1}^{n}\right)$ |
| :---: | :---: | :---: | :---: |
| $P_{b}$ | 0.001 | 0.001 | 0.004 |
| $P_{t}$ | 0.002 | 0.005 | 0.007 |
| $f$ | 0.002 | 0.006 | 0.008 |
| $A_{r c}$ | 0.002 | 0.006 | 0.007 |
| $F_{2}$ and $R$ | 0.001 | 0.002 | 0.005 |
| Extrapolation | 0.001 | 0.004 | 0.006 |
|  |  |  | 0.011 |
| Total | 0.004 |  | 0.016 |


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