# Measurement of the Left-Right Forward-Backward Asymmetry for Charm Quarks with $D^{\star+}$ and $D^{+}$Mesons 

The SLD Collaboration*

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Abstract
We present a direct measurement of $A_{c}=2 v_{c} a_{c} /\left(v_{c}^{2}+a_{c}^{2}\right)$ from the left-right forward-backward asymmetry of $D^{\star+}$ and $D^{+}$mesons in $Z^{0}$ events produced with the longitudinally polarized SLC beam. These $Z^{0} \rightarrow c \bar{c}$ events are tagged on the basis of event kinematics and decay topology from a sample of hadronic $Z^{0}$ decays recorded by the SLD detector. We measure $A_{c}^{0}=0.73 \pm 0.22$ (stat) $\pm 0.10$ (syst).

[^0]The detailed vertex structure of the electroweak theory is manifest in fermion production asymmetries at the $Z^{0}$ pole. The parameter $A_{f}=2 v_{f} a_{f} /\left(v_{f}^{2}+a_{f}^{2}\right)$, the combination of vector $\left(v_{f}\right)$ and axial vector ( $a_{f}$ ) couplings of the $Z^{0}$ to fermions of type $f$, represents the magnitude of parity violation in the $Z f f$ coupling and hence the size of the asymmetry in the fermion production cross section.

The Born-level cross section [1] $d \sigma / d \cos \theta$ for producing a final-state fermion at an angle $\cos \theta$ from the electron beam direction in the process $e^{+} e^{-} \rightarrow Z^{0} \rightarrow f \bar{f}$ is proportional to $\left(1-A_{e} P_{e}\right)\left(1+\cos ^{2} \theta\right)+2 A_{f}\left(A_{e}-P_{e}\right) \cos \theta$, where $P_{e}$ is the longitudinal polarization of the electron beam. At the SLAC Linear Collider (SLC), the ability to manipulate the helicity of the electron beam allows the isolation of the $Z f f$ vertex through the formation of the double asymmetry

$$
\tilde{A}_{F B}=\frac{\sigma_{F}^{L}-\sigma_{F}^{R}-\sigma_{B}^{L}+\sigma_{B}^{R}}{\sigma_{F}^{L}+\sigma_{F}^{R}+\sigma_{B}^{L}+\sigma_{B}^{R}}=\frac{3}{4}\left|P_{e}\right| A_{f},
$$

where $F(B)$ refers to fermions produced at angles less (greater) than $90^{\circ}$ to the electron beam, and $L(R)$ denotes that the $Z^{0}$ was produced with an electron beam of left-handed (right-handed) helicity.

This Letter and a companion document [2] report the first direct measurements of the magnitude of parity violation in the $Z c c$ coupling. We measure $A_{c}$, which could be sensitive to new physics contained in various extensions of the Standard Model [3], by selecting a sample of $Z^{0} \rightarrow c \bar{c}$ decays. $A_{c}$ can also be measured in experiments where $Z^{0}$ bosons are produced with unpolarized electrons [1], but here the forward-backward asymmetry is $\propto A_{e} A_{c}$.

For this analysis, $Z^{0} \rightarrow c \bar{c}$ events are tagged using fully and partially reconstructed decays of $D^{\star+}$ and $D^{+}$ mesons [4]. The charge of the primary charm quark is uniquely determined by the sign of the $D^{(*)+}$. As $Z^{0} \rightarrow b \bar{b}$ events are also a copious source of $D^{(\star)+}$ mesons, event kinematics and decay topology are used to reject $D^{(*)+}$ 's originating in $B$ hadron decays.

The measurement reported here is performed with 1.8 $\mathrm{pb}^{-1}$ of SLC luminosity taken in 1993 at a mean c.m. energy of $91.26 \pm 0.02 \mathrm{GeV}$. The data were taken with the SLAC Large Detector (SLD), a multi-purpose particle detector [5]. The trigger, and the event and track selection criteria, are as described in Ref. [6], except that the event thrust axis is determined using only charged tracks, reconstructed in the Vertex Detector (VXD) [7] and the Central Drift Chamber [8], and the polar angle of the thrust axis is allowed to be $\left|\cos \theta_{T}\right|<0.80$. Tracks are required to have at least one VXD hit to be used in the following analyses.

The SLC was operated with a polarized electron beam and an unpolarized positron beam [9]. The average polarization magnitude measured [10] for the 1993 data sample is $\left|P_{e}\right|=(63.0 \pm 1.1) \%$. The centroid position
in the $x y$ plane of the $2.6 \mu \mathrm{~m} \times 0.8 \mu \mathrm{~m}$ SLC Interaction Point (IP) is reconstructed with a measured precision of $\sigma_{I P}=(7 \pm 2) \mu \mathrm{m}$ using the tracks in sets of $\sim 30$ sequential hadronic $Z^{0}$ decays [11]. The median $z$ position of tracks at their point of closest approach to the IP in the $x y$ plane determines the $z$ position of the $Z^{0}$ primary vertex (PV) with a precision of $\sim 35 \mu \mathrm{~m}$ event by event.

The $D^{\star+}$ mesons are identified using the decay $D^{\star+} \rightarrow$ $\pi_{s}^{+} D^{0}$, where the $D^{0}$ decays via $D^{0} \rightarrow K^{-} \pi^{+}$or $D^{0} \rightarrow$ $K^{-} \pi^{+} \pi^{0}$ (satellite resonance) [12]. The $\pi_{s}^{+}$in the $D^{\star+}$ decay is known as the spectator pion and carries the sign of the charm quark. Two separate techniques, a kinematic analysis and a decay length analysis, are combined to select the $D^{\star+}$ sample. Since it is not necessary to reconstruct the $\pi^{0}$ in the satellite resonance [12], the analyses for the two decay modes $D^{0} \rightarrow K^{-} \pi^{+}$ and $D^{0} \rightarrow K^{-} \pi^{+} \pi^{0}$ are identical except for the mass ranges allowed for the $D^{0}$ candidates, which are 1.765 $<\mathrm{m}\left(K^{-} \pi^{+}\right)<1.965 \mathrm{GeV} / c^{2}$ and $1.500<\mathrm{m}\left(K^{-} \pi^{+}\right)<$ $1.700 \mathrm{GeV} / c^{2}$, respectively.

All pairs of oppositely charged tracks in a thrust axis hemisphere are combined to form $D^{0}$ candidates by assigning the $K^{-}$mass to one of the particles and the $\pi^{+}$ mass to the other. If the $D^{0}$ candidate mass lies within the ranges specified above, it is then combined with a $\pi_{s}^{+}$ candidate track having charge opposite to the $K^{-}$candidate. In the kinematic analysis, we rely on the fact that $D^{\star+}$ mesons in $c \bar{c}$ events are produced at much higher $x_{D^{\star}}=2 E_{D^{\star}} / E_{c . m}$, where $E_{D^{\star}}$ is the $D^{\star+}$ energy, than $D^{\star+}$ 's in $b \bar{b}$ events or other random combinatoric background (RCBG). Any $D^{\star+}$ candidate with $x_{D^{\star}}<0.4$ is rejected. The background is further reduced by requiring $\left|\cos \theta^{*}\right|<0.9$, where $\theta^{*}$ is the opening angle between the direction of the $D^{0}$ in the lab frame and the $K$ in the $D^{0}$ rest frame, and by requiring the $\pi_{s}^{+}$candidate have $p>$ $1 \mathrm{GeV} / c$.

In the complementary decay length analysis, we rely on the fact that $D^{0}$ 's in $c \bar{c}$ events have a long 3 -D decay length $(\langle L\rangle \sim 1 \mathrm{~mm})$ and are produced at the $Z^{0} \mathrm{PV}$. Since the decay length resolution is $\left\langle\sigma_{L}\right\rangle \sim 200 \mu \mathrm{~m}$, a clean separation of these events from RCBG is possible, even at low $x_{D}$. A vertex fit is performed on the tracks in a $D^{0}$ candidate, and the combination is retained only if the $\chi^{2}$ probability of both tracks coming from the same vertex is greater than $1 \%$. Next, a decay length significance cut of $L / \sigma_{L}>2.5$ is applied to remove RCBG vertices. A cut requiring the $x y$ impact parameter of the $D^{0}$ momentum vector to the IP be less than $20 \mu \mathrm{~m}$ (approx. our resolution in this quantity) is also applied. This cut rejects $D$ decays occurring in $b \bar{b}$ events since these $D$ 's have significant $\left\langle p_{\perp}\right\rangle$ relative to the parent $B$ flight direction and, with the long average $B$ lifetime, do not appear to originate from the PV. Finally, we require $x_{D^{\star}}>0.2$ and make no cuts on $\cos \theta^{*}$ or minimum $\pi_{s}^{+}$momentum, since the charm purity of the remaining sample is sufficiently high.

Once either of the two selection criteria has been satisfied, the mass difference $(\Delta m)$ between the $D^{\star+}$ and $D^{0}$ is formed, and the data is divided into signal ( $\Delta m<0.150$ $\mathrm{GeV} / c^{2}$ ) and sideband ( $0.160<\Delta m<0.200 \mathrm{GeV} / c^{2}$ ) regions. The union of the two samples of $D^{\star+}$ candidates is used to perform the asymmetry measurement. The overlap of the sets of candidates from the kinematic and decay length analyses is $28 \%$.

After all analysis cuts, the composition of the remaining events is estimated using a Monte Carlo (MC) simulation [11] to obtain the signal and RCBG $\Delta m$ shapes. All MC events with three tracks from a correctly-signed, three-prong charm decay are taken as the asymmetrycarrying signal; the RCBG shape is taken from all other entries. The relative normalizations of signal and RCBG shapes are adjusted so that the predicted numbers of events match those observed in the data signal and sideband regions. Figure 1 shows the signal and background shapes superimposed on the data. The unnormalized MC, though not used to predict the fraction of RCBG, predicts the populations of the signal and sideband regions to $\sim 20 \%$, reasonable agreement given data statistics and uncertainties in $D^{(*)+}$ and background production and decay rates.

Candidates for $D^{+} \rightarrow K^{-} \pi^{+} \pi^{+}$are formed by combining two same-sign pion candidates with an opposite-sign kaon candidate. A series of cuts is applied to reject background. We require $x_{D+}>0.4, \cos \theta^{*}>-0.8$, and the three tracks are each required to have $p>1 \mathrm{GeV} / c$. To reject $D^{\star+}$ decays, the differences between $m\left(K^{-} \pi^{+} \pi^{+}\right)$ and $m\left(K^{-} \pi^{+}\right)$are formed for each of the pions, and both are required to be greater than $0.160 \mathrm{GeV} / c^{2}$. To remove RCBG, we require a good vertex fit ( $>1 \%$ probability) and $L / \sigma_{L}>3.0$ for the $D^{+}$decay length. Finally, the colinearity between the $D^{+}$momentum and the vertex flight direction is required to be less than 5 mrad in $x y$ and less than 20 mrad in $r z$, to reject $D^{+}$'s from $b \bar{b}$ events.

After all selection criteria, $D^{+} \rightarrow K^{-} \pi^{+} \pi^{+}$candidates fall in the range $1.800<m\left(K^{-} \pi^{+} \pi^{+}\right)<1.940 \mathrm{GeV} / c^{2}$, while sidebands are defined as $1.640<m<1.740 \mathrm{GeV} / c^{2}$ and $2.000<m<2.100 \mathrm{GeV} / c^{2}$. The estimate of the background in the signal region is made from the MC in the same manner as in the $D^{\star+}$ analysis. Figure 2 shows the signal and background superimposed on the data.

After cuts, the number of candidates in each sample is 88 for $D^{\star+} \rightarrow \pi_{s}^{+}\left(K^{-} \pi^{+}\right), 131$ for $D^{\star+} \rightarrow \pi_{s}^{+}\left(K^{-} \pi^{+} \pi^{0}\right)$, and 98 for $D^{+} \rightarrow K^{-} \pi^{+} \pi^{+}$. Monte Carlo estimates for the fractions of $c \rightarrow D^{(\star)+}, b \rightarrow D^{(\star)+}$, and RCBG in each sample are $\left(f_{c}, f_{b}, f_{R C B G}\right)=(0.52,0.22,0.26),(0.50$, $0.22,0.28)$, and ( $0.70,0.14,0.16$ ), respectively.

Figure 3 shows the $-q \cdot \operatorname{sign}\left(P_{e}\right) \cdot \cos \theta_{D}$ distribution, where $\theta_{D}$ is the polar angle of the $D^{(\star)+}$ meson momentum and $q$ is its charge; the data shows a large asymmetry. To extract $A_{c}$, we use an unbinned maximum likelihood fit based on the Born-level cross section for fermion production in $Z^{0}$-boson decay similar to that
used in Ref. [13]. The likelihood function has the form

$$
\begin{aligned}
\ln \mathcal{L}=\sum_{i=1}^{n} \ln \left\{P_{c}^{j}\left(x_{D}^{i}\right)\right. & {\left[\left(1-P_{e} A_{e}\right)\left(1+y_{i}^{2}\right)\right.} \\
& \left.+2\left(A_{e}-P_{e}\right) y_{i} A_{c}^{D}\left(1-\Delta^{c}\right)\right] \\
& +P_{b}^{j}\left(x_{D}^{i}\right)\left[\left(1-P_{e} A_{e}\right)\left(1+y_{i}^{2}\right)\right. \\
& \left.+2\left(A_{e}-P_{e}\right) y_{i} A_{b}^{D}\left(1-\Delta^{b}\right)\right] \\
& \left.+P_{R C B G}^{j}\left(x_{D}^{i}\right)\left[\left(1+y_{i}^{2}\right)+2 A_{R C B G} y_{i}\right]\right\},
\end{aligned}
$$

where $y=q \cdot \cos \theta_{D}, n$ is the total number of candidates, and $A_{c}^{D}$ and $A_{b}^{D}$ are the asymmetries from $D^{(*)+}$ decays in tagged $c \bar{c}$ and $b \bar{b}$ events, respectively. Since the measured asymmetry in the sideband regions is expected to be small and is consistent with zero, we take $A_{R C B G}=0$ for the central value. The functions $\Delta^{f}(y)$ are the $\mathcal{O}\left(\alpha_{s}\right)$ QCD radiative corrections to the asymmetry, including quark mass effects [14]. The terms $P_{c}^{j}, P_{b}^{j}$, and $P_{F C B G}^{j}$ are the probabilities that a candidate from the $j$ th decay mode is either signal from a $c \bar{c}$ or $b \bar{b}$ events, or RCBG, calculated from the relative fractions and $x_{D}$ distributions. The $x_{D}$ distributions used for $c \bar{c}$ and $b \bar{b}$ (RCBG) are taken from the MC (sidebands); the shapes are parametrized as in Ref. [15].

In this analysis, we take $A_{b}^{D}$ to be fixed and fit only for $A_{c}^{D}=A_{c}$. We estimate $A_{b}^{D}$ in a similar manner to Refs. $[13,16]$. We start with the standard model prediction [17], $A_{b}=0.935$, and assign it an error of $\pm 0.105$ to cover the range of measurements from LEP and SLD [18]. To arrive at the mixing-corrected value $A_{b}^{D}$, the fraction of $D^{(*)+}$ coming from the spectator part of $B_{d}$ decays is taken halfway between its two extrema: all $D^{(*)+}$ 's in $B$ decays come only from $B_{d}$ decays, or $D^{(\star)+}$ 's come equally from all types of $B$ decays $\left(B_{u}, B_{d}, B_{s}, \Lambda_{b}\right)$. For these two assumptions, the mixing parameters [19] $\chi_{d}=0.16 \pm 0.02$ or $\bar{\chi}=0.12 \pm 0.01$, respectively, are then applied to arrive at an average mixing dilution factor $1-2 \chi_{m i x}=0.72 \pm 0.09$. The correction for wrongsign $D^{(*)+}$ from the $W^{-}$in $b \rightarrow c W^{-}$is the same as in Ref. [13]. These combine to $A_{b}^{D}=0.64 \pm 0.11$, where the error is taken as an experimental systematic error. We have taken $A_{e}^{0}$ to be $0.162 \pm 0.012$ [20]. Performing the maximum likelihood fit to the data sample, we obtain $A_{c}=0.71 \pm 0.20$ (stat). As a check, a simple binned fit of the type described in Ref. [2] yields $A_{c}=0.74 \pm 0.24$.

Possible systematic errors have been estimated and are summarized in Table 1. The largest uncertainties result from our lack of knowledge of the RCBG due to limited statistics. After subtracting the residual signal in the sideband region, we obtain a net sideband asymmetry of $+0.05 \pm 0.10$. We therefore take 0.15 as an upper limit on $A_{R C B G}$. The uncertainty in $f_{R C B G}$ is a combination of the statistical error on the relative fractions of signal and background from data and MC and an average of the variation in $f_{R C B G}$ allowed by: matching the signal and background shapes in the intermediate region
between the signal and sideband regions; using wrongsign combinations for the background shape; and adjusting the sideband signal content to produce the observed sideband asymmetry. Our sensitivity to the RCBG $x_{D}$ distribution was checked by performing the analysis with $P_{R C B G}$ derived from the MC background instead of the data sidebands. The error due to nonuniform $\cos \theta_{D}$ acceptance between signal and RCBG is estimated using the one standard deviation limit allowed by data signal and sideband entries. We varied $f_{b} /\left(f_{b}+f_{c}\right)$, the fraction of signal events from $Z^{0} \rightarrow b \bar{b}$, by $\pm 30 \%$ to account for differences between our MC and the range of measurements of $D^{(*)+}$ production in $Z^{0}$ decay $[13,16,21]$. Modifying $\left\langle x_{f}\right\rangle$ in heavy quark fragmentation [18] and the exact shape of the fragmentation functions gave estimates of our sensitivity to these effects. An uncertainty of $\pm 0.02$ in the value [20] of $\alpha_{s}\left(M_{Z}^{2}\right)$ used to calculate the $\mathcal{O}\left(\alpha_{s}\right)$ correction is also included.

To obtain $A_{c}^{0}$, the charm asymmetry parameter at the $Z^{0}$ pole, we applied: electroweak corrections $[17,22]$ for initial and final state radiation, vertex corrections, $\gamma$ exchange, and $\gamma-Z^{0}$ interference totaling $0.8 \%$; and final state, $\mathcal{O}\left(\alpha_{s}^{2}\right)$ QCD corrections for massive quarks [23] totalling $2.3 \pm 1.0 \%$. The final result is

$$
A_{c}^{0}=0.73 \pm 0.22(\text { stat }) \pm 0.10(\text { syst })
$$

When combined with our other measurement [2] using a lepton tag, this yields $A_{c}^{0}=0.59 \pm 0.19$. This is in good agreement with the LEP average [18] of $A_{c}^{0}=0.698 \pm$ 0.087 , and the Standard Model prediction [22] of $A_{c}^{0}=$ 0.67 for $\sin ^{2} \theta_{W}^{e f . f}=0.23$.
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TABLE I. Contributions to the estimated systematic error.

| Source | Error |
| :---: | :---: |
| $A_{R C B G}$ | 0.044 |
| $f_{R C B G}$ | 0.038 |
| $R C B G x$ distribution | 0.039 |
| $R C B G \cos \theta$ acceptance | 0.045 |
| $A_{b}^{D}$ | 0.020 |
| $f_{b} /\left(f_{b}+f_{c}\right)$ | 0.005 |
| $c$ and $b$ fragmentation | 0.035 |
| $A_{e}$ | 0.003 |
| $P_{e}$ | 0.013 |
| QCD correction | 0.009 |
| Total | $\mathbf{0 . 0 9 5}$ |

## FIGURE CAPTIONS

Figure 1. The $\Delta m$ distributions from the kinematic and decay length analyses for (a) $D^{\star+} \rightarrow D^{0} \pi_{s}^{+}, D^{0} \rightarrow$ $K^{-} \pi^{+}$and (b) $D^{\star+} \rightarrow D^{0} \pi_{s}^{+}, D^{0} \rightarrow K^{-} \pi^{+} \pi^{0}$. The points represent the data and the solid (hatched) histogram is the estimated signal (background).
Figure 2. The mass distribution for $D^{+} \rightarrow K^{-} \pi^{+} \pi^{+}$. The signal and background are shown as in Fig. 1.
Figure 3. The distribution of $-q \cdot \operatorname{sign}\left(P_{e}\right) \cdot \cos \left(\theta_{D}\right)$ for the 317 signal events. The background shown is the scaled signal-subtracted sideband asymmetry.



Fig. 2

Fig. 1


Fig. 3


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