# POLARIZED HADRONIC COLLISIONS: QCD AND TEST OF ELECTROWEAK GAUGE MODELS* 

Masud Chaichian<br>Department of High Energy Physics, University of Helsinki, Helsinki, Finland

Masaki Hayashi ${ }^{\dagger}$<br>Stanford Linear Accelerator Center<br>Stanford University, Stanford, California, 94805

## JACQUES SOFFER

Centre de Physique Théorique, CNRS, Luminy, F-13288 Marseille, France

- KENJI Yamagishi ${ }^{*}$

Stanford Linear Accelerator Center
Stanford University, Stanford, California, 94305

Submitted to Physical Review D

[^0]
#### Abstract

Lowest order QCD is applied for the angular distributions of high-mass dileptons with large transverse momentum produced in reactions, $\bar{p} p, p p \rightarrow$ $\left(\gamma^{*}, Z_{1}^{0}, Z_{2}^{0}, \ldots\right)+X \rightarrow \ell^{+} \ell^{-}+X$ with longitudinally polarized proton beam(s). General formulas, which are applicable to any gauge model of the underlying electroweak interactions, are given. Numerical results are presented for the angular distributions in $\bar{p} p$ and $p p$ collisions at $\sqrt{s}=540 \mathrm{GeV}$ for the CERN $\bar{p} p$ collider and $\sqrt{s}=2 \mathrm{TeV}$ for the Fermilab Tevatron within the standard model and the left-right model, which is also consistent with existing data. Signals which could distinguish between the different electroweak gauge models are revealed.


## 1. Introduction

The standard $S U(2) \times U(1)$ electroweak model of Glashow, Weinberg and Salam ${ }^{1}$ has been quite successful in all respects including the predictions for the gauge bosons, $W^{ \pm}$and $Z^{0}$, which have been experimentally found at the CERN $\bar{p} p$ collider. ${ }^{2}$ However, there exist other electroweak models which differ from the standard one, but in low energy region coincide with it. ${ }^{3}$ Such models, besides other considerations, emerge also from some grand unified theories and thus have their own raison $d^{\prime} \hat{e} t r e .^{4}$ Therefore, it is of considerable interest to study such models on the same footing as the standard one and look for their experimental verifications. One such method is the detailed study of the angular distributions of the dileptons produced in the hadron-hadron collisions. To carry out the most detailed study we start with the polarized proton beams, especially since such experiments are feasible and are under consideration. The case of unpolarized hadronic reactions, of course, come out as a special case.

Many authors ${ }^{5-9}$ have studied the polarization effects for the gauge bosons $W^{ \pm}$and $Z^{0}$ production and their decay into lepton pairs in polarized hadronic collisions. The polarization effects in the hadronic decays of $W^{ \pm}$have been studied in Ref[ $\left.{ }^{10}\right]$. On the basis of such studies it has been emphasized that the experiments with a polarized proton beam would provide a variety of useful information, supplementing those of unpolarized collisions ${ }^{11-14}$ on the underlying electroweak interactions and the production mechanism of their gauge bosons. Further, a recent study has indicated that polarized proton beams at intensities close to the ordinary intensity of unpolarized beams are attainable with the new technology. ${ }^{15}$

In this paper we calculate and discuss the angular distributions of high-mass dileptons produced with large transverse momentum in high energy polarized and unpolarized hadronic collisions. Because of restriction to such a kinematical region, we have all the right to utilize the lowest order ,i.e., $O\left(\alpha_{s}\right)$ perturbative QCD which has been proven to describe quite successfully similar processes. ${ }^{16}$ We consider the reactions

$$
\begin{equation*}
\bar{p} p, p p \rightarrow\left(\gamma^{*}, Z_{1}^{0}, Z_{2}^{0}, \ldots\right)+X \rightarrow \ell^{+} \ell^{-}(\ell=e \quad \text { or } \quad \mu)+X \tag{1.1}
\end{equation*}
$$

where the proton beam $p$ is (or both $p p$ are) longitudinally polarized. The present work is the extension of our previous one ${ }^{14}$ in which the case of unpolarized beams has been studied within the standard electroweak model. Here we consider polarized beams and aim at other tests which can distinguish between the standard Glashow-Weinberg-Salam and the left-right electroweak models. A short account of this work has previously been reported. ${ }^{17}$ Kinnunen and Lindfors ${ }^{7}$ have also studied the angular distributions for $\ell^{+}$produced in the reaction with the longitudinally polarized proton beam $p_{h}$ with a helicity $h$

$$
\bar{p} p_{h} \rightarrow\left(\gamma^{*}, Z^{0}\right)+X \rightarrow \ell^{+} \ell^{-}+X
$$

in the rest system of $Z^{0}$ at $M=M_{Z}$. We differ from their study in that, whilst they restrict themselves to the Drell-Yan mechanism and to the standard model, we consider the first order QCD processes (dilepton production with large transverse momentum) and also consider the comparisons of the predictions of the standard and the left-right models. Also unlike in Ref. 6, we will not use the 3-quarks $\mathrm{SU}(6)$ wave function model for the spin dependent structure functions.

In Section 2 we present all the basic formulas for the reactions (1.1) for the general electroweak models. Section 3 presents two electroweak models we have considered, namely the standard and the left-right ones, together with the parametrization for the polarized parton distributions. Section 4 is devoted to the numerical results for differential cross-sections and the polarization asymmetries for the coefficients in the angular distribution. Section 5 contains the conclusion.

## 2. Basic Formulas

The Lagrangian for the neutral-current interaction reads as:

$$
\begin{equation*}
\mathcal{L}_{i n t}=e \bar{\ell} \gamma_{\mu} \ell A^{\mu}+\sum_{i} C_{i} \bar{\ell} \gamma_{\mu}\left(a_{i}^{\ell}-b_{i}^{\ell} \gamma_{5}\right) \ell Z_{i}^{\mu}+\sum_{i} C_{i} \bar{f} \gamma_{\mu}\left(a_{i}^{f}-b_{i}^{f} \gamma_{5}\right) f Z_{i}^{\mu} \tag{2.1}
\end{equation*}
$$

where $A_{\mu}, \ell, f$ and $Z_{i}^{0}(i=1,2, \ldots)$ are the photon, lepton, quark with flavour $f$, and $i-$ th neutral gauge boson field, respectively. $a_{i}$ and $b_{i}\left(a_{i}^{f}\right.$ and $b_{i}^{f}$ ) denote the vector and axial-vector coupling constants of the lepton (quark f) to the $Z_{i}^{0}$-boson. These couplings and the parameters $C_{i}$ which depend on the gauge group under consideration will be specified in the next section.

In the lowest order of QCD perturbation theory the angular distributions of high-mass $(M)$ lepton pairs produced with large transverse momentum $Q_{T}$ in reactions (1.1) are given by two hard parton processes: quark $q$-antiquark $\bar{q}$ annihilation into ( $\gamma^{*}, Z_{1}^{0}, Z_{2}^{0}, \ldots$ ) and a gluon $G$, and gluon-quark Compton scattering. The relevant Feynman diagrams are shown in Figs. 1a and 1b. We have calculated the differential cross-sections of the lepton pair from the decay of ( $\gamma^{*}, Z_{1}^{0}, Z_{2}^{0} \ldots$ ) produced in polarized annihilation and Compton subprocesses at fixed $M^{2}, \hat{t}$ and a solid angle $\Omega_{\ell}^{*}=(\theta, \phi)$ of one of leptons in the dilepton restframe. The final formulas for these partonic differential cross-sections, assuming massless leptons and quarks, are presented below.

For the annihilation subprocess (denoted by A)

$$
\begin{equation*}
q\left(h_{1}\right)+\bar{q}\left(h_{2}\right) \rightarrow\left(\gamma^{*}, Z_{1}^{0}, Z_{2}^{0}, \ldots\right)+G \rightarrow \ell^{+} \ell^{-}+G \tag{2.2}
\end{equation*}
$$

( $h_{1}$ is the helicity of the quark and $h_{2}$ is that of the antiquark), we obtain

$$
\begin{align*}
& \frac{d \hat{\sigma}_{A}\left(h_{1}, h_{2}\right)}{d M^{2} d \hat{t} d \Omega_{\ell}^{*}}=\frac{d \hat{\sigma}_{A}}{d M^{2} d \hat{t}}(\text { unpol. })\left(1-h_{1} h_{2}\right) \frac{3}{16 \pi} \\
& {\left[\left(1-\frac{h_{1} N_{f}}{K_{f}}\right)\left\{1+\cos ^{2} \theta+\hat{A}_{0}\left(\frac{1}{2}-\frac{3}{2} \cos ^{2} \theta\right)+\hat{A}_{1} \sin 2 \theta \cos \phi+\hat{A}_{2} \cdot \frac{1}{2} \sin ^{2} \theta \cos 2 \phi\right\}\right.} \\
& \left.+2\left(L_{f}-h_{1} M_{f}\right) / K_{f}\left\{\hat{A}_{3} \sin \theta \cos \phi+\hat{A}_{4} \cos \theta\right\}\right] \tag{2.3}
\end{align*}
$$

For the Compton scattering (denoted by $C$ )

$$
\begin{equation*}
G(\Lambda)+q\left(h_{1}\right) \rightarrow\left(\gamma^{*}, Z_{1}^{0}, Z_{2}^{0}, \ldots\right)+q \rightarrow \ell^{+} \ell^{-}+q \tag{2.4}
\end{equation*}
$$

( $\Lambda$ is the helicity of the gluon), we have

$$
\begin{align*}
& \frac{d \hat{\sigma}_{C}\left(\Lambda, h_{1}\right)}{d M^{2} d \hat{t} d \Omega_{\ell}^{*}}=\frac{d \hat{\sigma}_{A}}{d M^{2} d \hat{t}}(\text { unpol. }) \frac{3}{16 \pi} \\
& {\left[( 1 - \frac { h _ { 1 } N _ { f } } { K _ { f } } ) \left\{\left(1+h_{1} \Lambda \hat{B}_{00}\right)\left(1+\cos ^{2} \theta\right)+\left(\hat{A}_{0}+h_{1} \Lambda \hat{B}_{0}\right)\left(\frac{1}{2}-\frac{3}{2} \cos ^{2} \theta\right)\right.\right.}  \tag{2.5}\\
& \left.+\left(\hat{A}_{1}+h_{1} \Lambda \hat{B}_{1}\right) \sin 2 \theta \cos \phi+\left(\hat{A}_{2}+h_{1} \Lambda \hat{B}_{2}\right) \frac{1}{2} \sin ^{2} \theta \cos 2 \phi\right\} \\
& \left.+2\left(L_{f}-h_{1} M_{f}\right) / K_{f}\left\{\left(\hat{A}_{3}-h_{1} \Lambda \hat{B}_{3}\right) \sin \theta \cos \phi+\left(\hat{A}_{4}-h_{1} \Lambda \hat{B}_{4}\right) \cos \theta\right\}\right]
\end{align*}
$$

where caret denotes quantities at the parton level. The coefficients $\hat{A}_{i}$ (which take the same form in both annihilation and Compton subprocesses), $\hat{B}_{00}$ and $\hat{B}_{i}(i=0,1,2,3,4)$ are functions of parton momenta $\mathbf{p}_{1}$ and $\mathbf{p}_{2}$ in the dilepton rest-system and read as:

$$
\hat{A}_{0}=\hat{A}_{2}=\frac{p_{1 x}^{2}+p_{2 x}^{2}}{\left|\mathbf{p}_{1}\right|^{2}+\left|\mathbf{p}_{2}\right|^{2}}, \quad \hat{A}_{1}=\frac{p_{1 x} p_{1 z}+p_{2 x} p_{2 z}}{\left|\mathbf{p}_{1}\right|^{2}+\left|\mathbf{p}_{2}\right|^{2}}
$$

$$
\begin{gather*}
\hat{A}_{3}=\frac{\left|\mathbf{p}_{1}\right| p_{1 x}-\left|\mathbf{p}_{2}\right| p_{2 x}}{\left|\mathbf{p}_{1}\right|^{2}+\left|\mathbf{p}_{2}\right|^{2}}, \quad \hat{A}_{4}=\frac{\left|\mathbf{p}_{1}\right| p_{1 z}-\left|\mathbf{p}_{2}\right| p_{2 z}}{\left|\mathbf{p}_{1}\right|^{2}+\left|\mathbf{p}_{2}\right|^{2}} \\
\hat{B}_{00}=\frac{\left|\mathbf{p}_{2}\right|^{2}-\left|\mathbf{p}_{1}\right|^{2}}{\left|\mathbf{p}_{1}\right|^{2}+\left|\mathbf{p}_{2}\right|^{2}} \\
\hat{B}_{0}=\hat{B}_{2}=\frac{p_{2 x}^{2}-p_{1 x}^{2}}{\left|\mathbf{p}_{1}\right|^{2}+\left|\mathbf{p}_{2}\right|^{2}}, \quad \hat{B}_{1}=\frac{p_{2 x} p_{2 z}-p_{1 x} p_{1 z}}{\left|\mathbf{p}_{1}\right|^{2}+\left|\mathbf{p}_{2}\right|^{2}} \\
\hat{B}_{3}=\frac{\left|\mathbf{p}_{1}\right| p_{1 x}+\left|\mathbf{p}_{2}\right| p_{2 x}}{\left|\mathbf{p}_{1}\right|^{2}+\left|\mathbf{p}_{2}\right|^{2}}, \quad \hat{B}_{4}=\frac{\left|\mathbf{p}_{1}\right| p_{1 z}+\left|\mathbf{p}_{2}\right| p_{2 z}}{\left|\mathbf{p}_{1}\right|^{2}+\left|\mathbf{p}_{2}\right|^{2}} \tag{2.6}
\end{gather*}
$$

All informations about the underlying electroweak interactions are contained in $K_{f}, L_{f}, M_{f}$, and $N_{f}:$

$$
\begin{aligned}
K_{f}= & \frac{e_{f}^{2}}{M^{4}}-2 \sum_{i} e_{f}\left(\frac{C_{i}}{e}\right)^{2} a_{i} a_{i}^{f} \frac{\operatorname{Re} D_{i}}{M^{2}}+2 \sum_{i<j}\left(\frac{C_{i} C_{j}}{e^{2}}\right)^{2} \\
& \left(a_{i} a_{j}+b_{i} b_{j}\right)\left(a_{i}^{f} a_{j}^{f}+b_{i}^{f} b_{j}^{f}\right) \operatorname{Re}\left(D_{i} D_{j}^{*}\right) \\
& +\sum_{i}\left(\frac{C_{i}}{e}\right)^{4}\left(a_{i}^{2}+b_{i}^{2}\right)\left\{\left(a_{i}^{f}\right)^{2}+\left(b_{i}^{f}\right)^{2}\right\}\left|D_{i}\right|^{2} \\
L_{f}= & -2 \sum_{i} e_{f}\left(\frac{C_{i}}{e}\right)^{2} b_{i} b_{i}^{f} \frac{\operatorname{Re} D_{i}}{M^{2}}+2 \sum_{i<j}\left(\frac{C_{i} C_{j}}{e^{2}}\right)^{2} \\
& \left(a_{i} b_{j}+b_{i} a_{j}\right)\left(a_{i}^{f} b_{j}^{f}+b_{i}^{f} a_{j}^{f}\right) \operatorname{Re}\left(D_{i} D_{j}^{*}\right) \\
& +4 \sum_{i}\left(\frac{C_{i}}{e}\right)^{4} a_{i} b_{i} a_{i}^{f} b_{i}^{f}\left|D_{i}\right|^{2}, \\
M_{f}= & -2 \sum_{i} e_{f}\left(\frac{C_{i}}{e}\right)^{2} b_{i} a_{i}^{f} \frac{\operatorname{Re} D_{i}}{M^{2}}+2 \sum_{i<j}\left(\frac{C_{i} C_{j}}{e^{2}}\right)^{2} \\
& \left(a_{i} b_{j}+b_{i} a_{j}\right)^{\prime}\left(a_{i}^{f} a_{j}^{f}+b_{i}^{f} b_{j}^{f}\right) \operatorname{Re}\left(D_{i} D_{j}^{*}\right) \\
& +2 \sum_{i}\left(\frac{C_{i}}{e}\right)^{4} a_{i} b_{i}\left\{\left(a_{i}^{f}\right)^{2}+\left(b_{i}^{f}\right)^{2}\right\}\left|D_{i}\right|^{2},
\end{aligned}
$$

$$
\begin{align*}
N_{f}= & -2 \sum_{i} e_{f}\left(\frac{C_{i}}{e}\right)^{2} a_{i} b_{i}^{f} \frac{\operatorname{Re} D_{i}}{M^{2}}+2 \sum_{i<j}\left(\frac{C_{i} C_{j}}{e^{2}}\right)^{2} \\
& \left(a_{i} a_{j}+b_{i} b_{j}\right)\left(a_{i}^{f} b_{j}^{f}+b_{i}^{f} a_{j}^{f}\right) \operatorname{Re}\left(D_{i} D_{j}^{*}\right)  \tag{2.7}\\
& +2 \sum_{i}\left(\frac{C_{i}}{e}\right)^{4}\left(a_{i}^{2}+b_{i}^{2}\right) a_{i}^{f} b_{i}^{f}\left|D_{i}\right|^{2}
\end{align*}
$$

where $D_{i}$ is the propagator of the $Z_{i}^{0}$-boson with its mass $M_{Z_{i}}$ and the width $\Gamma_{Z_{i}}:$

$$
\begin{equation*}
D_{i}=\left(M^{2}-M_{Z_{i}}^{2}+i M_{Z_{i}} \Gamma_{Z_{i}}\right)^{-1} \tag{2.8}
\end{equation*}
$$

The differential cross-sections in the unpolarized case are ${ }^{14}$ :

$$
\begin{align*}
& \frac{d \hat{\sigma}_{A}}{d M^{2} d \hat{t}}(\text { unpol. })=\frac{4}{9} \cdot \frac{2}{3} \frac{\alpha^{2} \alpha_{s}}{\hat{s}^{2}} \frac{\left(\hat{t}-M^{2}\right)^{2}+\left(\hat{u}-M^{2}\right)^{2}}{\hat{t} \hat{u}} M^{2} K_{f}, \\
& \left.\frac{d \hat{\sigma}_{C}}{d M^{2} d \hat{t}} \text { (unpol. }\right)=\frac{1}{6} \cdot \frac{2}{3} \frac{\alpha^{2} \alpha_{s}}{\hat{s}^{2}} \frac{\left(\hat{s}-M^{2}\right)^{2}+\left(\hat{u}-M^{2}\right)^{2}}{-\hat{s} \hat{u}} M^{2} K_{f} . \tag{2.9}
\end{align*}
$$

with the standard notations.
In order to calculate the cross-sections $d \sigma_{A, C} / d M^{2} d y d Q_{T}^{2}$ (where $y$ is the rapidity of the dilepton) and the coefficients $A_{i}(i=0,1,2,3,4)$ in the angular distributions for the polarized hadronic collisions, one has to convolute the corresponding quantities for the subprocesses (i.e. the ones with caret) with the parton spin distribution functions inside the hadrons $f_{f( \pm)}^{p(+)}, G_{ \pm}^{+}(x)$, etc. (e.g., $f_{f( \pm)}^{p(+)}$ and $G_{ \pm}^{+}(x)$ denote the spin distribution functions of the valence quark $f$ and the gluon $G$ with the helicity $\pm 1$ inside a proton with $h=+1$.) Then the differential cross-section for processes (1.1) can be expanded in terms of the
$\Omega_{\ell}^{*}(\theta, \phi)$ as:

$$
\begin{align*}
& \frac{d \sigma\left(h_{1}, h_{2}\right)}{d M^{2} d y d Q_{T}^{2} d \Omega_{\ell}^{*}} \propto 1+\cos ^{2} \theta+A_{0}\left(h_{1}, h_{2}\right)\left(\frac{1}{2}-\frac{3}{2} \cos ^{2} \theta\right) \\
& +A_{1}\left(h_{1}, h_{2}\right) \sin 2 \theta \cos \phi+A_{2}\left(h_{1}, h_{2}\right) \frac{1}{2} \sin ^{2} \theta \cos 2 \phi  \tag{2.10}\\
& +A_{3}\left(h_{1}, h_{2}\right) \sin \theta \cos \phi+A_{4}\left(h_{1}, h_{2}\right) \cos \theta
\end{align*}
$$

[The formula for the angular distribution at the one-loop order have been derived in Ref. ${ }^{18}$ ] The total coefficients of the angular distributions can be obtained in an analogous way as in the unpolarized case, by summing over the annihilation and the Compton contributions, i.e.,

$$
\begin{align*}
& \text { for } \bar{p} p_{h} \text { - collision with the helicity } h= \pm 1 \\
& \qquad A_{i}( \pm)=\frac{A_{i} d \sigma_{A}( \pm)+A_{i} d \sigma_{C}( \pm)}{d \sigma( \pm)}, \quad(i=0,1,2,3,4) \tag{2.11}
\end{align*}
$$

where

$$
\begin{gather*}
\qquad d \sigma( \pm)=d \sigma_{A}( \pm)+d \sigma_{C}( \pm) \\
\qquad d \sigma_{A, C}( \pm)=d \sigma_{A, C}( \pm) / d M^{2} d y d Q_{T}^{2} \\
\text { for } p_{h} p_{h}-\text { collision with the helicity } h= \pm 1 \\
A_{i}( \pm \pm)=\frac{A_{i} d \sigma_{A}( \pm \pm)+A_{i} d \sigma_{C}( \pm \pm)}{d \sigma( \pm \pm)}, \quad(i=0,1,2,3,4) \tag{2.12}
\end{gather*}
$$

where

$$
d \sigma( \pm \pm)=d \sigma_{A}( \pm \pm)+d \sigma_{C}( \pm \pm)
$$

$$
d \sigma_{A, C}( \pm \pm)=d \sigma_{A, C}( \pm \pm) / d M^{2} d y d Q_{T}^{2}
$$

In the following we present the formulas derived assuming that the valence quark $f$ and the gluon $G$ are polarized, but the sea-quark component remains unpolarized in the proton.
for $\bar{p} p_{h}$-collision
One can define the asymmetry of the $\left(1+\cos ^{2} \theta\right)$ term of the cross-section (See Eq.(2.10)) due to the longitudinal beam polarization as

$$
\begin{equation*}
\text { Asymmetry }=\frac{d \sigma(-)-d \sigma(+)}{d \sigma(-)+d \sigma(+)}=\frac{\sum_{f}\left\{\Delta F^{p \bar{p}}(A)+\Delta F_{00}^{p \bar{p}}(C)\right\} N_{f}}{\sum_{f}\left\{F^{p \bar{p}}(A)+F^{p \bar{p}}(C)\right\} K_{f}} \tag{2.13}
\end{equation*}
$$

where

$$
\begin{gather*}
\Delta F^{p \bar{p}}(A)=\Delta f_{f}^{p}\left(x_{1}\right) f_{\bar{f}}^{\bar{p}}\left(x_{2}\right) d \hat{\sigma}_{A}, \\
\Delta F_{o 0}^{p \bar{p}}(C)=\left\{-\Delta G\left(x_{1}\right) f_{\bar{f}}^{\bar{p}}\left(x_{2}\right) \hat{B}_{00}+\Delta f_{f}^{p}\left(x_{1}\right) G\left(x_{2}\right)\right\} d \hat{\sigma}_{C}, \\
F^{p \bar{p}}(A)=f_{f}^{p}\left(x_{1}\right) f_{\bar{f}}^{\bar{p}}\left(x_{2}\right) d \hat{\sigma}_{A}, \\
F^{p \bar{p}}(C)=\left\{G\left(x_{1}\right) f_{\bar{f}}^{\bar{p}}\left(x_{2}\right)+f_{f}^{p}\left(x_{1}\right) G\left(x_{2}\right)\right\} d \hat{\sigma}_{C} \\
d \hat{\sigma}_{A, C}=d \hat{\sigma}_{A, C} / d M^{2} d \hat{t}, \\
\Delta f_{f}^{p}\left(x_{1}\right)=f_{f(+)}^{p(+)}\left(x_{1}\right)-f_{f(-)}^{p(+)}\left(x_{1}\right) \\
f_{f}^{p}\left(x_{1}\right)=f_{f(+)}^{p(+)}\left(x_{1}\right)+f_{f(-)}^{p(+)}\left(x_{1}\right) \tag{2.14a}
\end{gather*}
$$

(The similar formulas hold for $\Delta f_{f}^{\bar{p}}\left(x_{2}\right)$ etc.)

$$
\Delta G\left(x_{1}\right)=G_{+}^{+}\left(x_{1}\right)-G_{-}^{+}\left(x_{1}\right)
$$

$$
\begin{equation*}
G\left(x_{1}\right)=G_{+}^{+}\left(x_{1}\right)+G_{-}^{+}\left(x_{1}\right) \tag{2.14b}
\end{equation*}
$$

From Eq. (2.13) it is clear that the sign of this asymmetry is related through $N_{f}$ to that of the axial couplings $b_{i}^{f}$ and this is the only way to determine it.

Also one can define the polarization (spin) asymmetries for the coefficients in the angular distributions:

$$
\begin{equation*}
\Delta A_{i}=\frac{A_{i}(-)-A_{i}(+)}{A_{i}(-)+A_{i}(+)}, \quad(i=0,1,2,3,4) \tag{2.15a}
\end{equation*}
$$

Writing in an explicit form we have for $i=0,1,2$

$$
\begin{equation*}
\Delta A_{i}=\frac{\sum_{f}\left\{\Delta F_{i}^{p \bar{p}}(A)+\Delta F_{i}^{p \bar{p}}(C)\right\} N_{f}}{\sum_{f}\left\{F_{i}^{p \bar{p}}(A)+F_{i}^{p \bar{p}}(C)\right\} K_{f}}, \quad(i=0,1,2) \tag{2.15b}
\end{equation*}
$$

where

$$
\begin{gathered}
\Delta F_{i}^{p \bar{p}}(A)=\Delta f_{f}^{p}\left(x_{1}\right) f_{\bar{f}}^{\bar{p}}\left(x_{2}\right) \hat{A}_{i} d \hat{\sigma}_{A}, \quad(i=0,1,2,3,4), \\
\Delta F_{i}^{p \bar{p}}(C)=\left\{-\Delta G\left(x_{1}\right) f_{\bar{f}}^{\bar{p}}\left(x_{2}\right) \hat{B}_{i}+\Delta f_{f}^{p}\left(x_{1}\right) G\left(x_{2}\right) \hat{A}_{i}\right\} d \hat{\sigma}_{C}, \quad(i=0,1,2), \\
F_{i}^{p \bar{p}}(A)=f_{f}^{p}\left(x_{1}\right) f_{\bar{f}}^{\bar{p}}\left(x_{2}\right) \hat{A}_{i} d \hat{\sigma}_{A}, \quad(i=0,1,2,3,4), \\
F_{i}^{p \bar{p}}(C)=\left\{G\left(x_{1}\right) f_{\bar{f}}^{\bar{p}}\left(x_{2}\right)+f_{f}^{p}\left(x_{1}\right) G\left(x_{2}\right)\right\} \hat{A}_{i} d \hat{\sigma}_{C}, \quad(i=0,1,2,3,4),
\end{gathered}
$$

Note that relations $A_{0}=A_{2}$ and $\Delta A_{0}=\Delta A_{2}$ hold on account of a $\mathbf{p}_{1} \leftrightarrow \mathbf{p}_{2}$ symmetry, reflecting the vector nature of the gluon ${ }^{19}$ (however, $A_{0} \neq A_{2}$ and $\Delta A_{0} \neq \Delta A_{2}$, if the gluon would appear to be a scalar particle).

For $i=3,4$ we have

$$
\begin{equation*}
\Delta A_{i}=\frac{\sum_{f}\left\{\Delta F_{i}^{p \bar{p}}(A)+\Delta F_{i}^{p \bar{p}}(C)\right\} M_{f}}{\sum_{f}\left\{F_{i}^{p \bar{p}}(A)+F_{i}^{p \bar{p}}(C)\right\} L_{f}}, \quad(i=3,4) \tag{2.15c}
\end{equation*}
$$

where

$$
\Delta F_{i}^{p \bar{p}}(C)=\left\{\Delta G\left(x_{1}\right) f_{\bar{f}}^{\bar{p}}\left(x_{2}\right) \hat{B}_{i}+\Delta f_{f}^{p}\left(x_{1}\right) G\left(x_{2}\right) \hat{A}_{i}\right\} d \hat{\sigma}_{C}, \quad(i=3,4)
$$

$p_{h} p_{h}-$ collision
Similarly one can define various experimentally accessible polarization asymmetries when both of the proton beams are longitudinally polarized:

$$
\begin{equation*}
\text { Asymmetry }=\frac{d \sigma(--)-d \sigma(++)}{d \sigma(--)+d \sigma(++)} \tag{2.16a}
\end{equation*}
$$

which can be rewritten as

$$
\begin{equation*}
\text { Asymmetry }=\frac{\sum_{f}\left\{\Delta F^{p p}(A)+\Delta F_{00}^{p p}(C)\right\} N_{f}}{\sum_{f}\left\{F^{p p}(A)+F_{00}^{p p}(C)\right\} K_{f}} \tag{2.16b}
\end{equation*}
$$

where

$$
\begin{gathered}
\Delta F^{p p}(A)=\left\{\Delta f_{f}^{p}\left(x_{1}\right) f_{\bar{f}}^{p}\left(x_{2}\right)+f_{\tilde{f}}^{p}\left(x_{1}\right) \Delta f_{f}^{p}\left(x_{2}\right)\right\} d \hat{\sigma}_{A}, \\
\Delta F_{00}^{p p}(C)=\left\{G\left(x_{1}\right) \Delta f_{f}^{p}\left(x_{2}\right)+\Delta G\left(x_{1}\right) f_{f}^{p}\left(x_{2}\right) \hat{B}_{00}\right\} d \hat{\sigma}_{C} \\
F^{p p}(A)=\left\{f_{f}^{p}\left(x_{1}\right) f_{\tilde{f}}^{p}\left(x_{2}\right)+f_{f}^{p}\left(x_{1}\right) f_{f}^{p}\left(x_{2}\right)\right\} d \hat{\sigma}_{A}, \\
F_{00}^{p p}(C)=\left\{G\left(x_{1}\right) f_{f}^{p}\left(x_{2}\right)+\Delta G\left(x_{1}\right) \Delta f_{f}^{p}\left(x_{2}\right) \hat{B}_{00}\right\} d \hat{\sigma}_{C}
\end{gathered}
$$

For the polarization asymmetries of the coefficients in the angular distribution
we have

$$
\begin{equation*}
\Delta A_{i}=\frac{A_{i}(--)-A_{i}(++)}{A_{i}(--)+A_{i}(++)}, \quad(i=0,1,2,3,4) \tag{2.17a}
\end{equation*}
$$

Explicitly for $i=0,1,2$ we have

$$
\begin{equation*}
\Delta A_{i}=\frac{\sum_{f}\left\{\Delta F_{i}^{p p}(A)+\Delta F_{i}^{p p}(C)\right\} N_{f}}{\sum_{f}\left\{F_{i}^{p p}(A)+F_{i}^{p p}(C)\right\} K_{f}}, \quad(i=0,1,2) \tag{2.17b}
\end{equation*}
$$

where

$$
\begin{array}{cc}
\Delta F_{i}^{p p}(A)=\left\{\Delta f_{f}^{p}\left(x_{1}\right) f_{\tilde{f}}^{p}\left(x_{2}\right)+f_{\tilde{f}}^{p}\left(x_{1}\right) \Delta f_{f}^{p}\left(x_{2}\right)\right\} \hat{A}_{i} d \hat{\sigma}_{A}, & (i=0,1,2), \\
\Delta F_{i}^{p p}(C)=\left\{G\left(x_{1}\right) \Delta f_{f}^{p}\left(x_{2}\right) \hat{A}_{i}+\Delta G\left(x_{1}\right) f_{f}^{p}\left(x_{2}\right) \hat{B}_{i}\right\} d \hat{\sigma}_{C}, & (i=0,1,2), \\
F_{i}^{p p}(A)=\left\{f_{f}^{p}\left(x_{1}\right) f_{f}^{p}\left(x_{2}\right)+f_{f}^{p}\left(x_{1}\right) f_{f}^{p}\left(x_{2}\right)\right\} \hat{A}_{i} d \hat{\sigma}_{A}, & (i=0,1,2), \\
F_{i}^{p p}(C)=\left\{G\left(x_{1}\right) f_{f}^{p}\left(x_{2}\right) \hat{A}_{i}+\Delta G\left(x_{1}\right) \Delta f_{f}^{p}\left(x_{2}\right) \hat{B}_{i}\right\} d \hat{\sigma}_{C}, & (i=0,1,2) .
\end{array}
$$

One has also $A_{0}=A_{2}$ and $\Delta A_{0}=\Delta A_{2}$, because of $p_{1} \leftrightarrow p_{2}$ symmetry and the vector nature of the gluon.

For $i=3,4$ we have

$$
\begin{equation*}
\Delta A_{i}=\frac{\sum_{f}\left\{\Delta F_{i}^{p p}(A)+\Delta F_{i}^{p p}(C)\right\} M_{f}}{\sum_{f}\left\{F_{i}^{p p}(A)+F_{i}^{p p}(C)\right\} L_{f}}, \quad(i=3,4) \tag{2.17c}
\end{equation*}
$$

where

$$
\begin{aligned}
& \Delta F_{i}^{p p}(A)=\left\{\Delta f_{f}^{p}\left(x_{1}\right) f_{\bar{f}}^{p}\left(x_{2}\right)-f_{\hat{f}}^{p}\left(x_{1}\right) \Delta f_{f}^{p}\left(x_{2}\right)\right\} \hat{A}_{i} d \hat{\sigma}_{A}, \quad(i=3,4), \\
& \Delta F_{i}^{p p}(C)=\left\{G\left(x_{1}\right) \Delta f_{f}^{p}\left(x_{2}\right) \hat{A}_{i}-\Delta G\left(x_{1}\right) f_{f}^{p}\left(x_{2}\right) \hat{B}_{i}\right\} d \hat{\sigma}_{C}, \quad(i=3,4),
\end{aligned}
$$

$$
\begin{gathered}
F_{i}^{p p}(A)=\left\{f_{f}^{p}\left(x_{1}\right) f_{f}^{p}\left(x_{2}\right)-f_{\hat{f}}^{p}\left(x_{1}\right) f_{f}^{p}\left(x_{2}\right)\right\} \hat{A}_{i} d \hat{o}_{A}, \\
F_{i}^{p p}(C)=\left\{G\left(x_{1}\right) f_{f}^{p}\left(x_{2}\right) \hat{A}_{i}-\Delta G\left(x_{1}\right) \Delta f_{f}^{p}\left(x_{2}\right) \hat{B}_{i}\right\} d \hat{o}_{C}, \\
(i=3,4) .
\end{gathered}
$$

## 3. Electroweak Models and the Parametrizations

There is a nontrivial class of left-right models in which the lowest-mass gauge boson $Z_{1}^{0}$ is indistinguishable in mass and fermion couplings from the standard $Z^{0}$, but which allows a second gauge boson $Z_{2}^{0}$ as low as 200 GeV [see Ref. 3]. In such a left-right model the vector and axial-coupling constants of the lepton $\ell$ (quark $f$ ) to the $Z_{i}^{0}$-boson $(i=1,2), a_{i}^{\ell}$ and $b_{i}^{\ell}\left(a_{i}^{f}\right.$ and $\left.b_{i}^{f}\right)$ are expressed as follows:

For $i=1$ ( the lighter gauge boson $Z_{1}^{0}$ ), one has the standard model values:

$$
\begin{align*}
& a_{1}^{\ell}=x_{L}-\frac{1}{4} \\
& b_{1}^{\ell}=-\frac{1}{4}, \quad \text { for } \quad \ell=e, \mu, \quad \text { and } \quad \tau \tag{2.18a}
\end{align*}
$$

and

$$
\begin{align*}
a_{1}^{f} & =\frac{1}{2} I_{3}^{f}-e_{f} x_{L} \\
b_{1}^{f} & =\frac{1}{2} I_{3}^{f} \tag{2.18b}
\end{align*}
$$

where $I_{3}^{f}$ is the third component of the left-handed weak isospin of the quark, $e_{f}$ is the charge of the quark $f$ divided by the electric charge $e$, and $x_{L}=e^{2} / g_{L}^{2}=$ $\sin ^{2} \theta_{W}$ with $\theta_{W}$ being the Weinberg angle.

For $i=2$ (the heavier gauge boson $Z_{2}^{0}$ ), one has

$$
\begin{align*}
& a_{2}^{\ell}=\left(x_{L} / x_{R}\right)^{1 / 2}\left(1-x_{L}-x_{R}\right)^{-1 / 2}\left\{-\frac{1}{4}\left(1-x_{L}+x_{R}\right)+x_{R}\right\} \\
& b_{2}^{\ell}=\frac{1}{4}\left(x_{L} / x_{R}\right)^{1 / 2}\left(1-x_{L}-x_{R}\right)^{1 / 2}, \quad \text { for } \quad \ell=e, \mu, \quad \text { and } \quad \tau \tag{2.19a}
\end{align*}
$$

$$
\begin{align*}
& a_{2}^{f}=\left(x_{L} / x_{R}\right)^{1 / 2}\left(1-x_{L}-x_{R}\right)^{-1 / 2}\left\{\frac{1}{2} I_{3}^{f} \cdot\left(1-x_{L}+x_{R}\right)-e_{f} x_{R}\right\} \\
& b_{2}^{f}=-\left(x_{L} / x_{R}\right)^{1 / 2}\left(1-x_{L}-x_{R}\right)^{1 / 2} \cdot \frac{1}{2} I_{3}^{f} \tag{2.19b}
\end{align*}
$$

where $x_{R}=e^{2} / g_{R}^{2}\left[g_{R}\right.$ being the $S U(2)_{R}$ coupling constant $]$ is the parameter which characterizes the properties (mass, width, fermion coupling...) of the $Z_{2}^{0}$. A gauge-group-dependent parameter $C_{i}$ within the left-right model we consider is given as:

$$
\begin{equation*}
C_{1}=C_{2}=e x_{L}^{-1 / 2}\left(1-x_{L}\right)^{-1 / 2} \tag{2.19c}
\end{equation*}
$$

In our numerical calculations we employ the standard model as well as the leftright model with the following parameters which reproduce the standard values at $Z=Z_{1}^{0}$, with three fermion generations, i.e., $N_{f}=6$ :

$$
\begin{align*}
x_{L} & =0.233, \quad x_{R}=0.5 \\
M_{Z_{1}} & =93 \mathrm{GeV}, \quad M_{Z_{2}}=200 \mathrm{GeV}  \tag{2.20}\\
\Gamma_{Z_{1}} & =2.87 \mathrm{GeV}, \quad \Gamma_{Z_{2}}=3.77 \mathrm{GeV} .
\end{align*}
$$

As the parton spin distribution functions in the longitudinally polarized proton we employ the ones of Carlitz- Kaur(plus gluon) model, according to which the (spin) distributions of the $u$ and $d$ quarks read as: ${ }^{20}$

$$
\begin{align*}
& f_{u}^{p}(x)=u_{v}+\bar{u}, \\
& f_{d}^{p}(x)=d_{v}+\bar{d} \tag{2.21a}
\end{align*}
$$

where

$$
\bar{u}(x)=\bar{d}(x)=\frac{0.6}{x} \cdot(1-x)^{10}
$$

$$
\begin{align*}
& \Delta f_{u}^{p}(x)=f_{u(+)}^{p(+)}(x)-f_{u(-)}^{p(+)}(x)=\left(u_{v}-\frac{2}{3} d_{v}\right) \cos 2 \theta \\
& \Delta f_{d}^{p}(x)=f_{d(+)}^{p(+)}(x)-f_{d(-)}^{p(+)}(x)=-\frac{1}{3} d_{v} \cos 2 \theta \tag{2.21b}
\end{align*}
$$

with a spin dilution factor

$$
\begin{equation*}
\cos 2 \theta=\left\{1+0.052 x^{-1 / 2}(1-x)^{2}\right\}^{-1} \tag{2.21c}
\end{equation*}
$$

The sea-quark component is assumed to be unpolarized, i.e.,

$$
\begin{equation*}
\Delta f_{\bar{u}}^{p}(x)=\Delta f_{\bar{d}}^{p}(x)=0 . \tag{2.22}
\end{equation*}
$$

The spin distribution of the gluon inside the proton has been estimated as follows, ${ }^{21}$ assuming that the sea quarks are unpolarized and that the polarized gluons are emitted from the polarized valence quarks due to the QCD bremsstrahlung: ${ }^{22}$

$$
\begin{align*}
& G(x)=\frac{1.97}{x}(1-x)^{6}\left\{1+(1-x)^{2}\right\}  \tag{2.23}\\
& \Delta G(x)=G_{+}^{+}(x)-G_{-}^{+}(x)=0.43(2-x)(1-x)^{6}
\end{align*}
$$

For the (scale-violating) distributions of the valence quarks inside the proton ${ }^{23}$ $: u_{v}=u_{v}\left(x, Q^{2}\right)$ and $d_{v}=d_{v}\left(x, Q^{2}\right)$, we employ the ones by Glück, Hoffmann, and Reya, ${ }^{24}$ taking as the scale of QCD evolution, $Q^{2}=M^{2}=$ invariant mass squared of the lepton pair. For the QCD coupling constant $\alpha_{s}$ we use

$$
\begin{equation*}
\alpha_{s}\left(Q^{2}\right)=\frac{12 \pi}{33-2 N_{f}} \frac{1}{\ln Q^{2} / \Lambda^{2}} \tag{2.24}
\end{equation*}
$$

with $N_{f}=6$ and $\Lambda=0.4 \mathrm{GeV}$ which has been used in the fits of Ref. 24.

## 4. Numerical Results

As an application of the formulas discussed in Sections 2 and 3, we present in this Section the numerical results for the dileptons produced in $\bar{p} p_{h}$-collision at $\sqrt{s}=540 \mathrm{GeV}$ as well as in $p_{h} p_{h}$-collision at $\sqrt{s}=2 \mathrm{TeV}$. In order to get as large as possible cross-section, we carry out the integration over the rapidity $y$ of the dilepton in the range $-\ln 2 / \bar{x}_{T} \leq y \leq \ln 2 / \bar{x}_{T}$ which is obtained from the kinematical condition ${ }^{14}$

$$
\begin{equation*}
\left(x_{1}-\frac{1}{2} \bar{x}_{T} e^{y}\right)\left(x_{2}-\frac{1}{2} \bar{x}_{T} e^{-y}\right)=\frac{x_{T}^{2}}{4}, \tag{3.1}
\end{equation*}
$$

where $\bar{x}_{T}=\sqrt{x_{T}^{2}+4 \tau}, x_{T}=2 Q_{T} / \sqrt{s}$, and $\tau=M^{2} / s$. In the calculation $Q_{T}$ of the dilepton is fixed at $Q_{T}=5 \mathrm{GeV}$. In some cases, we also present the results obtained by integrating over $Q_{T}$ in the range $2 \leq Q_{T} \leq 12 \mathrm{GeV}$ (thereby introducing a cut-off in $Q_{T}$ ). Among various experimentally accessible coefficients in the angular distribution we will confine ourselves only to the parity-violating parameter $\alpha_{1}$ which appears in the polar angle distribution ${ }^{14}$

$$
\begin{equation*}
\frac{d N}{d \cos \theta}=C\left(1+\alpha_{1} \cos \theta+\alpha_{2} \cos ^{2} \theta\right) \tag{3.2}
\end{equation*}
$$

where

$$
\begin{align*}
C & =\frac{3}{8}\left(1+\frac{A_{0}}{2}\right) \\
\alpha_{1} & =\frac{A_{4}}{1+\frac{1}{2} A_{0}}, \quad \alpha_{2}=\frac{1-\frac{3}{2} A_{0}}{1+\frac{1}{2} A_{0}} \tag{3.3}
\end{align*}
$$

and present the results for the polarization asymmetry $\Delta A_{4}$ given in Eqs.(2.15c) and $(\mathbf{2} .17 \mathrm{c})$. Note that the curves for $\alpha_{1}$, both in the standard and the left-right models change their sign in the Gottfried-Jackson (GJ-) frame as a function of
$M$ near $M=M_{Z_{i}}$ on account of the $L_{f}$ term, the interference between the $\gamma^{*}$ and the $Z_{i}^{0}$-boson contributions. ${ }^{14}$ One can take the advantage of this feature in determining $Z_{i}^{0}$-boson mass thereby testing the electroweak models. We present the numerical results for $\bar{p} p$-collision at $\sqrt{s}=540 \mathrm{GeV}$ in Figs. 2-9 and for $p p$-collision at $\sqrt{s}=2 \mathrm{TeV}$ in Figs. 10-13.
$\bar{p} p-$ collision at $\sqrt{s}=540 \quad \mathrm{GeV}$
We show in Figs.2-4 the following curves for the differential cross-section:
Fig. 2: $d \sigma / d M d Q_{T}$ as a function of $M$ in unpolarized $\bar{p} p$-collision at $Q_{T}=5$ GeV within the framework of both the standard and the left-right models.

Fig. 3: $d \sigma / d M d Q_{T}$ for unpolarized $\bar{p} p$-collision as a function of $Q_{T}$ in the left-right model at $M=M_{Z_{1}}=93 \mathrm{GeV}$ and $M=M_{Z_{2}}=200 \mathrm{GeV}$.

Fig. 4: $d \sigma / d M$ for unpolarized $\bar{p} p$-collison as a function of $M$, calculated in the Drell-Yan model and the left-right model.

In Figs. 5-6 we present the curves for the asymmetry defined in Eq.(2.13).
Fig. 5: $\{d \sigma(-)-d \sigma(+)\} /\{d \sigma(-)+d \sigma(+)\}$ as a function of $M$, for $\bar{p} p_{h^{-}}$ collision at $Q_{T}=5 \mathrm{GeV}$ within the framework of the standard and the left-right models, where $d \sigma( \pm)=d \sigma( \pm) / d M d Q_{T}$.

Fig. 6: $\{d \sigma(-)-d \sigma(+)\} /\{d \sigma(-)+d \sigma(+)\}$ as a function of $M$, for $\bar{p} p_{h^{-}}$ collision within the framework of the standard and the left-right models, where $d \sigma( \pm)=\int_{2}^{12} d Q_{T} d \sigma( \pm) / d M d Q_{T}$. This quantity has been calculated also in Ref. $\left[{ }^{25}\right.$ ] using the Drell-Yan model within the framework of the standard model.

The curves for the polarization asymmetry of the coefficient $\Delta A_{4}$ under different conditions are shown in Figs. 7-9:

Fig. 7: $\Delta A_{4}$ as a function of $M$, for $\bar{p} p_{h}$-collision at $Q_{T}=5 \mathrm{GeV}$, calculated in the GJ-frame within the framework of the standard and the left-right models.

Fig. 8: $\Delta A_{4}$ as a function of $M$, for $\bar{p} p_{h}$-collision, integrated over $Q_{T}$ in the range $2 \leq Q_{T} \leq 12 \mathrm{GeV}$ and calculated in the GJ-frame within the framework of the standard and the left-right models.

Fig. 9: $\Delta A_{4}$ as a function of $Q_{T}$, for $\bar{p} p_{h}$-collision at $M=M_{Z_{1}}=93 \mathrm{GeV}$ and $M=M_{Z_{2}}=200 \mathrm{GeV}$, calculated in the GJ-frame within the framework of the left-right model.

$$
p p-\text { collision at } \sqrt{s}=2 \mathrm{TeV}
$$

In Figs. 10-12 we display the curves for the differential and the integrated cross-sections:

Fig. 10: $d \sigma / d M d Q_{T}$ as a function of $M$ for unpolarized $p p$-collision at $Q_{T}=5$ GeV within the framework of both the standard model and the left-right models.

Fig. 11: $d \sigma / d M d Q_{T}$ for unpolarized $p p$-collision as a function of $Q_{T}$ in the left-right model at $M=M_{Z_{1}}=93 \mathrm{GeV}$ and $M=M_{Z_{2}}=200 \mathrm{GeV}$.

Fig. 12: $\int_{2}^{12} d Q_{T} d \sigma / d M d Q_{T}$ as a function of $M$, calculated within the framework of the left-right model, for unpolarized pp-collision.

The polarization asymmetry of the cross-section defined in Eq.(2.16a): $\{d \sigma(--)-d \sigma(++)\} /\{d \sigma(--)+d \sigma(++)\}$ is shown in Fig. 13 as a function of $M$, for doubly polarized $p_{h} p_{h}$-collision, calculated within the framework of the standard and the left-right models, where $d \sigma( \pm \pm)=\int_{2}^{12} d Q_{T} d \sigma( \pm \pm) / d M d Q_{T}$.

Before concluding this section let us make a few remarks.

1. The predictions by the standard model cannot be discriminated from the ones by the left-right model near to $M \simeq M_{Z_{1}}$. The difference between
the two models starts to appear only in $M \gtrsim 150 \mathrm{GeV}$, and becomes most prominent in the region $M \simeq M_{Z_{2}}$.
2. The shapes of the curves in Figs. 5, 7 with fixed $Q_{T}(=5 \mathrm{GeV})$ are very similar to the ones of the curves in Figs. 6, 8 correspondingly in which $Q_{T}$ is integrated over in the region $2 \leq Q_{T} \leq 12 \mathrm{GeV}$, but the absolute values differ slightly.
3. The asymmetry of the coefficient $\Delta A_{4}$ (shown in Figs. 7, 8, and 9), calculated in the GJ-frame, almost coincides with the one calculated in the Collins-Soper (CS-) frame. ${ }^{26}$ The $\Delta A_{4}$ in the helicity frame differs somewhat from the one in the GJ-frame, taking smaller absolute values.
4. The asymmetries for the other coefficients $\Delta A_{i}(i=0-3)$ appear to be rather small in all the three (helicity, GJ-, and CS-) reference frames.
5. Although we have ignored the sea-quark polarization, it can be shown that these effects are rather small. ${ }^{27}$ This is not the case for the effects of gluon radiation which are important ${ }^{27}$, but which were not considered here for sake of simplicity.
6. When the beam energy increases the polarization effects seem to decrease. Existing calculations also indicate such tendency. ${ }^{7}$ which was also observe in the case of $W$ production. ${ }^{27}$ This fact suggests that polarized beam experiments at uitra high energies, say, at $\sqrt{s}=100 \mathrm{TeV}$ are not very encouraging.

## 5. Conclusion

As one can see from the figures presented in the previous Section the measurements of polarization asymmetries of the coefficients in the angular distribution using the polarized proton beams, which would constitute a "complete" experiment, would provide us with a variety of detailed information about different underlying electroweak gauge models, their couplings and thereby would allow to distinguish and verify such models. In particular the sign of the asymmetries is related to the structure of the underlying gauge theory. Besides, the polarized beam reactions could shed light on the production mechanism, such as reconfirmation of the vector nature of a gluon, and the spin distributions of the partons inside hadrons as well.

We conclude this paper by stressing that experimentation with the highenergy polarized proton beams with a sufficiently high luminosity accessible at the CERN $\bar{p} p$ collider and the Fermilab Tevatron would provide a powerful tool of investigation, complementing the ones obtainable in the unpolarized experiments, and might exploit new rich realm of "spin" physics.

## ACKNOWLEDGEMENTS

Two of the authors (M. H. and K. Y.) would like to thank Professor S. D. Drell and the other members of the Theory Group for their warm hospitality at SLAC. We also thank H. Aoyama for useful help in preparing the manuscript. This work was supported by the U.S. Department of High Energy under contract number DE-AC03-76SF00515.

## REFERENCES

1. S. Weinberg, Phys. Rev. Lett. 19 (1967) 1264;
A. Salam, Proc. of the 8-th Nobel Symposium, edited by N. Svartholm (Almqvist and Wiksell, Stockholm 1968) p.36;
S.L. Glashow, Nucl. Phys. 22 (1961) 579.
2. G. Arnison et al.(UA1 collaboration), Phys. Lett. $\operatorname{B122}$ (1983) 103;
M. Banner et al. (UA2 collaboration), Phys. Lett. B122 (1983) 476;
G. Arnison et al. (UA1 collaboration), Phys. Lett. B126 (1983) 398;
M. Banner et al. (UA2 collaboration), Phys. Lett. B129 (1983) 130.
3. V. Barger, E.Ma, and K.Whisnant, Phys. Rev. D28 (1983) 1618 and references quoted therein.
4. H. Georgi, in Particle and Fields-1974, edited by C. E. Carlson, AIP Conference Proceedings No. 23 (American Institute of Physics, New York, 1975);
H. Fritzsch and P. Minkowski, Ann. Phys. (N.Y.) 93 (1975) 193.
5. H. S. Mani and S.D. Rindani, Phys. Lett. 84B (1979) 104.
6. F. E. Paige, T. L. Trueman, and T.N.Tudron, Phys. Rev. D19 (1979) 935;
F. E. Paige; Proc. Topical Workshop on Production of New Particles in Super-High Energy Collisions, edited by V. Barger and F. Halzen, University of Wisconsin, Madison, 1979.
7. R. Kinnunen and J. Lindfors, Nucl. Phys. B189 (1981) 63;
J. Lindfors; AIP Conference Proceedings 95 (1983) 259 (Editor G. Bunce).
8. K. Hidaka, Nucl. Phys. B192 (1981) 369.
9. J. Soffer: Proc. of the SPS Fixed Target Workshop held at CERN (1982); CERN Yellow Report 83-02 Vol. II p. 392 (Editor I. Mannelli);

See also, N. S. Craigie, K. Hidaka, M. Jacob, and F.M. Renard, Phys. Rep. 99 (1983) 69.
10. H. E. Haber and G. L. Kane, Nucl. Phys. B146 (1978) 109; F. E. Paige et al., in Ref.5.
11. For the calculation based on the standard model, see M. Hayashi, S. Homma, and K. Katsuura, J. Phys. Soc. Jpn. 50 (1981) 1427;
J. Finjord, G. Girardi, M. Perrottet, and P. Sorba, Nucl. Phys. $B 182$ (1981) 427;
P. Aurenche and J. Lindfors, Nucl. Phys. B185 (1981) 301;
I. H. Dumbar and N. Dombey, Phys. Lett. 101B (1981) 197;
D. J. E. Callaway, Ann. Phys.(N.Y.) 144 (1982) 282.

See also Ref. 13.
12. T.G. Rizzo, Phys. Rev. $D 27$ (1983) 1075.
13. G. Girardi, P. Mery, and P. Sorba, Z. Phys. C10 (1981) 363.
14. M. Chaichian, M. Hayashi, and K. Yamagishi, Phys. Rev. D25 (1982) 130, ibid. D26 (1982), 2534 (E).
15. N.S. Craigie,T.Niinikoski, A. Penzo, L. Van Rossum, R. D. Ruth L. Sivers, and J. Soffer, Saclay Report, D. Ph. PE 83-01 (1983).
16. M. Chaichian, O. Dumbrajs, and M. Hayashi, Phys. Rev. D20 (1979) 2873;
F. Halzen and D. M. Scott, Phys. Lett. 78B (1978) 318;
J. Finjord et al., in Ref. 10;
P. Aureche and J. Lindfors, Nucl. Phys. $B 185$ (1981) 274.
17. M. Chaichian, M. Hayashi, and K. Yamagishi, Trieste preprint IC/83/33 (1983).
18. K. Hagiwara, K. Hikasa, and N. Kai, Phys. Rev. Lett. 52 (1984) 1076.
19. N. Arteaga-Romero, A. Nicolaidis and J. Silva, Phys. Rev. Lett. 52 (1984) 172.
20. R. Carlitz and J. Kaur, Phys. Rev. Lett. 38 (1977) 673, ibid. 38 (1977) 1102 (E); J. Kaur, Nucl. Phys. B128 (1977) 219.
21. F. Close and D. Sivers, Phys. Rev. Lett. 39 (1977) 1116. See also J. Ralston and D. Soper, Nucl. Phys. $B 152$ (1979) 109.
22. G. Altarelli and G. Parisi, Nucl. Phys. B126 (1977) 298.
23. For a more complete analysis of scaling violation of the spin dependent structure function, see P. Chiappetta and J. Soffer, Preprint CPT-84/p. 1615, to appear in Phys. Rev. D.
24. M. Glūck, E. Hoffmann, and E. Reya, Z. Phys. C13 (1982) 119.
25. P. Aurenche and J. Lindfors in Ref. 10.
26. J.C. Collins and D. E. Soper, Phys. Rev. D16 (1977) 2219.
27. P. Chiappetta and J. Soffer, Preprint CPT-84/p.1650, to appear in Phys. Lett. B.

## Figure Captions

1. (a) The quark-antiquark annihilation diagrams.
(b) The quark-gluon Compton diagrams.
2. The differential cross-section $d \sigma / d M d Q_{T}$ vs $M$ for unpolarized $\bar{p} p$-collision at $\sqrt{s}=540 \mathrm{GeV}$ and $Q_{T}=5 \mathrm{GeV}$. The dashed (solid) curve corresponds to the standard (left-right) model.
3. The differential cross-section $d \sigma / d M d Q_{T}$ vs $Q_{T}$, calculated in the left-right model, for unpolarized $\bar{p} p$-collision at $\sqrt{s}=540 \mathrm{GeV}, M=M_{Z_{1}}=93 \mathrm{GeV}$ and $M=M_{Z_{2}}=200 \mathrm{GeV}$. The curve shown for $M=M_{Z_{2}}=200 \mathrm{GeV}$ is multiplied by $10^{2}$ to the actual values.
4. The differential cross-section $d \sigma / d M$ vs $M$ for unpolarized $\bar{p} p$-collision at $\sqrt{s}=540 \mathrm{GeV}$, calculated within the framework of the Drell-Yan model assuming the left-right model.
5. The asymmetry, $\{d \sigma(-)-d \sigma(+)\} /\{d \sigma(-)+d \sigma(+)\}$ vs $M$ for $\bar{p} p_{h}$-collision at $\sqrt{s}=540 \mathrm{GeV}$ and $Q_{T}=5 \mathrm{GeV}$, where $d \sigma( \pm)=d \sigma( \pm) / d M d Q_{T}$. The dashed (solid) curve corresponds to the one calculated within the framework of the standard (left-right) model.
6. The asymmetry, $\{d \sigma(-)-d \sigma(+)\} /\{d \sigma(-)+d \sigma(+)\}$ vs $M$ for $\bar{p} p_{h}$-collision at $\sqrt{s}=540 \mathrm{GeV}$, where $d \sigma( \pm)=\int_{2}^{12} d Q_{T} d \sigma( \pm) / d M d Q_{T}$. The dashed (solid) curve is the prediction by the standard (left-right) model.
7. The asymmetry of the coefficient $\Delta A_{4}$ vs $M$ for $\bar{p} p_{h}$-collision at $\sqrt{s}=540$ GeV and $Q_{T}=5 \mathrm{GeV}$, calculated in the GJ-frame. The dashed (solid) curve is the prediction by the standard (left-right) model.
8. The asymmetry of the coefficient $\Delta A_{4}$, integrated over $Q_{T}$ in the range
$2 \leq Q_{T} \leq 12 \mathrm{GeV}$, for $\rho p_{h}$-collision at $\sqrt{s}=540 \mathrm{GeV}$, shown as a function of $M$ in the GJ-frame. The dashed (solid) curve is the prediction by the standard (left-right) model.
9. The asymmetry of the coefficient $\Delta A_{4}$ vs $Q_{T}$ for $\bar{p} p_{h}$-collision at $\sqrt{s}=540$ $\mathrm{GeV}, M=M_{Z_{1}}=93 \mathrm{GeV}$ and $M=M_{Z_{2}}=200 \mathrm{GeV}$, calculated in the GJ-frame using the left-right model.
10. The differential cross-section $d \sigma / d M d Q_{T}$ vs $M$ for unpolarized $p p$-collision at $\sqrt{s}=2 \mathrm{TeV}$ and $Q_{T}=5 \mathrm{GeV}$. The dashed (solid) curve is the prediction by the standard (left-right) model.
11. The differential cross-section $d \sigma / d M d Q_{T}$ vs $Q_{T}$, for unpolarized $p p$ collision at $\sqrt{s}=2 \mathrm{TeV}, M=M_{Z_{1}}=93 \mathrm{GeV}$ and $M=M_{Z_{2}}=200$ GeV , calculated in the left-right model.
12. $\int_{2}^{12} d Q_{T} d \sigma / d M d Q_{T}$ as a function of $M$, calculated within the framework of the left-right model, for unpolarized pp-collision.
13. The asymmetry, $\{d \sigma(--)-d \sigma(++)\} /\{d \sigma(--)+d \sigma(++)\}$ vs $M$ for doubly polarized $p_{h} p_{h}$-collision at $\sqrt{s}=2 \mathrm{TeV}$, calculated within the framework of both the standard (dashed curve) and the left-right (solid curve) models, where $d \sigma( \pm \pm)=\int_{2}^{12} d Q_{T} d \sigma( \pm \pm) / d M d Q_{T}$.


Fig. 1


Fig. 2


Fig. 3


Fig. 4


Fig. 5


Fig. 6


Fig. 7


Fig. 8


Fig. 9


Fig. 10


Fig. 11


Fig. 12


Fig. 13


[^0]:    * Work supported by the Department of Energy, contract DE-AC03-76SF00515.
    $\dagger$ Permanent address: Department of Physics, Saitama Medical College, Saitama 350-04, Japan.
    * Permanent address: Department of Physics, Tokuyama University, Yamaguchi 745, Japan.

