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GAUGE BOSON MASSES AND MIXINGS IN LEFT-RIGHT SYMMETRIC MODELS*

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ABSTRACT

We study $SU(2)_L \times SU(2)_R \times U(1)_{B-L}$ gauge models with a completely general Higgs sector. The scalars which are consistent with the known low-energy phenomenology are determined. The results are used to obtain useful constraints on the $W_L - W_R$ mixing angle, ξ . In particular, we derive the stringent upper limit $\xi \leq 0.002$.

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The standard $SU(2)_L \times U(1)$ gauge model¹ can accomodate all the present electroweak data. The recent discovery² of the weak gauge bosons at CERN, with average masses³ $M_W = 80.9 \pm 2.0$ GeV and $M_Z = 93.0 \pm 2.0$ GeV, confirm the validity of the standard model at low energies. Theses masses, in conjunction with the extrapolated and corrected value of the weak mixing angle,⁴⁻⁶ $sin^2 \theta^{W,Z} = 0.217 \pm 0.014$, and with the definition

$$\rho \equiv \frac{M_W^2}{M_Z^2 \cos^2 \theta^{W,Z}} \tag{1}$$

yield $\rho = 0.97 \pm 0.07$. Similarly, the preliminary CDHS results⁷ lead to $\rho = 0.99 \pm 0.07$. This is consistent with the measurements of the neutral current strength,⁴ and is to be compared to the prediction $\rho = 1$, obtained in the standard theory when the Higgs fields are doublets of the $SU(2)_L$ group. In constrast, Higgs with higher weak isospin give $\rho \neq 1.^8$ Excluding unnatural cancellations, the dominance of Higgs doublets in the $SU(2)_L \times U(1) \rightarrow U(1)_{e.m.}$ breaking is strongly favoured by experiment.

The standard model, however, has many open theoretical questions. Some of them can be understood by going to enlarged theories. An appealing extension of the standard model is the $SU(2)_L \times SU(2)_R \times U(1)_{B-L}$ gauge theory,⁹⁻¹³ which represents the minimal incorporation of left-right symmetry at high energies. In this model, the spontaneous breaking of parity symmetry provides a deeper understanding⁹ of the V-A weak structure observed at low energies. In addition, the scale of parity restoration can be related to the neutrino mass,¹⁰ as well as to the magnitude of some CP-violation effects.¹¹ Furthermore, the $SU(2)_L \times SU(2)_R \times U(1)$ model could be an effective stage in the breaking of some grand unification groups.¹² These attractive features motivate a great deal of interest in these theories¹³ and make worthwhile serious experimental and theoretical efforts to constrain left-right symmetric models as much as possible. In the spectrum of these models one has elementary Higgs fields, which spontaneously generate fermion and gauge boson masses. Usually, one chooses the minimal Higgs sector which makes the low energy limit of the model consistent with experiment.^{10,13} Although this choice can be justified from the point of view of simplicity, it certainly represents one of the arbitrary features of the theory. Indeed, an enlarged scalar spectrum might also be consistent with the available experimental data. Obviously, these data constrain the symmetry properties of the Higgs fields and the pattern of symmetry breaking. The main purpose of the present note is to study systematically these constraints.

Let us introduce a generic set of Higgs fields, $\varphi_{\alpha} \sim (I_L, I_R, Y)$, where $I_L(I_R)$ is the left (right) weak isospin and Y = B - L is the hypercharge. The α -index denotes the I_L, I_R, Y quantum numbers and, eventually, distinguishes Higgs fields with the same symmetry properties. Gauge boson masses arise from the Lagrangian term

$$\mathcal{L} = \sum_{\alpha} Tr \left(D^{\mu} \varphi_{\alpha} \right)^{\dagger} \left(D_{\mu} \varphi_{\alpha} \right) ,$$
$$D^{\mu} \varphi_{\alpha} = \partial^{\mu} \varphi_{\alpha} - ig \vec{W}_{L}^{\mu} \cdot \vec{L} \varphi_{\alpha}$$
$$- ig \varphi_{\alpha} \vec{R} \cdot \vec{W}_{R}^{\mu} - i(g'/2) Y \varphi_{\alpha} B^{\mu}$$

In the covariant derivative, \vec{L} and \vec{R} are the matrix representations according to which the Higgs transform under $SU(2)_L$ and $SU(2)_R$ gauge rotations, respectively. Denoting by $\mu^2(A-A')$ the gauge boson mass term associated with $A^{\dagger}_{\mu} A'^{\mu}$, the elements of the 5×5 mass matrix read

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$$\mu^{2}(W_{L}^{i} - W_{L}^{i}) = g^{2}\ell_{i}$$

$$\mu^{2}(W_{R}^{i} - W_{R}^{i}) = g^{2}r_{i}$$

$$\mu^{2}(W_{L}^{i} - W_{R}^{j}) = g^{2}m_{ij}$$

$$\mu^{2}(B - B) = g^{\prime}(\ell_{3} + r_{3} + 2m_{33})$$

$$\mu^{2}(W_{L}^{3} - B) = -gg^{\prime}(\ell_{3} + m_{33})$$

$$\mu^{2}(W_{R}^{3} - B) = -gg^{\prime}(r_{3} + m_{33})$$
(2a)

with i = 1, 2, 3, and

$$m_{ij} = \sum_{\alpha} Tr \langle R_j \varphi_{\alpha}^{\dagger} L_i \varphi_{\alpha} \rangle$$
$$\ell_i = \sum_{\alpha} Tr \langle (L_i)^2 \varphi_{\alpha} \varphi_{\alpha}^{\dagger} \rangle$$
$$r_i = \sum_{\alpha} Tr \langle (R_i)^2 \varphi_{\alpha}^{\dagger} \varphi_{\alpha} \rangle$$
(2b)

In these results, the brackets indicate that the vacuum expectation value of the Higgs fields has been taken. We have used $\langle Q\varphi\rangle = 0$, where the charge operator Q is the usual combination of gauge generators, namely, $Q = T_{3L} + T_{3R} + T_Y/2$.

The structure of the mass matrix reveals that, to suppress right-handed currents and left-right mixings at low energies, parity must be broken by left-handed singlets, $\Delta_{\beta}^{R} \sim (0, I, Y \neq 0)$, acquiring vacuum expectation values much higher than the W_{L} mass scale, i.e.,

$$\frac{\sum_{\alpha} Tr \langle \chi_{\alpha} \chi_{\alpha}^{\dagger} \rangle}{\sum_{\beta} \langle \Delta_{\beta}^{R} (\Delta_{\beta}^{R})^{\dagger} \rangle} = 0(\eta) \ll 1 \quad . \tag{3}$$

Here, $\eta = M_{W_L}^2/M_{W_R}^2$ and the χ_{α} are scalars with $I_L \neq 0$, inducing the standard $SU(2)_L \times U(1) \rightarrow U(1)_{e.m.}$ transition. In the limit $\eta \ll 1$, the neutral eigenstates of

the mass matrix are

$$\begin{split} Z_L^{\mu} &= \cos\theta \, W_L^{3\mu} - \sin\theta \, tg \, \theta \, W_R^{3\mu} - \sigma \, tg \, \theta \, B^{\mu} \\ Z_R^{\mu} &= (\sigma/\cos\theta) \, W_R^{3\mu} - tg \, \theta \, B^{\mu} \\ A^{\mu} &= \sin\theta \, (W_L^3 + W_R^3)^{\mu} + \sigma \, B^{\mu} \quad , \end{split}$$

where $\sin^2\theta = {g'}^2/(g^2 + 2{g'}^2)$, $\sigma^2 = \cos 2\theta$ and A^{μ} is the photon field. Now, the current associated with the neutral Z_L boson is

$$J_{\mu} = (g/\cos\theta) \left(J_{L\mu}^3 - \sin^2\theta \ J_{\mu}^{e.m.}\right) \quad . \tag{4}$$

By identifying θ with the standard weak angle, Eq. (4) is just the successful standard neutral current. In other words, $SU(2)_L \times SU(2)_R \times U(1)$ models with a general scalar spectrum, implemented with the hierarchy given by Eq. (3) and with $\theta = \theta_W$, have a low energy neutral current phenomenology in agreement with experiment. The reason is that, for $\eta \ll 1$, the eigenstates of the mass matrix are independent of the details of the Higgs sector. However, the mass eigenvalues depend on the ℓ , r and mparameters. Indeed, the right-handed boson masses carry relevant information on the isospin of the Δ^R scalars. More interesting for our purposes is the left-handed boson sector. Calculating the masses and introducing them in Eq. (1) yields

$$\rho = \frac{Tr \sum_{\alpha} (\tilde{L})^2 \langle \chi_{\alpha} \chi_{\alpha}^{\dagger} \rangle}{2 Tr \sum_{\alpha} (L_3)^2 \langle \chi_{\alpha} \chi_{\alpha}^{\dagger} \rangle} \quad , \tag{5}$$

where $(\tilde{L})^2 \equiv (\tilde{L})^2 - (L^3)^2$. Barring unnatural cancellations, $\rho = 1$ is obtained only with $I_L = 1/2$ Higgs fields. The experimental value of ρ indicates that the spontaneous $SU(2)_L \times U(1)$ breaking in left-right symmetric theories is strongly dominated by $\chi_{\alpha} \sim$ $(1/2, I_R, Y)$ fields. This result is easy to understand, since that breaking is essentially controlled by the I_L isospin of χ_{α} . We remark that present data still have room for the small effects of order η which have been neglected in Eqs. (4) and (5). Let us address now to some considerations which will shed more light on the restrictions on the scalar sector. In left-right symmetric models, the scalar potential is invariant under the transformation $\varphi_{\alpha} \leftrightarrow \overline{\varphi}_{\alpha}$, where $\overline{\varphi}_{\alpha} \sim (I_R, I_L, Y)$ is the parity conjugate field of $\varphi_{\alpha} \sim (I_L, I_R, Y)$. Consider the $\Delta_{\beta}^L \equiv (\overline{\Delta}_{\beta}^R) \sim (I, 0, Y)$, with $I \neq 1/2$, and the $\chi_{\alpha} \sim (1/2, I_R, Y)$ fields. From Eq. (3) and the fact Δ^L scalars induce $\rho \neq 1$, it follows the hierarchy

$$\langle (\Delta^L_\beta)^{\dagger} \ \Delta^L_\beta \rangle \ \ll \ v_R^2$$

where $v_R^2 = \sum_{\gamma} \langle \Delta_{\gamma}^R (\Delta_{\gamma}^R)^{\dagger} \rangle$. This parity-breaking configuration minimizes the potential.^{10,13} Let us evaluate the order of magnitude of the $\bar{\chi}_{\alpha} \sim (I_R, 1/2, Y)$ vacuum expectation values in this configuration. For reasons that will shortly become clear, we first discuss the $I_R \neq 0$ case. We exclude the uninteresting fields that do not contribute appreciably to the sum in Eq. (5) and approximate $Tr \langle \chi_{\alpha} \chi_{\alpha}^{\dagger} \rangle \simeq k^2$ and $Tr \langle \bar{\chi}_{\alpha} \bar{\chi}_{\alpha}^{\dagger} \rangle \simeq \bar{k}^2$. For our purpose, the relevant part of the potential is given approximately by

$$V \simeq (-\mu^2 + \lambda_1 v_R^2) (k^2 + \bar{k}^2) + \lambda_2 v_R^2 k \, \bar{k}$$

+ $\lambda_3 (k^4 + \bar{k}^4) + \lambda_4 \, k^2 \, \bar{k}^2$,

where the λ_i are linear combinations of Yukawa couplings. The conditions for the minimum imply either $\bar{k} \simeq k$ or

$$\bar{k} \simeq rac{\lambda_2}{2(2\lambda_3 - \lambda_4)} rac{v_R^2}{k}$$
 (6)

Provided the λ_i are not unnaturally large or small, Eq. (6) yields $\bar{k} \gg v_R$. Now, the $\rho = 1$ requirement for the $\bar{\chi}_{\alpha}$ field is inconsistent with both solutions, unless $\chi_{\alpha} \sim (1/2, 1/2, Y)$. Indeed, $I_R \neq 1/2$ requires $\bar{k} \ll k$, which is far from being satisfied at the minimum of the potential. We notice that the argument is not valid if χ_{α} has $I_R = 0$, for then $\bar{\chi}_{\alpha}$ is a Δ^R -type scalar.

We conclude that the present low energy data strongly restricts the Higgs sector in $SU(2)_L \times SU(2)_R \times U(1)_{B-L}$ models. The Higgs spectrum which acquires relevant vacuum expectation values and leads to the correct low energy phenomenology is composed of: (i) $SU(2)_R \times U(1)_{B-L}$ -breaking $\Delta_{\beta}^R \sim (O, I, Y)$ fields and (ii) $SU(2)_L \times U(1)$ breaking $\chi_{\alpha} \sim (1/2, 1/2, Y = 0, \pm 2)$ and $\chi_{\alpha} \sim (1/2, 0, Y = \pm 1)$ fields; the former, when Y = 0, also generates charged fermion masses. The $\Delta_{\beta}^L \sim (I, O, Y,)$, $I \neq 1/2$, scalars do not generate substantial gauge boson masses. For completeness, we recall that the minimal Higgs sector used in the literature¹³ corresponds to the three scalars $\Delta^R = \bar{\Delta}^L \sim (0, 1, 2)$ and $\chi \sim (1/2, 1/2, 0)$.

We can now deduce a useful constraint on the $W_L^{\pm} - W_R^{\pm}$ mixing angle, ξ , which is induced by the (charged) non-diagonal term in Eq. (2). Among our restricted Higgs fields, only the $\chi_{\alpha} \sim (1/2, 1/2, Y)$ type may connect W_L^{\pm} with W_R^{\pm} . These scalars fulfill-

$$\sum_{\alpha} Tr \langle (\tau_1)^2 \chi_{\alpha} \chi_{\alpha}^{\dagger} \rangle \geq \left| \sum_{\alpha} Tr \langle \tau_- \chi_{\alpha}^{\dagger} \tau_+ \chi_{\alpha} \rangle \right|$$

where τ_i are the Pauli matrices and $\tau_{\pm} = (\tau_1 \pm i\tau_2)/\sqrt{2}$. This tells us that the mass matrix elements induced by χ_{α} obey $\mu^2 (W_L^{\pm} - W_L^{\pm}) \geq |\mu^2 (W_L^{\pm} - W_R^{\pm})|$. The other Higgs representations will certainly contribute to the W_L -mass generation. It follows that the mixing angle is bounded by

$$|\xi| \simeq \frac{|\mu^2 (W_L^{\pm} - W_R^{\pm})|}{M_{W_R}^2} \le \eta \quad . \tag{7}$$

This bound was noticed¹⁴ in the context of the minimal Higgs sector. Now, we claim that Eq. (7) constitutes a completely general constraint (arising in fact from low-energy requirements) involving two of the fundamental parameters of left-right symmetric theories.

We finally consider some phenomenological implications of Eq. (7). To reach our bound we have made no assumptions about the U_R mixing matrix appearing in the charged right-handed current. However, the usual analyses¹⁵ essentially assume either $U_R = U_L$ or $U_R = U_L^*$, with U_L being the left-handed mixing matrix. Let us quote the most stringent published bounds on ξ and η . On the one hand, non-leptonic $\Delta S = 1$ decays yield¹⁶ $|\xi| \leq 4 \times 10^{-3}$. This limit, unfortunately, is subject to the theoretical uncertainties associated with non-leptonic processes. The safer semi-leptonic decays and the bottom lifetime measurements have been recently used¹⁷ to reach $|\xi| \leq 5.5 \times 10^{-3}$, obtained if one includes a 5% fractional theoretical error in $(U_L)_{us}$ due to SU(3) symmetry breaking and radiative corrections when analyzing semi leptonic hyperon and K_{e3} decays.¹⁸ A 10% error leads to $|\xi| \leq 8 \times 10^{-3}$. On the other hand, the analyses^{14,19} of the $K^{\circ} - \bar{K}^{\circ}$ transition yield $\eta \leq 1/430$. This bound has been confirmed by a variety of hadronic models²⁰ and eventual cancellations with neutral Higgs mediated transitions are ruled out.²¹ Since QCD corrections²² reduce the quoted limit by at least a factor 3, $\eta \leq 1/430$ has to be considered as a conservative bound. Using this value in Eq. (7) we obtain

$$|\xi| \leq 2.3 \times 10^{-3}$$
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which represents the most stringent constraint now available. The introduction of QCD effects would yield $|\xi| \leq 8 \times 10^{-4}$.

If left-right symmetry is present at high energies, a careful analysis of weak low energy transitions could in the near future detect the presence of the mixing between left and right-handed currents. An eventual determination of a non-vanishing ξ would reveal, through Eq. (7), the range of energies where parity should be restored. There is already a claim²³ of a significant departure of ξ from zero. Unfortunately, the analysis is rather model dependent and we cannot infer with confidence a lower bound on η . Discussions with J. Bagger, F. Gilman, H. Reno and G. Senjanović are gratefully acknowledged. I would like to thank the Fulbright/Spanish M.E.C. Commission for financial support.

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