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HADRON PRODUCTION BY e⁺e⁻ ANNIHILATION AT CENTER-OF-MASS ENERGIES BETWEEN 2.6 AND 7.8 GeV PART II. JET STRUCTURE AND RELATED INCLUSIVE DISTRIBUTIONS*

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ABSTRACT

We present results on the jet structure observed in multihadronic events produced by e^+e^- annihilation in the Mark I magnetic detector at SPEAR. The evidence for jet structure and the jet axis angular distribution are reported. We give inclusive distributions of the hadrons in Feynman x, rapidity, and transverse momentum relative to the jet axis.

I. INTRODUCTION

In the preceding paper¹ (hereafter referred to as I) we presented results on the total cross section and inclusive momentum distributions for multihadronic events produced by e^+e^- annihilation in the center-ofmass energy ($E_{c.m.}$) range from 2.6 to 7.8 GeV from the Mark I magnetic detector at SPEAR. In this paper we present results on the jet structure observed in these events.

In e^+e^- collisions the electron and positron predominantly annihilate to form a single virtual photon which subsequently produces a leptonantilepton pair (e.g., $\tau^+\tau^-$), or a quark-antiquark pair which converts into hadrons. At sufficiently high energy the multihadronic events produced by e e annihilation are expected to form two back-to-back jets due to the limiting of transverse momentum along the original quark direction.²⁻⁵ The spins of the quarks can be determined from the jet axis angular distribution. Evidence for such jet structure was first observed at SPEAR for $E_{c.m.}$ of 4.8 GeV and greater.⁶ If the jet structure is due to quark jets, then it is of interest to study inclusive distributions of hadrons relative to the jet direction in order to obtain information about the fragmentation of quarks into hadrons. In this paper we present hadron inclusive distributions in Feynman x, rapidity, and transverse momentum relative to the jet direction in multihadronic events from e^+e^- annihilation in the E range from 3.0 to 7.8 GeV.

As in I we limit ourselves to data away from the ψ resonances⁷ and restrict ourselves even further to data away from the charm threshold region.⁸ The apparatus, trigger criteria, general analysis procedures, hadronic event selection, luminosity measurement, and general

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Monte Carlo calculation of detector efficiency are described in I. We shall give a complete report on the jet structure analysis. The evidence for jet structure is presented in Section II. Section III describes the measurement of the jet axis angular distribution. The determination of inclusive distributions in variables relative to the jet direction is the subject of Section IV.

II. EVIDENCE FOR JET STRUCTURE

One of the most definitive predictions of quark-parton constituent models of elementary particles is that the hadrons produced in e^+e^- annihilation should form back-to-back jets.²⁻⁵ The e^+ and e^- annihilate to form a single virtual photon which produces a quark-antiquark pair, each of which fragments to hadrons, as shown in Fig. 1. The jet structure arises from the limiting of transverse momentum of the hadrons relative to the original parton direction and should become apparent at energies high enough that the total momentum of the hadrons is large compared with the fundamental transverse momentum limitation. The original quark-pair angular distribution is expected to be the same as for any pair of spin-1/2 particles: $1 + \cos^2\theta$, where θ is the polar angle relative to the e^+ beam direction.

In searching for jet structure in multihadronic events produced in e⁺e⁻ annihilation, one is faced with two fundamental problems:

- If there is a direction relative to which transverse momentum is limited, what is that direction for a particular event?
- 2. If the transverse momentum is indeed limited, what is the measure of that limitation?

In addition, there are problems caused by detection inefficiencies. Charged particles were measured over only 65% of 4π sr in the Mark I

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detector, described in I. Neutral particles were detected with significantly worse efficiency and resolution than charged particles and were not used in this analysis. Multihadronic events were almost never fully reconstructed.

The procedure⁹ which was used^{6,10} to solve these problems will now be described. First, we find the direction which minimizes the sum of squares of transverse momenta for each event. To do this, we diagonalize the tensor

$$T^{\alpha\beta} = \sum_{i} \left(\delta^{\alpha\beta} \vec{p}_{i}^{2} - p_{i}^{\alpha} p_{i}^{\beta} \right) , \qquad (2.1)$$

where the summation is over all detected charged particles and α and β refer to the spatial components of each particle momentum \vec{p}_i . Since $T^{\alpha\beta}$ is like a moment of inertia tensor, we are finding principal moments in momentum space. We obtain the eigenvalues λ_1 , λ_2 , and λ_3 which are the sums of squares of transverse momenta with respect to the three eigenvector directions. The smallest eigenvalue λ_3 is the minimum sum of squares of transverse momenta, and the eigenvector direction associated with it is the reconstructed jet axis. This method of calculating the jet axis is not perfect. It is impossible to determine the jet axis exactly, even with perfect detection, unless one knows precisely which particle comes from which jet, in which case one could simply find the resultant momenta of two groups of particles. Using Monte Carlo simulations of the detector and jet models in which the true jet axis was known for each event, we have studied other methods for finding the jet axis, such as maximizing the sum of the absolute values of the longitudinal momenta, and have found that the method described above is the best approximation of which

we are aware. The median angle between the true jet axis and the reconstructed jet axis for hadronic events with three or more prongs in the Mark I detector at 7.3 GeV was estimated to be 24°. The method also has the advantage that it is a well-defined mathematical procedure which can be applied to any detected event or to events generated by any Monte Carlo model and which does not use large amounts of computer time.

A jet axis can be determined for any event regardless of whether it is jet-like. Once the jet axis is determined, we obtain a quantitative measure of how jet-like an event is from the sphericity (S):

$$S = \frac{3\lambda_{3}}{\lambda_{1} + \lambda_{2} + \lambda_{3}} = \frac{3\left(\sum_{i} p_{\perp i}^{2}\right)_{\min}}{2\sum_{i} \vec{p}_{i}^{2}} \qquad (2.2)$$

The sphericity is the ratio of the minimum sum of squares of transverse momenta normalized to the sum of squares of total momenta. The sphericity approaches 0 for events with limited transverse momentum (jet-like events) and approaches 1 for events with large multiplicity and isotropic particle distributions.

Monte Carlo simulations were used to determine how jet-like hadronic events differ from isotropic hadronic events in the detector. The detector was simulated as described in I. Events were generated according to Lorentz-invariant phase space or a limited transverse momentum jet model¹¹ in which phase space was modified by a matrix element squared of the form

$$M^{2} = e^{-\left(\sum_{i} p_{\perp i}^{2}\right)/2b^{2}}, \qquad (2.3)$$

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where $p'_{\perp i}$ is the momentum perpendicular to the jet axis for the ith particle and b is a parameter chosen to fit the data. The sum is over all produced particles. The assumed jet axis angular distribution was of the form

$$\frac{\mathrm{d}\sigma}{\mathrm{d}\Omega} \propto 1 + \alpha \, \cos^2\theta \quad . \tag{2.4}$$

We used $\alpha = 1$ in agreement with the measurement of the jet axis angular distribution which is described in detail in Section III. Generated events has only pions with the charged and neutral multiplicities given by separate Poisson distributions as in I. Initial-state radiation was included in the production of the events. Some specific checks were performed using models which included production of etas, kaons, and nucleons.

Multihadronic events were selected as described in I. For this analysis we used only those events with three or more observed tracks in order to reduce the contamination from beam-gas interactions, two-photon processes, and $\tau^+\tau^-$ production. Additional cuts were applied as in I to remove multiprong events originating from QED processes (mainly Bhabha scattering events containing a delta ray or converted photon). These cuts are particularly important for the jet analysis because they selectively reduce background in events containing a track with momentum near the beam energy; these events are relatively rare in multihadronic processes. Contamination of this event sample is estimated to range from 1% for E = 3 GeV to 4% for E > 7 GeV from beam-gas interactions, to be <2% from two-photon processes, and to be $\leq 7\%$ from $\tau^+ \tau^$ production. We used the large blocks of data collected at $E_{c.m.}$ of 3.0, 4.8, 6.2, and 7.4 GeV, which consisted of 1100, 7300, 6800, and 14500 multihadronic events, respectively, after cuts. From I we recall that 3.0 GeV is below the threshold for production of charmed quarks and the other energies are above.

The data at each energy were compared with Monte Carlo simulations based on either the phase-space model or the jet model. At each energy the total multiplicity and ratio of charged pions to neutral pions for both models were obtained by fitting to the observed charged particle mean momentum and mean multiplicity. The parameter b in Eq. (2.3) was chosen by fitting to the observed mean p_{\perp} with respect to the observed jet axis. The observed distribution of p_{\perp} at 7.4 GeV is shown in Fig. 2 along with the predictions of the two models. The jet model reproduces the data rather well whereas phase space predicts too many particles at high p_{\perp} . The mean produced p_{\perp} in the jet model was found to be in the range 325 to 360 MeV/c with no particular energy dependence. From hadron interaction data we would have expected the mean p_{\perp} to be in the range 300 to 350 MeV/c.

The observed sphericity distributions were compared with the predictions of the two models. Figure 3 shows the observed S distributions for the lowest energy, 3.0 GeV, and for the two highest energies, 6.2 and 7.4 GeV. At 3.0 GeV the data agree with the predictions of either the phase-space model or the jet model. At this energy the limiting of transverse momentum to an average of 350 MeV/c has no effect on the phase-space particle distributions as manifested in the S distribution since the predictions of the two models are the same. At 6.2 and 7.4 GeV the S distributions are peaked toward low S favoring the jet model over the phase-space model. At the highest energies the two larger eigenvalues λ_1 and λ_2 are nearly equal.

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Figure 4 shows the observed S distribution at 7.4 GeV compared with the predictions of both a jet model and a phase-space model in which kaons and etas were produced along with pions. Etas and π° 's were produced with equal probability before phase-space effects, and kaon fractions were fitted to agree with the data.¹²

The agreement of the observed sphericity distributions with the jet model as opposed to the phase-space model is evidence for jet structure in e^+e^- hadron production. Differences in the detailed shape of the S distributions between the data and the jet model can be caused by differences in the shape of the multiplicity distributions (see Fig. 15 in I) and interparticle correlations caused by decaying resonances and particles.

The difference between the jet model and phase-space model predictions for sphericity as a function of energy can be seen quantitatively in Fig. 5 which shows the observed mean S versus $E_{c.m.}$. The phase-space model predicts that the mean S should increase as $E_{c.m.}$ increases whereas the jet model predicts that the mean S should decrease. The data clearly show a decreasing mean S with increasing $E_{c.m.}$ consistent with the jet model.

The evidence for jet structure is corroborated by the distributions of the cosine of the angle between any pair of particles, shown in Fig. 6. At 6.2 and 7.4 GeV the data show more pairs of particles at small angles to each other and at angles near 180° to each other than the phase-space model predicts. The distributions agree well with the jet model.

Further corroboration for the jet model can be found in the observed single particle inclusive x distribution presented in Fig. 7 for events

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at 7.4 GeV. (x is the scaling variable 2p/E , where p is the particle momentum.) The jet model reproduces this distribution quite well whereas the phase-space model predicts too few particles with $x \ge 0.4$. However, one could argue that the reason the S distributions agree with the jet model is that the jet model produces a larger number of events with high momentum particles and such events tend to have low S. To determine whether the agreement of the S distributions is simply a consequence of the agreement of the xdistributions, we examined the S distributions for those events in which no particle has x > 0.4. For these events the x distributions for both models agree with the data. The S distributions for such events at 7.4 GeV are shown in Fig. 8(a). The jet model is still preferred over the phase-space model. The S distributions for events having a particle with x > 0.4 are shown in Fig. 8(b). Although the agreement is not perfect, the data are definitely in better agreement with the jet model. Therefore we conclude that the agreement of the S distributions with the jet model is not due simply to the agreement of the x distributions and, furthermore, the agreement of the x distributions is a consequence of the jet structure. In fact, in the jet model the production of high momentum particles is directly related to the limiting of transverse momentum relative to an axis.

Another possible cause for the appearance of jet structure is the production of resonances or new particles. In order to search for jets which are actually the decays of particles or resonances we examined the distributions of observed masses of jets as shown in Fig. 9 for 7.4 GeV data. The jet mass is the effective mass of all detected particles in an event on one side of a plane through the interaction vertex and perpendicular to the jet axis. Pion masses were used for all particles. Figure 9(a) shows the mass distribution for all jets. The spikes at masses of zero and the pion mass are due to zero-particle and one-particle jets, respectively. Most jet masses are less than 2 GeV/c². Figure 9(b) shows the mass distribution for 2-prong, charge = 0 jets. One can see that some jets are K_S^0 's and that there is a shoulder at the ρ^0 mass. There is no evidence for the f⁰. There is no evidence for any structure in the mass distribution for 3-prong, charge = ±1 jets, shown in Fig. 9(c). We conclude that there is no evidence for copious production of resonances which could lead to jet structure in the majority of the events. However, neutral particles are not detected and are therefore not included in the mass calculations. The effects of charmed particle production are not evident from these distributions and will be discussed further in Section IV.

The evidence for jet structure is statistical; that is, single events cannot be interpreted as either jet-like or isotropic. Events produced from the jet model Monte Carlo simulation can appear to be of either type. In the SPEAR energy range the limitation of transverse momentum to ~350 MeV/c is not enough to make jets obvious. However, for the purposes of illustration, we show in Fig. 10 a sample 7.4 GeV event: a "typical" jet-like event. The reconstructed jet axis is shown. The event has eight tracks, two of which have x > 0.3. The other six tracks have low momentum. The event has S = 0.081. The observed energy is less than $E_{c.m.}$ and the momenta do not balance, so there are missing particles.

III. MEASUREMENT OF JET AXIS ANGULAR DISTRIBUTION

In quark-parton models the angular distribution of the jet axis is determined by the angular distribution of the original quark pair. Thus the spins of the quarks can be inferred from a measurement of this angular distribution. The most general angular distribution for production of any quarks or particles through a single virtual photon is¹³

$$\frac{d\sigma}{d\Omega} = \frac{1}{2} (\sigma_{\rm T} + \sigma_{\rm L}) [1 + \alpha \cos^2 \theta + P^2 \alpha \sin^2 \theta \cos^2 \phi] , \qquad (3.1)$$

where θ is the polar angle of the particle with respect to the e⁺ beam direction, ϕ is the azimuthal angle with respect to the (horizontal) plane of the storage ring, and P is the degree of transverse polarization of each beam. The quantity α is given by

$$\alpha = \frac{\sigma_{\rm T} - \sigma_{\rm L}}{\sigma_{\rm T} + \sigma_{\rm L}} , \qquad (3.2)$$

where $\sigma_{\rm T}$ and $\sigma_{\rm L}$ are the transverse (helicity ±1 along the particle direction) and longitudinal (helicity 0 along the particle direction) production cross sections. For the production of a pair of spin-1/2 particles, for example the QED reaction $e^+e^- \rightarrow \mu^+\mu^-$, $\alpha = 1$. For a pair of spin-0 particles $\alpha = -1$. For multihadron production, α is bounded between these two extreme values and depends, in general, on $E_{\rm c.m.}$ and the particle type and momentum. (The same expression in different form is given by Eq. (1.2) in I where the single particle inclusive cross section is discussed.)

The transverse polarization term in Eq. (3.1) does not provide any new information that could not be obtained by measuring the polar angle dependence alone. However, the detector had a limited acceptance in polar angle $(50^{\circ} \text{ to } 130^{\circ})$ but had a full 2 azimuthal acceptance. The existence of transverse beam polarization thus allowed a more precise measurement of the jet axis angular distribution from the azimuthal angle distribution alone. Use of the ϕ distribution for the jet axis was more important than for the case of single particle inclusive distributions because in the latter case the acceptance cuts off fairly cleanly at the polar angle edge of the detector whereas in the former case the jet axis polar angle distribution is smeared by the additional complication of the jet axis determination.

In high energy e^+e^- storage rings the beams become transversely polarized under certain conditions through the mechanism of synchrotron radiation with spin-flip.¹⁴ This is called radiative beam polarization and was first discussed by Ternov, Loskutov, and Korovina in 1961.¹⁵ The amount of spin-flip radiation is extremely small compared with the ordinary (nonflip) synchrotron radiation. In 1963 Sokolov and Ternov¹⁶ showed that for initially unpolarized electrons or positrons of charge e, mass m, and energy $E = \gamma mc^2$ in uniform motion in a circle of radius ρ there is a gradual buildup of transverse polarization according to

$$P(t) = \frac{8\sqrt{3}}{15} \left(1 - e^{-t/\tau_0} \right) , \qquad (3.3)$$

where the characteristic time τ_0 is given by

$$\frac{1}{\tau_{o}} = \frac{5\sqrt{3}}{8} \frac{e^{2} h \gamma^{5}}{m^{2} c^{2} \rho^{3}} \qquad (3.4)$$

Positrons are polarized parallel to the magnetic field, electrons antiparallel. For a storage ring consisting of a set of identical bending magnets of bending radius ρ and straight sections combining to an orbit of circumference $2\pi R$, a convenient formula for the polarization time constant is

$$\tau_{o}(sec) = 98.7 \frac{\left[\rho(M)\right]^{3}}{\left[E(GeV)\right]^{5}} \frac{R}{\rho} .$$
 (3.5)

The most distinctive feature of Eq. (3.5) is the very strong energy dependence. At SPEAR the polarization time constant is approximately 14 minutes at 3.7 GeV per beam.

The transverse beam polarization was observed to reach about 80% of the expected maximum value at $E_{c.m.} = 7.4 \text{ GeV.}^{17}$ The resulting azimuthal asymmetries were used to determine the jet axis angular distribution and the single particle inclusive angular distributions for multihadronic events. The data from $e^+e^- \rightarrow \mu^+\mu^-$ taken simultaneously with the multihadronic data at 7.4 GeV were used to determine a time-average value of $p^2 = 0.47 \pm 0.05$.

Figure 11 shows the observed jet axis ϕ distributions for jet axes with $|\cos\theta| \leq 0.6$ for 6.2 and 7.4 GeV data. (Since the jet axis is a symmetry axis, the angle ϕ + 180° is equivalent to the angle ϕ .) At 6.2 GeV, where the beam energy corresponds to a spin-depolarization resonance, the ϕ distribution is flat. The 6.2 GeV data were used to check that there was no ϕ asymmetry introduced by the detector. At 7.4 GeV a strong azimuthal dependence is observed.⁶,¹⁰ The ϕ distribution shows an asymmetry with maxima and minima at the same values of ϕ as for $e^+e^- \Rightarrow \mu^+\mu^-$.

The observed jet axis ϕ asymmetry at 7.4 GeV and the measured value of P² were used to determine the parameter α for the jet axis angular distribution as given by Eq. (3.1). The observed value of α for the jet axis is $\alpha = 0.50 \pm 0.07$. From the jet model Monte Carlo simulation, which included the angular distribution for the produced jet axis as in Eq. (3.1), we found that the observed value of α is less than the true value of α which describes the production of the jets because of the incomplete acceptance of the detector, the loss of neutral particles, and our method of reconstructing the jet axis. The simulation was used to calculate a ratio of observed to produced values of α of 0.52 at 7.4 GeV. This ratio was then used to correct the observed α to obtain $\alpha = 0.97 \pm 0.14$ for the produced jet axis angular distribution. In terms of σ_L and σ_T this value of α corresponds to $\sigma_L/\sigma_T = 0.02 \pm 0.07$. The error in α is statistical only; we estimate that the systematic errors in the observed α can be neglected. The systematic error due to model dependence in the correction factor relating the observed to the produced values of α is expected to be small compared to the statistical error. The jet axis angular distribution was thus found to be consistent with that for a pair of spin-1/2 particles, as predicted for jets originating from quarks.

An azimuthal asymmetry was also observed¹⁸ in the single particle inclusive ϕ distributions for the same sample of data at 7.4 GeV, as shown in Fig. 12 for particles with x > 0.3 and $|\cos\theta| \leq 0.6$. Again the asymmetry is observed to have the same sign as for μ -pair production. This observation is not surprising since the particles in these events were used to calculate the jet axis. The effect is momentum dependent in that the highest momentum particles tend to follow the jet axis while the lowest momentum particles are produced isotropically. The measured value of p^2 and the $\cos\theta$ and ϕ distributions of the particles as a function of x were used to determine the inclusive hadron α as a function of x. The jet model Monte Carlo simulation was used to predict the single particle angular distributions for all values of particle momenta. Figure 13 shows the values for the inclusive hadron α as a function of x at 7.4 GeV compared with the jet model calculation. The model assumed the value $\alpha = 0.97 \pm 0.14$ for the jet axis angular distribution. The prediction agrees well with the data for all values of x.

At energies other than 7.4 GeV it was not possible to make a precise determination of the jet axis angular distribution because of the small beam polarization and consequent absence of ϕ asymmetry. The cos θ distribution of the jet axis was too strongly affected by the limited acceptance of the detector in $\cos\theta$. We were able, however, to measure the inclusive hadron α versus x by fitting the inclusive $\cos\theta$ distributions. These determinations are less precise than those using polarized beams. Figure 14 shows best-fit values of α for various energies as a function of x. At 3.0 GeV the inclusive α distribution is consistent with isotropy for all values of x. At the higher energies α begins to increase with increasing x beginning at $x \sim 0.3$ to maximum values near 1 at the higher values of x. These values are consistent with the polarized beam measurement. The jet model simulation with a jet axis angular distribution of $1 + \cos^2 \theta$ can reproduce this dependence of α on x and E including the isotropy at c.m. 3.0 GeV. In fact, we begin to observe nonzero values for α at about the energies where jet structure begins to be differentiated from phase space.

The data strongly support a jet hypothesis for hadron production in e⁺e⁻ annihilation. The jet model Monte Carlo simulation reproduces not only the sphericity distributions for whole events but also the single particle inclusive momentum and angular distributions. The jet axis angular distribution integrated over azimuthal angle is proportional to 1 + (0.97 ± 0.14) $\cos^2\theta$ at 7.4 GeV, giving $\sigma_L/\sigma_T = 0.02 \pm 0.07$. The jet

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axis angular distribution is consistent with that for a pair of spin-1/2 particles as expected in quark-parton models.

IV. INCLUSIVE DISTRIBUTIONS IN VARIABLES RELATIVE TO THE JET DIRECTION

We have seen that multihadronic events produced by e⁺e⁻ annihilation exhibit jet structure as would be expected from a quark-pair origin. If the jet structure is indeed due to quark-parton jets, inclusive distributions in variables relative to the jet direction, which is expected to be the quark direction, will give information about the fragmentation of quarks into hadrons. One can study the dependence of the inclusive distributions in momentum transverse to the jet axis on the scaled momentum parallel to that axis. In addition, these inclusive distributions can be compared with similar distributions from other processes, such as leptoproduction and hadron-hadron interactions.

In order to investigate such questions we have measured inclusive distributions in Feynman x, rapidity, and transverse momentum relative to the jet axis. We have studied the biases which might be introduced by the methods used to measure these distributions. The jet model Monte Carlo simulation was used to calculate corrections so that the distributions presented here are the best representations of the true distributions that we can measure given our knowledge of the detector and the production model.

For the measurement of inclusive distributions we used the multihadronic events with three or more detected charged particles at fixed $E_{c.m.}$ values of 3.0 and 4.8 GeV and in three energy ranges from 5.6 to 7.8 GeV. Although there is no differentiation between jet structure and isotropic production at 3.0 GeV, multihadronic events at that energy presumably occur via the production and fragmentation of quark-antiquark pairs. The 3.0 GeV data is therefore of use in providing a comparison with physics below charm threshold. The data samples consisted of 1100 events at 3.0 GeV, 7300 events at 4.8 GeV, 23000 events from 5.6 to 6.3 GeV, 15900 events from 6.3 to 7.0 GeV, and 51900 events from 7.0 to 7.8 GeV after cuts had been applied.

We constructed the observed jet axis as described in Section II. The components of each particle momentum parallel to (p_{\parallel}) and perpendicular to (p_{\perp}) the jet axis were then calculated, as shown in Fig. 15. We then produced observed inclusive distributions in p_{\parallel} , p_{\perp} , and rapidity. The problem then was to correct these distributions for geometric acceptance, trigger bias, data analysis cuts, radiative corrections, and incorrect determination of the jet axis. Studies were made using the jet model Monte Carlo simulation in which we knew the true jet axis for every event. It was found that the observed distributions in p_{\parallel} for all events were similar enough to the produced distributions that they could be corrected to give the true distributions. The rapidity and p_{\perp} distributions, however, were more sensitive to the correct determination of the jet axis and could not be reasonably corrected without applying further event selection criteria. The method used for these distributions will be described later.

Since the inclusive quantity $s d\sigma/dx$ ($s = E_{c.m.}^2$), shown in Fig. 17(a) of I, nearly scales, we were led to examine the inclusive distributions for $s d\sigma/dx_{\parallel}$, where x_{\parallel} , or Feynman x, is defined by

$$x_{\parallel} = 2p_{\parallel}/E_{c.m.}$$
 (4.1)

In quark-parton models x_{\parallel} is the fraction of parton momentum carried by the hadron in the direction of the parton.

The inclusive s $d\sigma/dx_{\parallel}$ distribution is given for each x_{\parallel} bin by

$$s \frac{d\sigma}{dx_{\parallel}} (x_{\parallel i}) = \frac{s \cdot N(x_{\parallel i})}{\varepsilon(x_{\parallel i}) \cdot L \cdot \delta x_{\parallel i}} , \qquad (4.2)$$

where $N(x_{\parallel i})$ is the number of detected tracks in the bin centered on $x_{\parallel} = x_{\parallel i}$, L is the integrated luminosity for the data sample, $\delta x_{\parallel i}$ is the bin width, and $\varepsilon(x_{\parallel i})$ is the single particle inclusive detection efficiency determined from the Monte Carlo simulation for the x_{\parallel} bin centered at $x_{\parallel i}$. The efficiency $\varepsilon(x_{\parallel i})$ is made up of several parts:

$$\varepsilon(\mathbf{x}_{\parallel \mathbf{i}}) = \frac{N_{\mathbf{D}}(\mathbf{x}_{\parallel \mathbf{i}})}{N_{\mathbf{p}}(\mathbf{x}_{\parallel \mathbf{i}})} \varepsilon_{\mathbf{v}}^{\mathbf{b}(1+\delta)} , \qquad (4.3)$$

where $N_D(x_{\parallel|1})$ is the number of detected particles in the x_{\parallel} bin centered at $x_{\parallel 1}$ in the Monte Carlo calculation $(x_{\parallel}$ is calculated relative to the observed jet axis), $N_p(x_{\parallel|1})$ is the number of produced particles for events with no initial-state radiation in the x_{\parallel} bin centered at $x_{\parallel|1}$ $(x_{\parallel}$ is calculated relative to the true jet axis), ε_v is the correction for loss of events due to requiring the vertex to lie within the interaction region fiducial volume, b is the correction for background from beam-gas interactions, and δ is the radiative correction factor as described in Eqs. (4.6), (4.7), and (4.9) of I. Initial-state radiation was included in the produced events so that the efficiency of the detector for events in a moving center-of-mass system at energy lower than $E_{c.m.}$ was included. The effects of the inclusion of initial-state radiation are an overall decrease in efficiency because nonradiative events have higher multiplicities than those in which there was significant radiation and an additional decrease in inclusive distribution efficiency for high momentum particles because events with significant radiation cannot have particles with momentum near the beam energy. Incorrect jet axis determination is corrected for by the shifting of particles between the produced and detected x_{\parallel} bins. It is important to include the effect of the jet axis correction in events with significant initial-state radiation because these events do not fit the assumption of back-to-back jets. The inclusive distributions were corrected so as to include multihadronic events with all produced multiplicities, including events with two charged particles. Heavy lepton production was not subtracted. Since only events with at least three charged tracks were used, the effect of heavy leptons was negligible.

The corrected s $d\sigma/dx_{\parallel}$ distributions versus x_{\parallel} are shown in Fig. 16. If we compare the distributions in s $d\sigma/dx_{\parallel}$ with those in s $d\sigma/dx$ (see Fig. 17(a) of I), we see that as $E_{c.m.}$ increases the two distributions become more alike because p_{\perp} is a decreasing fraction of p. At the lower energies the distributions have quite different shapes. When e^+e^- quark fragmentation distributions are compared, for example, with leptoproduction, they should be compared in terms of the variable x_{\parallel} . Except for the $E_{c.m.} =$ 3.0 GeV data, the s $d\sigma/dx_{\parallel}$ distributions scale for $x_{\parallel} \ge 0.1$ to within $\pm 10\%$ which is at the level of our normalization and systematic uncertainties. In order better to illustrate the scaling behavior in x_{\parallel} , we show in Fig. 17 the values of s $d\sigma/dx_{\parallel}$ in various x_{\parallel} bins versus $E_{c.m.}$. For $E_{c.m.} \ge 4.8$ GeV s $d\sigma/dx_{\parallel}$ distributions appear to scale better than s $d\sigma/dx$ distributions.

In order to measure the inclusive distributions in p_{\perp} and rapidity we found that we needed to require that a fairly high momentum particle be detected in order to be able to find an observed jet axis which was close enough to the true jet direction that we could use the jet model Monte Carlo simulation to calculate corrections. However, requiring that a high momentum particle be detected biases the inclusive distributions. The method used to remove the bias is the following:¹⁹

- 1. Find the observed jet axis as described in Section II.
- 2. Divide the event into two jets with a plane through the interaction vertex and perpendicular to the jet axis.
- 3. If the highest-momentum particle on one side of the plane (x_{max}) has x greater than some minimum value, measure the inclusive distributions in x_{\parallel} , p_{\perp} , and rapidity for all the particles on the <u>other</u> side of the plane from the chosen particle.
- 4. Repeat step 3 for the other side of the plane. This means that an event may be counted twice in the inclusive distributions, but no particle is counted more than once. The inclusive distributions are normalized to the total number of jets contributing.

Corrections were calculated by applying this procedure to both the produced and detected events in the Monte Carlo simulation. For the produced events the true jet direction is known, so corrections for finding the wrong jet axis in the detected events could be calculated. The corrections, of course, are somewhat model dependent. We have some confidence in this correction procedure, however, because the jet model distributions agree rather well with the data.

As a test of the effectiveness of this method for removing biases due to requiring a high momentum particle, we apply it to the x_{\parallel} distributions which we have already measured for all events. We used the highest energy data sample, $7.0 < E_{c.m.} < 7.8$ GeV, because it has the best statistics (and also because it has the best defined jet structure).

The particle density distribution $(1/\sigma)d\sigma/dx_{\parallel}$ is given for each x_{\parallel} bin by

$$\frac{1}{\sigma} \frac{d\sigma}{dx_{\parallel}} (x_{\parallel i}) = \frac{N(x_{\parallel i})}{\varepsilon(x_{\parallel i})(N_{i}/\varepsilon_{i})\delta x_{\parallel i}} , \qquad (4.4)$$

where $N(x_{\parallel i})$ is the number of detected tracks in the bin centered on $x_{\parallel} = x_{\parallel i}$ in a jet opposite a jet containing a particle with x larger than some cut, $\varepsilon(x_{\parallel i})$ is the single particle inclusive detection efficiency, N_{j} is the number of jets with x_{max} larger than the cut, ε_{j} is the efficiency for detecting such a jet, and $\delta x_{\parallel i}$ is the bin width. Here $\varepsilon(x_{\parallel i})$ is given by

$$\varepsilon(\mathbf{x}_{\parallel i}) = \frac{N_{D}(\mathbf{x}_{\parallel i})}{N_{P}(\mathbf{x}_{\parallel i})},$$
 (4.5)

where $N_{D}(x_{\parallel i})$ is the number of detected particles in the x_{\parallel} bin centered at $x_{\parallel i}$ in a jet opposite a jet containing a particle with x larger than the cut in the Monte Carlo calculation and $N_{p}(x_{\parallel i})$ is the same quantity for produced events in the Monte Carlo calculation. The inclusive distributions are radiatively corrected in the same manner as for s $d\sigma/dx_{\parallel}$, that is, $N_{p}(x_{\parallel})$ is calculated from the produced x_{\parallel} distribution for events with no initial-state radiation. The extra correction factors in Eq. (4.3) are no longer needed since they cancel with the same quantities for the jet efficiency. ε_{i} is given by

$$\varepsilon_{j} = \frac{N_{jD}}{N_{jP}} , \qquad (4.6)$$

where N_{jD} is the number of detected jets with x_{max} larger than the cut in

the Monte Carlo calculation and N_{jP} is the number of produced jets with x_{max} larger than the cut in events with no initial-state radiation.

In Fig. 18 are shown the corrected distributions $(1/\sigma)d\sigma/dx_{\parallel}$ versus x_{\parallel} for various cuts on x_{\max} (which is at positive x_{\parallel} and is not plotted) for 7.0 < E < 7.8 GeV. σ is the cross section for jets with x max within the specified range and the distributions $(1/\sigma)d\sigma/dx_{\parallel}$ are thus distributions of particle density in x_{\parallel} . We see that these distributions are nearly independent of the x cut and agree with the distribution for all events for negative x_{\parallel} . Only for $x_{max} > 0.7$ do we see a significant effect in the x_{\parallel} distribution on the opposite side: requiring a particle with $x_{max} > 0.7$ reduces the particle density for small $|x_{\parallel}|$ and increases the particle density for large $|x_{\parallel}|$. On the same side as the x_{max} particle we do see a correlation: the particle density decreases as ${ extsf{x}}_{\max}$ increases. We conclude that this method produces a relatively bias-free \mathbf{x}_{\parallel} distribution for negative x_{\parallel} since the x_{\parallel} distribution opposite a jet with x_{\max} > 0.3 looks like the x_{\parallel} distribution for all events. The ratio of observed jets with x $_{max}$ > 0.3 to all events is 0.60 for 7.0 < E $_{c.m.}$ < 7.8 GeV. We chose to use x_{max} > 0.3 for our analysis because the statistics are better than for the other cuts. Of those observed jets with $x_{max} > 0.3$, only 4.7% have $x_{max} > 0.7$, so the difference in distributions for $x_{max} > 0.7$ has little effect on the total sample.

In fact, we have made a physical observation: we have shown that the particle density distribution in x_{\parallel} in one jet is independent of the x_{max} cut in the other jet. There is no particular reason why this has to be so, although it is expected in the quark-parton model. In Fig. 19 we show the $(1/\sigma)d\sigma/dx_{\parallel}$ distributions produced by the limited transverse momentum jet model Monte Carlo calculation. In contrast with the data, the Monte

Carlo does show a dependence of the negative x_{\parallel} distribution on the x_{max} cut used on the opposite side. For the Monte Carlo the particle density for small $|x_{\parallel}|$ decreases and that for large $|x_{\parallel}|$ increases as x_{max} increases. The x_{\parallel} distribution opposite a jet with $x_{max} > 0.3$ is significantly different from the distribution for all events.

The corrected $(1/\sigma)d\sigma/dx_{\parallel}$ distributions for $x_{max} > 0.3$ for the data at various $E_{c.m.}$ are shown in Fig. 20. $(1/\sigma)d\sigma/dx_{\parallel}$ distributions for all events at the same energies are shown in Fig. 21, where σ is the event cross section. The distributions in Fig. 20 for negative $\boldsymbol{x}_{\parallel}$ agree quite well with those in Fig. 21 for all x_{\parallel} considered to be positive if those in Fig. 21 are divided by two (because the distributions in Fig. 21 are for both jets). We see that the method works well for all energies, that is, the x_{\parallel} distributions opposite a jet with $x_{max} > 0.3$ look like those for all events. To obtain $(1/\sigma)d\sigma/dx_{\parallel}$ for all events from $(1/\sigma)d\sigma/dx_{\parallel}$ for particles opposite a jet with $x_{max} > 0.3$, assume that the distribution for positive x_{\parallel} is the reflection of that for negative x_{\parallel} about x_{\parallel} = 0. One observation that can be made about the distributions $(1/\sigma)d\sigma/dx_{\parallel}$ for the various energies is that they scale rather well for all energies, including 3.0 GeV, for $x_{\parallel} \ge 0.2$. That $(1/\sigma)d\sigma/dx_{\parallel}$ scales for E ≥ 4.8 GeV is not surprising since s d σ/dx_{\parallel} scales and R is approximately constant. However, R at 3.0 GeV is a factor of 1.6 smaller than R at the higher energies. Evidently, normalizing the inclusive distributions in x_{\parallel} to the total hadronic cross section rather than the integrated luminosity makes up for this difference.

Inclusive distributions in rapidity and p_{\perp} relative to the jet direction were then measured using the method just described. The rapidity y is defined by

$$y = \frac{1}{2} \ln \left(\frac{E + p_{\parallel}}{E - p_{\parallel}} \right) , \qquad (4.7)$$

where E is the energy of the particle assuming a pion mass. Figure 22 shows the corrected particle density distributions $(1/\sigma)d\sigma/dy$ versus y for various x cuts for 7.0 < E < 7.8 GeV. As was the case for c.m. $(1/\sigma)d\sigma/dx_{\parallel}$ for negative x_{\parallel} , we see that the distributions for negative y are nearly independent of the x cut. For $x_{max} > 0.7$ there is a decrease in particle density for y between -1.5 and 0. For positive y, of course, we see a decrease in multiplicity as the x cut increases, as was noted previously for the x_{\parallel} distributions. We then used the cut $x_{max} > 0.3$ to produce corrected distributions in rapidity density at the other energies, as shown in Fig. 23. The unbiased distributions of particles in rapidity relative to the jet direction would look like Fig. 23 with the distributions for positive y given by reflections of those for negative y about y = 0. Or, equivalently, the distributions for negative y multiplied by two could be plotted as $(1/\sigma)d\sigma/d|y|$ versus |y| in order to compare with conventional presentations. The distributions $(1/\sigma)d\sigma/dy$ increase in width as E increases. The distributions for the three highest energy ranges are quite similar in shape and appear to level off to a plateau for y between -1.0and 0. The value of $(1/\sigma)d\sigma/dy$ at the plateau is about 1.45 and is somewhat energy dependent. The dip in $(1/\sigma)d\sigma/dy$ for y between -0.2 and 0 may be due to systematic errors in our data analysis. Because of tracking problems, we did not use particles with transverse momentum relative to the beam direction less than 150 MeV/c and were required to rely on the Monte Carlo simulation to correct for this cut.

2

Inclusive distributions in p, relative to the jet direction are of considerable interest because they are the basis of the definition of jet structure. Figure 24 shows the corrected distributions $(1/\sigma)d\sigma/dp^2$, versus p_{\parallel}^2 for particles opposite (negative x_{\parallel}) jets with various x_{max} cuts for $7.0 < E_{c.m.} < 7.8$ GeV. The distributions are independent of the x max cut, except for $x_{max} > 0.7$ which shows a decrease in particle density for $p_1^2 < 0.6 (GeV/c)^2$. The corrected distributions $(1/\sigma)d\sigma/dp_1^2$ versus p_1^2 measured for particles opposite jets with x > 0.3 for the various $E_{c.m.}$ values are presented in Fig. 25. The p_1^2 distributions are very similar in shape for $E_{c.m.} \ge 4.8$ GeV. The area under each curve increases as $E_{c.m.}$ increases because of the increasing multiplicity. For $E_{c.m.}$ = 3.0 GeV the p_1^2 distribution falls off slightly faster as p_1^2 increases and there are no particles with $p_1^2 > 0.6 (GeV/c)^2$. The values of the differential cross sections in the distributions shown in Fig. 25 should be multiplied by two since they represent only one of the two jets in an event.

In order to illustrate how the corrections might affect the p_{\perp}^2 distributions we present in Fig. 26 the uncorrected observed distributions $(1/N_{ev})dN/dp_{\perp}^2$ for particles opposite jets with $x_{max} > 0.3$, where N_{ev} is the number of observed jets with $x_{max} > 0.3$ and dN/dp_{\perp}^2 is the number of particles observed per $(GeV/c)^2$ in each p_{\perp}^2 bin. By comparing Figs. 25 and 26 one can see that the effect of the Monte Carlo corrections is to increase the particle density at high p_{\perp}^2 relative to that at low p_{\perp}^2 . This is because the detector acceptance makes it more difficult to detect both a jet and a particle at high p_{\perp} to it. In any case, the Monte Carlo corrections do not change appreciably the similarity in shapes of the

distributions for $E_{c.m.} \ge 4.8$ GeV nor do they change the observation that the slopes decrease as p_1^2 increases.

Figure 27 shows the same distributions as in Fig. 25 plotted versus P_{\perp} rather than p_{\perp}^2 . These distributions were used to calculate the average transverse momentum relative to the jet direction $\langle p_{\perp} \rangle$ for each of the $E_{c.m.}$. Figure 28 shows $\langle p_{\perp} \rangle$ opposite jets with $x_{max} > 0.3$ versus $E_{c.m.}$. The dependence of $\langle p_{\perp} \rangle$ on $E_{c.m.}$ is simple evidence for jet structure since $\langle p_{\perp} \rangle$ levels off as $E_{c.m.}$ increases. The value of $\langle p_{\perp} \rangle$ for 7.0 < $E_{c.m.} < 7.8$ GeV is 364 ± 2 MeV/c where the error is statistical only. To estimate the systematic error we calculated $\langle p_{\perp} \rangle$ for various x_{max} cuts for 7.0 < $E_{c.m.} < 7.8$ GeV (see Fig. 24 for p_{\perp}^2 distributions for these x_{max} cuts). The range of $\langle p_{\perp} \rangle$ for different x_{max} cuts was within ±10 MeV/c of $\langle p_{\perp} \rangle$ for $x_{max} > 0.3$, so we estimate the systematic error for $\langle p_{\perp} \rangle$ to be ±10 MeV/c.

The distributions $(1/\sigma)d\sigma/dp_{\perp}^2$ versus p_{\perp}^2 , shown in Fig. 25, do not fit single exponentials in p_{\perp}^2 , as might have been expected from phenomenological arguments, except at $E_{c.m.} = 3.0$ GeV. For $E_{c.m.} \ge 4.8$ GeV the p_{\perp}^2 distributions fit reasonably well to a sum of two exponentials in p_{\perp}^2 : $(1/\sigma)d\sigma/dp_{\perp}^2 = c_1e^{-b_1^2p_{\perp}^2} + c_2e^{-b_2^2p_{\perp}^2}$; the parameters for such fits are given in Table I. Only statistical errors were used to determine χ^2 . The distributions given by the single exponential fit for $E_{c.m.} = 3.0$ GeV and by the sum-of-two-exponentials fit for $7.0 < E_{c.m.} < 7.8$ GeV are represented by the solid lines in Fig. 25. The coefficients of p_{\perp}^2 , b_1 and b_2 , are plotted versus $E_{c.m.}$ in Figs. 29(a) and 29(b). The larger coefficient b_1 is consistent with about 10 (GeV/c)⁻² for the three highest energy ranges; it is a little larger at 4.8 GeV and a little smaller at 3.0 GeV. The smaller coefficient b_2 is consistent with about 4 $(\text{GeV/c})^{-2}$ for all energies $E_{c.m.} \ge 4.8$ GeV. Thus we have shown quantitatively that the shapes of the p_1^2 distributions are quite similar for $E_{c.m.} \ge 4.8$ GeV.

In Fig. 30 we compare the p_{\perp}^2 distribution for 7.0 < E c.m. < 7.8 GeV with that for the jet model Monte Carlo. We see that for $p_1^2 > 0.6 (GeV/c)^2$ the Monte Carlo distribution is lower than the data. $\langle p_{_{
m I}} \rangle$ for the Monte Carlo distribution is 343 MeV/c, about 20 MeV/c lower than for the data. We also note that the Monte Carlo distribution is not a single exponential in p_{\perp}^2 . What could be the reason for the excess of high p_{\perp} particles? The answer may be found in Figs. 31(a) and 31(b) which show the $K^{\pm}\pi^{\mp}$ invariant mass distributions for 7.0 < $E_{c.m.}$ < 7.8 GeV for both particles with $p_{_{\rm I}}$ < 0.8 GeV/c and for one or both particles with $p_{_{\rm I}}$ \ge 0.8 GeV/c. (No time-of-flight information was used; each combination was plotted twice once for each mass assignment.) For the first case we see no signal, but for the second case we see a peak near the D° mass of 1864 MeV/c².²⁰ We therefore have conclusive evidence that some of the high p particles are the result of D^{O} production and decay into $K^{-\pi^+}$. Other D decays have been studied by Monte Carlo, but only the two-body decay $D^{0} \rightarrow K^{-\pi^{+}}$ contributes significantly to the $p_1 > 0.8 \text{ GeV/c}$ region. In fact, it is possible, although this hypothesis shouldn't be taken quantitatively, to produce a quite adequate representation of the observed p_1^2 distribution by adding to the jet model Monte Carlo a contribution from phase space production of $D^{O*} \overline{D}^{O*} \pi^+ \pi^-$, where $D^{O*} \rightarrow D^O \gamma$ or $D^O \pi^O$ and D^O decays only to $\bar{K}\pi^+$, as shown in Fig. 32. The relative normalization of the two models was chosen by requiring that the number of high p_1^2 particles agree with the data. One should note that all high p particles do not necessarily

come from charmed particle decays, and we cannot show that the second exponential in p_{\perp}^2 is completely due to charm. Some high p_{\perp} particles can result from ordinary two-jet production, and the jet model p_{\perp}^2 distribution is not a single exponential in p_{\perp}^2 .

We have measured the dependence of the p_{\perp} distributions on x_{\parallel} , or Feynman x, for 7.0 < $E_{c.m.}$ < 7.8 GeV. Figure 33 shows the corrected distributions $(1/\sigma)d\sigma/dp_{\perp}^2$ versus p_{\perp}^2 for several x_{\parallel} ranges for particles opposite jets with $x_{max} > 0.3$. The distributions are normalized to the cross section for jets with $x_{max} > 0.3$. From these distributions we see that particles with x_{\parallel} between 0.1 and 0.3 are the major contributors to the high p_{\perp}^2 region. Particles with x_{\parallel} less than 0.1 and between 0.3 and 0.5 contribute about equally to the high p_{\perp}^2 region. We were able to calculate $\langle p_{\perp} \rangle$ for the x_{\parallel} ranges with x_{\parallel} less than 0.5; the p_{\perp} distributions for x_{\parallel} greater than 0.5 are too poorly defined because of the limited statistics to allow a calculation of $\langle p_{\perp} \rangle$. In Fig. 34 we present $\langle p_{\perp} \rangle$ versus x_{\parallel} for three x_{\parallel} ranges. $\langle p_{\perp} \rangle$ increases with increasing x_{\parallel} in a manner quite like the "seagull" effect seen in hadronic physics and leptoproduction.²¹

The p_1^2 distributions for $x_{\parallel} < 0.1$ and $0.1 < x_{\parallel} < 0.3$ can be fitted to sums of two exponentials in p_1^2 , while the distribution for $0.3 < x_{\parallel} < 0.5$ requires only a single exponential. The parameters of the fits to $(1/\sigma) d\sigma/dp_1^2 = c_1 e^{-b_1 p_1^2} + c_2 e^{-b_2 p_1^2}$ are listed in Table II. The minimum p_1^2 used in the fits was varied somewhat to obtain reasonable fits. The fitted distributions are represented by the solid lines in Fig. 33. The values of the coefficients of p_1^2 , b_1 and b_2 , are plotted versus x_{\parallel} in Figs. 35(a) and 35(b). Since the single coefficient for $0.3 < x_{\parallel} < 0.5$ was in agreement with the smaller coefficient for the other two x_{\parallel} ranges, it was plotted in Fig. 35(b). The larger coefficients for $x_{\parallel} < 0.1$ and $0.1 < x_{\parallel} < 0.3$ are both consistent with 10 $(\text{GeV/c})^{-2}$, the same value that was found for the p_{\perp}^2 distribution integrated over x_{\parallel} . The smaller coefficients and the single coefficient for $0.3 < x_{\parallel} < 0.5$ are consistent with 4 $(\text{GeV/c})^{-2}$, again in agreement with the smaller coefficient for the p_{\perp}^2 distribution integrated over x_{\parallel} . If we were to assume that the exponential with the smaller slope is due to charmed particle production, then we would be forced to conclude that all particles with $0.3 < x_{\parallel} < 0.5$ are the result of charmed particle decay, which is unlikely. Unfortunately, we have been able to study only the decay $D^0 \rightarrow K^-\pi^+$ which has a branching ratio of only $(3.0 \pm 0.6)\%$.²⁰ We have been otherwise unable to separate the charm production component in this analysis.

We have looked for charge correlations between the leading particle in one jet and all other observed particles in events with three or more detected charged particles. The data sample used was the highest energy range 7.0 < $E_{c.m.}$ < 7.8 GeV. We plotted x_{\parallel} distributions using the same method as was described in connection with Fig. 18, except that two distributions were produced -- one for those particles with the same charge as x_{max} and another for those particles with the opposite charge to the x_{max} particle. In Fig. 36 we present the observed ratio (opposite charge)/ (same charge) of these two distributions in x_{\parallel} for two different x_{max} cuts: $x_{max} > 0.5$ and $x_{max} > 0.7$. x_{max} is at positive x_{\parallel} , and, of course, is not included. For these distributions we have used only events in which the total charge was 0 if an even number of particles was observed or ±1 if an odd number was observed. In general, since the detector did not have complete acceptance, one or more particles were not detected, so we do not expect to conserve charge. Given the charged particle multiplicity distribution for each x_{\parallel} bin, we could calculate the statistical expectation for the charge ratio as a function of x_{\parallel} . For example, for an event with 3 charged particles and total charge ±1 the probability that any 2 particles have opposite charge is 2/3 and the probability that any 2 particles have the same charge is 1/3, so the ratio of opposite charge to same charge is expected to be 2. The expected ratio decreases as the multiplicity increases. The statistical expectation versus x_{\parallel} is represented by the dashed line in Fig. 36.

We see that for positive x_{\parallel} the ratio of opposite charge to same charge is much larger than the statistical expectation. This means that there are same-side correlations: particles in the same jet as the x_{max} particle tend to have the opposite charge to the x_{max} particle. Such an effect can be caused by neutral resonances and is expected for various other models. For negative x_{\parallel} there is no evidence for charge correlations. (Such correlations would be long-range charge correlations.) For $x_{max} > 0.7$ the point at $x_{\parallel} = -0.85$ is high compared with the statistical expectation, but the difference is not statistically significant. There were only 18 events contributing to this point. Of these 3 had the same charge as x_{max} and 15 had the opposite charge, whereas we would have expected 6 and 12. The probability of observing a charge ratio of 5 or more is about 10%.

The statistical expectation is generally a little larger than the measured charge ratio for negative x_{\parallel} . In principle, when calculating the statistical expectation for negative x_{\parallel} we should have taken into account the observed charge correlation at positive x_{\parallel} . This would have had the effect of lowering the statistical expectation slightly for negative x_{\parallel} . The effect would be small because the number of particles

at positive x_{\parallel} is small for such large x_{max} cuts (see Fig. 18). Some quark-parton models predict a charge correlation between leading particles in opposite jets due to their production from a quark-antiquark pair. Particles with $x_{\parallel} < -0.5$ are certainly the leading particles in the jet opposite the jet with x_{max} , yet we see no such effect. It may be that to see these leading-particle charge correlations, both particles must have x very near 1; unfortunately, the statistics of our data sample, even with 52,000 events, are not sufficient for such a measurement. Also, since events with a high-x particle at this energy have low multiplicities, charge correlation due to charge conservation makes other charge correlation effects more difficult to observe.

V. CONCLUSIONS

Studies of hadron production by e^+e^- annihilation have yielded very exciting and fundamental results. Among these results is the strong evidence for jet structure for $E_{c.m.} \ge 4.8$ GeV as shown by the agreement of the observed sphericity distributions with the jet model rather than the phase-space model predictions. By making use of the transversely polarized e^+ and e^- beams at 7.4 GeV, the jet axis angular distribution was measured to be proportional to 1 + (0.97 \pm 0.14) $\cos^2\theta$, consistent with that for a pair of spin-1/2 particles. A jet model Monte Carlo simulation is able to reproduce not only the sphericity distributions for whole events but also the single particle inclusive momentum and angular distributions.

Inclusive distributions in s $d\sigma/dx_{\parallel}$, where x_{\parallel} (Feynman x) = $2p_{\parallel}/E_{c.m.}$ and p_{\parallel} is the component of particle momentum parallel to the jet direction, scale for $x_{\parallel} > 0.1$ for $E_{c.m.} \ge 4.8$ GeV to within ±10%, which is at the

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level of our normalization and systematic uncertainties. Inclusive distributions in $(1/\sigma)d\sigma/dx_{\parallel}$, where σ is the total hadronic cross section, scale rather well for $x_{\parallel} \ge 0.2$ for all energies between 3.0 and 7.8 GeV away from the resonance regions. The x_{\parallel} distribution for one jet is nearly independent of the magnitude of the momentum of the leading particle in the other jet.

Distributions in rapidity with respect to the jet direction have been measured and show the development of a plateau for the three highest energy regions measured, from 5.6 to 7.8 GeV.

Distributions in p_{\perp}^2 relative to the jet direction have been measured. The average p_{\perp} has been measured as a function of $E_{c.m.}$ and levels off at a constant value for the three highest energy regions measured, giving direct evidence for jet structure. The p_{\perp}^2 distributions do not agree with a simple limited transverse momentum jet model. The distributions in p_{\perp}^2 can be fitted to the sum of two exponentials in p_{\perp}^2 . Charmed meson production accounts for some of the high p_{\perp} particles observed. Distributions in p_{\perp}^2 as a function of x_{\parallel} have been measured for 7.0 < $E_{c.m.}$ < 7.8 GeV. The average p_{\perp} increases with increasing x_{\parallel} for $x_{\parallel} \leq 0.5$.

Evidence for same-side charge correlations has been found: particles in the same jet as a large-x leading particle tend to have charge opposite to that of the leading particle. There is no evidence for opposite-side charge correlations.

The data are in general agreement with the predictions of quarkparton constituent models. The recent data from $PETRA^{22}$ for e^+e^- annihilation at energies up to $E_{c.m.} = 36$ GeV have confirmed the results reported here from the Mark I detector at SPEAR and have extended the analysis to the confirmation of the QCD predictions of three- and four-jet events.

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TABLE I

Fits to $\frac{1}{\sigma} \frac{d\sigma}{dp_{\perp}^2} = c_1 e^{-b_1 p_{\perp}^2} + c_2 e^{-b_2 p_{\perp}^2}$ for particles opposite jets with $x_{max} > 0.3$ for various $E_{c.m.}$ for $p_{\perp}^2 > 0.01 (GeV/c)^2$.

E _{c.m.} (GeV)	^c 1 [(GeV/c) ⁻²]	^b 1 [(GeV/c) ⁻²]	^c 2 [(GeV/c) ⁻²]	^b 2 [(GeV/c) ⁻²]	x ²	Degrees of freedom
3.0	11.08 ±0.45	8.95 ±0.42			10.40	11
4.8	9.37 ±0.86	13.18 ±1.56	4.93 ±0.98	4.43 ±0.36	4.86	11
5.6-6.3	12.15 ±0.69	10.41 ±0.68	4.13 ±0.80	3.93 ±0.27	23.75	19
6.3-7.0	11.53 ±1.01	11.07 ±1.08	5.87 ±1.17	4.25 ±0.30	36.70	18
7.0-7.8	13.97 ±0.49	10.23 ±0.44	4.62 ±0.56	3.77 +0.17	29.86	21

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TABLE II

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Fits to $\frac{1}{\sigma} \frac{d\sigma}{dp_{1}^{2}} = c_{1}e^{-b_{1}p_{1}^{2}} + c_{2}e^{-b_{2}p_{1}^{2}}$ for particles in various x_{\parallel} ranges opposite jets with $x_{max} > 0.3$ for $7.0 < E_{c.m.} < 7.8$ GeV.

x^{-2} x^{-2} y^{-2} y^{-2}	0.41 19.17 15	.24 21.44 17	15.69 11
2] [(GeV/G	3 3.79±0	2 4.17±C	
c2 [(GeV/c) ⁻	0.96±0.3	2.50±0.5	
b ₁ [(GeV/c) ⁻²]	10.37±0.72	8.82±1.12	3.88±0.21
c1 [(GeV/c) ⁻²]	8.98±0.47	3.09±0.47	1.24 ± 0.09
x range	$p_{\rm L}^2 > 0.09 ({\rm GeV/c})^2$	$p_{L}^{2} > 0.04 (GeV/c)^{2}$	0.3 - 0.5

FIGURE CAPTIONS

- 1. Hadron production by e e annihilation in quark-parton model.
- 2. Observed single particle p₁ with respect to jet axis for events with three or more detected charged particles for 7.4 GeV data compared with the jet model (solid curve) and phase-space model (dashed curve) predictions.
- 3. Observed sphericity distributions for data, jet model (solid curves) and phase-space model (dashed curves) for (a) E = 3.0 GeV, (b) E = 6.2 GeV, and (c) E = 7.4 GeV.
- 4. Observed sphericity distribution at 7.4 GeV compared with prediction for jet model with pions only (solid curve), jet model with pions, kaons, and etas (dashed curve), phase-space model with pions only (dashed-dotted curve), and phase-space model with pions, kaons, and etas (dotted curve).
- 5. Observed mean sphericity vs. E for data, jet model (solid c.m. curve), and phase-space model (dashed curve).
- Distributions of the cosine of diparticle angles for data, jet model (solid curves), and phase-space model (dashed curves) for
 (a) E = 6.2 GeV and (b) E = 7.4 GeV.
- 7. Observed single particle x distribution for events with three or more detected charged particles at 7.4 GeV compared with the jet model (solid curve) and phase-space model (dashed curve) predictions.
- 8. Observed sphericity distributions at 7.4 GeV for data, jet model (solid curves) and phase-space model (dashed curves) for (a) events with largest x ≤ 0.4 and (b) events with largest x > 0.4.

- 9. Observed jet mass distributions at 7.4 GeV for (a) all jets,
 (b) 2-prong, charge = 0 jets, and (c) 3-prong, charge = ±1 jets.
 Pion masses were used for all particles. The arrows indicate the masses of particles or resonances having the indicated decay modes.
- 10. Momentum space representation of a sample 7.4 GeV event. p_x , p_y , p_z refer to the three spatial components of the particle momenta. The z-axis lies along the positron direction. This event has 8 tracks, 2 with x > 0.3. The reconstructed jet axis is represented by the dashed line. The event has S = 0.081.
- 11. Observed distributions of jet axis azimuthal angles from the plane of the storage ring for jet axes with |cosθ| ≤ 0.6 for
 (a) E = 6.2 GeV and (b) E = 7.4 GeV.
- 12. Observed single particle inclusive distributions in azimuthal angle ϕ for particles with x > 0.3 and $|\cos\theta| \le 0.6$ for

(a) $E_{c.m.} = 7.4 \text{ GeV}$ and (b) $E_{c.m.} = 6.2 \text{ GeV}$.

- 13. Observed inclusive α vs. x for particles with $|\cos\theta| \leq 0.6$ in hadronic events at $E_{c.m.} = 7.4$ GeV. The prediction of the jet model Monte Carlo simulation for a jet axis angular distribution with $\alpha = 0.97 \pm 0.14$ is represented by the shaded band.
- 14. Inclusive hadron angular distribution coefficient α vs. x obtained from fits to 1 + α (x)cos² θ for (a) $E_{c.m.} = 3.0 \text{ GeV}$, (b) $E_{c.m.} = 4.8 \text{ GeV}$, (c) 5.6 < $E_{c.m.} < 6.8 \text{ GeV}$, and (d) 6.8 < $E_{c.m.} < 7.6 \text{ GeV}$.
- 15. Illustration of a hadronic event from e^+e^- annihilation showing the jet axis and the components of the momentum \vec{p} of a particle parallel to (p_{\parallel}) and perpendicular to (p_{\perp}) the jet axis.

- 16. Corrected single particle inclusive x_{\parallel} distributions s $d\sigma/dx_{\parallel}$ vs. x_{\parallel} for various $E_{c.m.}$. $x_{\parallel} = 2p_{\parallel}/E_{c.m.}$, where p_{\parallel} is the component of particle momentum parallel to the jet direction.
- 17. Corrected single particle inclusive x_{\parallel} distributions s $d\sigma/dx_{\parallel}$ vs. $E_{c.m.}$ for various x_{\parallel} ranges.
- 18. Corrected particle density distributions $(1/\sigma)d\sigma/dx_{\parallel}$ vs. x_{\parallel} for various x_{max} cuts for 7.0 < E < 7.8 GeV. x_{max} is the highest-xparticle on one side of the event and is not plotted. The jet direction is oriented so that x_{max} is at positive x_{\parallel} . The distributions are normalized to the cross sections for jets with x_{max} within the specified range.
- 19. Particle density distributions $(1/\sigma)d\sigma/dx_{\parallel}$ vs. x_{\parallel} for various x_{max} cuts for jet model Monte Carlo at $E_{c.m.} = 7.3$ GeV.
- 20. Corrected particle density distributions $(1/\sigma)d\sigma/dx_{\parallel}$ vs. x_{\parallel} for $x_{max} > 0.3$ for various $E_{c.m.}$. x_{max} is at positive x_{\parallel} and is not plotted. The distributions are normalized to the cross sections for jets with $x_{max} > 0.3$.
- 21. Corrected particle density distributions $(1/\sigma) d\sigma/dx_{\parallel}$ vs. x_{\parallel} for all events for various $E_{c.m.}$. The distributions are normalized to the total cross sections for multihadronic events.
- 22. Corrected particle density distributions $(1/\sigma)d\sigma/dy$ vs. y for various x_{max} cuts for 7.0 < E < 7.8 GeV. x_{max} is the highest-x particle on one side of the event and is not plotted. The jet direction is oriented so that x_{max} is at positive y. The distributions are normalized to the cross sections for jets with x_{max} within the specified range.

- 23. Corrected particle density distributions $(1/\sigma)d\sigma/dy$ vs. y for $x_{max} > 0.3$ for various $E_{c.m.}$. y is the rapidity of the particle relative to the jet direction assuming a pion mass. x_{max} is at positive y and is not plotted. The distributions are normalized to the cross sections for jets with $x_{max} > 0.3$.
- 24. Corrected $(1/\sigma)d\sigma/dp_{\perp}^2$ vs. p_{\perp}^2 for particles opposite jets with various x_{max} cuts for 7.0 < $E_{c.m.}$ < 7.8 GeV. p_{\perp} is the component of particle momentum perpendicular to the jet direction. The distributions are normalized to the cross sections for jets with x_{max} within the specified range.
- 25. Corrected $(1/\sigma)d\sigma/dp_{\perp}^2$ vs. p_{\perp}^2 for particles opposite (negative x_{\parallel}) jets with $x_{max} > 0.3$ for various $E_{c.m.}$. p_{\perp} is the component of particle momentum perpendicular to the jet direction. The distributions are normalized to the cross sections for jets with $x_{max} > 0.3$. The solid lines represent the fits, discussed in the text, to the distributions for $E_{c.m.} = 3.0$ GeV and $7.0 < E_{c.m.} < 7.8$ GeV.
- 26. Observed $(1/N_{ev}) dN/dp_{\perp}^2$ for particles opposite jets with $x_{max} > 0.3$ in events with 3 or more charged particles. N_{ev} is the number of observed jets with $x_{max} > 0.3$ and dN/dp_{\perp}^2 is the number of particles observed per (GeV/c)² in each p_{\perp}^2 bin.
- 27. Corrected $(1/\sigma)d\sigma/dp_{\perp}$ vs. p_{\perp} for particles opposite jets with $x_{max} > 0.3$ for various $E_{c.m.}$. p_{\perp} is the component of particle momentum perpendicular to the jet direction. The distributions are normalized to the cross sections for jets with $x_{max} > 0.3$.

- 28. Average transverse momentum relative to the jet direction $\langle p_{\perp} \rangle$ for particles opposite jets with $x_{max} > 0.3$ vs. E_{c.m.}.
- 29. Coefficients of p_{\perp}^2 , (a) b_1 and (b) b_2 , for fits of the form $(1/\sigma)d\sigma/dp_{\perp}^2 = c_1 e^{-b_1 p_1^2} + c_2 e^{-b_2 p_2^2}$ for particles opposite jets with $x_{max} > 0.3$ vs. $E_{c.m.}$.
- 30. Comparison of the corrected $(1/\sigma)d\sigma/dp_{\perp}^2$ vs. p_{\perp}^2 for particles opposite jets with $x_{max} > 0.3$ for 7.0 < $E_{c.m.} < 7.8$ GeV with the produced jet model Monte Carlo distribution for all events at $E_{c.m.} = 7.3$ GeV.
- 31. $K^{\pm}\pi^{\mp}$ invariant mass distributions for 7.0 < E_{c.m.} < 7.8 GeV for (a) both particles with p_{\perp} < 0.8 GeV/c and (b) one or both particles with $p_{\perp} \ge 0.8$ GeV/c. p_{\perp} is the component of particle momentum perpendicular to the observed jet axis. No time-of-flight information was used; each combination was plotted twice--once for each mass assignment.
- 32. Observed p_{\perp}^2 distribution for particles opposite jets with $x_{max} > 0.3$ in events with 3 or more charged particles for $7.0 < E_{c.m.} < 7.8$ GeV. p_{\perp} is the component of particle momentum perpendicular to the observed jet axis. The data is compared with the sum of the Monte Carlo predictions of the jet model and a charmed meson production model. The Monte Carlo distribution is normalized to the total number of particles in the data. The relative normalization of the two models was chosen by requiring that the number of high p_{\perp}^2 particles agree with the data.
- 33. Corrected $(1/\sigma)d\sigma/dp_{\perp}^2$ for particules in various x_{\parallel} ranges opposite jets with $x_{max} > 0.3$ for 7.0 < E c.m. < 7.8 GeV. The distributions

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are normalized to the cross section for jets with $x_{max} > 0.3$. The solid lines represent the fits discussed in the text.

- 34. Average transverse momentum relative to the jet direction $\langle p_{\perp} \rangle$ vs. x_{\parallel} for particles opposite jets with $x_{max} > 0.3$ for $7.0 < E_{c.m.} < 7.8$ GeV.
- 35. Coefficients (a) b_1 and (b) b_2 for fits of the form $\begin{array}{c} -b_1 p_1^2 & -b_2 p_1^2 \\ (1/\sigma) d\sigma/dp_1^2 = c_1 e & + c_2 e & \text{vs. } x_{\parallel} \text{ for particles opposite} \\ \text{jets with } x_{\max} > 0.3 \text{ for } 7.0 < E_{c.m.} < 7.8 \text{ GeV.} \end{array}$
- 36. Observed ratio of the number of particles with opposite charge to the x_{max} particle to the number of particles with the same charge as x_{max} for (a) $x_{max} > 0.5$ and (b) $x_{max} > 0.7$ vs. x_{\parallel} for $7.0 < E_{c.m.} < 7.8$ GeV. x_{max} is at positive x_{\parallel} . The statistical expectations, calculated from the charged particle multiplicity distributions for each x_{\parallel} bin, are represented by the dashed lines.





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Fig. 2



Fig. 3





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Fig. 5



Fig. 6







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Fig. 8



Fig. 9







Fig. 11



Fig. 12



Fig. 13











Fig. 16



Fig. 17



Fig. 18







Fig. 20









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Fig. 24













Fig. 28


Fig. 29

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Fig. 34



Fig. 35



