

Study of CP asymmetry in B^0 - \bar{B}^0 mixing with inclusive dilepton events

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We present a measurement of the asymmetry A_{CP} between same-sign inclusive dilepton samples $\ell^+\ell^+$ and $\ell^-\ell^-$ ($\ell = e, \mu$) from semileptonic B decays in $\Upsilon(4S) \rightarrow B\bar{B}$ events, using the complete data set recorded by the BABAR experiment near the $\Upsilon(4S)$ resonance, corresponding to 471 million $B\bar{B}$ pairs. The asymmetry A_{CP} allows comparison between the mixing probabilities $\mathcal{P}(\bar{B}^0 \rightarrow B^0)$ and $\mathcal{P}(B^0 \rightarrow \bar{B}^0)$, and therefore probes CP and T violation. The result, $A_{CP} = (-3.9 \pm 3.5(\text{stat.}) \pm 1.9(\text{syst.})) \times 10^{-3}$, is consistent with the Standard Model expectation.

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A neutral B meson can transform to its antiparticle through the weak interaction. A difference between the probabilities $\mathcal{P}(\bar{B}^0 \rightarrow B^0)$ and $\mathcal{P}(B^0 \rightarrow \bar{B}^0)$ is allowed by the Standard Model (SM), and is a signature of violations of both CP and T symmetries. This type of CP violation, called CP violation in mixing, was first observed in the neutral kaon system [1], but has not been observed in the neutral B system, where the SM predicts an asymmetry of the order of 10^{-4} [2]. The current experimental average of CP asymmetry in mixing measured in the B^0 system alone is $A_{CP} = (+2.3 \pm 2.6) \times 10^{-3}$ [3], dominated by the BABAR [4, 5], DØ [6], and Belle [7] experiments¹. A recent measurement in a mixture of B^0 and B_s^0 mesons by the DØ collaboration deviates from the SM expectation by more than three standard deviations [8]. Improving the experimental precision is crucial for understanding the source of this apparent discrepancy.

The neutral B meson system can be described by an effective Hamiltonian $\mathbf{H} = \mathbf{M} - i\mathbf{\Gamma}/2$ for the two states $|B^0\rangle$ and $|\bar{B}^0\rangle$. Assuming CPT symmetry, the mass eigenstates can be written as $|B_{L/H}\rangle = p|B^0\rangle \pm q|\bar{B}^0\rangle$. If $|q/p| \neq 1$, both CP and T symmetries are violated. Details of the formalism can be found in Refs. [10, 11].

The $B^0\bar{B}^0$ pair created in the $\Upsilon(4S)$ decay evolves coherently until one B meson decays. In this analysis, we use the charge of the lepton (electron or muon) in

semileptonic B decays to identify the flavor of the B meson at the time of its decay. If the second B meson has oscillated to its antiparticle, it will produce a lepton that has the same charge as the lepton from the first B decay. The CP asymmetry A_{CP} between $\mathcal{P}(\bar{B}^0 \rightarrow B^0)$ and $\mathcal{P}(B^0 \rightarrow \bar{B}^0)$ can be measured by the charge asymmetry of the same-sign dilepton event rate $\mathcal{P}_{\ell\ell}^{\pm\pm}$:

$$A_{CP} = \frac{\mathcal{P}_{\ell\ell}^{++} - \mathcal{P}_{\ell\ell}^{--}}{\mathcal{P}_{\ell\ell}^{++} + \mathcal{P}_{\ell\ell}^{--}} = \frac{1 - |q/p|^4}{1 + |q/p|^4}. \quad (1)$$

This asymmetry is independent of the B decay time.

We present herein an updated measurement of A_{CP} using inclusive dilepton events collected by the BABAR detector at the PEP-II asymmetric-energy e^+e^- storage rings at SLAC National Accelerator Laboratory. The data set consists of 471×10^6 $B\bar{B}$ pairs produced at the $\Upsilon(4S)$ resonance peak (on-peak) and 44 fb^{-1} of data collected at a center-of-mass (CM) energy 40 MeV below the peak (off-peak) [12]. Monte Carlo (MC) simulated $B\bar{B}$ events equivalent to 10 times the data set based on EvtGen [13] and GEANT4 [14] with full detector response and event reconstruction are used to test the analysis procedure. The main changes with respect to the previous BABAR analysis [4] include doubling the data set, a higher signal selection efficiency, improved particle identification algorithms, and a time-independent approach instead of a time-dependent analysis.

The BABAR detector is described in detail elsewhere [15]. Events are selected if the two highest-momentum particles in the event are consistent with the electron or muon hypotheses. All quantities are evaluated

¹ The quoted average excludes the DØ inclusive dimuon result [8] and the recently published LHCb result [9].

in the CM frame unless stated otherwise. The higher-momentum and lower-momentum lepton candidates are labeled as 1 and 2, respectively. Four lepton combinations are allowed: $\ell_1\ell_2 = \{ee, e\mu, \mu e, \mu\mu\}$, as are four charge combinations, for a total of 16 subsamples. We assume e - μ universality, i.e., equal A_{CP} for all $\ell_1\ell_2$ combinations. The time-integrated signal yields can be written as [16]

$$N_{\ell_1\ell_2}^{\pm\pm} = \frac{1}{2}N_{\ell_1\ell_2}^0(1 \pm a_{\ell_1} \pm a_{\ell_2} \pm A_{CP})\chi_d^{\ell_1\ell_2}, \quad (2)$$

$$N_{\ell_1\ell_2}^{\pm\mp} = \frac{1}{2}N_{\ell_1\ell_2}^0(1 \pm a_{\ell_1} \mp a_{\ell_2})(1 - \chi_d^{\ell_1\ell_2} + r_B), \quad (3)$$

in the limit of $A_{CP} \ll 1$ and $a_{\ell_j} \ll 1$, where $a_{\ell_j} = (\epsilon_{\ell_j}^+ - \epsilon_{\ell_j}^-)/(\epsilon_{\ell_j}^+ + \epsilon_{\ell_j}^-)$ is the average charge asymmetry

of the detection efficiency for lepton j , r_B is the B^+/B^0 event ratio, $\chi_d^{\ell_1\ell_2}$ is the effective mixing probability of neutral B mesons including efficiency corrections, and $N_{\ell_1\ell_2}^0$ is the neutral B signal yield for the $\ell_1\ell_2$ flavor combination.

A small fraction of the background comes from $e^+e^- \rightarrow f\bar{f}(\gamma)$ continuum events ($f \in \{u, d, s, c, e, \mu, \tau\}$). This contribution is subtracted using the off-peak data and the integrated luminosity ratio [12] between the on-peak and off-peak data sets. The remaining background comes from $B\bar{B}$ events, where at least one lepton candidate originates from $B \rightarrow X \rightarrow \ell Y$ cascade decays, or from a hadron misidentified as a lepton.

Including the background, we expand Eqs.(2,3) to parameterize the total observed numbers of events as

$$M_{\ell_1\ell_2}^{\pm\pm} = \frac{1}{2}N_{\ell_1\ell_2}^0(1 + R_{\ell_1\ell_2}^{\pm\pm})\left[1 \pm a_{\ell_1} \pm a_{\ell_2} \pm \frac{1 + \delta_{\ell_1\ell_2}R_{\ell_1\ell_2}^{\pm\pm}}{1 + R_{\ell_1\ell_2}^{\pm\pm}}A_{CP}\right]\chi_d^{\ell_1\ell_2}, \quad (4)$$

$$M_{\ell_1\ell_2}^{\pm\mp} = \frac{1}{2}N_{\ell_1\ell_2}^0(1 + R_{\ell_1\ell_2}^{\pm\mp})(1 \pm a_{\ell_1} \mp a_{\ell_2})(1 - \chi_d^{\ell_1\ell_2} + r_B), \quad (5)$$

where $R_{\ell_1\ell_2}^{\pm\pm}$ and $R_{\ell_1\ell_2}^{\pm\mp}$ are background-to-signal ratios under the condition $A_{CP} = 0$, and $\delta_{\ell_1\ell_2}$ is the probability of a same-sign background event being consistent with the flavors of the neutral B pairs at the time of their decay after B^0 - \bar{B}^0 mixing, i.e., $\ell^+\ell^+$ ($\ell^-\ell^-$) for B^0B^0 ($\bar{B}^0\bar{B}^0$), minus the probability of the opposite case, i.e., $\ell^+\ell^+$ ($\ell^-\ell^-$) for \bar{B}^0B^0 ($B^0\bar{B}^0$). The detailed derivation can be found in the supplemental material [16]. For the opposite-sign events, signal is CP symmetric. The background originating from B^0B^0 ($\bar{B}^0\bar{B}^0$) preferably contributes to $\ell^+\ell^-$ ($\ell^-\ell^+$) because a primary lepton tends to have a higher momentum than a cascade lepton. Therefore, the background yield is also a function of A_{CP} . However, the coefficient of A_{CP} is less than 0.01 for the final data sample, so it is ignored in the fits.

Events with ≥ 1 lepton (single-lepton sample) are used to constrain the charge asymmetry of the detector efficiency $a_\ell \equiv (a_{\ell_1} + a_{\ell_2})/2$. The inclusive single-lepton asymmetry a_{on} in on-peak data can be expressed as [16]

$$a_{\text{on}} = \alpha + \beta\chi_d A_{CP} + \gamma a_\ell, \quad (6)$$

where parameters α , β , and γ are functions of the following quantities: the fractions and asymmetries of the continuum background, misidentified leptons, and cascade leptons; the B^0/B^+ ratio; and $w_{B^0}^{\text{casc}}$ the probability of the cascade-lepton's charge incorrectly identifying the B flavor at the time of the B decay.

We build a χ^2 fit using the 8+8+1 equations represented by Eqs. (4)–(6) to extract A_{CP} . For the single-lepton sample, we use only electrons since the purity is much higher than that of muons.

The event selection requires ≥ 4 charged particle tracks and the normalized second-order Fox-Wolfram moment [17] $R_2 < 0.6$. The leptons should satisfy $0.6 \text{ GeV} < p_{\ell_2} \leq p_{\ell_1} < 2.2 \text{ GeV}$. The polar angle θ of the electron (muon) candidate in the laboratory frame is required to satisfy $-0.788 < \cos\theta < 0.961$ ($-0.755 < \cos\theta < 0.956$). The lepton is rejected if, when combined with another lepton of opposite charge, the invariant mass is consistent with that of a J/ψ or a $\psi(2S)$ meson, or when arising from a photon conversion. The lepton tracks must pass a set of quality requirements. For dilepton events, the invariant mass of the lepton pair must be greater than 150 MeV. The proper decay time difference Δt of the two B mesons can be determined from the distance along the collision axis between the points of closest approach of the lepton tracks to the beam spot, and the boost factor ($\simeq 0.56$) of the CM frame. We require $|\Delta t| < 15$ ps and its uncertainty $\sigma_{\Delta t} < 3$ ps.

Electrons and muons are identified by two separate multivariate algorithms that predominately use the shower shape and energy deposition in the electromagnetic calorimeter for electrons, and the track path length and cluster shape in the instrumented flux return for muons. The electron (muon) identification efficiency is approximately 93% (40%–80% depending on momentum). The probability of a hadron being identified as an electron (muon) is $< 0.1\%$ ($\sim 1\%$).

To further suppress background, we use random forest multivariate classifiers [18]. Off-peak data are used to represent continuum events, and simulated events are used for signal and $B\bar{B}$ background. In the dilepton sam-

ple, we use six variables: p_{ℓ_1} , p_{ℓ_2} , thrust and sphericity [19] of the rest of the event, the opening angle θ_{12} of the two tracks in the CM frame, and Δt . Separate classifiers are trained on the same-sign and opposite-sign samples. The ee , $e\mu$, μe , and $\mu\mu$ samples are also trained separately. The dilepton signal probability distributions of the classifiers are shown in Fig. 1. We select events with a probability > 0.7 to minimize the statistical uncertainty based on fits to the $B\bar{B}$ MC sample. The final on-peak data sample includes 2.5% continuum background for all dilepton samples, and 35% (8%) $B\bar{B}$ background in the same-sign (opposite-sign) sample.

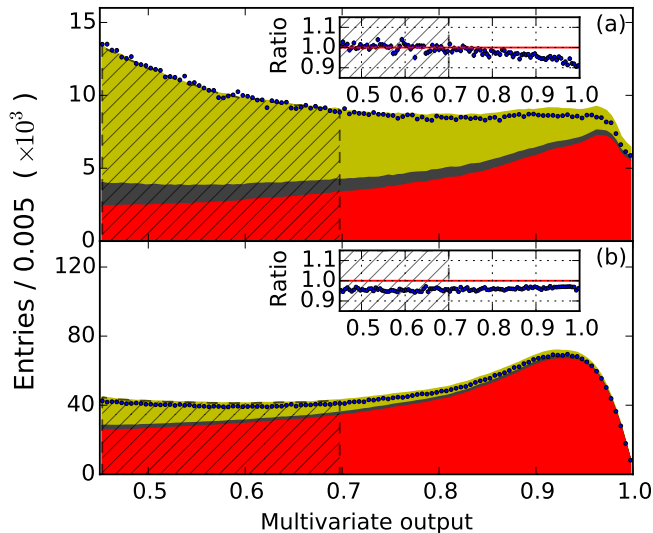


FIG. 1. (Color online) Signal probability distributions from the dilepton multivariate algorithm for (a) the same-sign sample and (b) the opposite-sign sample; all lepton flavors are combined. Points are continuum-subtracted data; shaded regions from bottom to top are for signal, $B\bar{B}$ background with ≥ 1 misidentified lepton, and $B\bar{B}$ background with both real leptons. Hatched region is rejected. Data/MC ratios are shown in inset plots. Regions below 0.45 are not shown.

Approximately 0.1% (3%) of selected electrons (muons) in dilepton samples are misidentified. According to the simulation, nearly 98% of the misidentified electrons come from pions and 87% (12%) of the misidentified muons come from pions (kaons). To correct for the difference in the muon misidentification rates between data and MC samples, we study the muon identification efficiency in clean kaon and pion control samples from the process $D^{*+} \rightarrow D^0\pi^+$ followed by $D^0 \rightarrow K^-\pi^+$ (and the charge-conjugate process). The ratios of the efficiencies between data and MC samples are used to scale the misidentified muon component in the MC sample. The corrections to μ^+ (μ^-) is 0.792 ± 0.012 (0.797 ± 0.013). Since the misidentification rate is very low for electrons, we use a much larger pion control sample from $K_S^0 \rightarrow \pi^+\pi^-$ decays. This control sample has a lower momentum spectrum and does not cover the region of

$p > 2.5$ GeV in the laboratory frame, which accounts for less than 8% of the misidentified leptons. The corrections to misidentified e^+ (e^-) is 1.00 ± 0.10 (0.56 ± 0.10). The quoted uncertainties are conservative estimates that result from mismatched momentum spectra and from a small fraction of kaons and protons among misidentified electrons.

For the single-lepton sample, the random forest algorithm uses the number of tracks, the event thrust, R_2 , the difference between the observed energy in the event and the sum of the e^+e^- beam energies, the cosines of the angles between the lepton and the axes of the thrust and the sphericity of the rest of the event, and the zeroth-order and second-order polynomial moments L_0 and L_2 , where $L_n = \sum p_i (\cos \theta_i)^n$, p_i is the momentum of a particles in the rest of the event and θ_i is the angle between that particle and the single-lepton candidate. We optimize the selection requirement by minimizing the uncertainty of the charge asymmetry after the continuum component is subtracted from the on-peak data. A total of 8.5×10^7 single electrons are selected in the on-peak data, of which approximately 63% are from direct semileptonic B decays. Finally, the single electrons are randomly sampled so that the signal momentum spectrum matches that of the dilepton events.

Raw asymmetries of the single electrons in the on- and off-peak data are found to be $a_{\text{on}} = (4.16 \pm 0.14) \times 10^{-3}$ and $a_{\text{off}} = (11.1 \pm 1.4) \times 10^{-3}$. The larger asymmetry in the off-peak data is primarily due to the radiative Bhabha background and the larger detector acceptance in the backward (positron-beam) direction. The continuum fraction $f_{\text{cont}} = (10.32 \pm 0.02)\%$ is obtained from the ratio of the selected single electrons and the integrated luminosities in off- and on-peak data [12]. The neutral B fraction in the $B\bar{B}$ component $f_{B^0} = (48.5 \pm 0.6)\%$ is the $\Upsilon(4S) \rightarrow B^0\bar{B}^0$ branching fraction [20] corrected for the selection efficiency. The cascade event fractions $f_{B^0}^{\text{casc}} = 19.8\%$ and $f_{B^\pm}^{\text{casc}} = 15.3\%$ are obtained from simulation, with negligible statistical uncertainties. The fraction of the misidentified electron is 0.19%, and the asymmetry is approximately 35%. The difference between direct and cascade electron asymmetries is $(-1.16 \pm 0.25) \times 10^{-3}$ in MC. The probability $w_{B^0}^{\text{casc}}$ in MC is found to be $(73.8 \pm 0.1)\%$. Using these numerical values, we determine the coefficients in Eq. (6): $a_{\text{on}} - \alpha = (2.60 \pm 0.20) \times 10^{-3}$, $\beta\chi_d = 0.057 \pm 0.001$, and $\gamma = 0.8951 \pm 0.0002$.

The fitting procedure is tested on the $B\bar{B}$ MC sample; the result $A_{CP}^{\text{MC}} = (-1.00 \pm 1.04) \times 10^{-3}$ is consistent with the CP -symmetric simulation model. We artificially create a non-zero A_{CP} by reweighing mixed events in the MC sample, and confirm that the fitting procedure tracks the change in the A_{CP} without bias. The continuum-subtracted event yields are shown in Table I and are used in Eqs. (4-5) for the fit. The result of the fit to data, after correcting for the small bias (-1.0×10^{-3}) in the simula-

TABLE I. Continuum-subtracted number of events.

	$\ell^+\ell^+$	$\ell^+\ell^-$	$\ell^-\ell^+$	$\ell^-\ell^-$
ee	$82\,303 \pm 320$	$426\,296 \pm 783$	$425\,309 \pm 782$	$81\,586 \pm 323$
$e\mu$	$55\,277 \pm 263$	$384\,552 \pm 684$	$378\,261 \pm 660$	$55\,878 \pm 264$
μe	$67\,399 \pm 290$	$467\,591 \pm 737$	$475\,363 \pm 744$	$67\,152 \pm 290$
$\mu\mu$	$47\,384 \pm 243$	$277\,936 \pm 619$	$278\,691 \pm 618$	$48\,145 \pm 247$

tion, is $A_{CP} = (-3.9 \pm 3.5) \times 10^{-3}$, $a_{e_1} = (3.4 \pm 0.6) \times 10^{-3}$, $a_{e_2} = (3.0 \pm 0.6) \times 10^{-3}$, $a_{\mu_1} = (-5.6 \pm 1.1) \times 10^{-3}$, and $a_{\mu_2} = (-6.5 \pm 1.1) \times 10^{-3}$. The remaining free parameters are $N_{\ell_1\ell_2}^0$ and $\chi_d^{\ell_1\ell_2}$. The χ^2 value is 6.2 for 4 degrees of freedom. The correlations between A_{CP} and a_{e_1} , a_{e_2} , a_{μ_1} , and a_{μ_2} are -0.41 , -0.47 , -0.54 , and -0.51 , respectively. Correlations among other parameters are negligible. Figure 2 shows the fit results for the six data-taking periods and the four flavor subsamples.

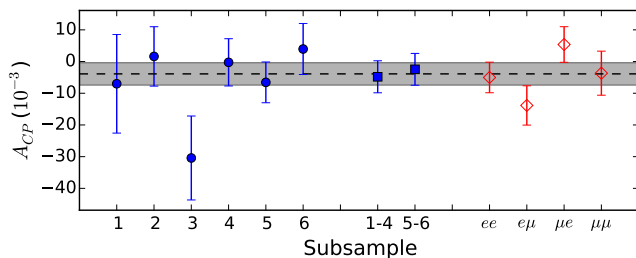


FIG. 2. (Color online) A_{CP} of the six data-taking periods (dots), the first four and the last two periods (squares), and the four flavor subsamples (rhombuses). The horizontal band is the $\pm 1\sigma$ region of the final fit result. All error bars are statistical only.

The systematic uncertainties are summarized in Table II. The branching fractions in the B decay chain partially determine the background-to-signal ratio. We correct the MC samples so that important branching fractions are consistent with the world average [20]. These branching fractions correspond to inclusive B semileptonic decays, $B \rightarrow \tau\nu_\tau X$, charm production (D^0 , \bar{D}^0 , D^\pm , D_s^\pm , Λ_c^+ , and $\bar{\Lambda}_c^-$) from B decays, and inclusive charm semileptonic decays. The corrections vary for most decays between 0.57 and 1.32, depending on the channel. We estimate the systematic uncertainty by varying the corrections over their uncertainties, which are dominated by the errors of the world averages.

The systematic uncertainties due to misidentified leptons are estimated by varying the uncertainties of the corrections to e^+ , e^- , μ^+ , and μ^- individually, and separately for the dilepton and single-electron samples.

In the single-electron MC sample, the charge asymmetry of the electron in $B^0\bar{B}^0$ is slightly different from that in B^+B^- by $(0.46 \pm 0.18) \times 10^{-3}$. Since we cannot separate B^+B^- electrons from $B^0\bar{B}^0$ electrons in data, the single-electron asymmetry measurement is the average of the two asymmetries, which is half the difference away

from the $B^0\bar{B}^0$ electron charge asymmetry. The systematic uncertainty is determined by the change in A_{CP} after shifting the asymmetry in the signal component of the single-electron sample by half the charge asymmetry difference.

The difference in charge asymmetry between the direct and the cascade electrons is found to be $a_e^{\text{casc}} - a_e^{\text{dir}} = (-1.16 \pm 0.25) \times 10^{-3}$ in the single-electron MC sample. The difference between the lower-momentum and the higher-momentum electron asymmetries is negative. This trend is consistent with the result of the fit to the dilepton data: $a_{e_2} - a_{e_1} = (-0.4 \pm 0.7) \times 10^{-3}$. For muons, the corresponding values are $a_\mu^{\text{casc}} - a_\mu^{\text{dir}} = (-0.47 \pm 0.28) \times 10^{-3}$ and $a_{\mu_2} - a_{\mu_1} = (-0.9 \pm 1.2) \times 10^{-3}$. In each case, we set the cascade lepton charge asymmetry to that of the direct lepton, and use the change in A_{CP} as a systematic uncertainty.

The background-to-signal ratios $R_{\ell_1\ell_2}^{\pm\pm}$ and $R_{\ell_1\ell_2}^{\pm\mp}$ (under the condition $A_{CP} = 0$) in the dilepton sample are determined from the MC sample. The correction for the misidentified lepton background has been dealt with above. The real lepton portion of the ratio is in principle the same between $\ell^+\ell^+$ and $\ell^-\ell^-$ samples because the particle identification efficiencies cancel between the background and the signal. In the MC sample, they are consistent within 1σ . Varying $R_{\ell_1\ell_2}^{++}$ and $R_{\ell_1\ell_2}^{--}$ or $R_{\ell_1\ell_2}^{+-}$ and $R_{\ell_1\ell_2}^{-+}$ simultaneously in the same direction results in negligible changes in A_{CP} . If they are varied independently, the quadratic sum of the changes in A_{CP} is larger. We use the latter as a systematic uncertainty.

The random forest output distribution in the data could be different from that in the MC sample. The selection efficiency in the MC $B\bar{B}$ dilepton events is approximately 2% larger than that in the data. We move the dilepton random forest selection for the MC sample, while keeping data the same, so that the selected MC events are reduced by up to 6%. We take the average change in A_{CP} as a systematic uncertainty.

Several other sources of systematic uncertainties are studied and found to be negligible. These include the overall dilepton signal fraction estimate, the kinematic difference between on-peak and off-peak data due to different CM energies, the continuum component fraction, the probability $w_{B^0}^{\text{casc}}$, the neutral-to-charged B ratio, the same-sign background dilution factors $\delta_{\ell_1\ell_2}$, and the overall cascade event fraction.

In conclusion, we measure the CP asymmetry $A_{CP} = (-3.9 \pm 3.5 \pm 1.9) \times 10^{-3}$ in $B^0\bar{B}^0$ mixing using inclusive dilepton decays. This result is consistent with the SM prediction and the world average [3]. This measurement represents a significant improvement with respect to our previous result [4] (superseded by this result), and is among the most precise measurements [9, 20]. A Comparison of experimental results and averages is shown in Fig. 3.

We are grateful for the excellent luminosity and ma-

TABLE II. Summary of systematic uncertainties on A_{CP} .

Source	(10^{-3})
Generic MC bias correction	1.04
MC branching fractions	0.43
Misidentified lepton corrections in dilepton events	0.77
Misidentified e correction in single electron events	0.65
Neutral/charged B difference	0.74
Direct-/cascade e asymmetry difference	0.44
Direct-/cascade μ asymmetry difference	0.34
Background-to-signal ratios	0.68
Random forest cut efficiency	0.08
Total	1.90

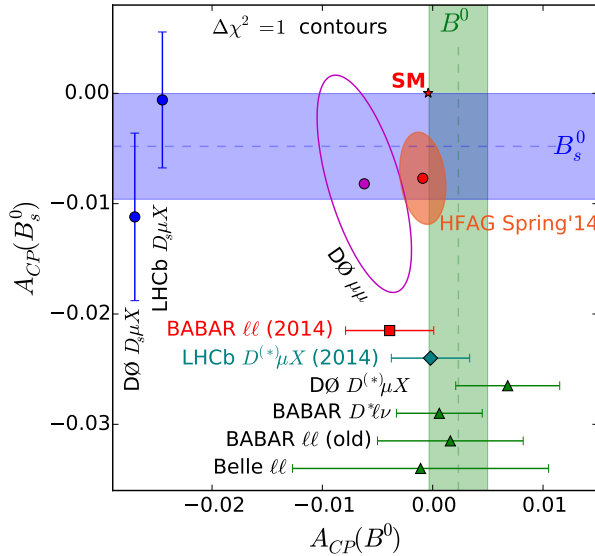


FIG. 3. (Color online) Measurements of CP asymmetry in neutral B mixing, including this measurement (red square), recent LHCb result [9] (teal rhombus), Refs. [4–7] (B^0 ; green triangles), Refs. [21, 22] (B_s^0 ; blue dots), and Ref. [8] (B^0 , B_s^0 mixture; magenta contour). The vertical band is the average of Refs. [4–7] and several other older measurements (not shown). The horizontal band is the average of Refs. [21, 22]. The world average “HFAG Spring ’14” [3] is also shown (orange contour).

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Study of CP asymmetry in B^0 - \bar{B}^0 mixing with inclusive dilepton events

Supplemental material

The *BABAR* Collaboration

DILEPTON EVENT YIELDS

The probability of a neutral B pair producing a same-sign or opposite-sign dilepton pair through two semileptonic B decays is

$$\mathcal{P}^{\pm\pm}(\Delta t) \propto e^{-\Gamma|\Delta t|} |q/p|^{\mp 2} [\cosh(\Delta\Gamma\Delta t/2) - \cos(\Delta m\Delta t)] \quad (1)$$

$$\mathcal{P}^{\pm\mp}(\Delta t) \propto e^{-\Gamma|\Delta t|} [\cosh(\Delta\Gamma\Delta t/2) + \cos(\Delta m\Delta t)]. \quad (2)$$

The asymmetry of the same-sign event

$$A_{CP} = \frac{\mathcal{P}(\Delta t)^{++} - \mathcal{P}(\Delta t)^{--}}{\mathcal{P}(\Delta t)^{++} + \mathcal{P}(\Delta t)^{--}} = \frac{|p/q|^2 - |q/p|^2}{|p/q|^2 + |q/p|^2}. \quad (3)$$

At the limit of $A_{CP} \ll 1$, we have $|q/p|^{\mp 2} = (1 \pm A_{CP})$. Integrating over Δt , we have $\mathcal{P}^{\pm\pm} \propto (1 \pm A_{CP})\chi_d$ and $\mathcal{P}^{\pm\mp} \propto (1 - \chi_d)$, where χ_d is the integrated mixing probability. Next, we consider the charge asymmetry $a_{\ell_j} = (\epsilon_{\ell_j}^+ - \epsilon_{\ell_j}^-)/(\epsilon_{\ell_j}^+ + \epsilon_{\ell_j}^-)$ for lepton ℓ_j , where $\epsilon_{\ell_j}^\pm$ is the reconstruction efficiency of ℓ_j^\pm . For each lepton, a factor of $(1 \pm a_{\ell_j})$ is included, depending on its charge. Since we do not separate charged B and neutral B , and B^+B^- events do not mix and always produce opposite-sign lepton pairs, we add a term r_B to $\mathcal{P}^{\pm\mp}$, where r_B is the ratio of B^+B^- to $B^0\bar{B}^0$ events. Therefore, we can write

$$\mathcal{P}^{\pm\pm} \propto (1 \pm a_{\ell_1} \pm a_{\ell_2} \pm A_{CP})\chi_d, \quad (4)$$

$$\mathcal{P}^{\pm\mp} \propto (1 \pm a_{\ell_1} \mp a_{\ell_2})(1 - \chi_d + r_B), \quad (5)$$

where we have used $a_{\ell_j} \ll 1$.

We then sum over all $B\bar{B}$ events and let $N_{\ell_1\ell_2}^0$ be the total time-integrated $B^0\bar{B}^0$ dilepton signal yield for one of the four lepton flavor combinations $\ell_1\ell_2 \in \{ee, e\mu, \mu e, \mu\mu\}$. We obtain the dilepton signal event yields

$$N_{\ell_1\ell_2}^{\pm\pm} = \frac{1}{2} N_{\ell_1\ell_2}^0 (1 \pm a_{\ell_1} \pm a_{\ell_2} \pm A_{CP}) \chi_d^{\ell_1\ell_2}, \quad (6)$$

$$N_{\ell_1\ell_2}^{\pm\mp} = \frac{1}{2} N_{\ell_1\ell_2}^0 (1 \pm a_{\ell_1} \mp a_{\ell_2})(1 - \chi_d^{\ell_1\ell_2} + r_B), \quad (7)$$

where $\chi_d^{\ell_1\ell_2}$ is the effective mixing probability after considering the slight difference between the same-sign and the opposite-sign event selection efficiencies. We also change the interpretation of a_{ℓ_j} from the charge asymmetry of individual ℓ_j to the average charge asymmetry of ℓ_j over its momentum spectrum.

The measured events in data contain background, $M_{\ell_1\ell_2}^{\pm\pm} = N_{\ell_1\ell_2}^{\pm\pm}/f_{\ell_1\ell_2}^{\pm\pm}$, where $f = N_S/(N_S + N_B)$ is the signal fraction. We estimate the signal N_S and the background N_B from simulation. However, if A_{CP} is non-zero in data, N_S and N_B will be incorrect since the simulation assumes $A_{CP} = 0$. So the same-sign signal yield should be parameterized as $N_{S;\ell_1\ell_2}^{\pm\pm}(1 \pm A_{CP})$. For the same-sign background, some events have the lepton pair charge consistent with that of being from a mixed B^0B^0 or $\bar{B}^0\bar{B}^0$ pair decay, for example, $B^0 \rightarrow \ell^+X$ and the other $B^0 \rightarrow D^+D^-$ with $D^+ \rightarrow \ell^+Y$. Some have a pair of the wrong charge, for example, both $B^0 \rightarrow \bar{D}^0\pi^+$ with $\bar{D}^0 \rightarrow \ell^-X$. Therefore, the background same-sign event yield can be parameterized as $N_{B;\ell_1\ell_2}^{\pm\pm}(1 \pm \delta_{\ell_1\ell_2}A_{CP})$, where $\delta_{\ell_1\ell_2}$ is a dilution factor: $\delta = (n_c - n_w)/N_B$, where N_B is the total number of the same-sign background events, including mixed and unmixed events, and n_c (n_w) is the number of mixed events that produce a same-sign background lepton pair with charges consistent with (opposite to) the signal leptons from a mixed event.

Using these parameterizations, and letting the background-to-signal ratio under the condition $A_{CP} = 0$ be $R_{\ell_1\ell_2}^{\pm\pm} = N_{B;\ell_1\ell_2}^{\pm\pm}/N_{S;\ell_1\ell_2}^{\pm\pm}$, we can express the same-sign event yield as

$$M_{\ell_1\ell_2}^{\pm\pm} = \frac{1}{2} \left(N_{\ell_1\ell_2}^0 (1 \pm a_{\ell_1} \pm a_{\ell_2} \pm A_{CP}) \chi_d^{\ell_1\ell_2} \right) \frac{(1 \pm A_{CP}) + R_{\ell_1\ell_2}^{\pm\pm} (1 \pm \delta_{\ell_1\ell_2}A_{CP})}{1 \pm A_{CP}} \quad (8)$$

$$= \frac{1}{2} N_{\ell_1 \ell_2}^0 (1 \pm a_{\ell_1} \pm a_{\ell_2}) [1 \pm A_{CP} + R_{\ell_1 \ell_2}^{\pm\pm} (1 \pm \delta_{\ell_1 \ell_2} A_{CP})] \chi_d^{\ell_1 \ell_2} \quad (9)$$

$$= \frac{1}{2} N_{\ell_1 \ell_2}^0 (1 \pm a_{\ell_1} \pm a_{\ell_2}) [1 + R_{\ell_1 \ell_2}^{\pm\pm} \pm (1 + \delta_{\ell_1 \ell_2} R_{\ell_1 \ell_2}^{\pm\pm}) A_{CP}] \chi_d^{\ell_1 \ell_2} \quad (10)$$

$$= \frac{1}{2} N_{\ell_1 \ell_2}^0 (1 + R_{\ell_1 \ell_2}^{\pm\pm}) \left[1 \pm a_{\ell_1} \pm a_{\ell_2} \pm \frac{1 + \delta_{\ell_1 \ell_2} R_{\ell_1 \ell_2}^{\pm\pm}}{1 + R_{\ell_1 \ell_2}^{\pm\pm}} A_{CP} \right] \chi_d^{\ell_1 \ell_2}. \quad (11)$$

Here we have again used $A_{CP} \ll 1$ and $a_{\ell_j} \ll 1$, and only kept the first-order terms in A_{CP} and a_{ℓ_j} . For the opposite-sign events, the signal events come from unmixed events and do not have CP asymmetry. A small fraction of background comes from mixed events. A mixed $B^0 B^0$ event contributes preferably to $\ell^+ \ell^-$ than to $\ell^- \ell^+$ samples because a primary lepton tends to have a higher momentum than a cascade lepton. Therefore, the background event yield should be parameterized similar to the same-sign background $N_{B^0, \ell_1 \ell_2}^{\pm\mp} (1 \pm \delta_{\ell_1 \ell_2}^{\text{os}} A_{CP})$. Let $R_{\ell_1 \ell_2}^{\pm\mp} = N_{B^0, \ell_1 \ell_2}^{\pm\mp} / N_{S^0, \ell_1 \ell_2}^{\pm\mp}$ and ignore the higher order of a_{ℓ_j} and A_{CP} , we can express the opposite-sign event yield as

$$M_{\ell_1 \ell_2}^{\pm\mp} = \frac{1}{2} N_{\ell_1 \ell_2}^0 (1 \pm a_{\ell_1} \mp a_{\ell_2}) [1 + R_{\ell_1 \ell_2}^{\pm\mp} (1 \pm \delta_{\ell_1 \ell_2}^{\text{os}} A_{CP})] (1 - \chi_d^{\ell_1 \ell_2} + r_B) \quad (12)$$

$$= \frac{1}{2} N_{\ell_1 \ell_2}^0 (1 \pm a_{\ell_1} \mp a_{\ell_2}) [1 + R_{\ell_1 \ell_2}^{\pm\mp} \pm \delta_{\ell_1 \ell_2}^{\text{os}} R_{\ell_1 \ell_2}^{\pm\mp} A_{CP}] (1 - \chi_d^{\ell_1 \ell_2} + r_B) \quad (13)$$

$$= \frac{1}{2} N_{\ell_1 \ell_2}^0 (1 + R_{\ell_1 \ell_2}^{\pm\mp}) \left[1 \pm a_{\ell_1} \mp a_{\ell_2} \pm \frac{\delta_{\ell_1 \ell_2}^{\text{os}} R_{\ell_1 \ell_2}^{\pm\mp}}{1 + R_{\ell_1 \ell_2}^{\pm\mp}} A_{CP} \right] (1 - \chi_d^{\ell_1 \ell_2} + r_B). \quad (14)$$

The coefficient of A_{CP} is less than 0.01 in the final data sample, therefore we can safely ignore it in the fit model.

SINGLE LEPTON ASYMMETRY

For the single lepton asymmetry, in the following equations, the various a 's are sample asymmetries indicated by the sub- and super-scripts. The subscripts "on", "cont", and B represent on-peak, continuum, and B samples (or components), respectively. The superscripts "dir", "casc", and "fake" represent direct, cascade, and misidentified lepton components, respectively. The relations between the on-peak single lepton asymmetry as well as the detector efficiency asymmetry and A_{CP} can be written as

$$a_{\text{on}} = f_{\text{cont}} a_{\text{cont}} + (1 - f_{\text{cont}}) a_B, \quad (15)$$

$$a_B = f_{B^0} a_{B^0} + (1 - f_{B^0}) a_{B^\pm}, \quad (16)$$

$$a_{B^0} = f_{B^0}^{\text{fake}} a_{B^0}^{\text{fake}} + f_{B^0}^{\text{casc}} a_{B^0}^{\text{casc}} + (1 - f_{B^0}^{\text{fake}} - f_{B^0}^{\text{casc}}) a_{B^0}^{\text{dir}}, \quad (17)$$

$$a_{B^\pm} = f_{B^\pm}^{\text{fake}} a_{B^\pm}^{\text{fake}} + f_{B^\pm}^{\text{casc}} a_{B^\pm}^{\text{casc}} + (1 - f_{B^\pm}^{\text{fake}} - f_{B^\pm}^{\text{casc}}) a_{B^\pm}^{\text{dir}}, \quad (18)$$

where

$$a_{B^0}^{\text{dir}} = \chi_d A_{CP} + a_\ell^{\text{dir}}, \quad (19)$$

$$a_{B^0}^{\text{casc}} = (1 - 2w_{B^0}^{\text{casc}}) \chi_d A_{CP} + a_\ell^{\text{casc}}, \quad (20)$$

$$a_{B^\pm}^{\text{dir}} = a_\ell^{\text{dir}}, \quad (21)$$

$$a_{B^\pm}^{\text{casc}} = a_\ell^{\text{casc}}, \quad (22)$$

with $w_{B^0}^{\text{casc}}$ the probability of the wrong B flavor being tagged by the charge of the cascade lepton. We are particularly interested in a_e^{dir} . Thus we create a function

$$a_{\text{on}} = \alpha + \beta \chi_d A_{CP} + \gamma a_e^{\text{dir}}. \quad (23)$$

Assuming $a_{B^0}^{\text{fake}} = a_{B^\pm}^{\text{fake}} = a_B^{\text{fake}}$ and $f_{B^0}^{\text{fake}} = f_{B^\pm}^{\text{fake}} = f_B^{\text{fake}}$, and letting $\delta_e^{\text{casc}} = a_e^{\text{casc}} - a_e^{\text{dir}}$, we expand a_B ,

$$\begin{aligned} a_B &= f_{B^0} a_{B^0} + (1 - f_{B^0}) a_{B^\pm} \\ &= f_{B^0} [f_B^{\text{fake}} a_B^{\text{fake}} + f_{B^0}^{\text{casc}} a_{B^0}^{\text{casc}} + (1 - f_B^{\text{fake}} - f_{B^0}^{\text{casc}}) a_{B^0}^{\text{dir}}] \\ &\quad + (1 - f_{B^0}) [f_B^{\text{fake}} a_B^{\text{fake}} + f_{B^\pm}^{\text{casc}} a_{B^\pm}^{\text{casc}} + (1 - f_B^{\text{fake}} - f_{B^\pm}^{\text{casc}}) a_{B^\pm}^{\text{dir}}] \\ &= f_B^{\text{fake}} a_B^{\text{fake}} + f_{B^0} f_{B^0}^{\text{casc}} a_{B^0}^{\text{casc}} + f_{B^0} (1 - f_B^{\text{fake}} - f_{B^0}^{\text{casc}}) a_{B^0}^{\text{dir}} \\ &\quad + (1 - f_{B^0}) f_{B^\pm}^{\text{casc}} a_{B^\pm}^{\text{casc}} + (1 - f_{B^0}) (1 - f_B^{\text{fake}} - f_{B^\pm}^{\text{casc}}) a_{B^\pm}^{\text{dir}} \end{aligned} \quad (24)$$

$$\begin{aligned}
&= f_B^{\text{fake}} a_B^{\text{fake}} + f_{B^0} f_{B^0}^{\text{casc}} [(1 - 2w_{B^0}^{\text{casc}}) \chi_d A_{CP} + a_e^{\text{casc}}] \\
&\quad + f_{B^0} (1 - f_B^{\text{fake}} - f_{B^0}^{\text{casc}}) (\chi_d A_{CP} + a_e^{\text{dir}}) \\
&\quad + (1 - f_{B^0}) f_{B^\pm}^{\text{casc}} a_e^{\text{casc}} + (1 - f_{B^0}) (1 - f_B^{\text{fake}} - f_{B^\pm}^{\text{casc}}) a_e^{\text{dir}} \\
&= f_B^{\text{fake}} a_B^{\text{fake}} + a_e^{\text{casc}} [f_{B^0} f_{B^0}^{\text{casc}} + (1 - f_{B^0}) f_{B^\pm}^{\text{casc}}] \\
&\quad + \chi_d A_{CP} [f_{B^0} f_{B^0}^{\text{casc}} (1 - 2w_{B^0}^{\text{casc}}) + f_{B^0} (1 - f_B^{\text{fake}} - f_{B^0}^{\text{casc}})] \\
&\quad + a_e^{\text{dir}} [f_{B^0} (1 - f_B^{\text{fake}} - f_{B^0}^{\text{casc}}) + (1 - f_{B^0}) (1 - f_B^{\text{fake}} - f_{B^\pm}^{\text{casc}})] \\
&= f_B^{\text{fake}} a_B^{\text{fake}} + (a_e^{\text{casc}} - a_e^{\text{dir}}) [f_{B^0} f_{B^0}^{\text{casc}} + (1 - f_{B^0}) f_{B^\pm}^{\text{casc}}] \\
&\quad + \chi_d A_{CP} [f_{B^0} f_{B^0}^{\text{casc}} (1 - 2w_{B^0}^{\text{casc}}) + f_{B^0} (1 - f_B^{\text{fake}} - f_{B^0}^{\text{casc}})] \\
&\quad + a_e^{\text{dir}} [f_{B^0} (1 - f_B^{\text{fake}}) + (1 - f_{B^0}) (1 - f_B^{\text{fake}})] \\
&= f_B^{\text{fake}} a_B^{\text{fake}} + \delta_e^{\text{casc}} [f_{B^0} f_{B^0}^{\text{casc}} + (1 - f_{B^0}) f_{B^\pm}^{\text{casc}}] \\
&\quad + \chi_d A_{CP} f_{B^0} [f_{B^0}^{\text{casc}} (1 - 2w_{B^0}^{\text{casc}}) + 1 - f_B^{\text{fake}} - f_{B^0}^{\text{casc}}] \\
&\quad + a_e^{\text{dir}} (1 - f_B^{\text{fake}}).
\end{aligned}$$

Inserting the above expression back into Eqs. (15) and (23), we find

$$\alpha = f_{\text{cont}} a_{\text{cont}} + (1 - f_{\text{cont}}) \{ f_B^{\text{fake}} a_B^{\text{fake}} + \delta_e^{\text{casc}} [f_{B^0} f_{B^0}^{\text{casc}} + (1 - f_{B^0}) f_{B^\pm}^{\text{casc}}] \}, \quad (25)$$

$$\beta = f_{B^0} (1 - f_{\text{cont}}) [f_{B^0}^{\text{casc}} (1 - 2w_{B^0}^{\text{casc}}) + 1 - f_B^{\text{fake}} - f_{B^0}^{\text{casc}}], \quad (26)$$

$$\gamma = (1 - f_{\text{cont}}) (1 - f_B^{\text{fake}}). \quad (27)$$

The fraction f_{cont} is the continuum fraction in the entire on-peak data sample; the fractions f_B^{casc} and f_B^{fake} are the cascade and fake fractions in $B\bar{B}$ events, respectively.