# Search for the decay modes $D^{0} \rightarrow e^{+} e^{-}, D^{0} \rightarrow \mu^{+} \mu^{-}$, and $D^{0} \rightarrow e^{ \pm} \mu^{\mp}$ 

J. P. Lees, V. Poireau, and V. Tisserand Laboratoire d'Annecy-le-Vieux de Physique des Particules (LAPP), Université de Savoie, CNRS/IN2P3, F-74941 Annecy-Le-Vieux, France<br>J. Garra Tico and E. Grauges<br>Universitat de Barcelona, Facultat de Fisica, Departament ECM, E-08028 Barcelona, Spain<br>A. Palano ${ }^{a b}$<br>INFN Sezione di Bari ${ }^{a}$; Dipartimento di Fisica, Università di Bari ${ }^{b}$, I-70126 Bari, Italy<br>G. Eigen and B. Stugu<br>University of Bergen, Institute of Physics, N-5007 Bergen, Norway<br>D. N. Brown, L. T. Kerth, Yu. G. Kolomensky, and G. Lynch<br>Lawrence Berkeley National Laboratory and University of California, Berkeley, California 94720, USA<br>H. Koch and T. Schroeder<br>Ruhr Universität Bochum, Institut für Experimentalphysik 1, D-44780 Bochum, Germany<br>D. J. Asgeirsson, C. Hearty, T. S. Mattison, J. A. McKenna, and R. Y. So<br>University of British Columbia, Vancouver, British Columbia, Canada V6T 1 Z1

A. Khan

Brunel University, Uxbridge, Middlesex UB8 3PH, United Kingdom
V. E. Blinov, A. R. Buzykaev, V. P. Druzhinin, V. B. Golubev, E. A. Kravchenko, A. P. Onuchin, S. I. Serednyakov, Yu. I. Skovpen, E. P. Solodov, K. Yu. Todyshev, and A. N. Yushkov Budker Institute of Nuclear Physics, Novosibirsk 630090, Russia
M. Bondioli, D. Kirkby, A. J. Lankford, and M. Mandelkern

University of California at Irvine, Irvine, California 92697, USA
H. Atmacan, J. W. Gary, F. Liu, O. Long, E. Mullin, and G. M. Vitug University of California at Riverside, Riverside, California 92521, USA
C. Campagnari, T. M. Hong, D. Kovalskyi, J. D. Richman, and C. A. West

University of California at Santa Barbara, Santa Barbara, California 93106, USA
A. M. Eisner, J. Kroseberg, W. S. Lockman, A. J. Martinez, B. A. Schumm, and A. Seiden University of California at Santa Cruz, Institute for Particle Physics, Santa Cruz, California 95064, USA
D. S. Chao, C. H. Cheng, B. Echenard, K. T. Flood, D. G. Hitlin, P. Ongmongkolkul, F. C. Porter, and A. Y. Rakitin California Institute of Technology, Pasadena, California 91125, USA
R. Andreassen, Z. Huard, B. T. Meadows, M. D. Sokoloff, and L. Sun

University of Cincinnati, Cincinnati, Ohio 45221, USA
P. C. Bloom, W. T. Ford, A. Gaz, U. Nauenberg, J. G. Smith, and S. R. Wagner University of Colorado, Boulder, Colorado 80309, USA
R. Ayad* and W. H. Toki

Colorado State University, Fort Collins, Colorado 80523, USA

Submitted to Physical Review D
Work supported by US Department of Energy contract DE-AC02-76SF00515.

## B. Spaan

Technische Universität Dortmund, Fakultät Physik, D-44221 Dortmund, Germany
K. R. Schubert and R. Schwierz

Technische Universität Dresden, Institut für Kern- und Teilchenphysik, D-01062 Dresden, Germany
D. Bernard and M. Verderi

Laboratoire Leprince-Ringuet, Ecole Polytechnique, CNRS/IN2P3, F-91128 Palaiseau, France
P. J. Clark and S. Playfer

University of Edinburgh, Edinburgh EH9 3JZ, United Kingdom
D. Bettoni ${ }^{a}$, C. Bozzi $^{a}$, R. Calabrese ${ }^{a b}$, G. Cibinetto ${ }^{a b}$, E. Fioravanti ${ }^{a b}$, I. Garzia ${ }^{a b}$, E. Luppi ${ }^{a b}$, M. Munerato ${ }^{a b}$, L. Piemontese ${ }^{a}$, and V. Santoro ${ }^{a}$

INFN Sezione di Ferrara ${ }^{a}$; Dipartimento di Fisica, Università di Ferrara ${ }^{b}$, I-44100 Ferrara, Italy
R. Baldini-Ferroli, A. Calcaterra, R. de Sangro, G. Finocchiaro,
P. Patteri, I. M. Peruzzi, ${ }^{\dagger}$ M. Piccolo, M. Rama, and A. Zallo INFN Laboratori Nazionali di Frascati, I-00044 Frascati, Italy
R. Contri ${ }^{a b}$, E. Guido ${ }^{a b}$, M. Lo Vetere ${ }^{a b}$, M. R. Monge ${ }^{a b}$, S. Passaggio ${ }^{a}$, C. Patrignani ${ }^{a b}$, and E. Robutti ${ }^{a}$ INFN Sezione di Genova ${ }^{a}$; Dipartimento di Fisica, Università di Genova ${ }^{b}$, I-16146 Genova, Italy
B. Bhuyan and V. Prasad

Indian Institute of Technology Guwahati, Guwahati, Assam, 781 039, India
C. L. Lee and M. Morii

Harvard University, Cambridge, Massachusetts 02138, USA
A. J. Edwards

Harvey Mudd College, Claremont, California 91711
A. Adametz and U. Uwer

Universität Heidelberg, Physikalisches Institut, Philosophenweg 12, D-69120 Heidelberg, Germany
H. M. Lacker and T. Lueck

Humboldt-Universität zu Berlin, Institut für Physik, Newtonstr. 15, D-12489 Berlin, Germany
P. D. Dauncey

Imperial College London, London, SW7 2AZ, United Kingdom
U. Mallik

University of Iowa, Iowa City, Iowa 52242, USA
C. Chen, J. Cochran, W. T. Meyer, S. Prell, and A. E. Rubin Iowa State University, Ames, Iowa 50011-3160, USA
A. V. Gritsan and Z. J. Guo

Johns Hopkins University, Baltimore, Maryland 21218, USA
N. Arnaud, M. Davier, D. Derkach, G. Grosdidier, F. Le Diberder, A. M. Lutz,
B. Malaescu, P. Roudeau, M. H. Schune, A. Stocchi, and G. Wormser Laboratoire de l'Accélérateur Linéaire, IN2P3/CNRS et Université Paris-Sud 11, Centre Scientifique d’Orsay, B. P. 34, F-91898 Orsay Cedex, France
D. J. Lange and D. M. Wright

Lawrence Livermore National Laboratory, Livermore, California 94550, USA
C. A. Chavez, J. P. Coleman, J. R. Fry, E. Gabathuler, D. E. Hutchcroft, D. J. Payne, and C. Touramanis University of Liverpool, Liverpool L69 7ZE, United Kingdom
A. J. Bevan, F. Di Lodovico, R. Sacco, and M. Sigamani

Queen Mary, University of London, London, E1 4NS, United Kingdom
G. Cowan

University of London, Royal Holloway and Bedford New College, Egham, Surrey TW20 0EX, United Kingdom
D. N. Brown and C. L. Davis

University of Louisville, Louisville, Kentucky 40292, USA
A. G. Denig, M. Fritsch, W. Gradl, K. Griessinger, A. Hafner, and E. Prencipe

Johannes Gutenberg-Universität Mainz, Institut für Kernphysik, D-55099 Mainz, Germany
R. J. Barlow, ${ }^{\ddagger}$ G. Jackson, and G. D. Lafferty

University of Manchester, Manchester M13 9PL, United Kingdom
E. Behn, R. Cenci, B. Hamilton, A. Jawahery, and D. A. Roberts

University of Maryland, College Park, Maryland 20742, USA
C. Dallapiccola

University of Massachusetts, Amherst, Massachusetts 01003, USA
R. Cowan, D. Dujmic, and G. Sciolla

Massachusetts Institute of Technology, Laboratory for Nuclear Science, Cambridge, Massachusetts 02139, USA
R. Cheaib, D. Lindemann, P. M. Patel, and S. H. Robertson

McGill University, Montréal, Québec, Canada H3A $2 T 8$
P. Biassoni ${ }^{a b}$, N. Neri ${ }^{a}$, F. Palombo ${ }^{a b}$, and S. Stracka ${ }^{a b}$

INFN Sezione di Milano ${ }^{a}$; Dipartimento di Fisica, Università di Milano ${ }^{b}$, I-20133 Milano, Italy
L. Cremaldi, R. Godang, ${ }^{\S}$ R. Kroeger, P. Sonnek, and D. J. Summers

University of Mississippi, University, Mississippi 38677, USA
X. Nguyen, M. Simard, and P. Taras

Université de Montréal, Physique des Particules, Montréal, Québec, Canada H3C 3J7
G. De Nardo ${ }^{a b}$, D. Monorchio ${ }^{a b}$, G. Onorato ${ }^{a b}$, and C. Sciacca ${ }^{a b}$

INFN Sezione di Napoli ${ }^{a}$; Dipartimento di Scienze Fisiche, Università di Napoli Federico $I I^{b}$, I-80126 Napoli, Italy
M. Martinelli and G. Raven

NIKHEF, National Institute for Nuclear Physics and High Energy Physics, NL-1009 DB Amsterdam, The Netherlands
C. P. Jessop, J. M. LoSecco, and W. F. Wang

University of Notre Dame, Notre Dame, Indiana 46556, USA
K. Honscheid and R. Kass

Ohio State University, Columbus, Ohio 43210, USA
J. Brau, R. Frey, N. B. Sinev, D. Strom, and E. Torrence University of Oregon, Eugene, Oregon 97403, USA
E. Feltresi ${ }^{a b}$, N. Gagliardi ${ }^{a b}$, M. Margoni ${ }^{a b}$, M. Morandin ${ }^{a}$, M. Posocco ${ }^{a}$, M. Rotondo ${ }^{a}$, G. Simi ${ }^{a}$, F. Simonetto ${ }^{a b}$, and R. Stroili ${ }^{a b}$

INFN Sezione di Padova ${ }^{a}$; Dipartimento di Fisica, Università di Padova ${ }^{b}$, I-35131 Padova, Italy
S. Akar, E. Ben-Haim, M. Bomben, G. R. Bonneaud, H. Briand, G. Calderini, J. Chauveau, O. Hamon, Ph. Leruste, G. Marchiori, J. Ocariz, and S. Sitt

Laboratoire de Physique Nucléaire et de Hautes Energies, IN2P3/CNRS, Université Pierre et Marie Curie-Paris6, Université Denis Diderot-Paris7, F-75252 Paris, France
M. Biasini ${ }^{a b}$, E. Manoni ${ }^{a b}$, S. Pacetti ${ }^{a b}$, and A. Rossi ${ }^{a b}$

INFN Sezione di Perugia ${ }^{a}$; Dipartimento di Fisica, Università di Perugia ${ }^{b}$, I-06100 Perugia, Italy
C. Angelini ${ }^{a b}$, G. Batignani ${ }^{a b}$, S. Bettarini ${ }^{a b}$, M. Carpinelli ${ }^{a b}$, G. Casarosa ${ }^{a b}$, A. Cervelli ${ }^{a b}$, F. Forti $^{a b}$, M. A. Giorgi ${ }^{a b}$, A. Lusiani ${ }^{a c}$, B. Oberhof ${ }^{a b}$, E. Paoloni ${ }^{a b}$, A. Perez ${ }^{a}$, G. Rizzo ${ }^{a b}$, and J. J. Walsh ${ }^{a}$ INFN Sezione di Pisa ${ }^{a}$; Dipartimento di Fisica, Università di Pisa ${ }^{b}$; Scuola Normale Superiore di Pisa ${ }^{c}$, I-56127 Pisa, Italy
D. Lopes Pegna, J. Olsen, A. J. S. Smith, and A. V. Telnov Princeton University, Princeton, New Jersey 08544, USA
F. Anulli ${ }^{a}$, R. Faccini ${ }^{a b}$, F. Ferrarotto ${ }^{a}$, F. Ferroni ${ }^{a b}$, M. Gaspero ${ }^{a b}$, L. Li Gioi ${ }^{a}$, M. A. Mazzoni ${ }^{a}$, and G. Piredda ${ }^{a}$ INFN Sezione di Roma ${ }^{a}$; Dipartimento di Fisica, Università di Roma La Sapienza ${ }^{b}$, I-00185 Roma, Italy
C. Bünger, O. Grünberg, T. Hartmann, T. Leddig, H. Schröder, C. Voss, and R. Waldi Universität Rostock, D-18051 Rostock, Germany
T. Adye, E. O. Olaiya, and F. F. Wilson

Rutherford Appleton Laboratory, Chilton, Didcot, Oxon, OX11 0QX, United Kingdom
S. Emery, G. Hamel de Monchenault, G. Vasseur, and Ch. Yèche CEA, Irfu, SPP, Centre de Saclay, F-91191 Gif-sur-Yvette, France
D. Aston, D. J. Bard, R. Bartoldus, J. F. Benitez, C. Cartaro, M. R. Convery, J. Dorfan, G. P. Dubois-Felsmann, W. Dunwoodie, M. Ebert, R. C. Field, M. Franco Sevilla, B. G. Fulsom, A. M. Gabareen, M. T. Graham,
P. Grenier, C. Hast, W. R. Innes, M. H. Kelsey, P. Kim, M. L. Kocian, D. W. G. S. Leith, P. Lewis, B. Lindquist, S. Luitz, V. Luth, H. L. Lynch, D. B. MacFarlane, D. R. Muller, H. Neal, S. Nelson, M. Perl, T. Pulliam, B. N. Ratcliff, A. Roodman, A. A. Salnikov, R. H. Schindler, A. Snyder, D. Su, M. K. Sullivan, J. Va'vra, A. P. Wagner, W. J. Wisniewski, M. Wittgen, D. H. Wright, H. W. Wulsin, C. C. Young, and V. Ziegler SLAC National Accelerator Laboratory, Stanford, California 94309 USA
W. Park, M. V. Purohit, R. M. White, and J. R. Wilson University of South Carolina, Columbia, South Carolina 29208, USA
A. Randle-Conde and S. J. Sekula

Southern Methodist University, Dallas, Texas 75275, USA
M. Bellis, P. R. Burchat, and T. S. Miyashita

Stanford University, Stanford, California 94305-4060, USA
M. S. Alam and J. A. Ernst

State University of New York, Albany, New York 12222, USA
R. Gorodeisky, N. Guttman, D. R. Peimer, and A. Soffer Tel Aviv University, School of Physics and Astronomy, Tel Aviv, 69978, Israel
P. Lund and S. M. Spanier

University of Tennessee, Knoxville, Tennessee 37996, USA
J. L. Ritchie, A. M. Ruland, R. F. Schwitters, and B. C. Wray University of Texas at Austin, Austin, Texas 78712, USA
J. M. Izen and X. C. Lou

University of Texas at Dallas, Richardson, Texas 75083, USA

F. Bianchi ${ }^{a b}$, D. Gamba ${ }^{a b}$, and S. Zambito ${ }^{a b}$<br>INFN Sezione di Torino ${ }^{a}$; Dipartimento di Fisica Sperimentale, Università di Torino ${ }^{b}$, I-10125 Torino, Italy<br>L. Lanceri ${ }^{a b}$ and L. Vitale ${ }^{a b}$<br>INFN Sezione di Trieste ${ }^{a}$; Dipartimento di Fisica, Università di Trieste ${ }^{b}$, I-34127 Trieste, Italy<br>F. Martinez-Vidal and A. Oyanguren<br>IFIC, Universitat de Valencia-CSIC, E-46071 Valencia, Spain

H. Ahmed, J. Albert, Sw. Banerjee, F. U. Bernlochner, H. H. F. Choi, G. J. King,<br>R. Kowalewski, M. J. Lewczuk, I. M. Nugent, J. M. Roney, R. J. Sobie, and N. Tasneem University of Victoria, Victoria, British Columbia, Canada V8W 3P6<br>T. J. Gershon, P. F. Harrison, and T. E. Latham<br>Department of Physics, University of Warwick, Coventry CV4 7AL, United Kingdom

H. R. Band, S. Dasu, Y. Pan, R. Prepost, and S. L. Wu

University of Wisconsin, Madison, Wisconsin 53706, USA
(Dated: July 26, 2012)
We present searches for the rare decay modes $D^{0} \rightarrow e^{+} e^{-}, D^{0} \rightarrow \mu^{+} \mu^{-}$, and $D^{0} \rightarrow e^{ \pm} \mu^{\mp}$ in continuum $e^{+} e^{-} \rightarrow c \bar{c}$ events recorded by the BABAR detector in a data sample that corresponds to an integrated luminosity of $468 \mathrm{fb}^{-1}$. These decays are highly GIM suppressed but may be enhanced in several extensions of the Standard Model. Our observed event yields are consistent with the expected backgrounds. An excess is seen in the $D^{0} \rightarrow \mu^{+} \mu^{-}$channel, although the observed yield is consistent with an upward background fluctuation at the $5 \%$ level. Using the Feldman-Cousins method, we set the following $90 \%$ confidence level intervals on the branching fractions: $\mathcal{B}\left(D^{0} \rightarrow\right.$ $\left.e^{+} e^{-}\right)<1.7 \times 10^{-7}, \mathcal{B}\left(D^{0} \rightarrow \mu^{+} \mu^{-}\right)$within $[0.6,8.1] \times 10^{-7}$, and $\mathcal{B}\left(D^{0} \rightarrow e^{ \pm} \mu^{\mp}\right)<3.3 \times 10^{-7}$.

PACS numbers: $13.20 . \mathrm{Fc}, 11.30 . \mathrm{Hv}, 12.15 . \mathrm{Mm}, 12.60 .-\mathrm{i}$

## I. INTRODUCTION

In the Standard Model (SM), the flavor-changing neutral current (FCNC) decays $D^{0} \rightarrow \ell^{+} \ell^{-}$are strongly suppressed by the Glashow-Iliopoulos-Maiani (GIM) mechanism. Long-distance processes bring the predicted branching fractions up to the order of $10^{-23}$ and $10^{-13}$ for $D^{0} \rightarrow e^{+} e^{-}$and $D^{0} \rightarrow \mu^{+} \mu^{-}$decays, respectively [1]. These predictions are well below current experimental sensitivities. The lepton-flavor violating (LFV) decay $D^{0} \rightarrow e^{ \pm} \mu^{\mp}$ is forbidden in the SM. Several extensions of the SM predict $D^{0} \rightarrow \ell^{+} \ell^{-}$branching fractions that are enhanced by several orders of magnitude compared with the SM expectations [1]. The connection between $D^{0} \rightarrow \ell^{+} \ell^{-}$and $D^{0}-\bar{D}^{0}$ mixing in new physics models

[^0]has also been emphasized [2].
We search for $D^{0} \rightarrow \ell^{+} \ell^{-}$decays using approximately $468 \mathrm{fb}^{-1}$ of data produced by the PEP-II asymmetricenergy $e^{+} e^{-}$collider [3] and recorded by the BABAR detector. The center-of-mass energy of the machine was at, or 40 MeV below, the $\Upsilon(4 S)$ resonance for this dataset. The BABAR detector is described in detail elsewhere [4]. We give a brief summary of the main features below.

The trajectories and decay vertices of long-lived hadrons are reconstructed with a 5-layer, double-sided silicon strip detector (SVT) and a 40-layer drift chamber (DCH), which are inside a 1.5 T solenoidal magnetic field. Specific ionization $(d E / d x)$ measurements are made by both the SVT and the DCH. The velocities of charged particles are inferred from the measured Cherenkov angle of radiation emitted within fused silica bars, located outside the tracking volume and detected by an array of phototubes (DIRC). The $d E / d x$ and Cherenkov angle measurements are used in particle identification. Photon and electron energy, and photon position, are measured by a $\mathrm{CsI}(\mathrm{Tl})$ crystal calorimeter (EMC). The steel of the flux return for the solenoidal magnet is instrumented with layers of either resistive plate chambers or limited streamer tubes [5], which are used to identify muons (IFR).

## II. EVENT RECONSTRUCTION AND SELECTION

We form $D^{0}$ candidates by combining pairs of oppositely charged tracks and consider the following final states: $e^{+} e^{-}, \mu^{+} \mu^{-}, e^{ \pm} \mu^{\mp}, \pi^{+} \pi^{-}$, and $K^{-} \pi^{+}$. We use the measured $D^{0} \rightarrow \pi^{+} \pi^{-}$yield and the known $D^{0} \rightarrow$ $\pi^{+} \pi^{-}$branching fraction to normalize our $D^{0} \rightarrow \ell^{+} \ell^{-}$ branching fractions. We also use the $D^{0} \rightarrow \pi^{+} \pi^{-}$candidates, as well as the $D^{0} \rightarrow K^{-} \pi^{+}$candidates, to measure the probability of misidentifying a $\pi$ as either a $\mu$ or an $e$. Combinatorial background is reduced by requiring that the $D^{0}$ candidate originate from the decay $D^{*}(2010)^{+} \rightarrow D^{0} \pi^{+}[6]$. We select $D^{0}$ candidates produced in continuum $e^{+} e^{-} \rightarrow c \bar{c}$ events by requiring that the momentum of the $D^{0}$ candidate be above 2.4 GeV in the center-of-mass (CM) frame, which is close to the kinematic limit for $B \rightarrow D^{*} \pi, D^{*+} \rightarrow D^{0} \pi^{+}$. This reduces the combinatorial background from $e^{+} e^{-} \rightarrow B \bar{B}$ events.

Backgrounds are estimated directly from data control samples. Signal $D^{0}$ candidates with a reconstructed $D^{0}$ mass above 1.9 GeV consist of random combinations of tracks. We use a sideband region above the signal region in the $D^{0}$ mass $([1.90,2.05] \mathrm{GeV})$ in a wide $\Delta m \equiv$ $m\left(D^{0} \pi^{+}\right)-m\left(D^{0}\right)$ window ( $[0.141,0.149] \mathrm{GeV}$ ) to estimate the amount of combinatorial background. The $D^{0}$ and $\Delta m$ mass resolutions, measured in the $D^{0} \rightarrow \pi^{+} \pi^{-}$ sample, are 8.1 MeV and 0.2 MeV , respectively. We estimate the number of $D^{0} \rightarrow \pi^{+} \pi^{-}$background events selected as $D^{0} \rightarrow \ell^{+} \ell^{-}$candidates by scaling the observed $D^{0} \rightarrow \pi^{+} \pi^{-}$yield, with no particle identification criteria applied, by the product of pion misidentification probabilities and a misidentification correlation factor $G$. The misidentification correlation factor $G$ is estimated with the $D^{0} \rightarrow K^{-} \pi^{+}$data control sample.

The tracks for the $D^{0}$ candidates must have momenta greater than 0.1 GeV and have at least 6 hits in the SVT. The slow pion track from the $D^{*+} \rightarrow D^{0} \pi^{+}$decay must have at least 12 position measurements in the DCH. A fit of the $D^{*+} \rightarrow D^{0} \pi^{+} ; D^{0} \rightarrow t^{+} t^{-}$decay chain is performed where the $D^{0}$ tracks $(t)$ are constrained to come from a common vertex and the $D^{0}$ and slow pion are constrained to form a common vertex within the beam interaction region. The $\chi^{2}$ probabilities of the $D^{0}$ and $D^{*}$ vertices from this fit must be at least $1 \%$. The reconstructed $D^{0}$ mass $m\left(D^{0}\right)$ must be within $[1.65,2.05] \mathrm{GeV}$ and the mass difference $\Delta m$ must be within $[0.141,0.149] \mathrm{GeV}$. We subtract a data-MonteCarlo difference of $0.91 \pm 0.06 \mathrm{MeV}$, measured in the $D^{0} \rightarrow \pi^{+} \pi^{-}$sample, from the reconstructed $D^{0}$ mass in the simulation.

We use an error-correcting output code (ECOC) algorithm [7] with 36 input variables to identify electrons and pions. The ECOC combines multiple bootstrap aggregated decision tree binary classifiers trained to separate $e, \pi, K$, and $p$. The most important inputs for electron identification are the EMC energy divided by the track
momentum, several EMC shower shape variables, and the deviation from the expected value divided by the measurement uncertainty for the Cherenkov angle and $d E / d x$ for the $e, \pi, K$, and $p$ hypotheses. For tracks with momentum greater than 0.5 GeV , the electron identification has an efficiency of $95 \%$ for electrons and a pion misidentification probability of less than $0.2 \%$. Neutral clusters in the EMC that are consistent with Bremsstrahlung radiation are used to correct the momentum and energy of electron candidates. The efficiency of the pion identification is above $90 \%$ for pions, with a kaon misidentification probability below $10 \%$.

Muons are identified using a bagged decision tree algorithm with 30 input variables. Of these, the most important are the number and positions of the hits in the IFR, the difference between the measured and expected DCH $d E / d x$ for the muon hypothesis, and the energy deposited in the EMC. For tracks with momentum greater than 1 GeV , the muon identification has an efficiency of around $60 \%$ for muons, with a pion misidentification probability of between $0.5 \%$ and $1.5 \%$.

The reconstruction efficiencies for the different channels after the above particle identification requirements are about $18 \%$ for $e^{+} e^{-}, 9 \%$ for $\mu^{+} \mu^{-}, 13 \%$ for $e^{ \pm} \mu^{\mp}$, and $26 \%$ for $\pi^{+} \pi^{-}$. The background candidates that remain are either random combinations of two leptons (combinatorial background), or $D^{0} \rightarrow \pi^{+} \pi^{-}$decays where both pions pass the lepton identification criteria (peaking background). The $D^{0} \rightarrow \pi^{+} \pi^{-}$background is most important for the $D^{0} \rightarrow \mu^{+} \mu^{-}$channel.

Figure 1 shows the reconstructed invariant mass distributions from Monte Carlo (MC) simulated samples for the three $D^{0} \rightarrow \ell^{+} \ell^{-}$signal channels. Also shown are the distributions from $D^{0} \rightarrow \pi^{+} \pi^{-}$reconstructed as $D^{0} \rightarrow \ell^{+} \ell^{-}$and $D^{0} \rightarrow K^{-} \pi^{+}$reconstructed as $D^{0} \rightarrow \ell^{+} \ell^{-}$for each signal channel. The overlap between the $D^{0} \rightarrow \ell^{+} \ell^{-}$and $D^{0} \rightarrow \pi^{+} \pi^{-}$distributions is largest for the $D^{0} \rightarrow \mu^{+} \mu^{-}$channel, while the $D^{0} \rightarrow \ell^{+} \ell^{-}$and $D^{0} \rightarrow K^{-} \pi^{+}$distributions are well separated.

The combinatorial background originates mostly from events with two semileptonic $B$ and/or $D$ decays. The sample of events selected by the above criteria are dominantly from $e^{+} e^{-} \rightarrow B \bar{B}$ events, rather than events from the $e^{+} e^{-} \rightarrow q \bar{q}, \quad(q=u, d, s, c)$ continuum. We use a linear combination (Fisher discriminant [8]) of the following five variables to reduce the combinatorial $B \bar{B}$ background:

- The measured $D^{0}$ flight length divided by its uncertainty.
- The value of $\left|\cos \theta_{\text {hel }}\right|$, where $\theta_{\text {hel }}$ is defined as the angle between the momentum of the positivelycharged $D^{0}$ daughter and the boost direction from the lab frame to the $D^{0}$ rest frame, all in the $D^{0}$ rest frame.
- The missing transverse momentum with respect to the beam axis.


FIG. 1: Reconstructed $D^{0}$ mass (left) and $\Delta m$ (right) for the three signal channels: $D^{0} \rightarrow e^{+} e^{-}$(top), $D^{0} \rightarrow \mu^{+} \mu^{-}$(middle), and $D^{0} \rightarrow e^{ \pm} \mu^{\mp}$ (bottom). The solid (black) histogram is the signal MC, the dashed (blue) histogram is $D^{0} \rightarrow \pi^{+} \pi^{-}$ MC reconstructed as $D^{0} \rightarrow \ell^{+} \ell^{-}$, and the dotted (red) histogram is $D^{0} \rightarrow K^{-} \pi^{+}$MC reconstructed as $D^{0} \rightarrow \ell^{+} \ell^{-}$. The $D^{0} \rightarrow \ell^{+} \ell^{-}$and $D^{0} \rightarrow \pi^{+} \pi^{-}$distributions have been normalized to unit area. The $D^{0} \rightarrow K^{-} \pi^{+}$normalization is arbitrary.

- The ratio of the $2^{\text {nd }}$ and $0^{\text {th }}$ Fox-Wolfram moments [9].
- The $D^{0}$ momentum in the CM frame.

The flight length for combinatorial background is symmetric about zero, while the signal has an exponential distribution. The $\left|\cos \theta_{\text {hel }}\right|$ distribution is uniform for signal but peaks at zero for combinatorial $B \bar{B}$ background. The neutrinos from the semileptonic decays in $B \bar{B}$ background events create missing transverse momentum, while there is none for signal events. The ratio of Fox-Wolfram moments uses general event-shape information to separate $B \bar{B}$ and continuum $q \bar{q}$ events. Finally, the signal has a broad $D^{0} \mathrm{CM}$ momentum spectrum that peaks at around 3 GeV , while combinatorial background peaks at the minimum allowed value of 2.4 GeV .

Figure 2 shows distributions of the Fisher discriminant $(\mathcal{F})$ for samples of $B \bar{B} \mathrm{MC}, D^{0} \rightarrow \mu^{+} \mu^{-}$signal MC, and continuum background MC. The separation between signal and $B \bar{B}$ background distributions is large, while the signal and continuum background distributions are


FIG. 2: Fisher discriminant, $\mathcal{F}$, distributions for samples of $B \bar{B}$ MC (dashed blue), $D^{0} \rightarrow \mu^{+} \mu^{-}$signal MC (solid black), and continuum MC (dotted red). The $\mathcal{F}$ distributions for $D^{0} \rightarrow e^{+} e^{-}$and $D^{0} \rightarrow e^{ \pm} \mu^{\mp}$ are similar to those of $D^{0} \rightarrow$ $\mu^{+} \mu^{-}$.

TABLE I: Selection criteria for the three $D^{0} \rightarrow \ell^{+} \ell^{-}$signal decay modes. The parameter in the last row is defined as $\delta \Delta m \equiv \Delta m-\Delta m_{0}$, where $\Delta m_{0}$ is the nominal $D^{*+}-D^{0}$ mass difference [11].

| Parameter | $e^{+} e^{-}$ | $\mu^{+} \mu^{-}$ | $e^{ \pm} \mu^{\mp}$ |
| :---: | :---: | :---: | :---: |
| $\left\|\cos \theta_{\text {hel }}\right\|$ | $<0.85$ | $<0.90$ | $<0.85$ |
| $\mathcal{F}$ | $>0.00$ | $>-0.25$ | $>0.00$ |
| $m\left(D^{0}\right)(\mathrm{GeV})$ | $[1.815,1.890]$ | $[1.855,1.890]$ | $[1.845,1.890]$ |
| $\|\delta \Delta m\|(\mathrm{MeV})$ | $<0.5$ | $<0.5$ | $<0.4$ |

similar. For example, requiring $\mathcal{F}$ to be greater than 0 removes about $90 \%$ of the $B \bar{B}$ background while keeping $85 \%$ of the signal. The minimum $\mathcal{F}$ value is optimized for each signal channel as described below.

We use the $\left|\cos \theta_{\text {hel }}\right|$ variable directly to remove continuum combinatorial background. Figure reffig:coshel shows distributions of $\left|\cos \theta_{\text {hel }}\right|$ before making a minimum $\mathcal{F}$ requirement, for $B \bar{B}$ background, continuum background, and signal. The drop-off for $\left|\cos \theta_{\text {hel }}\right|$ near 1.0 in the signal distributions is caused by the selection and particle identification requirements. The $B \bar{B}$ background peaks near zero, while the continuum background peaks sharply near one.

The selection criteria for each signal channel were chosen to give the lowest expected signal branching fraction upper limit for the null hypothesis (a true branching fraction of zero) using the MC samples. The Fisher discriminant coefficients were determined before applying the $\left|\cos \theta_{\text {hel }}\right|, D^{0}$ mass, and $\Delta m$ requirements. We then tested a total of 2700 configurations of $\left|\cos \theta_{\text {hel }}\right|, \mathcal{F}, D^{0}$ mass, and $\Delta m$ criteria. Table I summarizes the resulting best values for the maximum $\left|\cos \theta_{\text {hel }}\right|$, minimum $\mathcal{F}$, $m\left(D^{0}\right)$ signal window, and $\Delta m$ interval.

After the selection criteria in Table I were determined, the data yields in the sideband region were compared to the expectations from Monte Carlo samples. The $D^{0} \rightarrow \mu^{+} \mu^{-}$and $D^{0} \rightarrow e^{ \pm} \mu^{\mp}$ data yields were consis-


FIG. 3: Distributions of $\left|\cos \left(\theta_{\text {hel }}\right)\right|$ for the three signal channels: $D^{0} \rightarrow e^{+} e^{-}$(left), $D^{0} \rightarrow \mu^{+} \mu^{-}$(center), and $D^{0} \rightarrow e^{ \pm} \mu^{\mp}$ (right). The top distributions show Monte Carlo distributions for the combinatorial $B \bar{B}$ (dashed, blue) and continuum (dotted, red) backgrounds. The bottom distributions show the signal Monte Carlo with arbitrary normalization.
tent with the expectations from the Monte Carlo samples. However, the $D^{0} \rightarrow e^{+} e^{-}$sideband yield showed a substantial excess of events; 90 events were observed when $5.5 \pm 1.6$ were expected.

The excess of data sideband events over the expected background from Monte Carlo was investigated and found to have several distinct features: low track multiplicity, continuum-like event shape characteristics, tracks consistent with electrons produced in photon conversions, low $D^{0}$ daughter track momenta, and undetected energy along the beam axis. We found that such events result from hard initial state radiation events or two-photon interaction processes that are not simulated in the continuum MC samples used in the analysis. The following selection criteria were added in order to remove such background contributions:

- Events must have at least 5 tracks for the $D^{0} \rightarrow$ $e^{+} e^{-}$channel and at least 4 tracks for the $D^{0} \rightarrow$ $\mu^{+} \mu^{-}$and $D^{0} \rightarrow e^{ \pm} \mu^{\mp}$ channels.
- Events can have at most 3 electron candidates.
- The longitudinal boost of the event, reconstructed from all tracks and neutral clusters, along the highenergy beam direction $p_{z} / E$ in the CM frame must be greater than -0.5 for all three $D^{0} \rightarrow \ell^{+} \ell^{-}$channels.
- For $D^{0} \rightarrow \mu^{+} \mu^{-}$and $D^{0} \rightarrow e^{ \pm} \mu^{\mp}$ candidates, the pion track from the $D^{*+}$ decay and the leptons must be inconsistent with originating from a photon conversion.

The signal efficiencies for the $D^{0} \rightarrow e^{+} e^{-}, D^{0} \rightarrow \mu^{+} \mu^{-}$, and $D^{0} \rightarrow e^{ \pm} \mu^{\mp}$ channels for these additional criteria are $91.4 \%, 99.3 \%$, and $96.8 \%$, respectively. The $D^{0} \rightarrow e^{+} e^{-}$ sideband yield in the data with these criteria applied is reduced to 8 events where $4.5 \pm 1.3$ are expected, based on the Monte Carlo samples.

## A. Peaking $D^{0} \rightarrow \pi^{+} \pi^{-}$background estimation

The amount of $D^{0} \rightarrow \pi^{+} \pi^{-}$peaking background within the $m\left(D^{0}\right)$ signal window is estimated from data and calculated separately for each $D^{0} \rightarrow \ell^{+} \ell^{-}$channel using

$$
\begin{equation*}
N_{\pi \pi}^{B G}=\left(\sum_{i} N_{\pi \pi, i}^{N P} \cdot\left\langle p_{f, i}^{+}\right\rangle\left\langle p_{f, i}^{-}\right\rangle\right) \cdot \epsilon_{m\left(D^{0}\right)} \cdot G \tag{1}
\end{equation*}
$$

where the sum $i$ is over the six data-taking periods, $N_{\pi \pi, i}^{N P}$ is the number of $D^{0} \rightarrow \pi^{+} \pi^{-}$events that pass all of the $D^{0} \rightarrow \ell^{+} \ell^{-}$selection criteria except for the lepton identification and $m\left(D^{0}\right)$ signal window requirements, $\left\langle p_{f, i}^{+}\right\rangle\left\langle p_{f, i}^{-}\right\rangle$is the product of the average probability that the $\pi^{+}$and the $\pi^{-}$pass the lepton identification criteria, $\epsilon_{m\left(D^{0}\right)}$ is the efficiency for $D^{0} \rightarrow \pi^{+} \pi^{-}$background to satisfy the $m\left(D^{0}\right)$ signal window requirement, and $G$ takes into account a positive correlation in the probability that the $\pi^{+}$and the $\pi^{-}$pass the muon identification criteria. The value of $\left\langle p_{f, i}^{+}\right\rangle\left(\left\langle p_{f, i}^{-}\right\rangle\right)$is measured using the ratio of the $D^{0} \rightarrow \pi^{+} \pi^{-}$yield requiring that the $\pi^{+}\left(\pi^{-}\right)$satisfy the lepton identification requirements to the $D^{0} \rightarrow \pi^{+} \pi^{-}$yield with no lepton identification requirements applied. The $\left\langle p_{f, i}^{+}\right\rangle$and $\left\langle p_{f, i}^{-}\right\rangle$are measured separately for each of the six major data-taking periods due to the changing IFR performance with time. The probability that the $\pi^{+}$and $\pi^{-}$both pass the muon identification criteria is enhanced when the two tracks curve toward each other, instead of away from each other, in the plane perpendicular to the beam axis. We use $G=1.19 \pm 0.05$ for the $D^{0} \rightarrow \mu^{+} \mu^{-}$channel and $G=1$ for the $D^{0} \rightarrow e^{+} e^{-}$and $D^{0} \rightarrow e^{ \pm} \mu^{\mp}$ channels. The $G$ factor is measured using a high-statistics $D^{0} \rightarrow K^{-} \pi^{+}$ sample where the $K$ is required to have a signature in the IFR that matches that of a $\pi$ which passes the $\mu$ identification criteria. This is in good agreement with the MC estimate of the $G$ factor value, $1.20 \pm 0.10$.

## B. Combinatorial background estimation

The combinatorial background is estimated by using the number of observed events in a sideband region and the expected ratio of events $R_{\mathrm{cb}}$ in the signal and sideband regions, determined from MC simulation. The sideband is above the signal region in the $D^{0}$ mass ([1.90, $2.05] \mathrm{GeV})$ in a wide $\Delta m$ window $([0.141,0.149] \mathrm{GeV})$. We fit the $D^{0}$ mass and $\Delta m$ projections of the combinatorial background MC using $2^{\text {nd }}$-order polynomials. A two-dimensional probability density function (PDF) is formed by multiplying the one-dimensional PDFs, assuming the variables are uncorrelated. The combinatorial background signal-to-sideband ratio $R_{\mathrm{cb}}$ is then computed from the ratio of the integrals of the twodimensional PDF.

## III. RESULTS

The distribution of $\Delta m$ vs $D^{0}$ mass as well as projections of $\Delta m$ and the $D^{0}$ mass for the data events for the three signal channels are shown in Fig. 4. Peaks from $D^{0} \rightarrow K^{-} \pi^{+}$and $D^{0} \rightarrow \pi^{+} \pi^{-}$are visible at 1.77 GeV and 1.85 GeV in the $D^{0}$ mass distribution for $D^{0} \rightarrow \mu^{+} \mu^{-}$candidates. We observe $1,8,2$ events in the $D^{0} \rightarrow e^{+} e^{-}, D^{0} \rightarrow \mu^{+} \mu^{-}$, and $D^{0} \rightarrow e^{ \pm} \mu^{\mp}$ signal regions, respectively.

## A. $\quad D^{0} \rightarrow \ell^{+} \ell^{-}$Branching fractions

The yield of $D^{0} \rightarrow \pi^{+} \pi^{-}$decays in the $\pi \pi$ control sample, selected with the same $\mathcal{F}$ and $\left|\cos \theta_{\text {hel }}\right|$ criteria for each $D^{0} \rightarrow \ell^{+} \ell^{-}$signal mode (see Table I), is used to normalize the $D^{0} \rightarrow \ell^{+} \ell^{-}$signal branching fraction. For each $D^{0} \rightarrow \ell^{+} \ell^{-}$signal channel, the $D^{0} \rightarrow \pi^{+} \pi^{-}$ yield $N_{\pi \pi}^{\text {fit }}$ is determined by fitting the $D^{0}$ mass spectrum of the $D^{0} \rightarrow \pi^{+} \pi^{-}$control sample in the range [1.7, 2.0] GeV . The fit has three components: $D^{0} \rightarrow \pi^{+} \pi^{-}$ , $D^{0} \rightarrow K^{-} \pi^{+}$, and combinatorial background. The PDF for the $D^{0} \rightarrow \pi^{+} \pi^{-}$component is the sum of a Crystal Ball function and two Gaussians. The Crystal Ball function is a Gaussian modified to have an extended, power-law tail on the low side [10]. The PDF for the $D^{0} \rightarrow K^{-} \pi^{+}$component is the sum of a Crystal Ball function and an exponential function. The combinatorial background PDF is an exponential function.

The $D^{0} \rightarrow \ell^{+} \ell^{-}$branching fraction is given by

$$
\begin{equation*}
\mathcal{B}_{\ell \ell}=\left(\frac{N_{\ell \ell}}{N_{\pi \pi}^{\mathrm{fit}}}\right)\left(\frac{\epsilon_{\pi \pi}}{\epsilon_{\ell \ell}}\right) \mathcal{B}_{\pi \pi}=S_{\ell \ell} \cdot N_{\ell \ell} \tag{2}
\end{equation*}
$$

where $N_{\ell \ell}$ is the number of $D^{0} \rightarrow \ell^{+} \ell^{-}$signal candidates, $N_{\pi \pi}^{\mathrm{fit}}$ is the number of $D^{0} \rightarrow \pi^{+} \pi^{-}$candidates from the fit, $\epsilon_{\pi \pi}$ and $\epsilon_{\ell \ell}$ are the efficiencies for the corresponding decay modes, $\mathcal{B}_{\pi \pi}=(1.400 \pm 0.026) \times 10^{-3}$ is the $D^{0} \rightarrow$
$\pi^{+} \pi^{-}$branching fraction [11], and $S_{\ell \ell}$ is defined by

$$
\begin{equation*}
S_{\ell \ell} \equiv \frac{\mathcal{B}_{\pi \pi}}{N_{\pi \pi}^{\mathrm{fit}}} \frac{\epsilon_{\pi \pi}}{\epsilon_{\ell \ell}} \tag{3}
\end{equation*}
$$

The expected observed number of events in the signal region is given by

$$
\begin{equation*}
N_{\mathrm{obs}}=\mathcal{B}_{\ell \ell} / S_{\ell \ell}+N_{B G} \tag{4}
\end{equation*}
$$

The uncertainties on $S_{\ell \ell}$ and $N_{B G}$ are incorporated into a likelihood function by convolving a Poisson PDF in $N_{\text {obs }}$ with Gaussian PDFs in $S_{\ell \ell}$ and $N_{B G}$. We determine $90 \%$ confidence level intervals using the likelihood ratio ordering principle of Feldman and Cousins [12] to construct the confidence belts. The estimated branching fractions and one standard deviation uncertainties are determined from the values of $\mathcal{B}_{\ell \ell}$ that maximize the likelihood and give a change of 0.5 in the log likelihood relative to the maximum, respectively.

## B. Systematic uncertainties

Table II summarizes the systematic uncertainties. Several of the uncertainties in $\epsilon_{\pi \pi} / \epsilon_{\ell \ell}$ cancel, including tracking efficiency for the $D^{0}$ daughters, slow pion efficiency, and the efficiencies of the $\mathcal{F}$ and $D^{0}$ momentum requirements. The uncertainty on $\epsilon_{\pi \pi} / \epsilon_{\ell \ell}$ due to particle identification is $4 \%$. Bremsstrahlung creates a low-side tail in the $D^{0}$ mass distributions for the $D^{0} \rightarrow e^{+} e^{-}$ and $D^{0} \rightarrow e^{ \pm} \mu^{\mp}$ decay modes. The uncertainty $\epsilon_{\ell \ell}$ due to the modeling of this tail is $3 \%$ for $D^{0} \rightarrow e^{+} e^{-}$and $2 \%$ for $D^{0} \rightarrow e^{ \pm} \mu^{\mp}$. The Crystal Ball shape parameters that describe the low-side tail of the $D^{0}$ mass distribution were varied, leading to an uncertainty of $1.1 \%$ to $1.3 \%$ on $N_{\pi \pi}^{\mathrm{fit}}$. We use the world average for the $D^{0} \rightarrow \pi^{+} \pi^{-}$ branching fraction [11], which has an uncertainty of $1.9 \%$. We combine the above relative uncertainties in quadrature resulting in $4.6 \%$ to $5.4 \%$ systematic uncertainties on $S_{\ell \ell}$.

The $D^{0}$ mass range for the fit used to determine the combinatorial background PDF was varied from [1.70, $2.05] \mathrm{GeV}$ to $[1.80,2.05] \mathrm{GeV}$. The difference in the resulting signal-to-sideband ratio $R_{\mathrm{cb}}$ is taken as a systematic uncertainty. The pion misidentification probabilities for $e$ and $\mu$ measured in data are in good agreement with the MC simulation. We use the larger of either the difference between the data and the MC or the statistical uncertainty on the MC misidentification probabilities as a systematic uncertainty. For the $D^{0} \rightarrow \mu^{+} \mu^{-}$decay mode, we take the uncertainty on the MC estimate for the $G$ factor of $8 \%$ as a systematic uncertainty on the $G$ estimate from the $D^{0} \rightarrow K^{-} \pi^{+}$data control sample.

## C. Branching Fraction Results

Table III presents the results, where $N_{S B}$ is the number of events in the upper sideband, $N_{\mathrm{cb}}$ is the expected num-


FIG. 4: Data distributions of $\Delta m$ vs the reconstructed $D^{0}$ mass (top row) and projections of the $D^{0}$ mass (middle row) and $\Delta m$ (bottom row). The columns contain the distributions for the $D^{0} \rightarrow e^{+} e^{-}$(left), $D^{0} \rightarrow \mu^{+} \mu^{-}$(center), and $D^{0} \rightarrow e^{ \pm} \mu^{\mp}$ (right) decay modes. The shaded $D^{0}$ mass $(\Delta m)$ distributions represent the subset of events that fall in the $\Delta m$ ( $D^{0}$ mass) signal window. In the top row, the dotted (black) box indicates the signal region and the dashed (red) box indicates the sideband region. In the middle and bottom rows, the vertical dotted black lines indicate the boundaries of the signal region.
ber of combinatorial background events in the signal window, $N_{\pi \pi}^{B G}$ is the number of events from the $D^{0} \rightarrow \pi^{+} \pi^{-}$ peaking background, and $N_{B G}$ (data) is the expected number of total background events in the data.

For the $D^{0} \rightarrow e^{+} e^{-}$and $D^{0} \rightarrow e^{ \pm} \mu^{\mp}$ channels, the event yield in the signal region is consistent with background only. We observe 1 and 2 events with expected backgrounds of $1.0 \pm 0.5$ and $1.4 \pm 0.3$ events for the $D^{0} \rightarrow e^{+} e^{-}$and $D^{0} \rightarrow e^{ \pm} \mu^{\mp}$ channels, respectively. The $90 \%$ confidence interval upper limits for the branching fractions are $<1.7 \times 10^{-7}$ for $D^{0} \rightarrow e^{+} e^{-}$and $<3.3 \times 10^{-7}$ for $D^{0} \rightarrow e^{ \pm} \mu^{\mp}$.

For the $D^{0} \rightarrow \mu^{+} \mu^{-}$channel, we observe 8 events in the signal region, where we expect $3.9 \pm 0.6$ back-
ground events. There is a cluster of of $D^{0} \rightarrow \mu^{+} \mu^{-}$ candidate events in Fig. 4 just above and below the lower $D^{0}$ mass edge of the signal region, where the $D^{0} \rightarrow \pi^{+} \pi^{-}$background is expected. We expect $7.5 \pm 0.8$ $D^{0} \rightarrow \pi^{+} \pi^{-}$events in the entire $[1.7,2.05] \mathrm{GeV} D^{0}$ mass range, with $93 \%$ of these events falling within the narrower [1.830,1.875] GeV range. The combinatorial background in the $[1.830,1.875] \mathrm{GeV} D^{0}$ mass interval is expected to be $1.8 \pm 0.6$ events, giving a total expected background of $8.8 \pm 1.1$ events. In this interval, we observe 15 events. The probability of observing 15 or more events when $8.8 \pm 1.1$ events are expected is $4.6 \%$, which corresponds to a 1.7 standard deviation upward fluctuation from the mean for a Gaussian distribution

TABLE II: Systematic uncertainties. The uncertainty on $S_{\ell \ell}$ results from the uncertainties on $\epsilon_{\pi \pi} / \epsilon_{\ell \ell}, N_{\pi \pi}^{\mathrm{fit}}$, and $\mathcal{B}_{\pi \pi}$ added in quadrature. The systematic uncertainty on the overall background $N_{B G}$ is obtained from the uncertainties on $N_{\pi \pi}^{B G}$ and $N_{\mathrm{cb}}$ added in quadrature.

|  | $D^{0} \rightarrow e^{+} e^{-}$ | $D^{0} \rightarrow \mu^{+} \mu^{-}$ | $D^{0} \rightarrow e^{ \pm} \mu^{\mp}$ |
| :--- | :---: | :---: | :---: |
| $\epsilon_{\pi \pi} / \epsilon_{\ell \ell}$, particle ID | $4 \%$ | $4 \%$ | $4 \%$ |
| $\epsilon_{\pi \pi} / \epsilon_{\ell \ell}$, Bremsstrahlung | $3 \%$ | - | $2 \%$ |
| $N_{\pi \pi}^{\text {fit }}$ | $1.2 \%$ | $1.3 \%$ | $1.1 \%$ |
| $\mathcal{B}_{\pi \pi}$ | $1.9 \%$ | $1.9 \%$ | $1.9 \%$ |
| $S_{\ell \ell}$ | $5.4 \%$ | $4.6 \%$ | $5.0 \%$ |
| $N_{\pi \pi}^{B G}$ | $11 \%(0.004$ events $)$ | $16 \%(0.43$ events $)$ | $5 \%(0.02$ events $)$ |
| $N_{\mathrm{cb}}, R_{\mathrm{cb}}$ | $36 \%(0.35$ events $)$ | $20 \%(0.25$ events $)$ | $19 \%(0.20$ events $)$ |
| $N_{B G}$ | 0.35 events | 0.50 events | 0.20 events |

TABLE III: Results for the observed event yields ( $N_{\text {obs }}$ ), estimated background ( $N_{B G}$ ), and signal branching fractions ( $\mathcal{B}_{\ell \ell}$ ). The first uncertainty is statistical and the second systematic. $N_{S B}$ is the observed number of events in the sideband, $R_{\mathrm{cb}}$ is the signal-to-sideband ratio for combinatorial background, $N_{\mathrm{cb}}$ and $N_{\pi \pi}^{B G}$ are the estimated combinatorial and $D^{0} \rightarrow \pi^{+} \pi^{-}$ backgrounds in the signal region, $N_{\pi \pi}^{\text {fit }}$ is the fitted yield in the $D^{0} \rightarrow \pi^{+} \pi^{-}$control sample, $\epsilon_{\pi \pi}$ and $\epsilon_{\ell \ell}$ are the $\pi \pi$ control sample and signal selection efficiencies, determined from Monte Carlo samples, which have negligible statistical uncertainties. The systematic uncertainty on $\epsilon_{\pi \pi} / \epsilon_{\ell \ell}$ is included in the systematic uncertainty on $S_{\ell \ell}$, which is defined in Eqn. (3).

|  | $D^{0} \rightarrow e^{+} e^{-}$ | $D^{0} \rightarrow \mu^{+} \mu^{-}$ | $D^{0} \rightarrow e^{ \pm} \mu^{\mp}$ |
| :--- | :---: | :---: | :---: |
| $N_{S B}$ | 8 | 27 | 24 |
| $R_{\mathrm{cb}}$ | $0.121 \pm 0.023 \pm 0.044$ | $0.046 \pm 0.005 \pm 0.009$ | $0.042 \pm 0.006 \pm 0.008$ |
| $N_{\mathrm{cb}}$ | $0.97 \pm 0.39 \pm 0.35$ | $1.24 \pm 0.27 \pm 0.25$ | $1.00 \pm 0.25 \pm 0.20$ |
| $N_{\pi \pi}^{B G}$ | $0.037 \pm 0.012 \pm 0.004$ | $2.64 \pm 0.22 \pm 0.43$ | $0.42 \pm 0.08 \pm 0.02$ |
| $N_{B G}$ | $1.01 \pm 0.39 \pm 0.35$ | $3.88 \pm 0.35 \pm 0.50$ | $1.42 \pm 0.26 \pm 0.20$ |
| $N_{\pi \pi}^{\text {fit }}$ | $39930 \pm 210 \pm 490$ | $51800 \pm 240 \pm 660$ | $39840 \pm 210 \pm 430$ |
| $\epsilon_{\pi \pi}$ | $14.4 \%$ | $18.7 \%$ | $14.6 \%$ |
| $\epsilon_{\ell \ell}$ | $9.48 \%$ | $6.29 \%$ | $6.97 \%$ |
| $S_{\ell \ell}\left(\times 10^{-9}\right)$ | $53.4 \pm 0.2 \pm 2.9$ | $80.6 \pm 0.4 \pm 3.7$ | $73.9 \pm 0.4 \pm 3.7$ |
| $N_{\text {obs }}$ | 1 | 8 | 2 |
| $\mathcal{B}_{\ell \ell}\left(\times 10^{-7}\right)$ | $0.1{ }_{-0.4}^{+0.7}$ | $3.3_{-2.0}^{+2.6}$ | $0.5_{-0.9}^{+1.3}$ |
| $\mathcal{B}_{\ell \ell}\left(\times 10^{-7}\right) 90 \%$ C.I. | $<1.7$ | $[0.6,8.1]$ | $<3.3$ |

(i.e. $(\operatorname{Erf}(1.7 / \sqrt{2})+1) / 2=1-0.046)$. The probability of observing 8 events when $3.9 \pm 0.6$ events are expected is $5.4 \%$. We conclude that the excess over the expected background is not statistically significant. The Feldman-Cousins method results in a two-sided $90 \%$ confidence interval for the $D^{0} \rightarrow \mu^{+} \mu^{-}$branching fraction of $[0.6,8.1] \times 10^{-7}$.

In summary, we have searched for the leptonic charm decays $D^{0} \rightarrow e^{+} e^{-}, D^{0} \rightarrow \mu^{+} \mu^{-}$, and $D^{0} \rightarrow e^{ \pm} \mu^{\mp}$ using $468 \mathrm{fb}^{-1}$ of integrated luminosity recorded by the $B A B A R$ experiment. We find no statistically significant excess over the expected background. These results supersede our previous results [13] and are consistent with the results of the Belle experiment [14], which has set
similar upper limits on the branching fractions for these decays. The LHCb experiment has recently presented preliminary search results [15] for $D^{0} \rightarrow \mu^{+} \mu^{-}$, where they find no evidence for this decay and set an upper limit on the branching fraction of $<1.3 \times 10^{-8}$ at $95 \%$ C.L.

## Acknowledgments

We are grateful for the extraordinary contributions of our PEP-II colleagues in achieving the excellent luminosity and machine conditions that have made this work possible. The success of this project also relies critically on
the expertise and dedication of the computing organizations that support BABAR. The collaborating institutions wish to thank SLAC for its support and the kind hospitality extended to them. This work is supported by the US Department of Energy and National Science Foundation, the Natural Sciences and Engineering Research Council (Canada), the Commissariat à l'Energie Atomique and Institut National de Physique Nucléaire et de Physique des Particules (France), the Bundesministerium für Bildung und Forschung and Deutsche Forschungsgemein-
schaft (Germany), the Istituto Nazionale di Fisica Nucleare (Italy), the Foundation for Fundamental Research on Matter (The Netherlands), the Research Council of Norway, the Ministry of Education and Science of the Russian Federation, Ministerio de Ciencia e Innovación (Spain), and the Science and Technology Facilities Council (United Kingdom). Individuals have received support from the Marie-Curie IEF program (European Union) and the A. P. Sloan Foundation (USA).
[1] G. Burdman, E. Golowich, J. Hewett, S. Pakvasa, Phys. Rev. D 66, 014009 (2002).
[2] E. Golowich, J. Hewett, S. Pakvasa, and A. Petrov, Phys. Rev. D 79, 114030 (2009).
[3] PEP-II Conceptual Design Report, SLAC-0418 (1993).
[4] B. Aubert et al. (The BABAR Collaboration), Nucl. Instrum. Meth. A 479, 1 (2002).
[5] W. Menges, IEEE Nuc. Sci. Symp. Conf. Rec. 5, 1470 (2006).
[6] The use of charge conjugate processes is implied unless explicitly stated otherwise.
[7] T. G. Dietterich and G. Bakiri, Journal of Artifical Intelligence Research 2, 263 (1995).
[8] R. A. Fisher, Annals of Eugenics 7, 179 (1936).
[9] G.C. Fox and S. Wolfram, Phys. Rev. Lett. 41, 1581 (1978).
[10] M. J. Oreglia, Ph.D. thesis, Report No. SLAC-R-236 (1980); J. E. Gaiser, Ph.D. thesis, Report No. SLAC-R-255 (1982).
[11] K. Nakamura et al. (Particle Data Group), Journal of Phys. G 37, 075021 (2010).
[12] G. Feldman and R. Cousins, Phys. Rev. D 57, 3873 (1998).
[13] B. Aubert et al. (BABAR Collaboration), Phys. Rev. Lett. 93, 191801 (2004).
[14] M. Petric et al. (Belle Collaboration), Phys. Rev. D 81, 091102(R) (2010).
[15] W. Bonivento and F. Dettori et al. (LHCb Collaboration), LHCb-CONF-2012-005. Presented at the 47th Rencrontres de Moriond on Electroweak Interactions and Unified Theories, La Thuile, Italy, 3-10 March, 2012.


[^0]:    *Now at the University of Tabuk, Tabuk 71491, Saudi Arabia
    ${ }^{\dagger}$ Also with Università di Perugia, Dipartimento di Fisica, Perugia, Italy
    $\ddagger$ Now at the University of Huddersfield, Huddersfield HD1 3DH, UK
    ${ }^{\S}$ Now at University of South Alabama, Mobile, Alabama 36688, USA
    ${ }^{\text {a }}$ Also with Università di Sassari, Sassari, Italy

