Signatures of Majorana Fermions in Hybrid Superconductor-Topological Insulator Devices

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The ability to measure and manipulate complex particles in the solid state is a cornerstone of modern condensed-matter physics. Typical excitations of a sea of electrons, called quasiparticles, have properties similar to those of free electrons. However, in recent years exotic excitations with very different properties have been created in designer quantum materials, including Dirac fermions in graphene¹ and fractionally-charged quasiparticles in fractional quantum Hall systems². Here we report signatures of a new quasiparticle – the Majorana fermion – in Josephson junctions consisting of two superconducting leads coupled through a three-dimensional topological insulator³. We observe two striking departures from the common transport properties of Josephson junctions: a characteristic energy that scales inversely with the width of the junction, and a low characteristic magnetic field for suppressing supercurrent. To explain these effects, we propose a phenomenological model in which a one-dimensional wire of Majorana fermions is present along the width of the junction, similar to a theoretical prediction by Fu and Kane⁴. These results present an opening into the investigation of Majorana fermions in the solid state and their exotic properties, including non-Abelian statistics⁵, a suggested basis for fault-tolerant quantum computation⁶.

The Majorana fermion, a charge-neutral particle that is its own antiparticle, was proposed theoretically almost 75 years ago^7 . In the original context of high-energy physics, neutrinos have been proposed to be Majorana fermions, a designation that could help explain the domination of matter over antimatter in our universe⁸. Separately, electronic excitations in certain condensed matter systems have recently been predicted to act as Majorana fermions⁷. One such system is a three-dimensional topological insulator (TI) where superconducting correlations between particles are introduced, producing a "topological superconductor" with properties similar to a p + ipsuperconductor³. Such superconducting correlations can be induced by doping a TI with Cu, where deviations from conventional superconductivity have been seen⁹. Another way to create a topological superconductor is via the proximity effect, wherein a conventional superconductor is placed in contact with a TI^{10} . When two superconductors are connected by a TI, the TI "weak link" superconducts due to its proximity to the superconducting leads. This produces a Josephson junction (JJ) but with several important distinctions compared to a conventional JJ, where the weak link is typically an ordinary metal or insulator. Fu and Kane have predicted [4] a one-dimensional (1D) mode of Majorana fermions at the interface between a conventional superconductor and a superconducting topological surface state. Hence, JJs formed with a TI weak link are expected to have two 1D modes at the two superconductor-TI interfaces (arrows in Fig. 1a), which fuse to form a 1D wire of Majorana fermions (shown in purple in Fig. 1a) running along the width of the device⁴. The energy spectrum of these Majorana fermions is characterized by states within the superconducting gap, which cross at zero energy when the phase difference φ between the two superconducting leads is π (solid purple line, Fig. 1b).

To probe this exotic state, recent experiments have investigated transport in TI JJs, finding good agreement with conventional JJ behavior $^{11-15}$. Two characteristic properties are typically reported for JJs. The first is the product $I_C R_N$, where I_C is the critical current and R_N is the normal state resistance. $I_C R_N$ should be of order Δ/e (where Δ is the superconducting gap of the leads and e is the charge of the electron) and independent of device geometry¹⁶. Two experiments^{11,13} have noted a smaller-than-expected value for the product $I_C R_N$ in TI JJs. The second characteristic property is the "Fraunhofer-like" magnetic diffraction pattern, i.e. the decaying, oscillatory response of the supercurrent to the magnetic field B, applied perpendicular to the flow of the supercurrent. The first minimum in I_C should occur at $B = B_C$, when one quantum of flux $\Phi_0 = h/2e$ (where h is Planck's constant) is passed through the area of the device, and recent reports on in TI JJs^{14,15} match this expectation.

The main experimental results of this paper are a small value of $I_C R_N$ that scales with 1/W, where W is the width of the JJ, and a value of B_C that is ~5 times smaller than that expected from the device area. Neither of these results is predicted or previously seen for



FIG. 1: Phenomenological model for Majorana fermions in topological insulator Josephson junction. a, Schematic of a topological insulator Josephson junction. Two superconducting leads are patterned on top of Bi₂Se₃ forming a junction with length L and width W. Along the width of the device, a one-dimensional wire of Majorana fermions results (purple). b, Energy levels near $\varphi = \pi$ before momentum quantization along W (purple line) and after, where the topological state remains at E = 0 (solid purple circle) and the first quantized energy level at the value E_C (empty purple circles). c, Current-phase relation resulting from momentum quantization, producing an anomalous peak at $\varphi = \pi$. d, Scanning-electron micrograph of a device similar to the ones measured in this Letter.

conventional JJs nor TI JJs. To explain these experimental observations, we propose a two-fold phenomenological extension to the model in Ref 4. First we take into account confinement along the 1D Majorana wire, quantizing its energy levels at multiples of $E_C = h\nu_{ex}/2l$, with ν_{ex} the velocity of the carriers in the wire and l the length of the wire. In the present devices, the length of the wire is the width W of the JJ, hence $E_C = h\nu_{ex}/2W$. The effect of this quantization on the energy levels is shown in Fig. 1b. If the E = 0 state (Fig. 1b, solid purple dot) is topological in nature, i.e. it is a neutral Majorana mode, such confinement should not affect its existence nor change its energy from zero. The continuum of energy levels at $E \neq 0$, not protected from perturbations, are quantized in multiples of E_C (Fig. 1b, empty purple dots where only the first non-zero energy modes are shown for clarity). The second extension of Ref. 4 is to postulate that only the topological E = 0Majorana state carries supercurrent, while for $E \neq 0$ (separated from the topological state by E_C) the transfer of carriers from one lead to the other is dissipative. This results in an $I_C R_N$ set by the energy scale of confined modes along the width of the junction, rather than by Δ/e : $I_C R_N \propto E_C/e = h\nu_{ex}/2eW$. This also has an effect on the current-phase relation, which determines the supercurrent through the device as a function of φ . The supercurrent-carrying E = 0 state occurs at $\varphi = \pi$, producing a sharp peak in the current-phase relation at $\varphi = \pi$ (Fig. 1c), in contrast with the established sinusoidal current-phase relation for conventional JJs¹⁶, or a different-period sinusoid predicted for TI JJs¹⁷.

As described above, the result of confinement is to separate in energy the E = 0 1D modes (neutral Majorana modes) from the $E \neq 0$ (charged) 1D modes. A 1D mode can carry a supercurrent, but the critical current is strongly suppressed by interactions between charges^{18,19}. Thus a neutral mode can carry a larger supercurrent than a charged mode. In our experiment the lowest-energy charged modes are accessed when the current through the neutral mode is $1 \,\mu A$. We estimate that the charged modes cannot carry this much supercurrent. Hence the charged modes in our devices act as resistors carrying current but not supercurrent. When the charged modes become energetically accessible (i.e. for energies $\geq E_C$) they shunt the junction, causing the JJ to undergo a superconducting to metallic phase transition²⁰, which takes places because the 1D-charged-mode shunt resistance is greater than $h/4e^{2}$ ²¹. In this model, any additional supercurrent through the bulk (which might be expected in existing TIs, given the finite bulk conductivity) also ceases when the shunt resistance of the surface become energetically accessible.

To investigate the properties of JJs with TI weak links, Bi₂Se₃ crystals were synthesized either via a slow cooling of a binary melt of Bi and Se²² or by vapor-liquid-solid (VLS) growth²³ and flakes of thicknesses between 50 and 100 nm were obtained from these crystals via mechanical exfoliation¹. Junctions of lengths L between 20 and 80 nm and widths W between 0.5 and 3.2 μ m were fabricated via electron-beam lithography, followed by deposition of Ti/Al electrical leads (see the Supp. Info for details of the sample fabrication). A scanning electron



FIG. 2: *I-V* response of a topological insulator Josephson junction. (main) *V* vs. *I* for a devices of dimensions $(L, W) = (45 \text{ nm}, 1 \, \mu \text{m})$ for $B = 0, 2, 3, 5, 8, 10 \, \text{mT}$ and at a temperature of 12 mK. At $B = 0, I_C$ is 850 nA, which is reduced upon increasing *B*. For this device, the product $I_C R_N = 30.6 \, \mu \text{V}$, much lower than theoretically expected for conventional JJs. (upper-left inset) I - V curves overlap for all values of *B* at $V \geq 2\Delta/\text{e} \sim 300 \, \mu \text{V}$. (lower-right inset) Sweeps up (red) and down (black) in *I* show little hysteresis, indicating that the junction is in the overdamped regime.

micrograph of a completed device is shown in Fig. 1d. The DC response for a $(L,W)=(45 \text{ nm}, 1 \mu \text{m})$ junction at a temperature of 12 mK is shown in Fig. 2, where the DC voltage (V) is plotted as a function of the applied DC current (I). At B = 0, a typical DC Josephson response is observed (red curve): for $I \leq I_C = 850 \text{ nA}, V = 0$ and a supercurrent flows. Applying B perpendicular to the top surface of the ${\rm Bi}_2{\rm Se}_3$ reduces I_C until $B{=}10\,{\rm mT}$ when the superconducting leads are driven normal and the I-V curve becomes linear. For $I > I_C$, there is an excess current due to Cooper pairs leaking into a lowbarrier junction²⁴; this excess decreases with B. For V > $2\Delta/e\sim 300 \,\mu V$, all curves fall on top of each other (upper left inset of Fig. 2) for all values of B. Absence of hysteresis (lower right inset of Fig. 2), indicates that the junction is overdamped, consistent with calculations (Supp Info). R_N for this device is 35Ω and $I_C R_N = 30.6 \,\mu \text{V}$. Theoreretical expectations²⁵ for diffusive and ballistic weak links predict $I_C R_N$ to be $281 \,\mu\text{V}$ and $427 \,\mu\text{V}$, respectively, an order of magnitude higher than our measurements. As a control experiment, a device fabricated similarly to the TI JJs, except with a 75 nm-thick graphite weak link, has $I_C R_N = 244 \,\mu \text{V}$ (Supp. Info.), much closer to theoretical predictions. This suggests that something in the sample rather than the measurement setup reduces the values of $I_C R_N$.

Further insight into the nature of transport in TI JJs is



FIG. 3: 1/W dependence of $I_C R_N$. a, A comparison of two devices with similar R_N (56.1 and 51.5 Ω) and different widths W, 0.5 and 1 μ m. The device with $W=0.5 \,\mu$ m exhibits a larger I_C , in contrast to conventional JJs, where similar resistances lead to similar values of I_C . b, $I_C R_N$ vs. 1/W for all 14 devices (synthesized via two methods: a binary melt and VLS) showing the general trend of $I_C R_N \propto 1/W$. Using the phenomenological model of Fig. 1, a carrier velocity of $1.4\pm0.2\times10^4$ m/s is extracted.

found by investigating the width dependence of the characteristic quantity $I_C R_N$. A comparison of two junctions with $R_N = 56.1$ and 51.5Ω , and W=1 and $0.5 \mu m$, (both L=50 nm) is shown in Fig. 3a, demonstrating that halving W doubles I_C despite similar values of R_N . Measurements of R_N were carried out above the superconducting transition temperature of the leads in a four-terminal geometry, eliminating the resistance of the cryostat lines, but not the contact resistance between Ti/Al and Bi₂Se₃, which varies from device to device without apparent correlation to geometry or effect on $I_C R_N$ product. The mismatch of the I-V curves above I_C is due to the excess current mentioned in connection with Fig. 2 (inset), which is typically of order I_C^{25} and hence larger in the $W=0.5\,\mu\mathrm{m}$ device. The two curves approach each other as V approaches $2\Delta/e$ (inset Fig. 3a). The values of $I_C R_N$ for all 14 devices we measured that superconduct are shown as a function of 1/W in Fig. 3b. The trend is clear: a larger W produces a smaller $I_C R_N$. With benefit of hindsight, some previously reported experiments on TI JJs are consistent with $I_C R_N$ being related to 1/W. In very wide junctions no supercurrent is observed at all¹³. For intermediate values of W similar to ours a low $I_C R_N$ was measured¹¹. The velocity ν_{ex} of dissipative excita-

tions in the junction can be extracted from a linear fit of the data in Fig. 3b assuming a unity proportionality constant between $I_C R_N$ and E_C (i.e. $I_C R_N = E_C/e$), giving a value $1.4\pm0.2\times10^4$ m/s. Electrical transport measurements of the Fermi velocity ν_F for surface electrons in Bi_2Se_3 range from 10^5 m/s^{15} to 10^6 m/s^{11} , bracketing the value $\nu_{ex} = 4.2 \times 10^5 \text{ m/s}^{-26}$ extracted from ARPES, and larger than our inferred value. In fact, a lower group velocity is expected for the bound pairs of electrons and holes that shuttle Cooper pairs across the device²⁷. Specifically for Majorana fermions – a subset of these bound pairs – the velocity ν_M has been predicted to be less than ν_F by a factor $(\Delta/\mu)^2$ in Ref. [4] and (Δ/μ) in Ref. [28] (calculated for neutral modes created in graphene JJs), where μ is the chemical potential of the TI weak link relative to the Dirac point of the surface states. The typical ratio for Δ/μ in our samples is 10^{-3} , giving an estimate for the Majorana velocity of $0.42 \,\mathrm{m/s}$ for $(\Delta/\mu)^2$ and 4.2×10^2 m/s for (Δ/μ) . Given that we have ignored the proportionality constants in both the relationship between $I_C R_N$ and E_C , and between ν_M and $(\Delta/\mu)\nu_F$, our results are reasonably near expectations for ν_M given by Ref. [28].

The last characteristic response of TI JJs considered in this Letter is the magnetic diffraction pattern. The differential response dV/dI(B, I) for a (L, W) = (55 nm, M) $1.5 \,\mu\mathrm{m}$) device demonstrates an atypical relationship between I_C and B (Fig. 4a). Three features are of note: B_C is 5 times smaller than expected from the known device area; the shape of $I_C(B)$ deviates from a typical Fraunhofer pattern; and there exist added features in dV/dIat values of I above I_C whose magnitude and number depend on B. We consider the first two features below and address the third in dV/dI in the Supp. Info. The area of the devices is calculated as $W * (L + 2\lambda_L)$, where $\lambda_L = 50$ nm is the dirty London penetration depth for aluminum (Supp. Info). The extracted $I_C(B)$ is shown in Fig. 4b (red) and compared to the simulated Fraunhofer pattern (black) for the device area (see Supp. Info. for information on the simulation). B_C for this device is 1.70 mT, whereas it should be 9.3 mT, based on the device area measured from a scanning electron micrograph. We have measured a smaller-than-expected value of B_C in all our devices. The three minima in I_C on each side of B = 0 are unequally spaced, occurring at B=1.70, 6.25, and 11.80 mT. Even if the effective area of the junction were larger for unknown reasons, fitting the central peak to a Fraunhofer pattern would produce minima at 1.7, 3.4, and 5.1 mT, different from what is observed. The graphite control device exhibits a more conventional magnetic diffraction pattern (Supp. Info).

Drastic narrowing of $I_C(B)$ can occur if the currentphase relation (CPR) is peaked at certain values of φ , as our phenomenological model suggests. We note that an anomalous, peaked CPR has been theoretically predicted for a different device geometry, also a result of



FIG. 4: Magnetic interference pattern in topological insulator Josephson junction. a, Differential resistance dV/dIas a function of B and I showing an anomalous magnetic diffraction pattern for a $W=1.5\,\mu\text{m}$ junction. Two features are of note: a smaller than expected value of B_C at 1.70 mT and a nonuniform spacing between minima at values B=1.70, 6.50, 11.80 mT. b, (main) $I_C(B)$ (red) extracted from dV/dI in **a** is compared to the expected Fraunhofer pattern for the junction (black) where a reduction of the scale of the pattern and the nonuniform spacing are evident. (inset) A comparison of the simulated Frauhofer pattern for a sinusoidal (black) and an empirically-determined, peaked (red) CPR. The aperiodic minima observed in **a** are captured this CPR.

the presence of Majorana fermions 29 . In each case, one peak in the CPR occurs for each zero-energy crossing of states in the gap. For a single peak in the CPR, only a single, B=0 maximum is possible for $|\Phi| < \Phi_0$ (Supp. Info). The existence of multiple minima in $I_C(B)$ for $|\Phi| < \Phi_0$ indicates the presence of multiple peaks in the CPR – a result of coupling to fermionic modes in the device that create additional zero-energy crossings³⁰. For a given CPR, the resulting $I_C(B)$ is uniquely determined; however the reverse is not true: a peak in the CPR at, for example, $\varphi = \pi/2$ produces the same I_C (B) as a peak at $\varphi = \pi$. Through simulation, we are able to show that a smoothly-varying CPR cannot capture our results (Supp. Info) and only a CPR with peaks can create magnetic diffraction patterns like those observed in our devices. The magnetic diffraction pattern for one such peaked CPR that also includes a conventional, sinusoidal contribution from the bulk is compared to the typical Fraunhofer pattern (black) in the inset of Fig. 4b. Some, but not all, of the features observed in the experiment are captured by this CPR. Importantly it produces non-uniformly distributed minima at $\Phi_0/4$, $3\Phi_0/4$, and Φ_0 (see Supp. Info for details) matching the aperiodic structure of the minima seen in the experiment.

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Supplementary Information for Signatures of Majorana Fermions in Hybrid Superconductor-Topological Insulator Devices

Materials and methods

Single crystals, grown by the binary melt method, of $(\text{Bi}_{1-x}\text{Sb}_x)_2\text{Se}_3$ were synthesized by slow cooling a binary melt of Bi (99.9999%), Sb (99.999%) and Se (99.9999%) starting materials, mixed in the ratio 0.33:0.05:0.62. The actual amount of Sb in the single crystals is approximately 0.01, as measured in microprobe analysis. Bulk single crystals with dimensions $1 \times 1 \times 0.1 \text{mm}^3$ showed a non-metallic resistivity at low temperatures with a bulk carrier density of $7 \times 10^{16} \text{ cm}^{-3}$ as deduced by Hall and Shubnikov-de Haas analysis.

 $\rm Bi_2Se_3$ nanowires, synthesized via the vapor-liquidsolid (VLS) method, were grown in a 12-inch horizontal tube furnace with a quartz tube. $\rm Bi_2Se_3$ source powder (99.999%, from Alfa Aesar) was placed in the center of the furnace (540 °C). The growth substrate, a Si wafer with a thermally-evaporated, 10 nm Au film, was placed at a downstream, lower temperature zone (350 °C). High purity Ar gas delivers vapor from the source materials to a growth substrate at 130 sccm for 2 hours with 1 Torr pressure.

Samples of 50-100 nm thickness were prepared by mechanical exfoliation of the above material, using a method similar to exfoliation of graphene^{S_1}. Prior to sample exfoliation, $SiO_2(300 \text{ nm})/Si$ wafers were cleaned in acetone and isopropanol. HMDS was deposited on the SiO_2 surface in efforts to reduce the amount of H₂O contamination. Samples were exfoliated using Nitto-Denko tape and immediately after exfoliation PMMA 950 A4 (Microchem Crop.) was spun on the chip for 60 secs at 4000 rpm, followed by a baked for 30 mins at $180 \,^{\circ}\text{C}$. After electron beam exposure of the resist and development in MIBK/IPA 1:3, a 3 min UV-ozone was used to remove residual PMMA in the exposure contact areas. Ion milling of the exposed contact areas was performed to obtain low contact resistance to the Bi_2Se_3 flakes. The recipe of the ion mill is a 300 V beam voltage, 30 mA beam current producing an ion current density of $0.1 \,\mathrm{mA/cm^2}$, 60 V acceleration, 12 sccm argon flow, and a 10 secs exposure. Immediately following ion milling, the samples were loaded into e-beam evaporator with oil-free pumps and Ti/Al (3 nm and either 60 nm or 100 nm) were evaporated at a rate of 1 Å/s onto the sample at a pressure of $\sim 5 \times 10^{-8}$ Torr at the start of each evaporation.

Samples were measured in a ${}^{3}\text{He}/{}^{4}\text{He}$ dilution refrigerator with a base temperature of 12 mK. To reduce the effects of thermal radiation, three stages of filtering were employed: room-temperature LC π -filters, a 3-pole RC filter anchored to the mixing chamber designed to filter in the frequency range of 1 MHz to 5 GHz^{S2}, and 10 k Ω "on-chip" resistors used in conjunction with the inline capacitance of the twisted-pair wiring to produce a lowpass, RC-filter of cutoff frequency ~50 KHz. All experiments were performed in an electrically- and acousticallyshielded room. Device DC resistance and differential resistance were measured using a standard DC and lock-in technique. The applied AC current was kept low enough such that the AC voltage across the device never exceeded 500 nV, below the base temperature of the fridge $k_BT\sim 1 \mu eV$. To obtain accurate magnetic field values, a low-noise Yokogawa 7651 was used to supply the current to the superconducting magnet, producing a <0.3 μ T noise level in the magnet.

The transport properties of the exfoliated binary melt samples were characterized by making a device with contacts in a Hall-bar geometry and thickness of 100 nm. The extracted density, mobility and diffusion constant D of these samples are 7.8×10^{17} cm⁻³, 1950 cm²/Vs, $0.02 \text{ m}^2/\text{sec}$, respectively. We note that these values reflect merged contributions from both the surface and bulk, where it is expected that the surface electrons have a much higher mobility^{S3}. Hence, the values for mobility and D are a lower bound for the values of the surface electrons.

To extract the superconducting and normal state properties of the leads, four samples were prepared with the same recipe as the leads of the JJ devices: Ti/Al of thickness 3 nm/(60, 100 nm), both of $(L, W) = (10,1) \mu \text{m}$. Each thickness of Al was placed either directly on the SiO_2 substrate or on top of a Bi_2Se_3 flake. Characterization of these test samples was performed via a fourterminal resistance measurement at room temperature (290 K), 4 K and base temperature of the dilution refrigerator (12 mK). Little variation was found in the superconducting properties of the Al patterned on the SiO_2 substrate and on Bi₂Se₃. The resistivity of the samples at room temperature and 4K were $3.0 \times 10^{-8} \Omega$ -m and $0.3 \times 10^{-8} \Omega$ -m, respectively. The critical currents and magnetic fields for the 100 nm(60 nm)-thick Al-films were $488 \,\mu A(208 \,\mu A)$ and $11(13) \,\mathrm{mT}$ respectively.

Characteristic lengths and regimes for JJs

There are many different regimes in JJs that produce different behaviors. The regime applicable to the device is determined by the length of the junction L relative to five intrinsic length scales: coherence length of the Al leads $\xi_{Al}=1.6 \,\mu\text{m}$; the superconducting coherence length of the metallic (Bi₂Se₃) weak link ξ_N , and three properties of the (Bi₂Se₃) weak link unrelated to the superconductor: the thermal length ℓ_T , the mean-free path ℓ_e and the phase-coherence length ℓ_{φ} . ξ_N can be calculated from the diffusion constant by $\sqrt{\hbar D/\Delta}$, where Δ is the superconducting gap of Al, which we calculate from the BCS equation $\Delta=1.76 \, k_B T_C=151 \,\mu\text{eV}$, producing a value for ξ_N of ~280 nm. $\ell_T = \sqrt{\hbar D/2\pi k_B T}$, which at 12 mK is $1.3 \mu \text{m}$. ℓ_e can be extract from D as $D=1/2\nu_F\ell_e$, giving $\ell_e=80\,\mathrm{nm}$, where we have used the value of $\nu_F = 4.2 \times 10^5 \text{ m/s}$ from ARPES measurements^{S4}. l_{ω} was estimated from the half-width at half-max of the weak antilocalization correction to the longitudinal resistance (measured in the Hall bar) to be 650 nm. We note that ξ_N , ℓ_T , ℓ_e and perhaps ℓ_{φ} all represent lower bounds since we have used the average value of D from the surface and the bulk. The D for the surface electrons is expected to be higher. Further, W for the device should be compared to the Josephson penetration depth $\lambda_J = \sqrt{\Phi_o/(2\pi\mu_o j_C(2\lambda_L + L))}$, where λ_L is the London penetration depth $\sim 50 \text{nm}^{S5}$. We place a lower bound on λ_{J} by using the junction parameters that would make it the smallest, i.e. using the largest measured value of j_C and the longest value of L: producing a value for λ_I^{min} of 10 µm. This puts our junctions in the regime $L \sim \ell_e < \xi_N, \xi_{Al}, \ell_{\varphi}, L_T$ and $W < \lambda_J$, i.e. the short junction, quasi-ballistic regime. In this regime, $I_C R_N$ is expected to be described by either the KO-1 or KO-2 theory^{S6} and independent of W, neither of which expectation matches our data.

Supercurrent carried by the bulk

The typical thickness t for our devices is 75 nm. The calculated ξ_N is larger than this value, which means that both the surface and *entire* bulk should experience the proximity effect. We expect, however, that the supercurrent carried by the bulk to be smaller than that of the surface for two reasons. First, the Cooper pairs have to travel a longer distance from left to right lead through the bulk than through the surface. We can estimate this additional length by assuming the Cooper pairs have to go on average a distance t/2 from the left lead to the bulk, then another t/2 going from the bulk to the right lead. This makes the effective length of the device for the bulk states to be $L_{bulk} = L + t$. The second is the lower mobility of the bulk, producing a smaller value of D. For the device in Fig. 4 of the main manuscript $L=55\,\mathrm{nm}$ and t=95 nm, making L_{bulk} =150 nm. To calculate the reduction of the critical current, we assume D for the bulk states is 10 times smaller than the calculated value (a factor 12 has been experimentally determined^{S7} for the reduction of D for the bulk), giving a $\lambda_N^{bulk} \sim 65 \,\mathrm{nm}$. This estimate yields a bulk critical current of order five times smaller than that of the surface state S^6 .

We next consider the other possible mechanisms for the reduction of $I_C R_N$. A typical reduction comes from thermal noise, where the effect on $I_C R_N$ depends on the type of junction (overdamped or underdamped). The



FIG. 5: Additional features in dV/dI as function of temperature, I_{DC} , and B. a, Differential resistance dV/dI as a function of temperatures T_f as T_f is lower through T_C of the leads. For this device, a sharp transition to the superconducting state is observed at T_f =850 mK. b, Additional features in dV/dI as a function of Iare observed above I_C . c, dV/dI for values of T_f =12, 75, 150, 300, 400 mK. Shoulder dips are observed in dV/dI for the two temperatures 300 and 400 mK. d, dV/dI extracted for B=0, 0.75, 2.50, 8.00 mT from Fig. 4a of the main text. Shoulder dips are also apparent when the magnetic field is increased to 0.75 mT.

type of junction is determined the quality factor Q = $\sqrt{2eI_CC}/\hbar R_N$, where C is the capacitance of the JJ. We estimate C to be 0.5pF using a parallel plate capacitor model between the entire area of the leads of the device and the degenerately-doped Si, yielding Q=1.2. This is neither overdamped or underdamped, but at an intermediate value. Numerical evaluation of the I-V characteristics in this regime shows results similar to those of an overdamped junction S8 . The effect of thermal radiation on overdamped junctions has been calculated S8 , and shown to cause a smearing of the transition between the superconducting and normal state. Since the transitions we measure are still very sharp, we can rule out thermal fluctuations being a source of the reduction of $I_C R_N$. We can also calculate what the effect of thermal fluctuations would be had the junctions been in the underdamped regime S_5 : the effective thermal radiation temperature would have to be $3.4 \,\mathrm{K}$ to reduce $I_C R_N$ by the factors we observe. This high temperature is unphysical in our well-filtered setup.

$\begin{array}{c} \mbox{Additional features in the Differential Response} \\ \mbox{dV/dI as a function of T and B} \end{array}$

The differential response dV/dI for a $(L, W)=(50 \text{ nm}, 0.9 \,\mu\text{m})$ device as a function of fridge temperature T_f

is shown in Fig. S1a, where the device exhibits a sharp transition to dV/dI=0 below $T_f=850\,\mathrm{mK}$ of the leads. Above T_C , the devices shows a metallic temperature dependence of resistance. The differential response dV/dI(I) of this junction, typical for all devices measured, at $T_f=12 \text{ mK}$ is shown in Fig. S1b. Even aside from the transition from a superconducting state to a normal state, which produce large peaks at $I = I_C$, several features are evident and are indicated by labels 1-4. The first occurs in all devices as either a peak or a sharp rise in dV/dI (like the one shown in Fig. S1b), at $V = 200 \,\mu$ V. The second, broad peak appears at $V = 300 \,\mu\text{V}$, near $2\Delta/\text{e}$ of Al, where a peak in resistance is expected due to the quasiparticle contribution to the resistance from the leads S^{9} . The third and fourth peaks are both features occurring above 2Δ of the leads, occurring at $V = 500 \,\mu\text{V}$ and $V = 655 \,\mu\text{V}$, respectively. Peaks above 2Δ have also been seen previously in TI JJs^{S10}.

The effect of T_f on dV/dI is shown in Fig. S1c. A typical trend is observed, where increasing T_f reduces I_C . Additional "shoulder" dips appearing in dV/dI are evident in the T_f =300 mK and 400 mK traces. On the 400 mK trace, two dips are seen, at I=500 nA and 620 nA respectively.

Additional shoulder features are also seen in dV/dIabove I_C when a magnetic field B is applied (Fig. S1d). These are revealed in cuts of constant B in dV dI(B, I)for the device shown in Fig. 4 of the main text. At B = 0, there are two peaks in dV/dI at $I = \pm I_C$, and no other apparent features. At $B=0.75\,\mathrm{mT}$, dips are evident at $I = \pm 1.6 \,\mu\text{A}, V = 12.5 \,\mu\text{V}$ above the resistive transition. The single dip occurs for $0.6 \le B \le 1 \text{ mT}$. Two dips appear beginning at B=1 mT and persist throughout the entire second and third lobes, although to a much weaker degree in the third lobe. The double-dip is evident in the cut at $B=2.5 \,\mathrm{mT}$, occurring at $I\pm=0.9$ and $1.2 \,\mu\mathrm{A}$ and a value of V=7.4 and $12.1 \,\mu\text{V}$. The dips at $B=8 \,\text{mT}$ have all but disappeared, remaining weakly at $I \pm = 0.5$ and $0.9\,\mu\text{A}$ and V=6.3 and $12.1\,\mu\text{V}$. Currently, we have no explanation for these features which appear in all devices measured.

Andreev Bound States and the Current-Phase Relation

In this section we consider qualitatively the Andreev bound states (ABS) and the resulting current-phase relation (CPR). States in a JJ within the superconducting gap are associated with the coupled electron-hole pairs that are responsible for transferring Cooper pairs from one lead to the other^{S11}. These are known as ABS. To describe the CPR in our junction, we consider several different energy spectrum of ABS. The energy levels of conventional ABS are $E(\varphi) \propto \pm \Delta \sqrt{1 - T \sin^2(\varphi/2)} S^{11}$, where T is the transmission probability of Cooper pairs



FIG. 6: Determining the Current-Phase Relation from the Andreev Bound State Energy Spectrum. The CPR can be determined from the Andreev bound state (ABS) energy spectrum by taking the derivative of E with respect to φ . Qualitatively shown is the ABS spectrum (a) and the corresponding CPR (b) for conventional, ballistic JJs with a transmission probability T=0.9. The same plots (\mathbf{c}, \mathbf{d}) are shown for a p + ip and TI (without the lateral confinement of our model) JJs. ABS spectrum and CPR (e,f) for the phenomenological model of the main text. The inset of **e** shows the dependence of T on φ in our model. The CPR of (f) is peaked at the values of φ where the zero-energy crossings occur. g, The width of T in the inset of e and the corresponding CPR are set by E_C , the lateral confinement energy in the phenomenological model. h, (inset) ABS spectrum similar to S2e except with a anticrossing in the spectrum at $\varphi = \pi$. (main) CPR resulting from the ABS of the inset.

from left to right lead. From the energy spectrum of the ABS, the current phase relation (CPR) can be calculated as $I(\varphi) \propto \partial E / \partial \varphi^{S10}$. The energy spectrum for the ABS in a conventional JJ with T=0.9 is shown in Fig. S2a for the occupied (solid) and unoccupied (dashed) ABS states. The corresponding CPR, calculated by differentiating the $E(\varphi)$ plot, is shown in Fig. S2b, where a saw-tooth behavior is seen, occurring with a period of 2π . Note that for low values of T, this CPR becomes the conventional $sin(\varphi)^{S11}$. For p + ip and TI JJs, the energy of the ABS becomes $E(\varphi) \propto \pm \Delta \cos(\varphi/2)$, producing a zero-energy crossing at $\varphi = \pi^{S12}$. There is a correspondence between the p + ip and conventional energy spectrum of ABS for T = 1. The corresponding CPR is $I(\varphi) \propto \sin(\varphi/2)$, resulting in an anomalous 4π periodic CPR, predicted for p + ip JJs^{S12} and TI^{S13} JJs. The energy spectrum of the ABS and the CPR in this case are shown in Fig. S2c,d.

In our phenomenological model, the transmission coefficient T depends on φ , where the 1D charge modes at $\varphi \neq \pi$ have a low value for T – a result of the interactions in $1D^{S14}$ – and the neutral modes have a much higher value for T. This $T(\varphi)$ produces a CPR that is peaked at values of φ where the zero-energy modes occur. Fig. S2e shows an ABS spectrum for a $T(\varphi)$ (inset of Fig. S2e), corresponding to $T(\varphi)=1$ for $\varphi = \pi$ and $T(\varphi) = 1/10$ for $\varphi \neq \pi$. The exact value for T away from $\varphi = \pi$ can be changed without much change in the results. To connect the high- and low-T regions, we assume that the width of the peak in $T(\varphi)$ near π is set by the energy scale E_C , the energy associated with momentum quantization in the phenomenological model. This scenario is shown in Fig. S2g, where the linearized $E(\varphi)$ is calculated from Eq. 4 of Ref. [S15]. Using a value of $E_C = eI_C R_N = 31 \,\mu\text{eV}$ for the device in Fig. 4, values of 167° and 193° for φ_1 and φ_2 are obtained. T then is modeled as a gaussian with a half max at the values φ_1 and φ_2 . The calculated ABS spectrum for this transmission coefficient is shown in Fig. S2e, where a transition through E = 0 occurs on the scale of φ_1 and φ_2 around $\varphi = \pi$. The corresponding $I(\varphi)$ is shown in Fig. S2f, where is it seen that the φ -dependent T produces a anomalous CPR that is peaked around the values of φ where the zero-energy modes occur. This CPR is also 4π periodic. A similar CPR was obtained in Ref. S16, where a peak in the CPR was also found to be correlated with the zero-energy crossing in the ABS. In Fig. S2c and S2e, it was assumed that sermonic parity was conserved, which results in a protected crossing of the two states (solid and dashed lines) at $\varphi = \pi^{S17}$. If the parity of the junction is not preserved, an anti-crosssing of these two states occurs (inset of Fig. S2h), producing a CPR shown in Fig. S2h.

Simulation of Josephson Effect in the Presence of Magnetic Flux

The critical current through the devices as a function of applied field was calculated in a manner closely following that of Tinkham^{S5}, but with the extended junction model modified to allow non-standard current-phase relationships and spatial inhomogeneities critical current density. With the flake surface parallel to the x-y plane, applied field *B* along *z*, and current along *x*, the phase difference between the leads as a function of the position y along the junction is given by

$$\varphi(y) = \varphi_0 + \frac{2\pi}{\Phi_0} \int_0^y dy' \int_0^{L+2\lambda_L} dx B_z(x, y'), \quad (1)$$

where φ_0 is the phase difference at y=0, Φ_0 is the magnetic field flux quantum, L is the length of the junction, and λ_L is the London penetration depth. This follows



FIG. 7: Magnetic diffraction patterns for conventional current-phase relations. Magnetic diffraction patterns (red) for **a**, sinusoidal $I(\varphi)$, **b** saw-toothed sinusoidal $I(\varphi)$, **c**,**d**, sinusoidal $I(\varphi)$ with two different nonuniform critical current line densities K_c . In **b-d**, the magnetic diffraction pattern for the sinusoidal $I(\varphi)$ (black) from **a** is plotted for comparison. In each figure, the current-phase relations used to produced the magnetic diffraction pattern is shown in the inset.

from integrating the vector potential **A** around a rectangular contour that includes a path at y'=0 and y'=yand taking advantage of the fact that $\mathbf{A} = (\Phi_0/2\pi)\nabla\gamma$ inside the superconducting leads, where γ is the non-gaugeinvariant phase [defined so that $\varphi = \Delta\gamma - (2\pi/\Phi_0) \int \mathbf{A} \cdot d\mathbf{s}$]. With normalized current-phase relationship (CPR) $i(\varphi) = I(\varphi)/I_C$ and critical current line density $K_c(y)$, we obtain critical current

$$I_C = max_{\varphi_0} \int_0^W dy K_c(y) i(\varphi(y)). \tag{2}$$

Note that this analysis is equally valid for 2π - and 4π periodic phase relations, so long as for the latter case we allow $\varphi(y)$ to range up to 4π and define $i(\varphi)$ over the full range. For a typical 2π -periodic current-phase relationship $I(\varphi) = I_C sin(\varphi)$ and uniform current density and field, the critical current drops to zero when an integer number of flux quanta are threaded through the junction area, corresponding to an integer number of cycles of Josephson current. A simulation of magnetic diffraction pattern (MDP) for $i(\varphi) = sin(\varphi)$ shows the typical Fraunhofer pattern S5 (Fig. S3a). Deviations from this typical pattern can occur because of non-sinusoidal CPR or from nonuniform critical current distribution along the junction. For a ballistic JJ, the CPR becomes more of a saw-toothed shape, for which the corresponding MDP is shown in Fig. S3b. There is a small change in the shape of the MDP, but the minima still occur at integer multiples of Φ_0 . Aside from a changing CPR, deviations from



FIG. 8: Magnetic diffraction patterns for anomalous current-phase relations. Magnetic diffraction patterns (red) for **a** two gaussian peaks in $I(\varphi)$ at $\varphi = \pm \pi$. **b**, the same as **a** but with an added conventional sinusoidal $I(\varphi)$ of 1/5 the amplitude of the anomalous peaks, **c**, the same **a**, with additional peaks at $\varphi = \pi/2, 3\pi/2$ and $5\pi/2, 7\pi/2$, resulting from additional zero-energy crossings. **d**, the same as **c** but with a conventional sinusoidal $I(\varphi)$ of 1/5 the amplitude of the anomalous peaks. In each figure, the current-phase relations used to produced the magnetic diffraction pattern are shown in the inset and each diffraction pattern is compared to the conventional sinusoidal case (black). **e**, A peaked CPR for an ABS spectrum in Fig. S2h, with additional zero-energy crossings at $\varphi = \pi/2, \pi$ and $3\pi/2$. **f**, same as **e** except with the sinusoidal bulk contribution added.

the Fraunhofer pattern for short junctions can occur for a non-uniform current distribution. Reductions of the the location of the first minimum as large as a factor of 2 can occur in the extreme limit when all of the current is concentrated near the end of the junction^{S18}. The MDP in this extreme case is shown for two different current distributions in Fig. S3c, d. None of these deviations produce a MDP similar to Fig. 4 of the main text.

Using this simulation, we empirically determine a CPR to match the MDP we observe in our devices. Not any CPR is possible: the CPR must be antisymmetric $I(\varphi) = -I(-\varphi)$, it must come from the derivative of the energy of the junction and must average to zero over a period such that the energy of the junction $E(\varphi) \propto \int d\varphi I(\varphi)$ does not continue to grow as a func-

tion of φ ^{S19}. In addition, the CPR must contain a term for the contribution of the bulk, which was estimated in our devices to be smaller than the surface, but not zero. In the following, we assume the bulk has a CPR $I(\varphi) \propto \sin(\varphi)$. To begin, we assume the simplest CPR that is peaked at values of π and 3π , with alternating signs but equal amplitude to satisfy the conditions on the CPR. This result is shown in Fig. S4a, where we see that the inclusion of peaks at $\varphi = \pi, 3\pi$ produces a narrowed MDP. It does not, however, reproduce the additional minima seen in Fig. 4. Note that this CPR is 4π -periodic, as expected for TI JJs. The first correction to the simple, peaked CPR above comes from the addition of the bulk term, which we include as a simple sinusoidal dependence on φ , $sin(\varphi)$, with 1/5 the amplitude (as estimated above) of the peaks in the CPR and is 2π -periodic. Compared to Fig. S4a, additional features in the MDP, are thereby introduced at $n\Phi_0$, where n is an integer. To get closer to the observed MDP, we add more zero-energy crossings, predicted in Ref. [S17]. We add two additional zero-energy modes or either side of $\varphi = \pi$ and 3π , at $\varphi = \pi/2, 3\pi/2$ and $5\pi/2, 7\pi/2$, and the corresponding MDP is shown in Fig. S4c.d. The MDP is calculated without (S4c) and with (S4d) the $sin(\varphi)$ contribution from the bulk. It is seen in Fig. S4d, a small notch in the MDP appears below the first expected minima, occurring at a value of $3\Phi_0$. A CPR similar to that used in Fig. S3c,d was calculated as an anomalous contribution to the CPR from Majorana fermions S16 , a result of difference in Josephson current from the even and odd Majorana occupancies in the JJ. The last CPR considered are of the form from Fig. S2h and are shown in Fig. S4e,f, where we again have used the multiple zero-energy crossings of Ref. [S17]. The bulk importance of the inclusion of a bulk term is evident here, where without the sinusoidal addition no sub- Φ_0 dips occur (Fig. S4e). The MDP of Fig. S4f produces minima at values $\Phi_0/4$, $3\Phi_0/4$ and Φ_0 , near the experimentally observed minima. We note that we cannot determine a unique CPR from the diffraction pattern but can only supply evidence for a peaked CPR. In our simulations, we were unable to obtain sub- Φ_0 dips for any uniform (i.e. non-peaked) CPR, but were only able to obtain MDPs that look similar to our experimental results using peaked CPRs.

MDPs for a varying bulk contribution are shown in Fig. S5. Fig. S5a is a 2D plot of the MDP for the CPR of Fig. S4e as a function of Φ and the amplitude of the sinusoidal contribution (Sine Amp). When Sine Amp=0 (all surface), the resulting MDP is the same as Fig. S4e, while for Sine Amp=1 (all bulk) the MDP is same as Fig. S3a. Fig. S5a shows that sub- Φ_0 minima are obtained for values of Sine Amp less than ~0.4. For Sine Amp=0.5 (red), the MDP obtained is shown in Fig. S5b, where it is seen that a narrowing of the central feature occurs when compared to a Fraunhofer pattern (black), but the minima still occur at integer values of Φ_0 . A MDP similar



FIG. 9: Dependence of the MDP on the bulk contribution. (a) A 2D plot of the MDP as a function of Φ and the amplitude of the sinusoidal bulk contribution (Sine Amp). Sub- Φ_0 minima are observed for values of Sine Amp less than ~0.4. (b) A 1D cut in **a** at a value of Sine Amp=0.5 (red), showing a narrowed central lobe [compared to the Fraunhofer pattern (black)] in the MDP but no minima below Φ_0 .

to the one calculated in Fig. S5b is seen in Fig. 2b of Ref. [S20].

A Graphite Control Device

To confirm that the anomalous features observed in TI JJs are a result of the interface between a TI and a conventional superconductor, a JJ was created using 75 nm-thick graphite as the weak link. The details of the device fabrication are identical to the fabrication of TI JJs, except the Ar ion mill step was not needed to produce low contact resistance. Instead, a 5 min UV-ozone exposure, typical in the creation of graphene devices S^{21} , was used. The results, taken at $T_f=12 \text{ mK}$, are shown in Fig. S5 where it is seen that the value of $I_C R_N$ is much higher at 244 μ V (Fig. S5a) and B_C is ~13 mT, closer to the predicted value of 14.3 mT (black line) for a device of $(L, W) = (0.05, 1) \, \mu \text{m}$. The control device allows for the exclusion of two factors that might have caused the anomalous results in TI JJs. In Fig. S5a, a plot of Vvs. I shows a value for the critical current of $8.1 \,\mu\text{A}$ on a device of resistance 30.2 Ω . The larger value of $I_C R_N$ obtained for the control device rules out the possibility of the thermal effects caused by poor filtering being a source of the reduced $I_C R_N$ in the TI JJs. In Fig. S5b, I_C vs. B (red), extracted from a plot of dV/dI(B, I) (inset of S5b) shows a more conventional dependence on B, closely matching the expected pattern (black). The high value of B_C in the control device rules out the possibility of flux focusing^{S22} reducing the values of B_C in TI JJs.



FIG. 10: Superconducting properties of a graphite control sample. (a) V vs. I for the $(L, W) = (50 \text{ nm}, 1 \, \mu\text{m})$ control device created from a 75 nm-thick graphite weak link, producing a $I_C R_N$ of $244 \, \mu\text{V}$, larger than the observed in TI JJs. (b) Extracted I_C vs. B (red) from dV/dI (inset) giving a value of B_C of 13 mT, close to the value of 14.3 mT expected from the device area.

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