Using Atom Interferometery to Search for New Forces

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Atom interferometry is a rapidly advancing field and this Letter proposes an experiment based on existing technology that can search for new short distance forces. With current technology it is possible to improve the sensitivity by up to a factor of 10^2 and near-future advances will be able to rewrite the limits for forces with ranges from 100 μ m to 1km.

New short distance forces are a frequent prediction of theories beyond the Standard Model and the search for these new forces is a promising channel for discovering new physics. Over the past 15 years there has been rapid advances in light pulse atom interferometry (AI) and in a wide variety of settings, AI is the most sensitive measurement. This Letter will explore the sensitivity of AI to new forces. AI holds great promise in improving currently sensitivity over a wide range of distances from roughly 100 μ m to 1 km.

New forces can couple to matter in many different ways; however, there is a benchmark parameterization that is frequently applicable to new forces where the potential between two particles is proportional to the mass of the particles

$$V(r) = \alpha \frac{G_N m_1 m_2}{r} \exp(-r/\lambda) \tag{1}$$

where α is a dimensionless number that characterizes the new force's strength relative to gravity and λ is the Compton wavelength of the particle being exchanged. The coupling, α , could be composition, spin or velocity dependent or have a power-law fall off rather than an exponential/Yukawa behavior; however, this parameterization is a standard benchmark and will be used in this Letter. Theories predict a wide range of λ and α . Some theories give $\alpha \gtrsim \mathcal{O}(1)$ such as gauge mediated supersymmetry theories that have moduli mediated forces [3], large extra dimensions [2] or theories that have gravity shut off at the scale of the cosmological constant [4]. Alternatively, many theories also predict $\alpha \ll 1[1]$. The most reknowned of these theories are Peccei-Quinn axions can mediate forces with $\alpha \lesssim 10^{-6}$ [5, 6]. Thus, while it is important to continue the search for $\alpha \sim 1$ to shorter distance forces, searching for subgravitational strength forces is also an important frontier to continue pursuing. Finally, there are forces that are not Yukawa forces of (1) and may intrinsically be stronger than gravity, but at long distances may show up as subgravitational strength forces [7].

Atom interferometry uses cold atoms that have their quantum mechanical wave packets spatially split in two and recombined. The final interference pattern measures the phase difference between the two paths. The experiment described in this Letter uses a source mass to create a potential that causes a relative phase between the two paths. By subtracting off the Newtonian potential and other backgrounds, a new Yukawa potential is visible. The AI experiment in this Letter is effective at probing new forces in the 1mm to 100m range with sensitivities down to $\alpha \sim 10^{-5}$ with already proven techniques in contrast to current experimental limits that have sensitivities of $\alpha \gtrsim 2 \times 10^{-4} [1, 8]$. Future improvements can increase the range of sensitivity to 100μ m to 1km and with sensitivities down to $\alpha \sim 10^{-9}$.

ATOM INTERFEROMETRY

The atom interferometry used in this proposal is similar to [9] and uses many of the techniques in [10]. Light pulse atom interferometry uses two counter-propagating lasers that couple hyperfine degenerate ground states of alkali (or alkali-like) atoms through a near-resonance Raman transition. While the lasers are on, the system undergoes Rabi oscillations between two states having a relative momentum $\hbar k_{\text{eff}} = m v_r$. By performing a $\frac{\pi}{2} - \pi - \frac{\pi}{2}$ series of Raman pulses, the atom's wave packet is split into a slow and fast component, then after an interrogation time, T, the states are reversed and the wave packet is brought back together for the final beam splitter that interferes the two halves of the wave packet. The maximal spatial separation of the wave packets in the interferometer is $v_r T$. There often is an initial velocity, v_i , to the atom's wave packets that is used to Doppler-select the desired atomic transitions. An initial velocity can also arise from the thermal velocities.

Atom interferometers are always run in pairs with the same lasers driving both interferometers in order to remove laser phase noise. The paired interferometers also reduce other common mode backgrounds such as the Sagnac effect. The distance between these interferometers can be large and a benchmark value of several meters will be used. Finally, interferometers are run with N_a atoms simultaneously in a bunch and the full experiment is performed N_b times. N_a is determined by the rate for cooling atoms and $10^8/s$ is currently possible. The interrogation time for the experiment will be $T \sim 0.1s$, so a benchmark values of $N_a \sim 10^7$ is reasonable. In several days $N_b \sim 10^7$ trials can be run and gives a shotnoise phase sensitivity of $\delta \phi = N_a^{-\frac{1}{2}} N_b^{-\frac{1}{2}} \sim 10^{-7}$.

Atomic fountains are frequently used in AI and start with an ensemble of evaporatively cooled atoms ($\tau < \mu K$) in a magneto-optical trap (MOT) that localizes that atoms to $\sigma_x \sim 100 \mu m$. The atoms are then launched with a velocity, v_l , vertically through a series of multiple Bragg or Raman transitions. The atoms subsequently follow ballistic motion for an interrogation time, $T = q/v_l$, defining v_l at the initial $\frac{\pi}{2}$ pules and performing the π pulse occurs at the apex of the trajectory. In atomic fountains, the atoms are instantaneously in free fall and decoupled from their environment except during periods when they are coupled to the lasers which last 10^{-5} s. The atoms are more isolated than meso- or macroscopic measurements that are vibrationally coupled to the environment and essentially removes the "chopping" used to isolate torsional pendulums or cantilevers from the environment.

Configuring the interferometer as a gyroscope, with v_l perpendicular to v_r and v_i , allows the atom's ballistic trajectory to be parallel to a planar face of the mass. This maximizes the time that the atoms spend close to the source mass, thus making a signal from a new short distance force as large as possible. The interferometer is sensitive to the potential as a function of distance away from the surface of the source mass if the recoil velocity is perpendicular to this face. By mapping out the potential, it is possible to look for new contributions beyond the Standard Model. This configuration minimizes the Earth's gravity; however, the phase from the Corriolis force (Sagnac effect) is maximized and controlling this is an important background discussed below.



FIG. 1: The diagram of the proposed experiment where the phase from the grey source mass is measured at distances of x_N and x_F from the nearer of the paired interferometers. The plane in gold represents a thin Casimir shield fitted with retroreflectors that allow optical access for the right moving laser.

The relative phase between the two paths arises from

several different contributions and not many exact results are known. There is a semi-classical, perturbative method for computing the phase differences and at lowest order in the potential, V(x), speed of light, c, and the width of the wave packet, σ_x , the general result is that the phase difference is integral of the perturbing potential over the unperturbed paths. There are several phase difference results that will be useful in deriving the sensitivity. The first is if the potential only depends on the position in the direction of v_r and where v_i is not important

$$\hbar\phi = (V(v_r T) - V(0))T \tag{2}$$

$$= \frac{V'}{m}\hbar k_{\rm eff}T^2 + \frac{V''}{m^2}(\hbar k_{\rm eff})^2T^3 + \cdots$$
 (3)

where the initial position of the atom is taken to be x = 0. In the second half the potential has been Taylor expanded, if applicable. The first term is proportional to the acceleration, and the second term is referred to as the recoil phase because it vanishes as m becomes large, keeping $k_{\rm eff}$ fixed. Finally, if v_i is important, the above expression becomes

$$\hbar\phi = \left(\frac{W(x_1 + x_2) - W(x_2) - W(x_1) + W(0)}{\left(x_1^{-1} - x_2^{-1}\right)^{-1}}\right)T \quad (4)$$

where $x_1 = (v_r+v_i)T$, $x_2 = v_iT$, and $W(x) = \int^x dx' V(x')$. If the potential depends on the distance in the v_l direction, no closed form is possible, but simple expressions can be obtained if V(x, y) is Taylor expandable.

PROPOSED EXPERIMENTAL DESIGN

Newton's constant is not known to a precision better than 10^{-4} , so it is necessary to perform a series of measurements to remove absolute sensitivity to G_N . The most straightforward manner to remove the uncertainty in G_N is to test the r^{-1} behavior of gravity by having a moveable source mass. The source mass will be taken to be a cylinder of radius, R, and width, w, and density, ρ , with the circular face of the cylinder forming a vertical plane. This geometry is motivated by calculational simplicity and none of the results depend sensitively upon the geometry. The height of the atomic fountains, $h = v_l^2/2g < R$, will take place near the center of the cylinder's face.

The Newtonian potential near the center of the cylinder can be calculated in the far field, $x \gg R$, and near field, $x \ll R$, limits near the center of the cylinder. In the far field limit

$$\frac{V_N(x,r)}{G_N\rho m} = \frac{\pi R^2 w}{x} \left(1 - \frac{w}{x} - \frac{3R^2}{16x^2} - \frac{r^2}{2x^2} \right)$$
(5)

where x is the distance to cylinder's face and r is the

distance from the cylinder's center.¹ In the near field limit the Newtonian potential is given by

$$\frac{V_N(x,r)}{G_N\rho m} = \frac{V_0(r)}{m} + 2\pi x \left((w^2 + R^2)^{\frac{1}{2}} - R - w \right) \\
+ \frac{\pi w x^2}{(w^2 + R^2)^{\frac{1}{2}}} - \frac{\pi r^2 x}{2} \left(\frac{R^2}{(w^2 + R^2)^{\frac{3}{2}}} - \frac{1}{R} \right) (6)$$

where $V_0(r)$ is an unmeasurable function, independent of the distance from the source.

There are several limits necessary for the Yukawa potential. The first is $\lambda \ll R, w$ where the potential from cylinder is

$$\frac{V_Y(x)}{\alpha G_N \rho m} = \begin{cases} 2\pi \lambda^2 \exp(-x/\lambda) & \lambda < R^2/x \\ \pi \lambda R^2 x^{-1} \exp(-x/\lambda) & \lambda > R^2/x \end{cases} .$$
(7)

For $\lambda \gg R, w$, the Yukawa potential looks Newtonian plus a correction arising from Taylor expanding the exponential. In the far field limit $(x \gg R)$ the Yukawa potential is

$$\frac{V_Y(x)}{\alpha G_N \rho m} = \frac{V_N(x)}{G_N \rho m} + \frac{\pi R^2 w x}{3\lambda^2}.$$
 (8)

Notice the absence of an $\mathcal{O}(\lambda^{-1})$ term because it is always an unmeasurable constant. In the near field limit ($x \ll R$), the Yukawa potential becomes

$$\frac{V_Y(x)}{\alpha G_N \rho m} = \frac{V_N(x)}{G_N \rho m} + \frac{2\pi x}{3\lambda^2} \left((w^2 + R^2)^{\frac{3}{2}} - R^3 - w^3 \right).$$
(9)

The physical size of the experiment ultimately limit the sensitivity. The size of the source mass sets the λ with maximum sensitivity and the benchmark value used is $R \leq 1$ m and w < 1 m. The other relevant physical constraint is how near the source mass can get to the interferometers, $x_N^{\min} \geq 200\mu$ m. The distance that the source mass can be moved from the interferometers does not limit the sensitivity so long as $x_F^{\max} \gtrsim R, w$.

The strategy to distinguish Newtonian gravity from a new Yukawa potential is to perform a near and a far measurement of the phase. The near measurement fixes what the Newtonian prediction is for the far measurement. If the inclusion of a Yukawa potential with strength α and range λ causes a difference between the far prediction and the far measurement greater than the shot noise limit, then this Yukawa potential is visible assuming that no backgrounds or uncertainties are larger. The scaling of the limits depend on λ and there two cases to be considered. If, $\lambda < R$, it is possible to get within the r^{-1} behavior of the Yukawa potential and move outside its range; furthermore, the radius of the cylinder is not determining the sensitivity. In the second case $\lambda > R, w$, it is possible to get within the r^{-1} and outside the range of the potential, but the size of the source mass is determining the sensitivity. For large λ , it may seem beneficial to move the source mass further from the source to make the difference between a Yukawa potential and the Newtonian potential more pronounced, growing as r^2/λ^2 ; however, the size of the Newtonian phase shift is falling as r^{-2} meaning that there is no parametric gain for moving the source mass a distance greater than R from the interferometers for any value of λ .

The biggest challenge of this experiment is the strategy of using a near measurement to extrapolate to a far prediction. The challenge is knowing both the source mass position and orientation precisely enough to make a 10^{-6} or better prediction for the far Newtonian prediction. Examining the subleading terms in the Newtonian potentials in (5) and (6), if there is an uncertainty in the position of the cylinder of δx , then there is an uncertainty in the Newtonian potential of $\delta x/R$ or $\delta x/x$, respectively. By having h < R reduces the uncertainty in the Newtonian prediction from uncertainty in the initial height of the atom. It is challenging but achievable to know the position of the block to $\delta x \sim 1 \mu m$ to be sensitive to $\alpha \sim 10^{-6}$; however, future improvements in sensitivity will not be limited by this. A better solution to knowing the position and orientation of the block is to use multiple interferometers situated near $r \sim R$ to actively measure the position and orientation Since the edge effects become $\mathcal{O}(1)$ of the source. near the edges, it is possible to use these additional measurements to locate the block and then use a central interferometer to use the near measurement to make the far prediction. This strategy will require six additional interferometers to over-determine the source's solid body coordinates. The remaining challenge is to keep these seven interferometers locked in place as the source mass moves, but this should be possible to a much greater accuracy. There is a residual uncertainty coming from "jitter" in the location of the MOTs. This motion is of the order of $\delta x \sim 1 \mu m$; however, it is stochastic with respect to the number of bunches of atoms, N_b , and therefore the uncertainty is $\delta x/RN_b^{\frac{1}{2}} \sim 10^{-9}$ and only limiting after several rounds of improvements.

The Sagnac effect, the phase induced by the Corriolis force is large, $\phi_{\text{Sag}} = k_{\text{eff}} v_l \omega_{\oplus} T^2 \sim 10^2$, where ω_{\oplus} is the angular velocity of the earth. The use of paired interferometers described above cancels the leading order Sagnac effect. The novel method of actively reducing the Sagnac effect is to rotate the lasers to compensate for the rotation of the Earth. It is possible to rotate lasers with nanoradian precision which reduces the Sagnac effect by a factor of 10^{-4} . The dominant way that the Sagnac

¹ The absence of an $\mathcal{O}(r/x)$ correction to the potential is due to the cylindrical symmetry and will not be important for the results.

effect contaminates the signal is from variation in relative v_l of the two interferometers which is stochastic in the number of bunches, reducing the size by $N_b^{-\frac{1}{2}}$. The final reduction in Sagnac contamination must come from vibration isolation and requires $\delta v_l^{\text{rel}}/v_l < 10^{-2}$.

The Casimir potential between an atom and a conducting plate is given by $V(x) = \hbar c \alpha_0 / x^4$, with α_0 being the polarizability of the atom and is 59.4Å³ for Cs[23]. The phase difference arising from the Casimir potential arises from (2) or (4) rather than (3) because of its rapid fall off. These reduce the size of the Casimir force relative to a macroscopic measurement device and it is not important for distances, (and consequently λ) greater than $\mathcal{O}(100\mu \text{m})$, but becomes important at shorter distances. In order to gain to reduce any residual phases, having a thin Casimir shield ($\mathcal{O}(50\mu m)$ in width) that isolates the atom from the source mass' position is helpful. While the the Casimir potential from the shield will still be measurable, it will not be correlated with the mass' position and therefore not directly a systematic effect. The primary way the Casimir potential enters as a background is by having the source mass deflect the shield and additionally through the "jitter" of the MOTs. The deflection of the shield is sufficiently small so long as the source mass is $\mathcal{O}(30\mu m)$ from the shield. The jitter gives a phase uncertainty of $\delta\phi_{\rm Cas}/\phi_{\rm Cas} \sim (\delta x/x)/N_b^{\frac{1}{2}} \sim 10^{-4}$ for $x = 100 \mu {\rm m}$ and is sufficiently small.² In addition to isolating the atoms, it will be necessary to attach retroreflectors on the shield to provide optical access for the outward propagating lasers necessary to drive the Raman transitions.

EXPECTED SENSITIVITY AND FUTURE IMPROVEMENTS

With the results of the previous section, the sensitivity to α and λ can be computed. Using the previously stated benchmarks for Cs the phase sensitivity of $\delta \phi =$ 10^{-7} from $N_a N_b = 10^{14}$, R, w = 1m, $x_{\rm N}^{\rm min} = 200 \mu$ m, h = 10cm, $\rho = 12 {\rm g/cm}^3$ for Pb and $\tau = 10$ nK, the sensitivity curve is plotted in Fig. 2 relative in blue to current experimental limits shown black. The peak sensitivity is $\alpha \sim 3 \times 10^{-6}$ and occurs for $\lambda \sim 0.5$ m which is determined by the size of the source mass. For 1mm $< \lambda < 10$ m, current AI is more sensitive than existing experiments. Additionally, from 100μ m $< \lambda <$ 1mm current AI techniques matches the experimental limits. This motivates considering future experimental improvements to if sensitivity is possible down to $\lambda \sim$ 100μ m.





FIG. 2: The current limits on new forces and where AI can probe with current nominal sensitivity and future improvements described in the text.

In the near future it will be possible to increase the magnitude of the momentum transferred to the atoms in the interferometer using a technique called large momentum transfer (LMT). LMT uses repeated Raman or Bragg transitions during the laser pulses that impart on the atoms up to 100 times more momentum as a single Raman transition. LMT significantly impacts sensitivity for larger λ , increasing sensitivity by a factor of 100; however, for shorter wavelengths, where $\lambda < v_r T$, there is no significant gain to sensitivity because the atoms immediately leave the region being sourced by Yukawa potential.³ The sensitivity is shown in Fig. 2 in green.

On the short distance front, increases in sensitivity must come through increases in phase sensitivity. One possibility is to increase the number of atoms being used in the experiment, which is limited by the length of the experiment and the rate for cooling atoms. In the future, a more effective way to increase sensitivity would be to use wave packets of entangled atoms where it is possible to have the sensitivity scale as N_a^{-1} (in contrast to $N_a^{-\frac{1}{2}}$) which is known as Heisenberg limited statistics (HS). HS potentially allows significant gains in sensitivity and the sensitivity curve is shown for a phase sensitivity of $\delta \phi = 10^{-9}$ in red in Fig. 2. In yellow, the sensitivity is shown for combining a LMT factor 100 and $\delta \phi = 10^{-9}$; however, at this level the stochastic uncertainty in the Newtonian prediction starts to become limiting. There are some caveats that may limit the sensitivity at shorter The first is that all of the phase results distances. are computed in the semi-classical limit; however, when $\lambda < \sigma_x$ this approximation breaks down and a more complete quantum mechanical treatment is necessary. Additionally, the interaction between the Casimir shield and atoms must be considered in much more detail,

³ If there is an initial velocity, v_i , from either a need to Dopplerselect atomic transitions or thermal motion, there is a small gain at short distances proportional to $(1 + v_i/v_r)^{-1}$ shown in (4).

particularly for the case of HS where preventing the decoherence of the wave packet is necessary.

This Letter has demonstrated that atom interferometry has the potential to improve the sensitivity to new forces in the 100μ m to 1km range using current technology or technologies that will be available in the near future. Additionally, atom interferometry can be useful in testing other types of forces other than the standard α - λ Yukawa potential such as spin, velocity and composition dependent forces.

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