## Study of $D_{s J}$ decays to $D^{*} K$ in inclusive $e^{+} e^{-}$interactions

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#### Abstract

We observe the decays $D_{s 1}^{*}(2710)^{+} \rightarrow D^{*} K$ and $D_{s J}^{*}(2860)^{+} \rightarrow D^{*} K$ and measure their branching fractions relative to the $D K$ final state. We also observe, in the $D^{*} K$ mass spectrum, a new broad structure at a mass of $\left(3044 \pm 8_{\text {stat }}\left({ }_{-5}^{+30}\right)_{\text {syst }}\right) \mathrm{MeV} / c^{2}$ having a width $\Gamma=\left(239 \pm 35_{\text {stat }}\left({ }_{-42}^{+46}\right)_{\text {syst }}\right)$ MeV . To obtain this result we use $470 \mathrm{fb}^{-1}$ of data recorded by the BABAR detector at the PEP-II asymmetric-energy $e^{+} e^{-}$storage rings at the Stanford Linear Accelerator Center running at center-of-mass energies near 10.6 GeV .


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## I. INTRODUCTION

[^0]The spectrum of known $c \bar{s}$ states can be described as two S-wave states $\left(D_{s}^{+}, D_{s}^{*+}\right)$ with $J^{P}=0^{-}, 1^{-}$, and four P-wave states $\left(D_{s 0}^{*}(2317)^{+}, D_{s 1}(2460)^{+}, D_{s 1}(2536)^{+}\right.$, $\left.D_{s 2}^{*}(2573)^{+}\right)$with $J^{P}=0^{+}, 1^{+}, 1^{+}, 2^{+}$. Whether this picture is correct remains controversial because the states at $2317 \mathrm{MeV} / c^{2}$ and $2460 \mathrm{MeV} / c^{2}$ [1] had been expected to lie at much higher masses [2]. Since the discovery of the new $D_{s}^{+}$mesons much theoretical work has been done, however new experimental results are needed in order to understand this sector of spectroscopy.

Recently, two new $D_{s}^{+}$mesons have been discovered, $D_{s 1}^{*}(2710)^{+}[3,4]$ and $D_{s J}^{*}(2860)^{+}[3]$. The analysis of $D_{s 1}^{*}(2710)^{+}$produced in $B$ decays gives the assignment
$J^{P}=1^{-}$. For $D_{s J}^{*}(2860)^{+}$assignments of $J^{P}=0^{+}[5,6]$ and $J^{P}=3^{-}[7]$ have been proposed.

We report here on a search for new $D_{s J}^{+}$mesons in the mass spectrum of $D^{(*)} K$ inclusively produced at the PEP-II asymmetric-energy $e^{+} e^{-}$storage rings and recorded by the BABAR detector. This paper is organized as follows. In Sect. II we give a short description of the BABAR experiment and in Sect. III we describe the data selection. Section IV is devoted to the study of the $D K$ system and in Sect. V we present the study of the $D^{*} K$ system. In Sect. VI we describe fits to the $D^{*} K$ mass spectrum while in Sect. VII we present an analysis of the angular distributions. Measurements of ratios of branching fractions are described in Sect. VIII and we summarize the results in Sect. IX.

## II. THE BABAR EXPERIMENT

This analysis is based on a $470 \mathrm{fb}^{-1}$ data sample recorded at the $\Upsilon(4 S)$ resonance and 40 MeV below the resonance. The BABAR detector is described in detail elsewhere [8]. We mention here only the parts of the detector which are used in the present analysis. Charged particles are detected and their momenta measured with a combination of a cylindrical drift chamber ( DCH ) and a silicon vertex tracker (SVT), both operating within the 1.5 T magnetic field of a superconducting solenoid. Information from a ring-imaging Cherenkov detector combined with energy-loss measurements in the SVT and DCH provide identification of charged kaon and pion candidates. The energies and locations of showers associated with photons are measured with a $\mathrm{CsI}(\mathrm{Tl})$ electromagnetic calorimeter.

## III. DATA SELECTION

We reconstruct the inclusive processes [9] listed in Table I. A particle identification algorithm is applied to all the tracks. Charged kaon identification has an average efficiency of $90 \%$ within the acceptance of the detector and an average pion-to-kaon misidentification probability of $1.5 \%$ per particle.

For all channels we perform a vertex fit for the $D^{0}$ and $D^{+}$daughters and require a $\chi^{2}$ probability greater than $0.1 \%$. For the $\pi^{0}$ candidates in channels (3),(4), and (6), we combine all photons with energy greater than 30 MeV in pairs, perform a fit with a $\pi^{0}$ mass constraint, and require a $\chi^{2}$ probability greater than $1 \%$. For the $D^{0} \rightarrow K^{-} \pi^{+} \pi^{0}$ decay channel we also perform a kinematic fit with a $D^{0}$ mass constraint. We obtain $K_{S}^{0} \rightarrow \pi^{+} \pi^{-}$candidates by means of a vertex fit and require a $\chi^{2}$ probability greater than $2 \%$. We accept only $K_{S}^{0}$ candidates with decay length greater than 0.5 cm . To obtain $D^{*+} K_{S}^{0}$ candidates, where $D^{*+} \rightarrow D^{0} \pi^{+}$, we combine fitted $D^{0}$ and $K_{S}^{0}$ candidates with a $\pi^{+}$candidate using a vertex fit which constrains the overall vertex to be


FIG. 1: (a) $K^{-} \pi^{+}$, (b) $K^{-} \pi^{+} \pi^{+}$mass distributions for all candidate events in channels (1) and (2) respectively.
located in the interaction region, requiring a $\chi^{2}$ probability greater than $0.1 \%$. Similarly, for $D^{*+} K_{S}^{0}$ candidates where $D^{*+} \rightarrow D^{+} \pi^{0}$ we combine fitted $D^{+}, K_{S}^{0}$ and $\pi^{0}$ candidates using a vertex fit which constrains the overall vertex to be located in the interaction region, requiring a $\chi^{2}$ probability greater than $0.1 \%$. Background from $e^{+} e^{-} \rightarrow B \bar{B}$ events is removed by requiring the center of mass momentum $p^{*}$ of the $D K$ or $D^{*} K$ system to be greater than $3.3 \mathrm{GeV} / c$.

To improve the signal to background ratio for channels with $D^{0} \rightarrow K^{-} \pi^{+}$we study the distribution of the angle $\theta_{K^{-}}$formed by the $K^{-}$from $D^{0}$ decay in the $K^{-} \pi^{+}$ rest frame with respect to the $K^{-} \pi^{+}$direction in the laboratory system. This distribution is expected to be flat. We observe an accumulation of combinatorial background close to $\cos \theta_{K^{-}}=1$. We improve the signal to background ratio by requiring $\cos \theta_{K^{-}}<0.9$.

To improve the signal to background ratio for $D^{+} \rightarrow$ $K^{-} \pi^{+} \pi^{+}$, we compare the $D^{+}$three-momentum and its flight direction and define $d_{x y}$ as the signed projected distance in the transverse plane. Background events are removed by requiring $d_{x y}>0$. The resulting $K^{-} \pi^{+}$and $K^{-} \pi^{+} \pi^{+}$invariant mass spectra for candidates in channels (1) (where we require in addition a reconstructed $K^{+}$) and (2) (where we require in addition a reconstructed $K_{S}^{0}$ ) are shown in Fig. 1. There are on average 1.01 candidates per selected event in both samples, and all candidates are retained for further analysis.

We fit the $K^{-} \pi^{+}$and $K^{-} \pi^{+} \pi^{+}$invariant mass spectra using a linear background and a single Gaussian peak obtaining $\sigma_{D^{0}}=7.6 \mathrm{MeV} / c^{2}$ and $\sigma_{D^{+}}=6 \mathrm{MeV} / c^{2}$. The signal region is defined within $\pm 2 \sigma$ while sideband regions are defined within $(-6 \sigma,-4 \sigma)$ and $(4 \sigma, 6 \sigma)$. The $D^{0}$ signal region contains $1.98 \times 10^{6}$ combinations with a purity $P=N_{S} /\left(N_{S}+N_{B}\right)=0.84$, where $N_{S}\left(N_{B}\right)$ is the number of signal (background) combinations. The $D^{+}$signal region contains $0.58 \times 10^{6}$ combinations with a purity $P=0.75$.

TABLE I: List of reconstructed final states. Here $X$ indicates the rest of the event, with any number of charged or neutral particles.

| Channel Reaction | $D^{*}$ decay mode | $D$ decay mode |  |
| :--- | :--- | :--- | :--- |
| $(1)$ | $e^{+} e^{-} \rightarrow D^{0} K^{+} X$ |  | $D^{0} \rightarrow K^{-} \pi^{+}$ |
| $(2)$ | $e^{+} e^{-} \rightarrow D^{+} K_{S}^{0} X$ |  | $D^{+} \rightarrow K^{-} \pi^{+} \pi^{+}$ |
| $(3)$ | $e^{+} e^{-} \rightarrow D^{* 0} K^{+} X$ | $D^{* 0} \rightarrow D^{0} \pi^{0}$ | $D^{0} \rightarrow K^{-} \pi^{+}$ |
| $(4)$ | $e^{+} e^{-} \rightarrow D^{*+} K_{S}^{0} X$ | $D^{*+} \rightarrow D^{+} \pi^{0}$ | $D^{+} \rightarrow K^{-} \pi^{+} \pi^{+}$ |
| $(5)$ | $e^{+} e^{-} \rightarrow D^{*+} K_{S}^{0} X$ | $D^{*+} \rightarrow D^{0} \pi^{+}$ | $D^{0} \rightarrow K^{-} \pi^{+}$ |
| $(6)$ | $e^{+} e^{-} \rightarrow D^{*+} K_{S}^{0} X$ | $D^{*+} \rightarrow D^{0} \pi^{+}$ | $D^{0} \rightarrow K^{-} \pi^{+} \pi^{0}$ |
| $(7)$ | $e^{+} e^{-} \rightarrow D^{*+} K_{S}^{0} X$ | $D^{*+} \rightarrow D^{0} \pi^{+}$ | $D^{0} \rightarrow K^{-} \pi^{+} \pi^{+} \pi^{-}$ |

## IV. STUDY OF THE DK SYSTEMS

We first study the $D^{0} K^{+}$and $D^{+} K_{S}^{0}$ mass spectra. In an inclusive environment the $D^{0}$ and $D^{+}$can come from $D^{*}$ decays. Candidate $D^{0} K^{+}$pairs where the $D^{0}$ is a $D^{*}$-decay product are identified by forming $D^{0} \pi^{+}, D^{0} \pi^{0}$, and $D \gamma$ combinations and requiring that the invariantmass difference between one of those combinations and the $D^{0}$ be within $\pm 2 \sigma$ of the known $D^{*}-D$ mass difference. Events belonging to these possible reflections (except for $D^{* 0} \rightarrow D^{0} \gamma$ events, which could not be isolated cleanly) are removed. In the same way, $D^{+} K_{S}^{0}$ combinations where the $D^{+} \pi^{0}$ and $D^{+}$invariant-mass difference is found to be within $\pm 2 \sigma$ of the known $D^{*}-D$ mass difference are removed.

We also study the distribution of $\theta_{K^{+}}\left(\theta_{K_{S}^{0}}\right)$, the angle between the $K^{+}\left(K_{S}^{0}\right)$ direction in the $D K$ rest frame and the $D K$ direction in the laboratory frame. We expect the distribution of this angle to be symmetric around zero [10], but we observe an accumulation of combinatorial background close to $\cos \theta_{K}=-1$. Due to the jetlike nature of the reaction $e^{+} e^{-} \rightarrow c \bar{c}$ we interpret this background as due to combinations for which the $K$ comes from the jet opposite to the $D$ meson. We therefore apply a conservative cut requiring $\cos \theta_{K}>-0.8$.

The resulting $D^{0} K^{+}$and $D^{+} K_{S}^{0}$ mass spectra are shown in Fig. 2. To improve the mass resolution, the nominal $D$ mass and the reconstructed 3 -momentum are used to calculate the $D$ energy for channels (1) and (2). The two mass spectra in Fig. 2 present similar features. The single bin peak at $2.4 \mathrm{GeV} / c^{2}$ results from decays of $D_{s 1}(2536)^{+}$to $D^{* 0} K^{+}$or $D^{*+} K_{S}^{0}$ in which the $\pi^{0}$ or $\gamma$ from the $D^{*}$ decay is missed. Since the $D_{s 1}(2536)^{+}$is believed to have $J^{P}=1^{+}$, decay to $D K$ is forbidden by angular momentum and parity conservation. We also observe a prominent narrow signal due to the $D_{s 2}^{*}(2573)^{+}$, a broad structure centered at the mass of the $D_{s 1}^{*}(2710)^{+}$, and a narrower structure at the position of the $D_{s J}^{*}(2860)^{+}$.

We perform a simultaneous binned $\chi^{2}$ fit to the two sideband-subtracted $D K$ mass spectra shown in Fig. 3(a) and Fig. 3(c). The fit range extends from $2.42 \mathrm{GeV} / c^{2}$ to $3.2 \mathrm{GeV} / c^{2}$ (the lower bound is chosen to exclude the $D_{s 1}(2536)^{+}$reflection). The background
for each of the two $D K$ mass distributions is described by a threshold function: $\left(m-m_{\mathrm{th}}\right)^{\alpha} e^{-\beta m-\gamma m^{2}-\delta m^{3}}$ where $m_{\mathrm{th}}=m_{D}+m_{K}$. In this fit, the $D_{s 2}^{*}(2573)^{+}$, $D_{s 1}^{*}(2710)^{+}$and $D_{s J}^{*}(2860)^{+}$peaks are described with relativistic Breit-Wigner lineshapes where spin-2 is assumed for $D_{s 2}^{*}(2573)^{+}$, spin- 1 for $D_{s 1}^{*}(2710)^{+}$and spin0 for $D_{s J}^{*}(2860)^{+}$. The Breit-Wigner function includes Blatt-Weisskopf form factors [11]. Mass resolution estimates are obtained using simulated events. We obtain single-Gaussian $\sigma$ 's of $2.7 \mathrm{MeV} / c^{2}$ and $3.6 \mathrm{MeV} / c^{2}$ at $D K$ masses of 2.71 and $2.86 \mathrm{GeV} / c^{2}$ respectively. Since the width values for the resonances present in the $D K$ mass spectra are much larger than these, resolution effects are ignored.

The result of the fit is shown in Figs. 3(a) and 3(c), and the parameter values obtained are summarized in Table II (Fit A). Figures 3(b) and 3(d) show also the fitted-background-subtracted $D_{K^{-} \pi^{+}}^{0} K^{+}$, and $D_{K^{-} \pi^{+} \pi^{+}}^{+} K_{s}^{0}$ invariant mass distributions. The fitted parameter values for the $D_{s J}^{*}(2860)^{+}$state are in agreement with our previous measurement [3], while the central value of the $D_{s 1}^{*}(2710)^{+}$mass is slightly higher than before.

## V. STUDY OF THE $D^{*} K$ SYSTEM

The $\Delta m=m(D \pi)-m(D)$ distributions for the five channels (3)-(7), are shown in Fig. 4. Backgrounds are small for channels (5)-(7) but larger for channels (3)-(4). Table III gives the fitted parameter values of the $\Delta m$ distributions together with purities and the definitions of signal and sideband regions. The values of $\sigma$ reported in Table III are obtained from fits performed using a polynomial background and a single Gaussian.

We have also studied the distributions of the angle $\theta_{K^{+}}^{*}$ $\left(\theta_{K_{S}^{0}}^{*}\right)$ between the $K^{+}\left(K_{S}^{0}\right)$ direction in the $D^{*} K$ rest frame and the $D^{*} K$ direction in the laboratory frame. We expect the distributions of this angle to be symmetric around zero for signal but we observe an accumulation of combinatorial background close to $\cos \theta_{K}^{*}=-1$. As in the case of the $D K$ system, we interpret this as being due to combinations for which the $K$ comes from the jet opposite to that yielding the $D^{*}$ meson. We therefore apply the conservative selection criterion $\cos \theta_{K}^{*}>-0.8$.


FIG. 2: $D K$ invariant mass distributions for (a) $D_{K^{-} \pi^{+}}^{0} K^{+}$, and (b) $D_{K^{-} \pi^{+} \pi^{+}}^{+} K_{s}^{0}$. Shaded histograms represent the $D$ mass sideband regions. The arrows indicate the expected positions of the $D_{s 2}^{*}(2573)^{+}, D_{s 1}^{*}(2710)^{+}$, and $D_{s J}^{*}(2860)^{+}$.


FIG. 3: Sideband-subtracted $D K$ invariant mass distributions for (a) $D_{K^{--\pi^{+}}}^{0} K^{+}$, (c) $D_{K^{-} \pi^{+} \pi^{+}}^{+} K_{s}^{0}$; (b) and (d) show the fitted-background-subtracted mass spectra. The curves show the functions described in the text.

TABLE II: The $\chi^{2} / \mathrm{NDF}$ and resonance parameter values obtained from the fits to the $D K$ and $D^{*} K$ mass spectra. Masses and widths are given in units of $\mathrm{MeV} / c^{2}$ and MeV , respectively. Uncertainties are statistical only.

| Fit | $\chi^{2} / \mathrm{NDF}$ | $D_{s 1}^{*}(2710)^{+}$ | $D_{s J}^{*}(2860)^{+}$ | $D_{s J}(3040)^{+}$ |
| :--- | :---: | :---: | :---: | :---: |
| $\mathrm{A}(D K)$ | $85 / 56$ | $m=2710.0 \pm 3.3$ | $m=2860.0 \pm 2.3$ |  |
|  |  | $\Gamma=178 \pm 19$ | $\Gamma=53 \pm 6$ |  |
| $\mathrm{~B}\left(D^{*} K\right)$ | $51 / 33$ | $m=2712 \pm 3$ | $m=2865.2 \pm 3.5$ | $m=3042 \pm 9$ |
| $\mathrm{C}\left(D K+D^{*} K\right)$ | $147 / 91$ | $\Gamma=103 \pm 8$ | $\Gamma=44 \pm 8.3$ | $\Gamma=214 \pm 34$ |
|  |  | $\Gamma=152 \pm 7$ | $m=2860 \pm 2$ | $m=3045 \pm 8$ |
|  |  |  | $\Gamma=52 \pm 5$ | $\Gamma=246 \pm 31$ |
|  |  |  | $\Gamma=2866 \pm 3$ |  |
| D $\left(D K+D^{*} K\right)$ | $149 / 93$ | $m=2710 \pm 2$ | $m=2862 \pm 2$ | $m=3044 \pm 8$ |
|  |  | $\Gamma=152 \pm 7$ | $\Gamma=48 \pm 3$ | $\Gamma=239 \pm 35$ |
| $\mathrm{E}\left(D^{*} K\right)$ | $65 / 38$ | $m=2716.7 \pm 2.5$ |  |  |
| F $\left(D^{*} K\right)$ |  | $\Gamma=108 \pm 5$ |  | $m=3047 \pm 12$ |
|  | $39 / 34$ |  |  | $\Gamma=216 \pm 46$ |



FIG. 4: The $\Delta m$ distributions for channels (3)-(7) after applying the corresponding $D$-candidate mass selection criteria.

TABLE III: Fitted parameters of the $\Delta m$ distributions together with purities and definitions of the regions used for signal and background.

| Channel | mass <br> $\mathrm{MeV} / c^{2}$ | $\sigma \mathrm{MeV} / c^{2}$ | purity (\%) | Signal region Sideband region |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
| $(3) \Delta m\left(D_{K^{-} \pi^{+}}^{0} \pi^{0}\right)$ | 142.02 | 1.08 | 83.3 | $\pm 2.5 \sigma$ | $10 \sigma-15 \sigma$ |
| $(4) \Delta m\left(D_{K^{-} \pi^{+} \pi^{+}} \pi^{0}\right)$ | 140.63 | 0.893 | 76.6 | $\pm 2.5 \sigma$ | $10 \sigma-15 \sigma$ |
| (5) $\Delta m\left(D_{\left.K^{-} \pi^{+} \pi^{+}\right)}\right.$ | 145.43 | 0.288 | 94.9 | $\pm 5 \sigma$ | $12 \sigma-22 \sigma$ |
| (6) $\Delta m\left(D_{K^{-} \pi^{+} \pi^{0} \pi^{+}}^{0}\right)$ | 145.43 | 0.351 | 87.1 | $\pm 3 \sigma$ | $10 \sigma-16 \sigma$ |
| $(7) \Delta m\left(D_{K^{-} \pi^{+} \pi^{+} \pi^{-}}^{0} \pi^{+}\right)$ | 145.43 | 0.266 | 90.5 | $\pm 5 \sigma$ | $12 \sigma-22 \sigma$ |



FIG. 5: The $m\left(D^{*} K\right)$ distributions for channels (3)-(7); the shaded histograms show the mass spectra from the $D^{*} \Delta m$ sideband regions. The arrows indicate the expected positions of the $D_{s 1}^{*}(2710)^{+}$and $D_{s J}^{*}(2860)^{+}$.

Figure 5 shows the reconstructed $D^{*} K$ mass spectra for channels (3)-(7) of Table I. The shaded distributions represent the background estimates from the $\Delta m$ sideband regions. Each distribution shows a narrow spike at threshold due to the $D_{s 1}(2536)^{+}$meson. We also observe structures around 2.71 and $2.86 \mathrm{GeV} / c^{2}$.

We have compared these mass spectra with those from generic $e^{+} e^{-} \rightarrow \bar{c} c$ Monte Carlo events. These events
were generated using a detailed detector simulation and subjected to the same reconstruction and event-selection procedure as used for the data. We find that the simulation underestimates the $D_{s 1}(2536)^{+}$and $D_{s 2}^{*}(2573)^{+}$ signals relative to the background. No such discrepancy is found in the study of non-strange final states, therefore we attribute this effect to poor knowledge of the strangecharmed meson cross sections [12]. We apply weights to
the $D_{s 1}(2536)^{+}$and $D_{s 2}^{*}(2573)^{+}$production in the Monte Carlo in order to obtain better agreement with the data.

Figure $5(3)$ shows the presence of a peaking background in channel (3) around $2.7 \mathrm{GeV} / c^{2}$. Using the Monte Carlo data we identify this reflection, which is present in the signal and the sideband regions, as being due to the $D_{s 2}^{*}(2573)^{+}$. Combinations of $D K$ originating from this narrow peak associate with a random $\pi^{0}$ to produce a relatively narrow structure in the $2.7 \mathrm{GeV} / c^{2}$ region. Our Monte Carlo study verifies that this reflection is almost completely removed by performing the $\Delta m$ sideband subtraction.

The total $D^{*} K$ mass spectrum, $\Delta m$-sidebandsubtracted and summed over channels (3)-(7), is shown in Fig. 6 and compared with that obtained from Monte Carlo simulations. The $D^{*} K$ mass spectrum, above the $D_{s 1}(2536)^{+}$signal, shows the presence of structures around $2.71,2.86$, and $3.04 \mathrm{GeV} / c^{2}$. Corresponding resonance contributions are not included in the Monte Carlo simulation. Since such enhancements are not evident in the Monte Carlo $D^{*} K$ mass spectrum, we conclude that these structures are not produced by reflections from known resonances. Monte Carlo simulations also show that these enhancements are not due to reflections from the $D_{s J}$ resonances observed in the $D K$ mass spectrum.

A structure close to $2.57 \mathrm{GeV} / c^{2}$ is seen in the Monte Carlo and is due to the decay $D_{s 2}^{*}(2573)^{+} \rightarrow D^{*} K$, included in the simulation. However the data do not show evidence for such a decay.

## VI. FITS TO THE $D^{*} K$ MASS SPECTRUM

We perform a binned minimum $\chi^{2}$ fit to the combined $D^{*} K$ mass spectrum. The fit is performed in the region $(2.58-3.48) \mathrm{GeV} / c^{2}$. The background is parametrized as $e^{-\beta m-\gamma m^{2}-\delta m^{3}}$, which provides a good description of the Monte Carlo in the same mass range. The $D_{s J}^{+}$peaks are described with relativistic Breit-Wigner lineshapes. Here and in the following fits we assume $J^{P}=1^{-}$and $J^{P}=3^{-}$ respectively for $D_{s 1}^{*}(2710)^{+}$and $D_{s J}^{*}(2860)^{+}$decays to $D K$. For the $D^{*} K$ system, we use an angular momentum $L=1, L=3$, and $L=0$ for $D_{s 1}^{*}(2710)^{+}, D_{s J}^{*}(2860)^{+}$, and $D_{s J}(3040)^{+}$respectively. Average mass resolutions are $2.5 \mathrm{MeV} / c^{2}$ and $3.5 \mathrm{MeV} / c^{2}$ at $D^{*} K$ masses of 2.71 and $2.86 \mathrm{GeV} / c^{2}$ respectively. Since the width values for the resonances present in the $D^{*} K$ mass spectra are much larger than these, resolution effects are ignored.

We observe the presence, above the $D_{s 1}^{*}(2710)^{+}$and $D_{s J}^{*}(2860)^{+}$, of a new broad structure peaking at 3.04 $\mathrm{GeV} / c^{2}$. The resonance parameters resulting from the fit are given in Table II (Fit B) and the corresponding fitted curves are shown in Fig. 7. Modifying the background to include an extra term in the exponential does not improve the fit significantly. We find that the width of the $D_{s 1}^{*}(2710)^{+}$differs somewhat between the $D K$ and $D^{*} K$ fits, while the parameter values for the structure at 2.86 $\mathrm{GeV} / c^{2}$ in the $D^{*} K$ mass spectrum are consistent with
those of the $D_{S J}^{*}(2860)^{+}$obtained from the $D K$ mass spectrum.

We next repeat the fits removing the resonances one by one from the PDF. We compute the statistical significance of each structure as $\sqrt{\Delta \chi^{2}}$ where $\Delta \chi^{2}$ is the difference in the fit $\chi^{2}$ with and without the resonance included, taking into account the variation in the number of parameters $(\Delta \mathrm{NDF}=3)$. We obtain statistical significances of $12.4,6.4$, and 6.0 standard deviations for the $D_{s 1}^{*}(2710)^{+}, D_{s J}^{*}(2860)^{+}$, and $D_{s J}(3040)^{+}$respectively.

We then perform simultaneous fits to the two $D K$ mass spectra and to the total $D^{*} K$ mass spectrum to better constrain the $D_{s 1}^{*}(2710)^{+}$parameters. We first test the possibility that the structure around $2.86 \mathrm{GeV} / c^{2}$ in the $D^{*} K$ mass spectrum is different from the $D_{s J}^{*}(2860)^{+}$ state observed in the $D K$ mass spectrum by adding to the fit two new parameters. The results from the fit are summarized in Table II (Fit C). We find the parameters of the $D_{s J}^{*}(2860)^{+}$in the $D K$ mass spectrum consistent with those measured in the $D^{*} K$ mass spectrum.

Assuming therefore that we are observing the same state, we constrain the $D_{s J}^{*}(2860)^{+}$parameters to be the same in both the $D K$ and $D^{*} K$ mass spectra (Fit D). Taking this as our reference fit, we obtain the following parameters for the three states:

$$
\begin{array}{r}
m\left(D_{s 1}^{*}(2710)^{+}\right)=2710 \pm 2_{\text {stat }}\left({ }_{-7}^{+12}\right)_{\text {syst }} \mathrm{MeV} / c^{2} \\
\Gamma=149 \pm 7_{\text {stat }}\left({ }_{-52}^{+39}\right)_{\text {syst }} \mathrm{MeV} \\
m\left(D_{s J}^{*}(2860)^{+}\right)=2862 \pm 2_{\text {stat }}\left({ }_{-2}^{+5}\right)_{\text {syst }} \mathrm{MeV} / c^{2} \\
\Gamma=48 \pm 3_{\text {stat }} \pm 6_{\text {syst }} \mathrm{MeV} \\
m\left(D_{s J}(3040)\right)=3044 \pm 8_{\text {stat }}\left({ }_{-5}^{+30}\right)_{\text {syst }} \mathrm{MeV} / c^{2} \\
\Gamma=239 \pm 35_{\text {stat }}\left({ }_{-42}^{+46}\right)_{\text {syst }} \mathrm{MeV} \tag{3}
\end{array}
$$

Here systematic uncertainties take into account the range of values obtained in different fits, including fits to the spectra obtained after modifying the $p^{*}$ selection criterion, modifying the $\Delta m$ criteria, and removing the $\cos \theta_{K}$ requirement. They also account for uncertainties in the spin assignment.

## VII. ANGULAR ANALYSIS

Since we observe both $D_{s 1}^{*}(2710)^{+}$and $D_{s J}^{*}(2860)^{+}$decays to both $D K$ and $D^{*} K$, we assume they have natural parity $J^{P}=1^{-}, 2^{+}, 3^{-}, \ldots\left(J^{P}=0^{+}\right.$is ruled out because of the $D^{*} K$ decay). We further test this hypothesis using angular analysis. We compute the helicity angle $\theta_{h}$ as the angle formed by the $\pi$ from the $D^{*}$ decay with respect to the kaon, in the $D^{*}$ rest frame. The angular distribution for natural parity is expected to be [13]

$$
\begin{equation*}
\frac{d N}{d \cos \theta_{h}} \cong 1-\cos ^{2} \theta_{h} \tag{4}
\end{equation*}
$$



FIG. 6: The sideband-subtracted $m\left(D^{*} K\right)$ distributions summed over channels (3)-(7). (a) Data, (b) Monte Carlo. The arrow near threshold indicates the position of the peak due to the $D_{s 1}(2536)^{+}$, which is off-scale. The other arrows indicate the expected positions of the $D_{s 1}^{*}(2710)^{+}, D_{s J}^{*}(2860)^{+}$, and $D_{s J}(3040)^{+}$.


FIG. 7: (a) Fit to the $D^{*} K$ invariant mass spectrum. (b) Residuals after subtraction of the fitted background. The curves are described in the text.
since, for the parity and angular momentum conserving decay of such a parent state, the coupling in the parent rest frame to the helicity-0 $D^{*}$ state involves a vanishing Clebsch-Gordan coefficient. Figure 8 shows the $D^{*} K$ mass spectrum separated for $\left|\cos \theta_{h}\right|<0.4((\mathrm{a}),(\mathrm{b}))$ and $\left|\cos \theta_{h}\right|>0.4((\mathrm{c}),(\mathrm{d}))$. We clearly observe an enhanced signal to background rate for the $D_{s 1}^{*}(2710)^{+}$in the $\left|\cos \theta_{h}\right|<0.4$ region. This does not hold for the $D_{s J}(3040)^{+}$. The non-observation of $D_{s J}(3040)^{+} \rightarrow D K$ also suggests unnatural parity for this state.

The mass spectra separated according to the value of $\left|\cos \theta_{h}\right|$ allow a better determination of the $D_{s 1}^{*}(2710)^{+}$
and $D_{s J}(3040)^{+}$parameters. When fitting the $\left|\cos \theta_{h}\right|<$ 0.4 data (Fit E) we fix the $D_{s J}^{*}(2860)^{+}$and $D_{s J}(3040)^{+}$ shape parameters to those resulting from the simultaneous fit of the $D K$ and $D^{*} K$ mass spectra (Fit D). In fitting the $\left|\cos \theta_{h}\right|>0.4$ data (Fit F), we fix the parameters of $D_{s 1}^{*}(2710)^{+}$and $D_{s, J}^{*}(2860)^{+}$to those from Fit D. The resulting $D_{s 1}^{*}(2710)^{+}$and $D_{s J}(3040)^{+}$parameters are given in Table II and the fit results are shown by the curves in Fig. 8.

We have studied the $\cos \theta_{h}$ distributions for the $D_{s 1}^{*}(2710)^{+}$and $D_{s J}^{*}(2860)^{+}$by producing $D^{*} K$ mass spectra in six intervals of $\cos \theta_{h}$. The mass spectrum in


FIG. 8: Fits to the $D^{*} K$ invariant mass spectra for (a) $\left|\cos \theta_{h}\right|<0.4$; (c) $\left|\cos \theta_{h}\right|>0.4$. (b) and (d) show the data after the fitted background is subtracted.
each interval was fitted with fixed resonance parameters. However these values have all been varied within their statistical and systematic errors. The efficiencies as a function of $\cos \theta_{h}$ in the two mass regions are obtained from Monte Carlo simulation of the five channels involved in the analysis. We find that the efficiency is almost uniform as a function of $\cos \theta_{h}$ with a small slope which we parametrize by a linear function.

The efficiency corrected $D_{s 1}^{*}(2710)^{+}$and $D_{s J}^{*}(2860)^{+}$ yields are plotted in Fig. 9, together with the normalized expectations for natural parity. The curves have $\chi^{2} / \mathrm{NDF}$ of $18.7 / 5$ and $6.3 / 5$ respectively. The large $\chi^{2}$ obtained for the $D_{s 1}^{*}(2710)^{+}$is related to the large uncertainties in the background parametrization. Other spin hypotheses have been tested but they give much larger $\chi^{2}$ values. We conclude that both states are consistent with having natural parity. We do not perform a similar analysis for $D_{s J}(3040)^{+}$because of the large uncertainties arising from fitting a very broad resonance with limited statistics.



FIG. 9: Distributions in $\cos \theta_{h}$ for (a) the $D_{s 1}^{*}(2710)^{+}$and (b) the $D_{s J}^{*}(2860)^{+}$.

## VIII. BRANCHING FRACTIONS

From Table I it can be seen that it is possible to obtain ratios of branching fractions with reduced systematic uncertainties, for $D_{s 1}^{*}(2710)^{+}$and $D_{s J}^{*}(2860)^{+}$by using channels (3),(1) and (4),(2) respectively.

These ratios are computed as:

$$
\begin{equation*}
r_{i}=\frac{N\left(D_{s J}^{*} \rightarrow D^{*} K\right)}{N\left(D_{s J}^{*} \rightarrow D K\right)} \frac{\epsilon\left(D_{s J}^{*} \rightarrow D K\right)}{\epsilon\left(D_{s J}^{*} \rightarrow D^{*} K\right)} \tag{5}
\end{equation*}
$$

where the $N\left(D_{s J}^{*}\right)$ are the signal yields and the $\epsilon\left(D_{s J}^{*}\right)$ are the corresponding efficiencies, and $i=1,4$. We note that the only difference between numerator and denominator final states is the presence of an extra $\pi^{0}$ from the $D^{*}$ decay.

Assuming a constant total width, the yields are obtained by fitting the $D K$ and $D^{*} K$ mass spectra using the same $D_{s 1}^{*}(2710)^{+}$and $D_{s J}^{*}(2860)^{+}$parameters, and are summarized in Table IV. Efficiencies are evaluated using Monte Carlo simulations, and only the ratio of efficiencies

$$
\begin{equation*}
\epsilon_{r}=\frac{\epsilon\left(D_{s J}^{*} \rightarrow D^{*} K\right)}{\epsilon\left(D_{s J}^{*} \rightarrow D K\right)} \tag{6}
\end{equation*}
$$

is involved in the measurement. This ratio is consistent with being uniform as a function of $D K\left(D^{*} K\right)$ mass and its values are reported in Table IV.

Systematic uncertainties are summarized in Table V. The $D_{s J}^{*}$ parameters have been varied within their statistical and systematic errors, the $p^{*}$ cut has been changed to 3.1 and $3.5 \mathrm{GeV} / c$, the $\cos \theta_{K}$ cuts have been increased to -0.6 . The systematic error arising from Monte Carlo statistics appears as the error on the ratio between the efficiencies. The error on the $D^{*}$ branching fractions is obtained from Ref. [14]. The shape of the background has been modified by adding an extra term in the exponential; its contribution to the total error is found to be negligible. Finally the $D^{*} \Delta m$ signal region has been reduced to $\pm 2 \sigma$.

We obtain the following ratios of branching fractions:

$$
\begin{array}{r}
r_{1}=\frac{\mathcal{B}\left(D_{s 1}^{*}(2710)^{+} \rightarrow D^{* 0} K^{+}\right)}{\mathcal{B}\left(D_{s 1}^{*}(2710)^{+} \rightarrow D^{0} K^{+}\right)}= \\
0.88 \pm 0.14_{\text {stat }} \pm 0.14_{\text {syst }} \\
r_{2}=\frac{\mathcal{B}\left(D_{s J}^{*}(2860)^{+} \rightarrow D^{* 0} K^{+}\right)}{\mathcal{B}\left(D_{s J}^{*}(2860)^{+} \rightarrow D^{0} K^{+}\right)}=  \tag{8}\\
1.04 \pm 0.17_{\text {stat }} \pm 0.20_{\text {syst }}
\end{array}
$$

where $D^{* 0} \rightarrow D^{0} \pi^{0}$, and:

$$
\begin{array}{r}
r_{3}=\frac{\mathcal{B}\left(D_{s 1}^{*}(2710)^{+} \rightarrow D^{*+} K_{S}^{0}\right)}{\mathcal{B}\left(D_{s 1}^{*}(2710)^{+} \rightarrow D^{+} K_{S}^{0}\right)}=  \tag{9}\\
1.14 \pm 0.39_{\mathrm{stat}} \pm 0.23_{\mathrm{syst}}
\end{array}
$$

$$
\begin{array}{r}
r_{4}=\frac{\mathcal{B}\left(D_{s J}^{*}(2860)^{+} \rightarrow D^{*+} K_{S}^{0}\right)}{\mathcal{B}\left(D_{s J}^{*}(2860)^{+} \rightarrow D^{+} K_{S}^{0}\right)}=  \tag{10}\\
1.38 \pm 0.35_{\text {stat }} \pm 0.49_{\text {syst }}
\end{array}
$$

where $D^{*+} \rightarrow D^{+} \pi^{0}$.
Averaging $r_{1}, r_{3}$ and $r_{2}, r_{4}$ we obtain:

$$
\begin{equation*}
\frac{\mathcal{B}\left(D_{s 1}^{*}(2710)^{+} \rightarrow D^{*} K\right)}{\mathcal{B}\left(D_{s 1}^{*}(2710)^{+} \rightarrow D K\right)}=0.91 \pm 0.13_{\text {stat }} \pm 0.12_{\text {syst }} \tag{11}
\end{equation*}
$$

$$
\begin{equation*}
\frac{\mathcal{B}\left(D_{s J}^{*}(2860)^{+} \rightarrow D^{*} K\right)}{\mathcal{B}\left(D_{s J}^{*}(2860)^{+} \rightarrow D K\right)}=1.10 \pm 0.15_{\text {stat }} \pm 0.19_{\text {syst }} \tag{12}
\end{equation*}
$$

We also make a test of isospin conservation. We use the yields obtained from the fit to the appropriate mass spectra and correct for efficiency and branching fractions. We obtain, within the errors, similar rates for resonance decays to $D^{0} K^{+}$and $D^{+} K_{S}^{0}$ as well as for decays to $D^{* 0} K^{+}$ and $D^{*+} K_{S}^{0}$, as expected from isospin conservation.

We now compare these results with theoretical expectations. In the work of Ref. [15], for $J^{P}=1^{-}$, two different quark model assignments are proposed for the $D_{s 1}^{*}(2710)^{+}$: the $l=2$ ground state, $1^{3} D_{1}$, and the $l=0$ first radial excitation, $2^{3} S_{1}$. In the first case the ratio $\mathcal{B}\left(D_{s 1}^{*}(2710) \rightarrow D^{*} K\right) / \mathcal{B}\left(D_{s 1}^{*}(2710) \rightarrow D K\right)$ is expected to be $0.043 \pm 0.002$, in the second case $0.91 \pm 0.04$. In this framework the $D_{s 1}^{*}(2710)^{+}$can be identified as the first radial excitation of the $D_{s}^{*}(2112)$. The same assignment is derived from Ref. [6] where a mass of $2711 \mathrm{MeV} / c^{2}$ is predicted for the state $2^{3} S_{1}$. However, in this case the expected ratio is 3.55 , in significant disagreement with the measured value.

In Ref. [16], in the framework of chiral doublers, $J^{P}=1^{-}$states are expected at masses of 2632 and 2720 $\mathrm{MeV} / c^{2}$.

The observation of $D_{s J}^{*}(2860)^{+} \rightarrow D^{*} K$ rules out the $J^{P}=0^{+}$assignment suggested by Refs. [5, 6]. In Ref. [7] the $J^{P}=3^{-}$assignment is proposed; however the predicted $\mathcal{B}\left(D_{s J}^{*}(2860) \rightarrow D^{*} K\right) / \mathcal{B}\left(D_{s J}^{*}(2860) \rightarrow D K\right)$ is 0.39 , which differs from our measurement at the level of three standard deviations. A better agreement is obtained if we compare with the calculations from Ref. [17] which expects a ratio of 0.6.

As to the possible interpretation of the $D_{s J}(3040)^{+}$ state, we note that Ref. [18] predicts two $J^{P}=1^{+}$radial excitations at 3082 and $3094 \mathrm{MeV} / c^{2}$.

## IX. CONCLUSIONS

In summary, in $470 \mathrm{fb}^{-1}$ of data collected by the $B A B A R$ experiment, we observe the decays of the $D_{s 1}^{*}(2710)^{+}$and

TABLE IV: Information related to the evaluation of the ratio of branching fractions for the $D_{s J}^{*}$ resonances.

| Decay | N | $\epsilon_{r}$ | $D^{*}$ B.F.(\%) | $r_{i}$ |
| :--- | :---: | :---: | :---: | :---: |
| $D_{s 1}^{*}(2710)^{+} \rightarrow D^{0} K^{+}$ | $6469 \pm 425$ |  |  |  |
| $D_{s 1}^{*}(2710)^{+} \rightarrow D^{* 0} K^{+}$ | $1247 \pm 173$ | $0.353 \pm 0.005$ | $61.9 \pm 2.9$ | $0.88 \pm 0.14$ |
| $D_{s J}^{*}(2860)^{+} \rightarrow D^{0} K^{+}$ | $1826 \pm 158$ |  |  |  |
| $D_{s J}^{*}(2860)^{+} \rightarrow D^{* 0} K^{+}$ | $415 \pm 55$ |  |  |  |
| $D_{s 1}^{*}(2710)^{+} \rightarrow D^{+} K_{S}^{0}$ | $2442 \pm 179$ |  |  |  |
| $D_{s 1}^{*}(2710)^{+} \rightarrow D^{*+} K_{S}^{0}$ | $258 \pm 75$ | $0.301 \pm 0.009$ | $30.7 \pm 0.5$ | $1.14 \pm 0.39$ |
| $D_{s J}^{*}(2860)^{+} \rightarrow D^{+} K_{S}^{0}$ | $781 \pm 83$ |  |  |  |
| $D_{s J}^{*}(2860)^{+} \rightarrow D^{*+} K_{S}^{0}$ | $100 \pm 23$ |  | $1.38 \pm 0.35$ |  |

TABLE V: Systematic uncertainties in the evaluation of the ratio of branching fractions.

| Ratio | $D_{s J}$ <br> parameters | MC |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 0.030 | $D^{*}$ | $p^{*}$ | $\cos \theta_{K}$ | $\Delta m$ | Total |  |
| B.F. | cut | cut | cut |  |  |  |  |
| $r_{1}$ | 0.030 | 0.013 | 0.042 | 0.018 | 0.120 | 0.044 | 0.14 |
| $r_{2}$ | 0.050 | 0.015 | 0.050 | 0.066 | 0.175 | 0.004 | 0.20 |
| $r_{3}$ | 0.077 | 0.033 | 0.018 | 0.042 | 0.128 | 0.160 | 0.23 |
| $r_{4}$ | 0.106 | 0.040 | 0.022 | 0.009 | 0.328 | 0.345 | 0.49 |

$D_{s J}^{*}(2860)^{+}$to $D^{*} K$ and measure their branching fractions relative to $D K$. A new, broad $D_{s J}^{+}$state is observed in the $D^{*} K$ mass spectrum at a mass near $3040 \mathrm{GeV} / c^{2}$. Possible spin-parity assignments for these states are discussed.

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