

Enhanced tunable narrow-band THz emission from laser-modulated electron beams

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Abstract

We propose and analyze a scheme to generate enhanced narrow-band terahertz (THz) radiation through down-conversion of the frequency of optical lasers using laser-modulated electron beams. In the scheme the electron beam is first energy modulated by two lasers with wave numbers k_1 and k_2 , respectively. After passing through a dispersion section, the energy modulation is converted to density modulation. Due to the nonlinear conversion process, the beam will have density modulation at wave number $k = nk_1 + mk_2$, where n and m are positive or negative integers. By properly choosing the parameters for the lasers and dispersion section, one can generate density modulation at THz frequency in the beam using optical lasers. This density-modulated beam can be used to generate powerful narrow-band THz radiation. Since the THz radiation is in tight synchronization with the lasers, it should provide a high temporal resolution for the optical-pump THz-probe experiments. The central frequency of the THz radiation can be easily tuned by varying the wavelength of the two lasers and the energy chirp of the electron beam. The proposed scheme is in principle able to generate intense narrow-band THz radiation covering the whole THz range and offers a promising way towards the tunable intense narrow-band THz sources.

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I. INTRODUCTION

There is growing interest in generating powerful Terahertz (THz) radiation to fill the frequency gap ranging from 0.1 THz to 30 THz which has wide applications in nondestructive imaging and spectroscopic studies of materials and molecules (for a recent review, see Refs. [1-3]). Considerable efforts have been made in both the laser community [4,5] and the accelerator community [6-10] to fill the gap. Using laser technologies to generate THz radiation has the advantage of being compact, but typically with a limited peak power. The accelerator-based THz sources are capable of providing intense THz radiation with MW peak power and are particularly suited for nonlinear optical phenomena studies and nonlinear spectroscopy measurements [7].

Accelerator-based THz sources typically fall into two categories. The first category uses ultrashort electron beam to generate intense broad-band THz radiation which is very suitable for single-cycle nonlinear optical phenomena studies [7]. One simple method to generate broad-band THz radiation is to compress the beam to picosecond (ps) or sub-ps level and the THz radiation may be generated from transition radiation, diffraction radiation, synchrotron radiation, undulator radiation, etc. However, it appears difficult to extend the radiation to > 5 THz which would require compressing the beam to sub-100 fs level. For the moderately relativistic beam (~ 50 MeV), the shortest bunch length is typically limited by the second order effects in the bunch compression and the space charge effects. Also a large compression ratio typically involves a serious degradation of the beam quality. There also exists many applications (e.g. THz imaging) that require (or could benefit from) a powerful narrow-band THz radiation. The second category typically aims to provide such kinds of narrow-band THz radiation using bunched electron beam with a density modulation repeated at THz frequency [8,9]. One method is to use a train of laser pulses to illuminate the photocathode to generate a train of electron beams repeated at THz frequency and the bunch trains can be used to generate narrow-band THz radiation when they are accelerated to relativistic energy [9]. However, the space charge force tends to wash out the longitudinal structure during the acceleration process and may limit the application to a relatively low current beam.

To mitigate the space charge effect, it is desirable to generate density modulation in electron beams when they are at relativistic energy. In Ref. [8] a laser is first shaped to have

a quasi-sinusoidal envelope at THz frequency and then used to generate energy modulation in the relativistic electron beam. After passing through a dispersion section the energy modulation is converted to density modulation. This method has been demonstrated to be very effective in generating tunable narrow-band THz radiation.

In this paper, we propose and analyze a scheme to generate intense tunable narrow-band THz radiation via laser-electron interactions. The proposed scheme is similar to that used in the echo-enabled harmonic generation free electron laser [11,12] except that here we only have one dispersion section and the aim is to down-convert the frequency of the lasers to generate THz modulation in the relativistic beam. The scheme is also analogous to the difference-frequency generation (DFG) of two lasers [5], with the relativistic electron beam being the nonlinear medium.

In the scheme the electron beam is first energy modulated by two lasers with wave number k_1 and k_2 , respectively. After passing through a dispersion section, the energy modulation is converted to density modulation. Due to the nonlinear conversion process, the beam will have density modulation at wave number $k = nk_1 + mk_2$, where n and m are positive or negative integers. By properly choosing the parameters for the lasers and dispersion section, one may generate density modulation at THz frequency in the beam using optical lasers. This density-modulated beam can be used to generate powerful narrow-band THz radiation. The central frequency of the THz radiation can be easily tuned by varying the wavelengths of the lasers and the energy chirp of the electron beam. The proposed scheme is in principle able to generate THz radiation covering the whole THz range. In addition to generation of THz radiation, the density modulated beam can also be used to enhance the performances of infrared free electron lasers [13] and plasma wake field accelerators [14,15].

II. GENERATION OF DENSITY MODULATION IN ELECTRON BEAM: THEORY

The scheme for generating density modulation in the electron beam is shown in Fig. 1. It consists of two modulators and one dispersion section. Two lasers with different wavelengths are used to modulate the beam energy in the undulators (modulator 1 and modulator 2). It is worth pointing out that when the wavelengths of the two lasers are close and the number of undulator periods N_p is small, i.e. $2|k_1 - k_2|/(k_1 + k_2) \ll 1/N_p$, one can eliminate the

second modulator and modulate the beam energy with both frequencies by sending the two laser beams simultaneously with the electron beam into the first undulator. In what follows, however, we will assume the more general setup shown in Fig. 1 which, in principle, allows to have arbitrary values k_1 and k_2 .

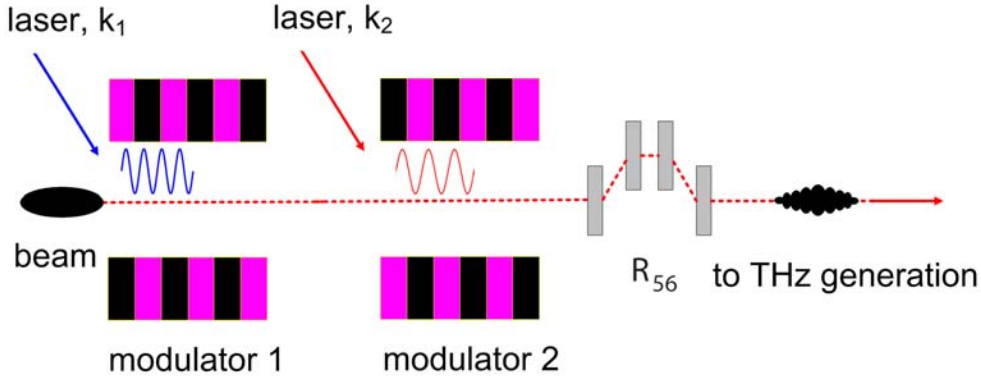


FIG. 1: Scheme for generation of density modulation in electron beam.

We assume an initial Gaussian beam energy distribution with an average energy E_0 and the rms energy spread σ_E , and use the variable $p = (E - E_0)/\sigma_E$ for the dimensionless energy deviation of a particle. Since the bunch length is typically much larger than the wavelength of the modulation, we neglect the variation of the beam current within the bunch and assume a longitudinally uniform beam. The initial longitudinal phase space distribution can then be written as $f_0(p) = N_0(2\pi)^{-1/2}e^{-p^2/2}$, where N_0 is the number of electrons per unit length of the beam. After passage through the two undulators, the beam energy is modulated with the amplitude ΔE_1 and ΔE_2 , so that the final dimensionless energy deviation p' is related to the initial one p by the equation $p' = p + A_1 \sin(k_1 z) + A_2 \sin(k_2 z + \phi)$, where $A_1 = \Delta E_1/\sigma_E$, $A_2 = \Delta E_2/\sigma_E$, k_1 and k_2 are the wave numbers of the laser in the first and second modulator respectively, z is the longitudinal coordinate in the beam, and ϕ is the phase difference of the second laser. The distribution function after the interaction with the laser becomes

$$f_1(z, p) = \frac{N_0}{\sqrt{2\pi}} \exp \left[-\frac{1}{2} (p - A_1 \sin k_1 z - A_2 \sin(k_2 z + \phi))^2 \right]. \quad (1)$$

Sending then the beam through the dispersion section with the dispersive strength R_{56} , converts the longitudinal coordinate z into z' , $z' = z + R_{56}p\sigma_E/E_0$ (where p now refers to the value at the entrance to the first dispersion section), and makes the distribution function

$$f_f(z, p) = \frac{N_0}{\sqrt{2\pi}} \exp \left[-\frac{1}{2} (p - A_1 \sin(k_1 z - Bp) - A_2 \sin(k_2 z - KBp + \phi))^2 \right], \quad (2)$$

where $B = R_{56}k_1\sigma_E/E_0$ and $K = k_2/k_1$.

After passing through the dispersion section, the beam will have density modulation at various frequencies. Integration of (2) over p gives the beam density $N(z)$ (and the associated with it the beam current) which contains various Fourier wave numbers $k_{n,m} = (n + mK)k_1$ in it (see [11,12]). The bunching factors $b_{n,m}$ for each harmonic is defined as $\langle (N(z)/N_0)e^{-ik_{n,m}z} \rangle$ where the brackets denote averaging over the longitudinal coordinate z . After some mathematical manipulations the bunching factor is found to be independent of the laser phase difference and can be written as [11,12]

$$b_{n,m} = \left| J_n((n + Km)A_1B) J_m((n + Km)A_2B) e^{-\frac{1}{2}((n+Km)B)^2} \right|. \quad (3)$$

For the case where only one modulator is present, Eq. (3) reduces to the well-known formulae for the bunching factor in a high-gain harmonic generation FEL [16].

For given values of the amplitudes of the modulation A_1 and A_2 and the value $n + Km$, Eq. (3) can be maximized over the variable B (the strength of the chicane). The result of such optimization for $n = 1$ and $m = -1$ is shown in Fig. 2. One can see from that figure

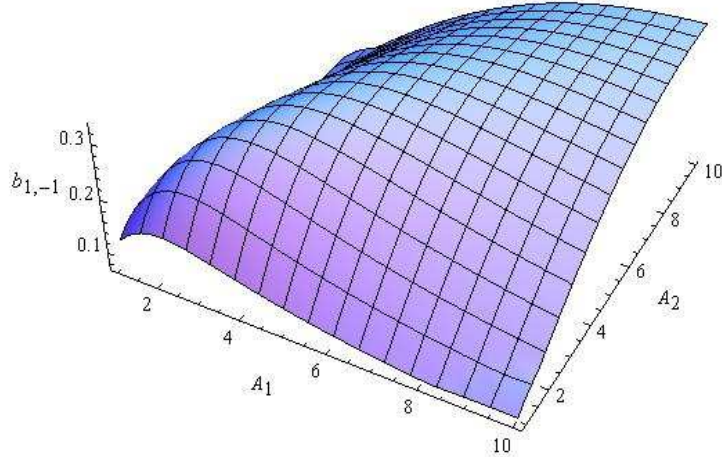


FIG. 2: The maximized bunching factor $b_{1,-1}$ as a function of the modulation amplitudes A_1 and A_2 .

that a value of the bunching factor can be close to 0.3 when A_1 and A_2 are larger (and approximately equal) than 3.

In another optimization procedure, we maximized the bunching factor (3) over the variables A_2 and B (that is over the second amplitude of the modulation and the chicane

strength) for a given value of A_1 . The result of such optimization is shown in Fig. 3. From this Figure one can see that it is most effective to use two lasers with close wave-

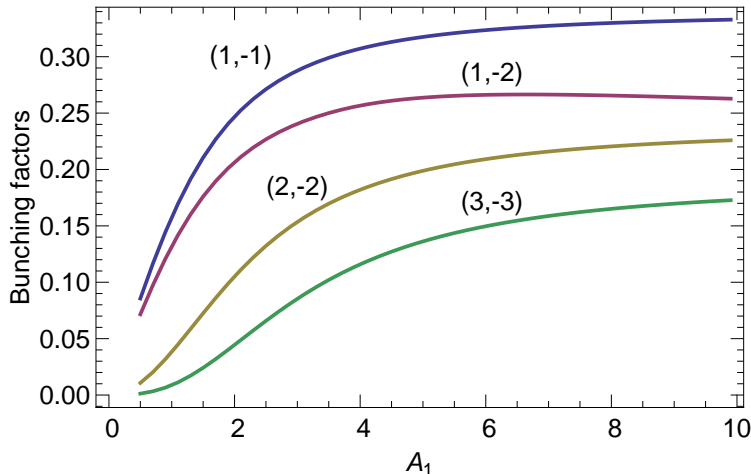


FIG. 3: The maximized bunching factors $b_{1,-1}$, $b_{1,-2}$, $b_{2,-2}$ and $b_{3,-3}$ as functions of the modulation amplitudes A_1 . The pairs (n, m) for each curve are shown in the picture.

length to modulate the beam and generate THz frequency modulation at the difference frequency ($n = 1, m = -1$), similar to the case in DFG of two lasers. For the case when $|n| + |m| > 2$, generation of THz radiation from DFG becomes ineffective, because it involves the $(|n| + |m|)$ th order polarization of the nonlinear medium. However, for our scheme the bunching factor for $|n| + |m| > 2$ is still on the same order as that for $n = 1$ and $m = -1$, so THz radiation with considerable intensity can still be generated.

To illustrate the dynamics occurring in the phase space of the beam, we show in Fig. 4 the phase space evolution of the beam for the optimized case with $K = 1.1$, $A_1 = 3$, $A_2 = 3.46$ and $B = 5.32$. The parameters are optimized for the $n = 1, m = -1$ harmonic with the wave number $k = 0.1k_1$. From Fig. 4b we see after modulator 2, the beam has an energy modulation envelope with the wave number $k = 0.1k_1$. The phase space is periodic with the period $10\lambda_1$. After passing through the dispersion section, the complicated structure generated in the phase space produces beam modulation with the wavelength $\lambda = 10\lambda_1$. The density modulation is clearly seen in Fig. 4d and the corresponding bunching factor is $b_{1,-1} = 0.29$.

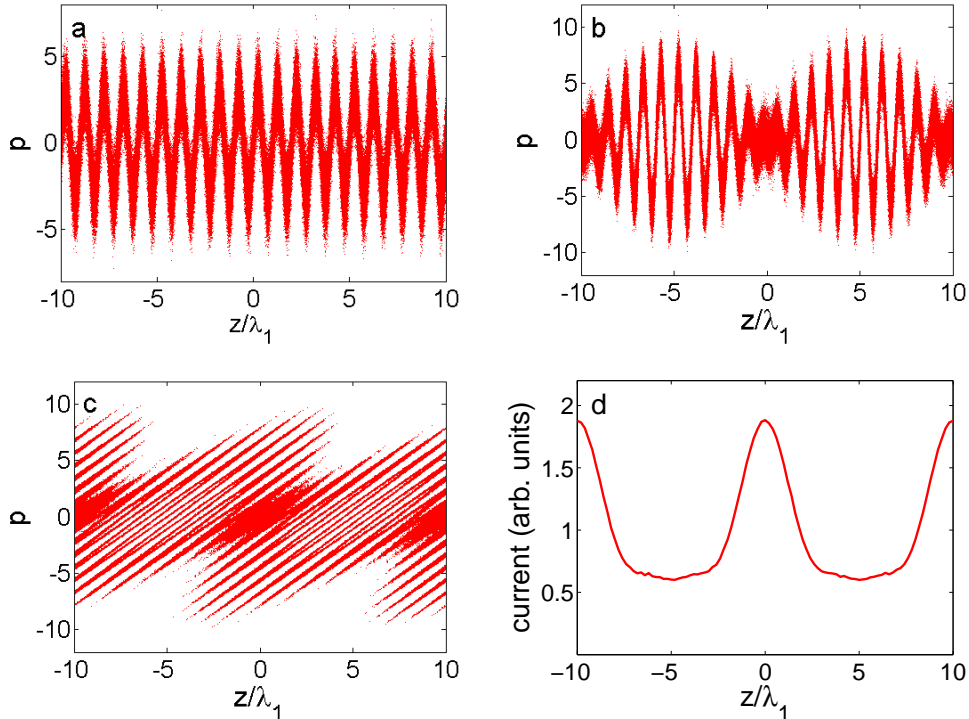


FIG. 4: The phase space of the beam optimized for the beam modulation with the wavelength equal to 10 laser wavelengths λ_1 . (a): phase space at the exit of modulator 1; (b): phase space at the exit of modulator 2; (c): phase space at the exit of the dispersion section; (d): current distribution at the exit of the dispersion section.

III. GENERATION OF DENSITY MODULATION IN ELECTRON BEAM: SIMULATION

Let's first consider an example where the wavelengths of the two lasers are close and their frequency difference lies in the THz region. We consider a Ti:Sapphire laser which has a relatively broad bandwidth. The wavelength of the lasers are assumed to be $\lambda_1 = 770$ nm and $\lambda_2 = 780$ nm, respectively. We assume a moderately relativistic electron beam with energy of 60 MeV. The beam has a Gaussian distribution with rms bunch length of 0.5 ps, peak current of 200 A, and slice energy spread of 10 keV. Taking $n = 1$, $m = -1$ and $A_1 = 5.00$, we found that the parameters that maximize the bunching factor for the difference-frequency radiation were $A_2 = 5.28$ and $B = 27.20$ (corresponding to $R_{56} = 20.00$ mm). The beam current and corresponding bunching factors for the case before and after laser modulation are shown in Fig. 5.

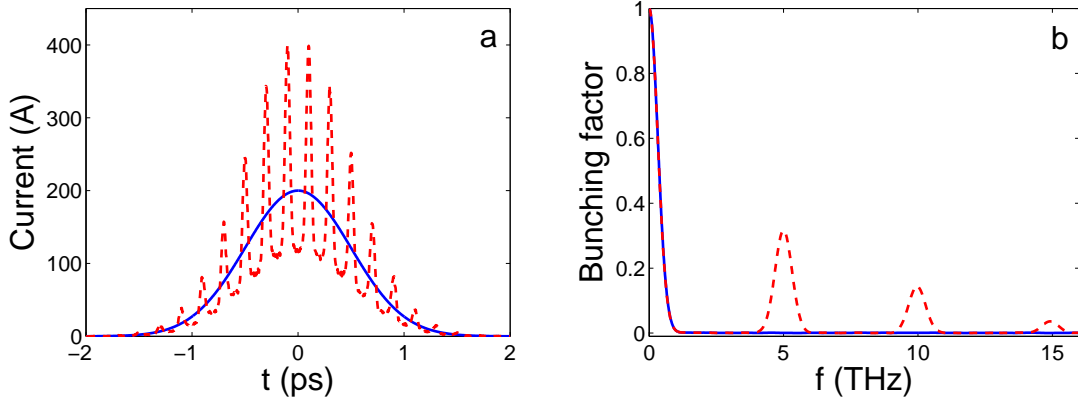


FIG. 5: (a) Initial current distribution (solid blue line) and that after the dispersion section (dashed red line); (b) Corresponding bunching factor for the initial current distribution (solid blue line) and that after the dispersion section (dashed red line).

From Fig. 5 we can see that the frequency component of the unmodulated beam only extends to about 1 THz while that for the laser-modulated beam has a strong spike at 5 THz which equals to the frequency difference of the two lasers. As can be seen in Fig. 3, the laser-modulated beam also contains considerable component at 10 THz and 15 THz which corresponds to $n = 2$, $m = -2$ and $n = 3$, $m = -3$, respectively. As discussed in last section, the bunching factors for these high harmonics decrease as $|n|$ and $|m|$ increases.

A more interesting case is to use one laser with fixed wavelength and a second laser with tunable wavelength to generate THz radiation covering a wide frequency range. The second laser can be generated from optical parametric amplifiers (OPA). For example, the OPA pumped by Ti:Sapphire laser at ~ 800 nm can easily provide tunable signal beam from $1.1 \mu\text{m}$ to $1.6 \mu\text{m}$ [17]. Assuming the wavelength of the laser in the first modulator is 800 nm and that in the second modulator is 1560 nm, taking $n = 1$ and $m = -2$, the generated radiation has a frequency of 10 THz. With the same beam parameters as in Fig. 3 and assuming $A_1 = 3$, we found that the parameters that maximize the bunching factor were $A_2 = 5.74$ and $B = 19.95$ (corresponding to $R_{56} = 14.67$ mm). The beam current distribution and bunching factor for the laser-modulated beam are shown in Fig. 6. As can be seen in Fig. 6, the laser-modulated beam was able to extend the THz radiation to 10 THz. Also there are considerable components at 20 THz and 30 THz (not shown in Fig. 6).

It is worth pointing out that one can also generate THz this way with DFG (wave number

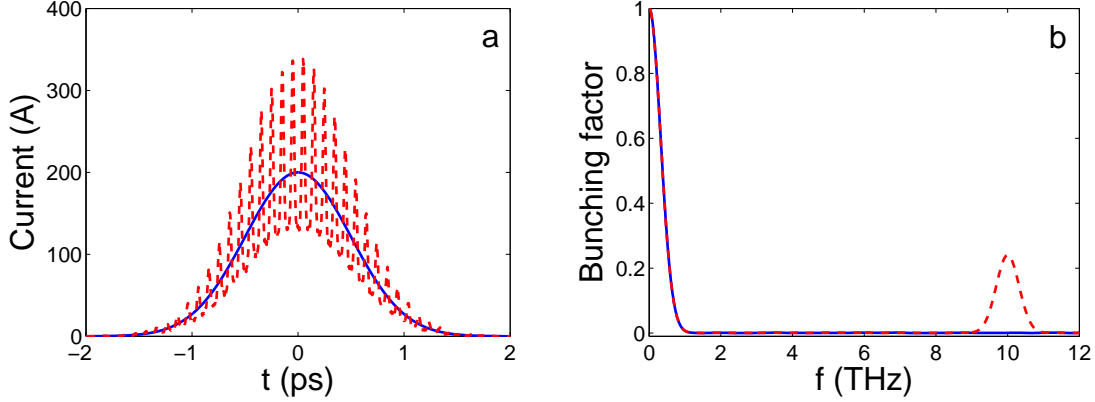


FIG. 6: (a) Initial current distribution (solid blue line) and that after the dispersion section (dashed red line); (b) Corresponding bunching factor for the initial current distribution (solid blue line) and that after the dispersion section (dashed red line).

of $2k_2 - k_1$), but it involves the third-order polarization [18] and the third-order nonlinear optical susceptibility is generally very small which limits the intensity of the generated THz radiation.

IV. GENERATION OF INTENSE NARROW-BAND THZ RADIATION

There are many methods to generate THz radiation using relativistic electron beams, e.g. transition radiation (TR), diffraction radiation, synchrotron radiation, undulator radiation, etc. To illustrate a possible application of the proposed scheme in generating powerful narrow-band THz, we consider TR which is typically generated when electron beam passes through a metallic foil. Assuming a round TR target with radius r , the TR spectral angular distribution for a single electron can be calculated as [19]

$$\frac{d^2U}{d\Omega d\omega} = \frac{e^2}{4\pi^3\epsilon_0 c} \frac{\beta^2 \sin^2 \theta}{(1 - \beta^2 \cos^2 \theta)^2} (1 - \Upsilon(\varsigma))^2, \quad (4)$$

where

$$\Upsilon(\varsigma) = \frac{\varsigma}{\beta\gamma \sin \theta} [J_1(\gamma \sin \theta \varsigma) K_2(\varsigma) - \gamma \theta J_2(\gamma \sin \theta \varsigma) K_1(\varsigma)]. \quad (5)$$

where $\varsigma = 2\pi r/\gamma\lambda$, θ is the polar angle, γ is the Lorentz factor.

Consider a relativistic electron beam with energy 60 MeV, rms bunch length of 1 ps and bunch charge of 1 nC. The two laser wavelengths are assumed to be 800 nm and 1560 nm,

respectively. Taking $n = 1$ and $m = -2$, the generated radiation has a central frequency of 10 THz. Assuming a round TR target with radius 5 mm and a collection angle of 0.2 rad, the calculated radiation energy density at various frequency is shown in Fig. 7.

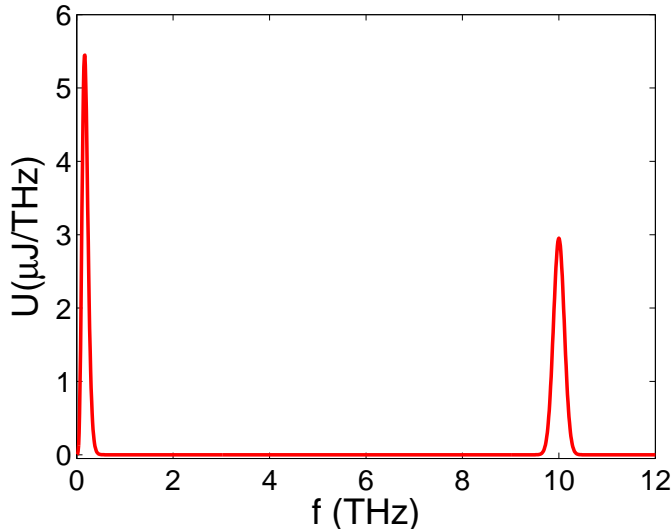


FIG. 7: Radiation energy density for a laser-modulated electron beam

The suppression of low frequency component in Fig. 7 is due to the finite size target effect of TR [19] which occurs when $\gamma\lambda_r > r$, where λ_r is the radiation wavelength. The peak radiation intensity is about $3 \mu\text{J}/\text{THz}$. This powerful narrow-band THz radiation should have wide applications in THz imaging, nonlinear spectroscopy, etc. Since the THz radiation is in tight synchronization with the lasers, it should provide a high temporal resolution for the optical-pump THz-probe experiments. Furthermore, the proposed scheme can be used in energy recovery linac (ERL [6]) to provide high average power ($\sim\text{kW}$) narrow-band THz radiation which may open up a new regime of THz sciences not accessible before.

V. TUNABILITY

Similar to the DFG scheme, the simplest way to tune the frequency of the THz radiation in our proposed scheme is to change the laser wavelength. The combination of a Ti:Sapphire laser with OPA should allow one to generate THz radiation covering a wide frequency range using the laser-modulated electron beams. In principle using a laser with wavelength at 800 nm and the other laser with wavelength from 1480 nm to 1600 nm should allow one to

generate THz radiation covering the whole THz range.

Another method to tune the THz radiation frequency in our scheme is through bunch compression or bunch decompression, depending on the sign of the energy chirp factor $h = dp/d\zeta$. Analysis shows in presence of energy chirp, the wave number shifts to $C(nk_1 + mk_2)$ (see, for example [20,21]), where $C = 1/(1 + hB)$ is the compression factor. And the corresponding optimized bunching factor is found to be

$$b_{n,m} = \left| J_m(C(n + Km)A_2B) J_n(C(n + Km)A_1B) e^{-\frac{1}{2}(C(n+Km)B)^2} \right|. \quad (6)$$

This method allows one to tune the THz frequency even when the laser wavelengths are fixed. Let's still consider the example when the laser wavelengths are 770 nm and 780 nm and $C = 1.5$ which means the beam is compressed by a factor of 1.5 after passing through the dispersion section. A comparison between Eq. (3) and Eq. (6) implies that one can simply keep B the same while decreasing the values of A_1 and A_2 by a factor of 1.5, then the density modulation is optimized at 7.5 THz. In this case, $h \approx 0.0123$ which corresponds to about 0.30 MeV/ps. The beam current distributions and bunching factors for the energy-chirped beam before and after the dispersion section are shown in Fig. 8.

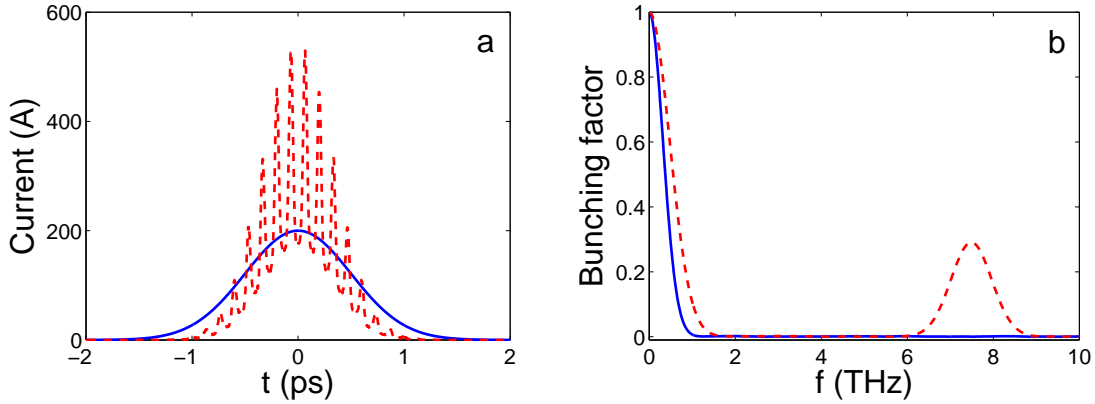


FIG. 8: (a) Initial current distribution (solid blue line) and that after the dispersion section (dashed red line); (b) Corresponding bunching factor for the initial current distribution (solid blue line) and that after the dispersion section (dashed red line).

From Fig. 8 one can see that the macroscopic envelope of the beam is compressed by a factor of 1.5 and the central frequency of the bunching is shifted from 5 THz to 7.5 THz. Using a beam with opposite energy chirp to down-shift the central frequency to lower frequency can be similarly studied.

VI. CONCLUSIONS

We proposed and analyzed a scheme to generate enhanced narrow-band THz radiation through down-conversion of the frequency of optical lasers using laser-modulated electron beams. The scheme can be understood as DFG of two lasers, with the relativistic electron beam being the nonlinear medium. As compared to the schemes of using ultrashort electron beam to generate THz radiation, our scheme has the advantage that the THz radiation is synchronized to the laser and thus allows a higher temporal resolution in optical-pump THz-probe experiments. It can be used in ERL to provide high average power narrow-band THz radiation which may open up a new regime of THz sciences not accessible before. The proposed scheme is in principle able to cover the whole THz range and offers a promising way towards the tunable intense narrow-band THz sources.

VII. ACKNOWLEDGEMENTS

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